



Article

Effect of Minor Ce Substitution for Pr on the Glass Formability and Magnetocaloric Effect of a Fe₈₈Zr₄Pr₄B₄ Metallic Glass

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Abstract: In the present work, $Fe_{88}Zr_4Pr_3B_4Ce_1$ metallic glass (MG) was successfully prepared by minor Ce substitution for Pr, and compared with $Fe_{88}Zr_4Pr_4B_4$ MG in terms of glass forming ability (GFA), magnetic and magnetocaloric properties. The GFA, T_c and the maximum magnetic entropy change ($-\Delta S_m^{peak}$) of the $Fe_{88}Zr_4Pr_3B_4Ce_1$ MG were found to decrease slightly. At the same time, the possible interaction mechanism of minor Ce replacing Pr was also explained. The critical exponents (β , γ and n) obtained by the Kouvel–Fisher method indicate that $Fe_{88}Zr_4Pr_3B_4Ce_1$ MG near T_c exhibits typical magnetocaloric behavior of fully amorphous alloys. The considerable maximum magnetic entropy change ($-\Delta S_m^{peak} = 3.84 \, \text{J/(kg} \times \text{K)}$) under 5 T) near its Curie temperature ($T_c = 314 \, \text{K}$) as well as RCP ($\sim 646.3 \, \text{J/kg}$ under 5 T) make the $Fe_{88}Zr_4Pr_3B_4Ce_1$ MG a better candidate as a component of the amorphous hybrids that exhibit table-shape magnetic entropy change profiles within the operation temperature interval of a magnetic refrigerator.

Keywords: metallic glass; glass forming ability; magnetic entropy change; adiabatic temperature change

1. Introduction

As is known, traditional gas compression-expansion refrigeration technology, dependent on fluorine-containing refrigerants, has many disadvantages such as greenhouse gas emission, destroying the ozone layer, low refrigeration efficiency, and so on. Therefore, magnetic refrigeration (MR) technology using magnetocaloric refrigerant has received a lot of attention because of its high efficiency, lower energy loss, environmental friendliness and structural compactness [1–6]. Magnetocaloric refrigerants are the magnetic materials that emit/absorb heat adiabatically when a magnetic field is applied/removed, which is called magnetocaloric effect (MCE) [4-6]. The magnetocaloric effect of the magnetic materials is induced by the reduction in magnetic entropy upon magnetization, and, as a consequence, the magnetocaloric properties of a magnet are usually evaluated by the change in magnetic entropy $(-\Delta S_m)$ under a certain magnetic field. As such, early research focused on the MCE of first-order magnetic phase transition (FOMPT) materials that exhibit a sharp $-\Delta S_m$ profile with rather high maximum $-\Delta S_m$ ($-\Delta S_m^{peak}$) [7–9]. However, the narrow working temperature intervals of these FOMPT materials make them difficult to match the requirements of magnetic refrigerants working in an Ericsson cycle; that is, a fattened $-\Delta S_m$ curve over the range of operating temperatures in a magnetic refrigerator [10]. In



Citation: Zhu, L.-Z.; Wang, Q.; Zheng, S.-H.; Wang, P.-J.; Ding, D.; Tang, B.-Z.; Yu, P.; Yao, J.-L.; Xia, L. Effect of Minor Ce Substitution for Pr on the Glass Formability and Magnetocaloric Effect of a Fe₈₈Zr₄Pr₄B₄ Metallic Glass. *Metals* 2023, 13, 1531. https://doi.org/ 10.3390/met13091531

Academic Editor: Sundeep Mukherjee

Received: 25 July 2023 Revised: 24 August 2023 Accepted: 28 August 2023 Published: 29 August 2023



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addition, the FOMPT materials inevitably show some disadvantages such as high magnetic and thermal hysteresis [11]. In contrast, amorphous magnetocaloric alloys that experience a second-order magnetic phase transition (SOMPT) exhibit several characteristics superior to the FOMPT materials, such as low energy loss induced by their negligible coercivity and high electric resistance, broadened $-\Delta S_m$ curve and tunable $-\Delta S_m$ peak temperature that make them easily composed to achieve the fattened $-\Delta S_m$ curve [12–31]. Unfortunately, although rare earth (RE)-based metallic glasses (MGs) exhibit rather high glass formability (GFA), excellent $-\Delta S_m^{peak}$ at low temperature and ultrahigh refrigeration capacity (RC), their formability and $-\Delta S_m^{peak}$ get worse when their Curie temperature (T_c) increases to or above the ambient temperature [12–18]. Thus, RE-based amorphous magnetocaloric alloys are more likely to be applied in low temperature refrigeration instead of room temperature (RT) refrigeration. The Fe-based amorphous magnetocaloric alloys exhibit good glass formability when their T_c is near the ambient temperature, but their $-\Delta S_m^{peak}$ is usually very low [19–23]. For example, Fe-Zr-B MGs with T_c ranging from the cold end (T_{Cold}) to the hot end (T_{Hot}) of domestic cooling equipment can be easily fabricated, but their $-\Delta S_m^{peak}$ under 5 T is less than 3.34 J/(kg \times K) [21–23], which is far from enough for them to be utilized as cooling agents in domestic cooling appliances. More recently, by microalloying the Fe-Zr-B MGs with other transition metals or RE metals, we successfully adjusted the T_c and improved the $-\Delta S_m^{peak}$ of the Fe-Zr-B MGs [24–31]. For instance, the $-\Delta S_m^{peak}$ under 5 T reaches 3.55 J/(kg \times K) at 336 K in the Fe₈₅Co₃Zr₅B₄Nb₃ amorphous ribbon [24] and at 333 K in the $Fe_{85}Zr_8B_4Sm_3$ amorphous ribbon [25]; it reaches 4.0 J/(kg \times K) at 323 K in the $Fe_{88}Zr_4Pr_4B_4$ amorphous ribbon [26] and 4.10 J/(kg \times K) at 335 K in the amorphous $Fe_{88}Zr_4Nd_4B_4$ ribbon [27].

However, preliminary results show that the excellent MCE of the iron-based MGs appear near or above the T_{Hot} of a domestic refrigerator. It is known that the high $-\Delta S_m^{peak}$ at temperatures higher than T_{Cold} but lower than T_{Hot} is also required for the construction of fattened $-\Delta S_m$ curves suitable for the Ericsson refrigeration cycle. Thus, it is necessary to develop a new type of metallic glass with excellent MCE at RT. As such, it is critical to decrease the $-\Delta S_m$ peak temperature of the iron-based MGs without dramatically deteriorating their $-\Delta S_m^{peak}$. In the present work, according to our preliminary results on the effect of Ce substitution on the T_c and $-\Delta S_m^{peak}$ of the Fe-Zr-B amorphous alloys [32], we add minor Ce to replace the Pr element in the Fe₈₈Zr₄Pr₄B₄ amorphous alloy for the purpose of obtaining good magnetocaloric properties at a temperature slightly lower than the T_{Hot} of a domestic refrigerator. The mechanism for the influence of minor Ce substitution on the magnetic as well as magnetocaloric properties of the Fe₈₈Zr₄Pr₄B₄ metallic glass was also investigated. The research results provide a feasible path for the Fe-Zr-B-RE amorphous alloy to reduce T_c and avoid significant deterioration of magnetocaloric properties while reducing costs.

2. Materials and Methods

The Fe₈₈Zr₄Pr₃B₄Ce₁ ingot was manufactured by arc-melting the high purity raw materials more than five times to ensure uniformity of composition [33]. Ribbons were fabricated by spraying the Fe₈₈Zr₄Pr₃B₄Ce₁ melt from a quartz tube to the surface of a copper roller rotating at a linear velocity of 55 m/s. The whole sample preparation process is protected by a high purity Ar atmosphere. The cross-sectional morphology of the Fe₈₈Zr₄Pr₃B₄Ce₁ as-spun ribbon was characterized through a Hitachi tungsten filament scanning electron microscope (SEM, model SU-1500). The ~40- μ m-thickness as-spun ribbons were selected for structural analysis by X-ray diffraction (XRD) using a Cu K_{α} radiation with a scanning speed of 1 °/min on a PANnalytical spectrometer. Under program-controlled temperature conditions, the glass transition behavior, melting and crystallization of Fe₈₈Zr₄Pr₃B₄Ce₁ ribbons were distinguished by measuring the power difference between the sample and the reference material as a function of temperature (i.e., the thermal effect information related to heat absorption and release). Hence, the thermodynamic parameters, including glass transition temperature (T_{α}), initial crystallization temperature (T_{α}) and liquidus tempera-

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ture (T_l) , were derived from the differential scanning calorimetry (DSC) curve measured by a NETZSCH DSC-404 C calorimeter at a heating speed of 20 K/min to evaluate the formability of the MG ribbon. The temperature dependence of the heat capacity $(C_p(T))$ curve of the glassy sample was measured by a Perkin-Elmer DIAMOND calorimeter. The magnetic measurements of the amorphous ribbons, including magnetization vs. temperature (M-T) curve, isothermal magnetization (M-H) curve and hysteresis loop, were performed on the vibrating sample magnetometer (VSM) module of a physical property measurement system (PPMS, model 6000, Quantum Design) after applying an oscillating magnetic field to a fully amorphous ribbon to eliminate residual magnetism. The sample for magnetic measurement was prepared by sticking several ribbons together using non-magnetic cement. To minimize the impact of demagnetization, the magnetic field is applied parallel to the length of the sample.

3. Results and Discussion

The Fe₈₈Zr₄Pr₃B₄Ce₁ as-spun ribbon is amorphous according to its XRD pattern shown in Figure 1. The cross-sectional morphology (the upper left inset of Figure 1a) and the prepared samples (the upper right inset of Figure 1a) of the Fe₈₈Zr₄Pr₃B₄Ce₁ as-spun ribbon, indicate a thickness of ~40 µm and a width of ~2 mm. The glassy characteristic of the Fe₈₈Zr₄Pr₃B₄Ce₁ ribbon is also illustrated by the upward glass transition hump before the downward crystallization peak on its DSC trace, as shown in Figure 1b. The onset of T_g and T_x of the amorphous ribbon determined from its DSC trace is ~795 K and ~856 K, respectively. The T_l of Fe₈₈Zr₄Pr₃B₄Ce₁ alloy obtained from its melting curve, which is illustrated in the inset of Figure 1b, is determined to be ~1545 K. Therefore, we can assess the GFA of the Fe₈₈Zr₄Pr₃B₄Ce₁ amorphous sample by calculating the reduced glass transition temperature ($T_{rg} = T_g/T_l = 0.515$) [34] as well as the parameter γ (= $T_x/(T_g + T_l)$ = 0.366) [35]. The T_{rg} of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG sample is slightly higher than that of the $F_{88}Zr_4Pr_4B_4$ MG [26], while the γ parameter is slightly decreased by the Ce substitution. Therefore, it seems that the Ce addition does not obviously change the glass formability of the Fe₈₈Zr₄Pr₄B₄ metallic glass. On the other hand, although the $Fe_{88}Zr_4Pr_3B_4Ce_1$ as well as $Fe_{88}Zr_4Pr_4B_4$ MGs do not show T_{rg} and γ values comparable to the bulk metallic glasses, their T_{rg} and γ values are still larger than most other Fe-Zr-B MGs [21-23], indicating that the Fe₈₈Zr₄Pr₃B₄Ce₁ and Fe₈₈Zr₄Pr₄B₄ alloys can be easily prepared into MG ribbon.

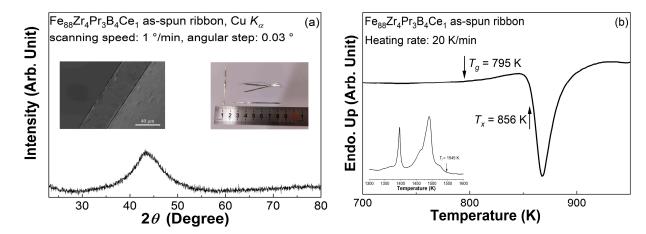


Figure 1. (a) XRD pattern of the $Fe_{88}Zr_4Pr_3B_4Ce_1$ as-spun ribbon measured at the scanning speed of 1 °/min: the upper-left is the cross-section morphology, the upper-right is the prepared sample; (b) The DSC traces and melting behaviors (inset) of the $Fe_{88}Zr_4Pr_3B_4Ce_1$ as-spun ribbon.

The M-T curve under 0.03 T of Fe $_{88}$ Zr $_4$ Pr $_3$ B $_4$ Ce $_1$ sample was measured after a zero-field-cooling process from RT. Figure 2a depicts the M-T curve under 0.03 T of the Fe $_{88}$ Zr $_4$ Pr $_3$ B $_4$ Ce $_1$ glassy sample. The ferromagnetic materials exhibit strong magnetism when magnetized.

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However, as the temperature increases, the intensification of thermal motion will affect the ordered arrangement of magnetic moments of the magnetic domain. When the temperature reaches enough to disrupt the orderly arrangement of magnetic moments of the magnetic domain, the magnetic domain is disrupted, the average magnetic moment becomes zero and the magnetism of ferromagnetic materials disappears and becomes paramagnetic. As seen in the (dM/dT)-T plots of the sample in the inset, T_c of the $Fe_{88}Zr_4Pr_3B_4Ce_1$ MG is thus determined at the minimum value of the dM/dT to be 314 K, which is about 9 K lower than that of the Fe₈₈Zr₄Pr₄B₄ MG [26]. The decreased T_c caused by the replacement of Ce for Pr may be closely related to the antiferromagnetic coupling of the Ce atom with the Fe atom [32]. The hysteresis loops of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG ribbon, as displayed in Figure 2b, suggest that the MG is paramagnetism at 380 K and soft magnetism at 200 K. The Fe₈₈Zr₄Pr₃B₄Ce₁ MG exhibits excellent soft magnetic properties with almost zero hysteresis and high magnetic susceptibility at 200 K, both of which are typical characteristics of fully amorphous alloys and are essential for magnetocaloric materials. The saturation magnetization (M_s) of the Fe₈₈Zr₄Pr₃B₄Ce₁ alloy (~129 Am²/kg at 200 K) is slightly lower than that of the Fe₈₈Zr₄Pr₄B₄ MG (~137 Am²/kg at 200 K [26]), indicating that the magnetocaloric properties of the $Fe_{88}Zr_4Pr_3B_4Ce_1$ MG may be not as high as $Fe_{88}Zr_4Pr_4B_4$ MG because both the M_8 and the $-\Delta S_m$ of the amorphous alloys are primarily determined by the ordering of their magnetic moments.

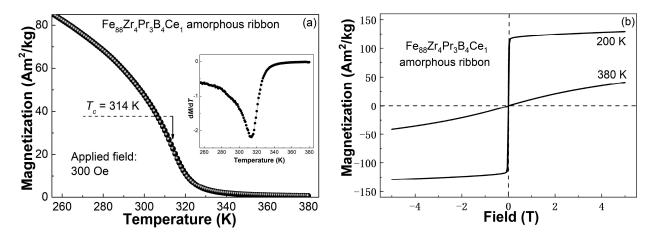


Figure 2. (a) M-T curve of the $Fe_{88}Zr_4Pr_3B_4Ce_1$ amorphous ribbon measured under a field of 0.03 T, the inset is the (dM/dT)-T curve; (b) Hysteresis loops of the $Fe_{88}Zr_4Pr_3B_4Ce_1$ amorphous ribbon measured at 200 K and 380 K under 5 T.

The temperature dependence of $-\Delta S_m$ ($-\Delta S_m$ -T curve) can be derived from the M-H curves measured at various temperatures. Figure 3a displays the M-H curves of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG from 200 K to 380 K under 5 T. On the basis of these M-H curves, the M²-H/M plots, namely the Arrott plots of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG, can be established accordingly, as illustrated in Figure 3b. The Arrott plots (M^2-H/M) at each temperature show a positive slope and are almost parallel to each other from 200 K to 380 K, both of which indicate the typical feature of the materials experiencing a SOMPT according to the Banerjee criterion [36]. The second-order magnetic transition allows the alloy to undergo a continuous phase transition in a broad temperature range and hence leads to a better overall cooling capacity. The $-\Delta S_m$ -T curves under various external magnetic fields of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG obtained from its M-H curves are depicted in Figure 4a. The $-\Delta S_m^{peak}$ of the Fe₈₈Zr₄Pr₃B₄Ce₁ ribbon reaches 1.15 J/(kg × K) under 1 T, $1.57 \text{ J/(kg} \times \text{K)}$ under 1.5 T, $1.94 \text{ J/(kg} \times \text{K)}$ under 2 T, $2.63 \text{ J/(kg} \times \text{K)}$ under 3 T, 3.26 J/(kg × K) under 4 T and 3.84 J/(kg × K) under 5 T at 312.5 K. The $-\Delta S_m^{peak}$ of the Fe₈₈Zr₄Pr₃B₄Ce₁ ribbon is marginally lower than that of the Fe₈₈Zr₄Pr₄B₄ MG [26], probably because of the lower magnetic moment of the Ce atom than the Pr atom due to there being only one up-paired electron in the 4f shell of Ce atom. The minor Ce atom subMetals 2023, 13, 1531 5 of 12

stitution for Pr atom reduces the total magnetic moment of the Fe₈₈Zr₄Pr₄B₄ MG, which is confirmed by the effective magnetic moment (μ_{eff}). As shown in Figure 4b, the temperature dependence of H/M of the Fe₈₈Zr₄Pr₄B₄ and Fe₈₈Zr₄Pr₃B₄Ce₁ ribbons were obtained from their M-T curves. According to the Curie–Weiss law [37], the slopes of the lines above their T_c are correlated to the μ_{eff} , and, thus, the μ_{eff} of the two MGs are calculated to be about 8.89 μ_B for Fe₈₈Zr₄Pr₄B₄ and 7.74 μ_B for Fe₈₈Zr₄Pr₃B₄Ce₁. Apparently, the μ_{eff} of the alloy is reduced with the addition of the Ce atom, resulting in a decrease in $-\Delta S_m^{peak}$.

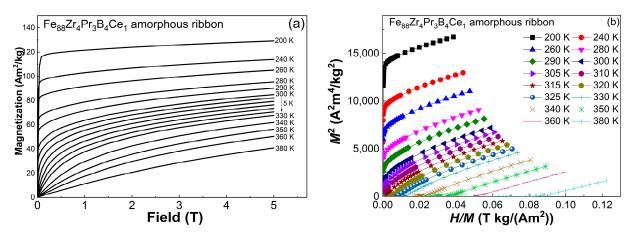


Figure 3. (a) Isothermal M-H curves of the Fe₈₈Zr₄Pr₃B₄Ce₁ amorphous ribbon at various temperatures under 5 T; (b) Arrott plots of Fe₈₈Zr₄Pr₃B₄Ce₁ amorphous ribbon.

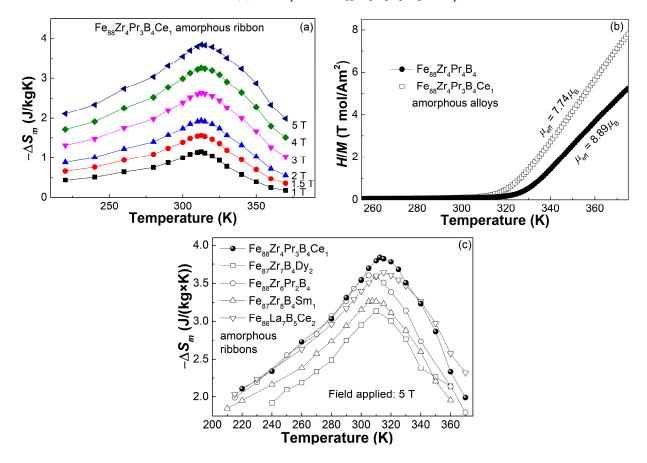
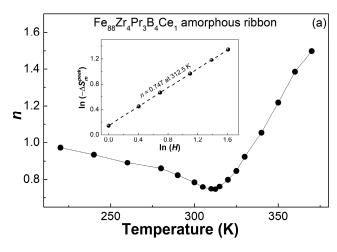


Figure 4. (a) $-\Delta S_m$ -T curves under various magnetic fields of the Fe₈₈Zr₄Pr₃B₄Ce₁ amorphous ribbon; (b) The effective magnetic moment of the Fe₈₈Zr₄Pr₃B₄Ce₁ and Fe₈₈Zr₄Pr₄B₄ amorphous ribbons; (c) $-\Delta S_m$ -T curves under 5 T of several Fe-based amorphous alloys with peak temperature near 310 K.

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Although the $-\Delta S_m^{peak}$ of the Fe₈₈Zr₄Pr₃B₄Ce₁ ribbon is not as high as that of the $Fe_{88}Zr_4Pr_4B_4$ MG, it is still higher than the $-\Delta S_m^{peak}$ near 310 K of other amorphous alloys and even high entropy alloys (HEA) reported in the literature [25,26,38-41]. For example, its $-\Delta S_m^{peak}$ under 5 T is about 234% higher than that of the Al₂₀Mn₂₀Fe₂₀Co_{15.5}Cr_{24.5} HEA (1.15 J/(kg \times K) at 314 K [38]), 193% higher than that of the Mn₂₀Al₂₀Co₁₄Fe₂₃Cr₂₃ HEA (1.31 J/($kg \times K$) at 310 K [39]), 22.3% higher than that of the Fe₈₇Zr₇B₄Dy₂ MG $(3.14 \text{ J/(kg} \times \text{K}) \text{ at } 308 \text{ K } [40])$, 17.4% higher than that of the Fe₈₇Zr₈B₄Sm₁ MG $(3.27 \text{ J/(kg} \times \text{K}) \text{ at } 308 \text{ K} \text{ [25]}), 5.5\% \text{ higher than that of the } \text{Fe}_{86}\text{La}_7\text{B}_5\text{Ce}_2 \text{ MG}$ $(3.64 \text{ J/(kg} \times \text{K}) \text{ at } 313 \text{ K} [41])$ and 6.67% larger than that of the Fe₈₈Zr₆Pr₂B₄ MG (3.6 J/(kg × K) at 306 K [26]). Figure 4c displays the $-\Delta S_m$ -T curves of several ironbased MGs under 5 T. The Fe₈₈Zr₄Pr₃B₄Ce₁ MG ribbon shows a rather high $-\Delta S_m^{peak}$ near 310 K. On the other hand, the relative cooling power ($RCP = -\Delta S_m^{peak} \times \Delta T_{FWHM}$, where ΔT_{FWHM} is the full width at the half of $-\Delta S_m^{peak}$ [42]) of the Fe₈₈Zr₄Pr₄B₃Ce₁ MG, can be calculated as 164.7 J/kg under 1.5 T and 646.3 J/kg under 5 T according to the $-\Delta S_m$ -T curve, both of which are similar to the values of amorphous alloys and much higher than those of the first-order magnetic transition alloys or compounds [26,41,43,44]. Since the Fe₈₈Zr₄Pr₃B₄Ce₁ MG experiences an SOMPT, it exhibits large value of magnetic entropy changes over a wide temperature range, which may be caused by the coupling interaction between RE-RE and RE-TM. Therefore, it can be predicted that Fe₈₈Zr₄Pr₃B₄Ce₁ MG has a good magnetocaloric effect over a large temperature range.

After constructing the $\ln(-\Delta S_m)$ - $\ln(H)$ plots at each temperature, we can achieve their slopes (defined as n) by linearly fitting and thus, observe the magnetocaloric behaviors of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG in more detail. Figure 5a represents the temperature dependence of n (n-T curve) of the Fe₈₈Zr₄Pr₃B₄Ce₁ amorphous ribbon. Similar to other amorphous alloys [21,22,24,26,27,40], the n of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG is close to 1 at temperatures well below its T_c , and smoothly drops to the minimum value near its T_c , then dramatically increases with the increasing temperature and approaches 2 at temperatures much higher than its T_c . The minimum n value of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG ribbon, which appears at 312.5 K and is shown in the inset of Figure 5a, is ~0.747 and is close to the predicted value of amorphous alloys proposed by V. Franco et al. based on the Arrott–Nokes equation [45]. Both the n-T curve and the minimum n value of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG indicate typical magnetocaloric behaviors similar to those of fully MGs.



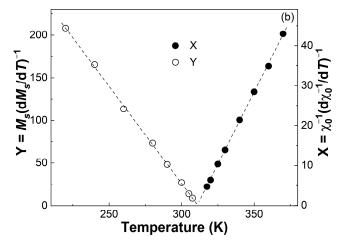


Figure 5. Cont.

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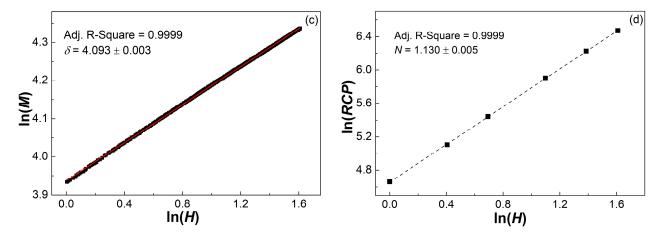


Figure 5. (a) The n-T curve of the Fe₈₈Zr₄Pr₃B₄Ce₁ amorphous ribbon, the inset is the linear fitting of the $\ln(-\Delta S_m^{peak})$ vs. $\ln(H)$ at 312.5 K; (b) Temperature dependence of $M_{st}(T)$ and $\chi_0(T)^{-1}$ of the Fe₈₈Zr₄Pr₃B₄Ce₁ amorphous ribbon; (c) The $\ln(M)$ vs. $\ln(H)$ plot at 315 K of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG; (d) The $\ln(RCP)$ - $\ln(H)$ plot of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG.

On the other hand, the magnetocaloric behavior near its T_c of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG can also be explored by its critical exponents; that is, $n(T_c) = 1 + (\beta - 1)/(\beta + \gamma)$ [45]. Wherein, β and γ are the exponents related to spontaneous magnetization (M_{st}) and initial susceptibility (χ_0), respectively, which can be described as follows [46]:

$$M_{st}(T) = M_0(-\varepsilon)^{\beta}, \, \varepsilon < 0, \, T < T_c \tag{1}$$

$$\chi_0(T)^{-1} = (H_0/M_0)\varepsilon^{\gamma}, \varepsilon > 0, T > T_c$$
 (2)

where M_0 and H_0 are the critical amplitudes, $\varepsilon = (T-T_c)/T_c$ is the reduced temperature. Based on Equations (1) and (2), Kouvel and Fisher proposed a method to determine the critical exponents β and γ with high accuracy, namely the Kouvel–Fisher (KF) method [47]. Equations (1) and (2) can be rewritten as:

$$Y = M_{st}(T) \cdot (dM_{st}(T)/dT)^{-1} = (T - T_c)/\beta$$
(3)

$$X = \chi_0(T)^{-1} \cdot (d\chi_0(T)^{-1}/dT)^{-1} = (T - T_c)/\gamma$$
(4)

As such, we constructed the modified Arrott plots ($M^{2.5}$ -(H/M)^{0.75}) at various temperatures of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG and obtained the temperature dependence of M_{st} and χ_0^{-1} from the intersections of the linear extrapolation of high field regions with $M^{2.5}$ and (H/M)^{0.75} axes, respectively. Figure 5b shows the temperature dependence of $M_{st}(T)\cdot(dM_{st}(T)/dT)^{-1}$ and $\chi_0(T)^{-1}\cdot(d\chi_0(T)^{-1}/dT)^{-1}$ of the ribbon. The critical exponents β and γ can be determined to be 0.438 and 1.384 from the slope of the linear fitting of the two plots. The values of β and γ are close to those of other iron-based MGs [45,48]. Therefore, the n value near T_c based on the KF method is calculated to be 0.692, which is slightly lower than the n value based on the Arrott–Nokes equation, but still higher than the theoretical value of the mean field model [45,49,50]. The reason for this may be related to the unique short-range ordered microstructure of MGs.

Furthermore, the field dependence of the refrigeration capacity is also controlled by the critical exponent, as follows [51]:

$$RC \propto H^N, N = 1 + \frac{1}{\delta}$$
 (5)

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where δ is the critical magnetization isotherm at T_c , that is:

$$M = DH^{\frac{1}{\delta}} \tag{6}$$

D is the critical amplitude. According to the Widom scaling relation ($\delta = 1 + \gamma/\beta$) [52], the exponent δ can be determined to be 4.160. Moreover, the determination of the exponent δ can also be obtained by the modified Equation (6), as follows [46]:

$$ln M = ln D + \frac{1}{\delta} ln H$$
(7)

Taking into account the measurement increments of 5 K in the M-H curves from 300 K to 330 K and the T_c of 314 K for the Fe₈₈Zr₄Pr₃B₄Ce₁ MG, the M-H curve at 315 K was selected to construct the $\ln(M)$ vs. $\ln(H)$ plot, as shown in Figure 5c. The linear fitting is rather accurate, with a regression coefficient (Adj. R-Square) of up to 0.9999. The value of the exponent δ is derived from the slope of the linear fitting to be 4.093 \pm 0.003, which is close to the result based on the Widom scaling relation. Therefore, according to Equation (5), we can obtain that RC is roughly proportional to $H^{1.24}$. The $\ln(RCP)$ - $\ln(H)$ plot of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG constructed from its RCP under different fields is illustrated in Figure 5d. The plot also fits well linearly and the slope is determined to be 1.130 \pm 0.005. Clearly, the N value obtained from the $\ln(RCP)$ - $\ln(H)$ plot is slightly lower than that obtained from the KF method and the modified Equation (6), but these values are around the range of iron-based MGs. The deviation of n and N are supposed to be due to the error in obtaining M_{st} and χ_0^{-1} from the modified Arrott plots.

A phenomenological universal behavior for the $-\Delta S_m$ of the SOMPT materials has been proposed by V. Franco et al. [53]. The $-\Delta S_m$ -T curves under all magnetic fields are normalized with their respective $-\Delta S_m^{peak}$; that is, $\Delta S'(T, H_{max}) = \Delta S_m(T, H_{max})/\Delta S_m^{peak}(T, H_{max})$. The temperature axis is divided into upper and lower parts with T_c as the boundary, and rescaled in different ways, as follows:

$$\theta = \begin{cases} -(T - T_c)/(T_{r1} - T_c), T \le T_c \\ (T - T_c)/(T_{r2} - T_c), T > T_c \end{cases}$$
(8)

where T_{r1} and T_{r2} are the starting and ending temperatures corresponding to ΔT_{FWHM} under different magnetic fields, respectively. Figure 6a shows $\Delta S_m/\Delta S_m^{peak}$ - θ curves under different magnetic fields of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG. We can find that the normalized ΔS_m curves under each magnetic field can collapse onto the same universal curve. This uniformity indicates the typically magnetocaloric behavior of the SOMPT Fe₈₈Zr₄Pr₃B₄Ce₁ MG.

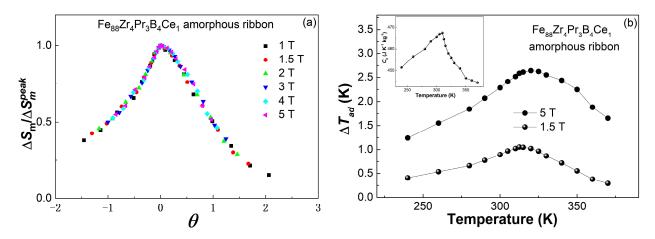


Figure 6. (a) Universal curves for $Fe_{88}Zr_4Pr_3B_4Ce_1$ amorphous ribbon under different magnetic fields; (b) ΔT_{ad} -T curves of the $Fe_{88}Zr_4Pr_3B_4Ce_1$ amorphous ribbon under 1.5 T and 5 T, the inset is its $C_v(T)$ curve.

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To evaluate the magnetocaloric properties of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG in a more direct way, we calculated the adiabatic temperature rise (ΔT_{ad}) of the amorphous ribbon, as follows:

 $\Delta T_{ad}(T, 0 \to H) = -\frac{T}{C_p(T)} \Delta S_m(T, 0 \to H)$ (9)

Figure 6b illustrates the temperature dependence of ΔT_{ad} (ΔT_{ad} -T curve) of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG obtained from its $-\Delta S_m$ -T curves and $C_p(T)$ curve (shown in the inset). The ΔT_{ad} reaches a maximum value of ~1.05 K under 1.5 T and ~2.64 K under 5 T, respectively. These well-known magnetocaloric materials (such as Gd [54], Gd₅(Si₂Ge₂) [7], MnAs [8] and Fe₄₉Rh₅₁ [55]) undergo a first-order magnetic phase transition, exhibiting a giant magnetocaloric effect. Therefore, the magnetic entropy change curve shows extremely high sharp peaks within a narrow temperature range, and the magnetic entropy change peak value is much higher than that of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG with a second-order magnetic phase transition in this study. Therefore, the RCP of Fe₈₈Zr₄Pr₃B₄Ce₁ MG is larger than that of famous magnetocaloric materials, but ΔT_{ad} is smaller than of these materials. Considering its relatively high $-\Delta S_m^{peak}$ at 312.5 K, RCP and ΔT_{ad} , the Fe₈₈Zr₄Pr₃B₄Ce₁ MG is a prospective candidate for an intermediate component of magnetic refrigerants with a table-shape $-\Delta S_m$ curve within the interval between T_{Cold} and T_{Hot} of a domestic refrigerator.

Improving the $-\Delta S_m^{peak}$ near RT as much as possible seems to be an effective way to improve the magnetocaloric properties of Fe-based MGs. In the previous study of Fe-Ce-B ternary MGs [56], Ce was partially replaced by B, and it was found that with the decrease in Ce atoms, the antiferromagnetic coupling between Ce and Fe atoms was weakened, resulting in the enhancement of 3d-3d interaction between Fe atoms and thus T_c increased. In the study of Fe-Zr-B ternary MGs [32], it was found that by replacing Zr with Ce, T_c decreased from 306 K to 283 K. In summary, the composition dependence of the MCE in the Fe-Zr-Pr-B quaternary amorphous alloys system can be explained by the antiferromagnetic coupling between Ce and Fe atoms and the Ce-Pr interaction caused by the introduction of Ce atoms, which may lead to the weakening of the 3d-3d interaction between Fe atoms. Therefore, the substitution of Ce for Pr will reduce the T_c of Fe₈₈Zr₄Pr₄B₄ MG. At the same time, because the magnetic moment of Ce atoms is lower than that of Pr atoms, the total magnetic entropy of the alloy will be reduced by the substitution of Ce for Pr, so the $-\Delta S_m^{peak}$ will be reduced. There are two reasons for choosing minor Ce to replace Pr in this research: firstly, Ce is cheaper than Pr, which can save costs; secondly, Ce and Pr are in adjacent positions in the periodic table of elements and the 4f shell is different from two electrons, which will not produce a large change. Based on the previous research results, it is expected that the total magnetic moment will not decrease too much while the minor Ce replaces Pr in reducing the T_c of Fe₈₈Zr₄Pr₄B₄ MG, so it is more likely to obtain magnetocaloric materials with good magnetocaloric properties near RT.

4. Conclusions

In summary, minor Ce was selected to replace the Pr atom in a $Fe_{88}Zr_4Pr_4B_4$ MG, and the $Fe_{88}Zr_4Pr_3B_4Ce_1$ amorphous ribbon with a thickness of ~40 micrometer was successfully prepared. The influences of the minor Ce substitution for Pr on GFA, magnetic properties and magnetocaloric effect of the $Fe_{88}Zr_4Pr_4B_4$ MG, as well as their mechanisms, were further studied. The main conclusions are detailed below:

- (i) The T_{rg} and γ indicate that the minor Ce substitution for Pr does not obviously change the glass formability of the Fe₈₈Zr₄Pr₄B₄ MG, but the glass formability of both the two ribbons is enough to vitrify them into glassy ribbon.
- (ii) The T_c of the Fe₈₈Zr₄Pr₃B₄Ce₁ ribbon decreases by 9 K compared with the Fe₈₈Zr₄Pr₄B₄ MG, which may be closely related to the antiferromagnetic coupling of the Ce atom with the Fe atom. The Fe₈₈Zr₄Pr₃B₄Ce₁ MG ribbon shows typical soft magnetic characteristics of fully amorphous alloys but slightly lower M_s than that of the Fe₈₈Zr₄Pr₄B₄

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- MG at 200 K. The M^2 -H/M plots at various temperatures indicate the typical SOMPT feature of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG.
- (iii) According to the Maxwell Equation, the $-\Delta S_m^{peak}$ of the Fe₈₈Zr₄Pr₃B₄Ce₁ ribbon reaches 3.84 J/(kg × K) under 5 T at 312.5 K, which is slightly lower than that of the Fe₈₈Zr₄Pr₄B₄ MG but still higher than the $-\Delta S_m^{peak}$ near 310 K of other amorphous alloys and even high entropy alloys reported in literature.
- (iv) The n-T curve, the minimum n value and the normalized universal curve of the Fe₈₈Zr₄Pr₃B₄Ce₁ MG ribbon also indicate the typical magnetocaloric behaviors of fully amorphous alloys. The values of n and N obtained by the KF method deviate slightly from those obtained by the linear fitting of the field dependence of $-\Delta S_m^{peak}$ and RCP, which may be due to the error in multiple derivation of the KF method.

Consequently, considering the relatively high $-\Delta S_m^{peak}$ near 310 K, RCP (~646.3 J/kg under 5 T) and ΔT_{ad} (~2.64 K under 5 T), the Fe₈₈Zr₄Pr₃B₄Ce₁ MG ribbon has great potential for application as an intermediate component of magnetic refrigerants with a flattened $-\Delta S_m$ curve in a domestic refrigerator.

Author Contributions: Conceptualization, L.X., P.Y. and J.-L.Y.; methodology, D.D.; validation, Q.W. and B.-Z.T.; investigation, L.-Z.Z., S.-H.Z. and P.-J.W.; data curation, Q.W., L.-Z.Z. and B.-Z.T.; writing—original draft preparation, L.-Z.Z. and Q.W.; writing—review and editing, D.D. and L.X.; funding acquisition, L.X. and P.Y. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the National Natural Science Foundation of China, grant number 51871139, 52071196 and 52071043.

Data Availability Statement: Data sharing is not applicable.

Acknowledgments: This research was technically supported by the Center for Advanced Microanalysis of Shanghai University.

Conflicts of Interest: The authors declare no conflict of interest.

References

- 1. Gschneidner, K.A., Jr.; Pecharsky, V.K.; Tsokol, A.O. Recent developments in magnetocaloric materials. *Rep. Prog. Phys.* **2005**, 68, 1479. [CrossRef]
- 2. Yu, B.F.; Gao, Q.; Zhang, B.; Meng, X.Z.; Chen, Z. Review on research of room temperature magnetic refrigeration. *Int. J. Refrig.* **2003**, *26*, 622–636. [CrossRef]
- 3. Gschneidner, K.A., Jr.; Pecharsky, V.K. Magnetocaloric Materials. Annu. Rev. Mater. Sci. 2000, 30, 387–429. [CrossRef]
- 4. De Oliveira, N.A.; von Ranke, P.J. Theoretical aspects of the magnetocaloric effect. Phys. Rep. 2010, 489, 89–159. [CrossRef]
- 5. Franco, V.; Blázquez, J.S.; Ipus, J.J.; Law, J.Y.; Moreno-Ramírez, L.M.; Conde, A. Magnetocaloric effect: From materials research to refrigeration devices. *Prog. Mater. Sci.* **2018**, 93, 112–232.
- 6. Pecharsky, V.K.; Gschneidner, K.A., Jr. Magnetocaloric effect and magnetic refrigeration. *J. Magn. Magn. Mater.* **1999**, 200, 44–56. [CrossRef]
- 7. Pecharsky, V.K.; Gschneidner, K.A., Jr. Giant magnetocaloric effect in Gd₅(Si₂Ge₂). Phys. Rev. Lett. 1997, 78, 4494. [CrossRef]
- 8. Wada, H.; Morikawa, T.; Taniguchi, K.; Shibata, T.; Yamada, Y.; Akishige, Y. Giant magnetocaloric effect of MnAs_{1-x}Sb_x in the vicinity of first-order magnetic transition. *Phys. B Condens. Matter* **2003**, *328*, 114–116. [CrossRef]
- 9. Yao, J.; Wang, P.; Mozharivskyj, Y. Tuning Magnetic and Structural Transitions through Valence Electron Concentration in the Giant Magnetocaloric Gd_{5-x}Eu_xGe₄ Phases. *Chem. Mater.* **2012**, 24, 552–556. [CrossRef]
- Hashimoto, T.; Kuzuhara, T.; Sahashi, M.; Inomata, K.; Tomokiyo, A.; Yayama, H. New application of complex magnetic materials to the magnetic refrigerant in an Ericsson magnetic refrigerator. J. Appl. Phys. 1987, 62, 3873–3878. [CrossRef]
- 11. Franco, V.; Blázquez, J.S.; Ingale, B.; Conde, A. The Magnetocaloric Effect and Magnetic Refrigeration Near Room Temperature: Materials and Models. *Annu. Rev. Mater. Res.* **2012**, *42*, 305–342. [CrossRef]
- 12. Luo, Q.; Wang, W.H. Magnetocaloric effect in rare-based bulk metallic glasses. J. Alloys Compd. 2010, 495, 209–216. [CrossRef]
- 13. Ma, L.Y.; Gan, L.H.; Chan, K.C.; Ding, D.; Xia, L. Achieving a table-like magnetic entropy change across the ice point of water with tailorable temperature range in Gd-Co-based amorphous hybrids. *J. Alloys Compd.* **2017**, 723, 197–200. [CrossRef]
- 14. Wu, C.; Ding, D.; Xia, L.; Chan, K.C. Achieving tailorable magneto-caloric effect in the Gd-Co binary amorphous alloys. *AIP Adv.* **2016**, *6*, 035302. [CrossRef]
- 15. Bingham, N.S.; Wang, H.; Qin, F.; Peng, H.X.; Sun, J.F.; Franco, V.; Srikanth, H.; Phan, M.H. Excellent magnetocaloric properties of melt-extracted Gd-based amorphous microwires. *Appl. Phys. Lett.* **2012**, *101*, 102407. [CrossRef]

Metals 2023, 13, 1531 11 of 12

16. Tang, B.Z.; Xie, H.X.; Li, D.M.; Xia, L.; Yu, P. Microstructure and its effect on magnetic and magnetocaloric properties of the Co₅₀Gd_{50-x}Fe_x glassy ribbons. *J. Non-Cryst. Solids* **2020**, *533*, 119935. [CrossRef]

- 17. Wang, X.; Tang, B.Z.; Wang, Q.; Yu, P.; Ding, D.; Xia, L. Co₅₀Gd_{48-x}Fe₂Ni_x amorphous alloys with high adiabatic temperature rise near the hot end of a domestic magnetic refrigerator. *J. Non-Cryst. Solids* **2020**, *544*, 120146. [CrossRef]
- 18. Tang, B.Z.; Liu, X.P.; Li, D.M.; Yu, P.; Xia, L. Effect of Ni substitution on the formability and magnetic properties of Gd₅₀Co₅₀ amorphous alloy. *Chin. Phys. B* **2020**, 29, 056401. [CrossRef]
- 19. Álvarez, P.; Sánchez Llamazares, J.L.; Gorria, P.; Blanco, J.A. Enhanced refrigerant capacity and magnetic entropy flattening using a two-amorphous FeZrB(Cu) composite. *Appl. Phys. Lett.* **2011**, *99*, 232501. [CrossRef]
- 20. Lai, J.W.; Zheng, Z.G.; Zhong, X.C.; Franco, V.; Montemayor, R.; Liu, Z.W.; Zeng, D.C. Table-like magnetocaloric effect of Fe_{88-x}Nd_xCr₈B₄ composite materials. *J. Magn. Mater.* **2015**, *390*, 87–90. [CrossRef]
- 21. Yu, P.; Zhang, J.Z.; Xia, L. Effect of boron on the magneto-caloric effect in $Fe_{91-x}Zr_9B_x$ (x = 3, 4, 5) amorphous alloys. *J. Mater. Sci.* **2017**, 52, 13948–13955. [CrossRef]
- Wang, X.; Wang, Q.; Tang, B.Z.; Ding, D.; Cui, L.; Xia, L. Magnetic and magneto-caloric properties of the amorphous Fe_{92-X}Zr₈B_x ribbons. *Materials* 2020, 13, 5334. [CrossRef]
- 23. Mishra, D.; Gurram, M.; Reddy, A.; Perumal, A.; Saravanan, P.; Srinivasan, A. Enhanced soft magnetic properties and magnetocaloric effect in B substituted amorphous Fe–Zr alloy ribbons. *Mater. Sci. Eng. B* **2010**, 175, 253–260. [CrossRef]
- 24. Wu, Y.B.; Wang, Q.; Tang, B.Z.; Pan, L.L.; Ding, D.; Xia, L. Outstanding glass formability and magneto-caloric effect of a Fe₈₅Co₃Zr₅B₄Nb₃ metallic glass. *J. Non-Cryst. Solids* **2021**, *566*, 120885. [CrossRef]
- 25. Chen, L.S.; Zhang, J.Z.; Wen, L.; Yu, P.; Xia, L. Outstanding magnetocaloric effect of Fe_{88-x}Zr₈B₄Sm_x (x = 0, 1, 2, 3) amorphous alloys. *Sci. China Phys. Mech. Astron.* **2018**, *61*, 056121.
- 26. Wang, Q.; Ding, D.; Tang, B.Z.; Yu, P.; Chan, K.C.; Xia, L. Excellent magnetocaloric performance of a Fe₈₈Zr₄Pr₄B₄ amorphous alloy and its amorphous hybrids. *Intermetallics* **2023**, *161*, 107982. [CrossRef]
- 27. Wang, P.J.; Wang, Q.; Zheng, S.H.; Zhu, L.Z.; Ding, D.; Tang, B.Z.; Yu, P.; Yao, J.L.; Xia, L. Improvement of Curie temperature and magnetic entropy change of a Fe₈₈Zr₈B₄ metallic glass by minor Nd substitution. *J. Non-Cryst. Solids* **2023**, *611*, 122347. [CrossRef]
- 28. Guo, D.Q.; Yuan, Y.D.; Chan, K.C. The effect of different minor additions on the magneto-caloric effect of FeZrB metallic ribbons near room temperature. *J. Magn. Magn. Mater.* **2018**, 446, 12–17. [CrossRef]
- 29. Li, X.; Pan, Y. Magnetocaloric effect in Fe-Zr-B-M (M = Ni, Co, Al, and Ti) amorphous alloys. *J. Appl. Phys.* **2014**, *116*, 093910. [CrossRef]
- 30. Fang, Y.K.; Yeh, C.C.; Hsieh, C.C.; Wang, C.W.; Chang, H.W.; Chang, W.C.; Li, X.M.; Li, W. Magnetocaloric effect in Fe–Zr–B–M (M = Mn, Cr, and Co) amorphous systems. *J. Appl. Phys.* **2009**, *105*, 07A910. [CrossRef]
- 31. Gan, L.H.; Ma, L.Y.; Tang, B.Z.; Ding, D.; Xia, L. Effect of Co substitution on the glass forming ability and magnetocaloric effect of Fe₈₈Zr₈B₄ amorphous alloys. *Sci. China Phys. Mech. Astron.* **2017**, *60*, 076121. [CrossRef]
- 32. Li, A.L.; Wang, Q.; Tang, B.Z.; Yu, P.; Ding, D.; Xia, L. Magnetocaloric effect of the Fe₈₇M₈B₅ (M = Zr, Ce) amorphous alloys. *Mater. Sci. Eng. B* **2022**, *286*, 116033. [CrossRef]
- 33. Mozharivskyj, Y. Preparation of magnetocaloric materials. In *Comprehensive Inorganic Chemistry III*, 3rd ed.; Reedijk, J., Poeppelmeier, K.R., Eds.; Elsevier Ltd.: Amsterdam, The Netherlands, 2023; Volume 5, pp. 178–198.
- 34. Turnbull, D. Under what conditions can a glass be formed? Contemp. Phys. 1969, 10, 473–488. [CrossRef]
- 35. Lu, Z.P.; Liu, C.T. A new glass-forming ability criterion for bulk metallic glasses. Acta Mater. 2002, 50, 3501–3512. [CrossRef]
- 36. Banerjee, B.K. On a generalised approach to first and second order magnetic transitions. Phys. Lett. 1964, 12, 16–17. [CrossRef]
- 37. Arrott, A.S. Generalized Curie-Weiss law. Phys. Rev. B 1985, 31, 2851. [CrossRef]
- 38. Zhang, Y.K.; Zhu, J.; Hao, Z.H.; Hao, W.X.; Mo, Z.J.; Li, L.W. Tunable magnetic phase transition and magnetocaloric effect in the rare-earth-free Al-Mn-Fe-Co-Cr high-entropy alloys. *Mater. Des.* **2023**, 229, 111894. [CrossRef]
- 39. Zhang, Y.K.; Xu, P.; Zhu, J.; Yan, S.M.; Zhang, J.C.; Li, L.W. The emergence of considerable room temperature magnetocaloric performances in the transition metal high-entropy alloys. *Mater. Today Phys.* **2023**, *32*, 101031. [CrossRef]
- 40. Peng, J.X.; Tang, B.Z.; Wang, Q.; Bai, C.; Wu, Y.; Chen, Q.X.; Li, D.M.; Ding, D.; Xia, L.; Guo, X.L.; et al. Effect of heavy rare-earth (Dy, Tb, Gd) addition on the glass-forming ability and magneto-caloric properties of Fe₈₉Zr₇B₄ amorphous alloy. *J. Alloys Compd.* **2022**, 925, 166707. [CrossRef]
- 41. Wang, C.H.; Wang, Q.; Tang, B.Z.; Zhou, X.; Ding, D.; Xia, L. Achieve good magneto-caloric response near the ambient temperature in a Fe₈₆La₇B₅Ce₂ amorphous ribbon. *J. Magn. Magn. Mater.* **2022**, 547, 168954. [CrossRef]
- 42. Wood, M.E.; Potter, W.H. General analysis of magnetic refrigeration and its optimization using a new concept: Maximization of refrigerant capacity. *Cryogenics* **1985**, *25*, *667–683*. [CrossRef]
- 43. Dubenko, I.; Ali, N.; Stadler, S.; Zhukov, A.; Zhukova, V.; Hernando, B.; Prida, V.; Prudnikov, V.; Gan'shina, E.; Granovsky, A. Magnetic, magnetocaloric, magnetotransport, and magneto-optical properties of Ni–Mn–In-Based Heusler alloys: Bulk, ribbons, and microwires. *Nov. Funct. Magn. Mater. Springer Ser. Mater. Sci.* 2016, 231, 41–83.
- 44. Pathak, A.K.; Dubenko, I.; Stadler, S.; Ali, N. Magnetic and magnetocaloric properties of Gd₆X₂Si₃ (X = Ni, Co) and Ln₆Co₂Si₃ (Ln = Pr, La). *J. Appl. Phys.* **2011**, 109, 07A913. [CrossRef]
- 45. Franco, V.; Blázquez, J.S.; Conde, A. Field dependence of the magnetocaloric effect in materials with a second order phase transition: A master curve for the magnetic entropy change. *Appl. Phys. Lett.* **2006**, *89*, 222512. [CrossRef]
- 46. Fisher, M.E. The theory of equilibrium critical phenomena. Rep. Prog. Phys. 1967, 30, 615–730. [CrossRef]

Metals 2023, 13, 1531 12 of 12

- 47. Kouvel, J.S.; Fisher, M.E. Detailed Magnetic Behavior of Nickel Near its Curie Point. Phys. Rev. 1964, 136, A1626. [CrossRef]
- 48. Gebara, P.; Hasiak, M. Investigation of critical behavior in the vicinity of ferromagnetic to paramagnetic phase transition in the Fe₇₅Mo₈Cu₁B₁₆ alloy. *J. Appl. Phys.* **2018**, *124*, 083904. [CrossRef]
- 49. Hiroyoshi, H.; Hoshi, A.; Nakagawa, Y. Arrott-Noakes plots near the Curie temperature of Fe₃Pt: Ordered and disordered alloys in high magnetic fields. *J. Appl. Phys.* **1982**, *53*, 2453–2455. [CrossRef]
- 50. Oesterreicher, H.; Parker, F.T. Magnetic cooling near Curie temperatures above 300 K. J. Appl. Phys. 1984, 55, 4334–4338. [CrossRef]
- 51. Franco, V.; Conde, A. Scaling laws for the magnetocaloric effect in second order phase transitions: From physics to applications for the characterization of materials Lois d'échelle gouvernant l'effet magnétocalorique des transitions de phase de seconde ordre: De la physique aux applications permettant de caractériser les matériaux. *Int. J. Refrig.* **2010**, *33*, 465–473.
- 52. Widom, B. Equation of State in the Neighborhood of the Critical Point. J. Chem. Phys. 1965, 43, 3898–3905. [CrossRef]
- 53. Franco, V.; Blázquez, J.S.; Conde, A. The influence of Co addition on the magnetocaloric effect of Nanoperm-type amorphous alloys. *J. Appl. Phys.* **2006**, *100*, 064307. [CrossRef]
- 54. Dan'kov, S.Y.; Tishin, A.M.; Pecharsky, V.K.; Gschneidner, K.A., Jr. Magnetic phase transitions and the magnetothermal properties of gadolinium. *Phys. Rev. B* **1998**, *57*, 3478–3490. [CrossRef]
- 55. Nikitin, S.A.; Myalikgulyev, G.; Tishin, A.M.; Annaorazov, M.P.; Asatryan, K.A.; Tyurin, A.L. The magnetocaloric effect in Fe₄₉Rh₅₁ compound. *Phys. Lett. A* **1990**, *148*, 363–366. [CrossRef]
- 56. Zheng, S.H.; Wang, Q.; Zhu, L.Z.; Wang, P.J.; Ding, D.; Tang, B.Z.; Yu, P.; Yao, J.L.; Xia, L. Excellent Magnetocaloric Performance of the Fe₈₇Ce₁₃-xBx (x = 5, 6, 7) Metallic Glasses and Their Composite. *Materials* **2023**, *16*, 4393. [CrossRef] [PubMed]

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