

Article

Compositional Optimization and Structural Properties of the Filled Skutterudite $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{11.5}\text{Sn}_{0.5}$

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Abstract: A compositional and crystallographic study was carried out on the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{11.5}\text{Sn}_{0.5}$ filled skutterudite system ($0.40 \leq x \leq 0.80$) with the aim to determine the equilibrium Sm filling fraction (y) within the considered x range. The relevance of the material lies in its potential thermoelectric properties: in analogy with similar skutterudites systems, these features should in fact result as being improved with respect to the ones of the corresponding Sn-free system thanks to the partial substitution of Sn for Sb, which is expected to lower the phonon thermal conductivity. The results of Rietveld refinements allowed us to study the skutterudite structural properties and to discuss them, adopting a comparative approach with respect to the ones of the Sn-free system $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$. Relying on the refined Sm occupancy factors, the p/n crossover is shown to be located at $x \sim 0.53$, meaning that the introduction of Sn induces an enlargement of the p -region; moreover, at variance with the Sn-free system, the coefficient of thermal expansion does not show any significant mismatch between n - and p - compositions, which should ensure a prolonged lifetime of a device made of n - and p - legs that both derive from the studied system.

Keywords: thermoelectrics; filled skutterudites; coefficient of thermal expansion; powder x-ray diffraction; Rietveld method; electron microscopy

1. Introduction

Filled skutterudites form a wide family of intermetallic compounds thoroughly studied for their potential thermoelectric properties [1–7]. They formally derive from skutterudites, binary compounds investigated for the first time by Oftedal in the first half of the last century [8]. Skutterudites have the general formula MX_3 ($\text{M} \equiv \text{Co}, \text{Rh}, \text{Ir}$, and $\text{X} \equiv \text{P}, \text{As}, \text{Sb}$) and crystallize in a body-centered cubic cell belonging to the $Im\bar{3}$ space group; the atomic arrangement consists of two atomic positions, namely the $8c$ ($1/4, 1/4, 1/4$) and the $24g$ ($0, y, z$), which are occupied by the M and X atom, respectively. M is coordinated to 6 X atoms forming strongly tilted octahedra. The parent compound CoSb_3 does not present exploitable thermoelectric properties despite its high charge carrier mobility, due to its overly large thermal conductivity ($\lambda \sim 10 \text{ W m}^{-1} \text{ K}^{-1}$ at 293 K [9]).

It is in fact well known that the optimization of a material's thermoelectric properties implies the maximization of the power factor σS^2 and the minimization of λ_e and λ_{ph} (where σ is the

electrical conductivity, S the Seebeck coefficient, and λ_e and λ_{ph} the electron and phonon thermal conductivity, respectively). This approach follows the phonon-glass electron-crystal (PGEC) concept [10], which states that the ideal thermoelectric material should conduct heat like a glass and electricity like a crystal. The maximization of σS^2 results from the optimization of the charge carriers concentration, the increase of which at the same time causes an increase of σ and a drop of S ; it implies the knowledge of the material's band structure and its engineering. The reduction of λ_e , in turn, is limited by the Wiedemann–Franz law:

$$\frac{\lambda_e}{\sigma} = LT \quad (1)$$

where L is the Lorenz number [11]. Therefore, the most convenient way to reduce thermal conductivity is the manipulation of λ_{ph} , which essentially consists in the introduction of scattering centers, such as interstitial and substitutional atoms, able to disturb the phonon propagation throughout the structure. The introduction of interstitial and substitutional atoms, as well as actions directed toward the modification of extrinsic factors, such as density enhancement [12–14], porosity control [15], nanostructuring [16], mesostructuring [17], or precipitation of nano-sized secondary phases [18], can be mentioned among the most effective methods to enhance phonon scattering, and hence to reduce λ_{ph} .

In the framework of the introduction of foreign atoms, and according to Slack's intuition [19], filling the Sb_{12} icosahedral cage formed in skutterudites around the $2a$ position (0,0,0) by a proper atom (mainly a lanthanide or an alkaline-earth element [1,7,20]) strongly reduces thermal conductivity, as testified by many filled skutterudite systems, such as for example $RE_{0.1}Co_4Sb_{12}$ ($RE \equiv La, Ce, Nd, Sm, Yb, Eu$), which display much lower thermal conductivity values ranging between 3.5 and 5.5 $W\ m^{-1}\ K^{-1}$ at 293 K, depending on the rare earth identity [21]. Even more relevant results can be obtained when a double or a multiple filling of the $2a$ position by different filler atoms is operated, such as in the case of the $(Sm,Gd)_y(Fe_xNi_{1-x})_4Sb_{12}$ [22], the $(Ba,Sr,DD,Yb)_y(Fe_xNi_{1-x})_4Sb_{12}$ ($DD \equiv$ didymium, a Nd/Pr mixture) [23], the $Ce_xNd_xFe_{3.7}Ni_{0.3}Sb_{12}$ [24], the $Mm_y(Fe_xCo_{1-x})_4Sb_{12}$ ($Mm \equiv$ mischmetal, a natural mixture of Ce, La, Pr, and Nd) [25], and the $Ba_xYb_yCo_4Sb_{12}$ systems [26]. When the transition metal is also partially substituted, additional phonon scattering is provided, and thermal conductivity is further reduced. Following this idea, a large variety of filled skutterudites containing two different transition metals were prepared and studied; even when limiting oneself to antimonides, several Fe/Ni [27–31], Fe/Co [32–37], and Ni/Co [38–40] filled skutterudites systems are documented in the literature.

A third way aimed at introducing further disorder into the structure, and hence at reducing λ , involves the partial substitution of Sb at the $24g$ site by various elements or element mixtures, such as Sn [32,33,41,42], Ge [32,43,44], Te [45], Se [46], Se/Te [46], Te/S [47], or Te/Sn [48]. Sn-doping, in particular, proved to be particularly effective at reducing phonon thermal conductivity, as testified by $DD_{0.59}Fe_{2.7}Co_{1.3}Sb_{11.8}Sn_{0.2}$ [32], as well as by $Ce_yCo_4Sb_{12-\delta}Sn_\delta$ [42], $Nd_{0.6}Fe_2Co_2Sb_{12-\delta}Sn_\delta$ [41], and $CoSb_{3-\delta}Sn_\delta$ [49]. The positive effect occurs despite the closeness of Sn and Sb atomic masses, which makes mass fluctuation scattering negligible.

The partial substitution of Sb by an aliovalent atom also exerts an effect on the electronic properties of the material. Even without resorting to band structure calculations, skutterudites can be described through Zintl's approach, which allows one to explain the diamagnetic and semiconducting nature of $CoSb_3$ [1,7]. The substitution of Co by a Fe/Ni mixture induces an electron imbalance, which can be only partly restored by the injection of electrons from the filler: it is in fact well known that the filling fraction is an intrinsic property of a given skutterudite system [1], also affecting the structural properties of the material [50], and that a different filler amount can hardly be forced into the structure [27] unless drastic techniques are used, such as synthesis at a high [14] or extremely high pressure [51]. Consequently, p - and n -conducting skutterudites occur; in the $Sm_y(Fe_xNi_{1-x})_4Sb_{12}$ system, for example, the p/n crossover is located at $x \sim 0.63$ [29]. It can thus be expected that the partial substitution of Sb by Sn, namely by an atom with an electron that is less in the outer shell, requires the insertion of a larger number of electrons deriving from the filler to reach the electron count of a degenerate semiconductor. Nevertheless, since the introduction of filler atoms

does not generally satisfy the requirement for a degenerate semiconductor for the aforementioned reasons, it can be expected that Sn/Sb-based skutterudites are characterized by a larger p -compositional extent than the Sb-based ones, as indeed verified for $\text{CoSb}_{3-\delta}\text{Sn}_\delta$, where the Sb substitution by Sn was in fact originally employed to obtain p - CoSb_3 [52].

Following the idea of increasing the disorder degree of the structure, the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{11.5}\text{Sn}_{0.5}$ filled skutterudite was taken into consideration, as it derives from the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ system, which was thoroughly studied by the present research group [53–61] for its promising thermoelectric properties, which provide $ZT = 0.55$ at ~ 600 K [62]. As aforementioned, the filling fraction is of primary importance in driving the electronic properties of a filled skutterudite; nevertheless, its equilibrium value can hardly be predicted a priori, and the issue needs to be fixed in the first stages of the study of a new system to ensure the preparation of pure samples. A preliminary work of compositional optimization was thus undertaken on the chosen system: in the absence of literature data, experimental y values found for each x in the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ system [29] were employed for the synthesis of Sn-containing samples. A subsequent compositional and structural study was performed in order to reveal the actual Sm content of specimens, and ultimately to optimize the synthesis procedure.

Moreover, a further technologically relevant issue when dealing with a thermoelectric material concerns its coefficient of thermal expansion (CTE). Ideally, the CTE mismatch between the n - and p -leg of a thermoelectric device should be as small as possible, in order to reduce the thermal stress caused by the uninterrupted work under large temperature gradients, and therefore to prolong the device lifetime. It is generally meant for this goal to be reached if both the p - and the n -elements derive from the same matrix [63]; nevertheless, the issue is not obvious, and this prediction is only confirmed in some cases, such as for the $(\text{Ba,DD,Yb,Sr})_y\text{Fe}_3\text{NiSb}_{12}$ system [23]. In most skutterudite systems, on the contrary, CTE is shown to be higher for p - than in n -compositions [63,64], so that Rogl et al. proposed for instance the dispersion of nano-sized $\text{Ta}_{0.8}\text{Zr}_{0.2}\text{B}$ particles into a $(\text{Mm,Sm})_y\text{Co}_4\text{Sb}_{12}$ matrix to reduce the n/p CTE mismatch [65]. In this respect, an interesting case is represented by $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$, which displays a significant p/n CTE mismatch [61], as a consequence of the discontinuity occurring at the p/n crossover in the lattice parameter trend *vs.* the Fe content [29]. In the present work, crystallographic data collected up to 773 K were employed to determine the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{11.5}\text{Sn}_{0.5}$ CTE, which revealed a much lower p/n mismatch and thus a very promising mechanical behavior.

2. Materials and Methods

2.1. Synthesis

Four compositions belonging to the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{11.5}\text{Sn}_{0.5}$ system ($x = 0.40$ and $y = 0.06$; $x = 0.55$ and $y = 0.23$; $x = 0.60$ and $y = 0.31$; $x = 0.80$ and $y = 0.55$) were prepared via the conventional melting-quenching-annealing technique commonly used for the Sn-free system [29,61]; in the absence of specific literature data, the Sm amount (y) to be added in association to each x value was chosen to be identical to the experimental value observed in the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ system [29]. The starting materials were stoichiometric amounts of Fe (Alfa-Aesar, Kandel, Germany, 99.99 wt. %), Ni (Alfa-Aesar, Kandel, Germany, 99.99 wt. %), Sm (NewMet, Waltham Abbey, UK, 99.9 wt. %), and pre-alloyed $\text{Sb}_{0.96}\text{Sn}_{0.04}$. The precursor alloy, in turn, was prepared from due amounts of Sb (Mateck, Jülich, Germany, 99.99 wt. %) and Sn (Sigma Aldrich, Darmstadt, Germany, 99.99 wt. %) by melting the proper mixture at 903 K in a quartz vial sealed under Ar gas ($P = 80$ KPa). Materials were mixed and placed into a quartz tube, which was evacuated, closed, and heated up to 1238 K, and then rapidly cooled to obtain microcrystalline phases that can be easily decomposed in favor of the filled skutterudite during the subsequent annealing treatment. In addition, the rapid cooling of the liquid phase prevents the formation of the $(\text{Fe}_x\text{Ni}_{1-x})\text{Sb}$ phase, which is stable at high temperature and does not evolve into the filled skutterudites at the annealing temperature. Samples were then annealed under vacuum at 873 K for ten days, and afterwards slow-cooled. Samples were named Fe40_303, Fe55_373, and so on, where the first number stands for the Fe % amount with respect to the overall

(Fe + Ni) content, and the second one stands for the temperature in K which the diffraction pattern was collected at.

2.2. Scanning Electron Microscopy–Energy-Dispersive x-Ray Spectroscopy (SEM-EDS)

Samples were cut in pieces to be micrographically polished prior to the observation by electron microscopy coupled to an energy dispersive system (Zeiss LEO 1430, Jena, Germany, equipped with EDS INCA Energy 200, Link Analytical–Oxford Instruments, Abingdon-on-Thames, UK). By this technique, the occurrence of phases was studied, and their composition was evaluated. Microphotographs were taken both by backscattered and secondary electrons, and EDS analyses were performed on at least five points for each sample.

2.3. High Temperature Powder X-Ray Diffraction

The room and high temperature structural properties of all the samples were studied by a Bragg–Brentano powder diffractometer (PANalytical X'pert Pro, Almelo, The Netherlands, Cu $K\alpha$ radiation); Ge was used as an internal standard to accurately determine the skutterudite lattice parameter of each specimen. Samples were crushed, ground, sieved through a 75 μm sieve, placed on an alumina sample-holder, and introduced into a high temperature oven chamber (Anton Paar, HTK 1200N, Graz, Austria); diffraction patterns were collected at room temperature (303 K), as well as at 373, 473, 573, 673, and 773 K (angular range: 10–112°, step 0.017°, time per step: 90 s). Samples were protected from oxidation by He atmosphere. The structural models of skutterudite and, when possible, of extra phases, were refined for samples Fe40, Fe55, and Fe60 by the Rietveld method through the FullProf software, version September 2020 [66]. Due to the large content of extra phases, it was not possible to refine the skutterudite structural model of sample Fe80. On the contrary, the skutterudite cell parameter was calculated for all the compositions by the least squares method. To this purpose, the Ge CTE was found by collecting the diffraction patterns of Ge at the same temperatures as the samples, and by refining the Ge lattice parameter. The CTE values resulting at the different temperatures for Ge were found in good agreement with literature data [67], and were employed to calculate the Ge cell parameter at each temperature; the cell parameter $a = 5.6575 \text{ \AA}$ [67] was used as the room temperature reference value.

3. Results

3.1. Compositional and Morphological Characterization

SEM microphotographs indicate that in all the samples, except in Fe80, the filled skutterudite is the main phase; nevertheless, even other phases are present: in particular, three differently colored regions appear in Figure 1. Relying on EDS analyses, the darkest one consists of (Fe,Ni)Sb₂, the lightest one of Sb_{1-x}Sn_x, and the intermediate one of the Sn-containing skutterudite. Moreover, the observation of Figure 1 also suggests that Fe55 is essentially formed of skutterudite, the amount of extra phases being almost negligible (see Figure 1b), and that Fe80 is mainly composed of Sb_{1-x}Sn_x and (Fe,Ni)Sb₂.

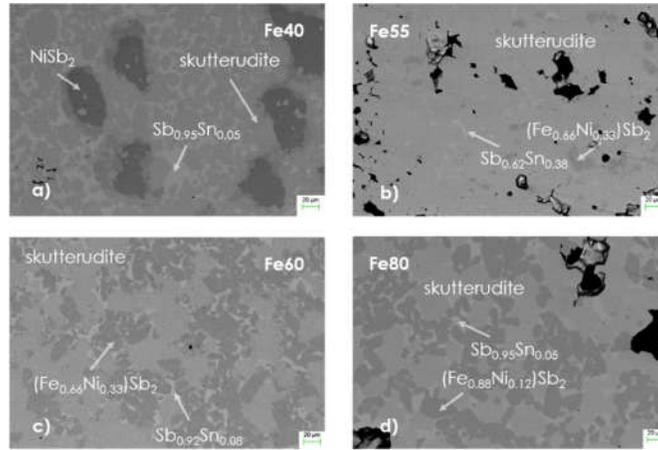


Figure 1. SEM microphotographs taken by backscattered electrons on the polished surface of the samples (a) Fe40, (b) Fe55, (c) Fe60, and (d) Fe80.

The results of the room temperature x-ray diffraction analyses confirm the outcome of the electron microscopy while revealing the presence of tiny amounts of other extra phases, such as for example SbSn. An overview of the compositional analyses of all the samples is provided in Table 1; the amounts of extra phases whose structural models could be refined are reported too. The amount of additional phases in Fe80 was not quantified due to the impossibility to refine the structural models of phases contributing to the sample.

Similarly to Sn-free skutterudites [22], even the present samples present a high porosity degree, as observable in Figure 2, where microphotographs taken by secondary electrons are collected.

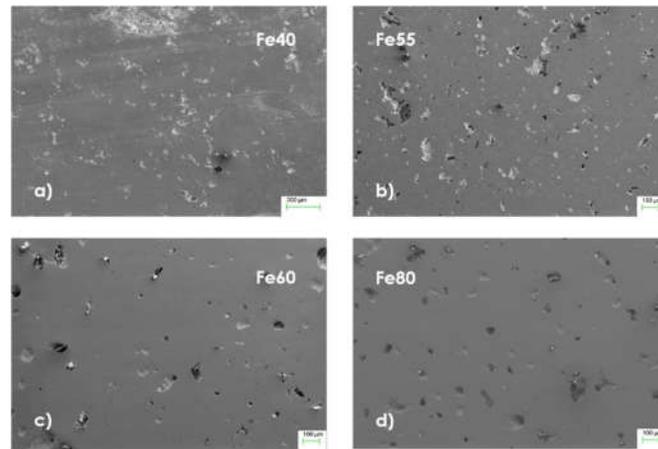


Figure 2. SEM microphotographs taken by secondary electrons on the polished surface of the samples (a) Fe40, (b) Fe55, (c) Fe60, and (d) Fe80.

Table 1. Refined composition, amount of additional phases as revealed by EDS and x-ray diffraction, skutterudite cell parameter, and Rietveld agreement factors for each sample. Sample Fe80 is mainly composed of the extra phases Sb and FeSb₂.

Sample	Refined composition	Additional phases (wt.%)	Skutterudite <i>a</i> cell parameter [Å]	χ^2 ¹	Skutterudite R_B ²
Fe40_303			9.0948(1)	18.5	9.39
Fe40_373			9.1023(1)	15.0	9.91
Fe40_473	Sm _{0.22} (Fe _{0.41} Ni _{0.59}) _{3.9} Sb _{11.8} Sn _{0.2}	Sb _{0.95} Sn _{0.05} (11%)	9.1128(1)	12.5	10.5
Fe40_573			9.1245(1)	12.7	9.43
Fe40_673			9.1370(1)	12.1	11.0
Fe40_773			9.1487(1)	12.8	9.88
Fe55_303					9.1004(1)
Fe55_373	Sm _{0.26} (Fe _{0.55} Ni _{0.45}) _{3.7} Sb _{11.5} Sn _{0.5}	Fe _{0.66} Ni _{0.33} Sb ₂ (traces); SbSn (traces)	9.1085(1)	6.85	6.11
Fe55_473			9.1203(1)	7.63	6.18
Fe55_573			9.1326(1)	6.58	6.19
Fe55_673			9.1457(1)	5.81	5.79
Fe55_773			9.1585(1)	6.03	5.18
Fe60_303			9.1005(1)	8.39	8.26
Fe60_373	Sm _{0.27} (Fe _{0.59} Ni _{0.41}) _{3.7} Sb _{11.7} Sn _{0.3}	Sb _{0.92} Sn _{0.08} (9%); Fe _{0.66} Ni _{0.33} Sb ₂ (29%)	9.1086(1)	8.03	9.26
Fe60_473			9.1203(1)	7.27	7.48
Fe60_573			9.1322(1)	6.08	7.90
Fe60_673			9.1453(1)	6.90	8.25
Fe60_773			9.1573(1)	4.66	5.14
Fe80_303			9.1181(1)	--	--
Fe80_373			9.1267(1)	--	--
Fe80_473	Sm _{0.61} (Fe _{0.79} Ni _{0.21}) _{3.9} Sb _{11.8} Sn _{0.2}	Sb; FeSb ₂ ; SbSn (traces)	9.1392(1)	--	--
Fe80_573			9.1508(1)	--	--
Fe80_673			9.1661(1)	--	--
Fe80_773			9.1831(1)	--	--

$$^1 \chi^2 = \left(\frac{R_{wp}}{R_{exp}} \right)^2 \quad ^2 R_B = \frac{\sum_k |I_{k,obs} - I_{k,calc}|}{\sum_k |I_{k,obs}|}$$

3.2. Structural Characterization

The skutterudite structural model was refined by the Rietveld method for the samples Fe40, Fe55, and Fe60 according to the previously described cubic cell crystallizing in the $Im\bar{3}$ space group. For each diffraction pattern, in the last refinement cycles the structural parameters (y and z atomic coordinates of Sb, and the Sm occupancy factor of the $2a$ position), as well as the scale factor, nine peak parameters (U , V , W , η [the Gaussian/Lorentzian mixing parameter], Y [the θ dependence of η], and four asymmetry parameters), and the background points were refined. The background was fitted by linear interpolation of a set of ~ 70 points taken from the experimental pattern, and the peak profiles were optimized by the pseudo-Voigt function. The Fe and Ni occupancy factors were fixed to the value obtained from the EDS analyses, due to the closeness of their atomic scattering factors. The (Sb + Sn) occupancy factor was constrained at 1, relying on the EDS results, which indicate a (Sb,Sn)/(Fe,Ni) amount ratio slightly higher than 3 for each composition. The Sm occupancy factor, on the contrary, was refined for all the compositions at each temperature considered, being a reliable and critical parameter in the compositional optimization of the studied system. Angular regions corresponding to Ge peaks were excluded from the refinements. In Figure 3, the Rietveld refinement plot of sample Fe55_373 is reported as a representative example; a small peak attributable to an unknown compound is marked with an asterisk. The agreement factors (χ^2 and the skutterudite R_B),

as well as the skutterudite cell parameters, can be found in Table 1; the refinement plots of all the samples at each temperature considered are reported as Supplementary Materials.

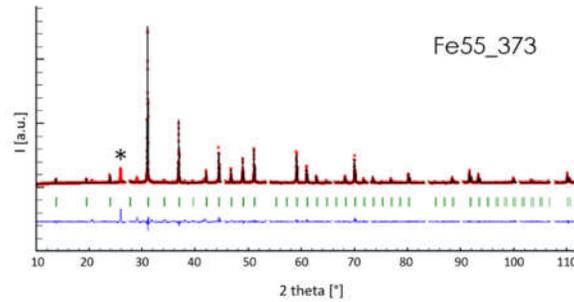


Figure 3. Rietveld refinement plot of sample Fe55_373. The red and black lines are the experimental and the calculated diffractograms, respectively; the lower blue line is the difference curve; green vertical bars indicate the calculated positions of Bragg peaks of the filled skutterudite; the asterisk indicates the presence of a small amount of an unknown compound. Angular regions corresponding to the positions of Ge peaks were excluded.

The skutterudite cell parameter linearly increases along the whole considered temperature span, as shown in Figure 4: the data can be excellently fitted by regression lines, as reported in Table 2, where the equations of the regression lines, as well as the corresponding R^2 value, are collected. A more detailed data analysis indicates that the expected value of the skutterudite cell parameter a is very close to the experimental one; the goodness of the fit is further confirmed by the R^2 value. The slightly lower R^2 value of Fe80 is due to the presence of extra phases within the sample, which does not allow a more accurate determination of the cell parameter.

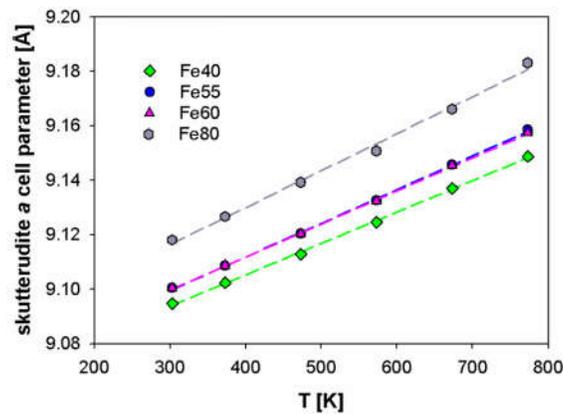


Figure 4. Trend of the skutterudite a cell parameter as a function of the temperature for each sample. The dashed lines are the regression lines fitting the experimental points; the error bars are hidden by data markers.

Table 2. Equation of the regression lines $a = mT + q$ fitting the a lattice parameter *vs.* the temperature (T) for each composition; the expected a values at 303 K and the calculated R^2 values are reported too.

Sample	Equation of the regression line	Expected a value at 303 K [\AA]	R^2
Fe41	$a = 1.1520 \times 10^{-4} T + 9.0592$	9.0941	0.999
Fe55	$a = 1.2370 \times 10^{-4} T + 9.0623$	9.0998	0.999
Fe59	$a = 1.2135 \times 10^{-4} T + 9.0633$	9.1001	0.999
Fe79	$a = 1.3595 \times 10^{-4} T + 9.0756$	9.1168	0.994

The Sm occupancy factor is a crucial parameter in the study of the structural and electronic properties of filled skutterudites, as described in the Introduction and discussed in more detail in the following section. Moreover, the high atomic number of the element allows a reliable determination of its occupancy factor. In Figure 5, the trend of the Sm occupancy factor in the $2a$ site as a function of the temperature is reported for each sample, revealing a roughly linear increase.

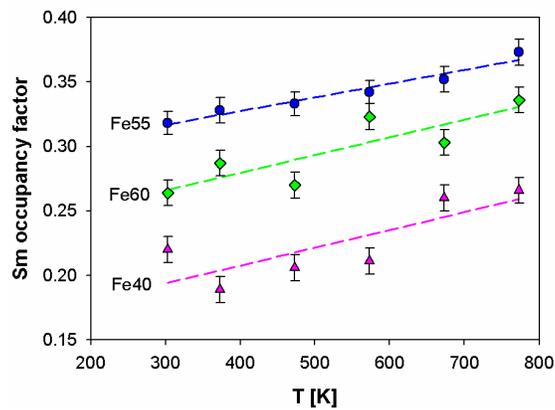


Figure 5. Trend of the Sm occupancy factor in the $2a$ site as a function of the temperature for each sample. The dashed lines are the regression lines fitting the experimental points.

4. Discussion

The position of the p/n crossover in filled skutterudites can be at least roughly determined, relying on the simple bonding model adopted in the framework of the Zintl's concept. According to this approach, CoSb_3 , and also the isoelectronic $\text{Fe}_{0.5}\text{Ni}_{0.5}\text{Sb}_3$, are degenerate semiconductors, as experimentally confirmed [1]. Filling the cavity located in $(0,0,0)$ with an electropositive element introduces a certain number of electrons per filler atom, which tend to fix the electron imbalance; nevertheless, filler atoms generally introduce excessive holes or excessive electrons, thus giving rise to p - and n -skutterudites, respectively. A convenient graphical method highlighting the position of the crossover in the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ system consists in reporting two lines in a y *vs.* x diagram: the one representing the Sm amount theoretically necessary to exactly reproduce the electronic count of the parent compound CoSb_3 , and the one fitting the experimental y data corresponding to each x value. The crossing point of the two lines can be considered as the p/n crossover, as revealed by the structural data. In Figure 6, the thick and thin dash-dot green lines represent the ideal and the regression lines, respectively, for the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ system: as aforementioned, the p/n crossover is located at $x \sim 0.63$, as indeed confirmed by the room temperature Seebeck measurements [29]. When Sb is partly substituted by an element with an electron that is less in the outer shell, such as Sn, fewer electrons are provided for the skutterudite bonding scheme and more electrons are required from the filler to fix the electron imbalance; as a consequence, the ideal line moves toward higher y values, meaning that higher Sm amounts are necessary to reproduce the electron count of a compensated semiconductor. This scenario is evident in Figure 6, where the thick dashed blue line represents the

ideal line for the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{11.5}\text{Sn}_{0.5}$ system. The blue points appearing within the diagram represent the refined y values of this system. Two main issues are worth noting: first of all, experimental y values can be satisfactorily fitted by a line, similarly to the Sn-free system. This evidence allows one to localize the crossing point of the two lines, and hence the p/n crossover, which results in being located at $x \sim 0.53$, thus confirming the expectation for a larger p -region with respect to the Sn-free system.

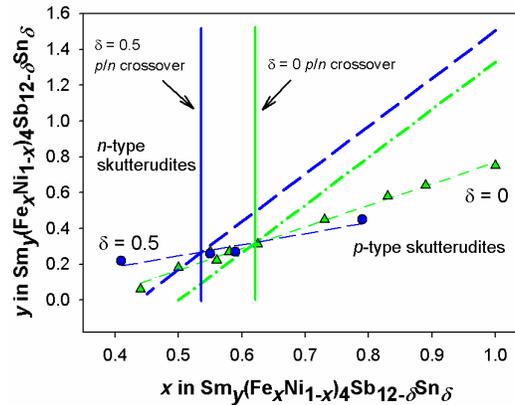


Figure 6. Sm content (y) in $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12-\delta}\text{Sn}_\delta$ filled skutterudites as a function of x . The thick dash-dot green and dashed blue lines represent the theoretical Sm amount necessary to reproduce the electronic count of a compensated semiconductor in the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ and $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{11.5}\text{Sn}_{0.5}$ systems, respectively; the thin ones are the regression lines interpolating experimental points; vertical lines highlight the position of the p/n crossover for both systems. Error bars are hidden by data markers; the data of the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ system are taken from ref. [29].

Secondly, the samples Fe40 and Fe80 are characterized by y values quite far from the ones typical of the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ system. The latter outcome is the reason why both cited samples are polyphasic and also provides a clear indication toward the synthesis of monophasic samples, which is essential for reliable measurements of the skutterudite transport properties. This conclusion is confirmed by the substantial monophasicity of sample Fe55, which presents a refined y very close to the one of the composition with the same Fe content in the Sn-free system.

The analysis of microphotographs taken at a higher magnification by backscattered electrons on polyphasic samples also suggests the skutterudite formation mechanism. It is known that after the melting–quenching stage, leading to $(\text{Fe,Ni})\text{Sb}_2$ and Sb [55], the subsequent annealing treatment promotes the formation of the filled skutterudite. The image of sample Fe80 shown in Figure 7 confirms that the skutterudite formation occurs by a reaction between $(\text{Fe,Ni})\text{Sb}_2$ and $\text{Sb}_{1-x}\text{Sn}_x$, and that it stops before the complete consumption of the reacting alloys, most probably due to the incorrect Sm amount.

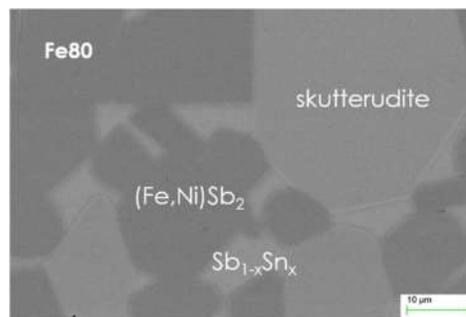


Figure 7. SEM microphotograph taken by secondary electrons on the polished surface of sample Fe80.

Despite the presence of different amounts of additional phases, the results of the Rietveld refinements on the filled skutterudite (performed on Fe40, Fe55, and Fe60), as well as of the cell parameters determination at each temperature (performed on all the samples), reveal intriguing characteristics of the skutterudite structure, especially when compared to the ones of the Sn-free system $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$.

In Figure 8, the trend of the skutterudite cell parameter a is reported as a function of the Fe content (x) at each considered temperature. For the sake of comparison, the cell parameter of the Sn-free system at room temperature is also reported. Again, two main issues can be noticed. Firstly, the cell parameters values indirectly confirm that Sn indeed entered the skutterudite structure, since for each composition they are larger than the corresponding ones of the Sn-free system, as a direct consequence of the larger size of Sn^{4+} (2.94 Å) [49] with respect to Sb^{5-} (2.45 Å) [49]. A further confirmation of this conclusion comes from the analysis of the Sm–Sb/Sn interatomic distance, which can be considered as the size of the cavity centered on the $2a$ site: as evidenced in Figure 9, at each temperature the cited distance is larger for the Sn-containing than for the Sn-free skutterudite. The observed increase in the interatomic distance with an increasing temperature is also in good agreement with the slight increase in the Sm occupancy factor with a rising temperature observed in all the analyzed samples (Fe40, Fe55, and Fe60) and reported in Figure 5. A strict correlation between the cage size and the filler content was previously demonstrated [29].

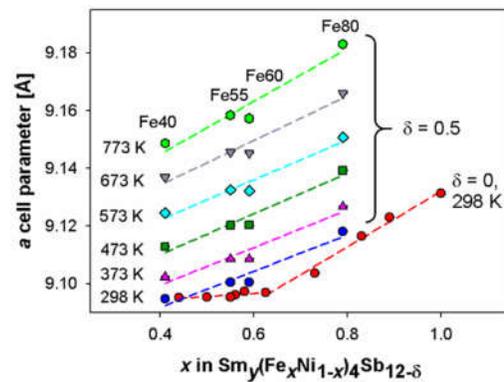


Figure 8. Trend of the a lattice parameter as a function of the Fe content (x) at each temperature; the room temperature values for the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ system (red circles), taken from ref. [29], are also reported as a term of comparison.

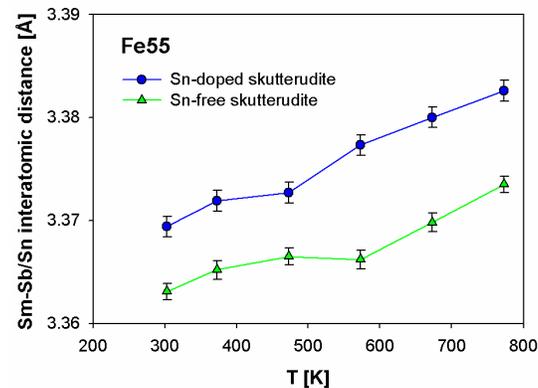


Figure 9. Trend of the Sm–Sb interatomic distances as a function of the temperature for the sample Fe55 of the Sn-containing and the Sn-free skutterudite systems; the data of the latter are taken from ref. [61]. The dashed lines are regression lines.

Secondly, the observation of Figure 8 suggests that the slope change occurring in the trend of the cell parameter of the Sn-free system in correspondence of the p/n crossover, widely discussed in [29,61] and possibly attributed to a low/high spin transition of Fe^{2+} , seems to be absent from the Sn-containing one.

The coefficient of linear thermal expansion (CTE) is defined in a certain temperature range as:

$$CTE = \frac{1}{a_{T_0}} \frac{(a_T - a_{T_0})}{T - T_0} \quad (2)$$

with a_{T_0} being the cell parameter at the reference temperature T_0 ($T_0 = 303$ K in this work). Due to the excellent linearity of the skutterudite cell parameters *vs.* temperature along the considered temperature range (see Table 1), only one CTE was calculated for each composition. The obtained CTE values are reported in Figure 10 as a function of the composition, together with the ones of the Sn-free system, taken from [61]. In good agreement with the aforementioned lacking slope change in the cell parameter *vs.* x shown in Figure 8, even the CTE trend shows no discontinuity in the Sn-containing samples; on the contrary, in the Sn-free system $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$, a 16% CTE mismatch between samples with $x = 0.55$ and $x = 0.63$ occurs [61]. This is quite an important and promising point, since a small CTE mismatch between n - and p - compositions is of primary importance in the design of thermoelectric devices with n - and p - legs deriving from the same matrix. The data reported in Figure 10 thus suggest that the employment of an Sn-containing n -composition and an Sn-free p -composition could conveniently build the n - and the p -leg of a thermoelectric device made of the same skutterudite matrix having virtually identical CTE values. The described result assumes a remarkable significance because most of the skutterudite CTE values reported in the literature present a noticeable gap between the higher p - and the lower n - values; even when limiting oneself to Fe/Ni-based antimonides skutterudites, the $\text{DD}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ system represents an interesting example, displaying a 23% CTE mismatch between compositions with $x = 0.5$ and $x = 0.75$ [64]; similarly, the $\text{Mm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ system is characterized by a 24% CTE mismatch between the sample with $x = 1$ and the one with $x = 0.62$ [64]. Within this scenario, the only skutterudite system presenting p - and n -compositions with a substantially identical value of CTE is $\text{Ba}_{0.09}\text{Sr}_{0.02}\text{DD}_{0.22}\text{Yb}_{0.02}\text{Fe}_{2.4}\text{Ni}_{1.6}\text{Sb}_{12}$ [23], even if one must take into account that the study is limited to the compositions $\text{Ba}_{0.09}\text{Sr}_{0.02}\text{DD}_{0.22}\text{Yb}_{0.02}\text{Fe}_{2.4}\text{Ni}_{1.6}\text{Sb}_{12}$ and $\text{Ba}_{0.15}\text{DD}_{0.28}\text{Yb}_{0.05}\text{Fe}_3\text{NiSb}_{12}$. Finally, looking in more detail at the obtained data, one can note that the CTE values of Sn-containing samples are significantly higher than the ones of the corresponding Sn-free compositions. This result is in good agreement with the aforementioned larger size of Sn^{4+} than Sb^{5-} , and it is analogous to the behavior of Sn-containing and Sn-free samples belonging to other systems, such as the $\text{Tl}_y\text{CoSb}_{11-\delta}\text{Sn}_\delta$ one [68].

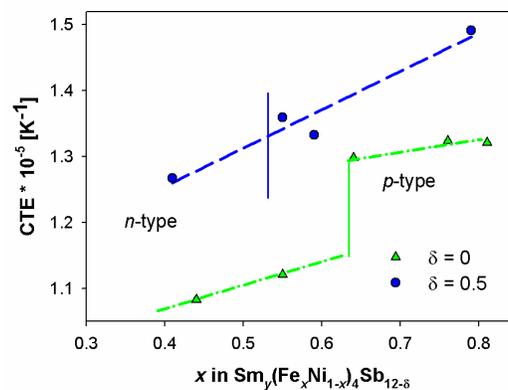


Figure 10. Trend of CTE as a function of x for the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{11.5}\text{Sn}_{0.5}$ and $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ systems. The dashed blue line is a regression line, while the dash-dot green lines are guides for the eye. Vertical lines separate n - from p -compositions for both systems; their position relies on structural data. Error bars are hidden by data markers; the data of the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{12}$ system are taken from ref. [61].

5. Conclusions

A compositional and crystallographic study was performed on several samples belonging to the $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{11.5}\text{Sn}_{0.5}$ system, due to its potential interest as a thermoelectric material. The composition was optimized by determining the experimental y value (i.e., the Sm content) corresponding to each x (i.e., the Fe content).

The crystallographic investigation performed on the filled skutterudite phase allowed us to draw the following conclusions.

- Relying on the refined Sm amounts, the p/n crossover is expected to be located at $x \sim 0.53$, meaning that the p -region is enlarged with respect to the Sn-free system.
- No slope change is observed in the trend of the skutterudite cell parameter *vs.* x in correspondence of the p/n crossover at any considered temperature.
- A much smaller CTE mismatch is revealed between p - and n -compositions in the present system than in the Sn-free one, which makes $\text{Sm}_y(\text{Fe}_x\text{Ni}_{1-x})_4\text{Sb}_{11.5}\text{Sn}_{0.5}$ a promising thermoelectric material in terms of mechanical properties.

Supplementary Materials: The following are available online at www.mdpi.com/2075-4701/10/5/692/s1: Rietveld refinement plots.

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