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A Density Functional Theory Study on the Effect of Lattice Impurities on the Electronic Structures and Reactivity of Fluorite

Wei Jiang, Zhiyong Gao *, Wei Sun, Jiande Gao and Yuehua Hu *

School of Minerals Processing and Bioengineering, Central South University, Changsha 410083, China; jiangwei0425@csu.edu.cn (W.J.); sunmenghu@csu.edu.cn (W.S.); fyjgjd@163.com (J.G.) * Correspondence: zhiyong.gao@csu.edu.cn (Z.G.); huyuehuacsu@126.com (Y.H.)

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Abstract: Fluorite (CaF₂), a halogen elemental mineral, always co-exists with other minerals. The Ca element in fluorite is often replaced by rare earth elements (REEs), such as cerium (Ce) and yttrium (Y). In this work, the electronic structures of fluorite crystals containing REE (Ce, Th, U, and Y) impurities were studied by density functional theory (DFT). The calculated results showed that the presence of impurities increased the lattice parameter of fluorite. The impurities caused the Fermi level to shift towards the high energy direction, making the fluorite accept electrons more easily. The impurities except Y led to the occurrence of an impurities state in the valence band. The Mullinken population values of F–REE bonds were larger than that of F–Ca and F–F bonds, and F–Y bonds had the largest population value. Analysis of the frontier molecular orbital showed that the impurities contributed greatly to the lowest unoccupied molecular orbital (LUMO). The interaction between oleic acid and impurities-bearing fluorite were discussed. The results suggested that the incorporation of impurities would enhanced the reactivity of fluorite with oleic acid.

Keywords: impurity; fluorite; density functional theory; frontier molecular orbital; reactivity

1. Introduction

Fluorite (CaF₂) is an important ore of fluorine, and becomes a strategic resource reserve in many countries. Crystalline fluorite has a very low index of refraction and an unusual ability to transmit ultraviolet light. It is widely used in many industries, such as aluminum fluoride manufacturing, glass manufacturing, primary aluminum production, ceramic, enamels, and hydrofluoric acid. China, Mexico, Namibia, Kenya, and South Africa are the major producing and exporting countries [1].

Fluorite often coexists with other calcium-containing minerals such as calcite, gypsum, and francolite due to the similarity in their formation characteristics [2–4]. Separation of fluorite from its associated gangue minerals is commonly carried out by flotation [5,6]. The conventional collectors used in the flotation of fluorite ores are fatty acids (oleic acid, for example) and their salts [7].

Fluorite crystals exist in a variety of colors, ranging from colorless through white, yellow, green, and purple to blue, but purple is the most common [1]. The various colors of fluorite may be attributable to the different impurities in the fluorite crystal [8]. It is reported that REE, such as cerium (Ce) and yttrium (Y), can replace the calcium (Ca) in fluorite in a form of isomorphism [9]. When the amount of substitution reaches a certain value, the replaced fluorite is called yttrofluorite and cerfluorite. In addition, the ion radius of calcium (1.06 Å) in fluorite (CaF₂) crystal is very close to 1.10 Å of thorium (Th) and especially 1.05 Å of tetravalent uranium (U) [8,10]. It can be found that U and Th replace Ca in fluorite crystal in some scenarios. Lattice defects may change the Fermi energy, frontier orbital, and electronic structure of minerals which exert a considerable influence on the

surface properties of minerals [11,12]. It is tenable to infer that, the incorporation of impurities such as Ce, Th, U, and Y in the fluorite crystal may lead to the different floatability of fluorite.

So far, the study about the impact of impurity defects on the flotation performance has been mainly focused on sulfide ores by density functional theory (DFT) calculations. Ye et al. investigated the effect of three typical impurities (iron, copper, and cadmium) on the flotation behavior of sphalerite [13]. They also studied the electronic structures of bulk sphalerite containing 14 typical kinds of impurities by [14]. Li et al. calculated the electronic property of pyrite crystals containing As, Se, Te, Co, or Ni atoms. The results showed that pyrite containing As, Co, or Ni was easier to oxidize by oxygen than pyrite containing Se or Te, and pyrite containing Co or Ni had greater interaction with xanthate [15]. Chen et al. investigated the adsorption of oxygen molecules (O₂) on galena (100) surfaces containing Ag, Cu, Bi, and Mn impurities and found that the impurities could change the semiconductor electronic structure of galena surface and influence the adsorption of oxygen molecules [16].

However, few theoretical studies concerning the influence of impurities on the surface properties of fluorite crystals have been published. In this study, the electronic structures of fluorite bearing Ce, Th, U, and Y impurities were studied by DFT calculations, and the influence of impurities on the reactivity of fluorite was predicted. The findings in the effect of these impurities on the electronic structure and reactivity of fluorite would help solve some encountered problems in fluorite flotation practice.

2. Computational Details

The lattice parameter of fluorite crystal was obtained from the literature [17]. The symmetry group of fluorite crystal is FM-3M. The unit cell consists of eight F atoms and four Ca atoms, and the cell parameters are a = b = c = 5.4631 Å and $\alpha = \beta = \gamma = 90^{\circ}$. By replacing one Ca atom by an impurity REE atom, a crystal structure of impurity-bearing CaF₂ was produced. The models of the fluorite supercells are shown in Figure 1.



Figure 1. Models of (a) perfect and (b) impurity-bearing fluorite crystals.

All of calculations in this work were carried out by the Material Studio (MS) 7.0 package. Geometry optimization, a first-principle pseudopotential method based on DFT, was performed using the CASTEP module [18]. Plane wave (PW) basis sets and ultrasoft pseudopotentials were employed for the DFT calculations [19,20]. Based on the test results, GGA-PBESOL [21,22] was set as the exchange correlation functional and 330 eV was used as the cut-off energy. The Brillouin zone was sampled with Monkhorst and Pack special k-points of a $4 \times 4 \times 4$ grid for all structure calculations [23–26]. Only valence electrons were considered explicitly using ultrasoft pseudopotentials [27–29], and pseudo atomic calculations were performed for Ca $3s^23p^64s^2$, F $2s^22p^5$, Ce $4f^{1}5s^25p^65d^{1}6s^2$, Th $6s^26p^66d^27s^2$, U $5f^36s^26p^66d^{1}7s^2$, Y $4s^24p^64d^{1}5s^2$. The convergence tolerances for geometry optimization calculations were set to the maximum displacement of 0.001 Å, the maximum force of 0.03 eV/Å, the maximum energy change of 1.0×10^{-5} eV/atom, and the maximum stress of 0.05 GP, and the self-consistent field (SCF) convergence tolerance was set to 1.0×10^{-6} eV/atom. Other parameters were default settings.

After geometry optimization, the density of state and the Mullilken population of fluorite supercells were calculated with a single-point energy method using CASTEP module. The Fermi energy and the frontier orbital were calculated also by a single-point energy method using DMol3 module with the same setting parameters as CASTEP. Both structure optimization and frontier orbital calculations of oleic acid were performed by Dmol3 with GGA-PBESOL functional, DNP basis set, all electron core potentials, basis file of 3.5, multipolar expansion of Hexadecapole, global orbital cutoff of 3.7 Å, occupation of fermi and SCF tolerance of 1.0×10^{-6} eV/atom. Other parameters were default settings.

3. Results and Discussion

3.1. Lattice Parameter

The unit cell parameters of impurity-bearing fluorite crystals are shown in Table 1. The lattice parameters of CaF₂ bearing Ce, Th, U, and Y impurities are slightly larger than that of the perfect CaF₂, and the Th-bearing fluorite has the maximum parameter. The lattice dilatation might lead to the distortion of the lattice which would change the electronic structure of fluorite [14].

Impurity Type	Lattice Parameter/Å	Deviation/%
No impurity	5.463	0
Ce	5.561	1.79
Th	5.566	1.88
U	5.545	1.50
Y	5.542	1.44

Table 1. Lattice parameter of impurity-bearing and perfect fluorite crystals.

Note: the deviation representing deviations of calculated values from reference values (5.463 Å).

3.2. Fermi Level

Fermi level (E_F) [13,30–32], synonymous with Fermi energy, is widely used in semiconductor physics. If the electrons in fluorite crystals can be considered as a thermodynamic system, Fermi level is the chemical potential of the system based on statistical theory. From band structure theory, the Fermi level can be considered as a hypothetical energy level of an electron, such that in thermodynamic equilibrium, this energy level would have a 50% probability of being occupied at any given time. The Fermi level of the perfect and impurity-bearing CaF₂ is shown in Table 2.

Table 2 shows that the Fermi level of a perfect CaF₂ crystal is –5.698 eV. For impurity-bearing CaF₂, the Fermi level increases, indicating that the probability of the quantum state being occupied by electrons increases. The incorporation of these impurities causes fluorite crystal to be easier to accept electrons [33], which favors the adsorption of oleic acid on fluorite.

Table 2. Fermi energies of perfect and impurity-bearing fluorite crystals.

Species	Perfect	Ce	Th	U	Y
Ef/eV	-5.698	-2.24	-2.54	-2.55	-2.509

3.3. Density of States

Figure 2 shows the density of state (DOS) diagram of perfect and impurity-bearing fluorite crystals. The appearance of impurity atoms causes the total density peak to shift towards the lower energy and Fermi level to move towards higher energy. This indicates that the presence of impurities makes fluorite accept electrons more easily, and hence enhances the oxidation ability of fluorite crystals (consistent with the Fermi level study) [34,35], which facilitates the reaction of fluorite with reductive collectors (oleic acid).

Figure 3 shows the partial density of state (PDOS) of impurity-bearing fluorite crystals. Impurity atom has an impurity energy level near the Fermi level. The impurity levels of Ce, Th, and U are mainly composed of f orbitals, while the impurity level of Y is mainly contributed by the d orbital. The impurity atoms Ce, Th, and U have the energy level in the valence band except Y.



Figure 2. Density of state (DOS) of perfect and impurity-bearing fluorite crystals.



Figure 3. Partial density of state (PDOS) of impurity atoms in fluorite crystal.

Figures 4 and 5 show the PDOS of the Ca and F atoms adjacent to the impurity atom. The presence of impurity atoms causes the PDOS peaks of Ca and F atoms to move towards the lower energy. The state density near the Fermi level in the perfect fluorite crystal is mainly provided by the F atom. But, the presence of the impurity atoms causes the peak to shift to the left direction, and the peak near the Fermi level is provided by the impurity atom, indicating that impurity atoms play a dominant role in determining the chemical properties of impurity-bearing fluorite.



Figure 4. PDOS of a single Ca atom adjacent to the impurity atom in fluorite crystals.



Figure 5. PDOS of a single F atom adjacent to the impurity atom in fluorite crystals.

3.4. Analysis of the Mulliken Population

According to Mulliken population of a chemical bond [36–38], the covalency and ionic strength of the bond can be estimated. A high population value indicates a covalent bond, while a low value implies an ion-interacting bond. Substituted impurity atom mainly affects the atoms closed to it, so the Mulliken population analysis was carried out on the atoms and bonds adjacent to the impurity atom. The results are shown in Table 3.

Table 3 shows the p orbital of the Ca atom in the perfect fluorite crystal is not involved in bonding. Ca atoms can donor electrons, the main loss of electrons comes from the d orbital. F atoms can accept electrons, the main gain of electrons happens in the p orbital. The occurrence of impurity atoms gives rise to the redistribution of atomic valence and charge in fluorite crystals. The presence of Ce, Th, U, and Y increases the charge value of the F atom and decreases the charge value of the Ca atom. But, the impurity atoms are positively charged. The increase of positive charge in fluorite crystal enhances the adsorption of oleic acid anions onto the fluorite, which is beneficial for fluorite flotation.

Defect Trues	Smarias	Population				Tatal	Charman
Delect Type	Species	S	р	d	f	Total	Charge/e
Dorfoot fluorito	F	1.96 (0.04)	5.71 (-0.71)	0.00	0.00	7.67	-0.67
reflect fluorite	Ca	2.15 (-0.15)	6.00 (0)	0.51 (1.49)	0.00	8.66	1.34
Ce-bearing fluorite	F	1.95 (0.05)	5.66 (-0.66)	0.00	0.00	7.61	-0.61
	Ca	2.19 (-0.19)	6.00 (0)	0.53 (1.47)	0.00	8.72	1.28
	Ce	2.21 (-0.21)	6.32 (-0.31)	1.02 (0.98)	1.40 (0.60)	10.94	1.06
Th-bearing fluorite	F	1.95 (0.05)	5.64 (-0.64)	0.00	0.00	7.59	-0.59
	Ca	2.18 (-0.18)	6.00 (0)	0.57 (1.43)	0.00	8.75	1.25
	Th	2.28 (-0.28)	6.31 (-0.31)	1.88 (0.12)	0.58 (1.42)	11.05	0.95
U-bearing fluorite	F	1.95 (0.05)	5.64 (-0.64)	0.00	0.00	7.59	-0.59
	Ca	2.18 (-0.18)	6.00 (0)	0.55 (1.45)	0.00	8.73	1.27
	U	2.28 (-0.28)	6.44 (-0.44)	1.06 (0.94)	3.31 (0.69)	13.09	0.91
Y-bearing fluorite	F	1.95 (0.05)	5.67 (-0.67)	0.00	0.00	7.62	-0.62
	Ca	2.20 (-0.20)	6.00 (0)	0.50 (1.5)	0.00	8.70	1.30
	Y	2.30 (-0.30)	6.32 (-0.32)	1.32 (1.68)	0.00	9.93	1.07

Table 3. Mulliken population of impurity atom and the atoms adjacent to impurity atom in impuritybearing fluorite crystals.

Note: In parentheses, the positive number represents the value of lost electrons, and the negative number represents the value of accepted electrons.

Table 4 shows the Mulliken population values of the bonds formed between the impurity atom and adjacent atoms in impurity-bearing fluorite crystals. The presence of impurity atoms reduces the population value of F–Ca bonds and the covalency, but increases the bond length. It increases the population value of F–F bonds and the covalency, decreases the bond length. The population values of F–REE bonds are larger than that of F–Ca and F–F bonds, indicating that the covalency of F–REE bond is larger and hence the covalency of fluorite crystal is improved. It is wide accepted that the atoms on the commonly exposed surfaces of fluorite present unsaturated bonds [39–41]. Accordingly, the exposed REE atoms on the fluorite surface with unsaturated bonds have a stronger interaction with oleate ions, i.e., the interaction between oleic acid and fluorite becomes stronger. Therefore, the stronger the covalency is, the stronger the adsorption of oleic acid is [42]. The existence of impurity defects is favorable for the fluorite flotation.

Defect Type	Bond	Population	Length (Å)
Danka ak flas anita	F–Ca	0.08	2.3590
reflect fluorite	F–F	-0.04	2.7240
	F–Ca	0.07	2.3890
Ce-bearing fluorite	F–F	-0.03	2.7126
	F–Ce	0.11	2.4668
	F–Ca	0.06	2.3916
Th-bearing fluorite	F–F	-0.03	2.7164
	F–Th	0.10	2.4681
	F–Ca	0.07	2.3866
U-bearing fluorite	F–F	-0.03	2.7216
	F–U	0.12	2.4447
	F–Ca	0.07	2.3806
Y-bearing fluorite	F–F	-0.03	2.7026
	F-Y	0.13	2.4588

Table 4. Mulliken population of bonds formed between the impurity atom and the atoms adjacent to the impurity atoms in impurity-bearing fluorite crystals.

3.5. Effect of Impurity on the Reactivity of Fluorite

It is well established that oleic acid (OA) reacted with the Ca atoms on the surface of fluorite to form calcium oleate by chemical reaction [43–45]. During the reaction, the OA loses electrons and is

oxidized while the fluorite accepts electrons and is reduced. As discussed above, impurities in the crystal can change the electronic structures of the fluorite, such as the Fermi energy, density of states, and the Mulliken population. Since the surface reactivity of fluorite is mainly dependent on these properties mentioned, the interaction of fluorite with flotation reagent (especially collector) would be changed.

The extent of the interaction of minerals with organics can be described by frontier molecular orbital theory was proposed by Fukui in 1952 [46]. The central idea of the theory is that the mineral with highest occupation molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO) is the most reactive in its interaction with organics. The HOMO energy is the highest, the most active and most likely to donate electrons. The LUMO energy is the lowest in all unoccupied orbitals and most likely to accept electrons.

HOMO and LUMO energies determine the ability of electron gain, loss and transfer of a molecule, and hence determines its main chemical properties. According to the linear combination principle of molecular orbitals, the molecular orbital consists of many atomic orbitals:

$$\Psi = c_1 \phi_1 + c_2 \phi_2 + \dots + c_n \phi_n \tag{1}$$

where ψ is the molecular orbital; ϕ is the atomic orbital; *c* is the atomic orbital coefficient. The magnitude of the atomic orbital coefficient of HOMO and LUMO represents the contribution of the constituent atom to the molecular orbital. The positive and negative sign of atomic orbital coefficient represent bonding and antibonding between the atoms, respectively. But, only the absolute value of the coefficient was concerned in this study. The greater the coefficient is, the stronger the effect of the atom exerts on orbital reactivity.

The fluorite acquires electrons and is reduced when reacted with oleic acid, so the LUMO of fluorite is considered here. Table 5 shows the frontier orbital coefficients of perfect and impuritybearing CaF₂ crystals. The impurity atoms in the fluorite lattice leads to smaller orbital coefficients for Ca and F and larger ones for the impurity atoms. The effect of impurity atoms on the fluorite LUMO follows the order, Th > Y > Ce > U. The greater the orbital coefficient is, the greater its contribution to LUMO is. The largest atomic orbital coefficient of impurity compared to those of Ca and F, is indicative of the decisive role of impurity atoms in determining the reactivity of fluorite.

Table 5. Frontier orbital coefficients of perfect and impurity-bearing fluorites.

Defect Type	Atomic Orbital Coefficient of LUMO
Perfect fluorite	0.323Ca + 0.306F
Ce-bearing fluorite	0.216Ca + 0.283F + 0.809Ce
Th-bearing fluorite	0.006Ca + 0.036F + 0.993Th
U-bearing fluorite	0.037Ca + 0.041F + 0.553U
Y-bearing fluorite	0.064Ca + 0.111F + 0.974Y

The reaction between OA and fluorite happens between the HOMO of OA as electron donor and the LUMO of fluorite as electron acceptor. According to the frontier orbital theory, the extent of their interaction can be defined by the following Equation:

$$\Delta E = \left| E_{\rm HOMO}^{\rm OA} - E_{\rm LUMO}^{\rm CaF_2} \right| \tag{2}$$

where $E_{\text{HOMO}}^{\text{OA}}$ is the HOMO level of the OA, and $E_{\text{LUMO}}^{\text{CaF}_2}$ is the LUMO level of CaF₂. Based on frontier orbital theory, the smaller the value of ΔE is, the stronger the interaction between OA and fluorite is [14]. The HOMO and LUMO values of perfect CaF₂, the impurity-bearing CaF₂, and ΔE values are shown in Table 6.

Table 6 shows that the ΔE between perfect CaF₂ and OA is 3.424 eV. For CaF₂ bearing Ce, Th, U, and Y impurities, the ΔE is much smaller, suggesting that the incorporation of these impurities can benefit the interaction between OA and fluorite. Among these impurity-bearing fluorite crystals, ΔE for the Th-bearing fluorite is smallest (2.376 eV), indicating that the interaction between the Th-bearing fluorite and OA is the strongest.

Defect Type	Еномо/eV	Elumo/eV	$\Delta E/eV$
Perfect fluorite	-9.175	-2.197	3.424
Ce-bearing fluorite	-3.05	-2.894	2.727
Th-bearing fluorite	-3.303	-3.245	2.376
U-bearing fluorite	-4.014	-2.962	2.659
Y-bearing fluorite	-9.395	-3.107	2.514
Oleic acid	-5.621	-0.944	-

Table 6. Frontier orbital energies of the impurity-bearing fluorite crystals and oleic acid.

4. Conclusions

The electronic structures of bulk fluorite bearing Ce, Th, U, and Y impurities were calculated using DFT. The results showed that the impurities changed the structure and electronic properties of fluorite, including the Fermi level, density of states, and the Mulliken population. The presence of impurities increased the lattice parameters of fluorite, and made the Fermi level shift towards the direction of high energy, causing the fluorite to accept electrons more easily. The results of DOS and Mulliken population indicated that the incorporation of impurity atoms made oleic acid more easily adsorb on fluorite. The frontier molecular orbital calculations suggested that the incorporation of impurities of Ce, Th, U, and Y can enhance the reactivity of fluorite with oleic acid.

Supplementary Materials: The following are available online at http://www.mdpi.com/2075-163X/7/9/160/s1, Table S1: The unit cell parameters of fluorite under different exchange correlation functional; Table S2: The unit cell parameters of fluorite under different cut-off energy values.

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Conflicts of Interest: The authors declare no conflict of interest.

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