

Article



# The Process Mineralogical Characterization of Bayan Obo Rare-Earth Tailings and Density Functional Theory Study of the Occurrence State of Sc

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Abstract: As Bayan Obo rare-earth tailings, which are generated after the production of mineral products with the raw ore from different mining areas, are considered secondary resources rich in valuable elements such as F, Fe, REE, and Nb, an effective method is urgently needed to recover such valuable elements for resource recycling and environmental conservation. A mineralogical analysis can enable process diagnosis, design, and optimization and is the key to comprehensively utilizing valuable elements. Hence, detailed mineralogical characterization is necessary as a starting point to develop a feasible processing flowsheet. In this study, various detection methods, namely inductively coupled plasma-optical emission spectrometry (ICP), X-ray Fluorescence Spectrometer (XRF), X-ray powder diffractometer (XRD), scanning electron microscopy system with an energy dispersive spectrometer (SEM-EDS), mineral liberation analysis (MLA), and electron probe microanalysis (EPMA), were applied to conduct detailed mineralogical characterization of Bayan Obo rare-earth tailings, and the occurrence state of Sc in the main Sc-bearing minerals was studied using density functional theory (DFT). The results showed that Fe mainly occurs in hematite, riebeckite, ankerite, siderite, and pyrite, with contents of 50.15 wt%, 27.94 wt%, 8.34 wt%, 4.92 wt%, and 5.59 wt%, respectively. Nearly all F occurs in 26.8 wt% fluorite. The main rare-earth minerals are bastnasite, apatite, and monazite (La), with contents of 5.0%, 5.0%, and 1.6% in Bayan Obo rare-earth tailings, respectively. Notably, 48.47%, 21.70%, 10.34%, and 10.28% of niobium element occurs in nioboaeschynite, pyrochlore, dingdaohengite, and ilmenorutile, respectively. Scandium was detected in five minerals, namely aegirine, riebeckite, monazite, ilmenorutile, and niobite, with average contents of 0.04 wt%, 0.22 wt%, 0.06 wt%, 0.06 wt%, and 1.58 wt%, respectively. According to the DFT analysis, the state of Sc in aegirine is different from that in riebeckite. Scandium in aegirine mainly substitutes Fe or enters the interstitial lattice site, while Sc in riebeckite tends to replace Fe. Based on these results, a process for recovering valuable elements from tailings is proposed.

Keywords: DFT; occurrence state; scandium; process mineralogical characterization

# 1. Introduction

In recent decades, attention to rare-earth mineral resources has increased worldwide [1,2]. The growing demand for green technologies has led to the large-scale application of rare-earth elements in advanced electronic products and increased the demand for rare-earth elements in the world's major economies, including the United States, the European Union, the United Kingdom, and Japan [3,4], with an estimated annual growth rate of 3.7% to 8.6% [5,6]. Deposits of high-grade rare-earth elements continue to be depleted. China's reserves have declined significantly over the past 50 years, despite being the world's richest country in rare-earth resources [6]. Therefore, there is an urgent need to



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**Copyright:** © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). exploit practical technology to recover rare-earth resources effectively from large quantities of rare-earth tailings with a high content [7].

Bayan Obo tailing pond, one of the world's largest rare-earth tailing ponds [8], contains tailings generated since the 1960s, at the rate of 386,000 tpa [9–12]. Currently, the tailing pond covers approximately 12 km<sup>2</sup> and stores approximately 200 million tons of tailings [13–17]. Tailings contain a large amount of iron, rare-earth elements, fluorine, Niobium, and other elements, which are a valuable secondary resource [18–20]. However, reprocessing tailings with methods such as recycling is difficult because of their low grade, fine particle sizes, and complex mineralogy among other factors [21]. Currently, the utilization of Bayan Obo tailings is still in the laboratory research stage. The main treatment options include physical separation, as well as hydrometallurgical and pyrometallurgical treatments [6,15,20,22–27]. In a typical Bayan Obo tailing treatment process, physical operations such as grinding, screening, magnetic force, flotation, gravity separation, and density-based separation are used as pretreatments to release and concentrate metallic parts (MFs) and non-metallic fractions (NMFs) [28].

The effective utilization of tailings and the optimal processing method depend on the mineral species, correlations and interlocking between minerals, and metal distribution characteristics [29]. The process mineralogy of tailings helps to provide essential information for recovery research [28,30]. Therefore, it is necessary to study the process mineralogy of tailings.

Process mineralogy is a widely accepted integrated discipline that combines quantitative (and qualitative) mineralogy and metallurgy [31–33]. The aim is to optimize metallurgical processes, reduce operating costs, and improve metal recovery through the comprehensive characterization of precursor ore mineralogy, mineral assemblages, grain size, and texture. Therefore, process mineralogy is commonly applied to grade and recovery optimization in the working process and has been applied to many deposit types, including rare-earth elements.

This study aims to contribute to the current knowledge by providing detailed characteristics of the occurrence states of valuable elements in tailings and their associations with physical enrichment and hydrometallurgical extraction, which may be a possible option for processing these resources. To fully understand the characteristics of the tailings, advanced characterization methods such as MLA, EPMA, XRD, and ICP were used in this study to analyze the process parameters of rare-earth ore, including element content, mineral composition, the occurrence state of elements, mineral particle size distribution, mineral combination, and deionization. The possible combination of Sc in the minerals was obtained by combining the DFT calculation results. Detailed basic theoretical data are provided for further improvement in the relevant beneficiation process, the recovery of other valuable minerals, and the comprehensive utilization of tailings.

#### 2. Materials and Reagents

Bayan Obo rare-earth tailings, provided by Baotou Iron and Steel (Group) Co., Ltd. of China (Baotou, Inner Mongolia, China), were sourced from the tailing pond of Bayan Obo and homogenized. Subsequently, 100 g dried rare-earth tailing sample was screened into different size fractions, namely +200 mesh, 200–250 mesh, 250–325 mesh, 325–400 mesh, 400–500 mesh, and –500 mesh, and placed in an oven at 105 °C for 48 h to reduce the error caused by the moisture in the sample. All dried samples were weighed and stored in zip-lock bags for later use.

Mineral phase analysis of the dried samples, which were ground to less than 250 mesh, was performed using an X-ray powder diffractometer (D8 Advance, Brock AXS GmbH, Bruker, Billerica, MA, USA). The operating conditions were Cu K $\alpha$  radiation of  $\lambda$  = 1.54060 Å as the excitation source, with 40 kV accelerating voltage, 40 mA current, a constant step of 0.019°, and a counting time of 1 s for each step for 2-theta, varying from 5° to 90°. The diffraction pattern was analyzed using the X Pert HighScore plus analysis software

(version 5.1, Malvern Panalytical, Malvern, UK) equipped with the International Centre for Diffraction Data (ICDD) database.

The particle size distribution of Bayan Obo rare-earth tailings was analyzed using a Malvern laser particle size analyzer (Mastersizer 3000, Malvery Instruments Ltd., Alemlo, The Netherlands), which can accurately quantify the morphological characteristics of non-spherical and non-smooth particles by processing the optical signals of different detection windows and obtaining the fractal dimension of sample particles for measurement to describe the effectiveness of the space occupied by the most complex shapes. The powdered sample was added to 50 mL of deionized water and placed in an ultrasonic instrument (20 kW) for 30 s. A 500 mL measuring cup filled with 2/3 deionized water was placed in the analyzer. Subsequently, the fully dispersed samples were slowly added to the measuring cup. The working parameters were as follows: red light was the main light source, blue light was the auxiliary light source, and the injection stirring speed was 3000 rpm.

The dried 1.0 g mineral powder was placed into a cylindrical plastic mold with a diameter of 30 mm. Subsequently, a 10:1 mixture of epoxy resin and curing agent was mixed with the sample, followed by rapid agitation for approximately 3 min to remove air. Subsequently, the processed mold was placed in the oven at 35 °C for 8 h to obtain the MLA resin sample. The curing sample was fixed in the polisher (MP-2G100A) purchased from Shandong Honghong Instrument Equipment Co., Ltd., with 25 N of polishing strength and 500 r/min of revolving speed to make the cut surface of the mineral smooth enough after 600, 800, 1200, 1500, and 2000 abrasive paper in turn. The polished samples were cleaned with distilled water inside a microwave ultrasonic cleaner for 5 min, removed, dried, and used for MLA and EPMA analyses.

Further mineralogical characterization, such as the association and distribution of each mineral and element in Bayan Obo rare-earth tailings, was performed using a Type-250 automatic mineral liberation analyzer (MLA) (FEI Company, Hillsboro, OR, USA). The analyzer was equipped with a suit of back-scattered scanning electron microscopy (SEM) system, an energy-dispersive spectrometry (EDS) probe, and a suit of MLA software. The operation conditions were as follows: the working distance was 11.6 mm, the frame resolution was 500 pixels, the probe current was 10 nA, and the electron beam accelerating voltage was 25 kV.

To accurately obtain the chemical composition of trace mineral elements, the polished samples were analyzed with a JEOL JXA-iSP-100 Electron Probe Microanalyzer equipped with five wavelength-dispersive spectrometers (WDSs) at the Laboratory of Guangzhou Tuoyan Analytical Technology Co., Ltd., in Guangdong Province, China. The operating conditions for the quantitative WDS analysis included an accelerating voltage of 15 kV, a probe beam current of 10 nA, and a 5–10  $\mu$ m beam spot size. The peak counting time was 10 s for F, K, P, Na, Ca, and Fe and 20 s for Al, Si, Mg, Mn, Ti, S, and Cl. The background counting time was half the peak counting time for the high- and low-energy background positions. The following standards were used: BaF<sub>2</sub>(F), quartz (Si), olivine (Mg), orthoclase (K), BaSO<sub>4</sub>(S), TiO<sub>2</sub>(Ti), Fe<sub>3</sub>O<sub>4</sub>(Fe), MnO<sub>2</sub>(Mn), albite (Na), spodumene (Al), NaCl(Cl), and apatite (Ca and P).

The precise quantification of trace elements, such as Sc, in Bayan Obo rare-earth tailings was performed using an inductively coupled plasma emission spectrometer (ICP-OES, PQ9000, Analytik Jena GmbH, Jena, Germany). The solid tailing samples were dissolved in the solution and prepared according to the following steps:

First, 0.2 g of solid dried sample was mixed with 6 mL of HCl solution, 2 mL of HNO<sub>3</sub> solution, and 2 mL of HF solution, and the mixture was then placed into a Teflon microwave digestion tank.

The tank was sealed and placed in a digestion instrument (WX-8000, Preekem Scientific Instruments Co., Ltd., Shanghai, China), and digestion was conducted according to the procedure, with the holding temperature set at 120 °C for 3 min under 15 bar pressure, 150 °C for 3 min under 20 bar pressure, 180 °C for 3 min under 30 bar pressure, 200 °C for 3 min under 40 bar pressure, and 220 °C for 45 min under 45 bar pressure.

The tank was removed after cooling and lowering pressure, and then the opened tank was heated to 160  $^{\circ}$ C, the solvent was evaporated to the size of a soybean (~0.25 mL), and finally the solution was moved to the volumetric bottle for the ICP-OES test.

Epoxy resin, curing agent (ethanediamine,  $NH_2CH_2CH_2NH_2$ ), and single-crystal diamond polishing solution (0.5 µm) were analytically pure products and were purchased from Shanghai McLean Biochemical Technology Co., Ltd., Shanghai, China.

#### 3. Results and Discussion

### 3.1. Composition Analysis of Bayan Obo Rare-Earth Tailings

# 3.1.1. Chemical Composition

The major element compositions of Bayan Obo rare-earth tailings are listed in Table 1. The main components of the tailings are CaO, Fe<sub>2</sub>O<sub>3</sub>, SiO<sub>2</sub>, and F, accounting for 30.50 wt%, 20.40 wt%, 13.10 wt%, and 14.20 wt%, respectively. The total rare-earth oxides, including La<sub>2</sub>O<sub>3</sub>, CeO<sub>2</sub>, and Nd<sub>2</sub>O<sub>3</sub>, exceed 2.5 wt%. Because of their high prices, 0.11% of Nb and 137.91 ppm of Sc are the most valuable elements in tailings. The total content of the main impurities, such as MnO, Al<sub>2</sub>O<sub>3</sub>, MgO, Na<sub>2</sub>O, and SiO<sub>2</sub>, is greater than 20 wt%, which seriously affects the grade of fluorite and iron concentrates and increases the cost of purification.

**Table 1.** Component analysis results of the samples (wt%).

	F	Na <sub>2</sub> O	MgO	$Al_2O_3$	SiO <sub>2</sub>	$P_2O_5$	SO <sub>3</sub>	K <sub>2</sub> O	CaO
Content	14.20	1.64	3.26	0.87	13.10	2.70	2.70	0.41	30.50
	TiO <sub>2</sub>	MnO	Fe <sub>2</sub> O <sub>3</sub>	BaO	$La_2O_3$	CeO <sub>2</sub>	$Nd_2O_3$	$Nb_2O_5$	Sc (ppm)
Content	0.69	1.36	20.40	4.92	0.68	1.57	0.46	0.16	137.91

## 3.1.2. Mineral Constituent and Particle Size Distribution

To comprehensively assess the residual value of tailings, it is necessary to know their mineral compositions and their distribution across particle sizes. Mineral composition determines the valuable components of the tailings and the particle size distribution is a proxy for the degree of dissociation of the target minerals. These factors determine the selection of beneficiation methods.

The XRD analysis results of Bayan Obo rare-earth tailings, shown in Figure 1, reveal that the main mineral phases are bastnasite ((Ce, La)[CO<sub>3</sub>]F), quartz (SiO<sub>2</sub>), biotite  $(K_2Mg_6(Al_2Si_6O_{20})(OH)_4)$ , aegirine (NaFeSi<sub>2</sub>O<sub>6</sub>), riebeckite (AB<sub>2</sub>C<sub>5</sub>T<sub>8</sub>O<sub>22</sub>W<sub>2</sub>, A = Na, K, Ca, Pb, and Li; B = Na, Ca,  $Mn^{2+}$ ,  $Fe^{2+}$ , Mg, and Li; C = Mg,  $Fe^{2+}$ ,  $Mn^{2+}$ , Al,  $Fe^{3+}$ ,  $Ti^{4+}$ , and Li; T = Si, Al, Ti<sup>4+</sup>, and Be; W = (OH), F, Cl, and  $O^{2-}$ ), barite (BaSO<sub>4</sub>), hematite (Fe<sub>2</sub>O<sub>3</sub>), pyrite (FeS<sub>2</sub>), and fluorite (CaF<sub>2</sub>). Although XRD is an important means of characterizing mineral phases, it can determine the existence of a phase but not its absence. The limit of detection (LOD) of XRD is influenced by many factors, such as dispersion, crystallinity, and the type of substance being detected. XRD can usually detect mineral phases with more than 5% content, indicating that the tailings contain at least one of the phases shown in Figure 1. Furthermore, different mineral formation environments result in differences in the elemental content of the same mineral, thus changing the XRD spectrum peaks, and the ICDD database does not contain all spectral peaks. Also, XRD cannot determine the specific elemental content in a mineral. Additional detection methods, such as EPMA and MLA, are required to detect the minerals contained in tailings and the content of each element in them.

The particle size distribution of Bayan Obo rare-earth tailings is shown in Figure 2, where only one asymmetrical peak is observed. All particles are above 500  $\mu$ m, but the content in the range of 0.70–140.52  $\mu$ m is 90%, and that in the range of 0.70–42.82  $\mu$ m is 50%, indicating that the tailings are dominated by fine tailings.

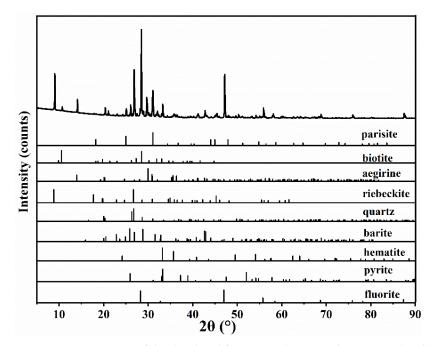


Figure 1. XRD pattern of the dried and fine-grained Bayan Obo rare-earth tailings.

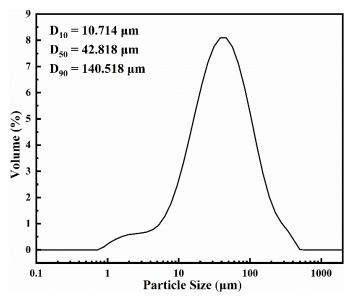


Figure 2. Particle size distribution of Bayan Obo rare-earth tailings.

The mineral compositions and contents of the tailings are shown in Figure 3. The iron minerals in the tailings are mainly hematite, siderite, ankerite, and pyrite, with contents of 11.8%, 1.7%, 8.5%, and 2.0%, respectively. The main rare-earth minerals are bastnasite, apatite, and monazite, with contents of 5.0%, 5.0%, and 1.6%, respectively. The silicate minerals are mainly biotite, riebeckite, and small quantities of albite and phlogopite, with contents of 1.2%, 15.5%, 0.7%, and 0.7%, respectively. The mineral with the highest content in the tailings is fluorite, and there are still large amounts of quartz and barite, with contents of 26.8%, 6.5%, and 5.6%, respectively. Both riebeckite and aegirine are single-chain silicate minerals with similar structures and similar contrast imaging under back-scattered electrons (BSEs). Therefore, they were classified into one category in this study. MLA images of Bayan Obo rare-earth tailings are shown in Figure 4, which is a detailed visual demonstration of Figure 3.

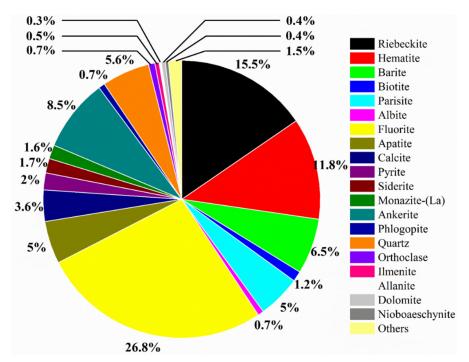


Figure 3. Mineral composition and contents in minerals associated with Bayan Obo tailings (wt%).

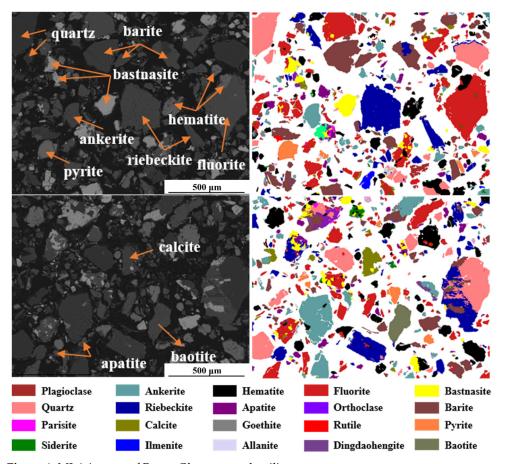


Figure 4. MLA images of Bayan Obo rare-earth tailings.

3.1.3. Distribution of Valuable Elements in Minerals

The valuable elements in Bayan Obo tailings include F, REE, Fe, Sc, and Nb. Therefore, the occurrence states of these elements in tailings are discussed in this study.

Iron in Bayan Obo tailings mainly occurs in the form of independent minerals, such as hematite, riebeckite, ankerite, siderite, and pyrite, with contents of 50.15 wt%, 27.94 wt%, 8.34 wt%, 4.92 wt%, and 5.59 wt%, respectively. The majority of the F was found in fluorite (97.20%). However, it was also found in bastnasite in trace amounts. Bayan Obo rare-earth deposits mainly consist of light rare-earth elements. In this study, the distributions of La and Ce were used instead of the distribution of rare earth. Cerium mainly occurs in dingdaohengite, monazite, allanite, bastnasite, and wollastonite, with contents of 6.52 wt%, 14.11 wt%, 3.87 wt%, 72.78 wt%, and 2.72 wt%, respectively. Lanthanum mainly occurs in monazite, bastnasite, and wollastonite, with contents of 42.17 wt%, 56.03 wt%, and 1.8 wt%, respectively. Notably, 86.89% of La and 98.20% of Ce in Bayan Obo rare-earth tailings occur in bastnasite and monazite, respectively. Therefore, the states of bastnasite and monazite as the main minerals of rare-earth occurrence are discussed later. Niobium was primarily found in nioboaeschynite (48.47 wt%), pyrochlore (21.70 wt%), dingdaohengite (10.34 wt%), and ilmenorutile (10.28 wt%), and also in baotite in trace amounts, as shown in Table 2.

Table 2. Distribution of F, REE, Fe, Sc, and Nb in Bayan Obo tailings.

Mineral	Fe (%)	Mineral	F (%)	Mineral	Ce (%)	Mineral	La (%)	Mineral	Nb (%)
hematite	50.15	fluorite	97.20	dingdaohengite	6.52	monazite	42.17	dingdaohengite	10.34
riebeckite	27.94	apatite	0.46	monazite	14.11	bastnasite	56.03	nioboaeschynite	48.47
ankerite	8.34	bastnasite	2.16	allanite	3.87	wollastonite	1.80	baotite	3.07
siderite	4.92	phlogopite	0.06	bastnasite	72.78			pyrochlore	21.70
pyrite	5.59	1 01		wollastonite	2.72			ilmenorutile	10.28

The results of the MLA software analysis were based on the qualitative mineral composition of the EDS scans. Regarding the low precision of EDS, which has a detection limit of about 0.5%, Sc has no independent mineral in the Bayan Obo ore and only hosts in the lattice of other minerals in the form of homomorphism, and its content is low. Thus, the analytical detection means of EDS and MLA cannot be used to study the occurrence state of Sc.

An electron probe microanalyzer (EPMA) uses a focused, high-energy electron beam to bombard the solid sample surface and stimulate the characteristic X-rays and a variety of electronic signals (such as secondary electrons and backscattered electrons) to perform qualitative and quantitative analyses of the elements in situ and morphological observations of the sample. It is the most basic in situ microbeam microzone analysis instrument used in the fields of mineralogy, petrology, geochemistry, mineral deposit science, comparative planetology, and materials science. An EPMA, with an analytical region of less than 1  $\mu$ m and a detection limit of approximately 100 ppm, was used to determine the occurrence of Sc in various minerals in Bayan Obo tailings.

The EPMA test results for the six silicate minerals are presented in Table 3. The presence of Sc was detected only in chain silicates (aegirine and riebeckite), in which  $SiO_4$  tetrahedrons are connected by sharing oxygen to form a continuous chain, and they are absent in silicates with other structures. Although some EPMA data are not zero, the values' reliability is deemed low because they are less than the detection limit. Therefore, they were not adopted in this paper.

The content of  $Sc_2O_3$  in aegirine was 0%–0.156%, and the average of the 19 samples was 0.037%. The chemical formula of aegirine was calculated according to the average content of each element as follows:  $Na_{0.948}Ca_{0.097}Mg_{0.038}Al_{0.031}Sc_{0.001}Fe^{3+}_{0.885}Si_2O_{5.992}F_{0.016}$ . The distribution of Sc in aegirine was investigated using EPMA line scanning and mapping, as shown in Figures 5a and 6. Sc is uniformly distributed in the individual aegirine spots, and the difference in composition is mainly due to the different aegirine spots.

Mineral Samples		Aegirine (% 19	(6)	R	iebeckite (% 21	(6)	Potass	sium Feldsp 7	oar (%)	P	agioclase (% 3	%)
•	Min	Max	Ave	Min	Max	Ave	Min	Max	Ave	Min	Max	Ave
Sc <sub>2</sub> O <sub>3</sub>	0	0.156	0.037	0	2.298	0.222	0	0.002	0.000	0	0.003	0.002
F	0.023	0.878	0.185	1.249	3.308	2.455	ND	ND	ND	ND	ND	ND
MgO	0.018	1.708	0.653	8.153	15.372	13.218	0	0	0	0	0.005	0.002
K <sub>2</sub> O	0	0.017	0.003	0.953	2.436	1.953	15.496	16.826	16.463	0.104	0.187	0.146
MnO	0.014	1.126	0.259	0.439	4.707	2.413	ND	ND	ND	ND	ND	ND
TiO <sub>2</sub>	0.056	1.163	0.264	0.000	0.095	0.037	0	0.001	0.000	0	0	0
CaO	0.365	4.961	1.697	0.950	3.289	1.725	0	0.017	0.006	6.942	7.083	7.011
FeO	26.004	29.834	27.813	11.121	23.672	14.414	0.214	0.336	0.260	0.383	0.434	0.407
Na <sub>2</sub> O	11.072	13.79	12.831	6.407	7.972	7.341	0.346	0.704	0.452	7.421	7.717	7.610
$Al_2O_3$	0.054	2.115	0.694	0.088	0.773	0.421	18.318	18.863	18.567	26.059	26.139	26.105
SiO <sub>2</sub>	50.599	53.16	52.388	52.707	55.229	54.033	62.681	64.186	63.764	58.427	58.545	58.497
Cl	0	0.005	0.002	0.000	0.005	0.001	ND	ND	ND	ND	ND	ND
Total	88.205	108.91	96.824	82.067	119.156	98.232	97.055	100.935	99.512	99.336	100.113	99.780
Mineral		Albite (%)	)		Mus (%)			Quartz (%)	)			
Samples		6			4			6				
_	Min	Max	Ave	Min	Max	Ave	Min	Max	Ave			
$Sc_2O_3$	0	0.014	0.006	0	0.003	0.001	0	0.007	0.002			
F	ND	ND	ND	4.622	6.067	5.156	ND	ND	ND			
MgO	0	0.011	0.003	20.179	23.274	22.236	ND	ND	ND			
K <sub>2</sub> O	0.097	0.169	0.125	10.495	10.854	10.658	ND	ND	ND			
MnO	ND	ND	ND	0.756	1.368	1.0913	ND	ND	ND			
TiO <sub>2</sub>	0	0.006	0.003	0.029	0.224	0.104	ND	ND	ND			
CaO	0.007	0.037	0.016	0	0.015	0.009	ND	ND	ND			
FeO	0.248	0.334	0.281	4.534	9.387	6.379	0.044	0.253	0.194			
Na <sub>2</sub> O	11.522	11.937	11.789	0.058	0.162	0.108	ND	ND	ND			
11 0	19.326	19.678	19.565	8.124	9.800	9.241	0.000	0.003	0.001			
$Al_2O_3$			(0.000	41 E0E	44.775	43.063	96.822	100.980	100.187			
$AI_2O_3$ SiO <sub>2</sub>	68.126	68.549	68.303	41.585	44.775	10.000	J0.022	100.700	100.107			
	68.126 ND	68.549 ND	68.303 ND	41.585 0.006	0.012	0.008	ND	ND	ND			

Table 3. EPMA test results of the seven silicate minerals.

Note: "ND" in the table indicates that it was not detected.

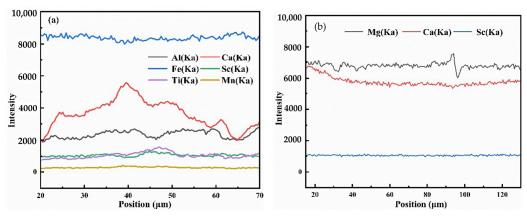


Figure 5. EPMA line scans of (a) aegirine and (b) riebeckite.

The content of  $Sc_2O_3$  in riebeckite was 0%–2.298%, and the average of the 21 samples was 0.222%. The chemical formula of riebeckite was calculated based on the average content of each element as follows:

 $(Ca_{0.83}Na_{0.104}K_{0.369}Mn_{0.302})Na_2(Fe_{0.385}{}^{3+}Fe_{1.393}{}^{2+}Mg_{2.935}Al_{0.073}Sc_{0.029}Ti_{0.004})[Si_8O_{22}] \end{tabular} (OH)_{0.852}F_{1.148}.$ 

The distribution of Sc in riebeckite was investigated using EPMA line scanning and mapping, as shown in Figures 5b and 7. The distribution of Sc in riebeckite is similar to that in aegirine. This may be because the ionic radius of Sc is similar to that of metal ions such as Fe<sup>3+</sup> and Al<sup>3+</sup>. Therefore, there is a possible competitive relationship in the formation of minerals. Scandium is in contact with various fluorine-bearing minerals during high-temperature and high-pressure geological activities, resulting in the formation

and disruption of complex fluoride of Sc. In the cooling process, F combines with calcium ions to form fluorite (CaF<sub>2</sub>) precipitates, whereas Sc forms a solid solution of aegirine and riebeckite with metal ions such as Na<sup>+</sup> and Fe<sup>3+</sup>. This could be the reason why Sc exists uniformly in aegirine and riebeckite and Sc-bearing minerals are associated with fluorite [34]. The complex of aluminum and fluorine ions is also stable during the formation of silicates with high Al content, such as feldspar and mica. However, unlike Sc, aluminum has tetrahedral coordination and can easily enter feldspar and mica. This may explain why Sc does not exist in feldspar and mica.

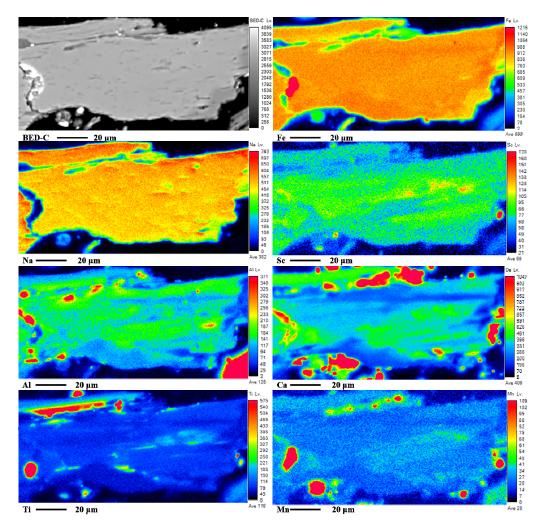


Figure 6. EPMA mapping of aegirine.

The EPMA test results for the four rare-earth minerals are listed in Table 4. Among them, only monazite contained Sc, and the content of  $Sc_2O_3$  was 0%-0.152%. The chemical formula of monazite was calculated according to the average content of each element as follows:  $(Eu_{0.001}Sm_{0.013}Er_{0.001}Y_{0.002}Ce_{0.495}Nd_{0.197}Th_{0.008}La_{0.244}Pr_{0.046}Gd_{0.002}Sc_{0.002})PO_4$ . The total value of the highest content of each element was 73.78% higher than that of the lowest content because the contents of the major elements La, Ce, Nd, and Pr were significantly different, with 353.75%, 36.78%, 187.93, and 74.90%, respectively. This finding may be attributed to the presence of two types of monazite. However, the content of  $Sc_2O_3$  in both types of monazite did not seem to have a significant effect.

Figure 7. EPMA mapping of riebeckite.

Table 4. EPMA test results of the four rare-earth mine	erals.
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Mineral Samples	В	astnasite (% 5	6)	Μ	lonazite (% 6	<b>()</b>		Apatite (%) 2	)	Р	yrochlore (9	%)
1	Min	Max	Ave	Min	Max	Ave	Min	Max	Ave	Min	Max	Ave
Sc <sub>2</sub> O <sub>3</sub>	0.000	0.000	0.000	0.000	0.152	0.058	0.002	0.005	0.004	0.000	0.010	0.005
F	1.170	1.892	1.664	ND	ND	ND	3.509	3.944	3.727	4.773	5.166	4.986
MnO	0.000	0.000	0.000	ND	ND	ND	0.083	0.093	0.088	0.000	0.010	0.003
TiO <sub>2</sub>	0.000	0.000	0.000	ND	ND	ND	ND	ND	ND	2.939	5.113	3.825
CaO	0.058	0.393	0.160	0.024	0.187	0.073	53.491	54.108	53.800	16.631	17.299	17.000
FeO	0.105	0.231	0.151	ND	ND	ND	0.033	0.059	0.046	0.029	0.149	0.081
Na <sub>2</sub> O	0.000	0.000	0.000	ND	ND	ND	0.210	0.269	0.240	6.334	6.988	6.618
$Al_2O_3$	0.000	0.004	0.000	ND	ND	ND	0.000	0.001	0.001	0.000	0.000	0.000
SiO <sub>2</sub>	0.091	0.233	0.170	0.022	0.421	0.265	0.000	0.002	0.001	0.049	0.718	0.272
Cl	0.069	0.101	0.083	ND	ND	ND	0.000	0.000	0.000	0.000	0.011	0.005
ThO <sub>2</sub>	0.053	0.487	0.256	0.003	2.137	0.435	ND	ND	ND	ND	ND	ND
$Nd_2O_3$	9.382	15.982	13.743	9.684	27.883	13.829	0.269	0.365	0.317	ND	ND	ND
$Pr_2O_3$	2.559	3.682	3.320	2.705	4.731	3.175	ND	ND	ND	ND	ND	ND
$Ce_2O_3$	34.868	37.374	36.279	26.860	36.740	33.888	0.338	0.388	0.363	0.645	1.198	0.902
$La_2O_3$	18.696	27.318	21.857	4.657	21.131	16.569	0.015	0.181	0.098	ND	ND	ND
$Sm_2O_3$	0.473	1.335	0.927	0.326	2.211	0.956	ND	ND	ND	ND	ND	ND
Eu <sub>2</sub> O <sub>3</sub>	ND	ND	ND	0.016	0.125	0.059	ND	ND	ND	ND	ND	ND
$Er_2O_3$	ND	ND	ND	0.060	0.178	0.118	ND	ND	ND	ND	ND	ND
$Dy_2O_3$	ND	ND	ND	0.000	0.054	0.015	ND	ND	ND	ND	ND	ND
$Y_2O_3$	ND	ND	ND	0.024	0.165	0.097	ND	ND	ND	ND	ND	ND
$Gd_2O_3$	ND	ND	ND	0.000	0.321	0.181	ND	ND	ND	ND	ND	ND
$Tb_2O_3$	ND	ND	ND	0	0.052	0.019	ND	ND	ND	ND	ND	ND
UO <sub>2</sub>	0.000	0.012	0.002	ND	ND	ND	ND	ND	ND	0.000	0.024	0.008
$Nb_2O_5$	ND	ND	ND	ND	ND	ND	ND	ND	ND	61.355	65.262	63.314
$Ta_2O_5$	ND	ND	ND	ND	ND	ND	ND	ND	ND	0.000	0.000	0.000
$SnO_2$	ND	ND	ND	ND	ND	ND	ND	ND	ND	0.000	0.000	0.000
$P_2O_5$	ND	ND	ND	28.470	30.132	29.621	41.104	41.156	41.130	ND	ND	ND
Total	67.524	89.044	78.613	72.862	126.62	99.358	99.054	100.573	99.814	64.895	132.794	96.959

Note: "ND" in the table indicates that it was not detected.

The EPMA test results for the eight iron-bearing minerals are listed in Table 5. Among these,  $Sc_2O_3$  was detected in two types of Nb-bearing minerals, namely ilmenorutile and niobite, with contents of 0%–0.122% and 0.575%–2.112%, respectively. The presence of Sc appears to be strongly related to Nd, which is consistent with Yang's result [35]. The chemical formula of niobite was calculated according to the average content of each element as follows: (Fe<sub>0.59</sub>Mn<sub>0.38</sub>Sc<sub>0.02</sub>)Nb<sub>2</sub>O<sub>6</sub>. The chemical formula of ilmenorutile could not be obtained because of its complex composition. Among the other iron-bearing minerals, only one ilmenite sample contained Sc, and its EPMA results were 0.335% MgO, 0.305% Nb<sub>2</sub>O<sub>5</sub>, 3.821% MnO, 44.307% FeO, 50.611% TiO<sub>2</sub>, 0.146% V<sub>2</sub>O<sub>3</sub>, and 0.038% Sc<sub>2</sub>O<sub>3</sub>. The composition, except for Sc<sub>2</sub>O<sub>3</sub>, was not significantly different from other ilmenite samples. Therefore, we speculated that there was no Sc<sub>2</sub>O<sub>3</sub> in ilmenite, which is consistent with Yang's result [35].

Table 5. EPMA test results of 8 iron-bearing minerals.

Mineral	I	Dolomite (%	6)		Ilmenite (%	)	Ilr	nenorutile (	(%)	:	Siderite (%	)
Samples		4			6			5			2	
	Min	Max	Ave	Min	Max	Ave	Min	Max	Ave	Min	Max	Ave
$Sc_2O_3$	0.000	0.002	0.001	0.000	0.038	0.008	0.000	0.122	0.061	0.000	0.000	0.000
$Nb_2O_5$	0.000	0.013	0.003	0.280	3.556	0.857	9.652	17.532	12.994	0.000	0.002	0.000
MgO	21.475	25.407	22.629	0.020	0.335	0.152	0.000	0.021	0.004	1.968	2.501	2.235
CoO	ND	ND	ND	0.000	0.012	0.005	0.000	0.017	0.007	ND	ND	ND
MnO	2.043	2.810	2.376	1.243	4.865	3.516	0.000	0.166	0.043	18.187	18.327	18.257
TiO <sub>2</sub>	ND	ND	ND	50.460	55.558	51.547	69.227	83.320	77.642	ND	ND	ND
CaO	31.198	37.980	34.555	0.011	0.170	0.083	0.060	2.131	0.570	3.251	5.026	4.139
FeO	8.832	12.814	10.563	ND	ND	ND	5.490	9.352	7.0518	32.011	32.930	32.471
NiO	ND	ND	ND	ND	ND	ND	0.000	0.003	0.001	ND	ND	ND
$Al_2O_3$	ND	ND	ND	0.000	0.005	0.002	0.000	0.013	0.004	ND	ND	ND
SiO <sub>2</sub>	ND	ND	ND	0.000	0.093	0.022	0.000	0.013	0.006	ND	ND	ND
$Ta_2O_5$	ND	ND	ND	0.000	0.004	0.001	0.000	0.111	0.023	ND	ND	ND
$Cr_2O_3$	ND	ND	ND	0.000	0.044	0.019	0.000	0.045	0.011	ND	ND	ND
$V_2O_3$	ND	ND	ND	0.146	0.229	0.193	0.383	0.852	0.563	ND	ND	ND
Total	ND	ND	ND	90.243	110.871	99.385	84.812	113.698	98.980	55.417	58.786	57.102
Mineral		Niobite (%	)		Ankerite (%	5)	Kı	utnohorite (	%)	N	lagnetite (%	6)
Samples		3			4		4		2			
	Min	Max	Ave	Min	Max	Ave	Min	Max	Ave	Min	Max	Ave
Sc <sub>2</sub> O <sub>3</sub>	0.575	2.112	1.583	0.002	0.01	0.006	0.000	0.000	0.000	0.000	0.000	0.000
$Nb_2O_5$	70.760	72.411	71.411	0.000	0.034	0.017	0.000	0.043	0.013	ND	ND	ND
MgO	ND	ND	ND	8.238	8.387	8.313	1.447	8.929	3.398	ND	ND	ND
CoO	0.000	0.000	0.000	ND	ND	ND	ND	ND	ND	ND	ND	ND
MnO	6.984	7.558	7.361	3.275	3.329	3.302	8.356	18.568	11.031	ND	ND	ND
TiO <sub>2</sub>	3.291	4.130	3.847	ND	ND	ND	ND	ND	ND	0.012	0.047	0.030
CaO	0.568	0.702	0.630	26.324	26.547	26.436	22.868	45.705	39.466	ND	ND	ND
FeO	10.682	13.454	11.623	17.719	17.743	17.731	2.013	5.319	2.912	93.043	93.553	93.298
$Ce_2O_3$	0	0.166	0.055	ND	ND	ND	ND	ND	ND	ND	ND	ND
$Al_2O_3$	0.000	0.000	0.000	ND	ND	ND	ND	ND	ND	0.000	0.006	0.003
SiO <sub>2</sub>	0.004	0.038	0.016	ND	ND	ND	ND	ND	ND	0.033	0.049	0.041
Ta <sub>2</sub> O <sub>5</sub>	0.008	0.082	0.046	ND	ND	ND	ND	ND	ND	ND	ND	ND
Total	92.870	101.222	96.843	55.558	56.050	55.804	34.684	78.564	56.820	93.088	93.655	93.372

Note: "ND" in the table indicates that it was not detected.

The EPMA test results for fluorite and calcite are listed in Table 6. No  $Sc_2O_3$  was detected in these two minerals. In this study, the mineral with the highest Sc content in Bayan Obo tailings was niobite, with a content of 1.58%, and the highest content of a single point was riebeckite, with a content of 2.30%. The content of Sc in different minerals and different samples of the same mineral varied greatly, and the content of  $Sc_2O_3$  was less than 0.10% in most samples. Only five minerals were confirmed to contain Sc, and the content of  $Sc_2O_3$  in descending order was niobite, riebeckite, ilmenorutile, monazite, and aegirine. In conclusion, very low amounts of Sc are dispersed in the Bayan Obo deposit, which is consistent with previous findings. However, the results differ from those of previous studies in the following points: (1) Our result regarding niobite is consistent with previous studies, showing a relative richness of Sc. However, the average Sc content was found to be

1.58%, which is higher than that measured by predecessors (0.22%, 0.67%, and 1.26%) [36].(2) Previous researchers found ilmenorutile to have the highest scandium content [37].

	eral ples	Fluori 1			eral ples	Calcite (%) 3		
	Min	Max	Ave		Min	Max	Ave	
$Sc_2O_3$	0.000	0.000	0.000	$Sc_2O_3$	0.000	0.000	0.000	
F	46.606	49.706	48.464	FeO	0.953	1.133	1.027	
Ba	0.000	0.367	0.035	MnO	2.141	4.420	2.951	
Ca	49.964	51.666	50.776	CaO	48.233	51.538	50.084	
Ce	0.000	0.045	0.013	MgO	0.238	0.361	0.283	
Y	0.000	0.059	0.026	$Nb_2O_5$	0.000	0.021	0.007	
Total	96.570	101.843	99.314	Total	51.565	57.473	54.351	

Table 6. EPMA test results of other minerals.

However, the average scandium content in ilmenorutile was only 0.06% in this work, whereas Yang did not detect the presence of Sc in ilmenorutile [35]. (3) Aegirine was considered to be the richest Sc among the silicates [38], but the Sc content of riebeckite (0.22%) was much higher than that of aegirine (0.037%) in this study. (4) For the same sample, the content of  $Sc_2O_3$  was uniformly distributed, which was not observed in a previous study. This may be related to the conditions of mineral formation.

# 3.2. Grain Size Distribution of Valuable Minerals

An important factor in mineral flotation is the particle size, and  $-75 \ \mu m$  is generally taken as a reference. Therefore, with 75  $\mu$ m as the dividing line, the proportions of fluorite, ilmenorutile, nioboaeschynite, bastnasite, dingdaohengite, monazite, riebeckite, and hematite below 75 µm are 59.11%, 74.4%, 73.38%, 85.50%, 89.04%, 86.56%, 65.08, and 85.62%, respectively. All pyrochlore particles are below  $-75 \,\mu\text{m}$ , and their specific distributions are listed in Table 7 and Figure 8. Due to the large particles of Fe- and F-bearing minerals, further grinding is required to recover iron and fluorine via flotation. The proportions of fluorite, ilmenorutile, pyrochlore nioboaeschynite, bastnasite, dingdaohengite, monazite, riebeckite, and hematite below 20 µm are 9.20%, 21.68%, 32.33%, 17.26%, 16.82%, 11.48%, 19.79, 6.45%, and 13.05%, respectively. The proportions of ilmenorutile, pyrochlore, and nioboaeschynite below 10 µm are 6.35%, 12.14%, and 6.66%, respectively. For physical beneficiation, minerals with particle size greater than 10  $\mu$ m are easy to recover, while minerals with particle size in the range of 5–10 µm are difficult to recover, and the mineral particle size is less than 5  $\mu$ m, which belongs to mud ore and is extremely difficult to recover. Therefore, Niobium-bearing minerals are generally fine, which seriously affects the recovery of niobium using flotation.

Table 7. Particle size distributions of the main valuable minerals in Bayan Obo tailings (%).

Size (µm)	Ilmenite	Pyrochlore	Nioboaeschynite	Bastnasite	Dingdaohengite	Monazite	Riebeckite	Hematite	Fluorite
>53	42.24	7.58	43.44	31.26	33.92	25.46	51.58	28.45	57.67
45~53	0.00	16.5	5.33	10.91	6.94	8.93	7.08	10.53	7.28
38~45	1.87	12.94	5.15	9.38	10.38	8.51	7.97	9.81	7.00
22~38	27.68	23.12	23.07	26.57	30.5	30.43	22.00	30.84	18.88
10~22	21.86	27.74	16.37	17.7	16.15	21.75	10.84	18.76	8.92
<10	6.35	12.14	6.66	4.17	2.11	4.95	0.53	1.60	0.26

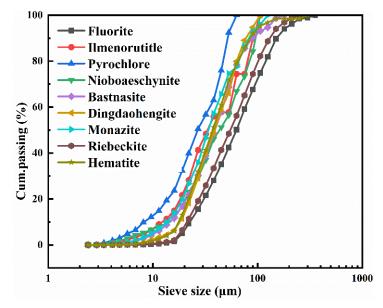


Figure 8. Cumulative particle size distributions of the main valuable minerals.

#### 3.3. The Main Valuable Minerals' Association

The free-exposed surface area method was used to analyze the association of monomer minerals, and the results are shown in Table 8. Overall, 79.39% of the fluorite was liberated, and non-liberated and partially liberated fluorite contents were closely associated with bastnasite, monazite, barite, riebeckite, hematite, siderite, ankerite, and calcite with associations of 5.32%, 1.01%, 1.38%, 3.39%, 0.74%, 1.68%, 2.28%, and 0.99%, respectively. Hence, 6.33% of the fluorite was associated with rare-earth minerals, and 8.09% of fluorite was dispersed in iron-bearing minerals. The flotation of fluorite significantly influenced the recovery of Fe and rare-earth elements but had minimal influence on the recovery of Nb and Sc. Therefore, further grinding was needed to reduce the association with other minerals and increase the degree of liberation.

Mineral	Liberated				Ass	ociation			
F1 '4	70.20	Barite	Hematite	Riebeckite	Siderite	Bastnasite	Monazite	Ankerite	Calcite
Fluorite	79.39	1.38	3.39	0.74	1.68	5.32	1.01	2.28	0.99
TT (*)	F4 00	Fluorite	Barite	Riebeckite	Apatite	Bastnasite	Quartz	Siderite	Ankerite
Hematite	74.22	9.36	1.19	3.19	1.35	2.14	2.37	1.16	1.84
Riebeckite	92 (7	Fluorite	Hematite	Barite	Quartz	Bastnasite	Monazite	Siderite	Calcite
Riebeckite	82.67	1.27	2	1.51	4.98	1.52	0.54	0.79	0.9
Manaaita	E4.14	Fluorite	Hematite	Riebeckite	Apatite	Quartz	Siderite	Ankerite	Calcite
Monazite	54.14	16.64	3.24	5.11	4.65	3.45	1.99	4.71	1.61
Dingdaohengite	(0.50	Fluorite	Hematite	Riebeckite	Barite	Apatite	Allanite	Bastnasite	Ankerite
Diliguaoriengite	60.59	13.56	2.11	3.7	1.15	2.46	1.33	3.35	4.22
Nioboaeschynite	(1.7(	Fluorite	Hematite	Riebeckite	Apatite	Bastnasite	Barite	Ilmenorutile	Ankerite
Nioboaescriyinte	61.76	10.19	1.53	3.75	3.89	2.53	2.72	1.03	2.12
Beele esta	47 05	Fluorite	Hematite	Riebeckite	Barite	Apatite	Quartz	Ankerite	Calcite
Bastnasite	47.85	24.36	3.55	4.02	1.29	7.02	2.57	3.21	1.76
		Fluorite	Hematite	Riebeckite	Barite	Monazite	magnetite	Nioboaeschynite	Biotite
Drugablana	28.09	16.59	6.17	8	3.71	2.35	1.41	2.02	1.72
Pyrochlore	38.98	Albite	Quartz	Bastnasite	Apatite	Ankerite	Wollastonite	Ilmenorutile	Calcite
		1.48	1.23	0.77	5.29	3.48	0.57	0.78	1.39

**Table 8.** Intergrowth of the main valuable minerals (%).

Mineral	Liberated	iberated Association											
		Fluorite	Hematite	Riebeckite	Barite	Quartz	Siderite	Nioboaeschynite	Ilmenite				
TI ('1	45 50	11.75	4.17	2.99	2.21	2.89	1.03	1.34	4.08				
Ilmenorutile	45.72	Baotite	Rutile	Bastnasite	Apatite	magnetite	Monazite	Ankerite	Calcite				
	-	0.95	1.16	3.26	2.78	5.05	1.63	1.93	3.15				

Table 8. Cont.

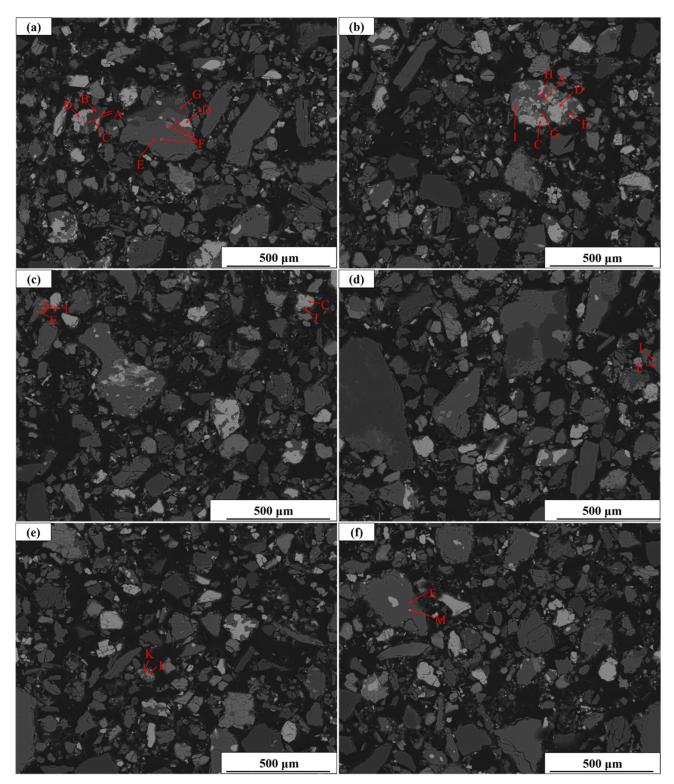
Monazite and bastnasite were liberated at 54.14% and 47.85%, respectively. Only 4.65% of the monazite and 7.02% of the bastnasite were associated with the REE-bearing mineral apatite, which could be floated and recovered together with monazite. Notably, 8.56% of monazite and 6.59% of bastnasite were associated with silicate minerals, and 16.64% and 15.05% of monazite were dispersed in fluorite and Fe-bearing minerals, respectively. In addition, 24.36% and 10.78% of bastnasite were dispersed in fluorite and Fe-bearing minerals, respectively. Hence, fluorite and Fe-bearing minerals significantly affected the flotation of monazite and bastnasite. However, bastnasite and monazite with apatite should be extracted separately. Since scandium is mainly present in silicate minerals, 1.27% of riebeckite is bonded with fluorite, so the flotation of fluorite has little influence on the recovery of Sc, and scandium mainly exists in flotation tailings. Nb-bearing minerals mainly include nioboaeschynite, pyrochlore, and ilmenorutile, which are 10.19%, 16.59%, and 11.75% bonded with fluorite, respectively. Therefore, the flotation of fluorite has a certain impact on the recovery of Nb, and part of Nb enters the flotation concentrate.

Fluorite, barite, apatite, bastnasite, and quartz were associated with 9.36%, 1.19%, 1.35%, 2.17%, and 2.37% of hematite, respectively, affecting the grade of the Fe concentrate. Hematite (6.19%) was dispersed in other Fe-bearing minerals, such as riebeckite, siderite, and ankerite. The extraction of hematite had little effect on Sc extraction but did not affect Nb extraction.

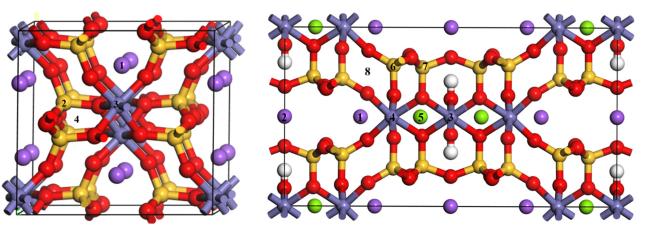
The liberation of Nb-bearing minerals, especially pyrochlore and ilmenorutile, was very low, at 38.98 and 45.72, respectively. Only 1.03%, 2.80%, and 5.42% of nioboaeschynite, pyrochlore, and ilmenorutile were associated with other Nb-bearing minerals, respectively. Hence, Nb enrichment was difficult to achieve. The BSE images of Bayan Obo rare-earth tailings are shown in Figure 9, which provide a visual illustration of the complex symbiotic relationships between minerals.

Since both Nb and Sc are partially present in ilmenorutile, Nb enrichment is accompanied by Sc enrichment to a certain extent. In total, 82.67% of the riebeckites are liberated. Therefore, Sc can be enriched by pretreatment. However, the distribution of Sc is highly scattered, and extraction is extremely difficult.

Density functional theory (DFT), which is a universal tool to predict the properties of molecules and condensed matter based on first principles [39,40], was used in this work to verify the occurrence state of Sc in aegirine. The simulated computations were conducted with the DFT-based Cambridge Serial Total Energy Package (CASTEP) code of the Materials Studio software (Materials Studio 2016, BIOVIA, San Diego, CA, USA) [41]. The valence electronic configurations of Na, Fe, O, Si, Mg, and Sc were [Ne]3s<sup>1</sup>, [Ar]3d<sup>8</sup>, [He]2s<sup>2</sup>2p<sup>4</sup>, [Ne]3S<sup>2</sup>3p<sup>2</sup>, [Ne]3s<sup>2</sup>, and [Ar]3d<sup>1</sup>4s<sup>2</sup>, respectively. The generalized gradient approximation with Perdew-Burke-Ernzerhof (GGA-PBE) was selected to calculate the exchange and correlation energies of electron–electron interactions with 400 eV of cut-off energy [42–45]. Other parameters were set as  $2.0 \times 10^{-6}$  eV/atom of energy tolerance,  $2 \times 2 \times 2$  grid of Brillouin zone, 0.05 eV/Å of force tolerance, and 0.002 Å of displacement tolerance [46]. As shown in Figure 10, a  $1 \times 1 \times 2$  supercell of aegirine and riebeckite is formed, and one Sc atom is substituted with one atom or in the interstitial lattice site. The structures were optimized according to the aforementioned parameters. The structural optimization was deemed complete when these parameters satisfied the convergence standard, and the calculation results were satisfactory.



**Figure 9.** BSE images of Bayan Obo rare-earth tailings: A, riebeckite; B, quartz; C, carite; D, bastnasite; E, fluorite; F, hematite; G, ankerite; H, apatite; I, ilmenorutile; J, dingdaohengite; K, pyrochlore; L, nioboaeschynite and M, monazite. (**a**–**f**) are SEM images of different field of view.3.4. Density Functional Theory Study of the Occurrence State of Sc in Aegirine Lattice.



**Figure 10.** Possible doping sites of  $1 \times 1 \times 2$  supercell aegirine (**left**) and  $1 \times 1 \times 2$  supercell riebeckite (**right**). The red ball represents the O atom, the purple ball represents the Na atom, the yellow ball represents the Si atom, the green ball represents the Mg atom, the white ball represents the H atom, and the lilac ball represents the Fe atom. One Sc substitutes one Na<sup>1</sup>, Si<sup>2</sup>, Fe<sup>3</sup>, and interstitial lattice site<sup>4</sup> of **left**, one Sc substitutes one Na<sup>1</sup>, Na<sup>2</sup>, Fe<sup>3</sup>, Fe<sup>4</sup>, Mg<sup>5</sup>, Si<sup>6</sup>, Si<sup>7</sup>, and interstitial lattice site<sup>8</sup> of **right**.

# 3.4. Formation of Sc in Aegirine Lattice

The formation energy ( $\Delta E$ ), which is used to analyze and compare the difficulty of formation with different impurity defects, refers to the energy required for an Sc atom to merge into the aegirine crystal and is calculated using the following formula [41,47]:

$$\Delta E = E_{impurity} + E_x - E_{perfect} - E_y \tag{1}$$

where  $E_{impurity}$  is the energy of aegirine with impurity defects;  $E_{perfect}$  is the energy of the perfect aegirine; x is the Na atom, Fe atom, or Si atom in aegirine; y is the Sc atom of the impurity; and  $E_x$  and  $E_y$  are the energies of the x atom and y atom, respectively. In the case of doping in a lattice gap,  $E_x = 0$  eV. Under the same calculation conditions, the smaller the value of  $\Delta E$ , the greater the possibility of the corresponding doping form. The four doping forms that represent the four occurrence states of Sc in aegirine and riebeckite are as follows:

$$Na_8 Fe_8 Si_{16}O_{48} + Sc \rightarrow Na_7 Sc Fe_8 Si_{16}O_{48} + Na$$
<sup>(2)</sup>

$$Na_8Fe_8Si_{16}O_{48} + Sc \rightarrow Na_8Fe_7ScSi_{16}O_{48} + Fe$$
(3)

$$Na_8 Fe_8 Si_{16} O_{48} + Sc \rightarrow Na_8 Fe_8 Si_{15} Sc O_{48} + Si$$

$$(4)$$

$$Na_8 Fe_8 Si_{16} O_{48} + Sc \rightarrow Na_8 Sc Fe_8 Si_{16} O_{48}$$
(5)

$$Na_{12}Fe_{12}Mg_8Si_{32}O_{96}H_8 + Sc \rightarrow Na_{11}ScFe_{12}Mg_8Si_{32}O_{96}H_8 + Na$$
 (6)

$$Na_{12}Fe_{12}Mg_8Si_{32}O_{96}H_8 + Sc \rightarrow Na_{12}Fe_{11}ScMg_8Si_{32}O_{96}H_8 + Fe$$
 (7)

$$Na_{12}Fe_{12}Mg_8Si_{32}O_{96}H_8 + Sc \rightarrow Na_{12}Fe_{12}Mg_7ScSi_{32}O_{96}H_8 + Mg$$
(8)

$$Na_{12}Fe_{12}Mg_8Si_{32}O_{96}H_8 + Sc \to Na_{12}Fe_{12}Mg_8Si_{31}ScO_{96}H_8 + Si$$
(9)

$$Na_{12}Fe_{12}Mg_8Si_{32}O_{96}H_8 + Sc \rightarrow Na_{12}Fe_{12}ScMg_8Si_{32}O_{96}H_8$$
 (10)

The Crystallographic Information File (cif) of aegirine and riebeckite was downloaded from the American Mineralogist Crystal Structure Database (AMCSD) [48,49], and the lattice parameters of aegirine were a = 9.6554 Å, b = 8.7952 Å, c = 10.5884 Å,  $\alpha = 90^{\circ}$ ,  $\beta = 107.396^{\circ}$ , and  $\gamma = 90^{\circ}$ . After optimization, the lattice parameters were a = 9.5727 Å, b = 8.7007 Å, c = 10.6098 Å,  $\alpha$  = 89.999°,  $\beta$  = 108.499°, and  $\gamma$  = 90°, which were very close to the experimental values in the literature [50,51]. The formation energies of Reactions (2)–(5) are shown in Table 9. The smallest of the four formation energies was -8.60 eV of Reaction (5), indicating that the most likely Sc doping occurred in the aegirine interstitial lattice site. In addition, the value of -6.88 eV for Reaction (3) was relatively small, indicating that Sc may also have a high probability of being present in aegirine upon Fe doping. The formation energies of Reactions (2) and (4) were -3.72 eV and 0.03 eV, respectively. This was much higher than those of the other reactions, indicating that Sc had a small chance of substituting Na and Si. Notably, the values of Reactions (2), (3) and (5) were negative, indicating that it was not very difficult for Sc to enter the aegirine cells under normal temperature and pressure.

**Table 9.** Formation energy ( $\Delta E$ ) of the Sc in aegirine and the lattice parameters of different cells containing Sc.

Species	$\Delta E$ (eV)	a	b	с	α	β	γ	V (Å <sup>3</sup> )
Perfect		9.5727	8.7007	10.6098	89.999	108.499	90	838.015
Sc for Na <sup>1</sup>	-3.72	9.6062	8.6819	10.5824	89.999	108.527	89.999	836.832
Sc for Fe <sup>3</sup>	-6.88	9.6208	8.7433	10.6389	89.997	108.275	89.996	849.78
Sc for Si <sup>2</sup>	0.03	9.6499	8.7368	10.6567	89.689	108.526	89.382	851.81
Sc in interstitial lattice site <sup>4</sup>	-8.60	9.6668	8.8179	10.5859	90.1197	109.285	89.9701	851.724

Note: 1, 2, 3, and 4 indicate the replacement position.

The lattice parameters of riebeckite were a = 9.860 Å, b = 18.070 Å, c = 5.333 Å,  $\alpha$  = 90°,  $\beta$  = 105.48°, and  $\gamma$  = 90°. After optimization, the lattice parameters were a = 9.873 Å, b = 17.735 Å, c = 5.307 Å,  $\alpha$  = 90.000°,  $\beta$  = 103.390°, and  $\gamma$  = 90°, which were very close to the experimental values in the literature [52]. The formation energies of Reactions (6)–(10) are shown in Table 10. Since Na, Fe, and Si in riebeckite had two different sites each, there were a total of eight alternative sites, as shown in Figure 10. The formation energies of Reaction (7) in two different Fe sites were –5.05 eV and –6.26 eV, respectively, indicating that Sc may also have a high probability of being present in riebeckite upon Fe doping. The formation energies of Reaction (10) was 1.92 eV, indicating that it was very difficult for Sc doping in the riebeckite interstitial lattice site.

**Table 10.** Formation energy ( $\Delta E$ ) of Sc in riebeckite and the lattice parameters of different cells containing Sc.

Species	$\Delta E$ (eV)	а	b	с	α	β	γ	V (Å <sup>3</sup> )
Perfect		9.873	17.735	5.307	90.000	103.390	90.000	1807.982
Sc for Na <sup>1</sup>	-1.38	9.895	17.820	10.582	90.000	103.410	90.000	1805.116
Sc for Na <sup>2</sup>	2.31	9.795	17.757	10.629	90.000	103.114	90.000	1800.400
Sc for Fe <sup>3</sup>	-5.05	9.880	17.752	10.644	90.000	103.135	90.000	1818.051
Sc for Fe $^4$	-6.26	9.910	17.821	10.625	90.000	103.365	90.000	1825.668
Sc for Mg <sup>5</sup>	863.05	9.852	17.771	10.603	90.008	103.513	90.002	1805.104
Sc for Si <sup>6</sup>	-0.58	9.887	17.736	10.648	90.149	103.694	90.004	1814.078
Sc for Si <sup>7</sup>	-0.41	9.904	17.790	10.629	89.863	103.615	90.442	1820.183
Sc in interstitial lattice site <sup>8</sup>	1.92	9.912	17.896	10.670	90.000	103.021	90.000	1844.043

Note: 1, 2, 3, 4, 5, 6, 7, and 8 indicate the replacement position.

The lattice parameters of different cells containing Sc are listed in Tables 9 and 10. The results showed that the cell volumes of aegirine with Sc for Fe, Si, and the interstitial lattice site were 849.78 Å<sup>3</sup>, 851.81 Å<sup>3</sup>, and 851.724 Å<sup>3</sup>, respectively, which were greater than the 838.015 Å<sup>3</sup> of perfect cell volume. This phenomenon also appeared in the Sc doping of riebeckite. This may be because the ionic radius of Sc<sup>3+</sup> (~81 Å) is larger than those of

 $Fe^{3+}$  (~64 Å) and Si<sup>4+</sup> (~42 Å) [53]. Therefore, the replacement of Sc for Na reduced the cell volume of aegirine because of the smaller ionic radius of Sc<sup>3+</sup> (~81 Å) than Na<sup>+</sup> (~95 Å).

#### 3.5. Proposed Flowsheet for Comprehensive Utilization of Tailings

A feasible process for the comprehensive utilization of Bayan Obo rare-earth tailings was designed based on the study of process mineralogical characterization, as shown in Figure 11. The flowsheet includes physical, pyrometallurgical, and hydrometallurgical processes.

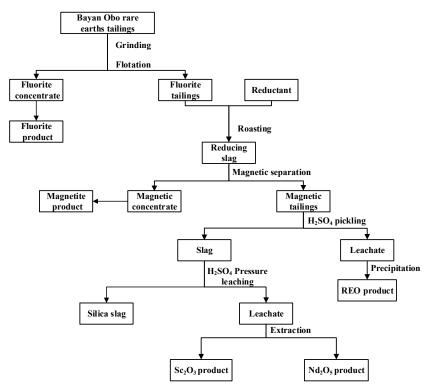


Figure 11. Flowsheet for comprehensive utilization of tailings.

Since 97.20% of the F element exists in 26.8% of the fluorite in Bayan Obo rare-earth tailings, the monomer dissociation of fluorite is 79.39%, and the fluorite particles above 53  $\mu$ m account for 57.67%; therefore, further grinding is needed to reduce the size of the fluorite particles and increase the liberation of the fluorite. The ground pulp is floated to produce a fluorite concentrate and tailings that are enriched in Fe, REE, Nb, and Sc. Because Sc mainly occurs in silicate minerals and some Nb-bearing minerals, in which it exists only in minor amounts, Sc and Nb need further enrichment. Hematite in the fluorite flotation tailings was magnetized (transformed to magnetite) by roasting under reducing conditions. Magnetite was then separated from the tailings via magnetic separation, enriching the residual tailings in REE and Nb. REE in tailings is mainly found in bastnasite, which can be decomposed at low temperatures by dilute acid, whereas minerals containing Sc and Nb are not easily decomposed at low temperatures. Therefore, more than 70% of REE can be recovered via low-temperature acid pickling. Finally, the pickled slag is leached under pressure to obtain a solution containing Nb, Sc, and non-toxic Si slag, which can be used as building materials. The entire process makes full use of valuable elements in tailings and is environmentally friendly.

### 4. Conclusions

Detailed mineralogical and chemical analyses of Bayan Obo rare-earth tailings were conducted with MLA, EPMA, XRD, ICP, and other analytical techniques. Valuable elements in the tailings include Fe, Fe, REE, and Nb; based on their deportment, a feasible flowsheet

was proposed for their recovery. The mineralogical parameters provide theoretical guidance and reference values for improving the beneficiation process of this type of tailing and the recycling of other valuable minerals.

There are numerous minerals in Bayan Obo tailings with complex symbiosis, with 97.2% of F present in fluorite and 50.15% of Fe in hematite, which was easily separated through magnetization. Bastnasite contained more than 60% REE, and nioboaeschynite contained 48.47% Nb. Sc was primarily found in aegirine, riebeckite, monazite, ilmenorutile, and niobite, with the highest average content of 1.85% in niobite. The DFT calculation results showed that Sc existed in the form of Fe substitution or intergranular doping in aegirine with a high probability.

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