

Table S1 Summary of quadratic model

Fit Statistics	R <sup>2</sup>	Adj R <sup>2</sup>	Pred R <sup>2</sup>	Adeq Precision	C.V. %	Std. Dev.	Mean
	0.98	0.97	0.86	28.76	2.02	1.60	79.35

Table S2 The experimental results are verified under optimized conditions

Test conditions	A	B	C	B
	NaOH/ILL	Tep (°C)	T (h)	Removal rate %
Optimum conditions	1.18	185.154	2.76	95.15
Adjustment conditions	1.2	185	2.7	94.5

Table S3. Parameters of kinetic models predicting the experimental data for Pb(II) and Cu(II)

	$q_{e,exp}(mg/g)$	Pseudo-first-order kinetic model				Pseudo-second-order kinetic model			
		$q_{e,cal}(mg/g)$	$K_1(\text{min}^{-1})$	$R^2$	$\chi^2$	$q_{e,cal}(mg/g)$	$K_2(10^{-3}g/(mg \cdot min))$	$R^2$	$\chi^2$
Pb(II)	279.74	271.14	0.5543	0.8971	2.9965	281.10	0.00361	0.9985	0.0292
Cu(II)	51.60	48.96	0.3217	0.9723	2.6469	51.80	0.00793	0.9986	0.4696