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Two Classes of Gamma-ray Bursts Distinguished within the First Second of Their Prompt Emission

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Abstract: Studies of Gamma-Ray Burst (GRB) properties, such as duration and spectral hardness, have found evidence for additional classes, beyond the short/hard and long/soft prototypes, using model-dependent methods. In this paper, a model-independent approach was used to analyse the gamma-ray light curves of large samples of GRBs detected by BATSE, *Swift*/BAT and *Fermi*/GBM. All the features were extracted from the GRB time profiles in four energy bands using the Stationary Wavelet Transform and Principal Component Analysis. *t*-distributed Stochastic Neighbourhood Embedding (*t*-SNE) visualisation of the features revealed two distinct groups of *Swift*/BAT bursts using the T_{100} interval with 64 ms resolution data. When the same analysis was applied to 4 ms resolution data, two groups were seen to emerge within the first second (T_1) post-trigger. These two groups primarily consisted of short/hard (Group 1) and long/soft (Group 2) bursts, and were 95% consistent with the groups identified using the T_{100} 64 ms resolution data. Kilonova candidates, arising from compact object mergers, were found to belong to Group 1, while those events with associated supernovae fell into Group 2. Differences in cumulative counts between the two groups in the first second, and in the minimum variability timescale, identifiable only with the 4 ms resolution data, may account for this result. Short GRBs have particular significance for multi-messenger science as a distinctive EM signature of a binary merger, which may be discovered by its gravitational wave emissions. Incorporating the T_1 interval into classification algorithms may support the rapid classification of GRBs, allowing for an improved prioritisation of targets for follow-up observations.

Keywords: gamma-ray burst; feature extraction; machine learning



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1. Introduction

Gamma-Ray Bursts (GRBs) are traditionally classified based on their duration and hardness as short/hard or long/soft bursts. These classes are separated at $T_{90} \approx 2$ s, derived from the duration distribution of the Third BATSE catalogue [1]. T_{90} is defined as the duration during which 5–95% of the counts above background are detected. The properties of these classes suggest different progenitors—long GRBs often lie in star-forming galaxies [2] and some long GRBs are associated with Type Ic supernovae [3–6] linking them to the deaths of massive stars [7]. Short GRBs are linked to compact object mergers [8,9], as some short GRBs have been identified near elliptical galaxies [10], and many are offset from their hosts [11,12]. The detection of GRB 170817A [13,14], associated with the neutron star merger GW170817, detected in gravitational waves by LIGO [15], lends further weight to this progenitor theory.

The classification of GRBs based on their duration is affected by the significant overlap between the duration distributions of the long and short groups, and is further complicated by a possible ‘intermediate’ class of GRBs, first identified through Gaussian fits to the duration distribution of GRBs in the third BATSE catalogue [16]. Clustering of the duration–hardness plane and multi-dimensional analyses of GRB samples from different satellites have also revealed evidence of more than two classes of bursts.

Salmon et al. [17] presents a review of previous studies and reports on an updated clustering analysis of *Swift*/BAT and *Fermi*/GBM bursts which finds that Gaussian models applied to *Swift*/BAT and *Fermi*/GBM GRB samples recover three clusters, including an intermediate-duration one. However, the latter is identified as an excess Gaussian component when an entropy criterion is used and the resulting best-fit solution contains two classes, which are broadly consistent with the typical short- and long-duration groups. A key conclusion of the analysis is that model-based methods may identify spurious components in one-, two- and multi-dimensional analyses of GRB samples and that model-independent analyses of GRBs should be conducted, for example, using GRB light curves.

Short GRBs with extended emissions have been detected, which may form an additional sub-class [18–20] and are possibly associated with a magnetar central engine [21]. These episodes, combined with the late X-ray flares in some short GRBs, and the non-detection of supernovae associated with some long GRBs, led to the suggestion of a new classification scheme by Zhang et al. [22]. Type I (massive star/collapsar origin) and Type II (compact-object merger origin) bursts are defined by multiple observational criteria beyond duration and hardness [23]. Other classification methods, based on afterglow and host galaxy properties [24], minimum variability timescales [25] and prompt emission and energetics, have been defined [26–30]. The instrument, sample size and classification method used can lead to different results [31], and the collapsar/merger fractions for each instrument's sample cannot simply be defined by a $T_{90} = 2$ s threshold [32].

Analysis of GRB light curves in several bands does not rely on summary statistics, such as parameters derived from spectral fits, which could be poorly fit or incorrect. Jespersen et al. [33] extracted features from 64 ms-resolution *Swift*/BAT light curves using Discrete Fourier Transforms and found two groups using t-distributed Stochastic Neighbourhood Embedding (t-SNE). This approach does not assume the underlying distribution of the variables, unlike model-based clustering and distribution fitting.

An alternative to Fourier analysis is wavelet analysis, which has been used to study non-stationary time-series [34]. Wavelet analysis has the advantage of extracting both frequency and temporal information, and for this reason it has been used to compress and de-noise GRB light curves for the study of their time evolution [35–37], to identify peaks [38–41], and to quantify the minimum variability timescale of GRBs [42–46]. Wavelet decomposition has been used to reduce the dimensionality of supernova light curves for classification [47], and has been combined with Principal Component Analysis (PCA) and t-SNE for classification [48,49]. Lochner et al. [48] found that classifiers performed better when supplied with wavelet coefficients of supernova light curves, in contrast to feature extraction using parametric models.

GRB pulses exhibit spectral evolution, including hard-to-soft [50] or intensity-tracking [51] behaviour. Other common features of all GRB pulses include longer-observed durations at lower energies [52] and asymmetric shapes [53,54]. These commonalities suggest that a similar emission mechanism creates GRB pulses, regardless of the progenitor [55,56].

However, pulses in short and long bursts also exhibit some differences. Long GRB pulses are observed to peak earlier at higher energies, but these spectral lags are not typically significant in short GRBs [18,54,57–63]. The minimum variability timescales [44–46] retrieved from wavelet analysis of long and short GRBs are ~ 200 ms and ~ 10 ms respectively. Hakkila and Preece [64] found that pulses in short GRBs are shorter and harder than long GRBs, and exhibit more spectral evolution. Coupled with the observation that shorter pulses have a higher peak flux and $\sim 90\%$ of short GRBs consist of a single pulse, compared to 25–40% for long GRBs, the pulse properties are likely to be a distinguishing feature in the first seconds of a burst. In particular, spectral evolution is evident at early times in previous studies of bursts from BATSE [65–70], *Swift* [71] and *Fermi*/GBM [72–74].

Redshift effects have not been observed in GRB light curves, as the standard time dilation of GRB pulses is thought to be masked by a contrasting effect whereby only the shorter, brightest portion of the burst is observed [75]. Therefore, analysis of GRB light curves is unlikely to be strongly affected by cosmological effects [76].

In this work, the light curves of GRBs in four energy bands from three different instruments are analysed, using wavelets as a feature-extraction method. The T_{100} burst intervals, during which 100% of the counts above background is recorded, are studied at 64-ms resolution, and the early phase of GRB emission (first few seconds) at 4-ms resolution. Wavelet coefficients are extracted and reduced and then visualised using PCA and t-SNE. Section 2 outlines the sample construction, while Section 3 provides details of the methods applied to perform feature extraction. Results are presented in Section 4 and consistency checks with other studies and between instrument samples are discussed in Section 5. The classification of notable GRBs is presented in Section 6. Possible signatures in the first second are discussed in Section 7, while conclusions are outlined in Section 8.

2. GRB Light Curves

The analysed GRB samples include bursts detected by the BATSE instrument on the *Compton Gamma-Ray Observatory* [77], the Burst Alert Telescope (BAT) on the *Neil Gehrels Swift Observatory* (hereafter *Swift*/BAT; Gehrels et al. [78]) and the Gamma-ray Burst Monitor (GBM) on the *Fermi Gamma-ray Space Telescope* (hereafter *Fermi*/GBM; Meegan et al. [79]).

2.1. BATSE

The BATSE 64 ms-binned light curves were stored as ascii files on the BATSE Public Data Archive (<https://heasarc.gsfc.nasa.gov/FTP/compton/data/batse/trigger/>, accessed on 17 February 2021). There were 2704 bursts in the final BATSE catalogue from 21 April 1991 to 17 August 2000, and 1956 light curves at 64 ms resolution were available. Background subtraction was applied via polynomial fits to the 64 ms light curves pre- and post-burst. The BATSE 4 ms-binned light curves were generated using the TTE files for individual bursts in the BATSE Public Data Archive, which stores 1732 TTE files, 1721 of which have successful background subtraction. The count rate was divided by the number of triggered detectors to obtain light curves measured in counts $s^{-1} \text{det}^{-1}$. The resulting light curves were stored in the four standard BATSE bands (20–50 keV, 50–100 keV, 100–300 keV and >300 keV).

2.2. Swift/BAT

The *Swift*/BAT Gamma-Ray Burst Catalogue (<https://swift.gsfc.nasa.gov/results/batgrbcatalog/>, accessed on 29 January 2021) hosts ascii files containing the 64 ms- and 4 ms-binned background-subtracted light curves. There were 1388 GRBs detected between 17 December 2004 and 28 August 2020 in this catalogue, which was extended from the Third *Swift* BAT Catalogue [80]. 1273 light curve files were available at 4 ms resolution, containing four background-subtracted light curves, corresponding to four bands (15–25 keV, 25–50 keV, 50–100 keV and 100–350 keV) in units of counts $s^{-1} \text{det}^{-1}$. Twenty-two bursts with no documented duration (T_{90}) were removed from the sample. At 64 ms resolution, light curves were available for the same set of bursts, with three additional GRBs added to the sample.

2.3. Fermi/GBM

Fermi/GBM light curves were generated from TTE data in 64 ms and 4 ms bins using the *Fermi*-GBM Data Tools [81]. A total of 3000 bursts from 10 August 2008 to 17 March 2021 were included, with 2678 successful background subtracted light curves created. Only triggered detectors were used, and the background intervals defined in the *Fermi*/GBM catalogue were used for background subtraction. Count rates were transformed to counts $s^{-1} \text{det}^{-1}$ by normalising according to the number of triggered detectors. Unlike *Swift* and BATSE, *Fermi*/GBM does not have defined light curve bands. Thus, they were chosen to capture the energy ranges of the NaI and BGO detectors, and the bands were considered in hardness ratio calculations. Four energy bands were considered: the *Fermi* trigger band (50–300 keV), the lower energy band used in hardness ratio calculations (8–50 keV), the energy range of the NaI detectors (8–1000 keV) and the higher energy range of the BGO

detectors (>1000 keV). The effect of the choice of these bands was studied by repeating the analysis of light curves within the four *Swift* bands, which was shown to produce similar results.

3. Feature Extraction

The feature extraction algorithm consists of multiple steps, which are outlined in Figure 1 for the analysis of light curves in the T_{100} interval at 64 ms resolution. Light curves were first pre-processed, before Stationary Wavelet Transform was applied. PCA was used to reduce the dimensionality of the resulting coefficients before visualisation with a t-SNE map. Figure 2 depicts the steps that were followed for the analysis of the first second of prompt emission. This section outlines the details of each step in the feature extraction algorithm.

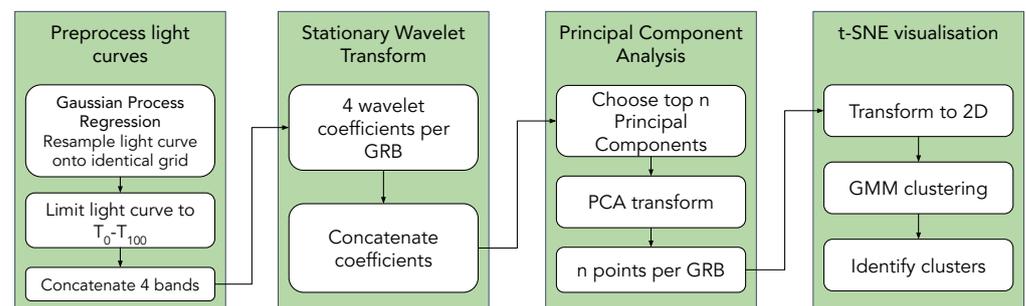


Figure 1. Flowchart of the feature extraction and clustering algorithm for analysis of 64 ms-binned light curves in the interval T_0 to T_{100} .

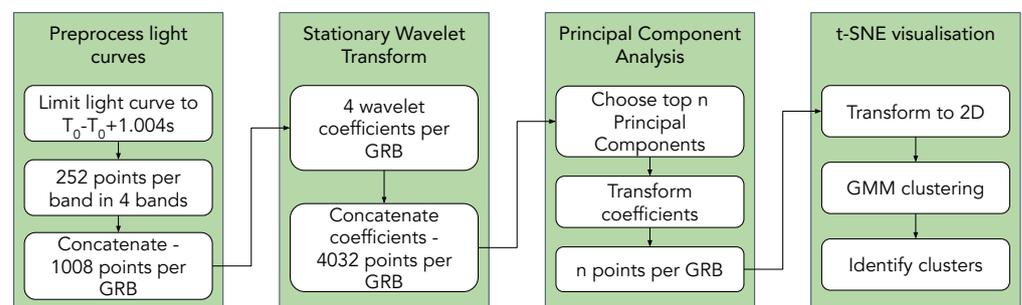


Figure 2. Flowchart of the feature extraction and clustering algorithm for analysis of light curves in the interval T_0 to $T_0 + 1.004$ s.

3.1. Light Curve Pre-Processing

3.1.1. 64 ms Light Curves

To obtain counts recorded at identical times relative to the trigger time for each light curve, BATSE and *Swift*/BAT light curves were modelled and resampled onto an identical grid using Gaussian Process Regression (GPR), a machine learning method that uses the input data to infer the function and explain the observations [82]. Gaussian processes model observations function as joint multivariate normal distributions, which can be fully specified by a mean function and covariance matrix. GPR determines the mean function and the entries of the covariance matrix using a user-specified covariance function (kernel). Hyperparameters of the kernel were optimised to maximise the marginal likelihood of the data under the Gaussian process prior.

The Gaussian Process model was implemented using the GPFlow library in Python [83], which originates from GPy but is built on TensorFlow [84]. A heteroscedastic regression model was used, which incorporates uncertainty in each point into the interpolation process by applying less weight to points with greater uncertainty. The radial-basis function

kernel (also known as squared exponential kernel) was used, as it is infinitely differentiable and produces smooth functions. The Adam and natural gradient optimisers were used to converge to the best-fit hyperparameters. The resulting equally spaced, evenly sampled 64 ms light curves were zero-padded beyond T_{100} to ensure noise was discarded. The T_{100} interval was extracted from the GRB catalogues. The four-band light curves were concatenated together and input to the feature extraction algorithm depicted in Figure 1.

3.1.2. 4 ms Light Curves

Wavelet decomposition requires a time series of equal and even lengths. At 4 ms resolution, the light curves were restricted to even-length time intervals starting at T_0 , the burst start time documented in the GRB catalogues. Light curves spanning different intervals were created and extended in intervals of 0.1 s until $T_0 + 3$ s. Many of the BATSE TTE datasets did not extend past 3 s, and BATSE light curves were zero-padded if they did not extend to the specified interval. For each GRB, the light curves in the four energy bands were concatenated together to form one vector to be input to the feature extraction algorithm, depicted in Figure 2 for the case in which light curves between T_0 and $T_0 + 1.004$ s were studied.

3.2. Wavelet Decomposition

Fourier analysis is often used to examine the frequency composition of signals and to extract features from time series (e.g., Jespersen et al. [33]). However, a drawback of Fourier transforms is the loss of temporal information and the stringent sine and cosine basis functions. Wavelets are more suited to the analysis of images, music and transient events, as they overcome the limitations of Fourier analysis by encoding both time and frequency information in the basis function [85]. The Stationary Wavelet Transform (SWT), also known as the \acute{A} Trous algorithm [86], is a shift-invariant transform, which convolves a signal with scaled and shifted versions of the basis wavelet function. The shift-invariance feature of the SWT has made it a popular method for pattern recognition [87,88]. The SWT returns two coefficients, known as Approximation and Detail coefficients, of equal length to the input signal. The coefficients are computed using a filter-bank algorithm [34] with low- and high-pass filters, which decomposes the input signal. Multiple levels of decomposition can be performed, whereby the output of the low-pass filter is successively fed to the next decomposition level.

The `pywt.swt` function of the PyWavelets package [89] was applied to the light curve vectors using the `symlet` family of wavelets, which is a more symmetric version of the Daubechies wavelet family [90], but other wavelet families produce similar results. A two-level decomposition was performed, resulting in four components of equal length to the vector containing the light curves in four bands (Figure 2). These were concatenated into one vector for each GRB prior to dimensionality reduction.

3.3. Principal Component Analysis

After performing a two-level wavelet decomposition, the dataset for each GRB increased in length by a factor of four. A dimensionality reduction technique was used to extract only the most significant information encoded in the wavelet coefficients. PCA is a form of decomposition, which extracts uncorrelated Principal Components from correlated data via an orthogonal transformation [91,92]. PCA involves eigenvalue decomposition of the covariance matrix of the input wavelet coefficient data. The eigenvectors are sorted by the magnitude of their eigenvalues. The user must choose how many eigenvectors to keep based on the percentage of variance explained by each eigenvector. The chosen eigenvectors represent the original data in a new PCA reference frame and are known as the Principal Components (PCs). The matrix of PCs is used to project the wavelet coefficients onto the lower-dimensional PCA space.

In this work, PCA was carried out using the `sklearn.decomposition.PCA` function. For *Swift*/BAT, the components whose cumulative variance reached >70% were chosen as

the new representation of the dataset, as the number of components required to meet >90% was large. For BATSE and *Fermi*/GBM, the number of retained components ensured that >90% of the variance was captured.

3.4. t-SNE

The chosen PCA components require transformation to a 2D space so that features can be visualised. Stochastic Neighbourhood Embedding (SNE; Hinton and Roweis [93]) provided a 2D visual representation of the components on arbitrary axes by computing the probability that each point is a neighbour of another point. This used a Gaussian probability density and Kullback–Leibler minimisation [94] to ensure that the low-dimensional space adequately represented the high-dimensional space. A user-specified parameter called Perplexity specified the importance of local or global structure. In general, the Perplexity can be considered representative of the number of nearest neighbours of each point.

t-SNE (t-distributed SNE; Maaten and Hinton [95]) used a Student t-distribution with a single degree of freedom, replacing the Gaussian comparison between points. The `sklearn.manifold.TSNE` method was used with a Perplexity, which maximises the separation of clusters in the final representation. In this case, the smaller *Swift*/BAT sample was analysed with a Perplexity of 40, while for the larger samples of BATSE and *Fermi*/GBM, Perplexities of 50 and 70 were used, respectively. The result is a 2D representation of the PCA feature space, in which similar light curves were grouped together.

3.5. GMM Clustering

Finally, Gaussian Mixture Model (GMM)-based clustering was applied to the t-SNE plots to identify clusters using the `MCLUST` package in R [96,97]. GMM clustering assumes that the observed data are generated from a mixture of K components, where the density of each component is described by a multivariate Gaussian distribution. `MCLUST` applies 14 different models and chooses the best-fit model and number of clusters based on the Bayesian Information Criterion (BIC; Schwarz et al. [98]). Since the underlying distributions are non-Gaussian, clusters are combined using the `clustCombi` function to converge on the optimum number of clusters, calculated via an entropy criterion [99].

4. Results

The results obtained by analysing GRB light curves, as described in Section 3 for the T_{100} intervals at 64 ms resolution, and for the first three seconds post-trigger at 4 ms resolution, are presented.

4.1. 64 ms Results

The t-SNE plots, coloured by burst duration (T_{90}), are shown in Figure 3 for the T_{100} intervals of bursts from BATSE, *Swift*/BAT and *Fermi*/GBM. t-SNE plots produce a mapping onto an arbitrary space, whereby the scale of the axes have no units or physical meaning. Thus, the t-SNE plots presented in this paper do not label the X and Y axes, and the precise position of points along the axes is not significant. However, the structure within the t-SNE space is significant and is identified. A separate group of shorter-duration bursts is evident in Figure 3b for *Swift*/BAT, while for BATSE and *Fermi*/GBM, the separation is not as clear.

GMM clustering, applied to the t-SNE map for *Swift*/BAT (Figure 3b), identified four clusters of bursts. However, the distribution is complex and is likely unsuitable for model-based clustering. When coloured by duration, it is clear that two groups of bursts were identified within the T_{100} intervals of *Swift*/BAT light curves: one consisting primarily of short bursts and a larger group of longer duration bursts.

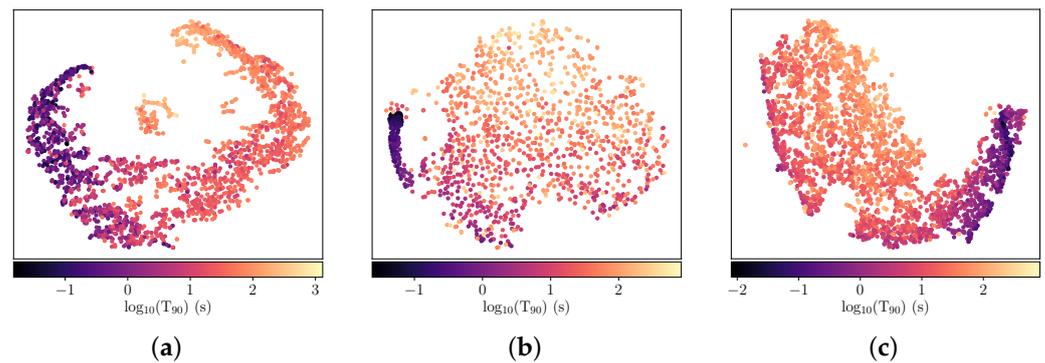


Figure 3. 2D t-SNE representation of the extracted wavelet and PCA features from the 64 ms light curves from T_0 to T_{100} , coloured by burst duration T_{90} , for (a) BATSE, (b) *Swift*/BAT and (c) *Fermi*/GBM.

4.2. 4 ms Results

The t-SNE plots from the analysis of the 4 ms light curves are shown in the animations in Figure 4, coloured by burst duration (T_{90}). The video animations are available to download in the Supplementary Materials. The intervals shown in each iteration of the t-SNE plot increase by 0.1 s, starting from the burst trigger time, T_0 . For *Swift*/BAT, a small group of shorter-duration bursts, begins to form and separate from the larger group of longer bursts within $T_0 + 0.2$ s. This shorter group of bursts grows and detaches from the longer group by T_0 to $T_0 + 1.004$ s, remaining detached up to the first 3 s post-trigger, which is the maximum interval available at 4 ms resolution. For BATSE and *Fermi*/GBM, the distinction between groups is not as clear, but a similar pattern is observed—a group of shorter bursts begins to form at $\sim T_0 + 0.2$ s and grows, separating itself from the larger, longer-duration group. We conclude that the time at which the two clusters of bursts become clearly separated is $T_0 + 1.004$ s.

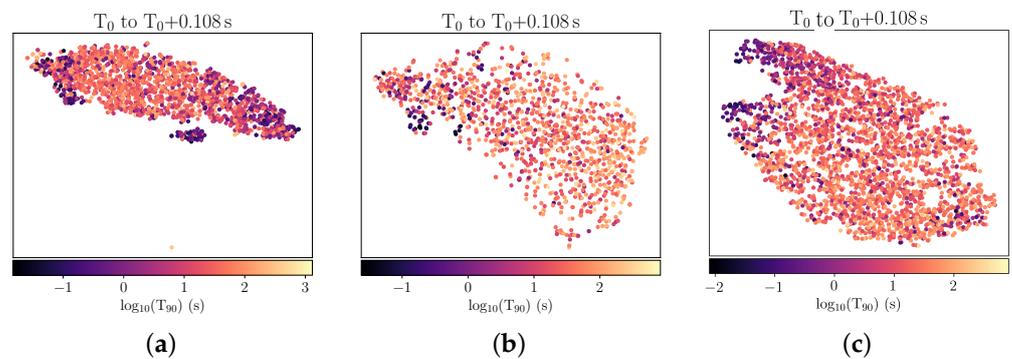


Figure 4. Animation of t-SNE projections for different GRB light-curve time-intervals at 4 ms resolution for (a) BATSE (b) *Swift*/BAT and (c) *Fermi*/GBM, coloured by their T_{90} duration. The title indicated on the top axis of each figure denotes the analysed time interval, since the burst trigger. The video files are available in the Supplementary Materials.

4.3. Properties of GRB Clusters Identified in the First Second Post-Trigger

2D t-SNE representation of the extracted wavelet and PCA features from the first second (T_0 to $T_0 + 1.004$ s) of GRB light curves, coloured by burst duration T_{90} and hardness ratio HR_{32} for BATSE, *Swift*/BAT and *Fermi*/GBM, are shown in Figure 5. The projections indicate the presence of two groups of bursts, which can be seen clearly in Figure 5b for *Swift*/BAT. For BATSE (Figure 5a) and *Fermi*/GBM (Figure 5c), this separation is less well-defined.

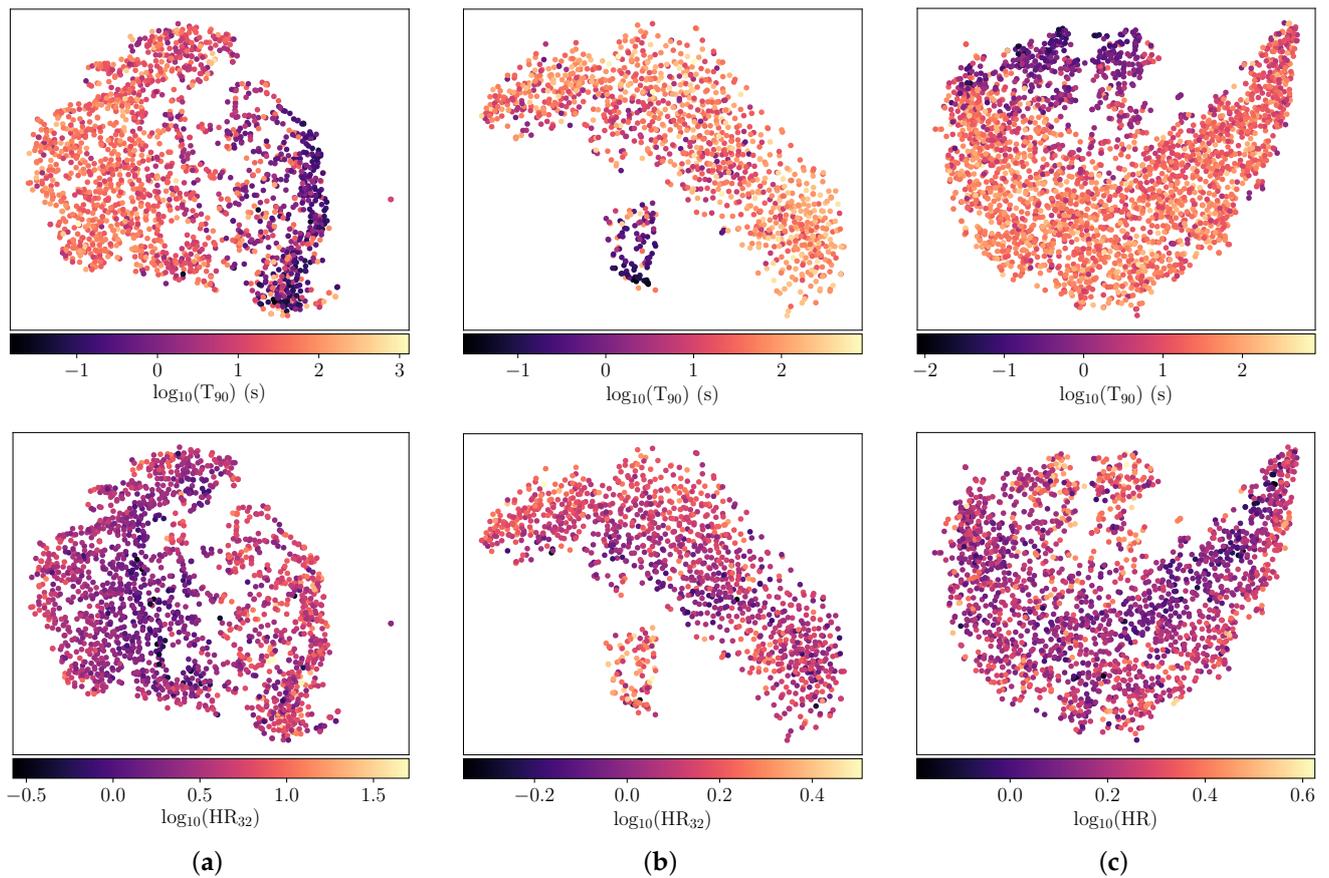


Figure 5. 2D t-SNE representation of the extracted wavelet and PCA features from the first second (T_0 to $T_0 + 1.004$ s) of burst light curves, coloured by burst duration T_{90} (top row) and hardness ratio HR_{32} (bottom row) for (a) BATSE, (b) *Swift*/BAT and (c) *Fermi*/GBM. Hardness ratios (HR_{32}) for *Swift*/BAT and BATSE are calculated as the ratio of fluence in Band 3 and Band 2. The hardness ratio of *Fermi*/GBM bursts is defined as the ratio of fluence in the 50–300 keV and 10–50 keV bands, calculated using the best-fit spectral parameters.

GMM clustering applied to the *Swift*/BAT projection identifies two separate groups, shown in Figure 6a. The group consisting of mostly short/hard bursts is labelled Group 1, and the larger, longer-duration group is denoted Group 2. The groups are shown projected onto the duration-hardness plane in Figure 6b.

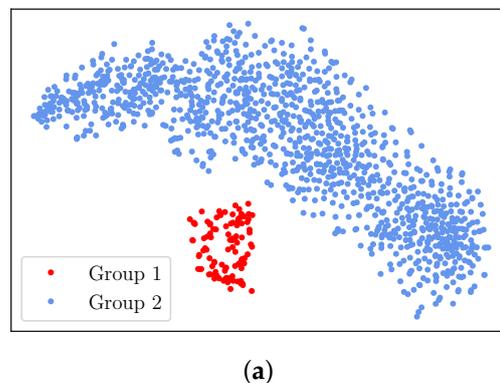


Figure 6. Cont.

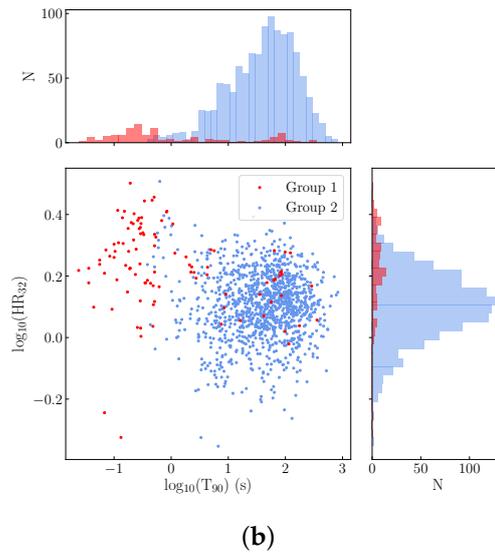


Figure 6. (a) The t-SNE map of *Swift*/BAT bursts derived from the T_0 to $T_0 + 1.004$ s interval at 4 ms resolution showing 2 clearly separated groups and (b) their projection onto the duration-hardness plane. Histograms indicate the distribution of duration and hardness for each group.

Two-dimensional Kolmogorov–Smirnov (KS) tests applied to Group 1 and Group 2 verify that there are statistically significant differences in GRB properties such as the duration (T_{90}), hardness (HR_{32}), peak energy (E_{peak}) and fluence (S) of the two clusters. Table 1 presents the results of the KS test. The probability (p -value) presented in Table 1 indicates the probability that Groups 1 and 2 are drawn from the same distribution. This hypothesis is rejected, as all probabilities are below 1%. Figure 7 demonstrates the distribution of the GRB properties for Group 1 and Group 2.

Table 1. Results of the 2D KS test comparing Group 1 and Group 2 identified within the first second of prompt emission of *Swift*/BAT bursts.

Parameter	p -Value
T_{90}	4.3×10^{-42}
HR_{32}	1.7×10^{-19}
E_{peak}	1.9×10^{-3}
Fluence (15–350 keV)	2.9×10^{-22}

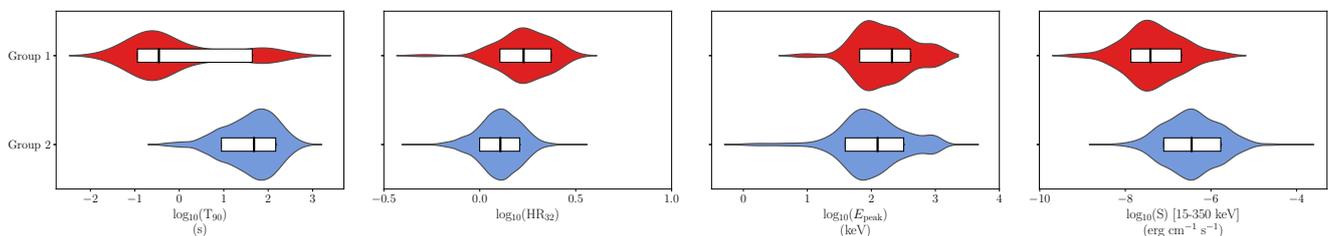


Figure 7. Violin plots showing the distribution of GRB properties for Group 1 (red) and Group 2 (blue) *Swift*/BAT bursts identified in the T_0 to $T_0 + 1.004$ s light curve interval. The white box plots represent the 1σ interval (i.e., the 16th to 84th percentile), with the median of each parameter marked as a black line.

Table 2 lists the cluster memberships of a subset of the *Swift* GRBs for both the analysis of the T_{100} interval at 64 ms resolution, and the interval from T_0 to $T_0 + 1.004$ s at 4 ms resolution. The full table is available to download from the Supplementary Materials. When the first 1 s of prompt emission is considered, Group 1 contains 107 bursts, 73 of

which are short-duration ($T_{90} < 2$ s). There are 1144 bursts in Group 2, containing 1112 long-duration bursts ($T_{90} > 2$ s). The composition of each group and the properties of GRBs in Groups 1 and 2 are further discussed in Section 5.

Table 2. Group membership of *Swift* GRBs, based on the analysis of the first second of prompt emission at 4 ms resolution (T_1) and the T_{100} interval at 64 ms resolution. The full table is provided in the Supplementary Materials.

GRB	T_1 Group	T_{100} Group	T_{90} (s)	HR ₃₂
GRB041220	2	2	5.6	1.3
GRB041223	2	2	109.1	1.8
GRB041224	2	2	177.6	1.2
...
GRB200809B	... ¹	2	4.2	1.8
GRB200819A	2	2	26.9	1.0
GRB200829A	... ¹	2	13.1	1.9

¹ No 4 ms light-curve file available.

As with the T_{100} analysis (Section 4.1), the results obtained for the T_0 to $T_0 + 1.004$ s interval at 4 ms resolution for BATSE and *Fermi*/GBM GRBs are not as clear-cut as they are for *Swift*/BAT. In the case of BATSE, GMM clustering with MCLUST identifies six clusters within the t-SNE projection in Figure 5a. However, we can tentatively identify two clusters of bursts for BATSE by eye. These two groups resemble the short/hard and long/soft groups identified for *Swift*/BAT. Similarly to *Swift*/BAT, a KS test applied to the two BATSE groups reveals significant differences in their duration, hardness, peak energy and peak flux. BATSE has a harder energy range than *Swift*/BAT; thus, the BATSE population contains more short/hard bursts. Therefore for BATSE, the short-duration Group 1 contains a larger proportion of bursts compared to *Swift*/BAT.

For *Fermi*/GBM, the projection in Figure 5c indicates two groups, primarily consisting of short/hard and long/soft bursts, but their clustering is not dense enough to allow for a clean separation between them. MCLUST identifies five clusters. This may indicate that the application of a Gaussian model does not adequately represent the underlying complex distributions [17].

5. Consistency Checks

The analysis of the first second of prompt emission (T_1) identifies two groups of bursts within the BATSE, *Swift*/BAT and *Fermi*/GBM samples. We focus this discussion on the more clear-cut results obtained with *Swift*/BAT.

5.1. T_{100} vs. T_1 Analysis

For *Swift*/BAT, two groups are identified using both the T_{100} and T_1 intervals. Table 2 provides the classification results obtained with each interval. The sample sizes of the two groups are shown in Table 3, separated into long- ($T_{90} > 2$ s) and short- ($T_{90} < 2$ s) duration bursts.

Table 3. Sample sizes of short-duration ($T_{90} < 2$ s) and long-duration ($T_{90} > 2$ s) bursts in the *Swift*/BAT sample, and Groups 1 and 2, based on the analysis of the T_1 and the T_{100} intervals.

Sample	Number of Bursts					
	T_1	$T_{90} < 2$ s	T_{100}	T_1	$T_{90} > 2$ s	T_{100}
<i>Swift</i> /BAT sample	107		107	1144		1147
Group 1	73		91	32		14
Group 2	34		16	1112		1133

A total of 95% (1185 of the 1251 bursts) of the classifications of *Swift*/BAT bursts determined using the T_1 interval at 4 ms resolution are consistent with those derived using the T_{100} intervals at 64 ms resolution. There are 21 short-duration bursts, which are classified as Group 2 bursts when the T_1 interval is considered, but move to Group 1 when the T_{100} interval is used for the analysis. There are 28 long-duration bursts, which move from Group 1 in the T_1 analysis to Group 2 when the T_{100} interval is considered. These include five bursts in the list of *Swift*/BAT bursts with extended emission episodes compiled by Gibson et al. [100]. The long-duration supernova-accompanied burst GRB 101219B moves to Group 2 in the T_{100} analysis, correctly placing it amongst the other bursts with associated supernovae. The inclusion of the full light-curve data in these cases is important for correct classification. The classification of bursts with associated supernovae is further discussed in Section 6. Some of the movement between groups may reflect the different temporal resolutions used for the T_1 (4 ms) and T_{100} (64 ms) analyses. The minimum variability timescale with short GRBs of order 10 ms would not necessarily be captured by the T_{100} analysis. There may also be cases where there are pre-trigger emissions that are not captured in the current approach, which starts at the trigger time.

5.2. Inter-Comparison of *Swift*/BAT and *Fermi*/GBM Results

In all three GRB samples, clear evidence of a separation into two groups by the end of the first second was observed. The clean separation of bursts in the *Swift*/BAT sample indicates that the T_1 interval could potentially be used to classify GRBs independently of their T_{90} duration. The less clear-cut cluster separation found in the BATSE and *Fermi*/GBM samples most likely arose from instrumental differences (e.g., energy ranges, triggering methods and sensitivities). Of the three instruments, *Swift*/BAT has the largest effective area, and detects more spectrally softer, long-duration GRBs [101], and fewer short GRBs, than BATSE or *Fermi*/GBM [80,102].

A total of 293 bursts were analysed, which were detected by both *Fermi*/GBM and *Swift*/BAT. There is excellent (274/293) agreement between the two instruments in the cluster membership of these GRBs using the T_1 interval at 4 ms resolution. Differences in classification can primarily be attributed to the lack of clear separation between groups in the *Fermi*/GBM sample, which makes cluster identification less definitive than it is for *Swift*/BAT. In 6 of the 19 cases where cluster membership is found to disagree between the two detectors, significantly different (>50%) T_{90} durations are recorded by the instruments.

5.3. Time Intervals

The analysis was repeated for different intervals within the bursts to investigate the intervals in which classes may be identified in the *Swift*/BAT sample.

First, the feature extraction analysis with 4 ms resolution light curves was performed for the interval of $T_0 - 1$ s to $T_0 + 1$ s (Figure 8a). The addition of pre-trigger data is shown to produce almost identical results to those obtained by starting at T_0 . However, the analysis requires additional Principal Components to explain the variance, indicating that including 1 s of data before the trigger adds more noise than information. Secondly, when the selected interval is between $T_0 + 1.004$ s and $T_0 + 2.008$ s, the separation disappears, as shown in Figure 8b, indicating that the early prompt emission in the first second post-trigger is the key interval for separating the two classes.

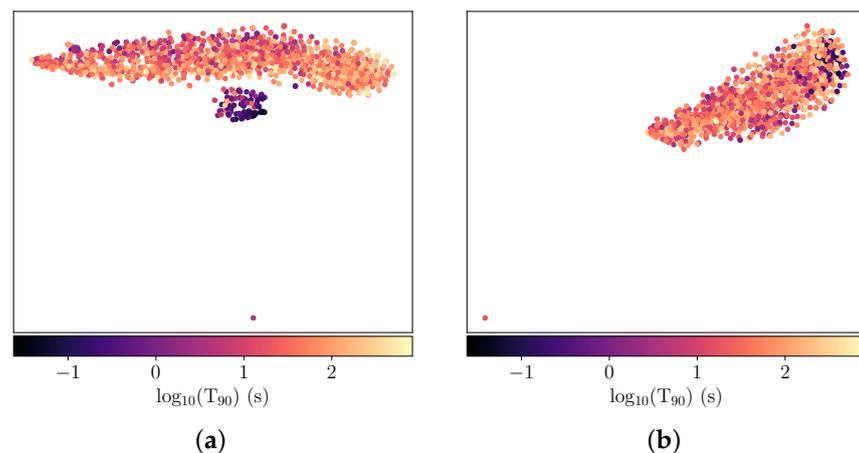


Figure 8. 2D t-SNE representation of the wavelet feature extraction applied to *Swift*/BAT light curves covering time intervals (a) $T_0 - 1$ s to $T_0 + 1$ s and (b) $T_0 + 1$ s to $T_0 + 2$ s. The plots are coloured by burst duration T_{90} .

5.4. Light Curve Classifications

In Salmon et al. [17], Gaussian Mixture Model-based clustering of the hardness- T_{90} plane identified two classes of bursts in the *Swift*/BAT and *Fermi*/GBM samples. The results suggest that the intermediate duration class may be an artefact of the application of unsuitable models, as was also suggested by Tarnopolski [25], Koen and Bere [103], Tarnopolski [104], Tarnopolski [105]. The results of the model-independent analysis of light curves presented in this paper and by Jespersen et al. [33] lend further support to this conclusion.

Jespersen et al. [33] found two distinct groups of bursts in their t-SNE map obtained from Fourier decomposition of full *Swift*/BAT light curves. The composition of the ‘type-S’ and ‘type-L’ groups from Jespersen et al. [33] are compared to the clusters found in this work. For the T_{100} interval, there is an agreement in classification for 96% of bursts, after removing bursts for which no light curve files are available. Although the same burst intervals are considered, Jespersen et al. [33] input flux-normalised light curves into a Fourier-based analysis, potentially leading to small differences in the resulting burst memberships compared to the wavelet-based analysis presented here. The light curves in this study were not flux-normalised, as the resulting t-SNE maps did not separate the groups.

More than 96% of the bursts classified using wavelets and the T_1 interval were found to match the membership assigned by Jespersen et al. [33] based on Fourier decomposition in the T_{100} interval. Eight of the 20 bursts found to be within Group 1 in this study, classified as type-L by Jespersen et al. [33], have extended emission episodes, which are not captured within the first second.

5.5. Collapsar ‘Contamination’

The fraction of *Swift*/BAT bursts within Groups 1 and 2 can be compared to the expected distributions that are specific to the *Swift*/BAT detector.

Bromberg et al. [32] quantified the contamination of short GRB samples by collapsar bursts by fitting the duration distribution of *Swift* bursts with a function representing the merger and collapsar duration distributions. The model is based on the plateau in the duration distribution for shorter durations than the jet breakout time, which is predicted by the collapsar model [106]. According to this model $\sim 40\%$ of *Swift*/BAT bursts with durations < 2 s are collapsar bursts. *Swift*/BAT is more sensitive to soft GRBs, meaning that low-fluence long GRBs contaminate the short GRB population to a greater extent than they do for BATSE ($\sim 10\%$) and *Fermi*/GBM ($\sim 15\%$).

There are 27 bursts for which Bromberg et al. [32] assigns a probability of being a non-Collapsar of $> 90\%$. The majority (23) of these are classified as Group 1 in this analysis,

indicating that Group 1 primarily consists of bursts arising from mergers. The collapsar (Group 2) contamination of *Swift*/BAT bursts with durations <2 s from our analysis of the first 1 s of prompt emission is 31.8%, or 34/107 bursts (Table 3), consistent within 1σ with the predictions in Bromberg et al. [32]. The collapsar contamination of short-duration bursts for the T_{100} analysis is significantly lower, at $\sim 15\%$. These results suggest that classification based on the T_1 interval may be useful for identifying collapsar ‘imposters’ in short GRB samples.

6. Notable GRBs

We discuss cluster membership for some notable GRBs. As a default, the discussion relates to the results obtained with the T_1 interval at 4 ms resolution unless otherwise indicated. We identify cluster membership for GRBs in any of the three analysed samples, which have associated kilonovae or supernovae. We note that cluster membership for the BATSE and *Fermi* samples is not as clear-cut as it is for the *Swift* sample, and the cut in t-SNE space is made by eye.

6.1. GRBs with Associated Supernovae

As discussed in Section 5.5, Group 2 is associated with collapsar bursts. Thus, it is expected that GRBs with associated supernovae will lie within Group 2. The list of 31 *Swift* and 10 *Fermi* Supernova (SN)-GRBs provided in Cano et al. [107] is extended to include additional SN-GRB events GRB 161219B/SN 2016jca [108], GRB 171205A/SN 2017htp [109], GRB 180728A/SN 2018fip [110,111], GRB 190114C/SN 2019jrj and GRB 190829A/AT2019oyw [112] and the peculiar short GRB 200826A [113–115]. Figure 9 indicates the location of these bursts within the t-SNE plot. The 25 SN-GRBs for which light curve files are available lie in Group 2 of *Swift*/BAT and *Fermi*/GBM, as expected, with the exception of GRB 101219B, which is an outlier to *Swift*/BAT Group 1 but lies within Group 2 of *Fermi*/GBM bursts. The analysis using the T_{100} interval correctly places GRB 101219B in Group 2 for *Swift*/BAT. The shortest collapsar burst detected to date, GRB 200826A, lies within Group 2 of the *Fermi*/GBM sample despite its observed duration of $T_{90} \approx 0.96$ s [115].

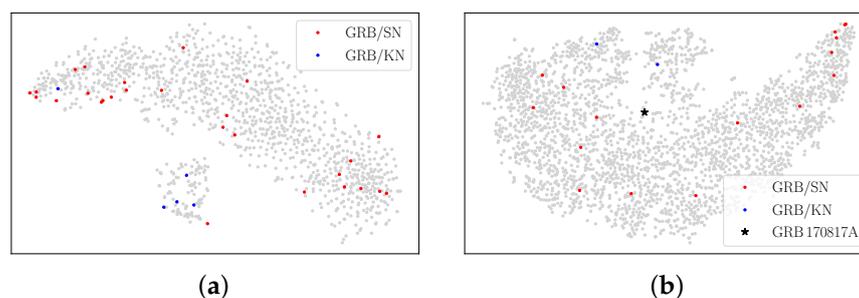


Figure 9. Locations of GRBs with associated Supernovae (GRB/SN) and possible Kilonovae (GRB/KN) within the t-SNE projections of the T_1 interval for (a) *Swift*/BAT and (b) *Fermi*/GBM. The location of the only confirmed kilonova, associated with GRB170817A, is indicated with a black star.

The remaining bursts are identified in Group 2, with their classifications unchanged by the interval used in analysis, with the exception of GRB 050824, which migrates to Group 1 when the T_{100} interval is used for analysis.

6.2. GRBs with Possible Kilonovae

The only confirmed kilonova is associated with GRB170817A, which is in the *Fermi*/GBM sample (Figure 9b) and does not clearly belong to either group. However, GRB 170817A was not a standard ‘short’ GRB, and would probably have been unremarked on if not for the associated gravitational wave source [13,14]. Near-infrared excesses, similar

to kilonova signatures, have been found in the afterglows of a handful of nearby short GRBs. Following detection in GRB 130603B [116,117], reanalysis of GRB 060614 [118,119], GRB 080503 [120] and GRB 050709 [121] revealed similar near-IR components. Since then, GRB 150101B [122], GRB 160821B [123–126] and GRB 200522A [127] have all been suggested as kilonova candidates.

Figure 9 shows that all the kilonova candidate bursts lie within Group 1 of *Swift* and *Fermi* GRBs, except for GRB 050709, for which no light curve file is available, and GRB 060614, which is in Group 2. GRB 060614 is an anomalous GRB with a short pulse followed by a longer period of soft flaring emission. Some properties of this burst are typical of the long GRB population [128], but the lack of supernova detection for this close burst ($z = 0.125$ Price et al. [129], Fugazza et al. [130]) and possible near-infrared excess led to the suggestion that this burst originates from a merger [22], or is within its own subclass [131–135]. Our results agree with the classification by Jespersen et al. [33], who place this burst in the longer-duration, collapsar group. When the T_{100} light-curve interval is considered, the classifications remain unchanged for the kilonova candidates, with the exception of GRB 080503, which moves to Group 2. This is an example of a GRB with a short initial spike and extended emission, which may be the result of a merger rather than a collapsar [120]. The T_1 interval appears to return the more appropriate classification in this case.

7. Discussion

Studies of GRB pulses at early times have revealed that the dominant radiation process is usually photospheric emission [136–141]. These thermal pulses exhibit significant spectral evolution, with bursts usually evolving to be dominated by synchrotron emission [137,139,142]. If this is the case, the first second of all GRBs should be dominated by thermal pulses; therefore, the radiation process is unlikely to be the driver of the observed differences in light curves that appear at early times.

The feature extraction algorithm may identify differences in the spectral evolution and pulse shapes of the two burst groups. The spectral lags of long and short bursts are different, with many short bursts exhibiting zero lag [18,63]. The minimum variability timescales for short and long bursts have also been found to be different [44–46]. For example Golkhou et al. [46] found median minimum variability timescales of 10 ms and 45 ms for short and long bursts, respectively. Hakkila and Preece [64] found that pulses in short GRBs are shorter and harder than those in long GRBs, and exhibit more rapid spectral evolution. Coupled with the observation that shorter pulses have a higher peak flux and ~90% of short GRBs consist of a single pulse, compared to 25–40% for long GRBs, pulse properties are likely to be a distinguishing feature in the first pulses and first seconds of a burst. Short GRBs have shorter pulse durations and their triple peaked substructure shows more intense precursor and decay peaks (on either side of the central peak) than long GRBs Hakkila et al. [56].

The magnitude of the PCA components in the different *Swift*/BAT energy bands indicate that Bands 2 and 3 contain the most variance; therefore, they are the most important for the 4 ms light curves. Figure 10 shows that the results of the feature extraction algorithm only applied to Band 3 data, showing that some segregation of the bursts into two groups is evident using light curves in one energy band. Thus, energy-dependent pulse characteristics are not the sole driver of the classification.

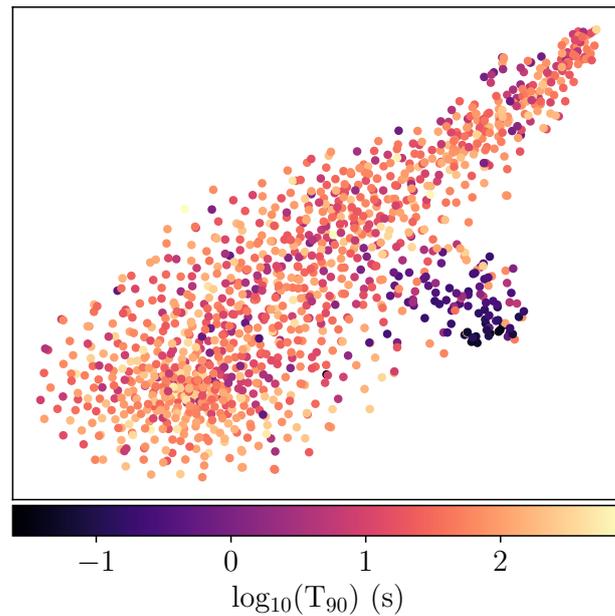


Figure 10. 2D t-SNE representation of the wavelet coefficients and PCA features extracted from the light curves measured in Band 3 for *Swift*/BAT (50–100 keV). The plot is coloured by burst duration T_{90} .

Cumulative Counts

Figure 6 shows that, for the *Swift*/BAT sample, Group 1 and Group 2 GRBs, identified within the T_1 interval, mostly consist of bursts from the classical short-duration ($T_{90} < 2$ s) and long-duration ($T_{90} > 2$ s) samples, respectively. However, there are some ‘strays’, as shown in Table 3 and discussed in Section 5.

The counts measured in Band 3 (50–100 keV) of the first second of *Swift*/BAT 4 ms light curves are summed and normalised by the number of light curves, to obtain an average cumulative counts measure for bursts in each group in Table 3 (Figure 11). The cumulative counts of Group 1 and Group 2 bursts track those of short and long GRBs, respectively, during the first second.

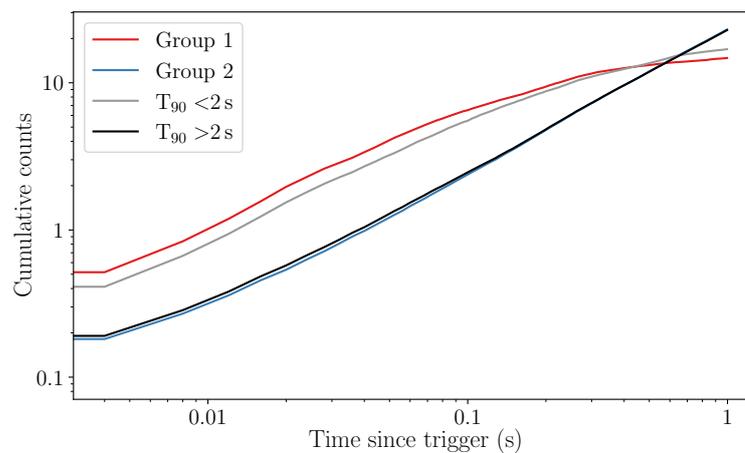


Figure 11. Normalised cumulative counts of Band 3 (50–100 keV) *Swift*/BAT 4 ms light curves. Short ($T_{90} < 2$ s) and long ($T_{90} > 2$ s) duration bursts, and those within the Groups 1 and 2 identified from the first 1 s of prompt emission, are shown.

The results of this analysis suggest that the behaviour of GRB pulses in the first second carries essential information, which is needed to classify GRBs in the vast majority of cases,

independent of their duration. The characteristics of the ‘long’ Group 1 and ‘short’ Group 2 bursts suggests that they have not been misclassified, but are duration outliers of their identified class. Group 1 and Group 2 bursts evolve in a similar way to the traditional short and long classes, respectively.

Previous studies have interpreted the cumulative GRB light-curves slope as a measure of the cumulative power output of the central engine [143]. Combined with the association of Group 1 and 2 bursts with kilonovae and supernovae, respectively (Section 6), the cumulative counts behaviour in the first second suggests that Group 1 and 2 represent distinct progenitors, namely, the merger and collapsar populations.

8. Conclusions

Wavelet decomposition, combined with PCA and t-SNE, provides an effective method for extracting the similarities between gamma-ray light curves from BATSE, *Swift*/BAT and *Fermi*/GBM. The features extracted from the T_{100} interval of light curves in four energy bands at 64 ms resolution reveal a separation between two groups of bursts. These groups are labelled Group 1 and Group 2. Two groups have also been identified through feature extraction from high resolution (4 ms) light curves within the first seconds of prompt emission. The shortest timescale at which this separation is clear is one second (T_1 interval).

The separation between groups is clearest for *Swift*/BAT and is less distinct for the BATSE and *Fermi*/GBM samples of bursts, perhaps due to instrumental effects. Despite the different timescales and resolutions that were studied, there is >95% agreement between the groups identified within the T_{100} and T_1 interval for *Swift*/BAT. The T_{100} interval is shown to produce different and more classical classifications for some bursts, especially those with long emission episodes. There is also >95% agreement between the results of the T_1 analysis with the results of the Fourier-based feature extraction of *Swift*/BAT light curves by Jespersen et al. [33]. The separation between *Swift*/BAT groups is clearest when all four energy bands are considered. However, energy-dependent characteristics are not the sole effect that drives the classification, as some separation can only be seen when one energy band is considered. Pulse shape and evolution may be important, and the accumulation of counts within the first second is found to be distinct between groups.

Group 1 mostly consists of short-duration, spectrally hard bursts. Group 2 mostly consists of spectrally soft, long-duration bursts. When segmented at $T_{90} = 2$ s, the traditional dividing line between long and short GRBs, we found that 99% (97%) of *Swift*/BAT Group 2 bursts have durations >2 s when the T_{100} (T_1) interval is used. A total of 32% of the 107 GRBs with $T_{90} < 2$ s are identified as Group 2 bursts when the T_1 interval is used, consistent (within 1σ) with a model in which the duration distribution of *Swift* bursts is fit with a function representing the merger and collapsar distributions, possibly reflecting the amount of collapsar ‘contamination’ in the short GRB sample. The observed contamination fraction is significantly lower (16%) when the T_{100} interval is used. Thus, the groups can be associated with distinct progenitors, namely, mergers and collapsars. GRBs with associated supernovae are within Group 2, while GRBs with suspected kilonovae lie in Group 1.

Previous studies found that the pulse and spectral properties of the early seconds of long GRBs are similar to those of short GRBs. In this analysis, no significant differences can be identified in pulse or spectral properties to account for Group 1 and Group 2 GRBs being distinguishable in the T_1 interval. Differences in minimum variability timescale, identifiable only when the 4 ms resolution data are used, may account for some of the observed behaviour. However, the two groups in subsequent 1 s intervals should also be evident, which is not the case. The observed different slopes in the first second between the two groups in the combined cumulative counts may point towards differences in the central engine.

The presented results indicate that the nature of a burst may be inferred from the earliest prompt emission, without considering the full burst duration. Prompt classification will be helpful in the era of ‘big data’ in time-domain astronomy. Gravitational wave detectors will detect mergers at increased rates in the near- and longer-term [144]. State-of-

the-art optical surveys such as the Vera Rubin Observatory will deliver an increased number of transient targets in the crowded optical sky [145]. While many optical transients are false positives, the rare gamma-ray transients can pinpoint the unambiguous target of interest. The early detection and classification of these gamma-ray transients will help to prioritise counterpart follow-up for optical telescopes and spectroscopic observations. Classification schemes and triggering algorithms could incorporate a wavelet-based analysis, such as that presented here, to prioritise targets for follow-up observations.

Supplementary Materials: The following are available online at <https://www.mdpi.com/article/10.3390/galaxies10040078/s1>. The electronic version of this article showcases Figure 4 as three mp4 animations of the t-SNE plots for BATSE, *Swift* and *Fermi*. We provide the full version of Table 2 which includes the classification of *Swift*/BAT GRBs using the first second of prompt emission.

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