



Article Model-Free Non-Cascade Integral Sliding Mode Control of Permanent Magnet Synchronous Motor Drive with a Fast Reaching Law

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Abstract: Electric vehicle has become the main trend of the development of automobile industry. As a highly symmetrical system, the characteristics of drive motor will have a great impact on the driving comfort. Aiming at the control regulation of permanent magnet synchronous motor (PMSM) drive, a model-free and non-cascade sliding mode control with a fast-reaching law is proposed in this paper. Firstly, the mathematical model of PMSM is constructed as an ultra-local model without considering any motor parameters. Then, to improve the response speed, an integral sliding mode method with a fast reaching law is proposed, and the fast convergence can be realized. The controller system adopts single loop non-cascade control, which greatly simplifies the system structure. In order to further improve the anti-disturbance performance of the system, the dual disturbance observers are used to compensate the disturbance through feed-forward control. The stability of the system is proved by Lyapunov. Finally, the experimental results show that the proposed method has faster convergence speed and stronger anti-disturbance ability.

Keywords: permanent magnet synchronous motor; model-free control; fast sliding mode reaching law; dual disturbance observers; electric vehicle

1. Introduction

Due to its high power, high reliability and strong practicability, permanent magnet synchronous motor (PMSM) has been widely used in the symmetrical structure with complex working condition, such as electric vehicle, robot and other industrial productions [1]. The ride quality and driving comfort of electric vehicle are closely related to the dynamic performance of motor driver system, and the electric vehicle creates a symmetrical entity with the road during operation, and its reference frame is represented by the dynamic, the control characteristics of drive motor also have the direct impact on battery performance. Commonly, the double-loop cascade control with PI approach through field-oriented control is adopted [2]. However, due to the strongly coupled nonlinear characteristics, and the influence of external uncertain factors such as load torque and parameters uncertainties, it is difficult to achieve good control performance by the common PI control method. In recent years, to improve the dynamic response and anti-disturbance performance, some advanced control algorithms have been proposed to improve the motor control performance, such as sliding mode control [3,4], model predictive control [5], model-free adaptive control [6], backstepping control [7].

Among these methods, sliding mode control, which is a kind of variable structure control [8] attracts the attention because of its fast convergence speed and robustness. However, common linear sliding mode control is difficult to achieve finite time convergence. Although terminal sliding mode control [9] can achieve finite time convergence, its convergence speed is not ideal. The integral sliding mode method accelerates the convergence rate of the system. Integral sliding mode control can eliminate the reaching phase by



Citation: Li, T.; Liu, X. Model-Free Non-Cascade Integral Sliding Mode Control of Permanent Magnet Synchronous Motor Drive with a Fast Reaching Law. *Symmetry* **2021**, *13*, 1680. https://doi.org/10.3390/ sym13091680

Academic Editors: Yunlong Shang, Jufeng Yang and Qi Zhang

Received: 15 August 2021 Accepted: 9 September 2021 Published: 12 September 2021

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Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). enforcing sliding mode throughout the whole process of system response and thus the invariance of the system to parameter variation is guaranteed starting from the initial time instant [10]. Sliding mode control is usually divided into two parts, one is sliding mode surface design and the other is reaching law control. The reaching law control is directly related to the process of reaching the sliding surface. In [11], an exponential approximation law is proposed to accelerates the convergence speed. By adding a terminal attractor to the arrival law [12], the convergence speed is effectively accelerated, but the parameter adjustment is complex. The system state variables and the power term of the sliding mode function are introduced in a new sliding mode reaching law to improves the convergence speed of the system [13].

In addition, sliding mode control can suppress the matched disturbance in the system, which means the uncertainties exist in the same channel as that of the control input [14,15]. But it is weak in suppressing the mismatched disturbance, such as the load disturbance of PMSM in non-cascade control. The disturbance rejection technique based on disturbance observer becomes an effective method to deal with the disturbance, such as disturbance observer [16], extended disturbance observer [17,18], finite time disturbance observer [19], nonlinear disturbance observer [20], sliding mode observer [21], reduced-order observer [22].

Although sliding mode control has some robustness for the disturbance, it is still a model-based control method, and the control performance has a high dependence on the motor parameters. In the process of motor operation, it is difficult to accurately know the motor parameters. Recently, the model-free control has aroused wide attention. It is based on the ultra-local model, which is established by the input and output of the system [23]. The technology does not depend on the parameters of the control system, and it has been used in parking system [24], robot [25], PMSM [26]. In [27], a model-free predictive current control method based on an ultra-local model is proposed for PMSM. This method only uses the input and output of the system without considering any motor parameters. The model-free adaptive integral sliding mode is applied to PMSM to achieve a good speed tracking effect [6]. In [28], a non-cascaded model-free predictive speed control of PMSM is proposed to achieve fast dynamic response.

In this paper, a model-free non-cascade integral sliding mode control of permanent magnet synchronous motor drive with a fast reaching law is proposed. The experimental results show that the proposed method has fast convergence and good anti load disturbance ability. The main contributions are as follows:

(1) A fast sliding mode reaching law is proposed for PMSM drive to improve the convergence rate.

(2) By introducing model-free control, the model is simplified and the dependence on motor parameters is avoided.

(3) By combining the proposed sliding mode control method, the dual disturbance observers are designed to further improve the anti-disturbance ability of the drive system.

This article is organized as follows. In Section 2, the model-free mathematical model of permanent magnet synchronous motor is presented. The design of double disturbance observers is introduced in Section 3. Section 4 describes the design of non-cascade integral sliding mode control with a fast reaching law. Experiments are verified in Section 5. Conclusion is followed in Section 6.

2. Ultra-Local Model of PMSM

The mathematical model of permanent magnet synchronous motor in the d-q axis rotor coordinate system can be expressed as [29,30]

$$\begin{cases} \frac{di_d}{dt} = \frac{-R_s i_d + n_p \omega L_q i_q}{L_d} + \frac{u_d}{L_d} + f_d \\ \frac{di_q}{dt} = \frac{-R_s i_q - n_p \omega L_d i_d}{L_q} - \frac{n_p \omega \Phi}{L_q} + \frac{u_q}{L_q} + f_q \\ \frac{d\omega}{dt} = \frac{n_p [(L_d - L_q) i_d i_q + \Phi i_q]}{J} - \frac{B}{J} \omega + f_\omega \end{cases}$$
(1)

where L_d , L_q are d-axis and q-axis stator inductances, i_d and i_q are the stator current, u_d and u_q are stator voltage, R_s is the stator resistance, n_p is the number of pole pairs, Φ is the rotor flux, J is the inertia, B is the coefficient of friction, ω is the mechanical angular speed. f_d , f_q , f_ω represent the disturbance caused by parameters variation, model uncertainties and external load disturbance, which are considered as bounded and change slowly during motor operation.

The electromagnetic torque is

$$T_e = n_p [(L_d - L_q)i_d i_q + \Phi i_q]$$
⁽²⁾

For surface PMSM, the d-axis inductance is equal to the q-axis inductance ($L_d = L_q$) and the electromagnetic torque can be expressed $T_e = n_p \Phi i_q$. From the third equation in Equation (1), which can be simplified as

$$\frac{d\omega}{dt} = \frac{n_p \Phi i_q}{J} - \frac{B}{J}\omega + f_\omega \tag{3}$$

According to the reference [23], the second and third expressions in the motor model (1) can be rewritten as

$$\begin{cases} \frac{di_q}{dt} = (\frac{1}{L_q} - \alpha_1)u_q + \frac{-R_s i_q - n_p \omega L_d i_d - n_p \omega \Phi}{L_q} + f_q + \alpha_1 u_q \\ \frac{d\omega}{dt} = (\frac{n_p \Phi}{J} - \alpha_2)i_q - \frac{B}{J}\omega + f_\omega + \alpha_2 i_q \end{cases}$$
(4)

where α_1 , α_2 are proportional adjustable factors, and the selection of parameters will affect the motor control performance. Then (4) can be rearranged as an ultra-local model

$$\begin{cases} \dot{i}_q = \alpha_1 u_q + F_q \\ \dot{\omega} = \alpha_2 i_q + F_\omega \end{cases}$$
(5)

where $F_q = (\frac{1}{L_q} - \alpha_1)u_q + \frac{-R_s i_q - n_p \omega L_d i_d - n_p \omega \Phi}{L_q} + f_q$ and $F_\omega = (\frac{n_p \Phi}{J} - \alpha_2)i_q - \frac{B}{J}\omega + f_\omega$ are lumped disturbances including parameter uncertainties and external unknown disturbances. Define the speed error *e* as

$$e = \omega_r - \omega \tag{6}$$

where ω_r and ω are desired speed and actual speed.

Define the state variables as $x_1 = e$, $x_2 = -\alpha_2 i_q$. Then, the derivation of x_1 and x_2 can be expressed as

$$\dot{x}_1 = \dot{\omega}_r - \dot{\omega} = -\alpha_2 i_q - F_\omega + \dot{\omega}_r \tag{7}$$

$$\dot{x}_2 = -\alpha_2(\alpha_1 u_q + F_q) \tag{8}$$

Then, (7) and (8) can be rewritten as

where $d_1 = -F_{\omega} + \dot{\omega}_r$, $\alpha_3 = -\alpha_2 \alpha_1$ and $d_2 = -\alpha_2 F_q$. d_1 and d_2 are matched disturbance and mismatched disturbance, respectively. Assumed that the disturbance is bounded and changed slowly in the system [31,32], thus the boundary of the disturbances in PMSM can be expressed as $|d_1| \le D_1$, $|\dot{d_1}| \le D_{11}$, and $|d_2| \le D_2$, $|\dot{d_{22}}| \le D_{22}$, where D_1 , D_{11} , D_2 , D_{22} are positive.

3. Design of Dual Disturbance Observers

Consider the uncertainty of the motor parameters and the influence of the load torque, in order to improve the anti-disturbance ability of the system, according to the principle of observer [33], the dual disturbance observers are designed to estimate the matched and mismatched disturbance in the system.

3.1. Design of Matched Disturbance Observer

The estimation of d_2 can be designed as

$$\begin{cases} \hat{d}_2 = p_1 + l_1 x_2 \\ \dot{p}_1 = -l_1 (\alpha_3 u_q + \hat{d}_2) \end{cases}$$
(10)

where \hat{d}_2 is the estimate of d_2 , p_1 is an internal variable, and l_1 is positive.

Proof. The estimation error is defined as $\varepsilon_1 = d_2 - \hat{d}_2$ and the derivation of the estimation error can be expressed as

$$\dot{\varepsilon}_1 = \dot{d}_2 - \dot{d}_2 = \dot{d}_2 - l_1 \varepsilon_1 \tag{11}$$

Let $V_1 = \frac{1}{2}\varepsilon_1^2$, and derivation of V_1 can be obtained as

$$\dot{\lambda}_1 = \dot{d}_2 \varepsilon_1 - l_1 \varepsilon_1^2 \tag{12}$$

Considering that the motor parameters change slowly in operation, assumed $\dot{d}_2 \approx 0$, and $\dot{V}_1 \leq 0$, the observer is asymptotically stable. \Box

3.2. Design of Mismatched Disturbance Observer

For the mismatched disturbance d_1 in (9), the following disturbance observer can be designed as

$$\begin{cases} d_1 = p_{21} + l_{21}x_1 \\ \dot{p}_{21} = -l_{21}(x_2 + \hat{d}_1) + \dot{\hat{d}}_1 \\ \dot{\hat{d}}_1 = p_{22} + l_{22}x_1 \\ \dot{p}_{22} = -l_{22}(x_2 + \hat{d}_1) \end{cases}$$
(13)

where p_{21} , p_{22} are internal variable, l_{21} , l_{22} are observer parameters and they are positive. **Proof.** Define

$$\tilde{\varepsilon}_2 = \left[\begin{array}{cc} \tilde{d}_1 & \tilde{d}_1 \end{array} \right]^T \tag{14}$$

$$\tilde{d_1} = d_1 - \hat{d_1}$$
 (15)

$$\tilde{d}_1 = \dot{d}_1 - \dot{d}_1$$
 (16)

where \tilde{d}_1 is the estimation error of d_1 , \tilde{d} is the estimation error of \dot{d}_1 . The derivative of \tilde{d}_1 is obtained by combined (13)

$$\dot{d}_1 = \dot{d}_1 - \dot{d}_1 = \dot{d}_1 - l_{21}\tilde{d}_1 - \dot{d}_1 = -l_{21}\tilde{d}_1 + \tilde{d}_1$$
(17)

Similar, $\dot{\tilde{d}}_1$ can be expressed as

$$\tilde{\vec{d}}_1 = \vec{d}_1 - \hat{\vec{d}}_1 = \vec{d}_1 - l_{21}\tilde{\vec{d}}_1 \tag{18}$$

The error dynamic equation of the observer can be expressed as

$$\dot{\tilde{\varepsilon}_2} = D\tilde{\varepsilon}_2 + E\ddot{d}_1 \tag{19}$$

$$D = \begin{bmatrix} -l_{21} & 1\\ -l_{22} & 0 \end{bmatrix} E = \begin{bmatrix} 0\\ 1 \end{bmatrix}$$
(20)

Considering that the disturbance changes slowly and bounded, $|d_1| \le D_1$, $|\dot{d}_1| \le D_{11}$, $\ddot{d}_1 \approx 0$. Because the observer parameters l_{21} and l_{22} are positive, according to Helviz's theorem, the observer is asymptotically stable. \Box

4. Design of Non-Cascade Integral Sliding Mode Control with a Fast Reaching Law

In order to realize the fast-tracking performance of PMSM, an integral sliding mode control with a fast sliding mode reaching law is designed in this part. The control block diagram is shown in Figure 1. In the traditional cascade control, the controller parameters should be tuned separately from the inner to the outer loop. And to avoid ringing and large overshoots, bandwidth of cascade controllers is often limited [34,35]. In this paper, the proposed non-cascade control method can effectively simplify the system structure and reduces the control periods between the speed loop and the current loop [36].

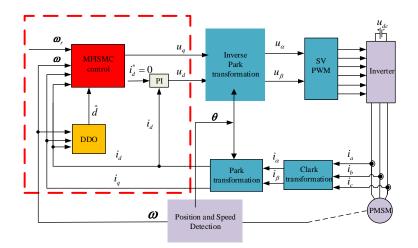


Figure 1. Control block diagram.

Firstly, an integral sliding surface is designed as [37]

$$s = \dot{e} + \alpha e + \beta \int e(\tau) d\tau$$
(21)

where α , β are positive. Then, take the derivate of Equation (21) and combined (9)

$$\dot{s} = \alpha_3 u_q + d_2 + \dot{d}_1 + \alpha (x_2 + d_1) + \beta e \tag{22}$$

In order to realize the sliding mode control, the common exponential reaching law is

$$\dot{s} = -m_1 \operatorname{sgn}(s) - m_2 s \tag{23}$$

where m_1 , m_2 are positive. The common exponential reaching law can only guarantee the faster convergence, when the sliding states are near to the sliding mode surface. A fast reaching law proposed with reference to [13]

$$\dot{s} = -k_1 \text{sgn}(s) - k_2 s - k_3 |s|^{b \text{sgn}(|s|-1)} s \tag{24}$$

where k_1 , k_2 , k_3 are positive. When the system is far away from the sliding mode surface, and s > 1, the sliding mode surface can be simplified as $\dot{s} = -k_1 - k_2 s - k|s|^b s$, its convergence speed is obviously faster than the common exponential reaching law. When s < 1, $-k_1 \text{sgn}(s) - k_2 s - k_3 |s|^{\text{bsgn}(|s|-1)} s$ become $-k_1 \text{sgn}(s) - k_2 s - k|s|^{-b} s$, similarly, the convergence speed is also faster than the common exponential reaching law. In conclusion, the fast reaching law has faster convergence speed.

Combined (22) and (24), the sliding mode control law can be derived as

$$u_q = \frac{-k_1 \text{sgn}(s) - k_2 s - k_3 |s|^{b \text{sgn}(|s|-1)} s - d_2 - \dot{d}_1 - \alpha (x_2 + d_1) - \beta e}{\alpha_3}$$
(25)

The above formula contains the amount of disturbances d_1 and d_2 , which are replaced by the estimated value of disturbance. The control law can be rewritten as

$$u_q = \frac{-k_1 \text{sgn}(s) - k_2 s - k_3 |s|^{b \text{sgn}(|s|-1)} s - \hat{d}_2 - \hat{d}_1 - \alpha (x_2 + \hat{d}_1) - \beta e}{\alpha_3}$$
(26)

Let $V = \frac{1}{2}s^2$, assumed that $\left| (\hat{d}_2 - d_2) \right| \le C_2$, $\left| (\hat{d}_1 - \hat{d}_1) \right| \le C_{11}$, $\left| (\hat{d}_1 - d_1) \right| \le C_1$, and C_1 , C_{11} , C_2 are positive, the derivative of \dot{V} is obtained by combined (9), (21) and (26)

$$\dot{V} = s\dot{s}
= s(\ddot{e} + \alpha \dot{e} + \beta e)
= s(\alpha_3 u_q + \dot{d}_1 + d_2 + \alpha(x_2 + d_1) + \beta e)
= s(-k_1 \text{sgn}(s) - k_2 s - k_3 |s|^{\text{bsgn}(|s|-1)} s - (\hat{d}_2 - d_2) - (\hat{d}_1 - \dot{d}_1) - \alpha(\hat{d}_1 - d_1))
\leq -k_2 s^2 - k_3 |s|^{\text{bsgn}(|s|-1)} s^2 + (C_2 + C_{11} + \alpha C_1 - k_1) |s|$$
(27)

when k_1 satisfies $C_2 + C_{11} + \alpha C_1 \le k_1$, $\dot{V} \le 0$, so the system is asymptotically stable.

5. Experimental Results and Analysis

In order to verify the effectiveness of the proposed model-free non-cascade integral sliding mode control of PMSM with the fast reaching law, the experiments are carried out in this section. In this experiment, a 130MB150A non-salient pole permanent magnet synchronous motor drive system is taken as an example. The experimental platform is shown in the Figure 2. The configuration of experimental system is shown in the Figure 3. The switching frequency of the IGBT is chosen as 10 kHz. After building the MATLAB/Simulink of the simulation host, the control algorithm is compiled into the object code. Then, it is downloaded to the target computer to run through the RT-SIM software. The PMSM is controlled through a special control card, so that the control performance of the proposed method can be verified conveniently in real time. The motor parameters are shown in Table 1.

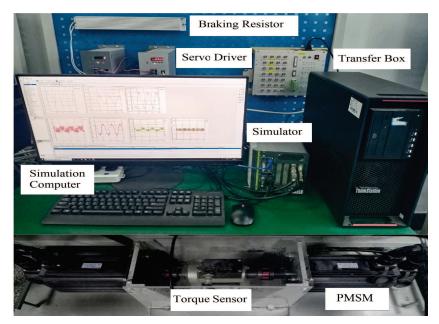


Figure 2. Experimental platform.

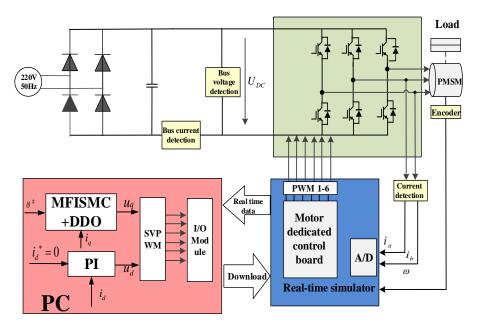


Figure 3. The configuration of the experimental PMSM drive system.

Table 1. Parameters of PMSM.

Description	Value	Unit
rated speed	1000	RPM
rated power	1.5	KW
moment of inertia	0.0027	kg⋅m ²
permanent magnet flux	0.32	Wb
line resistance	1.84	Ω
line inductance	6.65	mH
number of pole pairs	4	

In order to verify the fast-tracking performance of MFISMC + DDO, the proposed method is compared with PI controller and integral sliding mode control with exponential reaching law based on disturbance observers (ISMC+ DDO) in the experiment. In the PI control, the parameters of the speed loop are selected as $K_p = 0.04$, $K_i = 0.5$, and the two current loops are selected for the same parameters as $K_p = 9$, $K_i = 100$. In order to reduce chattering, b, k_3 are selected with smaller parameters. To ensure the faster convergence rate, k_2 , α , β are selected with larger parameters in the controller, and larger parameters will cause corresponding overshoot. Especially if the value of β is too large, it will cause a large overshoot. In order to alleviate the above problems, the parameters of the observer can alleviate the problem of excessive parameter selection of the controller to a certain extent. At the same time, the larger parameters of the observer can reduce the speed drop and accelerate the recovery time of the speed drop. In order to weigh the effects of fast convergence, speed overshoot, chattering and anti-disturbance, the parameters are obtained by trial and error method. The corresponding parameters are $l_1 = 25$, $l_{21} = 2$, $l_{22} = 30, b = 0.5, k_1 = 100, k_2 = 500, k_3 = 20, \alpha = 450, \beta = 10$. The system has obtained fascinating control effect through the final parameter selection.

In the process of motor starting, the load torque is 0.5 Nm. The reference speed is given as 200 RPM, 600 RPM and 1000 RPM. The speed waveforms with three methods are shown in Figure 4. It can be seen from the Figure 4 that ISMC + DDO and MFISMC + DDO methods almost have no overshoot. The overshoot of PI method with 200 RPM, 600 RPM and 1000 RPM is 28 r, 48 r, 81 r, respectively. The response time of PI, ISMC + DDO and MFISMC + DDO and MFISMC + DDO and MFISMC + DDO and mFISMC + DDO method at 200 RPM is 0.50 s, 0.27 s, 0.20 s, respectively. And the response time of the three methods at 600 RPM is 0.56 s, 0.29 s, 0.23 s, respectively.

response time of the three methods at 1000 RPM is 0.58 s, 0.32 s, 0.23 s, respectively. It can be seen from the experimental results that MFISMC + DDO method has the smaller overshoot and faster response speed under different speed.

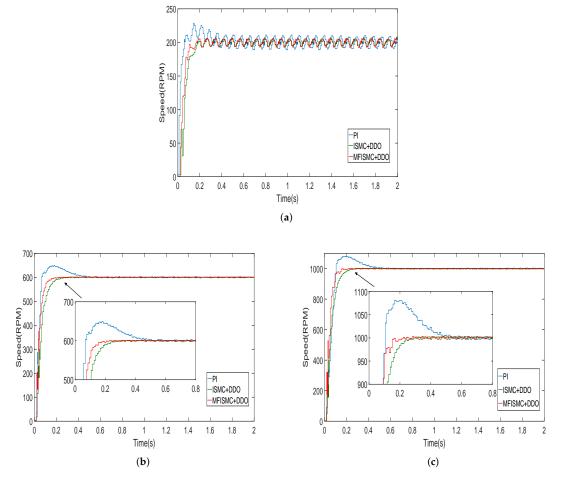


Figure 4. Experimental waveforms at different speeds: (a) n = 200 RPM; (b) n = 600 RPM; and (c) n = 1000 RPM.

In order to verify the anti-disturbance performance of the proposed method, the following experiments are carried out. The 1 Nm load disturbance is added to the PMSM at 5 s, and the load torque is removed at 10 s. The experimental results are shown in the Figure 5. The dq-axis current waveform of MFISMC + DDO method at different speeds is shown in Figure 6. The electromagnetic torque curve of MFISMC+DDO method is shown in Figure 7. Estimated value of d_1 is shown in Figure 8. In Figure 5, taking 1000 RPM as an example, the speed fluctuation and response time of MFISMC + DDO, PI and ISMC + DDO methods at 5 s are 13 r, 24 r, 15 r, and 0.20 s, 0.28 s, 0.23 s. At 10 s, the speed fluctuation and response time of the three methods are 14 r, 20 r, 14 r and 0.19 s, 0.24 s, 0.21 s. The experimental results show that the proposed MFISMC + DDO method has the faster recovery speed and the smaller speed fluctuation under load disturbance. The speed fluctuation and recovery time under other reference speed are shown in Table 2. The experimental results show that the proposed method has better anti-disturbance performance.

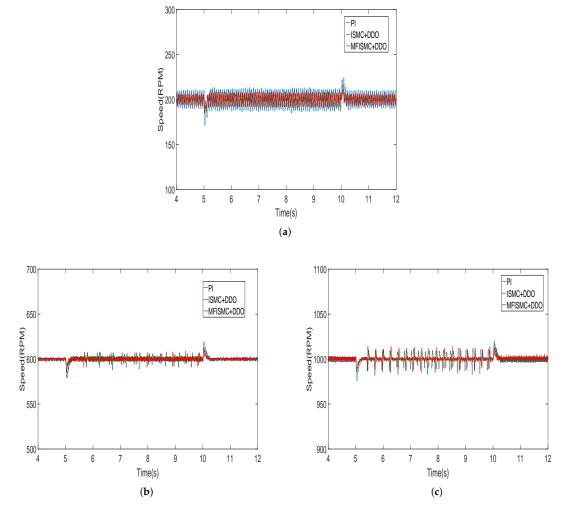


Figure 5. Experimental waveforms of different speeds under 1 Nm load disturbance: (**a**) n = 200 RPM; (**b**) n = 600 RPM; and (**c**) n = 1000 RPM.

Speed (RPM)	Control Scheme	Speed Fluctuation (RPM)		Adjustment Time (s)	
		Load Up	Load Down	Load Up	Load Down
200	MFISMC + DDO	-15	+13	0.12	0.21
	ISMC + DDO	-14	+16	0.15	0.21
	PI	-29	+ 24	0.19	0.25
600	MFISMC + DDO	-14	+13	0.12	0.16
	ISMC + DDO	-15	+13	0.14	0.19
	PI	-21	+19	0.25	0.24
1000	MFISMC + DDO	-13	+14	0.20	0.19
	ISMC + DDO	-15	+14	0.23	0.21
	PI	-24	+20	0.28	0.24

Table 2. The detailed performance comparison of three kinds of controllers under different reference speed.

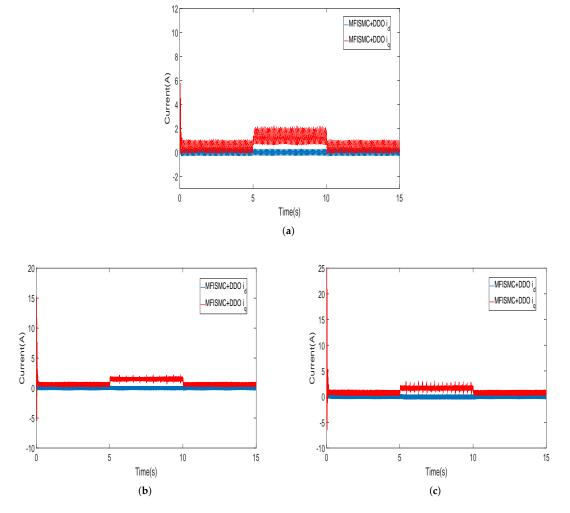


Figure 6. Dq-axis current waveform of MFISMC + DDO method at different speeds: (a) n = 200 RPM; (b) n = 600 RPM; and (c) n = 1000 RPM.

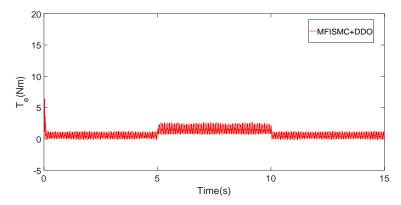


Figure 7. Electromagnetic torque waveform of MFISMC+DDO method under 1 Nm load disturbance.

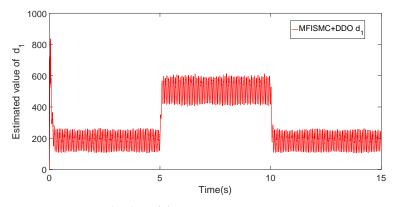


Figure 8. Estimated value of *d*₁.

In order to test the reversal performance of the proposed method, the reverse experiment is carried out. The reversal experiment is to verify the control effect of the proposed method when reversing and changing from positive to reverse. First, the reversal experiments with -200 RPM, -600 RPM and -1000 RPM are carried out. The experimental results are shown in the Figure 9. From the experimental results, the response speed and overshoot of reverse rotation are basically the same as those of forward rotation. The reverse start performance of MFISMC + DDO method is better than that of PI and ISMC + DDO methods. This effectively proves that the proposed method also has a good control effect during reversal. In order to further verify the reversal performance of the proposed method during operation, the experiments from forward rotation to reverse rotation are also carried out. When the motor runs at 200 RPM and 400 RPM, respectively, the speed is changed to -200 RPM and -400 RPM at 5 s. The experimental results are shown in Figure 10. The experimental results also show that the overshoot and response time of the MFISMC + DDO method are better than that of the PI and ISMC + DDO methods. It is proved that the proposed method also has excellent performance in inversion.

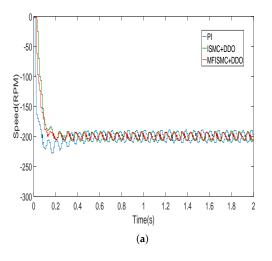


Figure 9. Cont.

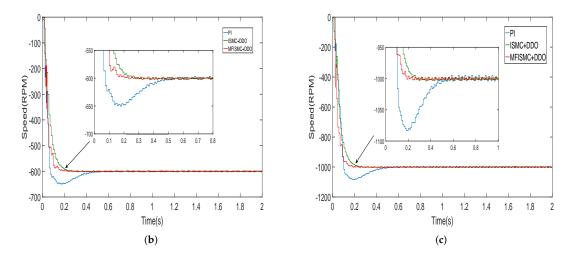


Figure 9. Experimental curves of different speeds: (a) n = -200 RPM; (b) n = -600 RPM; and (c) n = -1000 RPM.

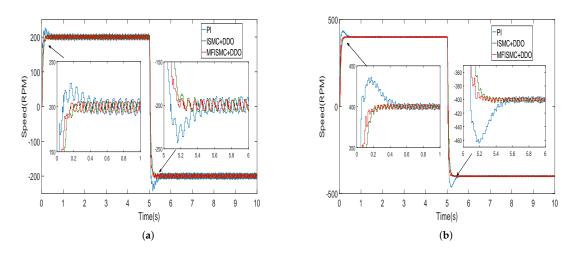


Figure 10. Experimental speed waveforms when the speed changes suddenly: (a) n = +200 RPM to n = -200 RPM ; (b) n = +400 RPM to n = -400 RPM .

The experimental results show that the proposed MFISMC + DDO method has fast convergence speed, small overshoot and strong anti-load disturbance ability.

6. Conclusions

In this paper, a model-free non-cascade integral sliding mode control with a fast reaching law is proposed for the speed regulation of PMSM drive. The fast reaching law effectively improves the convergence speed of the system. The model-free design greatly simplifies the system model. Through the model-free design, the dependence on the parameter uncertainty is effectively reduced. In view of the influence of external mismatched disturbances such as load torque changes, the system disturbances can be effectively estimated by the dual disturbance observers. The estimated disturbances are used for the feedforward compensation, which effectively improves the anti-load disturbance ability of the system. The experimental results verify that the proposed method has small overshoot, fast convergence speed and excellent resistance to load disturbance.

Author Contributions: T.L. completed all the experiments and wrote the manuscript, X.L. designed the proposed control strategy and conceived the structure of the paper. Both authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the National Natural Science Foundation of China under Grant No.61703222 and No.52037005, in part by the China Postdoctoral Science Foundation under Grant No.2018M632622, in part by the Science and Technology Support Plan for Youth Innovation of Universities in Shandong Province under Grant No. 2019KJN033.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Not applicable.

Acknowledgments: This research was funded by the National Natural Science Foundation of China under Grant No. 61703222 and No.52037005, in part by the China Postdoctoral Science Foundation under Grant No.2018M632622, in part by the Science and Technology Support Plan for Youth Innovation of Universities in Shandong Province under Grant No. 2019KJN033.

Conflicts of Interest: The authors declare no conflict of interest.

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