

Equations used for the four ES types maps processing

- Habitat Quality Equation:

$$Q_{xj} = H_j^* (1 - ((D_{xj}^z) / (D_{xj}^z - k_z))), \quad (3)$$

where Q_{xj} is the habitat quality in grid cell x with land-use/land-cover (LULC) type j , H_j indicates the habitat suitability of LULC type j , D_{xj} is the total threat level in grid cell x , with LULC or habitat type j , and k constant is the half-saturation constant (by default it is equal to 0.5).

- Recreation linear regression:

$$y_i = \beta_0 + \beta_1 x_{i1} + \dots + \beta_p x_{ip} \quad \text{for } i=1..n, \quad (4)$$

where $\beta_{0,1,2,\dots,n}$ are coefficients of the regression, x_{ip} is the coverage of each attribute in each cell or polygon (hereafter called 'cell') i , within an area of interest containing n cells. Study period used were: 2016 as pre-fire analysis and 2017 as post-fire analysis.

- Pollination Equation:

$$YW(f) = v(f) (\sum_{x \in X(f)} PYW(x) / |X(f)|), \quad (5)$$

where $YW(f)$ is the percentage of total crop yield attributable to wild pollinators, $X(f)$ is the set of pixels covering farm " f ", and $|X(f)|$ is the count of pixels covered by farm " f ", $v(f)$ is a scalar function $\in [0,1]$ which represents the percentage of crop yield grown on farm " f ", and $PYW(x)$ is the percentage of pollinator-dependent yield attributable to wild pollinators.

- Revised universal soil loss equation:

$$RUSLE_i = R_i \cdot K_i \cdot LS_i \cdot C_i \cdot P_i, \quad (6)$$

where R_i is rainfall erosivity, K_i is soil erodibility, LS_i is a slope length-gradient factor, C_i is a crop-management factor, and P_i is a support practice factor.