



# Article Study of Quenched Crankshaft High-Cycle Bending Fatigue Based on a Local Sub Model and the Theory of Multi-Axial Fatigue

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Abstract: For critical steel engine parts, such as crankshafts, the fatigue strength under the critical working condition is usually improved by the electromagnetic induction quenching technique. In a previous study, the strengthening effect of this approach was always evaluated by a constant, which may result in some errors with the change of the technological parameters. In this paper, a type of steel crankshaft is selected to study the strengthening effect of this approach; first a local sub model composed of the crankpin is built to simulate the magnetic–thermal coupling process, then, the residual stress field is determined by simulating the whole course of fabrication. Finally, the prediction of the fatigue limit load is proposed based on the residual stress and the strength parameters of the material. The experimental verification shows that, when compared to the general means of modification models, the modified McDiarmid multi-axial fatigue model is more suitable to be applied to analyze the fatigue property of this quenched crankshaft due to the markedly higher accuracy. Based on this study, a new fatigue-limit load-prediction approach of this kind of crankshaft can be proposed for engineering applications.

Keywords: crankshaft; electromagnetic induction quenching; multi-axial fatigue model; bending fatigue

# 1. Introduction

Nowadays, family cars are widely used in daily life. For this modern mechanical equipment, various dynamic loads are applied to the parts [1,2]. Thus, a special surface strengthening method is necessary to ensure that the parts can fulfil the corresponding service life requirements. Among these methods, the electromagnetic induction quenching approach is considered to be an effective choice [3,4]. This technique can effectively improve the fatigue strength of the metal parts, such as the steel crankshafts, to make them applicable to the high-power engine, thus corresponding technique parameters are necessary to be reasonably planned during the design stage.

In recent years, some experts focused on researching this problem. Among them, Cajner proposed a 2D simplified axial symmetrical model to conduct the numerical simulation of the electromagnetic induction quenching approach on a 42CrMo steel crankshaft; the experimental verification showed that this model can provide accurate surface hardness and hardness layer-depth results [5]. Dmitry conducted a technological parameter influence analysis of this approach and proposed a corresponding model to accurately simulate the process [6]. Mohan proposed a new optimal design method based on a satisfactory function, which was established during the electromagnetic induction quenching process [7]. Stephanie compared the mechanical and microstructure properties of the 42CrMo steel after electromagnetic induction quenching and conventional heat treatment process through the standard tensile experiment and pyramid hardness test. The result showed that yield strength and hardness of the steel after electromagnetic induction quenching were a little



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**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). lower than those of the steel after a conventional heat treatment process, which can be attributed to the size effect [8]. Dietmar applied the adaptive finite element analysis approach in simulating the electromagnetic induction quenching of the gear and obtained accuracy for the temperature and hardening curve [9]. Umberto researched the microstructure and mechanical property of the hardening layer and proposed that the main influence factors were the heating and cooling speeds during the electromagnetic induction quenching, as well as the peak value of the temperature [10]. Akram proposed novel alternate magnetic field treatments in EN8 steel and discovered that this approach could improve the wear resistance and reduce the coefficient of the friction of the material, which could be explained by the increase in the compressive residual stress and the microhardness. This method can also be applied to the fatigue property research of similar metal materials [11].

Nowadays, the turbocharging technique has been widely applied for improving the engine power, which results in the more critical demand for the fatigue strength of some key metal parts, such as the crankshaft. As a result of this, a more accurate assessment of the strengthening effect of this approach is necessary. However, the strengthening effect of this approach has not been quantitatively evaluated. In addition, the heat-up process of the electromagnetic induction quenching approach is usually no more than 20 s and corresponding components are surrounded by the coil. This situation makes the real-time experiment verification difficult to conduct.

In a previous study, we evaluated the strengthening effect of this technique by considering the residual stress as the mean stress and applied corresponding mean stress models to the prediction of the fatigue limit load of a given type of steel crankshaft [12,13]. The theoretical foundation of this approach is that both the mean and alternating stresses are uniaxial and in the same direction; whereas, for the parts with complicated shapes, the state of the alternating stress is usually multi-axial, even though the load applied to it is the uniaxial type [14,15]. This situation makes the application of the mean stress models unreasonable to some degree.

In this paper, a comprehensive assessment of the strengthening effect of the electromagnetic induction quenching technique is conducted. First, the whole process of this approach is simulated by a finite element model to provide the basic stress and temperature information. Then, a combination of the residual stress field obtained in a previous chapter and a verified multi-axial fatigue model are chosen to predict the fatigue limit load of the crankshaft. Finally, the predictions based on different models are checked by the corresponding experiment verification. The results show that, when compared to the usual modified models based on the mean stress, the modified McDiarmid multi-axial fatigue model can exhibit higher accuracy in this prediction, thus possessing practicability and value of popularization in actual engineering applications.

#### 2. Materials and Methods

## 2.1. The Prediction Process

Figure 1 shows the structural property of the electromagnetic induction quenching equipment, from which it can be determined that the whole equipment can be divided into three parts: the crankpin coil, the fillet coil, and the magnetizer between the coils and the crankshaft.

According to the fatigue damage theory, the quenching process used in actual engineering applications is considered for improving the fatigue strength of a given part in two ways: changing the structural stress and generating the compressive residual stress at the stress concentration point. During the quenching process, the same electric current flows through the coil during the quenching process. Due to the smaller cross-sectional area, the current density in the fillet coil is greater than that in the crankpin coil. In addition, the fillet coil is fabricated into an arc shape to ensure that the air gap between the coil and the crankshaft remains steady. In this way, a good heating effect is achieved. On the other hand, the structural stress on the crankshaft caused by the uneven material property is



not obvious [12]. Based on this assumption, the prediction of the fatigue limit load of the quenched steel crankshaft can be achieved as follows:

Figure 1. The structure diagram of the electromagnetic induction quenching equipment.

Step 1: In this step, the whole quenching process (including the heating and cooling stages) of a given type of crankshaft (the material is high-strength alloy steel) was exhibited by the finite element analysis. In this way, the temperature field evolution process was performed in detail.

Step 2: The temperature field evolution process obtained in the previous step was chosen to be the temperature load to simulate the residual stress field after the cooling stage.

Step 3: In this step, a verified multi-axial fatigue model was selected to be applied in predicting the fatigue limit load of the treated crankshaft based on two parameters: the combination of this stress field and the residual stress field above, and the shear fatigue strength of the material. The relationship between the prediction and existing parameters can be expressed as:

$$\tau_r + \frac{M_e}{M_A} \tau_A = \tau_b \tag{1}$$

In this equation,  $M_e$  and  $M_A$  are the prediction of the fatigue limit load and the certain load applied to the crankshaft, respectively;  $\tau_r$  and  $\tau_A$  are the effective stress of the residual stress field; and the effective stress under load  $M_A$ , respectively,  $\tau_b$  is the shear fatigue limit of the material.

#### 2.2. The Coordinate Transform Method

According to the prediction equation above, it is not difficult to find out that the key parameters among the prediction process are the effective stress of the residual stress field and the effective stress under the alternating load. Nowadays, these parameters are calculated based on the given stress state and the chosen multi-axial fatigue damage model. On the other hand, the critical plane approach is considered to be an effective method in researching the multi-axial fatigue components. For the simple construction objects, such as the smooth and notched specimens, the direction of the critical plane and corresponding effective stress can be easily determined by theoretical analysis; whereas, for the parts with complicated shape, such as the crankshafts, the direction of the critical plane cannot be directly determined due to the complex stress state.

In a previous study, we found that the modified McDiarmid model could provide a high enough accuracy to predict the fatigue limit load of the steel crankshaft. The critical plane according to this model is the plane with the maximum shear stress. In addition, the direction of this plane can be determined by a coordinate transform method. The principle of this method is shown in Figure 2.



Figure 2. A random plane crossing the calculation point.

As shown in Figure 2, point *O* is a random point in the three-dimensional space, as well as the original point of the coordinate system *O*-*XYZ*. The plane  $\Delta$  is a random plane in the space that crosses point *O*, and *n* is the normal vector of this plane. The angles between the projection of the normal vector *n* in the coordinate system *O*-*XYZ* and the *X*, *Z* axis are  $\theta$  and  $\varphi$ , respectively. For point *O*, the 3D stress tensor in the coordinate *O*-*XYZ* is expressed as:

$$\sigma = \begin{bmatrix} \sigma_{11} & \sigma_{12} & \sigma_{13} \\ \sigma_{21} & \sigma_{22} & \sigma_{23} \\ \sigma_{31} & \sigma_{32} & \sigma_{33} \end{bmatrix}$$
(2)

As shown in Figure 2, the coordinate *O-abn* is another coordinate that also crosses point *O*. Therefore, the expressions of the normal vector *n* and the *a*, *b* axis in the coordinate system can be expressed as:

$$n = \begin{bmatrix} n_x \\ n_y \\ n_z \end{bmatrix} = \begin{bmatrix} sin\theta cos\varphi \\ sin\theta sin\varphi \\ cos\theta \end{bmatrix}$$
(3)

$$a = \begin{bmatrix} a_x \\ a_y \\ a_z \end{bmatrix} = \begin{bmatrix} sin\varphi \\ -cos\varphi \\ 0 \end{bmatrix}$$
(4)

$$b = \begin{bmatrix} b_x \\ b_y \\ b_z \end{bmatrix} = \begin{bmatrix} \cos\varphi\cos\theta \\ \cos\theta\sin\varphi \\ -\sin\theta \end{bmatrix}$$
(5)

In plane  $\Delta$ , *m* is a random line that crosses point *O*. The angle between this line and the axial *a* is  $\alpha$ . Therefore, the expression of the unit vector along the line *m* is:

$$m = \begin{bmatrix} m_x \\ m_y \\ m_z \end{bmatrix} = \begin{bmatrix} \cos\alpha \sin\varphi + \sin\alpha \cos\theta \cos\varphi \\ -\cos\alpha \cos\varphi + \sin\alpha \cos\theta \sin\varphi \\ -\sin\theta \sin\alpha \end{bmatrix}$$
(6)

Based on these parameters, the shear stress in the plane *nom* can be expressed as:

$$\boldsymbol{\tau}_{ns} = \begin{bmatrix} \boldsymbol{m}_{x} \\ \boldsymbol{m}_{y} \\ \boldsymbol{m}_{z} \end{bmatrix}^{T} \begin{bmatrix} \sigma_{11} & \sigma_{12} & \sigma_{13} \\ \sigma_{21} & \sigma_{22} & \sigma_{23} \\ \sigma_{31} & \sigma_{32} & \sigma_{33} \end{bmatrix} \begin{bmatrix} \boldsymbol{n}_{x} \\ \boldsymbol{n}_{y} \\ \boldsymbol{n}_{z} \end{bmatrix}$$
(7)

Nowadays, the stress tensor of point O in Equation (2) can be easily determined by a finite element analysis. Therefore, the shear stress in any plane that crosses the same point can be determined by changing the values of the corresponding three angles from

Equations (3)–(7). In this way, the maximum value of the shear stress and corresponding critical plane direction can be determined.

#### 3. Results

## 3.1. Heating Stage Analysis

3.1.1. Mesh Model and Material Parameter

In this paper, the research was conducted on a steel crankshaft from a six-cylinder diesel engine. In addition, the electromagnetic field showed obvious dissipation properties in the air [16]. As a result of this, the far field technique was chosen to build the finite element model as follows:

As shown in Figure 3, this finite element model was built based on the finite element software Altair flux. In order to reduce the simulation content, the model was only composed of a quarter of the crankpin and located in an approximately infinite field. This sub model was cut from the crankpin of the crankshaft. The distance between the coil and the crankshaft was 0.8 mm. According to the electromagnetism theory, the induced current was mainly located on the surface of the steel part. As a result of this, the temperature increased much more rapidly in this area due to the skin effect. Therefore, in this model, the mesh sizes of the surface elements were relatively smaller to provide higher accuracy; whereas, for the inner scope, the sizes of the elements were much larger to provide higher efficiency. In this way, an overall balance between the speed and accuracy could be achieved.



Figure 3. A quarter-pin model in the electromagnetic field ((a) Geometric model; (b) mesh model).

In this paper, the crankshaft was made of 42CrMo steel. Table 1 shows the detailed information of this material, from which it can be discovered that some of the material properties, such as the heat conductivity, change with the temperature [17].

**Table 1.** Basic parameters of the material.

Temperature (°C)	Relative Permeability (Mur)	Volumetric Heat Capacity (J·m <sup>3</sup> ·°C)	Heat Conductivity (m·°C)	Electrical Resistivity (Ω∙m)
25	200	3,685,270	38.5	$1.8 imes10^{-7}$
100	194	3,795,044	35.5	$2.0 imes10^{-7}$
200	188	4,085,161	35.0	$3.2  imes 10^{-7}$
300	181	4,390,960	33.5	$4.2 imes10^{-7}$
400	170	4,759,487	32.5	$5.0 imes10^{-7}$
500	158	5,237,788	31.0	$6.2 imes10^{-7}$
600	141	5,842,545	28.0	$7.7 imes10^{-7}$
700	100	6,845,193	24.5	$9.7 imes10^{-7}$
760	1	8,429,075	20.0	$1.0 imes10^{-6}$
800	1	6,241,436	21.0	$1.2 imes 10^{-6}$
900	1	5,363,244	23.0	$1.2 imes 10^{-6}$
1000	1	5,308,357	22.5	$1.2 imes 10^{-6}$

#### 3.1.2. Definition of the Boundary Condition

In the heating stage, the temperature field was caused by a high-frequency current, which can be considered to be the load at this stage. As shown in Table 2, a clear conclusion can be discovered that the value of the current density in either coil is different from that in the other coil, while the values of the current intensity in both coils are the same. This phenomenon can be explained by the different cross-section areas of the two coils. In addition, the working mode of the fillet was continuously heated; whereas, for the crankpin, the current was terminated for 1 s after every 0.5 s of heating.

Table 2. Parameters of the load.

Detailed Parameter	Value
Current frequency	8000 Hz
Fillet working time	12 s
Crankpin working time	4 s
Current intensity	350 A
Current density (fillet coil)	$9.9 imes10^7 \mathrm{~A/m^2}$
Current density (crankpin coil)	$1.15  imes 10^8  ext{ A/m}^2$

During the heating process, the crankshaft and the coils were just placed in the air. According to the theory of thermodynamics, the thermal transmission types in this condition are heat convection and radiation. The corresponding boundary condition can, at this stage, be defined as:

$$-\lambda \frac{\partial T}{\partial n} = h(T_S - T_f) \tag{8}$$

For the parameters in the above formula,  $\lambda$  is the thermal conductivity,  $T_S$  is the temperature of the crankshaft surface, and  $T_f$  is the temperature of the air; h is the equivalent heat transfer coefficient. The corresponding transfer coefficients are 100 W/(m<sup>2</sup>·°C) and 0.8. In addition, the symmetric cross section of the model was set to be adiabatic due to the architectural feature of the crankpin.

#### 3.1.3. Simulation Results and Analysis

From Figures 4–7, the evolution process of the temperature field in different time nodes during the whole quenching process based on the finite element model built in the previous chapter is shown. As shown in Figure 4, the surface temperature of the fillet increases the fastest. This can be explained by the larger current density within the corresponding coil and longer heating time. After 6 s, an obvious increase can be discovered in the surface temperature of the fillet, as well as that of the crankpin. During this time node, the surface temperature was already high enough for the surface material to be transformed to austenite. However, the depth was still very thin (no more than 0.5 mm). On the other hand, the heating penetration of the fillet was obviously deeper than that of the crankpin. The reason for this phenomenon was also the differences between the working parameters. In Figures 5 and 6, the range of the high-temperature field obviously extends. The values of the heating depth at the fillet and the crankpin were nearly the same. The reason for this is the heat capacity at the fillet and heat conduction under the surface. This situation is beneficial for the generation of the surface layer. In Figure 7, after 12 s, the highest temperature point reached 1099 °C. The location of this point was at the central part of the crankpin.



**Figure 4.** Temperature field of the crankshaft (T = 3 s).



**Figure 5.** Temperature field of the crankshaft (T = 6 s).



**Figure 6.** Temperature field of the crankshaft (T = 9 s).



**Figure 7.** Temperature field of the crankshaft (T = 12 s).

#### 3.2. Cooling Process Analysis

# 3.2.1. Temperature Field Analysis

During this stage, the coolant was sprayed onto the surface of the crankshaft. The whole process lasted 10 s. As a result of this, an obvious decline in the surface temperature was discovered. In addition, the convective heat transfer coefficient between the crankshaft and the cooling liquid was much higher than that in the previous chapter. The detailed boundary condition information is shown in Table 3.

Table 3. Parameters of the boundary condition.

Parameter	Value
Convective heat transfer coefficient	$150.00 \text{ W}/(\text{m}^2 \cdot ^{\circ}\text{C})$
Radiative heat transfer coefficient	0.8
Young's modulus	210,000 MPa
Poisson's ratio	$1.35  imes 10^{-6} /  m K$
Coefficient of thermal expansion	1.35
Stefan-Boltzmann constant	$5.67 imes 10^{-8}~{ m W/(m^{-2}\cdot K^{-4})}$

Figures 8–11 show the temperature field evolution process of the crankshaft during the liquid cooling stage. The most notable feature was that, during this stage, the maximum temperature point gradually moved from the surface to the inner parts of the crankshaft. In Figure 9, the maximum temperature was 249 °C after 4 s. In Figure 10, the maximum temperature was 152 °C after 7 s. After 10 s, the surface temperature was nearly the same as the room temperature. In addition, compared to the crankpin, the cooling depth of the fillet was much higher. The main reason of this phenomenon can also be attributed to the higher heat capacity and quicker cooling speed of the former. Following this liquid cooling stage, the highest temperature dropped to 131 °C.

## 3.2.2. The Residual Stress Field Analysis

During this stage, the crankshaft was placed in the air until completely cooled. As a result of this, the internal thermal stress generated corresponding residual stress. In other words, the thermal load within this stage was the temperature field evolution process. Figure 12 shows the boundary condition of the finite element model during this stage. It can be concluded that the symmetrical freedom of the nodes on the symmetrical cut planes was fixed. The whole model was built based on the finite element software Abaqus.



Figure 8. Temperature field of the crankshaft (T = 1 s).



**Figure 9.** Temperature field of the crankshaft (T = 4 s).



**Figure 10.** Temperature field of the crankshaft (T = 7 s).



Figure 11. Temperature field of the crankshaft (T = 10 s).



Figure 12. Displacement boundary conditions of the crankshaft.

Figure 13 shows the residual stress field of the crankshaft. It can be observed that the type of the surface stress was compressive; whereas, for the inner area, the type was converted to tensile. The maximum stress point was located at the connecting area between the fillet and the crankpin with the value of -421.2 MPa.



Figure 13. The residual stress field distribution of the crankshaft.

## 3.3. Prediction and Experimental Verification

## 3.3.1. Multi-Axial Fatigue Model Selection

According to our previous study [17], for the parts with complicated shapes, the state of the alternating stress was usually multi-axial, even though the load applied to it was the uniaxial type. As a result, the fatigue type of this part was multi-axial [14,15]. According to our previous study, the stress ratio modified McDiarmid model can provide a high enough accuracy for the bending fatigue limit load prediction of the steel crankshaft. The definition of this model can be expressed as [18]:

$$\tau_{ns} + \frac{(1-R)\tau_{-1}}{2\sigma_h}\sigma_{n\max} = \tau_f'(2N_f)^c \tag{9}$$

where  $\tau_{ns}$  is the shear stress amplitude on the critical plane,  $\sigma_{nmax}$  is the maximum value of the normal, *R* is the stress ratio,  $N_f$  is the fatigue life,  $\tau_{-1}$  is the shear fatigue limit of the material,  $\sigma_b$  is the tensile strength of the material,  $\tau'_f$  and *c* are both material constants. The definition of the critical plane according to this model is the plane with the maximum shear stress, which can be determined by a combined coordinate transform and finite element method. The process of this method can be divided into two steps:

- 1. Determine the location of the maximum stress point of the crankshaft by a finite element model and record the stress tensor of the point.
- 2. Calculate the values of the shear stress in every plane. In this way, the coordinate of the maximum shear stress critical plane can be determined, as well as the normal stress.

## 3.3.2. Prediction Based on the Multi-Axial Fatigue Model

According to the method above, the first step was to determine the maximum stress point by the finite element method. Figure 14 shows the finite element model of the analysis, from which it can be observed that the boundary condition can be treated as restricting all the freedoms of the nodes at the right face for simplification. In this paper, a determined given bending moment (1000 N·m) was applied to the crankshaft; the result is shown in Figure 15.

As shown in Figure 15, the maximum Von Mises point under this given load is located at the fillet of the crankpin, and the corresponding value is 210.8 MPa; whereas, according to Figure 13, for the residual stress field, the value of the stress at the same point is 282 MPa. Table 4 shows the main parameters of the stress tensor of this point under the given load and from the residual stress field. Based on this parameter and the coordinate transform method mentioned in the Materials and Methods Section, the normal vector of the critical plane can be determined; the corresponding values are 136°, 90°, 91°, respectively. With the help of these three parameters, the shear and normal stresses of the critical plane from different sources can be determined; the results are shown in Table 5.



Figure 14. The finite element model of the crankshaft.



Figure 15. The Von Mises stress distribution of the crankshaft (under the given load).

Parameter	From the Given Load	From the Residual Str

Table 4. Stress components of the maximum stress point from different sources.

Parameter	From the Given Load	From the Residual Stress Field
S11	70.5 MPa	-72.5 MPa
S22	123 MPa	-75.1 MPa
S33	117 MPa	-323.8 MPa
S12	1.5 MPa	75.4 MPa
S13	-2.9 MPa	-1.6 MPa
S23	-118 MPa	2.03 MPa

Table 5. The stress components of the critical plane from the residual stress and the given load.

Parameter	<b>Residual Stress Field</b>	Given Load
Shear stress	−24.4 MPa	119.2 MPa
Normal stress	−157.3 MPa	—118.6 MPa

Based on these parameters and the modified McDiarmid model, the fatigue limit load of the crankshaft can be predicted. According to the previous study, the stress ratio of the bending fatigue experiment was -1, so the expression of the prediction can be proposed as:

$$\frac{M_e}{1000} \times 119.2MPa - 24.4MPa + \left[\frac{M_e}{1000} \times (-118.6MPa) - 157.3MPa\right] \times \frac{(1-R) \times 226MPa}{874MPa \times 2} = 226MPa$$
(10)

By solving this function, the value of the fatigue limit load of this crankshaft can be determined to be 3299 N·m.

3.3.3. Other Prediction Methods and Application

In the previous study [19], some researchers proposed different mean stress models to predict the fatigue limit load. The expressions of these commonly used mean stress models are shown in Table 6.

 Table 6. The expressions of the commonly used mean stress models.

Model Type	Expression	Model Type	Expression
Goodman Gerbera	$\sigma_{eq} = \frac{\sigma_a}{1 - \frac{\sigma_m}{\sigma_b}}$ $\sigma_{eq} = \frac{\sigma_a}{1 - \frac{\sigma_m}{\sigma_b}^2}$	Haigh Soderberg	$\sigma_{eq} = rac{\sigma_a}{1-\left(rac{\sigma_m}{\sigma_b} ight)^{0.5}} \ \sigma_{eq} = rac{\sigma_a}{rac{\sigma_a}{1-rac{\sigma_m}{\sigma_b}}}$
	$1 - \left(\frac{\sigma_m}{\sigma_b}\right)$		σy

In these equations,  $\sigma_{eq}$  is the effective stress amplitude,  $\sigma_a$  is the stress amplitude,  $\sigma_{-1}$  is the fatigue limit,  $\sigma_y$  is the yield strength,  $\sigma_m$  is mean stress, and  $\sigma_b$  is the tensile strength [19]. The predictions based on these four models are shown in Table 7.

Table 7. Predictions based on some other methods.

Model Name	Results (N·m)
Goodman	2494
Haigh	2956
Soderberg	2082
Gerbera	2683

## 3.3.4. Experimental Verification

In order to make a comprehensive contrast of the models mentioned above, a corresponding experimental verification was conducted at this stage to check the application of the prediction approach. Figure 16 shows the bending fatigue test bench of the crankshaft that consists of the electromagnetic vibration exciter, the master arm, the slave arm, the acceleration transducer, and the foundation bed. The crankshaft and the connected arms were vertically supported by springs, and the excitation force was generated by rotating the eccentric with the motor. In this way, a cyclic bending moment was applied to the crankshaft for fatigue testing. During the experiment process, the crack was expected to appear at the fillet of the crankshaft and the stiffness of the system decreased. As a result, the responsive acceleration and the amplitude of the load may increase if the frequency of the exciter remains unchanged. To avoid this unwanted situation, the rotation speed of the exciter decreases accordingly. When the speed decreases to a certain level, the crankshaft is considered broken [15]. In this paper, the value of the decrement of the rotate speed was 60 rpm. The serial number of the experiment standard used in this paper is QC-T637-2000 [20,21]. In this paper, 10 groups of experiments were conducted. The results are shown in Figure 17.



Figure 16. The bending fatigue experiment equipment.



Figure 17. Fatigue test results of the crankshaft.

As shown in Figure 17, the approximate liner regression relationship can be discovered between the fatigue life and the fatigue load in the double logarithmic coordinates. In addition, the squared value of the coefficient of association was 0.5265. In this paper, the sample size of the experiment was 10. According to the significance requirement of this parameter, the minimum value under this condition should be 0.497 when the significant degree is 1%. Therefore, these experimental results can be taken into the further analysis. Nowadays, most engineering equipment is required to be able to work normally during the designed working period [22,23]. In addition, the service life of a crankshaft is limited to a certain number of cycles, depending on the demand of the traveling distance. As a result, compared to the common fatigue property evaluation parameter (usually the fatigue life under a given load) [24,25], it is more important to correctly evaluate the high-cycle fatigue load of a crankshaft under a specified fatigue life [26,27]. According to the previous study, the SAFL (Statistical Analysis for Fatigue Limit) approach was considered to be an effective method to analyze the distribution property of the fatigue limit load [28]. Based on this method, the fatigue limit load prediction can be proposed. The results are shown in Table 8.

Load Value/N·m	Media Rank
2893	0.067308
3025	0.163462
3255	0.259615
3280	0.355769
3321	0.451923
3343	0.548077
3352	0.644231
3386	0.740385
3738	0.836538
3759	0.932692

Table 8. The median rank (failure rate) estimation of the fatigue limit load.

3.3.5. Prediction Errors and Discussion

According to the SAFL method, the distribution property of the fatigue limit load can be expressed by a Gaussian distribution function. As a result, the fatigue limit load of this crankshaft under a 50% survival rate was 3335 N·m.

As shown in Table 9, it can be found that the predictions based on the commonly used mean stress models results in obvious errors (the errors are all higher than 20%), which makes them inapplicable in this occasion; whereas the prediction provided by the modified McDiarmid multi-axial fatigue model is consistent with the experimental results (the error between them is less than 5%). The main reasons for this phenomenon may be analyzed by two sides:

Table 9. Errors of the predictions.

Model Name	Error
Goodman	32%
Haigh	22.8%
Soderberg	24.8%
Gerbera	43.2%
McDiarmid	1.1%

- (1) As shown in Table 5, the types of the normal and shear stress in the critical plane caused by the residual stress field are both compressive; whereas, for the alternating stress caused by the load, the type of shear stress in this critical plane is tensile and the type of normal stress is compressive. In addition, the ratios of the shear stress and the tensile stress from different sources are not the same. As a result, the effective stresses from these two sources are not in the same direction, which is not suitable for the application of the mean stress models.
- (2) According to our previous study, the fatigue damage type of the crankshaft in this condition is shear fatigue damage, while the modified McDiarmid multi-axial fatigue model is just considered to be a typical effective model in researching this type of problem. This makes the application of this model more effective.

# 4. Conclusions and Further Work Plan

In this paper, a new fatigue property prediction approach of quenched metal crankshaft was proposed. First, a local sub-model composed of the crankpin was built to simulate the magnetic-thermal coupling process. Then, the residual stress field was conducted by the subsequent thermal-mechanical coupling analysis. Finally, the fatigue limit load prediction of the treated crankshaft was achieved based on the parameters obtained above and the material property. The results show that this manufacturing procedure can generate uniform temperature fields at the surface of the crankpin area during the heating-up stage, which is beneficial to the forming of the uniform layer. In addition, when compared to the commonly used mean stress models, the modified McDiarmid multi-axial fatigue model can provide a high enough accuracy in predicting the fatigue limit load of the quenched crankshaft, which makes this model valuable in guiding the design of the manufacturing procedure.

During our study, we discovered that the extraction range of the sub model would not obviously influence the temperature field; whereas, for the residual stress field, different situations were discovered. Therefore, in our further work, we will focus on the influence of this factor. In addition, the material of the crankshaft in this paper was 42CrMo. The research on the application of this model in researching the crankshafts made by some other steel materials is still needed.

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