



Article High-Capacity Embedding Method Based on Double-Layer Octagon-Shaped Shell Matrix

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Abstract: Data hiding is a technique that embeds a secret message into a cover medium and transfers the hidden information in the secret message to the recipient. In the past, several data hiding methods based on magic matrix have used various geometrical shapes to transmit secret data. The embedding capacity achieved in these methods was often limited due to simple geometrical layouts. This paper proposes a data hiding scheme based on a double-layer octagon-shaped shell matrix. Compared to previous octagon-shaped data hiding methods, the proposed method embeds a total of 7 bits in each pixel pair, reaching an embedding capacity of 3.5 bits per pixel (bpp). Experimental results show that the proposed scheme has a higher embedding capacity compared to other irreversible data hiding schemes. Using the proposed method, it is possible to maintain the Peak Signal to Noise Ratio (*PSNR*) within an acceptable range with the embedding time less than 2 s.

Keywords: data hiding; magic matrix; irreversible information hiding; regular octagon-shaped shell; double layers

1. Introduction

Data hiding technique, also called as steganography, embeds a secret message into a cover medium and transfers the information hidden in the secret message to the recipient. The term "steganos" in Greek means "hidden", and "graphos," "to write." The earliest allusion to secret writing in the West with concrete evidence of intent appears in Homer's Iliad [1–4]. From ancient times to the present, steganography includes invisible ink, microdots, character arrangement, digital signatures, covert channels, and spread spectrum communication, etc., and ensures that the information is less likely to be noticed and harder to retrieve when the message is transmitted. It makes the information transfer more secure and integrated. The main characteristics of data hiding techniques include security, imperceptibility, embedding capacity, and integrity. As it is very important to know how much secret data can be hidden in a cover image, embedding capacity is an important factor in evaluating the quality of a data hiding technique. The larger the hiding capacity, the more satisfied is the transmitting side to transmit a large chunk of secret data. Also, when the embedding capacity is large, the possibility of the transmission being intercepted by a malicious attacker becomes less and the security becomes high.

In the past, several data hiding methods have been proposed. For example, the method of least significant bits (LSB) substitution [5] proposed by Chang and Cheng in 2004. The limitation of this method was that it was easy to detect the hidden information, resulting in poor security. In 2006, Zhang and Wang proposed exploiting modification direction (EMD) [6] method. In 2010, Lee and Chen designed a modulus function [7] to embed secret data using a mapping process between the variant Cartesian product and



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Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). each pixel group. The experimental results showed that Lee and Chen's scheme achieved a high embedding capacity and a low distortion. In 2017, Lee et al. proposed an REMD [8] method using image interpolation and edge detection that achieved an embedding capacity of 3.01 bpp with an average image quality of 33 dB.

In the field of irreversible information hiding, the EMD method is an epoch-making method. It uses modular functions to reduce the computational cost of the information hidden in the carrier; therefore, this series of EMD methods also brings more novelty. Chang et al., in 2008, proposed a method using a reference matrix based on Sudoku, which made use of a pixel pair as coordinates of a Sudoku matrix to specify the value to embed a 9-ary secret digit into each pixel pair [9]. Chang et al., in 2014, proposed a turtle shellbased scheme (also called TS scheme) [10] for data hiding, in which a reference matrix was constructed based on a hexagon-shaped shell to embed three secret bits into each pixel pair of the cover image. Kurup et al. (2015) proposed a data hiding method based on octagon-shaped shells [11]. In 2017, Leng and Tseng introduced the reference matrix based on regular octagon-shape shells [12]. The further improvement in [13] achieved a higher payload of 3.5 bpp. In 2018, Lee and Wang proposed a magic signet hiding method [14], which randomly generated non-repetitive values of 0–15 in the signet to fill the reference matrix. Recently, in 2019, Zhang et al. proposed an efficient and adaptive data-hiding scheme based on a secure reference matrix [15]. The method was secure because of its large number of possible solutions (about 10^{78} solutions) for resisting attacks. In 2019, Chang and Liu proposed two enhanced real time turtle shell-based data hiding schemes [16]. Both the schemes mapped each cover pixel pair onto the original or altered the turtle shell matrix to find out its associate set for embedding secret data. Then, the cover pixel pair was modified with minimum distortion according to the associate set. In 2020, Nguyen et al. proposed a new data hiding approach to embed secret data based on an x-cross-shaped reference-affected matrix [17]. The reference matrix consisted of three parts: petal matrix, calyx matrix, and stamen matrix, which were combined for executing the embedding procedure. Using this method, it was found that the smooth regions were more suitable for embedding secret data due to the smaller difference between pixel values. Unlike the traditional EMD method, the above-mentioned methods used a reference matrix instead of the extraction function in the embedding and extraction procedures.

All the magic matrices-based schemes mentioned above embedded a single layer of secret data in the reference matrix. First, a pair of cover pixels were mapped on the *x*- and *y*-axes coordinates of the reference matrix, and then the coordinate positions were replaced with the secret data. However, this limited the embedding capacity. In order to overcome the limitation, this paper proposes a new scheme based on double-layer octagon-shaped shell matrix in which each cover pixel pair is able to carry 7-bit sub-streams of secret data. This paper contributes to the related data hiding algorithms as follows.

- (1) The regular octagon-shaped shell method proposed in [12] carried only 5-bit of secret data for each pair of cover pixels. However, in our proposed scheme, additional 2-bits data was embedded in each cover pixel pair, leading to a higher embedding capacity of 3.5 bpp.
- (2) Peak signal to noise ratio (*PSNR*) and structural index similarity (*SSIM*) are two measuring tools that are widely used in image quality assessment. Especially in the steganography image, these two measuring instruments are used to measure the quality of imperceptibility. Based on the experimental analysis, results show that the average value of the stego-image quality had an acceptable value of 37dB on an average while *SSIM* values were between [0.9, 0.95]. We contend that our proposed method is more suitable for complex images to obtain a higher *SSIM* value. Also, as seen previously, the *PSNR* values remained stable for all the test images irrespective of their image texture.
- (3) Lastly, the computational cost in terms of embedding time is 1.82 s on an average.

2. Related Works

In 2006, Zhang and Wang proposed an epoch-making information hiding method, called the exploiting modification direction (EMD) method [6] in which a reference matrix M in the size of 256×256 was constructed based on a cross-shaped shell to embed secret data into each pixel pair of the cover image. In 2014, Chang et al. developed a data hiding scheme based on turtle-shaped shells [10] and then Leng [12] designed regular octagon-shaped shells for hiding secret data.

2.1. The EMD Embedding Method and the EMD Extensions

The exploiting modification direction (EMD) method [6] divided the to-be-hidden binary data into N pieces with L bits, and each secret piece is presented as a decimal value by D digital numbers in a (2n + 1)-ary notational system, where

$$L = \lfloor D \times \log_2(2n+1) \rfloor,$$

$$N = \begin{bmatrix} \frac{\text{Secret bits length}}{L} \end{bmatrix},$$
(1)

where *n* is a parameter to determine how many pixels of cover image are used to hide one secret digit.

In the embedding phase, EMD method firstly uses pseudo-random generator to permute all pixels of cover image according to a secret key. After that, EMD method partitions the permuted pixels into a series of groups. The group is denoted as a vector $P_n = (p_1, p_2, ..., p_n)$, which consists of n cover pixels. A weight vector $W_n = (w_1, w_2, ..., w_n) = (1, 2, ..., n)$ is defined. Therefore, the EMD method defines an embedding function f as weighted sum function modulo (2n + 1) for each group, a secret digit d can be carried by the n cover pixels, and at most one pixel is increased or decreased by one. f can be expressed as Equation (2):

$$f(p_1, p_2, \ldots, p_n) = \left[\sum_{i=1}^n (p_i \times w_i)\right] \mod (2n+1).$$
(2)

After embedding a secret digit *d*, the group P_n is modified into $Q_n = (q_1, q_2, ..., q_n)$, which is defined according to following conditions:

- 1. $Q_n = P_n = (p_1, p_2, \dots, p_n)$, if d = f.
- 2. When $d \neq f$, computes $s = d f \mod (2n + 1)$ and

$$q'_i = \left\{ egin{array}{c} p_i, \ if \ i
eq s \ p_i + 1, \ if \ i = s \end{array}
ight.$$
, and $s \leq n$, for $i = 1, 2, \ldots, n$.

Otherwise, $q'_i = \begin{cases} p_i, & \text{if } i \neq 2n + 1 - s \\ p_i - 1, & \text{if } i = 2n + 1 - s \end{cases}$, and s > n, for i = 1, 2, ..., n. From the above properties, the EMD method at most modifies only one-pixel value in a group. That is why the EMD embedding scheme's distortion induced in the stego-image is not great.

In the extracting phase, the secret digit can be extracted from stego-group $Q_n = (q_1, q_2, \ldots, q_n)$ by the following extraction function shown in Equation (3).

$$f(q_1, q_2, \ldots, q_n) = \left[\sum_{i=1}^n (q_i \times w_i)\right] \mod (2n+1).$$
(3)

The EMD method provides a good quality of stego-image with an average *PSNR* value of more than 51 dB, and the theoretical maximal embedded rate $R = \frac{\log_2(2n+1)}{n}$ of EMD method is 1.16 bpp for the best-case n = 2. For n = 2, the *PSNR* values of all test images averaged to 52.11 dB with embedding capacity of 1 bit per pixel (bpp).

To further improve the EMD scheme, several schemes based on magic matrix based (MMB) schemes have been proposed in the past few years. In 2010, Lee and Chen designed a modulus function [7] to embed secret data using a mapping process between the variant

Cartesian product and each pixel group. The experimental results showed that Lee and Chen's scheme achieved a high embedding capacity and a low distortion. The average *PSNR* was 51.157 dB when the embedding rate was 1 bit per grayscale pixel and the average *PSNR* was 31.847 dB when the embedding rate was 4 bpp with good security and absence of overflow/underflow. In 2017, Lee et al. proposed an REMD [8] method using image interpolation and edge detection that achieved an embedding capacity of 3.01 bpp with an average image quality of 33 dB.

2.2. Data Hiding Scheme Based on Turtle-Shaped Shells

In 2014, Chang et al. developed a data hiding scheme based on turtle-shaped shells, also called as TS scheme [10]. In their method, the secret data was represented in a binary format, 3 bits of which were embedded within every 2 pixels. Figure 1 presents a magic matrix M of size 256 × 256 based on turtle-shaped shells. In the matrix M, two adjacent elements in the same row have a difference of 1, and two neighboring elements present in the same column have an alternating difference of 2 and 3.

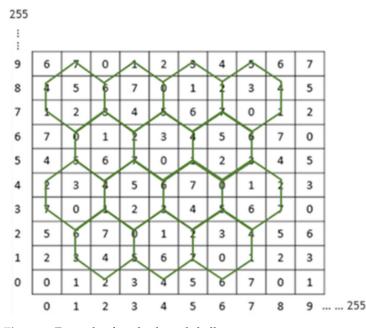


Figure 1. Example of turtle-shaped shell.

Let $m(p_i, p_{i+1})$ and $m(q_i, q_{i+1})$ be two numbers in the magic matrix M, where (p_i, p_{i+1}) and (q_i, q_{i+1}) represent the pairs of cover pixels and stego pixels, respectively. This is before/after a 3-bit secret data s_i has been concealed.

If the number $m(p_i, p_{i+1})$ falls in a turtle-shaped shell, then the secret number s_i also can be found in the same turtle-shaped shell, such that $s_i = m(q_i, q_{i+1})$. However, if $m(q_i, q_{i+1})$ is a number on the edge, then the number s_i can be found in the surrounding three turtle shells. A calculation needs to be done to find the minimum distance between (p_i, p_{i+1}) and (q_i, q_{i+1}) under the condition that $s_i = m(q_i, q_{i+1})$. Another special case occurs when the number $m(q_i, q_{i+1})$ is not located in any turtle-shaped shell. The solution, as shown in Figure 2, is to find the shortest distance between (p_i, p_{i+1}) and (q_i, q_{i+1}) equals the secret data s_i .

The turtle shell-based method can obtain an average *PSNR* of 49.4 dB and an average embedding capacity of 1.5 bpp. The limitation of the turtle shell scheme [10] was that the embedding rate was limited.

	0	1	2	3	4	15	6	7	8	19	10	11	255
0	-0	1	2	3	4	5	6	7	8	9	10	11	
1	-5	6	7	8	9	10	11	12	13	14	15	16	
2	11	12	13	14	15	16	17	18	19	20	21	22	
3	17	18	19	20	21	22	23	24	25	26	27	28	
4	23	24	25	26	27	28	29	30	31	0	1	2	
5 5	28	29	30	31	0	1	2	3	4	5	6	\mathcal{F}	
6 5	-1	12	3	4	5	6	7	8	9	10	11	12	
7 6	17	8	9	10	11	12	13	14	15	16	17	18	
8 6	13	14	15	16	17	18	19	20	21	22	23	24	
9 6	19	20	21	22	23	24	25	26	27	28	29	30	
10	24	25	26	27	28	29	30	31	0	1	2	3	
11	29	30	31	0	1	2	3	4	5	6	7	8	
1											¥		1
255													

Figure 2. An example of a reference matrix consisting of octagon-shaped shells.

2.3. The Regular Octagon-Shaped Shell Embedding Method

Kurup et al. (2015) proposed a data hiding method based on octagon-shaped shells [11], which also used a reference matrix. On average, the *PSNR* value obtained was 51.7 dB with an average embedding capacity of 2 bpp. In 2017, Leng and Tseng introduced the reference matrix based on regular octagon-shape shells [12] which achieved a payload of 2.5 bpp. The further improvement in [13] achieved the possible payload of 3.5 bpp.

As shown in Figure 2, Leng [12] constructed a reference matrix M in the size of 256 × 256 based on regular octagon-shaped shells for hiding secret data. The construction rules were as follows: In the same row of the reference matrix M, the value difference between two adjacent elements was set to "1", and the value difference between two adjacent elements in the same column was set to "5", followed by "6", "6", "6", and "5" in repeated cycles. The reference matrix M composed of a number of contiguous regular octagon-shaped shells. Each regular octagon-shaped shell had a total of 32 numbers, ranging from 0–31. Once the transmission side constructed a reference matrix, the secret message was embedded into the cover image to obtain stego-image. A pair of pixels represented the values of x- and y-axes of the reference matrix coordinates, where each pixel pair corresponded to a 32-ary notational system value.

The data embedding process is presented as follows. In the reference matrix $M = [m(i, j)]_{256 \times 256}$, assume that a secret binary stream *S* is embedded into a cover image *I* of size $W \times H$. The embedding procedure is described as follows:

Step 1: Convert the secret binary stream *S* into a sequence of 5 bits sub-streams $S = \{s_1, s_2, ..., s_n\}$, where *n* represents the number of 5-bit 32-ary digits.

Step 2: Divide the cover image *I* into non-overlapping pixel pairs (p_k, p_{k+1}) , $k\{1, 3, ..., W \times H - 1\}$. (p_k, p_{k+1}) are considered as the coordinates of the reference matrix *M* to specify the value of $m(p_k, p_{k+1})$.

Step 3: Embed a 5-bit secret digit $s_{t(1 \le t \le n)}$ into each pixel pair (p_k, p_{k+1}) to obtain a corresponding pixel pair (q_k, q_{k+1}) . Thereafter, the algorithm can be categorized into two cases.

Case 1: If $m(p_k, p_{k+1}) = s_t$, it means that the current pixel pair (p_k, p_{k+1}) completely corresponds to the 5-bit secret digit, viz., $m(p_k, p_{k+1}) = s_t$; therefore $(q_k, q_{k+1}) = (p_k, p_{k+1})$, directly skip to Step 4.

Case 2: If $m(p_k, p_{k+1}) \neq s_t$, it means that the current pixel pair cannot correspond to the 5-bit secret digit, viz., $m(p_k, p_{k+1}) \neq s_t$. Find the closest $m(p_r, p_c)$, which is equal to s_t , and then replace (p_k, p_{k+1}) with (p_r, p_c) in the cover image to hide the 5-bit secret digit s_t such that $(q_k, q_{k+1}) = (p_r, p_c)$. Find the closest $m(p_r, p_c)$ based on the following rules:

Rule 1: If $m(p_k, p_{k+1})$ is an internal number, e.g., m(3, 3), find $m(p_r, p_c) = s_t$ within the octagon.

Rule 2: If $m(p_k, p_{k+1})$ is an edge number, e.g., m(3, 5), m(5, 2), find $m(p_r, p_c) = s_t$ and closest to (p_k, p_{k+1}) in the two involved octagons.

Rule 3: If $m(p_k, p_{k+1})$ is not included in any octagon, e.g., m(5, 5), find $m(p_r, p_c) = s_t$ within no limited range.

Step 4: Repeat Step 3 to embed the next 5-bit sub-stream into subsequent pixel pairs until the entire secret data *S* is hidden.

Finally, obtain the stego-image I'.

In the process of data extraction, the receiving side constructed a reference matrix $M = [m(i, j)]_{256 \times 256}$ by using the information composed in the matrix. According to the stego-image I' and the reference matrix, the hidden pixel pairs were mapped to the coordinate positions of the reference matrix. In this way, the value of the coordinates of the reference matrix were extracted, which were the actual values of the secret data. Moreover, the data hiding based on octagon-shaped shell scheme greatly increases the embedding capacity under the acceptable image quality.

3. Proposed Scheme

This paper proposes a new scheme based on double-layer octagon-shaped shell matrix in which each cover pixel pair is able to carry 7-bit sub-streams of secret data, achieving an embedding capacity of 3.5 bpp. The following subsections present the construction of the double-layer octagon-shaped shell magic matrix, the embedding procedure, and the extraction procedure.

3.1. Construction of the Double-Layer Octagon-Shaped Shell Reference Matrix

In this section, we will construct a double-layer octagon-shaped shell reference matrix consisting of octagon-shaped shells for hiding secret data with high embedding capacity. The procedure can be divided into two parts. In the first part, we assign a 4-ary digit, referred to as type, to each octagon-shaped shell located at the top layer. In the second part, we assign a type attribute to each element at the bottom layer of the reference matrix.

Figure 2 shows the layout of octagon-shaped shells in the reference matrix. There are 51×51 octagons as shown in Figure 3. For ease of explanation, the type matrix of the octagon-shaped shell is denoted as $T = [t(i, j)]_{51 \times 51}$. The type matrix is constructed using the following rules: Firstly, the values of type in the same row change according to the gradient (ascent/descent) with a magnitude of "1". Secondly, the values of the elements in the same column change according to the gradient (ascent/descent) with a magnitude of "2". To demonstrate an example, we take four octagons near the origin (0, 0). First, we indicate their type values as {0, 1, 2, 3}, marked by red color in Figure 3. For example, t(0, 0) = 0, t(0, 1) = 1, t(1, 0) = 2, t(1, 1) = 3. In this manner, we assign the four octagon-based type values {0, 1, 2, 3} to the whole 51×51 octagons respectively.

For each element m(i, j) at the bottom layer of the reference matrix M, we assign an additional attribute, type, denoted as $t_m(i, j)$ corresponding to each element m(i, j). Each type $t_m(i, j)$ can be categorized into one of the following three cases, as shown in Figure 4a:

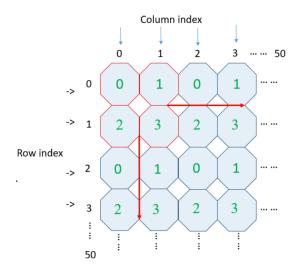


Figure 3. An example of octagon types in reference matrix at the top layer.

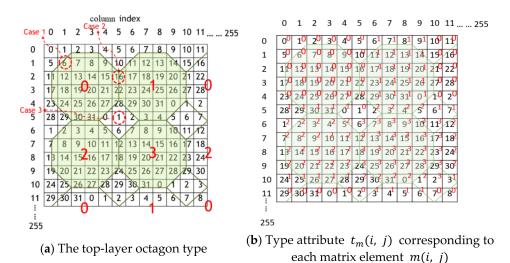


Figure 4. Double-layer octagon-shaped shell reference matrix. (a) The top-layer octagon type; (b) Type attributes corresponds to matrix elements.

Case 1: Elements m(i, j) are only included in a regular octagon. For example, m(1, 1) = 6 at the bottom layer is an internal number falling on a regular octagon with type assigned as t(0, 0) = 0. So, the type value of m(1, 1) can be represented by $t_m(1, 1) = 0$ as shown in Figure 4b.

Case 2: Elements m(i, j) are involved in two octagons. For example, m(2, 5) = 16 at the bottom layer is also located on the edge adjacent to two octagons whose type codes are t(0, 0) = 0 and t(0, 1) = 1 at the top layer. The value of m(i, j) involves two octagons whose type value can be calculated from the values of two octagons t(i, j) and t(k, l), using Equation (4), which is shown as follows. Accordingly, we obtain $t_m(2, 5) = 0$ which is shown in Figure 4b.

$$t_m(i,j) = \begin{cases} t(i,j) + t(k,l) - 1, & \text{if } t(i,j) + t(k,l) < 3\\ t(i,j) + t(k,l) - 2, & \text{if } t(i,j) + t(k,l) > 3 \end{cases}$$
(4)

Case 3: Elements m(i, j) are not involved in any octagon. The value of m(i, j) is assigned the type values based on the following rules:

Rule 1: For the element m(0, 0), which is located at the origin, its type value is set as 0, viz., $t_m(0, 0) = 0$ as shown in Figure 4b.

Rule 2: If the elements m(i, j) are located in the first column or the last column of the matrix, viz., m(i, 0) or m(i, 255), $0 \le i \le 255$, their type values are equivalent to the values shifted to the right or left by one, viz., $t_m(i, 0) = t_m(i, 1)$ or $t_m(i, 255) = t_m(i, 254)$ for $i\{0, 5, 10, \ldots, 255\}$.

Rule 3: If the elements m(i, j) are located in the first row or last row of the matrix, viz., m(0, j) or m(255, j), $0 \le j \le 255$, their type values are equivalent to the values when shifting down or moving up by one, viz., $t_m(0, j) = t_m(1, j)$ or $t_m(255, j) = t_m(254, j)$, $j\{0, 5, 10, \ldots, 255\}$.

Rule 4: If the elements m(i, j) are located in the middle of four octagons, e.g., m(5, 5) in Figure 4a, their values can be calculated according to Equation (5), e.g., $t_m(5, 5) = t(0, 0) = 0$, $t_m(5, 10) = t(0, 1) = 1$, $t_m(10, 5) = t(1, 0) = 2$, and $t_m(10, 10) = t(1, 1) = 3$, which are shown in Figure 4b.

$$t_m(5i, 5j) = t(i-1, j-1), \text{ for } i, j = 1, 2, \dots, 51.$$
 (5)

Accordingly, each $m(i, j) \in \{0, 1, ..., 31\}$ can be assigned a corresponding type value $t_m(i, j) \in \{0, 1, 2, 3\}$ and a double-layer reference matrix is generated for hiding secret data.

In the process of embedding a secret message, a double-layer octagon-shaped shell reference matrix can be created, which can embed 7-bits of secret data into every non-overlapping pixel pair. The construction of the double-layer matrix is similar to the method of the one-layer regular octagon-shaped shells [12]. The difference here is that the construction information in the proposed method has more additional information to reveal about the second layer. The construction of the second layer matrix (i.e., the type matrix) can be calculated according to the above steps. The extra information of the second layer includes the value with the coordinate (0, 0) in $T = [t(i, j)]_{51 \times 51}$, the construction rules of T, and the algorithm for generating type matrix T_m . The procedures for data embedding and extraction are described in detail in the following sections.

3.2. Data Embedding and Data Extraction Procedures

In this section, data embedding and extraction procedures of the proposed method are presented. Figure 5 shows the flow chart of the data embedding process. First, we divide the cover image into multiple non-overlapping pixel pairs (p_k , p_{k+1}). The binary secret stream *S* is divided into 7-bit sub-steams s_c , which are further converted into two numbers: 4-ary digit s_{c1} and 32-ary digit s_{c2} , respectively. The pair contains 4-ary and 32-ary numbers (s_{c1} , s_{c2}) hidden in each pixel pair using the constructed double-layer reference matrix. When all the secret data is embedded, we get a stego-image. The detailed steps for data embedding and data extraction are described in the Algorithms 1 and 2.

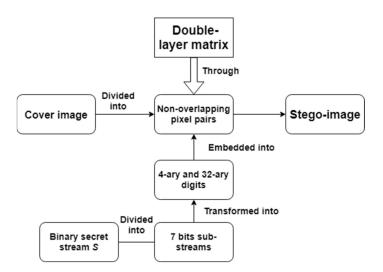


Figure 5. Flowchart of data embedding procedure.

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Algorithm 1. Data Embedding Algorithm.

Input: A cover image *I* sized $W \times H$, the binary secret stream *S* with length *L*. **Output:** A stego-image I'.

Step 1: Construct a one-layer reference matrix $M = [m(i, j)]_{256 \times 256}$ according to the rules described in Section 2. Thereafter, generate a double-layer reference matrix, assigning the type value $t_m(i, j)$ corresponding to each matrix element m(i, j) according to the rules described in Section 3.1.

Step 2: Divide the cover image *I* into non-overlapping pixel pairs (p_k , p_{k+1}) where

 $k = \{1, 3, ..., (W \times H - 1)\}$. Consider (p_k, p_{k+1}) as the coordinates of the matrix *M* to specify the value $m(p_k, p_{k+1})$ with the corresponding type $t_m(p_k, p_{k+1})$.

Step 3: Divide the secret message *S* into sub-streams s_c of 7 bits, where $c \in \{1, 2, ..., |\frac{L}{7}|\}$. For each sub-stream s_c , convert the first 2 bits into a 4-ary digit s_{c1} and the last 5 bits into a 32-ary digit s_{c2} , viz., $s_c = s_{c1} ||s_{c2}$ where "||" denotes the string concatenation operator.

Step 4: Embed each sub-stream s_c into each pixel pair (p_k, p_{k+1}) according to the following rules: Find the closest element m(u,v) by searching in a square of 25×25 centered on $m(p_k, p_{k+1})$, where $m(u,v) = s_{c2}$ and $t_m(u,v) = s_{c1}$. Replace (p_k, p_{k+1}) with (u,v) such that the stego-pixel pairs $(q_k, q_{k+1}) = (u, v)$, to embed the sub-stream s_c consisting of s_{c1} and s_{c2} .

Step 5: Repeat Step 4 until all the sub-streams are embedded. Finally, obtain the stego-image I'.

Algorithm 2. Data Extraction Algorithm.

Input: A stego-image I' sized $W \times H$.

Output: The binary secret stream *S*.

Step 1: Reconstruct the double-layer reference matrix $M = [m(i, j)]_{256 \times 256}$ where each matrix element m(i, j) corresponds to a type value $t_m(i, j)$, which is calculated according to the reules described in Section 3.1.

Step 2: Divide the stego-image I' into non-overlapping pixel pairs, where $k = \{1, 3, ..., (W \times H - 1)\}.$

Step 3: For each stego-pixel pair (q_k, q_{k+1}) , find two digits $m(q_k, q_{k+1})$ in 32-ary format and $t_m(q_k, q_{k+1})$ in 4-ary format, respectively. The hidden secret data is $s_c = s_{c1}||s_{c2}$, where $s_{c2} = m(q_k, q_{k+1})$ and $s_{c1} = t_m(q_k, q_{k+1})$, respectively.

Step 4: Convert *s*^{*c*} into binary bits of secret data.

Step 5: Repeat Steps 2–4 to extract all the sub-streams. Combine all the sub-streams to form the secret binary stream *S*.

3.3. Example of Data Embedding and Data Extraction Procedures

We will take two cover pixel pairs $(p_1, p_2) = (2, 7)$ and $(p_3, p_4) = (8, 7)$ as examples to explain the embedding and extraction procedures based on the proposed method. The secret message of 14-bit stream to be embedded is $S = "0110010\ 0000001"$. Figure 6 is the double-layer reference matrix related to the examples explained in this section. Figure 7 presents examples describing the data embedding process of the cover pixel pairs.

Assume that we want to hide the sub-stream "01 10010" in the first cover pixel pair (2, 7). The sub-stream "01 10010" is first divided into two segments, namely $s_{c1} =$ "01" and $s_{c2} =$ "10010". Thereafter, we need to convert binary digits into decimal digits, which results in two numbers 1 and 18 after conversion in the 4-ary and 32-ary systems respectively. Since m(2, 7) = 18 and $t_m(2, 7) = 1$ is shown in Figure 6, it is not necessary to change the cover pixel pair, and the secret message can be extracted at a later stage. Therefore, the stego-pixel pair (q_1, q_2) = (2, 7) is the same as the corresponding cover pixel pair (p_1, p_2) = (2, 7) as shown in Figure 7.

The second cover pixel pair is $(q_3, q_4) = (8, 7)$. The sub-stream "00 00001" to be hidden, is converted into decimal digits, which results in 0 and 1 in the 4-ary and 32-ary systems respectively. Marked by blue color in Figure 6, the location (5, 5) is closest to the location (8, 7) and satisfies $t_m(5, 5) = 0$ at the top layer and m(5, 5) = 1 at the bottom layer. Finally, the second cover pixel pair is replaced with the stego-pixel pair (q_3, q_4) = (5, 5), which is also shown in Figure 7.

	0	1	2	3	4	5	6	7	8	9	10	11	
0	00	1 ⁰	2 ⁰	3 ⁰	4 ⁰	5 ⁰	6 <mark>1</mark>	7 <mark>1</mark>	8 <mark>1</mark>	9 <mark>1</mark>	10	11	
1	5 ⁰	60	7 ⁰	80	90	10	11	12 <mark>1</mark>	13 <mark>1</mark>	14	15 ⁰	16	
2	11 ⁰	12	13	14	15 ⁰	16	17 <mark>1</mark>	18	19 ¹	20 <mark>1</mark>	21 ⁰	22 ⁰	
3	170	180	19 ⁰	20	21 ⁰	22	23 <mark>1</mark>	24 <mark>1</mark>	25 <mark>1</mark>	26	2 7 9	28	
4	23	24 ⁰	25 ⁰	26 ⁰	27	28	29 <mark>1</mark>	30 <mark>1</mark>	31 <mark>1</mark>	01	1	2 ⁰	
5	28 ¹	29	30 ¹	31 ¹	01	1 ⁰	22	3 ²	4 ²	52	6 ¹	71	
6	12	2 ²	3 ²	4 ²	52	6 ³	X ³	8 ³	9 ³	10	11 ³	12	
7	72	8 ²	9 ²	10	11 ²	123	13	14 ³	15	16 ³	17 ³	18 <mark>2</mark>	
8	13 ²	14	15 ²	162	172	18	19 ³	20	21 ³	22 ³	23 ³	24 <mark>2</mark>	
9	192	202	21 ²	22	23	243	25 ³	26 ³	27	283	29 ³	30 ²	
10	24 ¹	25 ¹	26 ¹	27 ¹	28	29 ²	302		02	1 ²	2 ³	31	
11	29 ⁰	⁄30 ⁰	31 ⁰	00	1	2 ⁰	3	4 ¹	5 ¹	61	7 ⁰	80	
1						-, (

Figure 6. Construction of double-layer octagon-shaped shell reference matrix.

Original pixel pair	Message to be embedded	Stego-pixel pair
(2, 7)	$(01)_2(10010)_2 \rightarrow (1)_4(18)_{32}$	(2, 7)
(8, 7)	$(00)_2(00001)_2 \rightarrow (0)_4(1)_{32}$	(5, 5)

Figure 7. Examples describing data embedding of pixel pairs.

A double-layer matrix is constructed according to the construction rules shown in Figure 6, on the receiving end. We then divide the stego-image into non-overlapping pixel pairs to embed the 7-bit secret message. Taking the first stego-pixel pair $(q_1, q_2) = (2, 7)$ as an example, the values of s_{c1} and s_{c2} are obtained from $t_m(2, 7)$ at the top layer and and m(2, 7) at the bottom layer of the double-layer matrix, where s_{c1} is 1 and s_{c2} is 18 respectively. Moreover, 1 and 18 are converted into binary data "01" and "10010" in the 4-ary and 32-ary number systems respectively. Finally, we get the combined secret sub-stream "0110010".

4. Experimental Results

Experiments were conducted using MATLAB R2017a to verify the performance of the proposed scheme. A total of six grayscale images were used from the University of Southern California-Signal and Image Processing Institute (USC-SIPI) image database [18] as shown in Figure 8. The size of each image was 512×512 pixels. The binary secret stream *S* was generated randomly. The parameters of Embedding Capacity (*EC*), Peak Signal to Noise Ratio (*PSNR*), and Structural Similarity Index (*SSIM*) were used as evaluation parameters to validate the performance of the proposed method. *EC* is the amount of secret message per pixel that can be embedded in the image. If the number of secret messages embedded in the image is more and the image quality can be maintained to a certain standard, then the data hiding method is supposed to have high imperceptibility and high embedding capacity. *PSNR* is used to measure the quality of the image. If the value of this parameter is high, it means that the image quality is good, and the secret message hidden in stego-image cannot be perceived easily by the human eye. Refer to Equations (6) and (7) to calculate *PSNR*. Refer to Equation (8) to calculate the *EC*.

$$PSNR(dB) = 10 \times \log_{10}\left(\frac{255^2}{MSE}\right)$$
(6)

$$MSE = \frac{1}{H \times W} \sum_{i=1}^{H} \sum_{j=1}^{W} \left(I_{(i,j)} - I'_{(i,j)} \right)$$
(7)

$$EC(bpp) = \frac{|S|}{H \times W}$$
(8)

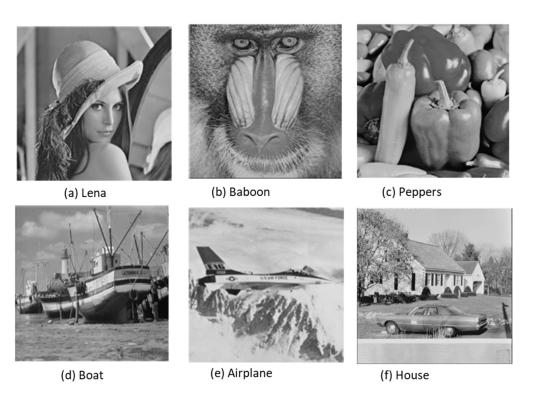


Figure 8. Six grayscale test images; they should be listed as (**a**) Lena, (**b**) Baboon, (**c**) Peppers, (**d**) Boat, (**e**) Airplane, and (**f**) House.

(*H* is the height of image, *W* is the width of image, *I* represents the cover image, and \vec{I} represents the stego-image. *MSE* represents mean-square error, *EC* represents embedding capacity, and |S| are the total number of secret bits that can be embedded).

In addition, the parameter of *SSIM* measures similarity between the original image and the stego image. This is in line with the human eye's judgment of image quality. The higher the *SSIM* value, the higher will be the similarity between the original image and the stego image.

SSIM value is calculated using Equation (9) as shown below, where μ_x and μ_y are the average values of the original image and the stego image respectively; σ_{xy} is the covariation between the original and the stego images respectively; and σ_x and σ_y are the variation of the original image and the stego image respectively. C_1 and C_2 are constants.

$$SSIM = \frac{(2\mu_x\mu_y + C_1)(2\sigma_{xy} + C_2)}{(\mu_x^2 + \mu_y^2 + C_1)(\sigma_x^2 + \sigma_y^2 + C_2)}$$
(9)

A comparison of the proposed method with the other four methods is shown in Table 1. It can be observed that the proposed scheme obviously outperforms the other methods in terms of the embedding capacity and image quality. To be more precise, we can see that the proposed method has a higher embedding capacity (3.5 bpp) compared to the methods in [12–17,19,20], with an acceptable decrease in the image quality. Also, the image quality of the proposed method is better than that of [13] at the same embedding capacity of 3.5 bpp. Our proposed method outperforms in terms of *PSNR* with an average value of 36.91 dB compared to the average *PSNR* of 30.62 dB obtained in [13]. While [14–16,20]

have higher average **PSNR** values of 44.12 dB, 46.37 dB, 46.84 dB, and 41.27 dB respectively, the embedding capacity of our proposed scheme is higher by 1.5 bpp.

 Table 1. Comparison of image quality (PSNR) and embedding capacity (EC).

 Lena
 Baboon
 Peppers
 Boat
 Airplane
 House
 Average

Images		Lena	Baboon	Peppers	Boat	Airplane	House	Average
	PSNR	44.14	44.14	44.14	44.02	44.17	46.13	44.12
Magic signet [14]	EC(bpp)	2	2	2	2	2	2	2
	PSNR	46.38	46.37	46.37	46.38	NA	46.37	46.37
Secure random matrix [15]	EC(bpp)	2	2	2	2	NA	2	2
	PSNR	46.85	46.85	46.84	NA	NA	NA	46.84
Fast turtle shell-based matrix (Scheme 2) [16]	EC(bpp)	2	2	2	NA	NA	NA	2
	PSNR	41.31	41.25	41.30	41.23	41.28	41.26	41.27
3D-sudoku [20]	EC(bpp)	2	2	2	2	2	2	2
	PSNR	43.00	42.98	42.99	43.01	42.98	43.01	43.01
Regular-octagon shape [12]	EC(bpp)	2.5	2.5	2.5	2.5	2.5	2.5	2.5
	PSNR	47.13	47.09	47.13	47.12	47.11	47.12	47.13
Two-layer turtle-shape [19]	EC(bpp)	2.5	2.5	2.5	2.5	2.5	2.5	2.5
	PSNR	40.37	38.14	40.35	NA	NA	NA	39.62
<i>x</i> -cross-shaped reference-affected matrix [17]	EC(bpp)	2.6134	2.6402	2.6211	NA	NA	NA	2.6249
	PSNR	30.59	30.59	30.62	NA	30.68	NA	30.62
Maximizing the payload-octagon [13]	EC(bpp)	3.5	3.5	3.5	NA	3.5	NA	3.5
	PSNR	36.93	36.91	36.91	36.92	36.89	36.92	36.91
Proposed scheme	EC(bpp)	3.5	3.5	3.5	3.5	3.5	3.5	3.5

As it can be seen in Table 2, we used six standard test images and set a fixed amount of embedding capacity to display changes in the *PSNR* for each image. For example, when the embedding capacity is 70×10^4 bits, the average *PSNR* of each image remains at 38.09 dB. At the embedding capacity of 50×10^4 bits, the *PSNR* remains at an average quality of 39.56 dB. Therefore, the *PSNR* value remains stable for each test image. The magnitude of the pixels change during the data embedding process, which depends on the constructed double-layer reference matrix and the embedding procedure. In other words, the image quality of the stego-image is independent of the cover image and it is possible to maintain the image quality within an acceptable range using the proposed method.

Table 2. The PSNR values (dB) of the proposed method under various payloads (bits).

	PSNR (PAYLOAD)	PSNR	PSNR	PSNR	PSNR	PSNR
Images		(50×10 ⁴)	(60×10 ⁴)	(70×10 ⁴)	(80×10 ⁴)	(90×10 ⁴)
	Lena	39.5476	38.7697	38.0882	37.5272	36.9899
	Baboon	39.5653	38.7780	38.0975	37.5150	37.0135
	Peppers	39.5849	38.7789	38.0879	37.5354	37.0206
	Boat	39.5528	38.7536	38.0963	37.5182	36.9911
	Airplane	39.5442	38.7618	38.1041	37.5161	37.0127
	House	39.5430	38.7628	38.0847	37.5231	37.0145
	Average	39.56	38.77	38.09	37.52	37.01

Table 3 shows the *SSIM* values of six standard test images at a fixed *EC* (3.5 bpp, which is 917,504 bits). Interestingly, the *SSIM* value for complex images such as Baboon is higher compared to the *SSIM* value for smooth images such as Airplane. This is a unique finding in our proposed method. Therefore, we contend that our proposed method is more suitable for complex images to obtain a higher *SSIM* value. Also, as seen previously, the *PSNR* values remains stable for all the test images irrespective of their image texture. To

confirm this, we tested our proposed method on 50 additional test images using USC-SIPI database [18] and Kodak Image database [21] as shown in Figure 9.

Table 3. The SSIM values for six standard test images at a fixed EC (3.5 bpp).

Image	SSIM	EC (bpp)	PSNR (dB)
Lena	0.9085	3.5	36.919709
Baboon	0.9685	3.5	36.914033
Peppers	0.9111	3.5	36.927763
Boat	0.9334	3.5	36.897141
Airplane	0.8986	3.5	36.919945
House	0.9224	3.5	36.914813

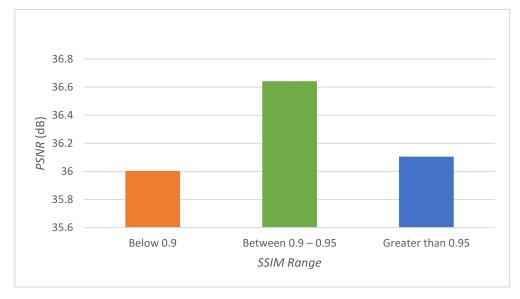


Figure 9. Range of SSIM values for 50 standard test images.

Based on the experiment on 50 test images, the *SSIM* values can be categorized into three groups as shown in the Figure 9. It is evident from the figure that the images which obtain *SSIM* values between [0.90, 0.95] are the most suitable for the proposed method as these images show the highest *PSNR* value. The *PSNR* range obtained for *SSIM* values between [0.90, 0.95] is [34.085597, 36.941688] dB, which falls in the acceptable image quality range.

We also calculated the *PSNR* values for six standard test images at different *EC* (bpp) as shown in Figure 10 below. The figure clearly shows that as the embedding rate increases, the *PSNR* value decreases similar to the property of methods based on the magic matrix hiding methods of [12–17,19,20,22]. However, interestingly, the *PSNR* values for the test images do not have much difference from each other, which again shows the point that the *PSNR* values remains stable using our proposed method irrespective of the image texture.

Table 4 shows the comparison of *EC* (bpp), *PSNR* (dB), and embedding time (seconds) among Chang et al.'s turtle shell in a single-layer embedding, Leng and Tseng's octagon-shaped shells scheme in a single-layer embedding, Xie et al.'s two-layer turtle shell matrix embedding, Shen et al.'s double-layer square magic matrix scheme, and the proposed method in a two-layer embedding using octagon-shaped shells. For simplicity, the representations [TS, 1, *EC*1.5], [Octagon, 1, *EC*2.5], [TS, 2, *EC*2.5], [Square, 2, *EC*2.5], [Ours, 2, *EC*3.5] stand for the methods exploiting Chang et al.'s turtle shell in a single-layer embedding [10] with *EC* = 1.5 bpp, Leng and Tseng's octagon-shaped shells scheme in a single-layer embedding [12] with *EC* = 2.5 bpp, Xie et al.'s two-layer turtle shell matrix embedding [19] with *EC* = 2.5 bpp. Shen et al.'s double-layer square magic matrix scheme with *EC* = 2.5 bpp. As mentioned earlier, with regards to the information

hiding method based on the magic matrix, under the same embedding capacity regardless of the image texture, the *PSNR* and *SSIM* values of all test images remain stable. Similarly, the execution time of each method also has this stable characteristic, which is presented in Table 4 and Figure 11.

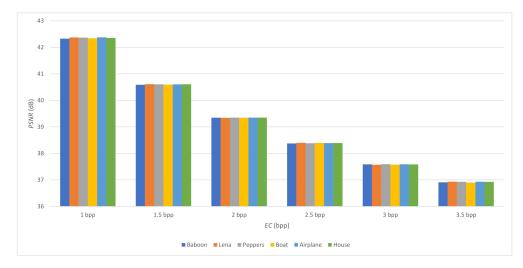


Figure 10. The *PSNR* values for six standard test images at different *EC* (bpp).

Table 4. Comparison of *EC*, *PSNR* values, and embedding time among Chang et al.'s turtle shell (TS) in a single-layer embedding, Leng's octagon-shaped shells scheme in a single-layer embedding, Xie et al.'s two-layer turtle shell matrix embedding, Shen et al.'s double-layer square magic matrix scheme, and the proposed method in a two-layer embedding using octagon-shaped shells.

	Chang et al.'s TS Scheme, Single-Layer Embedding [10]		Octagon Shells S Single	l Tseng's -Shaped Scheme, -Layer ling [12]	Two-Lay Shell	t al.'s er Turtle Matrix ling [19]	Shen et al Magic Two- Embedd	Matrix, Layer		oposed Fwo-Layer dding
	<i>EC</i> = 1.5		<i>EC</i> = 2.5		<i>EC</i> = 2.5		<i>EC</i> = 2.5		<i>EC</i> = 3.5	
	PSNR	Time	PSNR	Time	PSNR	Time	PSNR	Time	PSNR	Time
Lena	49.42	0.65	47.13	0.85	43.00	1.45	42.70	0.69	36.92	1.85
Airplane	49.40	0.63	47.11	0.85	42.98	1.45	42.69	0.68	36.92	1.85
Boat	49.40	0.69	47.12	0.89	43.01	1.49	42.68	0.70	36.90	1.89
Peppers	49.40	0.70	47.13	0.92	42.99	1.42	42.69	0.71	36.93	1.82
Baboon	49.39	0.78	47.09	0.92	42.98	1.42	42.68	0.75	36.91	1.82
House	49.40	0.69	47.12	0.87	43.01	1.47	42.68	0.70	36.91	1.87
Average	49.40	0.69	47.12	0.88	42.99	1.45	42.69	0.69	36.91	1.82

Table 4 shows the comparison of *EC* (bpp), *PSNR* (dB), and embedding time (seconds) among Chang et al.'s turtle shell in a single-layer embedding, Leng's octagon-shaped shells scheme in a single-layer embedding, Xie et al.'s two-layer turtle shell matrix embedding, Shen et al.'s double-layer square magic matrix scheme, and the proposed method in a two-layer embedding using octagon-shaped shells. For simplicity, the representations [TS, 1, *EC*1.5], [Octagon, 1, *EC*2.5], [TS, 2, *EC*2.5], [Square, 2, *EC*2.5], [Ours, 2, *EC*3.5] stand for the methods exploiting Chang et al.'s turtle shell in a single-layer embedding [10] with *EC* = 1.5 bpp, Leng and Tseng's octagon-shaped shells scheme in a single-layer embedding [12] with *EC* = 2.5 bpp, Xie et al.'s two-layer turtle shell matrix embedding [19] with *EC* = 3.5 bpp. Shen et al.'s double-layer square magic matrix scheme with *EC* = 2.5 bpp, and the proposed method in a two-layer embedding using octagon-shaped shells using octagon-shaped shells with *EC* = 3.5 bpp. As mentioned earlier, the *PSNR* and *SSIM* values of all test images remain stable for the information hiding method based on the magic matrix, under the same

embedding capacity regardless of the image texture. Similarly, the execution time of each method also shows stability, which is presented in Table 4 and Figure 11.

As seen in Figure 11, the method we proposed demonstrates maximum embedding capacity, and it also consumes the longest computation time. However, irrespective of the method, execution time of the maximum embedding capacity lies between 0.62 s and 1.90 s.

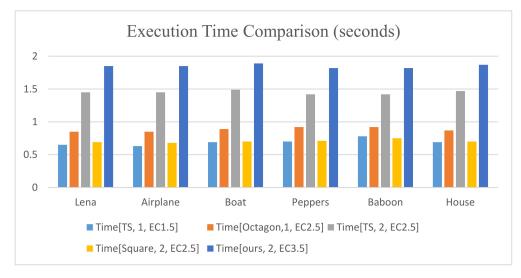


Figure 11. Comparison of execution time of five methods with different embedding capacities.

5. Conclusions

The steganography is used for covert communication in which secret data is hidden into a cover media, resulting in a stego-media. The key goal of steganography is to embed the maximum amount (capacity) of secret data to hide its existence with minimal distortion of the cover media. So, a data hiding methodology has to handle the tradeoff between "capacity" and "transparency/imperceptibility". Inspired from the regular octagon-shaped shells data hiding method of Leng and Tseng [12], we proposed a steganographic method based on double-layer octagon-shaped shell matrix with high embedding capacity superior to the existing data hiding schemes.

In the regular octagon-shaped shells data hiding method, a 5-bit secret message could be embedded per pixel pair in the octagon-shaped shell matrix. In the double-layer octagonshaped shells scheme proposed in this paper, we can further add 2 bits to enhance the embedding capacity. The digits of proposed reference matrix of the first layer are 2-bit data in the 4-ary number system, and the digits of second layer are 5-bit data in the 32-ary number system. Thus, each pixel pair can carry a total of 7-bit secret data, leading to a high embedding capacity of 3.5 bpp.

The experimental results verify that the proposed method is superior to the existing data hiding schemes in terms of embedding capacity, which was also able to maintain an acceptable visual quality of *PSNR* 37 dB on an average while *SSIM* values were between 0.9–0.95. We contend that our proposed method is more suitable for complex images to obtain a higher *SSIM* value as compared to other methods. Also, as seen previously, the *PSNR* values were stable for all the test images irrespective of their image texture. Moreover, the computation cost in terms of embedding time was 1.82 s on average.

In this article, there are two issues to be solved in the future.

(1) The first point is the results in Table 3 are showing the proposed algorithm is insecure because of the obtained *SSIM* values with high *EC*. When *SSIM* = 0.95, most people will be satisfied with the visual image of the image. While *SSIM* is lower than 0.90, it means that the defect may be twice as much as 0.95, and the naked eyes may perceive the picture deterioration and cause insecurity. According to our experimental results, when the *EC* value reaches 3.5 bpp, approximately 10% of pictures will have an *SSIM* slightly below 0.9. The results under 0.95 should be the limit for increasing the *EC*.

(2) From the experimental results in Figure 11, although the proposed method has a larger maximum embedding capability, it takes more time to implement information hiding than other methods. The execution time of the maximum embedding capacity was around 1.90 s. Therefore, in future, we will improvise the method showcased in paper [22] to develop another multi-layer information hiding method, in order to achieve better information hiding computational capabilities, making it more competitive in the real-time application environment.

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