


## Article

# Thermodynamic Analysis and Experimental Investigation of Al and F Removal from Sulfuric Acid Leachate of Spent LiFePO<sub>4</sub> Battery Powder

Yafei Jie <sup>1</sup>, Shenghai Yang <sup>1,2</sup>, Pengfei Shi <sup>1</sup>, Di Chang <sup>1</sup>, Gang Fang <sup>1</sup>, Caixuan Mo <sup>1</sup>, Jiang Ding <sup>1</sup>, Zhiqiang Liu <sup>3,4</sup>, Yanqing Lai <sup>1,2</sup> and Yongming Chen <sup>1,2,\*</sup> 

<sup>1</sup> School of Metallurgy and Environment, Central South University, Changsha 410083, China; yafeijie1221@126.com (Y.J.); yangsh@mail.csu.edu.cn (S.Y.); 183512165@csu.edu.cn (P.S.); cd203501005@csu.edu.cn (D.C.); gang.fang@csu.edu.cn (G.F.); mocx1101@csu.edu.cn (C.M.); 0501170314@csu.edu.cn (J.D.); laiyanning@csu.edu.cn (Y.L.)

<sup>2</sup> Hunan Provincial Key Laboratory of Nonferrous Value-Added Metallurgy, Changsha 410083, China

<sup>3</sup> Institute of Rare Metals, Guangdong Academy of Science, Guangzhou 510651, China; Lzqgd168@126.com

<sup>4</sup> State Key Laboratory of Rare Metals Separation and Comprehensive Utilization, Guangzhou 510651, China

\* Correspondence: csuchenyongming@163.com; Tel.: +86-186-8468-5548

**Abstract:** The co-precipitation thermodynamics of the Li<sup>+</sup>–Fe<sup>2+</sup>/Fe<sup>3+</sup>–Al<sup>3+</sup>–F<sup>–</sup>–SO<sub>4</sub><sup>2–</sup>–PO<sub>4</sub><sup>3–</sup>–H<sub>2</sub>O system at 298 K is studied, aiming to understand the precipitation characteristics. Based on the principle of simultaneous equilibrium and the mass action law, the missing *K<sub>sp</sub>* values of AlF<sub>3</sub> and FeF<sub>3</sub> were estimated. The results of thermodynamic calculation demonstrate that Al<sup>3+</sup> and F<sup>–</sup> in the sulfuric acid leachate could be preferentially precipitated in the form of AlPO<sub>4</sub> and FeF<sub>3</sub> by the precise adjustment of the final pH value. Only a small amount of P and Fe was lost by the precipitation of Fe<sub>3</sub>(PO<sub>4</sub>)<sub>2</sub>·8H<sub>2</sub>O, FePO<sub>4</sub>, and Fe(OH)<sub>3</sub> during the purification process. Controlling the oxidation of ferrous ions effectively is of critical significance for the loss reduction of P and Fe. Precipitation experiments at different pH value indicated that the concentration of Al<sup>3+</sup> and F<sup>–</sup> in the leachate decreased as the final pH value rose from 3.05 to 3.90. When the final pH value was around 3.75, aluminum and fluoride ion impurities could be deeply purified, and the loss rate of phosphate ions and iron ions could be reduced as much as possible. Relevant research results can provide theoretical guidance for the purification of leachate in the wet recycling process of lithium-ion batteries.

**Keywords:** spent LiFePO<sub>4</sub> battery; sulfuric acid leachate purification; co-precipitation thermodynamics; aluminum precipitation; fluorine removal



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## 1. Introduction

Greenhouse gas emissions are severely aggravating global climate change, and thus all countries should formulate national policies to achieve zero carbon emissions [1,2]. China, for instance, has pledged to peak nationwide CO<sub>2</sub> emissions by 2030 and achieve carbon neutrality by 2060 [3,4]. Aimed at this goal, the zero-carbon industry represented by clean and renewable energy is facing a critical moment of accelerated development [5]. In the past decade, China has become the world's largest market of new energy vehicles (EV) as its EV stock reached 3,810,000 in 2019, nearly half of the global stock [6]. Given that the service life of power batteries is approximately 5–8 years, it is predicted that the cumulative decommissioning of powder batteries in China will reach 90.5 GWh from 2020 to 2022, of which spent LiFePO<sub>4</sub> batteries will account for 53.8% (48.7 GWh) [7].

Compared with traditional fuel vehicles, EV power battery systems use mineral resources such as lithium, cobalt, nickel, manganese, copper, aluminum, iron, phosphorus, and graphite [8]. Recycling valuable metal resources from discarded lithium batteries is the key to the sustainable development of the EV industry. On the other hand, if not professionally treated, potentially toxic components inside them would be directly disposed of

in the environment, causing serious damage to both humans and the environment [9–11]. Processes of dealing with spent  $\text{LiFePO}_4$  batteries are the direct regeneration process and the hydrometallurgical method [12]. Although the direct regeneration process is relatively simple and inexpensive, the long-term performance of repaired electrode materials could hardly meet the standard of power battery materials [13]. The hydrometallurgical process is the mainstream technology for lithium iron phosphate batteries treatment in Chinese recycling enterprises because of its low energy consumption, high product purity, and wide adaptability of raw materials. This process mainly involves pretreatment, leaching (selective leaching of Li or simultaneous leaching of Fe and Li), purification, and preparation of battery materials. In the leaching process, mineral acids ( $\text{H}_2\text{SO}_4$  [14–17],  $\text{HCl}$  [14,18,19],  $\text{HNO}_3$  [14],  $\text{H}_3\text{PO}_4$  [14,20–23]) and organic acids (oxalic acid [14,24,25], citric acid [14], acetic acid [14], methyl sulfonic acid [26], and *p*-toluene sulfonic acid [26]) are used as the leaching agent to dissolve the target metal in spent  $\text{LiFePO}_4$  battery powder. Among them,  $\text{H}_2\text{SO}_4$  is widely used as a leaching agent by lithium battery recycling companies due to its low price, easy fabrication, and strong acidity. Various impurity ions, such as Al, Cu, and F, will inevitably enter the leachate and finally affect the physicochemical properties of regenerated electrode materials. Current research on the purification process of leachate largely focuses on spent  $\text{LiCoO}_2$  and ternary batteries; by contrast, there are few reports on the purification of acid leachate of the spent  $\text{LiFePO}_4$  battery. At present, the purification process of leachate includes solvent extraction, ion exchange and chemical precipitation [27,28]. Solvent extraction and ion exchange can achieve deep and stable removal of impurity elements, but they also have disadvantages such as high operating costs and strict control requirements. According to the type of sediment, the purification process of chemical precipitation can be divided into various methods, such as hydrolyzation–precipitation [29–31], sulfide precipitation, halide precipitation [32], and double salt precipitation [33]. Pagnanelli et al. [29] used the chemical precipitation to preliminarily remove Cu, Fe, Ni, Mn and Al impurities from the leach liquor of  $\text{LiCoO}_2$  electrode powder. The results showed that iron was fully removed when the pH value increased to 3.8, but other metals were only partially removed. The increasing pH determined the abatement of metal impurities, but simultaneously the loss of Co. Joo et al. [30] achieved effective removal of impurities including Al, Fe and Cu in pre-treated leach liquors of ternary cathode material by precipitation at pH 4.8 adjusted by the addition of 4 M NaOH. Kang et al. [31] removed over 99% Fe, Cu and Al in their hydroxides form by adjusting the pH of leach liquor to 6.5. Weng et al. [32] used  $\text{Na}_2\text{S}$  as a precipitator to effectively remove impurity copper ions in the form of  $\text{CuS}$  precipitation. Although the chemical precipitation method is easy to operate and has a high removal efficiency, it is generally accompanied by the loss of valuable metals. Owing to the complex composition of the leachate and the strict impurity limits for electrode materials, the combined process of chemical precipitation and organic solvent extraction is usually required to achieve deep and stable removal of impurities.

In this paper, sulfuric acid solution commonly used by lithium battery recycling companies is used as the leaching agent to treat spent  $\text{LiFePO}_4$  battery powder, the leachate contains various cations, such as  $\text{Li}^+$ ,  $\text{Fe}^{2+}$ ,  $\text{Fe}^{3+}$ ,  $\text{Al}^{3+}$  and several anions, such as  $\text{F}^-$ ,  $\text{SO}_4^{2-}$ , and  $\text{PO}_4^{3-}$ . In the process of chemical precipitation or solvent extraction to remove aluminum and fluorine, ferric iron ions tend to preferentially enter the separated phase, resulting in the loss of valuable elements and increased reagent consumption. In this study, on the basis of the simultaneous equilibrium principle and mass action law, the co-precipitation thermodynamics of the  $\text{Li}^+ - \text{Fe}^{2+} / \text{Fe}^{3+} - \text{Al}^{3+} - \text{F}^- - \text{SO}_4^{2-} - \text{PO}_4^{3-} - \text{H}_2\text{O}$  system is simulated and calculated to reveal the evolution law of the total equilibrium concentration of Al, F, P, and Fe, and the phase composition of precipitates at different final pH values, aiming to understand the precipitation characteristics. In addition, to validate the feasibility of thermodynamic calculation, trisodium phosphate dodecahydrate was used as neutralizer and ascorbic acid as a reducing agent to control the final pH value of

sulfuric acid leachate within predetermined range in an inert atmosphere and monitor the changes of Al, F, P and Fe contents in the leachate.

## 2. Experimental

### 2.1. Materials

Spent  $\text{LiFePO}_4$  cathode powder was provided by a battery recycling company (Nantong, China), and it was separated from aluminum foils by thermal treatment and screening. The composition of collected spent  $\text{LiFePO}_4$  cathode powder, determined by inductively coupled plasma optical emission spectroscopy (ICP-OES, SPECTROBLUE SOP) after leaching with aqua regia, is shown in Table 1. The sulfuric acid leaching solution is prepared by the leaching reaction of spent  $\text{LiFePO}_4$  cathode powder with 2.5 M  $\text{H}_2\text{SO}_4$  under the conditions of S/L = 1/7, leaching temperature 75 °C, and leaching time of 2 h. Prior to the precipitation, a small amount of reductive iron powder was added to leachate to remove the copper ions by replacement. It should be noted that since reductive iron powder was used to remove the copper ion by replacement, the iron ions in the solution mainly existed in the form of  $\text{Fe}^{2+}$ . The concentrations of metal ions (Fe, Li, Cu, Al, Na, K, Ca, Mg) and non-metal ions (P, S, Si) in the sulfuric acid leachate were examined by ICP-OES. The F content of sulfuric acid leachate was obtained through the fluoride ion selective electrode method. The composition of sulfuric acid leachate is shown in Table 2. Aside from main elements P, Fe, Li, and S, the composition of the solution also contains a small amount of impurity elements such as Al, F, Na, K, Ca, Si and Mg. Ascorbic acid and trisodium phosphate dodecahydrate used in the experiments were of analytical grade. The purity of high-purity argon gas was 99.99%.

**Table 1.** Chemical composition of the spent  $\text{LiFePO}_4$  cathode powder.

Elements	P	Fe	Li	Cu	Al	F
Wt.%	15.9	38.5	3.76	0.5	1.4	0.8

**Table 2.** Chemical composition of the sulfuric acid leachate.

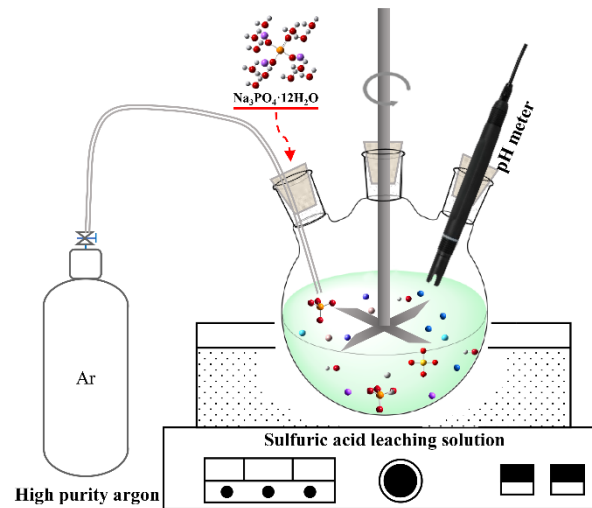
Elements	P	Fe	Li	Cu	Al	F
mg/L	22785.0	56320.0	5365.0	0.5	1999.0	1003.1
Elements	S	Na	K	Ca	Si	Mg
mg/L	84749.0	5.5	6.3	24.2	12.5	9.3

### 2.2. Methods

On the basis of the simultaneous equilibrium principle and mass action law, the co-precipitation thermodynamics of the  $\text{Li}^+ - \text{Fe}^{2+} / \text{Fe}^{3+} - \text{Al}^{3+} - \text{F}^- - \text{SO}_4^{2-} - \text{PO}_4^{3-} - \text{H}_2\text{O}$  system is simulated. The calculation process based on the Newton-Raphson iteration method was carried out by using Microsoft Excel. Owing to the lack of complete data on the activity component in the solution, the molar concentration of each species was used to replace the activity coefficient in the thermodynamic calculation.

The schematic plot of the precipitation experiment set-up is illustrated in Figure 1. In the bench-scale precipitation experiments, 250 mL of the sulfuric acid leachate was poured into a three-necked flask immersed in a water bath at 25 °C. Afterward, 0.5 g of ascorbic acid, a reducing agent, was added to the leachate to reduce ferric ions. Simultaneously, high-purity argon was introduced to prevent the oxidation of ferrous ions.  $\text{Na}_3\text{PO}_4 \cdot 12\text{H}_2\text{O}$  was added to the sulfuric acid leachate in real time to adjust the pH value of the system and keep it constant at a predetermined value. After the predetermined time, the liquid-solid separation of the feed solution was carried out, and then the composition of purified solution was analyzed by ICP-OES and the fluoride ion selective electrode method. The precipitate was vacuum dried at 60 °C for 24 h and then weighed and characterized.

The phase compositions of the precipitation were studied by X-ray diffraction (XRD, Rigaku D/max-2500, Rigaku Corporation, Tokyo, Japan) and Fourier transform infrared spectrometry (FT-IR, Nicolet 6700, Thermo Fisher Scientific, Waltham, USA). The elemental composition and chemical states on the surface of the electrode particles were detected by X-ray photoelectron spectroscopy (XPS, ESCALAB 250Xi, Thermo Fisher Scientific, Waltham, USA).



**Figure 1.** Schematic plot of the precipitation experiments set-up.

The removal rate of  $\text{Al}^{3+}$  and  $\text{F}^-$  as well as the loss rate of  $\text{Fe}$  during the purification process were computed by Equation (1).

$$R_i = \frac{C_{i0} \times V_0 - C_{i1} \times V_1}{C_{i0} \times V_0} \times 100\% \quad (1)$$

where  $R_i$  (%) is the removal rate of  $\text{Al}^{3+}$  and  $\text{F}^-$  as well as the loss rate of  $\text{Fe}^{2+}$ ,  $V_0$  (mL) is the volume of sulfuric acid leachate,  $V_1$  (mL) is the volume of purified solution,  $C_{i0}$  (mg/L) is the concentration of  $\text{Al}^{3+}$ ,  $\text{F}^-$ , and  $\text{Fe}^{2+}$  in the sulfuric acid leachate, and  $C_{i1}$  (mg/L) is the concentration of  $\text{Al}^{3+}$ ,  $\text{F}^-$ , and  $\text{Fe}^{2+}$  in the purified solution.

The loss rate of  $\text{PO}_4^{3-}$  in the purification process was calculated by Equation (2).

$$L_P = \frac{C_{p0} \times V_0 - C_{p1} \times V_1}{C_{p0} \times V_0 + \frac{m_p \times 95}{380}} \times 100\% \quad (2)$$

where  $L_P$  (%) is the loss rate of  $\text{PO}_4^{3-}$ ,  $V_0$  (mL) is the volume of sulfuric acid leachate,  $V_1$  (mL) is the volume of purified solution,  $C_{p0}$  (mg/L) is the concentration of  $\text{PO}_4^{3-}$  in the sulfuric acid leachate,  $C_{p1}$  (mg/L) is the concentration of  $\text{PO}_4^{3-}$  in the purified solution, and  $m_p$  (g) is the  $\text{Na}_3\text{PO}_4 \cdot 12\text{H}_2\text{O}$  dosage.

### 3. Thermodynamic Data and Calculation Model

#### 3.1. Ion Species and Their Thermodynamic Data

In the  $\text{Li}^+ - \text{Fe}^{2+} / \text{Fe}^{3+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system, the main species in the solution were assumed to be  $\text{H}^+$ ,  $\text{OH}^-$ ,  $\text{F}^-$ ,  $\text{PO}_4^{3-}$ ,  $\text{HPO}_4^{2-}$ ,  $\text{H}_2\text{PO}_4^-$ ,  $\text{H}_3\text{PO}_4$ ,  $\text{H}_2\text{SO}_4$ ,  $\text{HSO}_4^-$ ,  $\text{Fe}^{2+}$ ,  $\text{SO}_4^{2-}$ ,  $\text{FeSO}_4(\text{aq})$ ,  $\text{FeOH}^+$ ,  $\text{Fe}(\text{OH})_2(\text{aq})$ ,  $\text{Fe}(\text{OH})_3^-$ ,  $\text{Fe}(\text{OH})_4^{2-}$ ,  $\text{FeHPO}_4(\text{aq})$ ,  $\text{FeH}_2\text{PO}_4^+$ ,  $\text{FeF}^-$ ,  $\text{Fe}^{3+}$ ,  $\text{FeSO}_4^+$ ,  $\text{Fe}(\text{SO}_4)_2^-$ ,  $\text{FeOH}^{2+}$ ,  $\text{Fe}(\text{OH})_2^+$ ,  $\text{Fe}(\text{OH})_4^-$ ,  $\text{Fe}_2(\text{OH})_2^{4+}$ ,  $\text{Fe}_3(\text{OH})_4^{5+}$ ,  $\text{FeHPO}_4^+$ ,  $\text{FeH}_2\text{PO}_4^{2+}$ ,  $\text{FeF}^{2+}$ ,  $\text{FeF}_2^+$ ,  $\text{FeF}_3(\text{aq})$ ,  $\text{Li}^+$ ,  $\text{LiSO}_4^-$ ,  $\text{Li}(\text{OH})(\text{aq})$ ,  $\text{LiHPO}_4^-$ ,  $\text{Al}(\text{OH})_2^+$ ,  $\text{Al}(\text{OH})_2^+$ ,  $\text{Al}(\text{OH})_3(\text{aq})$ ,  $\text{Al}(\text{OH})_4^-$ ,  $\text{Al}_2(\text{OH})_2^{4+}$ ,  $\text{Al}_3(\text{OH})_4^{5+}$ ,  $\text{AlF}^{2+}$ ,  $\text{AlF}_2^+$ ,  $\text{AlF}_3(\text{aq})$ ,  $\text{AlF}_4^-$ ,  $\text{AlF}_5^{2-}$ , and  $\text{AlF}_6^{3-}$ . The reaction equations among these species and their equilibrium constant ( $K$ ) are shown in Table 3.

**Table 3.** Thermodynamic equilibrium equations and their equilibrium constants in the  $\text{Li}^+ - \text{Fe}^{2+} / \text{Fe}^{3+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system (298 K) [34–36].

Equation No.	Reaction	log K	Chemical Equilibrium Constant Relationship
(3)	$\text{H}_2\text{O} = \text{H}^+ + \text{OH}^-$	−14	$[\text{H}_2\text{O}] = [\text{H}^+] \times [\text{OH}^-] \times 10^{14}$
(4)	$\text{H}_3\text{PO}_4 = \text{H}^+ + \text{H}_2\text{PO}_4^-$	−2.04	$[\text{H}_3\text{PO}_4] = [\text{H}^+] \times [\text{H}_2\text{PO}_4^-] \times 10^{2.04}$
(5)	$\text{H}_2\text{PO}_4^- = \text{H}^+ + \text{HPO}_4^{2-}$	−7.2	$[\text{H}_2\text{PO}_4^-] = [\text{H}^+] \times [\text{HPO}_4^{2-}] \times 10^{7.2}$
(6)	$\text{HPO}_4^{2-} = \text{H}^+ + \text{PO}_4^{3-}$	−12.36	$[\text{HPO}_4^{2-}] = [\text{H}^+] \times [\text{PO}_4^{3-}] \times 10^{12.36}$
(7)	$\text{H}_2\text{SO}_4 = \text{HSO}_4^+ + \text{H}^+$	3	$[\text{H}_2\text{SO}_4] = [\text{HSO}_4^+] \times [\text{H}^+] \times 10^{-3}$
(8)	$\text{HSO}_4^+ = \text{SO}_4^{2-} + \text{H}^+$	−1.99	$[\text{HSO}_4^+] = [\text{SO}_4^{2-}] \times [\text{H}^+] \times 10^{1.99}$
(9)	$\text{FeSO}_{4(\text{aq})} = \text{SO}_4^{2-} + \text{Fe}^{2+}$	−2.2	$[\text{FeSO}_{4(\text{aq})}] = [\text{SO}_4^{2-}] \times [\text{Fe}^{2+}] \times 10^{2.2}$
(10)	$\text{FeOH}^+ = \text{Fe}^{2+} + \text{OH}^-$	−4.5	$[\text{FeOH}^+] = [\text{Fe}^{2+}] \times [\text{OH}^-] \times 10^{4.5}$
(11)	$\text{Fe}(\text{OH})_{2(\text{aq})} = \text{Fe}^{2+} + 2\text{OH}^-$	−7.4	$[\text{Fe}(\text{OH})_{2(\text{aq})}] = [\text{Fe}^{2+}] \times [\text{OH}^-]^2 \times 10^{7.4}$
(12)	$\text{Fe}(\text{OH})_3^- = \text{Fe}^{2+} + 3\text{OH}^-$	−10.0	$[\text{Fe}(\text{OH})_3^-] = [\text{Fe}^{2+}] \times [\text{OH}^-]^3 \times 10^{10.0}$
(13)	$\text{Fe}(\text{OH})_4^{2-} = \text{Fe}^{2+} + 4\text{OH}^-$	−9.6	$[\text{Fe}(\text{OH})_4^{2-}] = [\text{Fe}^{2+}] \times [\text{OH}^-]^4 \times 10^{9.6}$
(14)	$\text{FeHPO}_{4(\text{aq})} = \text{Fe}^{2+} + \text{HPO}_4^{2-}$	−3.6	$[\text{FeHPO}_{4(\text{aq})}] = [\text{Fe}^{2+}] \times [\text{HPO}_4^{2-}] \times 10^{3.6}$
(15)	$\text{FeH}_2\text{PO}_4^+ = \text{Fe}^{2+} + \text{H}_2\text{PO}_4^-$	−2.7	$[\text{FeH}_2\text{PO}_4^+] = [\text{Fe}^{2+}] \times [\text{H}_2\text{PO}_4^-] \times 10^{2.7}$
(16)	$\text{FeF}^+ = \text{Fe}^{2+} + \text{F}^-$	−0.8	$[\text{FeF}^+] = [\text{Fe}^{2+}] \times [\text{F}^-] \times 10^{0.8}$
(17)	$\text{FeSO}_4^+ = \text{Fe}^{3+} + \text{SO}_4^{2-}$	−4.04	$[\text{FeSO}_4^+] = [\text{Fe}^{3+}] \times [\text{SO}_4^{2-}] \times 10^{4.04}$
(18)	$\text{Fe}(\text{SO}_4)_2^- = \text{Fe}^{3+} + 2\text{SO}_4^{2-}$	−5.38	$[\text{Fe}(\text{SO}_4)_2^-] = [\text{Fe}^{3+}] \times [\text{SO}_4^{2-}]^2 \times 10^{5.38}$
(19)	$\text{FeOH}^{2+} = \text{Fe}^{3+} + \text{OH}^-$	−11.81	$[\text{FeOH}^{2+}] = [\text{Fe}^{3+}] \times [\text{OH}^-] \times 10^{11.81}$
(20)	$\text{Fe}(\text{OH})_2^+ = \text{Fe}^{3+} + 2\text{OH}^-$	−22.3	$[\text{Fe}(\text{OH})_2^+] = [\text{Fe}^{3+}] \times [\text{OH}^-]^2 \times 10^{22.3}$
(21)	$\text{Fe}(\text{OH})_4^- = \text{Fe}^{3+} + 4\text{OH}^-$	−34.4	$[\text{Fe}(\text{OH})_4^-] = [\text{Fe}^{3+}] \times [\text{OH}^-]^4 \times 10^{34.4}$
(22)	$\text{Fe}_2(\text{OH})_2^{4+} = 2\text{Fe}^{3+} + 2\text{OH}^-$	−25.1	$[\text{Fe}_2(\text{OH})_2^{4+}] = [\text{Fe}^{3+}]^2 \times [\text{OH}^-]^2 \times 10^{25.1}$
(23)	$\text{Fe}_3(\text{OH})_4^{5+} = 3\text{Fe}^{3+} + 4\text{OH}^-$	−49.7	$[\text{Fe}_3(\text{OH})_4^{5+}] = [\text{Fe}^{3+}]^3 \times [\text{OH}^-]^4 \times 10^{49.7}$
(24)	$\text{FeHPO}_4^+ = \text{Fe}^{3+} + \text{HPO}_4^{2-}$	−8.30	$[\text{FeHPO}_4^+] = [\text{Fe}^{3+}] \times [\text{HPO}_4^{2-}] \times 10^{8.30}$
(25)	$\text{FeH}_2\text{PO}_4^{2+} = \text{Fe}^{3+} + \text{H}_2\text{PO}_4^-$	−3.47	$[\text{FeH}_2\text{PO}_4^{2+}] = [\text{Fe}^{3+}] \times [\text{H}_2\text{PO}_4^-] \times 10^{3.47}$
(26)	$\text{FeF}^{2+} = \text{Fe}^{3+} + \text{F}^-$	−6.0	$[\text{FeF}^{2+}] = [\text{Fe}^{3+}] \times [\text{F}^-] \times 10^{6.0}$
(27)	$\text{FeF}_2^+ = \text{Fe}^{3+} + 2\text{F}^-$	−9.07	$[\text{FeF}_2^+] = [\text{Fe}^{3+}] \times [\text{F}^-]^2 \times 10^{9.07}$
(28)	$\text{FeF}_{3(\text{aq})} = \text{Fe}^{3+} + 3\text{F}^-$	−12.1	$[\text{FeF}_{3(\text{aq})}] = [\text{Fe}^{3+}] \times [\text{F}^-]^3 \times 10^{12.1}$
(29)	$\text{Li}(\text{OH})_{(\text{aq})} = \text{Li}^+ + \text{OH}^-$	−0.36	$[\text{Li}(\text{OH})_{(\text{aq})}] = [\text{Li}^+] \times [\text{OH}^-] \times 10^{0.36}$
(30)	$\text{LiSO}_4^- = \text{SO}_4^{2-} + \text{Li}^+$	−0.64	$[\text{LiSO}_4^-] = [\text{SO}_4^{2-}] \times [\text{Li}^+] \times 10^{0.64}$
(31)	$\text{LiHPO}_4^- = \text{Li}^+ + \text{HPO}_4^{2-}$	−0.72	$[\text{LiHPO}_4^-] = [\text{Li}^+] \times [\text{HPO}_4^{2-}] \times 10^{0.72}$
(32)	$\text{Al}(\text{OH})_2^+ = \text{Al}^{3+} + \text{OH}^-$	−9.01	$[\text{Al}(\text{OH})_2^+] = [\text{Al}^{3+}] \times [\text{OH}^-] \times 10^{9.01}$
(33)	$\text{Al}(\text{OH})_2^+ = \text{Al}^{3+} + 2\text{OH}^-$	−18.7	$[\text{Al}(\text{OH})_2^+] = [\text{Al}^{3+}] \times [\text{OH}^-]^2 \times 10^{18.7}$
(34)	$\text{Al}(\text{OH})_{3(\text{aq})} = \text{Al}^{3+} + 3\text{OH}^-$	−27.0	$[\text{Al}(\text{OH})_{3(\text{aq})}] = [\text{Al}^{3+}] \times [\text{OH}^-]^3 \times 10^{27.0}$
(35)	$\text{Al}(\text{OH})_4^- = \text{Al}^{3+} + 4\text{OH}^-$	−33.0	$[\text{Al}(\text{OH})_4^-] = [\text{Al}^{3+}] \times [\text{OH}^-]^4 \times 10^{33.0}$
(36)	$\text{Al}_2(\text{OH})_2^{4+} = 2\text{Al}^{3+} + 2\text{OH}^-$	−20.3	$[\text{Al}_2(\text{OH})_2^{4+}] = [\text{Al}^{3+}]^2 \times [\text{OH}^-]^2 \times 10^{20.3}$
(37)	$\text{Al}_3(\text{OH})_4^{5+} = 3\text{Al}^{3+} + 4\text{OH}^-$	−42.1	$[\text{Al}_3(\text{OH})_4^{5+}] = [\text{Al}^{3+}]^3 \times [\text{OH}^-]^4 \times 10^{42.1}$
(38)	$\text{AlF}^{2+} = \text{Al}^{3+} + \text{F}^-$	−6.09	$[\text{AlF}^{2+}] = [\text{Al}^{3+}] \times [\text{F}^-] \times 10^{6.09}$
(39)	$\text{AlF}_2^+ = \text{Al}^{3+} + 2\text{F}^-$	−11.12	$[\text{AlF}_2^+] = [\text{Al}^{3+}] \times [\text{F}^-]^2 \times 10^{11.12}$
(40)	$\text{AlF}_{3(\text{aq})} = \text{Al}^{3+} + 3\text{F}^-$	−15	$[\text{AlF}_{3(\text{aq})}] = [\text{Al}^{3+}] \times [\text{F}^-]^3 \times 10^{15}$
(41)	$\text{AlF}_4^- = \text{Al}^{3+} + 4\text{F}^-$	−18	$[\text{AlF}_4^-] = [\text{Al}^{3+}] \times [\text{F}^-]^4 \times 10^{18}$
(42)	$\text{AlF}_5^{2-} = \text{Al}^{3+} + 5\text{F}^-$	−19.4	$[\text{AlF}_5^{2-}] = [\text{Al}^{3+}] \times [\text{F}^-]^5 \times 10^{19.4}$
(43)	$\text{AlF}_6^{3-} = \text{Al}^{3+} + 6\text{F}^-$	−19.8	$[\text{AlF}_6^{3-}] = [\text{Al}^{3+}] \times [\text{F}^-]^6 \times 10^{19.8}$

### 3.2. Solid Species and Their Thermodynamic Data

In the  $\text{Li}^+ - \text{Fe}^{2+} / \text{Fe}^{3+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system,  $\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}$ ,  $\text{FePO}_4 \cdot 2\text{H}_2\text{O}$ ,  $\text{Al}(\text{OH})_3$ ,  $\text{AlPO}_4$ ,  $\text{Li}_3\text{PO}_4$ ,  $\text{AlF}_3$ ,  $\text{FeF}_3$ ,  $\text{FeF}_2$ ,  $\text{LiF}$ ,  $\text{Fe}(\text{OH})_2$ , and  $\text{Fe}(\text{OH})_3$  precipitations formed as the pH value and ion concentration in the solution changed. The solubility product constants  $K_{\text{sp}}$  of  $\text{AlF}_3$  and  $\text{FeF}_3$ , as well as their thermodynamic data  $\Delta_f G_i^\theta$  and  $\Delta_f S_i^\theta$ , have not been reported before in the literature. In this paper, the  $K_{\text{sp}}$  value of  $\text{AlF}_3$  and  $\text{FeF}_3$  was estimated according to their solubility and the equilibrium model of gradual dissociation.



### 3.2.1. Calculation of $K_{sp}$ Value of $AlF_3$

Assuming that a certain amount of  $AlF_3$  was added to deionized water, when  $AlF_3$  reached dissolution equilibrium, the main species in the solution and their equilibrium equations can be shown in Equations (38)–(43) in Table 2.

According to the simultaneous equilibrium principle and mass action law, the mass balance equations of F and Al are given as follows:

$$[F]_T = [F^-] + [AlF^{2+}] + 2[AlF_2^+] + 3[AlF_3] + 4[AlF_4^-] + 5[AlF_5^{2-}] + 6[AlF_6^{3-}] \quad (44)$$

$$[Al]_T = [Al^{3+}] + [AlF^{2+}] + [AlF_2^+] + [AlF_3] + [AlF_4^-] + [AlF_5^{2-}] + [AlF_6^{3-}] \quad (45)$$

where  $[F]_T$  and  $[Al]_T$  are designated as the total concentration of F and Al in equilibrium conditions;  $[Al^{3+}]$ ,  $[F^-]$ ,  $[AlF^{2+}]$ ,  $[AlF_2^+]$ ,  $[AlF_3]$ ,  $[AlF_4^-]$ ,  $[AlF_5^{2-}]$ , and  $[AlF_6^{3-}]$  are defined as the equilibrium concentration for each species in equilibrium conditions.

The chemical equilibrium constant relationship of Equations (38)–(43) in Table 1 is substituted into Equations (44) and (45) to obtain Equations (46) and (47).

$$[F]_T = [F^-] + [Al^{3+}] \times [F^-] \times 10^{6.09} + 2([Al^{3+}] \times [F^-]^2 \times 10^{11.12}) + 3([Al^{3+}] \times [F^-]^3 \times 10^{15}) + 4([Al^{3+}] \times [F^-]^4 \times 10^{18}) + 5([Al^{3+}] \times [F^-]^5 \times 10^{19.4}) + 6([Al^{3+}] \times [F^-]^6 \times 10^{19.8}) \quad (46)$$

$$[Al]_T = [Al^{3+}] + [Al^{3+}] \times [F^-] \times 10^{6.09} + [Al^{3+}] \times [F^-]^2 \times 10^{11.12} + [Al^{3+}] \times [F^-]^3 \times 10^{15} + [Al^{3+}] \times [F^-]^4 \times 10^{18} + [Al^{3+}] \times [F^-]^5 \times 10^{19.4} + [Al^{3+}] \times [F^-]^6 \times 10^{19.8} \quad (47)$$

According to the literature, the solubility of  $AlF_3$  is 0.67 g/100 mL of water at 20 °C [34]. Below this temperature, when  $AlF_3$  reached dissolution equilibrium, the  $[F]_T$  and  $[Al]_T$  values would be 0.239352 and 0.079784 mol/L, respectively. Combined with Equations (46) and (47), the  $[F^-]$  and  $[Al^{3+}]$  values were  $3.965 \times 10^{-4}$  mol/L and  $9.43 \times 10^{-7}$  mol/L when  $AlF_3$  reached dissolution equilibrium.

The  $K_{sp}$  definition of  $AlF_3(s)$  is shown in Equation (48). The  $K_{sp}$  value of  $AlF_3(s)$  was calculated to be  $4.53 \times 10^{-17}$ .

$$K_{sp} = [F^-]^3 \times [Al^{3+}] \quad (48)$$

### 3.2.2. Calculation of $K_{sp}$ Value of $FeF_3$

Given that a certain amount of  $FeF_3$  was added to deionized water, when  $FeF_3$  reached dissolution equilibrium, the main species in the solution and their equilibrium equations can be shown in Equations (26)–(28) in Table 2.

On the basis of the simultaneous equilibrium principle and mass action law, the mass balance equations of F and Fe are given as follows:

$$[F]_T = [F^-] + [FeF^{2+}] + 2[FeF_2^+] + 3[FeF_3] \quad (49)$$

$$[Fe]_T = [Fe^{3+}] + [FeF^{2+}] + [FeF_2^+] + [FeF_3] \quad (50)$$

where  $[F]_T$  and  $[Fe]_T$  are designated as the total concentration of F and Fe in equilibrium conditions;  $[Fe^{3+}]$ ,  $[F^-]$ ,  $[FeF^{2+}]$ ,  $[FeF_2^+]$ , and  $[FeF_3]$  are defined as the equilibrium concentration for each species in equilibrium conditions.

The chemical equilibrium constant relationship of Equations (26)–(28) in Table 2 is substituted into Equations (49) and (50) to obtain Equations (51) and (52).

$$[F]_T = [F^-] + ([Fe^{3+}] \times [F^-] \times 10^{6.0}) + 2([Fe^{3+}] \times [F^-]^2 \times 10^{9.07}) + 3([Fe^{3+}] \times [F^-]^3 \times 10^{12.1}) \quad (51)$$

$$[Fe]_T = [Fe^{3+}] + [Fe^{3+}] \times [F^-] \times 10^{6.0} + [Fe^{3+}] \times [F^-]^2 \times 10^{9.07} + [Fe^{3+}] \times [F^-]^3 \times 10^{12.1} \quad (52)$$

According to the literature, the solubility of  $FeF_3$  is 0.091 g at 20 °C/100 mL of water [34]. In this case, when  $FeF_3$  reached dissolution equilibrium, the  $[F]_T$  and  $[Fe]_T$  values would be 0.024193503 and 0.008064501 mol/L, respectively. From Equations (51) and (52), the  $[F^-]$  and  $[Fe^{3+}]$  values were  $7.52 \times 10^{-6}$  mol/L and  $8.51 \times 10^{-10}$  mol/L when  $FeF_3$  reached dissolution equilibrium.

The  $K_{sp}$  definition of  $\text{FeF}_3(\text{s})$  is presented in Equation (53). The  $K_{sp}$  value of  $\text{FeF}_3(\text{s})$  was calculated to be  $3.623 \times 10^{-25}$ .

$$K_{sp} = [\text{F}^-]^3 \times [\text{Fe}^{3+}] \quad (53)$$

### 3.2.3. Solid-State Reactions and Their Equilibrium Constant

The possible solid-state reactions among the species in the  $\text{Li}^+ - \text{Fe}^{2+} / \text{Fe}^{3+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system and their corresponding equilibrium constants are listed in Table 4.

**Table 4.** Solid-state reactions and their equilibrium constant of  $\text{Li}^+ - \text{Fe}^{2+} / \text{Fe}^{3+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system (298 K) [34–36].

Equation No.	Reaction	log K	Chemical Equilibrium Constant Relationship
(54)	$\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}(\text{s}) = 3\text{Fe}^{2+} + 2\text{PO}_4^{3-} + 8\text{H}_2\text{O}$	−36.85	$[\text{Fe}^{2+}]^3 \times [\text{PO}_4^{3-}]^2 = 10^{-36.85}$
(55)	$\text{FePO}_4 \cdot 2\text{H}_2\text{O}(\text{s}) = \text{Fe}^{3+} + \text{PO}_4^{3-} + 2\text{H}_2\text{O}$	−15.0039	$[\text{Fe}^{3+}] \times [\text{PO}_4^{3-}] = 10^{-15.0039}$
(56)	$\text{FePO}_4(\text{s}) = \text{Fe}^{3+} + \text{PO}_4^{3-}$	−21.886	$[\text{Fe}^{3+}] \times [\text{PO}_4^{3-}] = 10^{-21.886}$
(57)	$\text{Al}(\text{OH})_3 = \text{Al}^{3+} + 3\text{OH}^-$	−32.89	$[\text{Al}^{3+}] \times [\text{OH}^-]^3 = 10^{-32.89}$
(58)	$\text{AlPO}_4(\text{s}) = \text{Al}^{3+} + \text{PO}_4^{3-}$	−20.007	$[\text{Al}^{3+}] \times [\text{PO}_4^{3-}] = 10^{-20.007}$
(59)	$\text{Li}_3\text{PO}_4(\text{s}) = 3\text{Li}^+ + \text{PO}_4^{3-}$	−10.6253	$[\text{Li}^+]^3 \times [\text{PO}_4^{3-}] = 10^{-10.6253}$
(60)	$\text{AlF}_3(\text{s}) = \text{Al}^{3+} + 3\text{F}^-$	−16.3439	$[\text{Al}^{3+}] \times [\text{F}^-]^3 = 10^{-16.3439}$
(61)	$\text{FeF}_3(\text{s}) = \text{Fe}^{3+} + 3\text{F}^-$	−24.4409	$[\text{Fe}^{3+}] \times [\text{F}^-]^3 = 10^{-24.4409}$
(62)	$\text{FeF}_2(\text{s}) = \text{Fe}^{2+} + 2\text{F}^-$	−5.62709	$[\text{Fe}^{2+}] \times [\text{F}^-]^2 = 10^{-5.62709}$
(63)	$\text{LiF}(\text{s}) = \text{Li}^+ + \text{F}^-$	−2.77	$[\text{Li}^+] \times [\text{F}^-] = 10^{-2.77}$
(64)	$\text{Fe}(\text{OH})_2(\text{s}) = \text{Fe}^{2+} + 2\text{OH}^-$	−16.31	$[\text{Fe}^{2+}] \times [\text{OH}^-]^2 = 10^{-16.31}$
(65)	$\text{Fe}(\text{OH})_3(\text{s}) = \text{Fe}^{3+} + 3\text{OH}^-$	−38.8	$[\text{Fe}^{3+}] \times [\text{OH}^-]^3 = 10^{-38.8}$

### 3.3. Thermodynamic Model of the $\text{Li}^+ - \text{Fe}^{2+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$ System

The soluble species in the  $\text{Li}^+ - \text{Fe}^{2+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system and their equilibrium equations are shown in Equations (3)–(16) and (29)–(43) in Table 2, respectively. Via the simultaneous equilibrium principle, mass action law, and electroneutrality principle, Equations (66)–(72) were obtained.

$$[\text{P}]_{\text{T}} = [\text{PO}_4^{3-}] + [\text{HPO}_4^{2-}] + [\text{H}_2\text{PO}_4^-] + [\text{H}_3\text{PO}_4] + [\text{LiHPO}_4^-] + [\text{FeHPO}_4(\text{aq})] + [\text{FeH}_2\text{PO}_4^+] \quad (66)$$

$$[\text{Fe(II)}]_{\text{T}} = [\text{Fe}^{2+}] + [\text{FeSO}_4(\text{aq})] + [\text{FeOH}^+] + [\text{Fe}(\text{OH})_2(\text{aq})] + [\text{Fe}(\text{OH})_3^-] + [\text{Fe}(\text{OH})_4^{2-}] + [\text{FeHPO}_4(\text{aq})] + [\text{FeH}_2\text{PO}_4^+] + [\text{FeF}^+] \quad (67)$$

$$[\text{Li}]_{\text{T}} = [\text{Li}^+] + [\text{Li}(\text{OH})_{(\text{aq})}] + [\text{LiSO}_4^-] + [\text{LiHPO}_4^-] \quad (68)$$

$$[\text{S}]_{\text{T}} = [\text{SO}_4^{2-}] + [\text{H}_2\text{SO}_4] + [\text{HSO}_4^-] + [\text{FeSO}_4(\text{aq})] + [\text{LiSO}_4^-] \quad (69)$$

$$[\text{Al}]_{\text{T}} = [\text{Al}^{3+}] + [\text{AlF}^{2+}] + [\text{AlF}_2^+] + [\text{AlF}_3(\text{aq})] + [\text{AlF}_4^-] + [\text{AlF}_5^{2-}] + [\text{AlF}_6^{3-}] + [\text{Al}(\text{OH})^{2+}] + [\text{Al}(\text{OH})_2^+] + [\text{Al}(\text{OH})_3(\text{aq})] + [\text{Al}(\text{OH})_4^-] + 2[\text{Al}_2(\text{OH})_2^{4+}] + 3[\text{Al}_3(\text{OH})_4^{5+}] \quad (70)$$

$$[\text{F}]_{\text{T}} = [\text{F}^-] + [\text{AlF}^{2+}] + 2[\text{AlF}_2^+] + 3[\text{AlF}_3(\text{aq})] + 4[\text{AlF}_4^-] + 5[\text{AlF}_5^{2-}] + 6[\text{AlF}_6^{3-}] + [\text{FeF}^+] \quad (71)$$

$$2[\text{Fe}^{2+}] + [\text{FeOH}^+] + [\text{FeH}_2\text{PO}_4^+] + [\text{Li}^+] + 3[\text{Al}^{3+}] + 2[\text{Al}(\text{OH})^{2+}] + [\text{Al}(\text{OH})_2^+] + 4[\text{Al}_2(\text{OH})_2^{4+}] + 5[\text{Al}_3(\text{OH})_4^{5+}] + 2[\text{AlF}^{2+}] + [\text{AlF}_2^+] + [\text{FeF}^+] + [\text{H}^+] = [\text{Fe}(\text{OH})_3^-] + 2[\text{Fe}(\text{OH})_4^{2-}] + [\text{H}_2\text{PO}_4^-] + 2[\text{HPO}_4^{2-}] + 3[\text{PO}_4^{3-}] + [\text{LiHPO}_4^-] + [\text{LiSO}_4^-] + [\text{Al}(\text{OH})_4^-] + [\text{F}^-] + [\text{AlF}_4^-] + 2[\text{AlF}_5^{2-}] + 3[\text{AlF}_6^{3-}] + 2[\text{SO}_4^{2-}] + [\text{HSO}_4^-] + [\text{OH}^-] \quad (72)$$

When a solid phase is formed in the system, each component in the solid phase stable region must satisfy not only Equations (3)–(16), (29)–(43), and (66)–(72) but also their corresponding constraint equations. The constraint equations for different solid phase stable regions are provided in Table 5.

**Table 5.** Constraint equations for different solid phase stable region.

Eq no.	Equation
(73)	$([\text{Fe(II)}]_{\text{O}} - [\text{Fe(II)}]_{\text{T}}) / ([\text{F}]_{\text{O}} - [\text{F}]_{\text{T}}) = 3/2$
(74)	$[\text{Fe}^{2+}]^3 \times [\text{PO}_4^{3-}]^2 = 10^{-36.85}$
(75)	$[\text{Al}]_{\text{O}} - [\text{Al}]_{\text{T}} = [\text{P}]_{\text{O}} - [\text{P}]_{\text{T}}$
(76)	$[\text{Al}^{3+}] \times [\text{PO}_4^{3-}] = 9.84 \times 10^{-21}$
(77)	$([\text{Al}]_{\text{O}} - [\text{Al}]_{\text{T}}) / ([\text{F}]_{\text{O}} - [\text{F}]_{\text{T}}) = 1/3$
(78)	$[\text{Al}^{3+}] \times [\text{F}^-]^3 = 4.53 \times 10^{-17}$
(79)	$[(\text{P}]_{\text{O}} - [\text{P}]_{\text{T}}) - ([\text{Al}]_{\text{O}} - [\text{Al}]_{\text{T}}) / ([\text{Fe(II)}]_{\text{O}} - [\text{Fe(II)}]_{\text{T}}) = 2/3$
(80)	$[(\text{Al}]_{\text{O}} - [\text{Al}]_{\text{T}}) - ([\text{P}]_{\text{O}} - [\text{P}]_{\text{T}}) / ([\text{Fe(II)}]_{\text{O}} - [\text{Fe(II)}]_{\text{T}}) = 1/3$

Where [M] is the equilibrium concentration for each species;  $[\text{P}]_{\text{T}}$ ,  $[\text{Fe(II)}]_{\text{T}}$ ,  $[\text{Li}]_{\text{T}}$ ,  $[\text{S}]_{\text{T}}$ ,  $[\text{Al}]_{\text{T}}$ , and  $[\text{F}]_{\text{T}}$  are designated as the total concentration of phosphate, Fe, Li, sulfate, Al, and F in equilibrium conditions;  $[\text{P}]_{\text{O}}$ ,  $[\text{Fe(II)}]_{\text{O}}$ ,  $[\text{Li}]_{\text{O}}$ ,  $[\text{S}]_{\text{O}}$ ,  $[\text{Al}]_{\text{O}}$ , and  $[\text{F}]_{\text{O}}$  are defined as the initial total concentrations of phosphate, Fe, Li, sulfate, Al, and F before the precipitation of solid phases.

The possible stable regions of the  $\text{Li}^+ - \text{Fe}^{2+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system and their corresponding constraint equations are given in Table 6. By assigning values to  $[\text{P}]_{\text{O}}$ ,  $[\text{Fe(II)}]_{\text{O}}$ ,  $[\text{Li}]_{\text{O}}$ ,  $[\text{S}]_{\text{O}}$ ,  $[\text{Al}]_{\text{O}}$ , and  $[\text{F}]_{\text{O}}$ , the equations were solved using Microsoft Excel in accordance with the Newton-Raphson iteration method. In addition, the most thermodynamically stable region among all those possible corresponded to the lowest  $[\text{Al}]_{\text{T}}$  and  $[\text{F}]_{\text{T}}$  at a given pH value.

**Table 6.** Possible stable regions of  $\text{Li}^+ - \text{Fe}^{2+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system and their corresponding constraint equations.

No.	Stable Regions	Constraint Equations
1	Liquid phase	(3 16) + (29 43) + (66 72)
2	$\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}_{(\text{s})}$	(3 16) + (29 43) + (66 74)
3	$\text{AlPO}_4_{(\text{s})}$	(3 16) + (29 43) + (66 72) + (75 76)
4	$\text{AlF}_3_{(\text{s})}$	(3 16) + (29 43) + (66 72) + (77 78)
5	$\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}_{(\text{s})} + \text{AlPO}_4_{(\text{s})}$	(3 16) + (29 43) + (66 72) + (74) + (76) + (79)
6	$\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}_{(\text{s})} + \text{AlF}_3_{(\text{s})}$	(3 16) + (29 43) + (66 74) + (77 78)
7	$\text{AlPO}_4_{(\text{s})} + \text{AlF}_3_{(\text{s})}$	(3 16) + (29 43) + (66 72) + (76) + (78) + (80)
8	$\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}_{(\text{s})} + \text{AlPO}_4_{(\text{s})} + \text{AlF}_3_{(\text{s})}$	(3 16) + (29 43) + (66 72) + (74) + (76) + (78 79) + (80)

### 3.4. Thermodynamic Model of the $\text{Li}^+ - \text{Fe}^{3+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$ System

The species in the solution of the  $\text{Li}^+ - \text{Fe}^{3+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system and their equilibrium equations are shown in Equations (3)–(8) and (17)–(43) in Table 1, respectively. In accordance with the simultaneous equilibrium principle, mass action law, and electroneutrality principle, Equations (81)–(87) were obtained.

$$[\text{P}]_{\text{T}} = [\text{PO}_4^{3-}] + [\text{HPO}_4^{2-}] + [\text{H}_2\text{PO}_4^-] + [\text{H}_3\text{PO}_4] + [\text{LiHPO}_4^-] + [\text{FeHPO}_4^+] + [\text{FeH}_2\text{PO}_4^{2+}] \quad (81)$$

$$[\text{Fe(III)}]_{\text{T}} = [\text{Fe}^{3+}] + [\text{FeOH}^{2+}] + [\text{Fe(OH)}_2^+] + [\text{Fe(OH)}_4^-] + 2[\text{Fe}_2(\text{OH})_2^{4-}] + 3[\text{Fe}_3(\text{OH})_4^{5-}] + [\text{FeHPO}_4^+] + [\text{FeH}_2\text{PO}_4^{2+}] + [\text{FeF}^{2+}] + [\text{FeF}_2^+] + [\text{FeF}_3_{(\text{aq})}] + [\text{FeSO}_4^+] + [\text{Fe(SO}_4)_2^-] \quad (82)$$

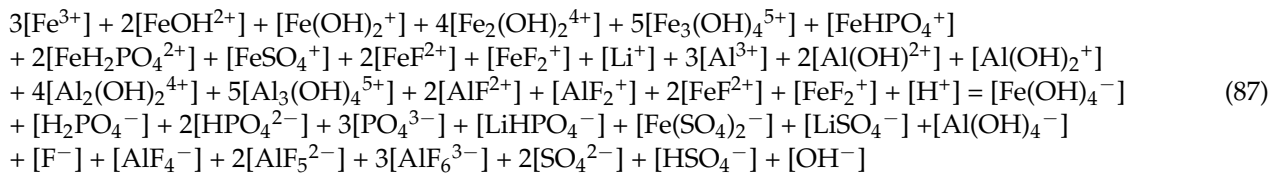
$$[\text{Li}]_{\text{T}} = [\text{Li}^+] + [\text{Li(OH)}_{(\text{aq})}] + [\text{LiSO}_4^-] + [\text{LiHPO}_4^-] \quad (83)$$

$$[\text{S}]_{\text{T}} = [\text{SO}_4^{2-}] + [\text{H}_2\text{SO}_4] + [\text{HSO}_4^-] + [\text{FeSO}_4^+] + 2[\text{Li(SO}_4)_2^-] + [\text{LiSO}_4^-] \quad (84)$$

$$[\text{Al}]_{\text{T}} = [\text{Al}^{3+}] + [\text{AlF}^{2+}] + [\text{AlF}_2^+] + [\text{AlF}_3_{(\text{aq})}] + [\text{AlF}_4^-] + [\text{AlF}_5^{2-}] + [\text{AlF}_6^{3-}] + [\text{Al(OH)}^{2+}] + [\text{Al(OH)}_2^+] + [\text{Al(OH)}_3_{(\text{aq})}] + [\text{Al(OH)}_4^-] + 2[\text{Al}_2(\text{OH})_2^{4+}] + 3[\text{Al}_3(\text{OH})_4^{5+}] \quad (85)$$

$$[\text{F}]_{\text{T}} = [\text{F}^-] + [\text{AlF}^{2+}] + 2[\text{AlF}_2^+] + 3[\text{AlF}_3_{(\text{aq})}] + 4[\text{AlF}_4^-] + 5[\text{AlF}_5^{2-}] + 6[\text{AlF}_6^{3-}] + [\text{FeF}^+] \quad (86)$$





When a solid phase is formed in the system, each component in the solid phase stable region must meet Equations (3)–(8), (17)–(43), and (81)–(87), as well as their corresponding constraint equations. The constraint equations for different solid phase stable regions are given in Table 7.

**Table 7.** Constraint equations for different solid phase stable region.

Eq No	Equation
(88)	$[\text{Fe(III)}]_{\text{O}} - [\text{Fe(III)}]_{\text{T}} = [\text{P}]_{\text{O}} - [\text{P}]_{\text{T}}$
(89)	$[\text{Fe}^{3+}] \times [\text{PO}_4^{3-}] = 1.3 \times 10^{-22}$
(90)	$[\text{Al}]_{\text{O}} - [\text{Al}]_{\text{T}} = [\text{P}]_{\text{O}} - [\text{P}]_{\text{T}}$
(91)	$[\text{Al}^{3+}] \times [\text{PO}_4^{3-}] = 9.84 \times 10^{-21}$
(92)	$([\text{Fe(III)}]_{\text{O}} - [\text{Fe(III)}]_{\text{T}}) / ([\text{F}]_{\text{O}} - [\text{F}]_{\text{T}}) = 1/3$
(93)	$[\text{Fe}^{3+}] \times [\text{F}^-]^3 = 1.089 \times 10^{-36}$
(94)	$[\text{Fe}^{3+}] \times [\text{OH}^-]^3 = 10^{-38.8}$
(95)	$([\text{P}]_{\text{O}} - [\text{P}]_{\text{T}}) / ([\text{Fe(III)}]_{\text{O}} - [\text{Fe(III)}]_{\text{T}}) + ([\text{Al}]_{\text{O}} - [\text{Al}]_{\text{T}}) = 1$
(96)	$([\text{Fe(III)}]_{\text{O}} - [\text{Fe(III)}]_{\text{T}}) / ([\text{P}]_{\text{O}} - [\text{P}]_{\text{T}}) + ([\text{F}]_{\text{O}} - [\text{F}]_{\text{T}}) = 1$

Where [M] is the equilibrium concentration for each species;  $[\text{P}]_{\text{T}}$ ,  $[\text{Fe(III)}]_{\text{T}}$ ,  $[\text{Li}]_{\text{T}}$ ,  $[\text{S}]_{\text{T}}$ ,  $[\text{Al}]_{\text{T}}$ , and  $[\text{F}]_{\text{T}}$  are designated as the total concentration of phosphate, Fe, Li, sulfate, Al, and F in equilibrium conditions;  $[\text{P}]_{\text{O}}$ ,  $[\text{Fe(III)}]_{\text{O}}$ ,  $[\text{Li}]_{\text{O}}$ ,  $[\text{S}]_{\text{O}}$ ,  $[\text{Al}]_{\text{O}}$ , and  $[\text{F}]_{\text{O}}$  are defined as the initial total concentrations of phosphate, Fe, Li, sulfate, Al, and F before the precipitation of solid phases.

The possible stable regions of the  $\text{Li}^+ - \text{Fe}^{3+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system and their corresponding constraint equations are presented in Table 8. The equations were solved using Microsoft Excel by assigning values to  $[\text{P}]_{\text{O}}$ ,  $[\text{Fe(III)}]_{\text{O}}$ ,  $[\text{Li}]_{\text{O}}$ ,  $[\text{S}]_{\text{O}}$ ,  $[\text{Al}]_{\text{O}}$ , and  $[\text{F}]_{\text{O}}$  on the basis of the Newton-Raphson iteration method. Moreover, the most thermodynamically stable region among all possible ones corresponded to the lowest  $[\text{Al}]_{\text{T}}$  and  $[\text{F}]_{\text{T}}$  at a given pH value.

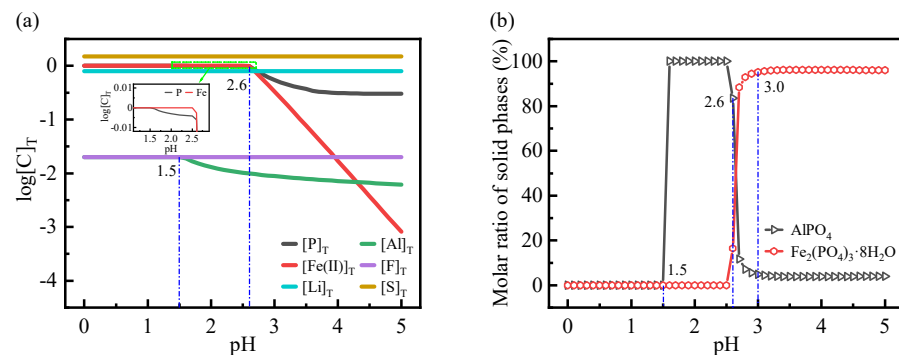
**Table 8.** Possible stable regions of  $\text{Li}^+ - \text{Fe}^{3+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system and their corresponding constraint equations.

No.	Stable Regions	Constraint Equations
1	Liquid phase	(3 8) + (17 43) + (81 87)
2	$\text{FePO}_4(\text{s})$	(3 8) + (17 43) + (81 87)
3	$\text{AlPO}_4(\text{s})$	(3 8) + (17 43) + (81 87) + (90 91)
4	$\text{FeF}_3(\text{s})$	(3 8) + (17 43) + (81–87) + (92–93)
5	$\text{Fe}(\text{OH})_3(\text{s})$	(3 8) + (17–43) + (81–87) + (94)
6	$\text{FePO}_4(\text{s}) + \text{AlPO}_4(\text{s})$	(3 8) + (17 43) + (81 87) + (89) + (91) + (95)
7	$\text{FePO}_4(\text{s}) + \text{FeF}_3(\text{s})$	(3 8) + (17 43) + (81 87) + (89) + (93) + (96)
8	$\text{FePO}_4(\text{s}) + \text{Fe}(\text{OH})_3(\text{s})$	(3 8) + (17 43) + (81–87) + (89) + (94)
9	$\text{AlPO}_4(\text{s}) + \text{FeF}_3(\text{s})$	(3 8) + (17–43) + (81 87) + (90 93)
10	$\text{AlPO}_4(\text{s}) + \text{Fe}(\text{OH})_3(\text{s})$	(3 8) + (17 43) + (81 87) + (90 91) + (94)
11	$\text{FeF}_3(\text{s}) + \text{Fe}(\text{OH})_3(\text{s})$	(3 8) + (17 43) + (81 87) + (93 94)
12	$\text{FePO}_4(\text{s}) + \text{AlPO}_4(\text{s}) + \text{FeF}_3(\text{s})$	(3 8) + (17 43) + (81 87) + (89) + (91) + (93) + (95) + (96)
13	$\text{FePO}_4(\text{s}) + \text{AlPO}_4(\text{s}) + \text{Fe}(\text{OH})_3(\text{s})$	(3 8) + (17 43) + (81 87) + (89) + (91) + (94)
14	$\text{AlPO}_4(\text{s}) + \text{FeF}_3(\text{s}) + \text{Fe}(\text{OH})_3(\text{s})$	(3 8) + (17 43) + (81 87) + (90 91) + (93 94)
15	$\text{FePO}_4(\text{s}) + \text{FeF}_3(\text{s}) + \text{Fe}(\text{OH})_3(\text{s})$	(3 8) + (17 43) + (81 87) + (89) + (93 94)
16	$\text{FePO}_4(\text{s}) + \text{AlPO}_4(\text{s}) + \text{FeF}_3(\text{s}) + \text{Fe}(\text{OH})_3(\text{s})$	(3 8) + (17 43) + (81 87) + (89) + (91) + (93 94)

#### 4. Results and Discussion

##### 4.1. $\text{Li}^+-\text{Fe}^{2+}-\text{Al}^{3+}-\text{PO}_4^{3-}-\text{SO}_4^{2-}-\text{F}^--\text{H}_2\text{O}$ System

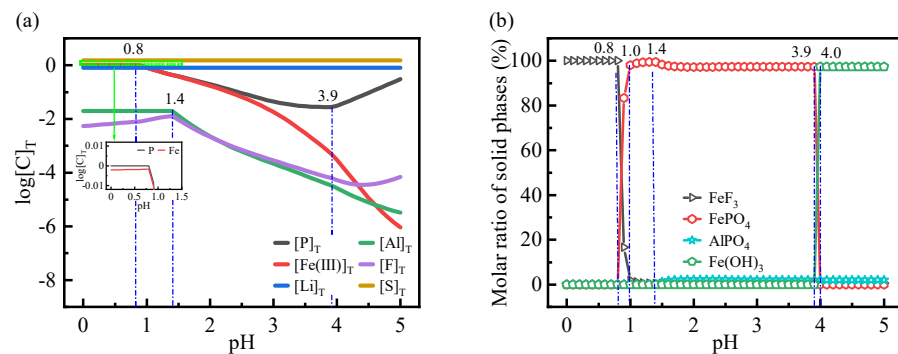
Figure 2 shows the element equilibrium total concentration and the solid phases distribution of the  $\text{Li}^+-\text{Fe}^{2+}-\text{Al}^{3+}-\text{PO}_4^{3-}-\text{SO}_4^{2-}-\text{F}^--\text{H}_2\text{O}$  system at the initial concentration of 1 M  $[\text{P}]_0$ , 1 M  $[\text{Fe}]_0$ , 0.8 M  $[\text{Li}]_0$ , 1.5 M  $[\text{S}]_0$ , 0.02 M  $[\text{Al}]_0$ , and 0.02 M  $[\text{F}]_0$ . At  $\text{pH} < 1.5$ , the total concentration of each element in the solution remained constant and no precipitation was generated. At  $1.5 \leq \text{pH} \leq 2.6$ , the total concentration of aluminum ions and phosphate ions decreased because the reaction of aluminum ions and phosphate ions formed  $\text{AlPO}_4$  precipitate (Figure 2b).  $\text{AlPO}_4$  was the main precipitate at  $\text{pH} = 1.5\text{--}2.6$ . At  $\text{pH} \geq 2.6$ , the total concentration of iron ions decreased and that of phosphate ions decreased more sharply because the reaction of ferric ions and phosphate ions formed  $\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}$  precipitate. Accordingly, the precipitates generated in the solution included  $\text{AlPO}_4$  and  $\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}$  when the pH value was above 2.5, and the molar proportion of  $\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}$  increased as the final pH value increased. At  $\text{pH} \geq 3.0$ , the molar proportion of  $\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}$  and  $\text{AlPO}_4$  remained stable, and  $\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}$  was the main precipitate,  $\text{AlPO}_4$  was the minor precipitate.



**Figure 2.** (a) Elements equilibrium total concentration and (b) solid phases distribution of the  $\text{Li}^+-\text{Fe}^{2+}-\text{Al}^{3+}-\text{PO}_4^{3-}-\text{SO}_4^{2-}-\text{F}^--\text{H}_2\text{O}$  system (298 K,  $[\text{P}]_0 = [\text{Fe(II)}]_0 = 1$  M,  $[\text{Li}]_0 = 0.8$  M,  $[\text{S}]_0 = 1.5$  M,  $[\text{Al}]_0 = [\text{F}]_0 = 0.02$  M).

##### 4.2. $\text{Li}^+-\text{Fe}^{3+}-\text{Al}^{3+}-\text{PO}_4^{3-}-\text{SO}_4^{2-}-\text{F}^--\text{H}_2\text{O}$ System

Figure 3 presents the element equilibrium total concentration and the solid phases distribution of the  $\text{Li}^+-\text{Fe}^{3+}-\text{Al}^{3+}-\text{PO}_4^{3-}-\text{SO}_4^{2-}-\text{F}^--\text{H}_2\text{O}$  system at the initial concentration of 1 M  $[\text{P}]_0$ , 1 M  $[\text{Fe}]_0$ , 0.8 M  $[\text{Li}]_0$ , 1.5 M  $[\text{S}]_0$ , 0.02 M  $[\text{Al}]_0$ , and 0.02 M  $[\text{F}]_0$ . At  $\text{pH} = 0$ , the total concentration of iron and fluoride ions was lower than the initial value, indicating that the formation of  $\text{FeF}_3$  precipitate in the  $\text{Li}^+-\text{Fe}^{3+}-\text{Al}^{3+}-\text{PO}_4^{3-}-\text{SO}_4^{2-}-\text{F}^--\text{H}_2\text{O}$  system decreased the total concentration of ferric ions and fluorine ions (Figure 3b).  $\text{FeF}_3$  was the only precipitate at  $\text{pH} \leq 0.8$ . At  $\text{pH} = 0\text{--}1.4$ , the total concentration of fluoride ion continuously increased, suggesting that the increase in pH value within the range was not conducive to the formation of  $\text{FeF}_3$ . At  $\text{pH} \geq 0.8$ , the total concentration of phosphate ions and iron ions substantially decreased because of the formation of  $\text{FePO}_4$ . At  $\text{pH} \geq 1.4$ , the total concentration of aluminum ions began to decrease owing to the formation of  $\text{AlPO}_4$ , whereas the concentration of fluoride ions also began to decrease because of the formation of  $\text{FeF}_3$ . At  $\text{pH} = 1.0\text{--}3.9$ ,  $\text{FePO}_4$  was the main precipitate,  $\text{FeF}_3$  and  $\text{AlPO}_4$  were the minor precipitate. At  $\text{pH} \geq 3.9$ , the total concentration of phosphate ions started to increase, because of the disappearance of  $\text{FePO}_4$  and the mass formation of  $\text{Fe}(\text{OH})_3$  with the increase in concentration of hydroxide ions. At  $\text{pH} \geq 4.0$ , the molar proportion of  $\text{FeF}_3$ ,  $\text{AlPO}_4$ , and  $\text{Fe}(\text{OH})_3$  precipitate remained stable, and  $\text{Fe}(\text{OH})_3$  was the main precipitate,  $\text{FeF}_3$  and  $\text{AlPO}_4$  was the minor precipitate.



**Figure 3.** (a) Elements equilibrium total concentration and (b) solid phases distribution of the  $\text{Li}^+ - \text{Fe}^{3+} - \text{Al}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{F}^- - \text{H}_2\text{O}$  system (298 K,  $[\text{P}]_0 = [\text{Fe(III)}]_0 = 1 \text{ M}$ ,  $[\text{Li}]_0 = 0.8 \text{ M}$ ,  $[\text{S}]_0 = 1.5 \text{ M}$ ,  $[\text{Al}]_0 = [\text{F}]_0 = 0.02 \text{ M}$ ).

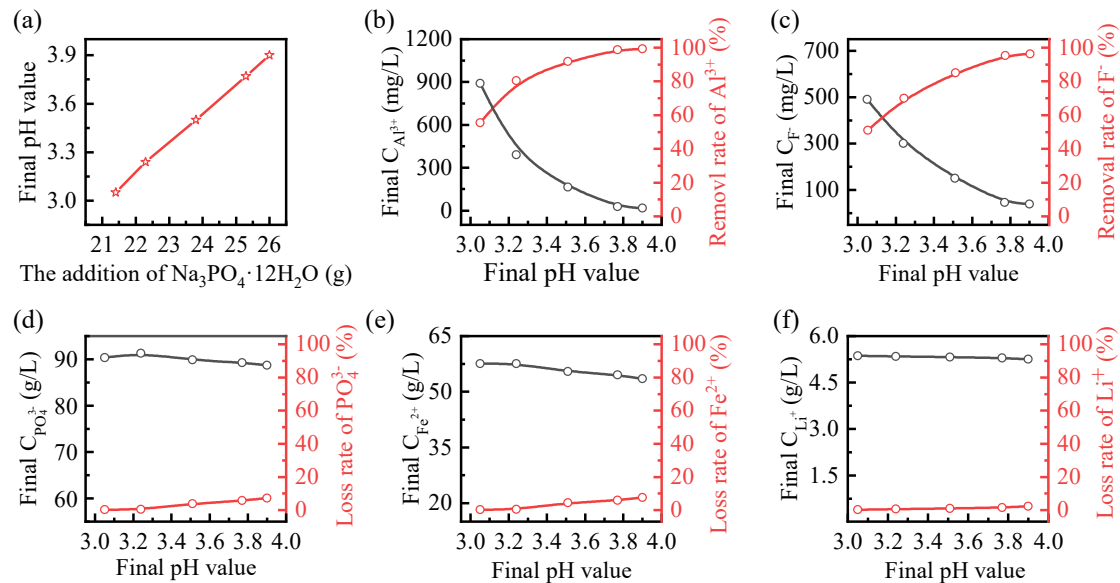
#### 4.3. Precipitation Experiments

Based on the results of above thermodynamic modeling calculation, the sulfuric acid leachate of spent  $\text{LiFePO}_4$  battery powder was employed to conduct bench-scale experiments to validate the feasibility of the separation and purification technology under the conditions of the reaction temperature of  $25^\circ\text{C}$ , reaction time of 5 min, and agitation rate of 400 rpm.

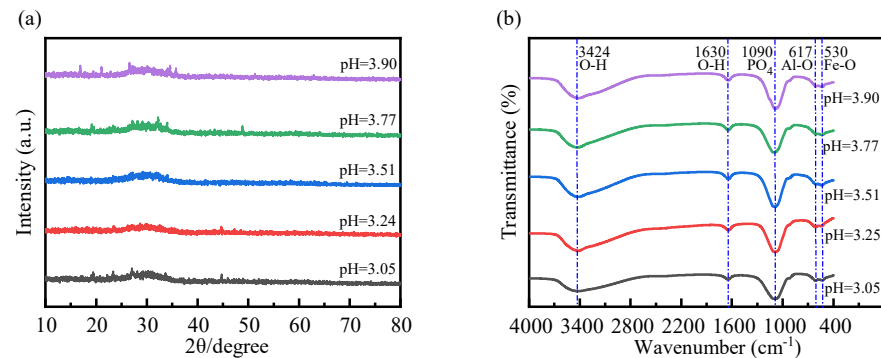
Figure 4 shows the effects of  $\text{Na}_3\text{PO}_4 \cdot 12\text{H}_2\text{O}$  dosage on the final pH value and precipitation behavior of each element in the solution. Figure 4a depicts the relationship between  $\text{Na}_3\text{PO}_4 \cdot 12\text{H}_2\text{O}$  dosage and the final pH value of the 250 mL solution. As indicated in Figure 4b,c, the final pH value of the solution had a considerable effect on the removal of aluminum and fluorine impurities by chemical precipitation. When the amount of  $\text{Na}_3\text{PO}_4 \cdot 12\text{H}_2\text{O}$  added was increased from 21.4 g to 25.3 g, the final pH value increased from 3.05 to 3.77. Correspondingly, the concentration of residual aluminum ions in the solution decreased from 890.5 mg/L to 27.55 mg/L. Moreover, the removal rate of aluminum ions increased from 55.48% to 98.62%, the concentration of residual fluoride ions decreased from 490.5 mg/L to 46.0 mg/L, and the removal rate of aluminum ions increased from 51.1% to 95.41%. By comparison, when the final pH value increased to 3.90, the concentration of residual aluminum and fluoride ions only slightly decreased from 27.55 mg/L to 15.95 mg/L and from 46.0 mg/L to 39.78 mg/L, respectively. The effects of the final pH value on  $\text{PO}_4^{3-}$ ,  $\text{Fe}^{2+}$ , and  $\text{Li}^+$  in the solution are illustrated in Figure 4d–f, respectively. As presented in Figure 4d, e, the loss rate of  $\text{PO}_4^{3-}$  and  $\text{Fe}^{2+}$  increased, when the final pH value increased from 3.05 to 3.77. Combined with the results of thermodynamic calculation, the increase in the loss rate of  $\text{PO}_4^{3-}$  and  $\text{Fe}^{2+}$  should be resulted by the formation of  $\text{FeF}_3$ ,  $\text{AlPO}_4$ ,  $\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}$ ,  $\text{FePO}_4$ , and  $\text{Fe(OH)}_3$ . When the final pH value increased from 3.05 to 3.90, the loss rate of  $\text{Li}^+$  slightly increased from 0.21% to 2.28% (Figure 4f). The high final pH value probably resulted in an increase in the amount of precipitation that contained lithium ions. In conclusion, the final pH value at about 3.77 could deeply purify the aluminum ions and fluoride ions, as well as reduce the loss rate of phosphate ions and iron ions as much as possible.

The XRD patterns and FT-IR spectra of precipitation obtained at different final pH values are plotted in Figure 5. As shown in Figure 5a, no obvious characteristic diffraction peak appeared on the XRD pattern, demonstrating that the precipitation had an amorphous structure. Figure 5b shows the FTIR spectra of precipitation. The wide absorption peak at  $3424 \text{ cm}^{-1}$  and the small absorption peak at  $1630 \text{ cm}^{-1}$  corresponded to the O–H bond stretching and bending vibrations in the precipitation, respectively [12]. The strong absorption peak at  $1090 \text{ cm}^{-1}$  was attributed to the P–O stretching vibrations in  $\text{PO}_4^{3-}$  [37]. The small absorption peak at  $617 \text{ cm}^{-1}$  represented the Al–O stretching vibrations in tetrahedral  $\text{AlO}_4^{5-}$  [38], and the absorption peak at  $530 \text{ cm}^{-1}$  corresponded to the Fe–O stretching vibrations [38]. According to the FTIR spectra of precipitation and the results

of thermodynamic simulation calculation, the main compositions of precipitation were  $\text{AlPO}_4$ ,  $\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}$ ,  $\text{FePO}_4$ , and  $\text{Fe}(\text{OH})_3$ .



**Figure 4.** Effects of (a)  $\text{Na}_3\text{PO}_4 \cdot 12\text{H}_2\text{O}$  dosage on the final pH value and precipitation behavior of (b)  $\text{Al}^{3+}$ , (c)  $\text{F}^-$ , (d)  $\text{PO}_4^{3-}$  and (e)  $\text{Fe}^{2+}$  and (f)  $\text{Li}^+$ .

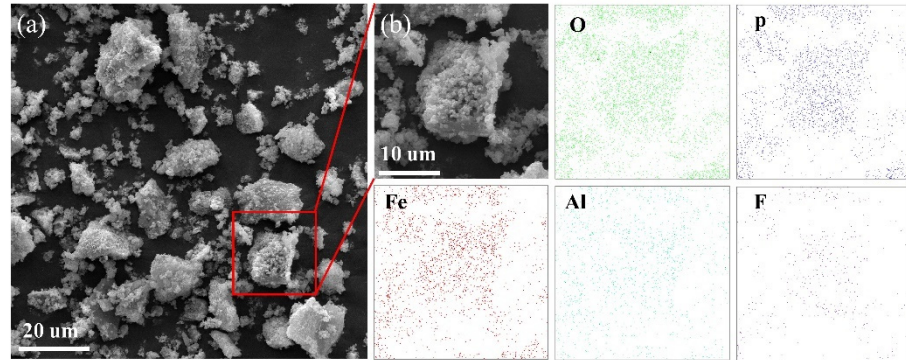


**Figure 5.** (a) X-ray diffraction (XRD) patterns and (b) Fourier transform infrared (FTIR) spectra of precipitate at different final pH value. (agitation rate = 400 rpm, reaction time = 5 min, and reaction temperature = 25 °C).

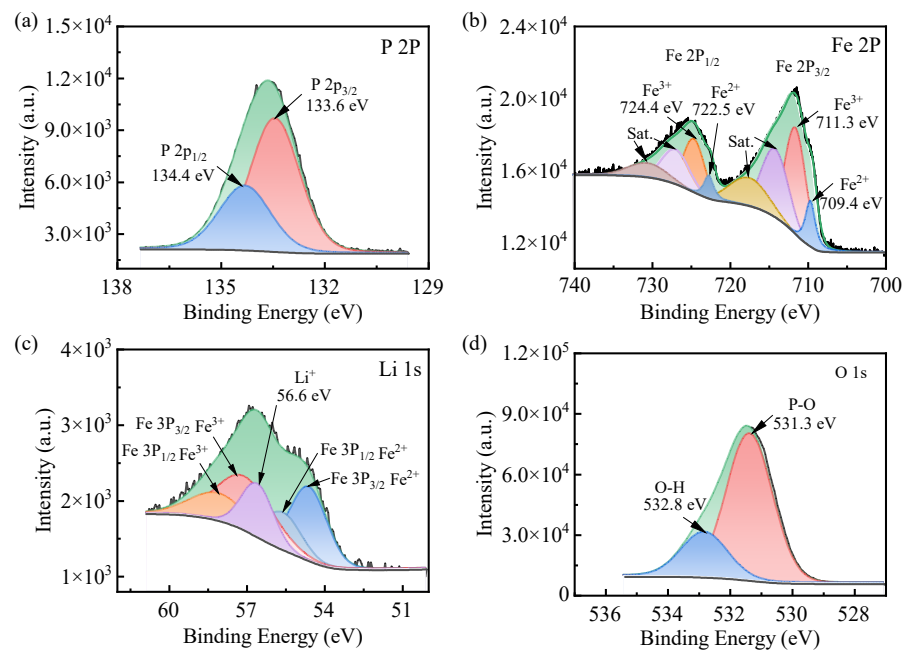
The SEM-EDS spectra of precipitation under the optimal conditions are presented in Figure 6. Figure 6a shows that the precipitation was inside small irregular particles. Figure 6b is a partially enlarged map of precipitation, and its EDS mapping indicated that the precipitation contained various elements, such as P, Fe, O, Al, and F.

The phase composition and surface chemical states of precipitation was further characterized via XPS analysis (Figure 7). The P 2p spectrum in Figure 7a shows that the peaks corresponding to the binding energies of P 2p<sub>3/2</sub> and P 2p<sub>1/2</sub> were located at 133.6 and 134.4 eV, respectively, which were caused by spin-orbit coupling. This result was consistent with the reported binding energies of P–O in  $\text{PO}_4^{3-}$  [39]. The Fe 2P spectrum in Figure 7b shows that the spin-orbit doublets of Fe 2p<sub>3/2</sub> and Fe 2p<sub>1/2</sub> were situated at approximately 712.0 and 725.0 eV, respectively. Each of them consisted of two main peaks (709.4 and 711.3 eV for Fe 2p<sub>3/2</sub>, 722.5 and 724.4 eV for Fe 2p<sub>1/2</sub>) and two satellites (713.9 and 717.3 eV for Fe 2p<sub>3/2</sub>, 727.0 and 730.4 eV for Fe 2p<sub>1/2</sub>) [40]. The results indicated that the iron element in the precipitation existed in the form of  $\text{Fe}^{2+}$  and  $\text{Fe}^{3+}$ , and the  $\text{Fe}^{3+}/\text{Fe}^{2+}$  molar ratio was 1.35. Owing to the overlapping photoelectron spectra of Li 1s and Fe 3p,

Gaussian peak fitting was performed for Li 1s (Figure 7c). The characteristic peak of Li 1s located at 56.6 eV was attributed to  $\text{Li}^+$  [40]. The O 1s spectrum was fitted with two peaks (Figure 7d). The strong peak at 531.3 eV was related to the P–O of phosphate groups, whereas the weak peak at 532.8 eV was associated with O–H. The characteristic peaks of Al 2p that appeared at 74.7 and 75.1 eV were related to Al–O from  $\text{AlPO}_4$  (Figure 7e), indicating that the aluminum element in the precipitation existed in the form of  $\text{AlPO}_4$ . Figure 7f shows the spectrum of F 1s. The characteristic peak of F 1s centered at 68.5 eV was ascribed to Fe–F. Therefore, the fluorine element in the precipitation existed as  $\text{FeF}_3$ .

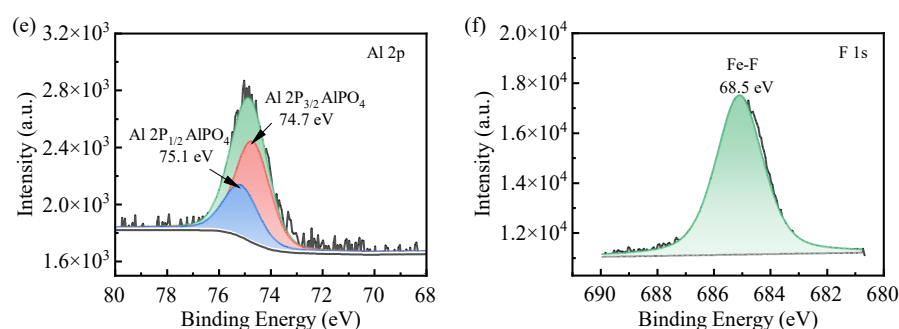


**Figure 6.** Scanning electron microscopy-energy-dispersive spectroscopy (SEM-EDS) spectra of precipitate under optimal conditions. (agitation rate = 400 rpm, reaction time = 5 min, reaction temperature = 25 °C, and final pH value 3.77). (a) SEM image of the precipitate; (b) Microstructure of the precipitate.



**Figure 7.** Cont.





**Figure 7.** X-ray photoelectron spectroscopy (XPS) spectra of precipitate under optimal conditions. (agitation rate = 400 rpm, reaction time = 5 min, reaction temperature = 25 °C, and final pH value 3.77). (a) P 2p; (b) Fe 2p; (c) Li 1s; (d) O 1s; (e) Al 2p; (f) F 1s.

## 5. Conclusions

The evolution law of the total equilibrium concentration of Al, Fe, P, and F, and the phase composition of precipitates at different final pH values are explained using the thermodynamic mathematical model. By adjusting the final pH value of the  $\text{Li}^+ - \text{Fe}^{2+} / \text{Fe}^{3+} - \text{PO}_4^{3-} - \text{SO}_4^{2-} - \text{H}_2\text{O}$  system, Al and F elements were precipitated in solid phases of  $\text{AlPO}_4$ , and  $\text{FeF}_3$ , whereas P and Fe elements were co-precipitated as  $\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}$ ,  $\text{FePO}_4$ , and  $\text{Fe}(\text{OH})_3$ , respectively. Among them,  $\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}$  is the main precipitate, and the precipitate also contains a small amount of  $\text{FePO}_4$ ,  $\text{Fe}(\text{OH})_3$ ,  $\text{AlPO}_4$ , and  $\text{FeF}_3$ . Therefore, selective precipitation of  $\text{Al}^{3+}$  and  $\text{F}^-$  can be precisely controlled by pH of the leaching solution, at the same time, the loss rate of P and Fe can be reduced. The removal mechanism of Al and F was further revealed by characterizing the precipitation via XRD, FTIR, SEM-EDS, and XPS. Results indicated that the precipitation mainly existed in the form of  $\text{AlPO}_4$ ,  $\text{Fe}_3(\text{PO}_4)_2 \cdot 8\text{H}_2\text{O}$ ,  $\text{FePO}_4$ ,  $\text{Fe}(\text{OH})_3$ , and  $\text{FeF}_3$ , consistent with the results of thermodynamic analysis.

**Author Contributions:** Conceptualization, S.Y. and Y.L.; methodology, Z.L. and Y.C.; software, Y.J.; validation, Y.C., S.Y. and Y.L.; formal analysis, P.S.; investigation, D.C.; resources, Y.C.; data curation, G.F.; writing—original draft preparation, Y.J.; writing—review and editing, Y.J., C.M. and J.D.; visualization, Y.C.; supervision, Z.L., S.Y. and Y.L.; project administration, Y.C.; funding acquisition, S.Y. and Y.C. All authors have read and agreed to the published version of the manuscript.

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**Conflicts of Interest:** The authors declare no conflict of interest.

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