

Article

Influence of an Ageing Heat Treatment on the Mechanical Characteristics of Iron-Aluminium Bronzes with β -Transformation Obtained via Centrifugal Casting: Modelling and Optimisation

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Abstract: Aluminium bronzes possess a unique combination of high strength and wear and corrosion resistance in aggressive environments; thus, these alloys find wide application in marine, shipbuilding, aviation, railway, offshore platform applications and other fields. Iron-aluminium bronzes (IABs) are the cheapest and most widely used. When the aluminium content is above 9.4 wt%, IAB is biphasic (i.e., it undergoes β -transformation) and can be subjected to all heat-treatment types, depending on the desired operating behaviour of the bronze component. This article presents correlations (mathematical models) between the primary mechanical characteristics (yield limit, tensile strength, elongation, hardness and impact toughness) and the ageing temperature and time of quench at 920 °C in water of Cu-11Al-6Fe bronze, obtained using the centrifugal casting method. The microstructure evolution was evaluated depending on the ageing temperature and time changes. Overall, the research was conducted in three successive inter-related stages: a one-factor-at-a-time study, planned experiment, and optimisations. Four optimisation tasks, which have the greatest importance for practice, were formulated and solved. The defined multiobjective optimisation tasks were solved by searching for the Pareto-optimal solution approach. The decisions were made through a nondominated sorting genetic algorithm (NSGA-II) using QstatLab. The optimisation results were verified experimentally. Additional samples were made for this purpose, quenched at 920 °C in water and subjected to subsequent ageing with the optimal values of the governing factors (ageing temperature and time) for the corresponding optimisation task. The comparison of the results for the mechanical characteristics with the theoretical optimisation results presents a good agreement.

Keywords: aluminium bronze with β -transformation; Cu-11Al-6Fe bronze; heat treatment; mechanical characteristics; optimisation of heat treatment



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1. Introduction

Aluminium bronzes (Cu-Al-X, X = Fe, Ni, Mn, Be, Co, Si and Sn) possess good strength as well as strong wear and corrosion resistance in aggressive environments [1]. Thus, these alloys find wide application in marine, shipbuilding, aviation, railway, offshore platform applications and other fields. Iron-aluminium bronzes (IABs), introduced to industry as early as 1870 [2], are the cheapest and most widely used [3,4]. The addition of iron facilitates the grain refinement in copper, increasing its strength. Copper forms an α -solid solution with aluminium. According to the Cu-Al-5Fe equilibrium system [1], the strength and hardness of IAB cannot be improved using heat treatment if the alloy contains less than 9.4 wt% aluminium. Such an IAB is single phase (α -phase). When the aluminium content

is above 9.4 wt%, IAB is biphasic (i.e., it undergoes β -transformation and can be subjected to all heat treatment types). The mechanical properties and service behaviour of IAB with β -transformation are a function of the microstructure; thus, its evolution can be controlled through an appropriate heat treatment according to the specific service behaviour and requirements of this bronze.

Many researchers have investigated the correlation between the heat-treatment governing factors and the microstructure evolution and mechanical properties of complex aluminium bronzes with β -transformation. For example, detailed and systematic information is contained in the review paper in [1]. Increasing the hardness of aluminium bronzes via heat treatment is a common subject of research [5–11]. Other mechanical properties, which were improved through heat treatment, are the impact toughness [9] of Cu-Al-Fe-Ni and Cu-Al-Fe-Mn bronzes and the tensile strength and elongation [10] of Cu-Al-Fe-Be and Cu-Al-Fe-Ni bronzes. However, such information is practically absent for IABs.

The effects of various heat treatment types on the mechanical characteristics (including fatigue strength in the air) of Cu-10Al-5Fe IAB, obtained as hot-rolled bars, were studied in our previous study [12]. The types of heat treatment were Type 1, annealing at 720 °C for 3 h, and Type 2, heating at 920 °C for 1 h and rapidly quenching in water at room temperature. Types 3 and 4 are like Type 2 but are followed by tempering at 600 °C and 300 °C, respectively, for 3 h and then air cooling. The third type of heat treatment provides the maximum impact toughness, whereas the fourth type provides the maximum hardness.

However, the relationships between the heat-treatment governing factors and mechanical characteristics of the alloys are typically nonlinear. For instance, Mi et al. [10] demonstrated that the relationships between the ageing temperature (time) and some properties (hardness, extensibility and electrical resistive) of beryllium and nickel aluminium bronze are nonlinear. Therefore, the influence of the ageing temperature and time on the mechanical characteristics of IAB with β -transformation must be investigated for a broader range of variation in both variables, considering their nonlinear effects. Thus, developing mathematical models of the correlations between the ageing temperature (time) and the mechanical characteristics of IAB enables determining the optimal heat-treatment regimes, depending on the specific requirements and operational behaviour of the corresponding bronze components.

In this study, the IAB was obtained using the centrifugal casting method. The centrifugal casting method, intended for axisymmetric parts (pipes, flywheels, cylinder liners, etc.), was invented by Alfred Krupp in 1852 [13]. The method essence consists of the fact that the mould filling and the crystallisation of the casting takes place under the action of centrifugal forces [2,14–18]. Depending on the location in space of the axis of rotation, centrifugal casting is carried out with a horizontal, vertical or inclined axis of rotation [19]. The method can be applied to both metals and non-metals [20]. Metal moulds are most often used in centrifugal casting [21]. The physical–mechanical properties of castings obtained using the centrifugal casting method are higher [22] than those of castings obtained via stationary methods. This is explained by the characteristic features of the process, ensuring always directional crystallisation, under the continuous action of centrifugal forces. The metal gradually crystallises in the direction from the surface to the inside of the castings. Therefore, the volume deficit is compensated by the liquid metal lying in the inner layers. The air circulation is particularly intense in centrifugal casting with a vertical axis of rotation, because the hot air is lighter and quickly leaves the mould. The cooled part of the melt has a higher density and moves to the outer surface of the casting, while the less cooled part has a lower density. As a result, heat flows occur in the melt, circulating in a radial direction. This facilitates directional crystallisation of the castings. The positive effect increases with an increasing mould rotation frequency [21]. In this directional crystallisation, the forming crystals grow from the outer surface of the casting to the inner surface. The inner surface of the casting hardens last and retains its correct geometric shape. Heterogeneous particles (gases, slag, etc.), which have a lower density, float to the inner surface. Therefore, a larger machining allowance should be provided for the inner surface of the casting. The more

significant advantages of the centrifugal casting are the possibility of obtaining castings from alloys having poor casting properties, high mechanical properties of castings, the reduction in machining allowances, the reduced consumption of liquid metal and the high performance. The main disadvantages are the increased tendency to liquation, difficulty in dosing, and the possibility of defects in the form of transverse and longitudinal cracks.

The primary goal of this study is to establish the influence of the ageing temperature and time on the main mechanical characteristics of IABs with β -transformations. These bronzes contain 10–13 wt.% aluminium and 4–6 wt.% iron. The presumption is that the effect of the ageing heat treatment on their mechanical characteristics is qualitatively the same for these bronzes.

Mathematical models of the leading mechanical characteristics of Cu-11Al-6Fe IAB were established depending on the ageing temperature and time. Optimisations were carried out according to the following criteria: (1) maximum plasticity, (2) maximum impact toughness (dynamic strength), (3) simultaneous high hardness and static strength and (4) simultaneous high hardness, static and dynamic strength. The investigation was conducted in 10 steps. Figure 1 presents the study flow chart.

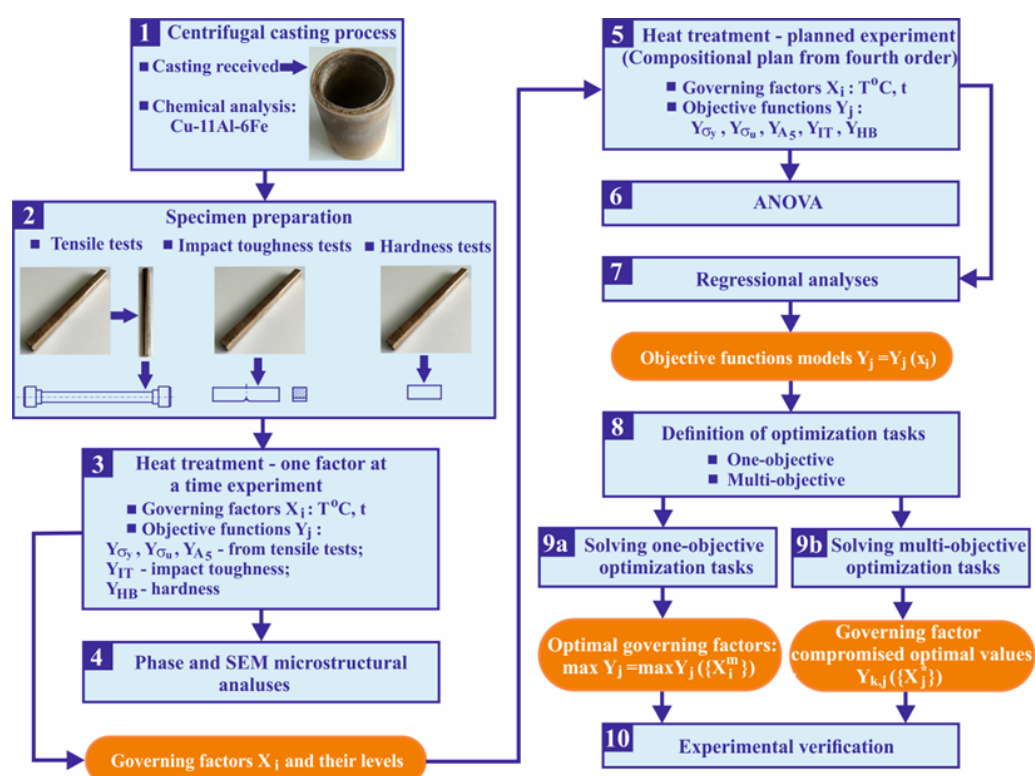


Figure 1. Flow chart of the study.

2. Materials and Methods

A chemical analysis of the IAB was performed using an optical emission spectrometer (Foundry-Master Optimum, Hitachi, Tokyo, Japan). Table 1 lists the composition in weight percentages.

Table 1. Chemical composition in percentages (wt.%) of the used Cu-11Al-6Fe bronze.

Cu	Al	Fe	Mn	Ni	Pb	Zn	Si	Sn	Mg	S	Other
80.95	11.0	6.26	0.905	0.391	0.028	0.280	0.022	0.071	0.005	0.010	Balance

The IAB was obtained using the true centrifugal casting method with a vertical axis in the form of a tube (Figure 2a) to eliminate the effect of hot-mechanical strengthening inherent in the commercial hot-rolled bars and to increase the casting density, with the following nominal sizes: external diameter 116 mm, length 180 mm and wall thickness 13 mm. The tubes were cut via a mechanical hacksaw along their axes into 17 blanks for each tube, with nominal overall dimensions of $180 \times 20 \times 13$ mm (Figure 2b). Part of the blanks intended to produce tensile specimens were subjected to turning to obtain a cylindrical shape with a 12 mm diameter (Figure 2c). All blanks (except three rotary and three prismatic blanks) were heated to 920°C for 1 h and rapidly quenched in water at 20°C . The temperature of 920°C was selected based on the chemical composition of the bronze and the section of the Cu-Al-Fe equilibrium phase diagram, with a 5% Fe plane [1] (Figure 3).

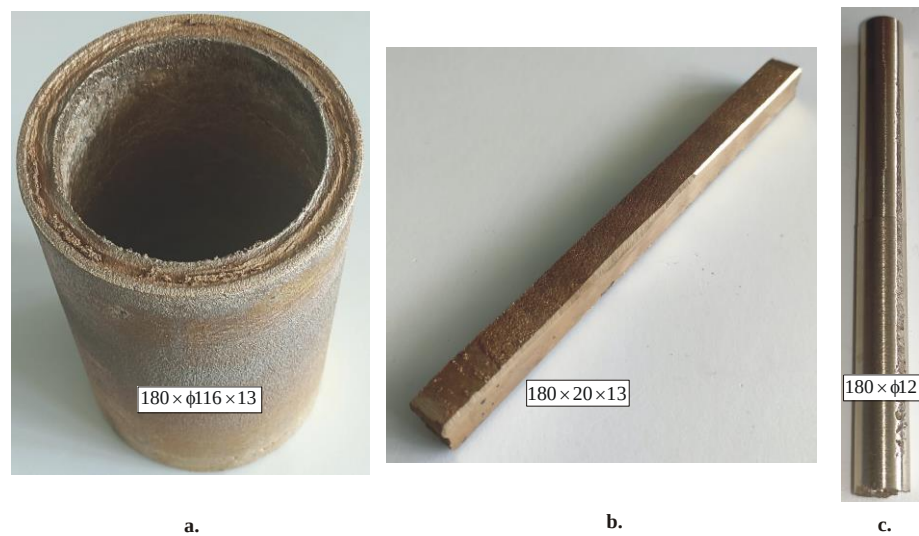


Figure 2. Workpiece evolution for the tensile tests: (a) a tube obtained via centrifugal casting; (b) cutting by erosion; (c) turning to produce a cylindrical shape (the sizes are in mm).

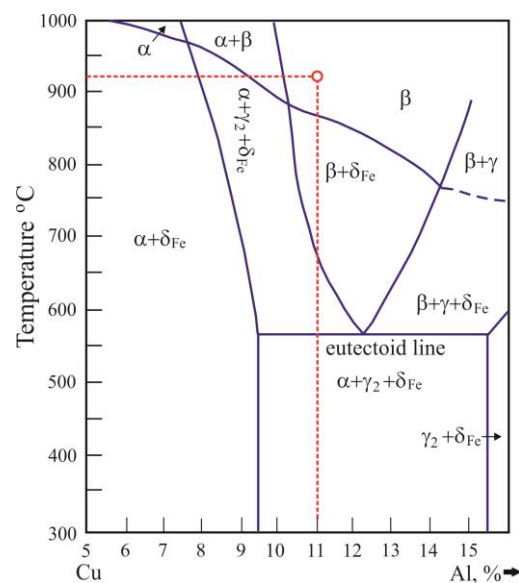


Figure 3. A section of the Cu-Al-5Fe equilibrium phase diagram with a 5% Fe plane [1].

The effects of the temperature and time ageing on the mechanical characteristics of the bronze were investigated in two stages: (1) scanning the factor space (in this case, a plane because there are two governing factors) using the one-factor-at-a-time method and

(2) based on the results of the first stage, conducting a planned experiment, regression analyses and optimisations. Seven ageing temperatures (20 °C, 200 °C, 300 °C, 400 °C, 500 °C, 600 °C and 700 °C) and four ageing times (1, 2, 3 and 4 h) were used in the first stage. Three specimens were used for each experimental point, and the result was obtained as the arithmetic mean of the measurements on the three specimens. The effects of ageing temperature (time) were studied at 3 h ageing time (500 °C ageing temperature). After the respective heat treatments of the cylindrical and prismatic blanks, tensile specimens (Figure 4a) and impact toughness specimens (Figure 4b) were manufactured.

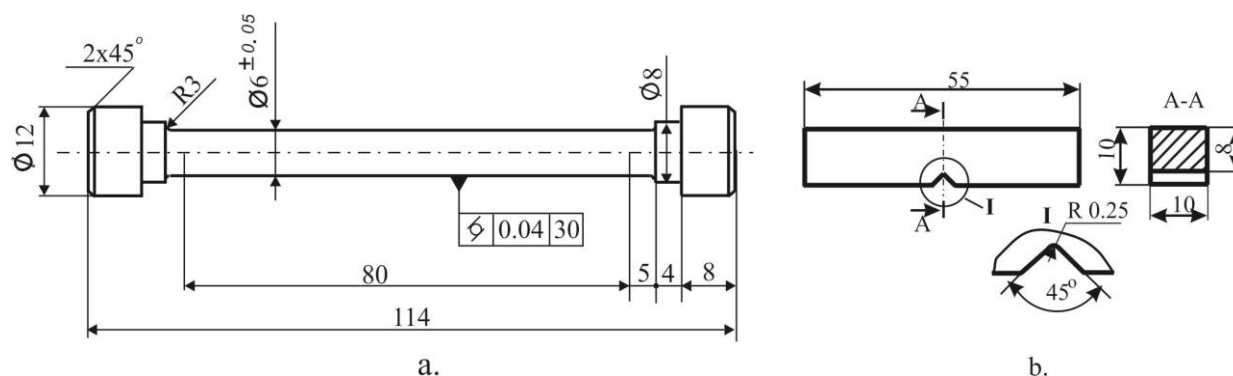


Figure 4. Specimen geometry: (a) tensile test; (b) Charpy impact toughness test.

The tensile tests were conducted at room temperature via a Zwick/Roell Vibrophore 100 testing machine. The impact toughness was explored using a Charpy universal impact tester (maximum impact energy: 300 J). A ZWICK/Indentec- ZHVm-S hardness tester was employed to measure the hardness using a spherical-ended indenter with a diameter of 2.5 mm, loading of 63 kg and holding time of 10 s. The phase analysis was performed with a Bruker D8 Advance X-ray diffractometer. The Crystallography Open Database was employed to determine the peak positions. The microstructure in the specimen cross-section was observed using scanning electron microscopy (LYRA I XMU Tescan) after polishing and etching the specimens using a 20% FeCl₃ solution. In addition, the energy-dispersive X-ray spectroscopy analysis was performed for the local assessment of the chemical composition at a point.

Regression analyses and optimisations were performed using QStabLab software [23]. The optimisations are based on regression models. The regression analysis is a statistical method (an extremely powerful tool for machine learning) to determine the relationship between a dependent variable Y (a characteristic of a technological object) and multiple independent variables x_i , $i = 1, 2, \dots, n$, that, in a statistical sense, influence the values of the target variable Y [24]. The method is based on data from experiments and observations and is often called the “black box” method. The technological object is considered as a “black box” in which one cannot peer and see the mechanism of ongoing processes, but one can only change the factors and track their influence on the dependent variable Y . But it is precisely this impossibility (namely, to use knowledge about the mechanism of processes in the technological object) that makes this method universal, because it does not use such specific information about the particular object. It can be concluded that the regression analysis is the best way to solve regression problems in machine learning using data modelling.

3. Experimental Results and Discussion

3.1. Ageing Temperature and Time Effects on Mechanical Characteristics: One-Factor-at-a-Time Method

3.1.1. Effects of the Ageing Temperature

Figure 5 presents the nominal stress–nominal strain diagrams obtained at various ageing temperatures. The ageing temperature substantially influences the static strength and plasticity of the bronze. Information on the yield limit, tensile strength and elongation depending on the ageing temperature was obtained from these diagrams.

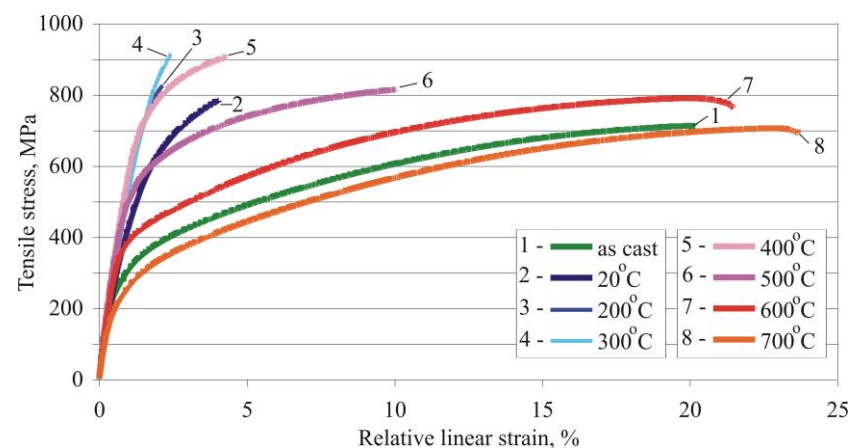


Figure 5. Effect of ageing temperature on the nominal stress—nominal strain diagram of Cu-11Al-6Fe bronze (ageing time 3 h).

Figure 6 illustrates the effects of the ageing temperature on the primary mechanical characteristics. The yield limit and tensile strength (Figure 6a) exhibit a similar trend of change: they increase as the temperature increases to 350–400 °C, after which they decrease. The rates of increase and decrease in the yield limit are greater than those of the tensile strength. The relative elongation characterises the material plasticity and indicates the opposite trend: the plasticity increases with an increase in the ageing temperature (Figure 6b). Figure 6c depicts the change in hardness depending on the ageing temperature. The change tendency of the hardness is analogous to that for the yield limit and tensile strength. Figure 6d presents the impact toughness change, depending on the ageing temperature. As expected, the change trend is analogous to that of the elongation and opposite the strength and hardness change trends. The four trendlines do not change their curvatures in the studied temperature interval.

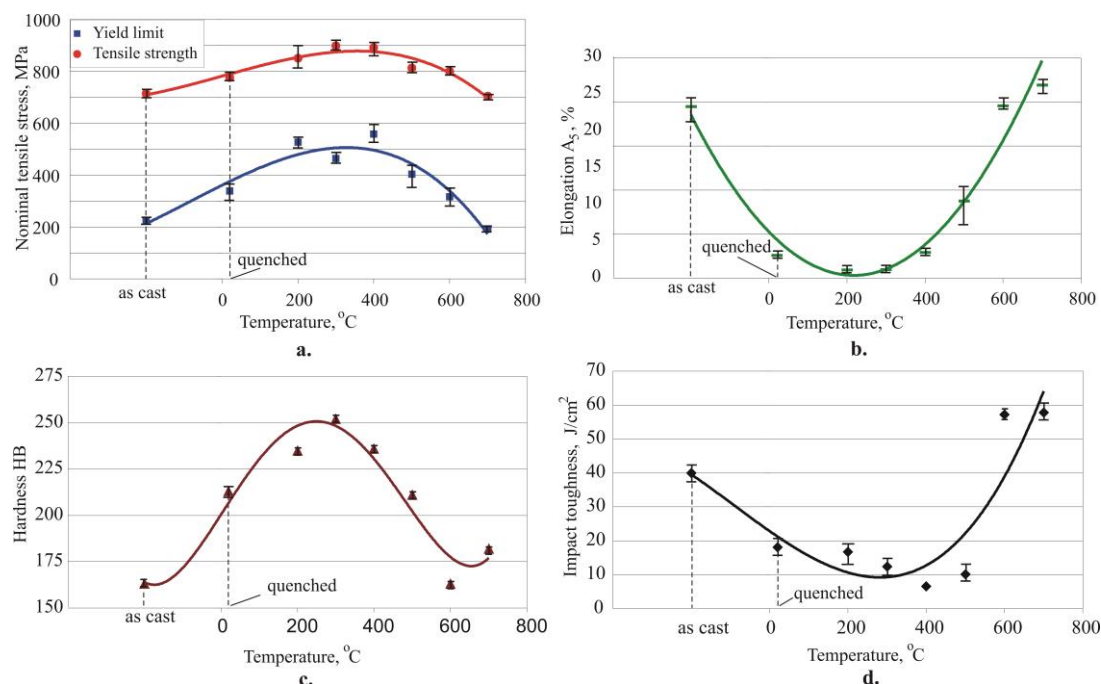


Figure 6. Effect of ageing temperature on the main mechanical characteristics of Cu-11Al-6Fe bronze (ageing time 3 h): (a) yield limit and tensile tests; (b) elongation; (c) hardness; (d) impact toughness.

3.1.2. Effects of the Ageing Time

Figure 7 illustrates the nominal stress–nominal strain diagrams obtained at various ageing times. A comparison with Figure 5 reveals that the influence of the ageing time within the studied time interval is significantly weaker than the effect of the ageing temperature. The influence of time ageing may be more significant for another ageing temperature. Therefore, time ageing cannot be ignored as a governing factor in the planned experiment.

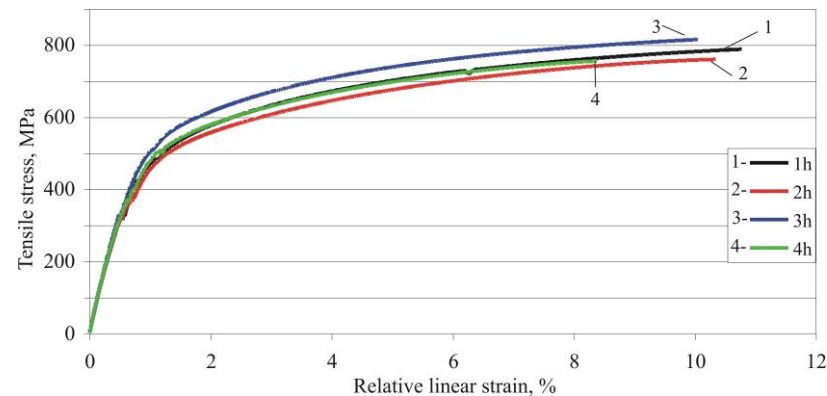


Figure 7. Effect of ageing time on the nominal stress–nominal strain diagram of Cu-11Al-6Fe bronze (ageing temperature 500 °C).

Figure 8 depicts the effects of the ageing time on the primary mechanical characteristics. The yield limit indicates a weak tendency to decrease with increased time, whereas the tensile strength reaches a maximum value at about 3 h of ageing time. The elongation and hardness display an analogous trend (in a narrow variation interval) to that of the tensile strength. In contrast, the impact toughness (analogous to the yield limit) decreases with an increasing ageing time.

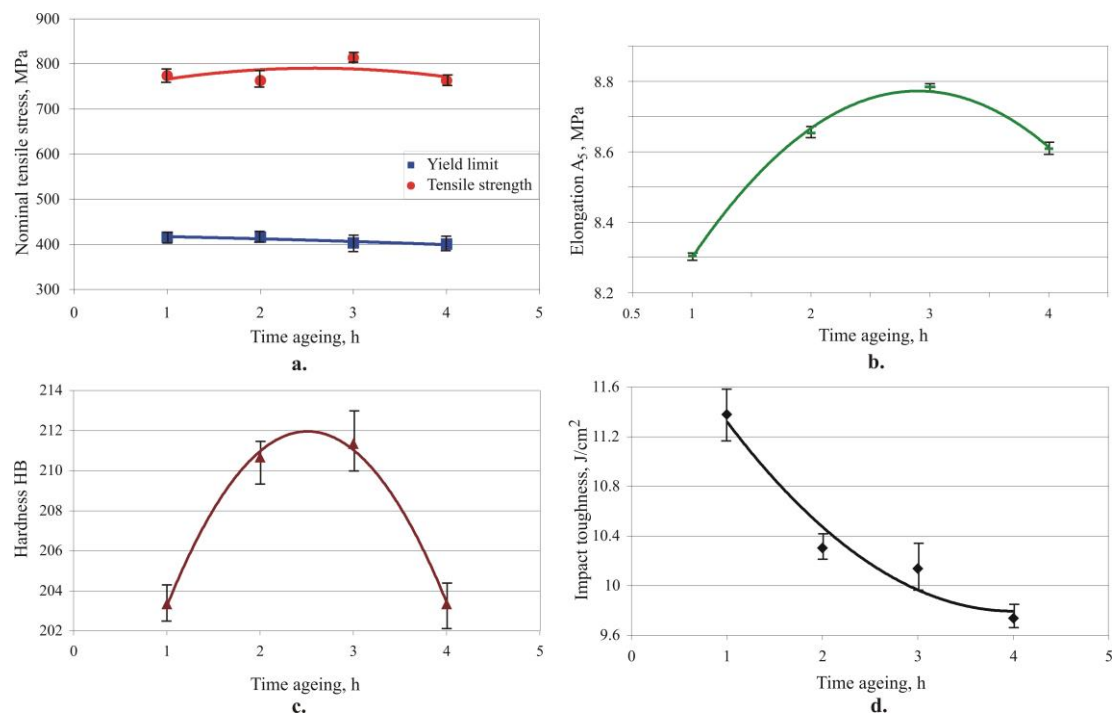


Figure 8. Effect of ageing time on the main mechanical characteristics of Cu-11Al-6Fe bronze (ageing time 3 h): (a) yield limit and tensile tests; (b) elongation; (c) hardness; (d) impact toughness.

3.2. Microstructure Evolution

Figure 9 illustrates the phase analysis outcomes. The structure after centrifugal casting is characterised by good homogeneity (Figure 10). The copper-enriched α -phase grains have an elongated shape (50–60 μm), which is characteristic of dendritic structures obtained by casting. The iron does not dissolve in copper and forms the intermetallic compound Fe_3Al with aluminium (Figure 9). The Fe_3Al is deposited into the copper solid solution in the form of dispersed and larger coagulated precipitates. The γ' - and β -phases are located between the α -phase grains and are observed as eutectoid zones $\text{Eg}(\alpha + \gamma')$ and acicular crystals obtained via a diffusionless (martensite-like) transformation $\beta \rightarrow \beta'$. The martensitic transformation in centrifugal casting is due to the rapid cooling, a characteristic of casting nonferrous alloys into metal moulds. The quantity of β' -phase (Cu_3Al) and γ -phase (Cu_9Al_4) is significantly less than the underlying α -solid solution (Figure 9).

After quenching at 920 $^{\circ}\text{C}$ in water and subsequent ageing at 20 $^{\circ}\text{C}$, a coarse-grained structure is formed (Figure 11). Dispersed martensitic-type needles are observed at the grain boundaries because of the diffusionless transformation $\beta \rightarrow \beta'$. Dispersed zones of the eutectoid breakdown $\text{Eg}(\alpha + \gamma')$ are observed between the needles. The iron partially dissolves in the β -phase and separates as the intermetallic compound Fe_3Al in a dispersed form.

After ageing at 200 $^{\circ}\text{C}$, an increase in acicular β' -grains is observed in terms of size and quantity (Figure 12) due to the inverse transformation $\gamma' \rightarrow \beta_1$ (Figure 9) due to temperature-accelerated diffusion. The β -phase is the hardest phase of all registered phases in Figure 9, and thus, the hardness as an integral mechanical characteristic of the studied bronze is significantly increased (see Figure 6c). A mechanical mixture of copper-enriched α -grains and the intermetallic compound Fe_3Al is formed between the acicular β -grains. No formed α -grain boundaries are observed.

As the ageing temperature increases to 300 $^{\circ}\text{C}$, the diffusion increases, causing the partial disintegration of acicular β' -grains: $\beta' \rightarrow \beta_1 + \gamma'$ (Figure 13). As a consequence of the coagulation of a dispersed phase of Fe_3Al , relatively large grains of this intermetallic compound are observed.

After ageing at 400 $^{\circ}\text{C}$, grains are observed whose boundaries represent stripe-shaped α -subgrains, marked with a dashed green line in Figure 14. A partial tearing of the borders is noticeable in places. Temperature-induced diffusion accelerates the nucleation of the α -solid solution network and the transformation $\beta' \rightarrow \text{Eg}(\alpha + \gamma') + \beta_1$. In the rest of the β' -grains, the dissolved iron is separated in the form of dispersed particles of Fe_3Al .

Figure 15 presents the structure after ageing at 500 $^{\circ}\text{C}$. The process of phase separation $\beta' + \beta_1 \rightarrow \text{Eg}(\alpha + \gamma')$ is finished. No metastable phases were found (Figure 9). Precipitated dispersed particles of Fe_3Al are observed in the grains of the α -solid solution. The refinement of the stripe-like α -grains is observed because of diffusion processes. The established maximum tensile strength (see Table 5) is a consequence of the homogeneous and refined structure and dispersed particles of Fe_3Al .

Figure 16 displays the structure of bronze subjected to ageing at 600 $^{\circ}\text{C}$ (i.e., the heating is above the eutectoid line of 565 $^{\circ}\text{C}$; see the static diagram in Figure 3). In this region, the α -phase, γ_2 -phase and δ_{Fe} are in equilibrium. All three phases are stable below the eutectoid line. Unlike the static diagram, the heating region also contains a β -phase due to an initially quenched structure (see position 2 in Figure 9). The metastable β' -phase is formed during air cooling, a consequence of the partial martensitic transformation $\beta \rightarrow \beta'$, and part of the grains undergo diffusion decay $\beta \rightarrow \alpha + \gamma'$. At this ageing temperature, zones form with lamellar α -subgrains (outlined with a white line).

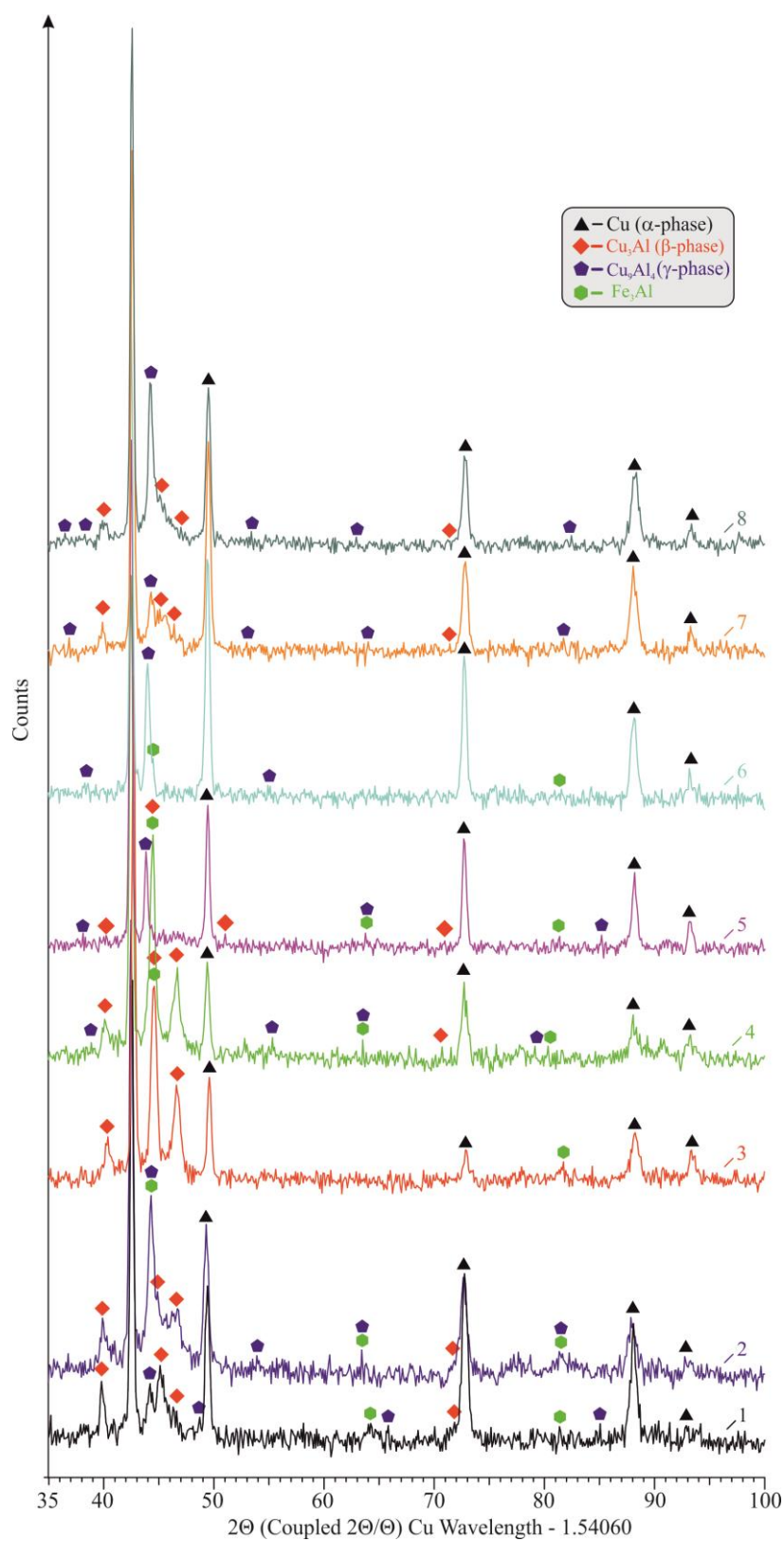


Figure 9. Phase analysis outcomes depending on ageing temperature: 1—as cast; 2—20 °C; 3—200 °C; 4—300 °C; 5—400 °C; 6—500 °C; 7—600 °C; 8—700 °C.

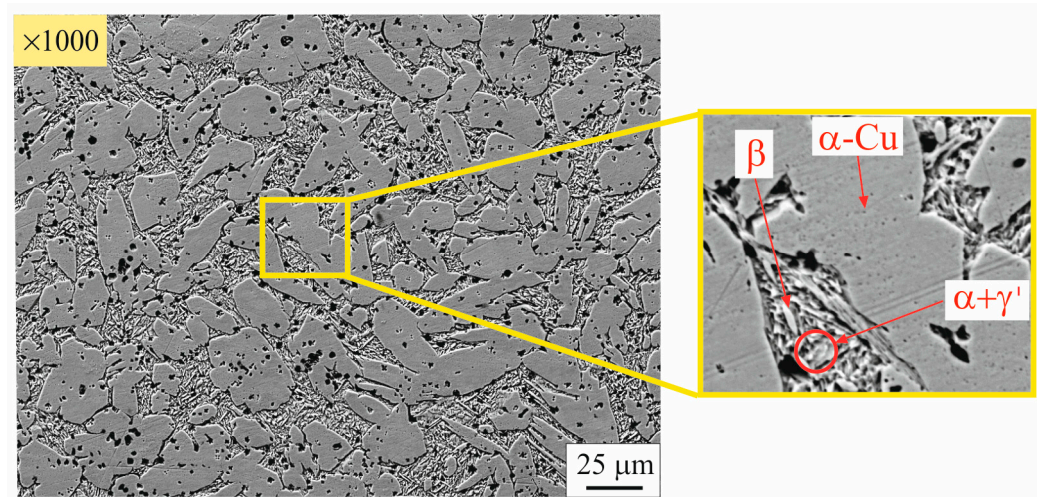


Figure 10. Microstructure in as-cast state.

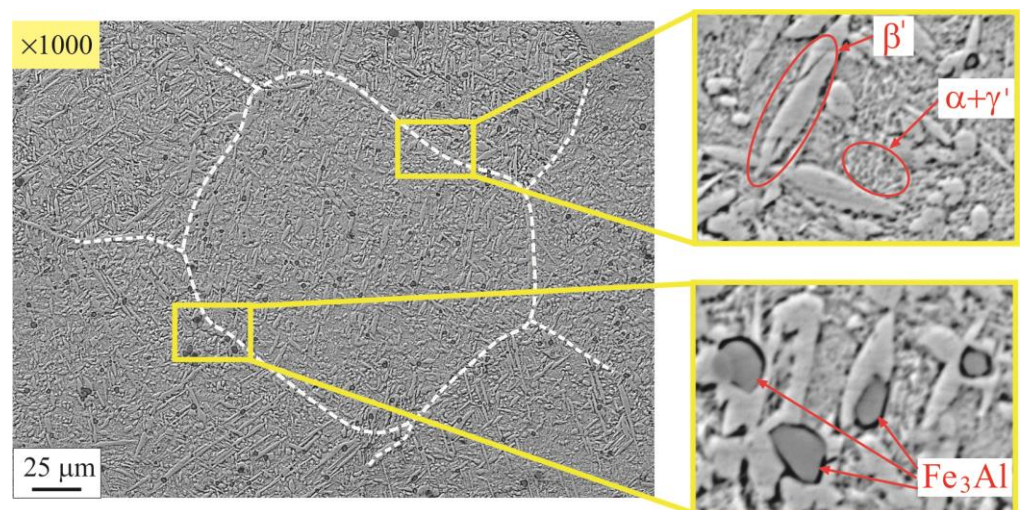


Figure 11. Microstructure at ageing temperature of 20 °C.

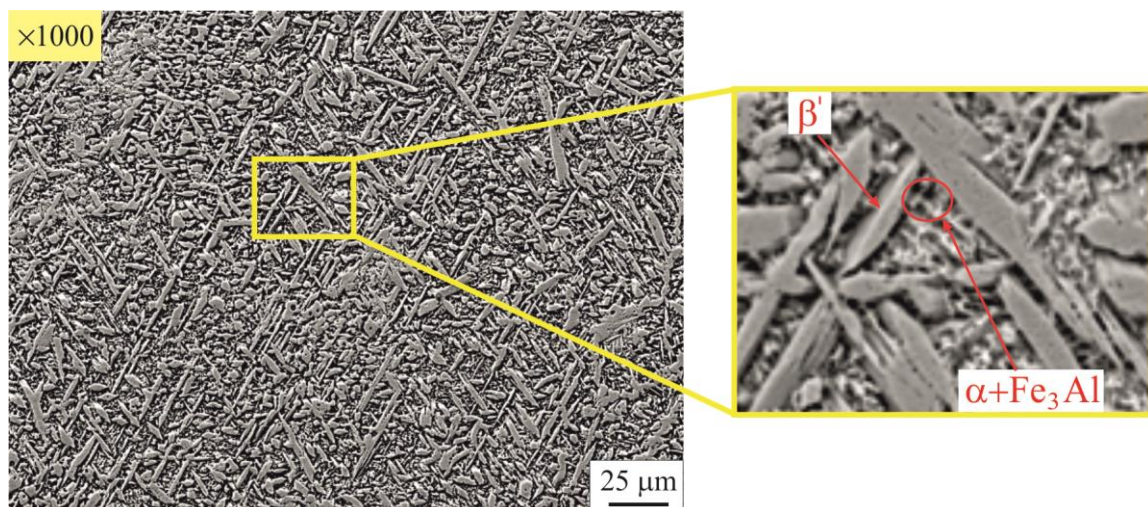


Figure 12. Microstructure at ageing temperature of 200 °C.

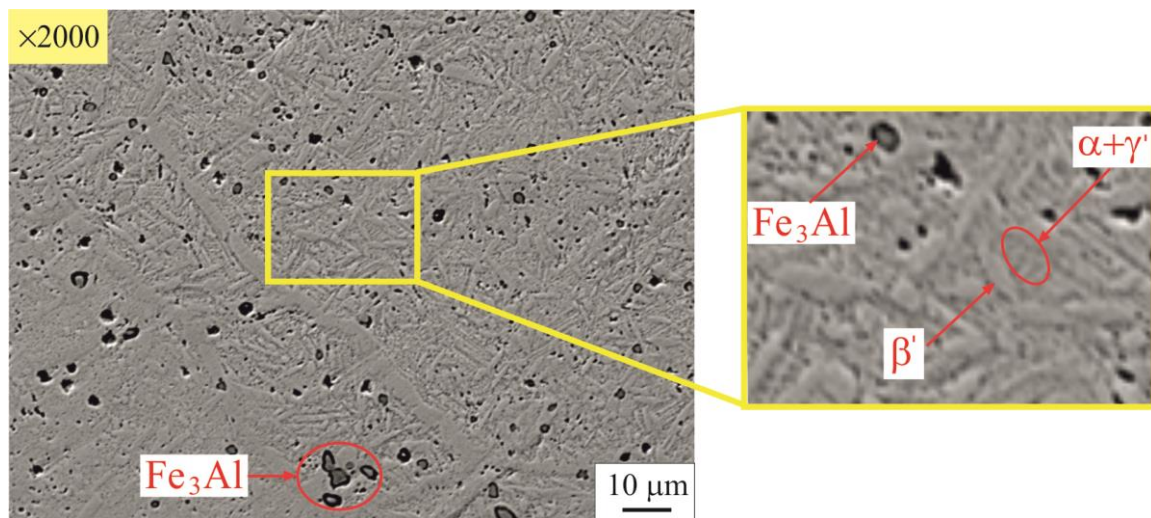


Figure 13. Microstructure at ageing temperature of 300 °C.

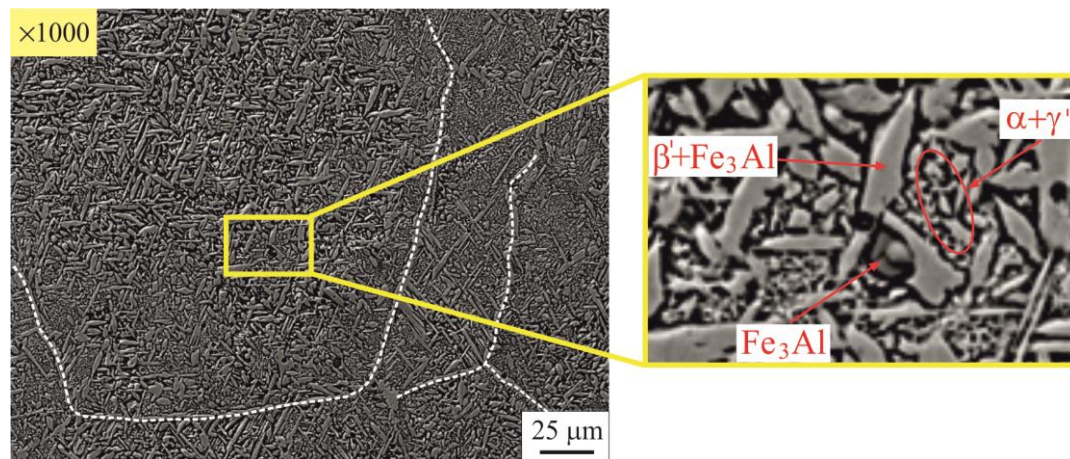


Figure 14. Microstructure at ageing temperature of 400 °C.

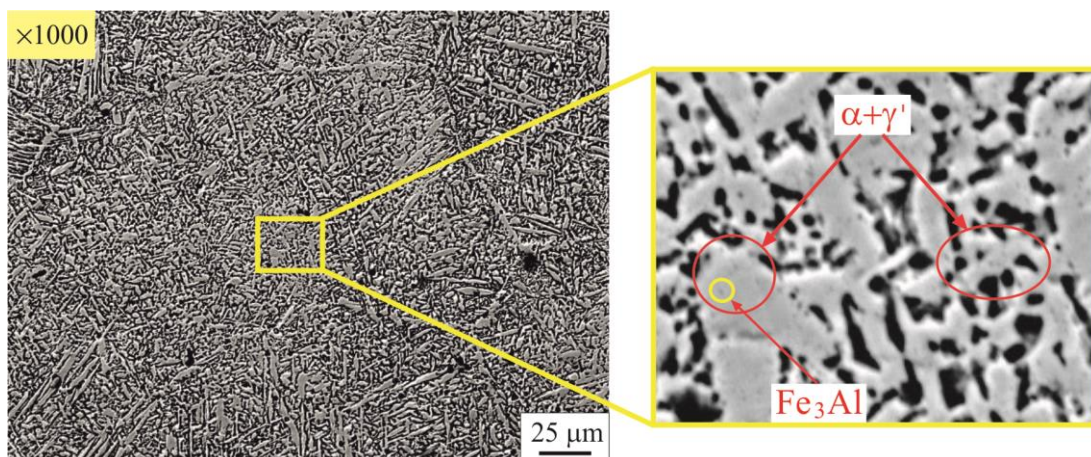


Figure 15. Microstructure at ageing temperature of 500 °C.

When the ageing temperature is 700 °C, conditions are created for grouping and subsequent coagulation of the copper-enriched α -phase (Figure 17). The mechanism of clustering and growth of equiaxed α -grains is likely similar to the process occurring at a lower temperature (see Figure 16). Higher temperatures accelerate the diffusion processes

and cause larger grains to enlarge at the expense of smaller grains. Thus, the resulting structure is inhomogeneous with the formed zones of the coarse-grained α -phase and enclosed zones containing a mechanical mixture of the partial martensitic and diffusion transformations $\beta \rightarrow \beta' + \gamma'$. The partial martensitic transformation is due to the higher cooling rate in the air. The β -phase increases its degree of homogeneity (respectively expanding its solubility region) when the heating temperature increases. A study [12] found that the β -phase partially dissolves iron atoms. This reason may be why no Fe_3Al peak is observed in the X-ray pattern in Figure 9.

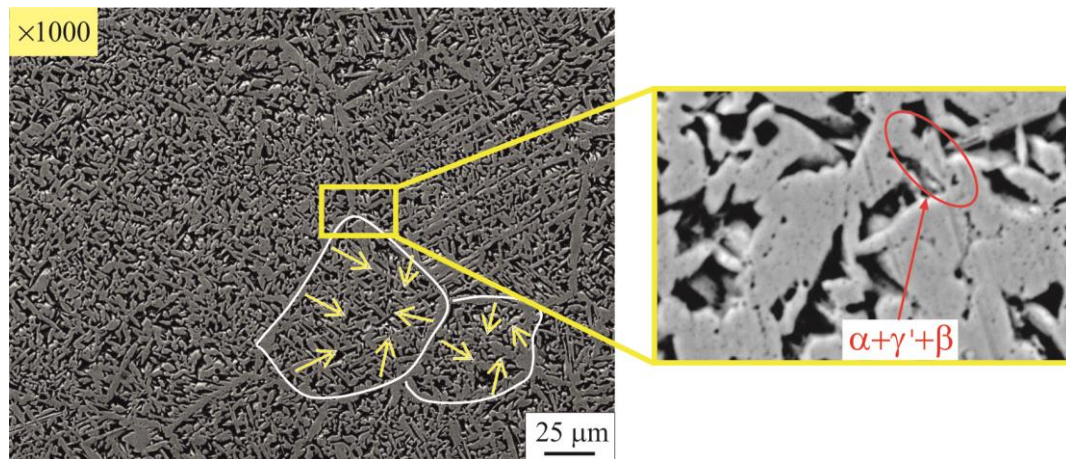


Figure 16. Microstructure at ageing temperature of 600 °C.

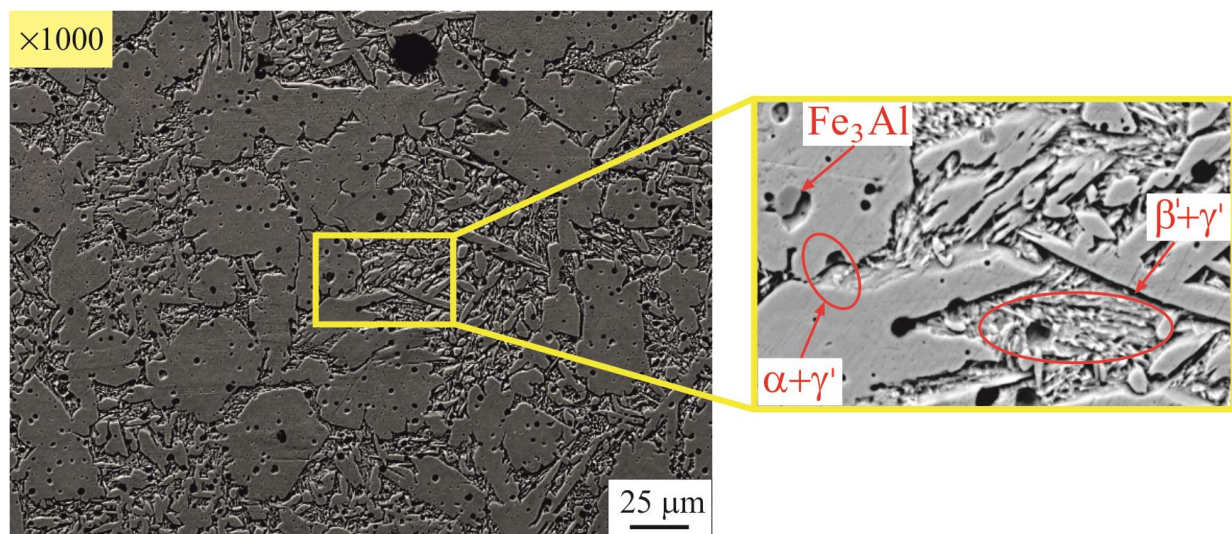


Figure 17. Microstructure at ageing temperature of 700 °C.

3.3. Effect of Heat Treatment on Mechanical Characteristics: Planned Experiment and Optimisation

According to the one-factor-at-a-time experimental results, the governing factors were chosen to change as follows: $200\text{ °C} \leq T \leq 700\text{ °C}$ and $1\text{ h} \leq t \leq 4\text{ h}$. Table 2 lists the governing factor levels. The correlation between natural $\tilde{x}_i$ and coded x_i coordinates is

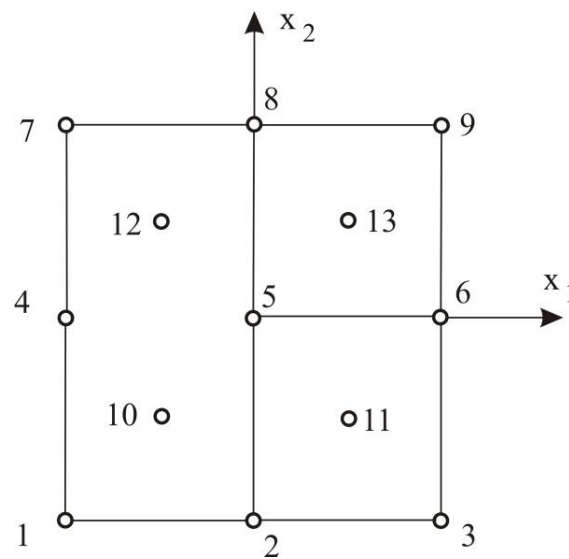
$$x_i = \frac{2(\tilde{x}_i - \tilde{x}_{0,i})}{\tilde{x}_{\max,i} - \tilde{x}_{\min,i}}, \quad (1)$$

where $\tilde{x}_{\max,i}$, $\tilde{x}_{0,i}$ and $\tilde{x}_{\min,i}$ are the upper, middle, and lower levels of the i th factor in natural coordinates, respectively.

Table 2. Governing factor levels.

Governing Factors			Levels									
	Natural	Coded	Natural					Coded				
Ageing temperature	T, °C	x_1	200	325	450	575	700	−1	−0.5	0	0.5	1
Ageing time	t, h	x_2	1	1.75	2.5	3.25	4					

The objective functions are the following mechanical characteristics: yield limit (Y_{σ_y}), tensile strength (Y_{σ_u}), elongation (Y_{A_5}), hardness (Y_{HB}) and impact toughness (Y_{IT}). Figure 18 provides the experimental points in the plane of governing factors. Table 3 lists the experimental outcomes for the chosen mechanical characteristics.

**Figure 18.** The experimental points in the governing factors plane.**Table 3.** Experimental design and outcomes.

No.	x_1	x_2	σ_y MPa	Y_{σ_y} MPa	σ_u MPa	Y_{σ_u} MPa	A_5 %	Y_{A_5} %	HB	Y_{HB}	IT J/cm ²	Y_{IT} J/cm ²
1	−1	−1	327	335.4	580.5	580.4	1.6	1.59	236	236.04	14.4	14.03
2	0	−1	413	413	794.5	798.9	2.85	2.66	232	227.35	8.5	8.8
3	1	−1	267	258.6	668	669.6	10.25	10.24	170	171.07	50.9	52.26
4	−1	0	329.5	322.9	614.5	616.9	1.8	1.81	250	251.06	17.3	18.83
5	0	0	397	397	700	700	2.7	3.07	222	227.34	8.6	8.8
6	1	0	239.5	246.1	619.5	617.1	11.6	11.61	155	156.05	58.6	57.07
7	−1	1	316.5	314.7	717.5	715.2	5.75	5.74	251	249.57	15.2	14.03
8	0	1	429.5	429.5	760.5	756.1	3.65	3.47	230	227.35	9.3	8.8
9	1	1	236	237.8	625.5	626.3	9.25	9.24	160	157.54	52.1	52.26
10	−0.5	−0.5	383.5	386.4	652	644.8	2.5	2.50	247	254.96	9.7	9.5
11	0.5	−0.5	310.5	307.6	730.5	726.1	10.15	10.15	184	187.84	57.7	55.5
12	−0.5	0.5	369	366.1	649.5	656.7	2.4	2.40	265	258.34	9.3	9.5
13	0.5	0.5	284.5	287.4	689	693.5	11.9	11.90	187	184.46	53.3	55.5

An analysis of variance (ANOVA) was conducted via QStatLab [23] to investigate the significance of the governing factors. Figure 19 provides the main ANOVA effects. For all objective functions, the most significant factor is x_1 (temperature). Time has the most substantial influence on the tensile strength. The yield limit (Figure 19a) is at its maximum when the temperature is at the middle level and the time is at the second level ($x_2 = -0.5$). The combination of maximum temperature and time at the middle level minimises the yield limit. The influence of the governing factors on the tensile strength is

similar (Figure 19b). When the temperature and time simultaneously occupy the fourth level ($x_1 = x_2 = 0.5$), the elongation is maximal (Figure 19c). The combination of the minimum time and temperature at the second level ($x_1 = -0.5$) minimises the elongation. When the temperature is at the second level ($x_1 = -0.5$) and the time is at the fourth level ($x_2 = 0.5$), the hardness is at a maximum (Figure 19d). The minimum hardness is obtained when the temperature is at a maximum and the time is at the middle level ($x_2 = 0$). The influence of the governing factors on the impact toughness is analogous to their influence on the elongation (Figure 19e). The ANOVA predicts the influence of the governing factors only in a qualitative aspect. More accurate results are obtained after mathematically modelling the studied mechanical characteristics.

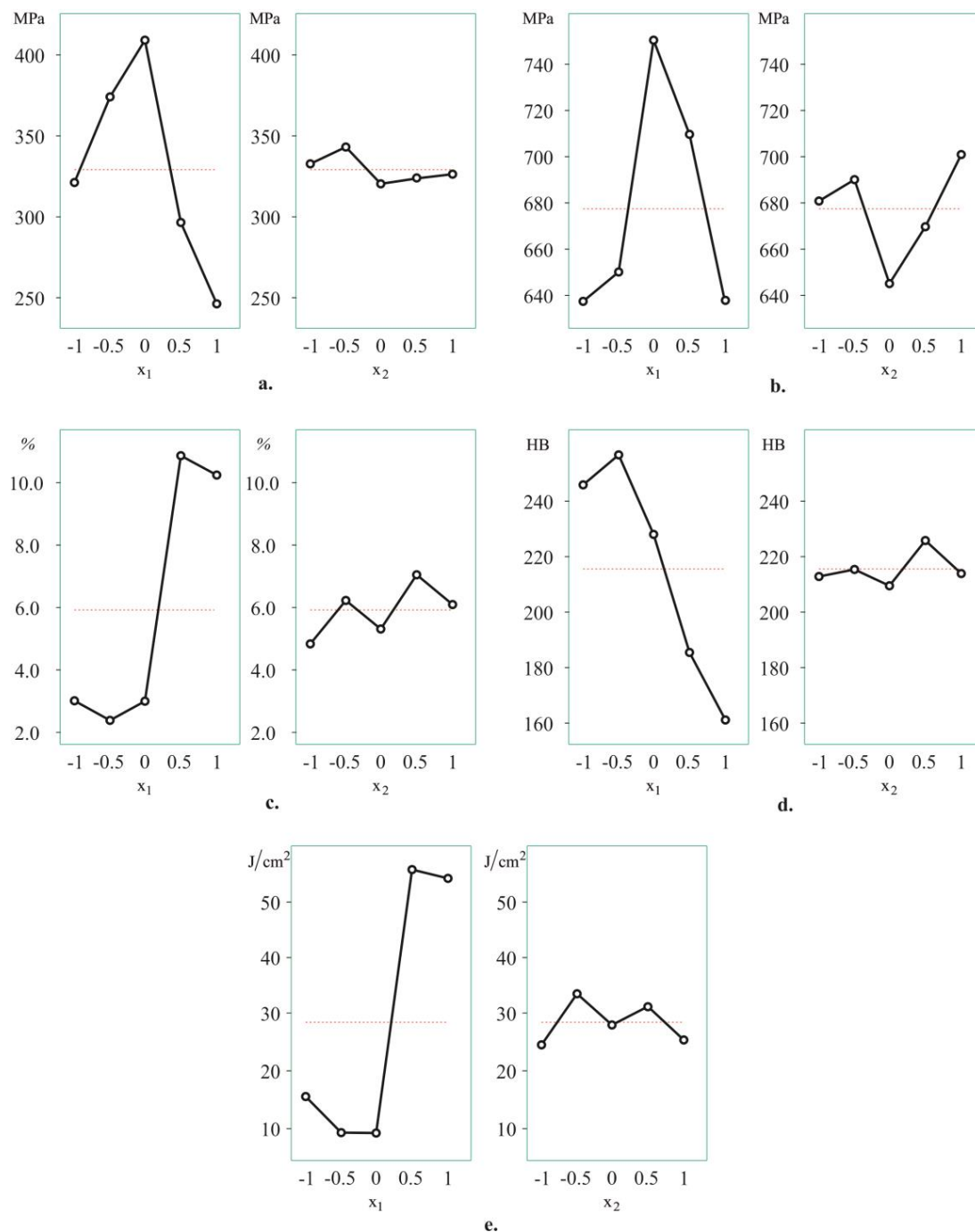


Figure 19. ANOVA main effects: (a) yield limit; (b) tensile strength; (c) elongation; (d) hardness; (e) impact toughness.

The experimental results for the mechanical characteristics were subjected to regression analyses. The significance of the regression coefficients was determined at $p = 0.05$. Given the chosen experimental design (five levels for each factor), the approximating polynomials may be of degree 4 or lower:

$$Y_k(\{X\}) = b_0 + \sum_{i=1}^m b_i x_i + \sum_{i=1}^{m-1} \sum_{j=i+1}^m b_{ij} x_i x_j + \sum_{i=1}^m b_{ii} x_i^2 + \dots, \quad k = 1, 2, \dots, q, \dots, \quad (2)$$

where $\{X\}$ denotes the vector of the governing factors, m represents the number of governing factors, and q indicates the number of objective functions.

The regression analyses were performed using QStatLab [23], and Table 4 presents the regression coefficients. The magnitude (absolute value) of the coefficients in front of the dimensionless variables indicates the significance of the corresponding governing factor (variable), and the absolute value of the coefficients in front of the products of the variables indicates the significance of the interaction between the governing factors. The regression coefficients in Table 4 indicate that (1) the ageing temperature is a much more significant factor than the ageing time, confirming the ANOVA results, and (2) the interaction between the governing factors is relatively weak, with the exception of the tensile strength.

Table 4. Coefficients of regression.

Coefficients	Objective Functions				
	Y_{σ_y}	Y_{σ_u}	Y_{A_5}	Y_{HB}	Y_{IT}
b_0	397.0000	700.0000	3.0667	227.3488	8.8
b_1	−92.1944	78.6389	10.4208	−80.9167	54.9611
b_2	−23.5417	−21.3825	0.8375	0	0
b_{11}	−308.1250	−165.4583	18.3639	−23.7907	118.2833
b_{22}	24.2500	77.5000	0	0	0
b_{12}	0	−44.5294	2.8958	−6.7647	0
b_{111}	53.7778	−78.5555	−5.5208	33.4167	−35.8444
b_{222}	31.7917	0	−0.4375	0	0
b_{112}	−18.6250	44.2771	0.3875	0	0
b_{122}	0	0	−1.8625	8.25	0
b_{1111}	195.625	82.4583	−14.7222	0	−89.1333
b_{2222}	0	0	0	0	0
b_{1112}	0	0	−4.1833	0	0
b_{1122}	−22.1250	−46.6250	0	0	−4.8
b_{1222}	0	0	0	0	0

Table 3 presents the values of the objective functions calculated using Equation (2) for the experimental points from the plan. The comparison between the experimental results for the objective functions and those predicted by the models (at the experimental points) displays excellent agreement. Figure 20 presents a graphical visualisation of the models. The type of surfaces confirms that the ageing temperature is the more significant of the two factors. The ageing time influences the tensile strength most strongly (confirming the ANOVA results), whereas the influence is weakly expressed for the other characteristics. The factor least sensitive to the ageing time is the impact toughness.

The two primary characteristics of static strength (yield limit and tensile strength) similarly depend on the temperature. As the temperature increases, the static strength increases and reaches its maximum value between 400 °C and 500 °C, after which it begins to decrease at a faster rate. The behaviour of hardness is similar, but it reaches its maximum values earlier (in the interval between 250 °C and 300 °C) and then decreases to a minimum. The elongation and the dynamic strength (impact toughness) display similar behaviour under temperature and time changes because both characteristics have a common physical basis. The behaviour of the dynamic strength when changing the temperature is opposite to that of the static strength. The maximum values of all objective functions, $\max Y_j$, and

their corresponding magnitudes of the governing factors, x_i^m , were found with QStatLab using the random search method with 1000 iterations. Table 5 lists the results.

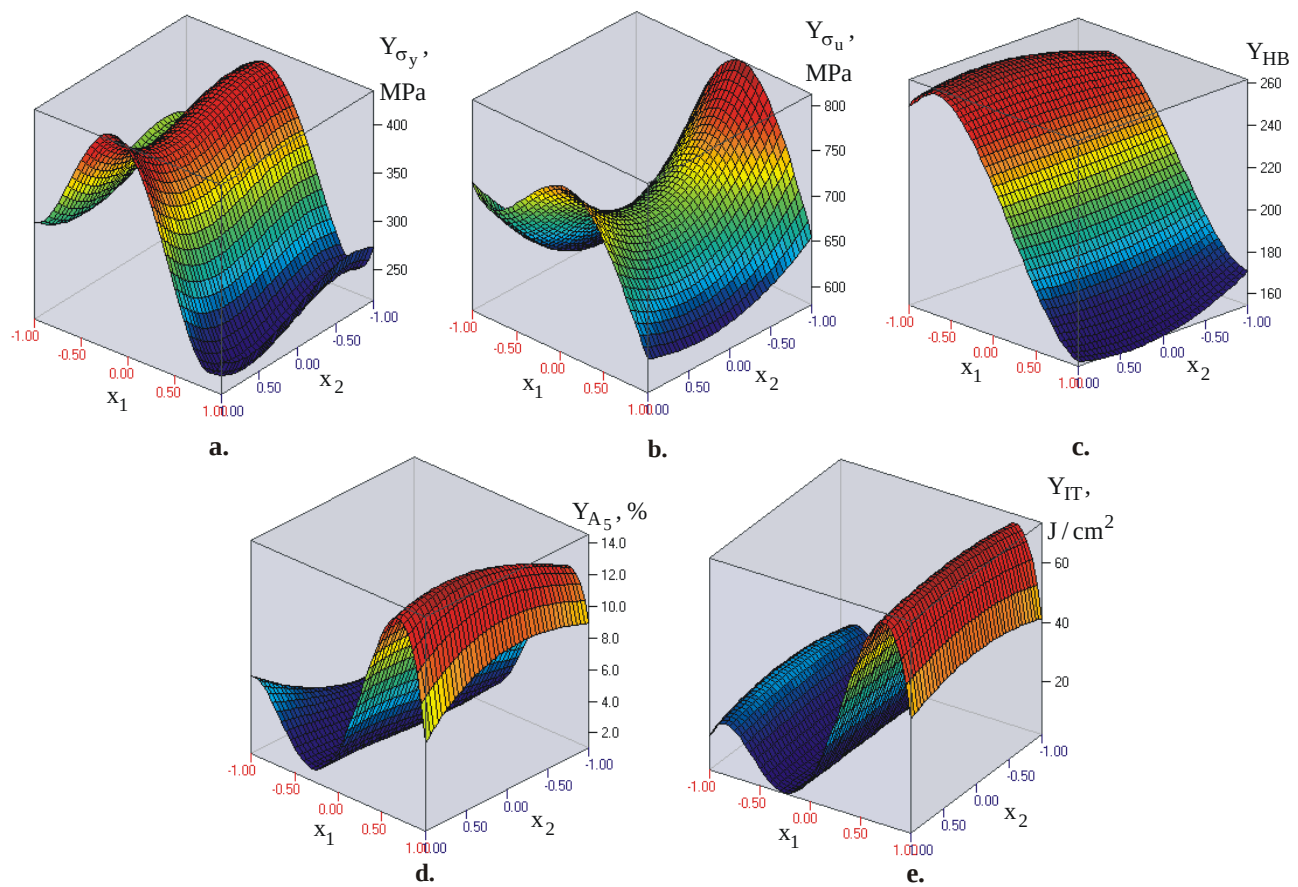


Figure 20. Graphical visualisation of the models: (a) yield limit; (b) tensile strength; (c) hardness; (d) elongation; (e) impact toughness.

Table 5. Maximum values of the objective functions and the corresponding governing factors.

Objective Functions	Governing Factors		Maximum Values $\max Y_j$
	Coded	Natural	
Y_{σ_y} , MPa	$x_1^m = -0.19582$ $x_2^m = 0.98008$	$T^m = 401\text{ }^\circ\text{C}$ $t^m = 3\text{ h } 58\text{ min}$	431.8
Y_{σ_u} , MPa	$x_1^m = 0.33077$ $x_2^m = -0.99671$	$T^m = 505\text{ }^\circ\text{C}$ $t^m = 1\text{ h}$	812.9
Y_{A_5} , %	$x_1^m = 0.75517$ $x_2^m = 0.41485$	$T^m = 639\text{ }^\circ\text{C}$ $t^m = 3\text{ h } 7\text{ min}$	14.6
Y_{HB}	$x_1^m = -0.68099$ $x_2^m = 0.39878$	$T^m = 280\text{ }^\circ\text{C}$ $t^m = 3\text{ h } 6\text{ min}$	261.8
Y_{IT} , J/cm ²	$x_1^m = 0.78857$ $x_2^m = 0.00032$	$T^m = 647\text{ }^\circ\text{C}$ $t^m = 3\text{ h } 41\text{ min}$	73.65

The correlations between the five objective functions were found by eliminating the governing factors for the pair of considered objective functions. These correlations are essential for setting and solving optimisation problems and for correctly defining the functional constraints. The correlations of the hardness with each of the other four mechanical characteristics were determined. Figure 21 graphically visualises the data. The dependencies of the mechanical characteristics on the hardness are nonlinear. As the hardness increases, the static strength increases up to a specific hardness value (approximately 230 HB for the yield

limit and 210 HB for the tensile strength), and subsequently decreases. The elongation and dynamic strength trendlines indicate a continuous decrease when the hardness increases.

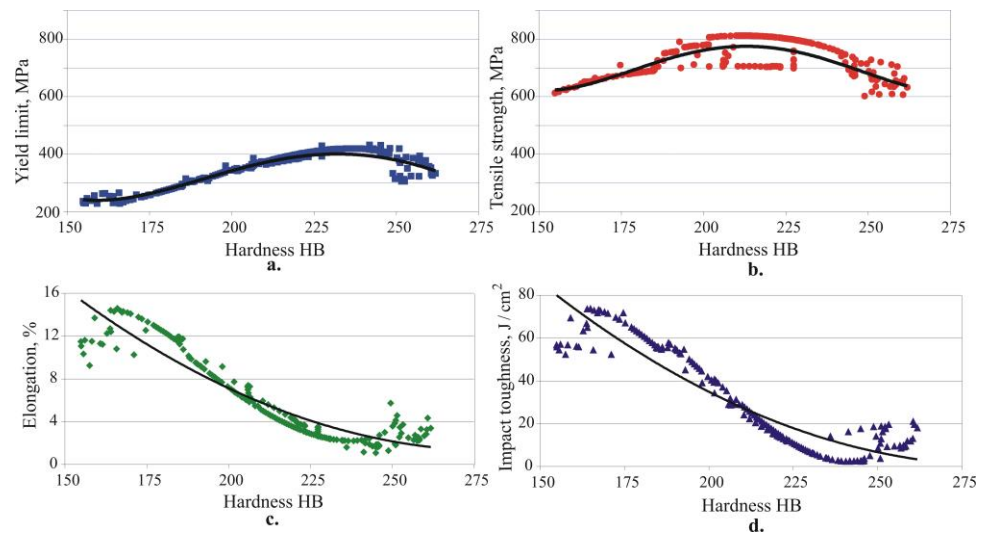


Figure 21. Graphical visualisation of the correlations between: (a) yield limit and hardness; (b) tensile strength and hardness; (c) elongation and hardness; (d) impact toughness and hardness.

Four optimisation tasks, which have the most significant importance for practice, were formulated and solved:

- (1) Maximum plasticity: $Y_{A_5} = \max Y_{A_5}$;
- (2) Maximum impact toughness (dynamic strength): $Y_{IT} = \max Y_{IT}$;
- (3) Simultaneous high hardness and static strength: The objective function vector is

$$\left\{ \vec{Y}(\{X\}) \right\} = \left[Y_{HB} \ Y_{\sigma_y} \ Y_{\sigma_u} \right]^T,$$

where $\{X\} = [x_1 \ x_2]^T \in \Gamma_x$ and Γ_x is the plane of the governing factors x_i . The objective functions must tend to their maximum values: $Y_{HB} \rightarrow \max Y_{HB}$, $Y_{\sigma_y} \rightarrow \max Y_{\sigma_y}$ and $Y_{\sigma_u} \rightarrow \max Y_{\sigma_u}$. Based on Figure 21, the following are the functional limitations: $Y_{HB} > 230$ HB, $Y_{\sigma_y} > 410$ MPa and $Y_{\sigma_u} > 750$ MPa.

- (4) Simultaneously high hardness, static and dynamic strength: The objective function vector is $\left\{ \vec{Y}(\{X\}) \right\} = \left[Y_{HB} \ Y_{\sigma_y} \ Y_{\sigma_u} \ Y_{IT} \right]^T$.

The objective functions must tend to their maximum values: $Y_{HB} \rightarrow \max Y_{HB}$, $Y_{\sigma_y} \rightarrow \max Y_{\sigma_y}$, $Y_{\sigma_u} \rightarrow \max Y_{\sigma_u}$ and $Y_{IT} \rightarrow \max Y_{IT}$. The following are functional limitations, according to Figure 21: $Y_{HB} > 190$ HB, $Y_{\sigma_y} > 320$ MPa, $Y_{\sigma_u} > 750$ MPa and $Y_{IT} > 49$ J/cm².

The first two single-objective optimisation tasks require determining the largest value of the corresponding function without functional limitations and satisfying the governing factor limitations (Table 2). Table 5 lists their solutions. The last two are multiobjective optimisation problems. The vector $\{X_j^*\} = [x_{1,j}^* \ x_{2,j}^* \ x_{3,j}^*]^T \in \Gamma_x$ must be determined so that the objective function magnitudes $Y_{k,j}(\{X_j^*\})$ to satisfy the conditions of the corresponding multiobjective optimisation task, and $x_{1,j}^*$, $x_{2,j}^*$ and $x_{3,j}^*$ are the compromised optimal values of the governing factors. The defined multiobjective optimisation tasks were solved by searching for the Pareto-optimal solution approach. The decision was made through the nondominated sorting genetic algorithm (NSGA-II) [25] using QstatLab. A Pareto front offering 50 compromised optimal solutions was obtained for each of the two

tasks. Figures 22 and 23 illustrate the Pareto front for the third and fourth optimisation problems. A compromised optimal solution is selected from each Pareto front. Table 6 contains detailed information regarding the solution results for the four optimisation tasks.

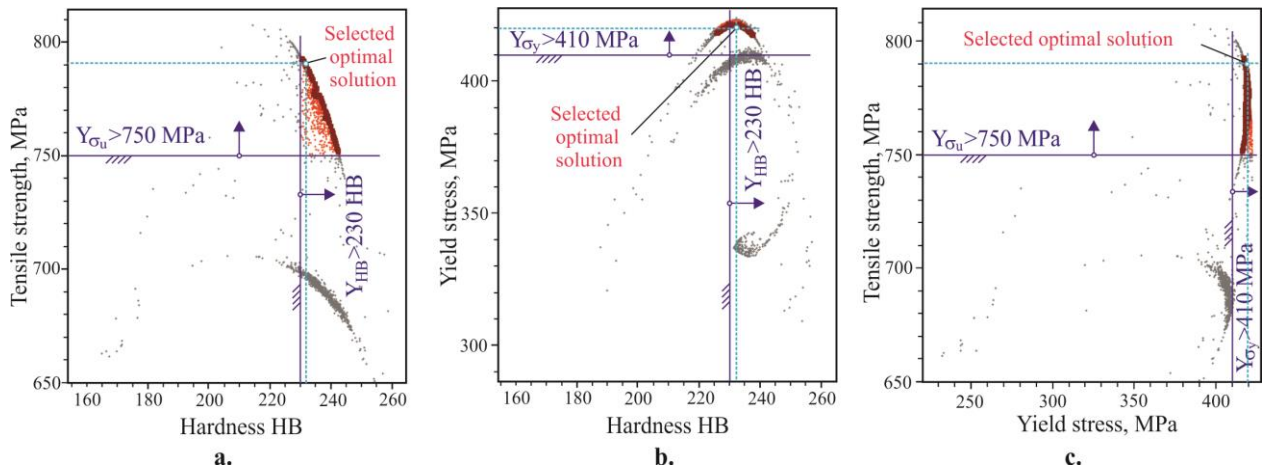


Figure 22. Generated Pareto front for third optimisation task: (a) tensile strength—hardness; (b) yield limit—hardness; (c) tensile strength—yield stress.

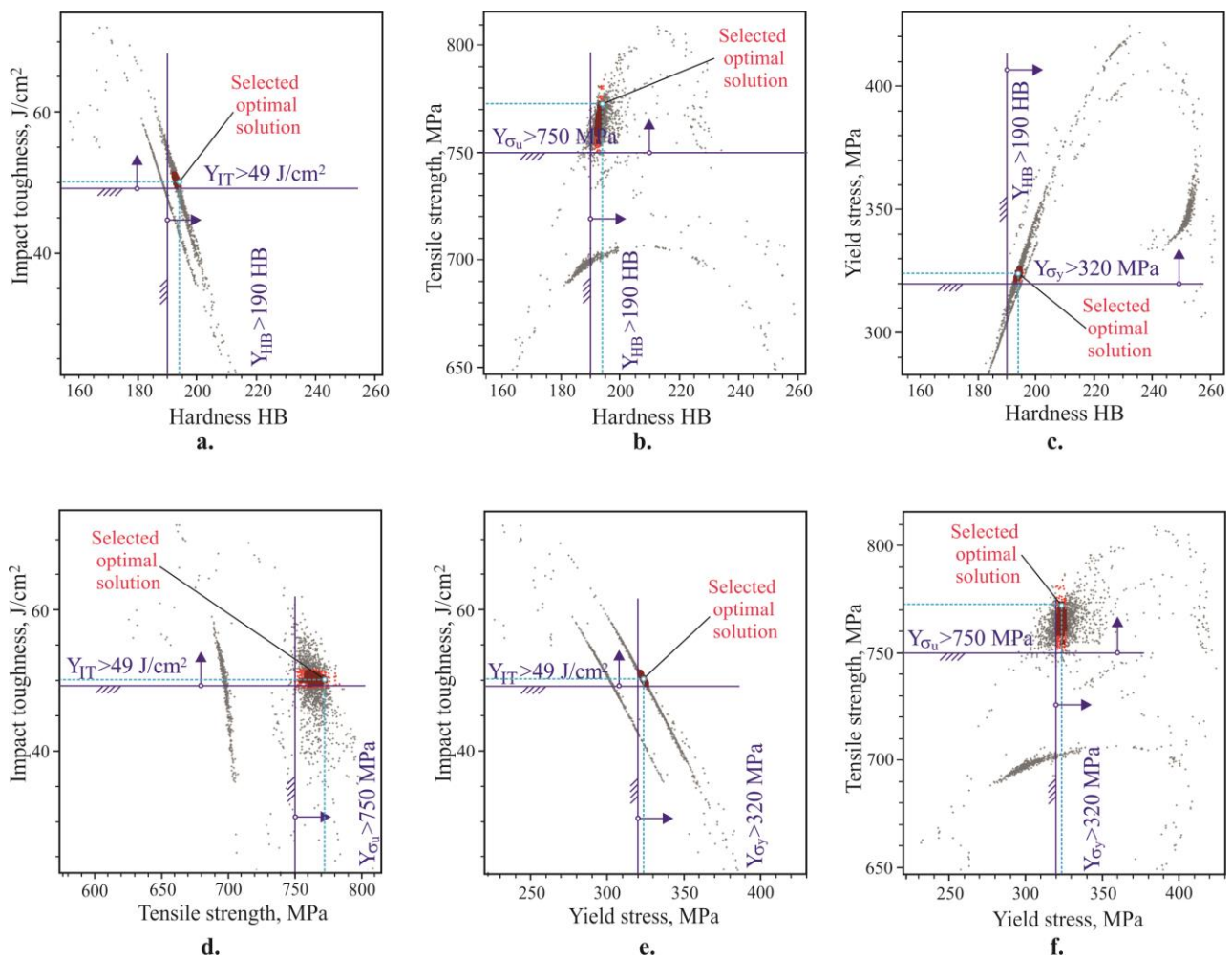


Figure 23. Generated Pareto front for fourth optimisation task: (a) impact toughness—hardness; (b) tensile strength—hardness; (c) yield stress—hardness; (d) impact toughness—tensile strength; (e) impact toughness—yield stress; (f) tensile strength—yield stress.

Table 6. Optimal compromise values of the objective functions and governing factors.

Optimisation Task	Optimal Governing Factors		Objective Functions $Y_j(\{X_i^*\})$				
	Codded	Natural	$Y_{A_5}, \%$	$Y_{IT}, \text{J/cm}^2$	Y_{HB}	Y_{σ_y}, MPa	Y_{σ_u}, MPa
1	$x_1^* = 0.75517$ $x_2^* = 0.41485$	$T^* = 639\text{ }^\circ\text{C}$ $t^* = 3\text{ h } 7\text{ min}$	$\max Y_{A_5} = 14.6$	72.86	166.00	228.54	654.43
2	$x_1^* = 0.78857$ $x_2^* = 0.00032$	$T^* = 647\text{ }^\circ\text{C}$ $t^* = 3\text{ h } 41\text{ min}$	14.3	$\max Y_{IT} = 73.65$	165.13	234.7	652.48
3	$x_1^* = -0.1163$ $x_2^* = -1$	$T^* = 421\text{ }^\circ\text{C}$ $t^* = 2\text{ h } 19\text{ min}$	2.25	3.98	234.64	419.45	791.22
4	$x_1^* = 0.4512$ $x_2^* = -0.8375$	$T^* = 563\text{ }^\circ\text{C}$ $t^* = 1\text{ h } 15\text{ min}$	8.52	50.01	194.23	323.78	772.88

The results of the optimisations were experimentally verified. For this purpose, additional samples were manufactured for tensile and impact toughness tests, which were hardened at $920\text{ }^\circ\text{C}$ in water and subjected to subsequent ageing with the optimal values (Table 6) of the governing factors for the respective optimisation task. The hardness was measured on the impact toughness samples. Each experimental result was obtained as the arithmetic mean of three samples. Table 7 presents the results. The comparison with the theoretical optimisation results displays good agreement.

Table 7. Experimental verification of the optimisation outcomes.

Optimisation Task	Optimal Values of the Objective Functions														
	Y _{A5} , %			Y _{IT} , J/cm ²			Y _{HB}			Y _{σ_y} , MPa			Y _{σ_u} , MPa		
	Optim. Value	Experim.		Optim. Value	Experim.		Optim. Value	Experim.		Optim. Value	Experim.		Optim. Value	Experim.	
		Min	Max		Min	Max		Min	Max		Min	Max		Min	Max
1	14.6	13.5	14.4	72.86	63.0	65.5	166.00	163	168	228.54	239	254	654.43	673	689
2	14.3	13.0	13.4	73.65	66.0	69.2	165.13	173	176	234.7	256	259	652.48	661	669
3	2.25	2.45	3.6	3.98	5.9	7.4	234.64	233	236	419.45	405	412	791.22	771	781
4	8.52	9.2	9.9	50.01	53.8	59.1	194.23	183	188	323.78	311	319	772.88	768	774

4. Conclusions

As outcomes of this investigation, the significant new findings concerning the ageing heat treatment of IAB with β -transformation, obtained using the centrifugal casting method, are presented below.

- The primary mechanical characteristics (yield limit, tensile strength, elongation, hardness and impact toughness) of IAB with β -transformation vary widely depending on the governing parameters of the ageing heat treatment. Therefore, their characteristics can be appropriately controlled according to the functional purpose of the corresponding bronze component. Of the two governing factors (temperature and time), the ageing temperature has a significantly greater weight. The temperature interval $640\text{ }^\circ\text{C}$ to $650\text{ }^\circ\text{C}$ maximises the plasticity and dynamic strength, whereas the hardness and static strength reach their maximum values in the interval of $280\text{ }^\circ\text{C}$ to $500\text{ }^\circ\text{C}$.
- Four optimisation tasks, with the most significance in practice, were formulated and solved. Thus, the optimal (compromise optimal) values of the temperature and time and the corresponding optimal (compromise optimal) magnitudes of the mechanical characteristics for the respective optimisation task were obtained.
- The correlations of the hardness with each of the other four mechanical characteristics were determined. The dependencies of the mechanical characteristics on the hardness are nonlinear. As the hardness increases, the static strength increases up to a specific

hardness value (approximately 230 HB for the yield limit and 210 HB for the tensile strength) and subsequently decrease. The elongation and dynamic strength trendlines display a continuous decrease when the hardness increases.

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References

1. Brezina, P. Heat treatment of complex aluminium bronzes. *Int. Met. Rev.* **1982**, *27*, 77–120. [\[CrossRef\]](#)
2. Alam, S.; Marshallt, R.I.; Sasaki, S. Metallurgical and tribological investigations of aluminium bronze bushes made by a novel centrifugal casting technique. *Tribol. Int.* **1996**, *29*, 487–492. [\[CrossRef\]](#)
3. Gao, L.L.; Cheng, X.H. Microstructure, phase transformation and wear behavior of Cu-10%Al-4%Fe alloy processed by ECAE. *Mater. Sci. Eng. A* **2008**, *473*, 259–265. [\[CrossRef\]](#)
4. Xu, X.; Zhao, H.; Hu, Y.; Zong, L.; Qin, J.; Zhang, J.; Shao, J. Effect of hot compression on microstructure evolution of aluminium bronze alloy. *J. Mater. Res. Technol.* **2022**, *19*, 3760–3776. [\[CrossRef\]](#)
5. Vu, A.T.; Nguyen, D.N.; Pham, X.D.; Tran, D.H.; Vuong, V.H.; Pham, M.K. Influence of strengthening phases on the microstructure and mechanical properties of CuAl₉Fe₄ alloy. *Int. J. Sci. Eng. Res.* **2018**, *9*, 346–351.
6. Chau, M.Q.; Vu, A.T.; Le, T.S.; Mai, V.T.; Nguyen, D.N.; Doan, X.T.; Do, H.C.; Nguyen, D.T. Influence of tempering time on microstructure and mechanical properties of CuAl₉Fe₄ alloy. *J. Mech. Eng. Res. Dev.* **2021**, *44*, 75–85.
7. Slama, P.; Dlouhy, J.; Kövér, M. Influence of heat treatment on the microstructure and mechanical properties of aluminium bronze. *Mater. Technol.* **2014**, *48*, 599–604.
8. Jain, P.; Nigam, P.K. Influence of heat treatment on microstructure and hardness of nickel aluminium bronze (Cu-10Al-5Ni-5Fe). *J. Mech. Civ. Eng.* **2013**, *4*, 16–21. [\[CrossRef\]](#)
9. Aaltonen, P.; Klemetti, K.; Hannien, H. Effect of tempering on corrosion and mechanical properties of cast aluminium bronzes. *Scand. J. Metall.* **1985**, *14*, 233–242.
10. Mi, G.; Zhang, J.; Wang, H. The effect of ageing heat treatment on the mechanical properties of Cu-Al-Fe-(x) alloys. *Key Eng. Mater.* **2011**, *467–469*, 257–262. [\[CrossRef\]](#)
11. Matijevic, B.; Sushma, T.S.K.; Prathvi, B.K. Effect of heat treatment parameters on the mechanical properties and microstructure of aluminium bronze. *Tech. J.* **2017**, *11*, 107–110.
12. Maximov, J.; Duncheva, G.; Anchev, A.; Dunchev, V.; Argirov, Y.; Todorov, V.; Mechkarova, T. Effects of heat treatment and severe surface plastic deformation on mechanical characteristics, fatigue and wear of Cu-10Al-5Fe bronze. *Materials* **2022**, *15*, 8905. [\[CrossRef\]](#) [\[PubMed\]](#)
13. Singh, C.; Dar, Y.A.; Malhotra, D.; Sharma, D. Study of Centrifugal Casting of Cast Iron Rolls and its Problem Formulation at India Factory, Malerkotla, Punjab (India). *Indian J. Appl. Res.* **2014**, *4*, 188–190. [\[CrossRef\]](#)
14. Chen, Z.; Su, Y.; Gong, S.W. Effect of Centrifugal Casting on Microstructures and Properties of Hypereutectic Al-18wt.%Si Alloy. In Proceedings of the International Forum on Energy, Environment and Sustainable Development (IFEESD 2016), Shenzhen, China, 16–17 April 2016; pp. 706–710.
15. Gupta, M.K.; Nayak, S.; Kachhawaha, A.K. Analysis of centrifugal casting defects on their manufacturing parameters. *J. Harmon. Res.* **2015**, *3*, 05–08.
16. Ebhota, W.S.; Karun, A.S.; Inambao, F.L. Centrifugal casting technique baseline knowledge, applications, and processing parameters: Overview. *Int. J. Mater. Res.* **2016**, *107*, 960–969. [\[CrossRef\]](#)
17. Jörg, F.; Betül, K.A.; Heiner, M.; Gerhard, K.; Erwin, B.R. Effect of Ti₆Al₄V surfaces manufactured through precision centrifugal casting and modified by calcium and phosphorus ion implantation on human osteoblasts. *Metals* **2020**, *10*, 1681. [\[CrossRef\]](#)
18. Mohapatra, S.; Sarangi, H.; Mohanty, U.K. Effect of processing factors on the characteristics of centrifugal casting. *Manuf. Rev.* **2020**, *7*, 26. [\[CrossRef\]](#)
19. Jurković, K.; Cajner, H.; Mrvar, P.; Bauer, B. Analysis of factor effects in process of vertical centrifugal casting. *Mater. Manuf. Process.* **2023**. [\[CrossRef\]](#)

20. Florenciano, J.T.O.; Ambrosi, A.; Hotza, D.; González, S.Y.G. Understanding centrifugal casting in the manufacture of functionally graded materials. *J. Eur. Ceram. Soc.* **2022**, *42*, 7089–7101. [[CrossRef](#)]
21. Panikolov, K.L.; Petrov, M.S. *Special Metal Casting Technology*; Technika: Sofia, Bulgaria, 1973. (In Bulgarian)
22. Lv, S.; Dou, R.; Yu, B.; Wang, J.; Liu, X.; Wen, Z. Experimental and numerical studies on the influence of centrifugal casting parameters on the solidification structure of Al-Cu alloy. *Mater. Res. Express* **2022**, *9*, 106506. [[CrossRef](#)]
23. Vuchkov, I.N.; Vuchkov, I.I. *QStatLab Professional*, version 5.5; Statistical Quality Control Software, User's Manual; QStatLab: Sofia, Bulgaria, 2009.
24. Vuchkov, I.; Stoyanov, S. *Mathematical Modeling and Optimization of Technological Objects*; Technics: Sofia, Bulgaria, 1986. (In Bulgarian)
25. Deb, K.; Pratap, A.; Agarwal, S.; Meyarivan, T. A fast and elitist multiobjective genetic algorithm: NSGA-II. *IEEE Trans. Evol. Comput.* **2002**, *6*, 182–197. [[CrossRef](#)]

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