

Review

Application of Machine Learning in Water Resources Management: A Systematic Literature Review

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Abstract: In accordance with the rapid proliferation of machine learning (ML) and data management, ML applications have evolved to encompass all engineering disciplines. Owing to the importance of the world's water supply throughout the rest of this century, much research has been concentrated on the application of ML strategies to integrated water resources management (WRM). Thus, a thorough and well-organized review of that research is required. To accommodate the underlying knowledge and interests of both artificial intelligence (AI) and the unresolved issues of ML in WRM, this overview divides the core fundamentals, major applications, and ongoing issues into two sections. First, the basic applications of ML are categorized into three main groups, prediction, clustering, and reinforcement learning. Moreover, the literature is organized in each field according to new perspectives, and research patterns are indicated so attention can be directed toward where the field is headed. In the second part, the less investigated field of WRM is addressed to provide grounds for future studies. The widespread applications of ML tools are projected to accelerate the formation of sustainable WRM plans over the next decade.

Keywords: classification; climate change; clustering; machine learning (ML); prediction; reinforcement learning; water resources management (WRM)



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1. Introduction

In recent years, machine learning (ML) applications in water resources management (WRM) have garnered significant interest [1]. The advent of big data has substantially enhanced the ability of hydrologists to address existing challenges and encouraged novel applications of ML. The global data sphere is expected to reach 175 zettabytes by 2025 [2]. The availability of this large amount of data is forming a new era in the field of WRM. The next step for hydrological sciences is determining a method to integrate traditional physical-based hydrology into new machine-aided techniques to draw information directly from big data. An extensive range of decisions, from superficial to complicated scientific problems, is now handled by various ML techniques. Only a machine is capable of fully utilizing big data because of its veracity, velocity, volume, and variety. In recent decades, ML has attracted a great deal of attention from hydrologists and has been widely applied to a variety of fields because of its ability to manage complex environments.

In the coming decades, the issues surrounding climate change, increasing constraints on water resources, population growth, and natural hazards will force hydrologists worldwide to adapt and develop strategies to maintain security related to WRM. The Inter-governmental Hydrological Programme (IHP) just started its ninth phase plans (IHP-IX, 2022-2029), which place hydrologists, scholars, and policymakers on the frontlines of action to ensure a water-secure world despite climate change, with the goal of creating a new and sustainable water culture [3]. Moreover, the rapid growth in the availability of hydrologic data repositories, alongside advanced ML models, offers new opportunities for improved assessments in the field of hydrology by simplifying the existing complexity. For instance, it is possible to switch from traditional single-step prediction to multi-step ahead

prediction, from short-term to long-term prediction, from deterministic models to their probabilistic counterparts, from univariate to multivariate models, from the application of structured data to volumetric and unstructured data, and from spatial to spatio-temporal and the more advanced geo-spatiotemporal environment. Moreover, ML models have contributed to optimal decision-making in WRM by efficiently modeling the nonlinear, erratic, and stochastic behaviors of natural hydrological phenomena. Furthermore, when solving complicated models, ML techniques can dramatically reduce the computational cost, which allows decision-makers to switch from physical-based models to ML models for cumbersome problems. Therefore, the new emerging hydrological crises, such as droughts and floods, can now be efficiently investigated and mitigated with the assistance of the advancements in ML algorithms.

Recent research has focused on the feasibility of applying ML techniques, specifically the subset of ML known as deep learning (DL), to various subfields of hydrology. In accordance with the research advancements in this field, various review articles have been published. The research domains, and descriptions of the recent review articles are summarized in Table 1. Previous reviews have effectively encouraged the development of well-known WRM subjects, provided in-depth explorations of those subjects, and addressed future research trends to better handle significant problems. However, a thorough review is required for some reasons. Prior to this review, multidisciplinary reviews tended to be objective and disregard the reader's background knowledge. Moreover, they have rarely considered the instructional components of the subject and provided a comprehensive overview of an advanced problem or illuminated the mathematical structures of algorithms rather than focusing on their applications. Additionally, some cutting-edge engineering applications of ML, such as RL and other novel approaches to adapting ML to traditional prediction issues, have not yet been covered.

Table 1. Recent review articles on machine learning applications in WRM.

Research Domain	Description	Ref.
Streamflow forecasting	A comprehensive review of artificial intelligence models used in the review domain is presented, with the goal of optimizing reservoir operations.	[4]
Flood, precipitation estimation, water quality, and groundwater	An in-depth review of machine-learning applications in the review domain is presented.	[5]
Groundwater level modeling	An in-depth review of the ability of ML models in monitoring and predicting different aspects of the review domain is presented.	[6]
Hydropower operation	A systematic review of hydropower operation optimization using ML is presented.	[7]
Groundwater level prediction	The state-of-the-art ML models implemented in the review domain and the milestones achieved in this domain are presented.	[8]
Drought prediction	The most used architectures in the review domain during the last two decades are evaluated.	[9]
Water quality modeling	The state-of-the-art applications of machine learning and deep learning in the review domain are presented.	[10]
Water quality evaluation	The applications of ML in various water environments such as surface and ground water, drinking water, seawater, and sewage are described.	[11]
Groundwater level prediction	Various ML and AI techniques and their corresponding methodologies in the review domain are discussed.	[12]
High-flow extremal hydrology	A comprehensive review is presented including an overview of the state-of-the-art AI techniques and examples of their applications, followed by a SWOT analysis to benchmark their predictive capabilities.	[13]
Hydro-climatic processes	An in-depth review of the different techniques of prediction interval development in the review domain is presented.	[14]
Streamflow forecasting	An in-depth review of decadal progress in the regionalization of hydrological modeling for predictions in ungauged basins from 2000 to 2019 is presented.	[15]
Suspended sediment load prediction	Three popular artificial intelligence-based models are described, mainly focusing on the research between January 2015 and November 2020 in the review domain.	[16]
Water resources in arboriculture	An overview of the application of new technologies in the analysis of crop water status to improve irrigation management, with a focus on arboriculture is presented.	[17]
Drought prediction	Various artificial intelligence techniques used in the review domain are presented.	[18]

3. Major Application of ML in WRM

ML algorithms are typically categorized into three main groups: supervised, unsupervised, and RL [5]. A comparison of these is summarized in Table 2. Supervised learning algorithms employ labeled datasets to train the algorithms to classify or predict the output, where both the input and output values are known beforehand. Unsupervised learning algorithms are trained using unlabeled datasets for clustering. These algorithms discover hidden patterns or data groupings without the need for human intervention. RL is an area of ML that concerns how intelligent an agent is to take action in an environment to obtain the maximum reward. In both supervised and RL, inputs and outputs are mapped such that the agent is informed of the best strategy to take in order to complete a task. In RL, positive and negative behaviors are signaled through incentives and penalties, respectively. As a result, in supervised learning, a machine learns the behavior and characteristics of labeled datasets, detects patterns in unsupervised learning, and explores the environment without any prior training in RL algorithms. Thus, an appropriate category of ML is required based on the engineering application. The major ML learning types in WRM are summarized in Figure 2, where the first segment covers the core contents of the research reviewed in the following sections.

Table 2. Comparison of supervised, unsupervised, and reinforcement learning algorithms.

Learning Types	Type of Data	Training	Used for	Algorithms
Supervised Learning	Labeled data	Trained using labeled data (extra supervision)	Regression for nowcasting and forecasting	Classification in binary and multiple classes Linear regression, logistic regression, RF, SVM, KNN, RNN, DNN, etc.
Unsupervised Learning	Unlabeled data	Trained using unlabeled data without any guidance (no supervision)	Clustering	K—Means, C—Means, Agglomerative Hierarchical Clustering, DBSCAN, Gaussian Mixture Models, OPTICS, etc.
Reinforcement Learning	Without predefined data	Works based on the interaction between agent and environment (no supervision)	Decision making	Q—Learning, SARSA, DQN, double DQN, dueling DQN, etc.

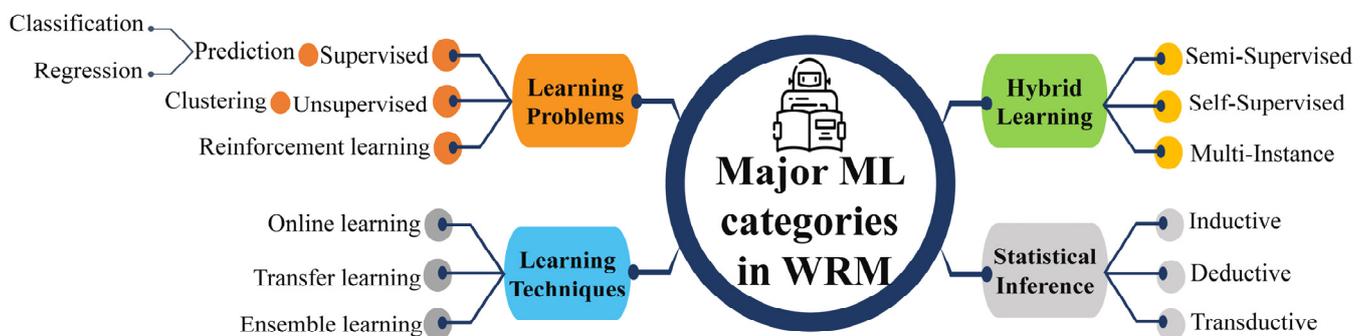


Figure 2. Four major types of machine learning.

3.1. Prediction

The term “prediction” refers to any technique that uses data processing to get an estimation of an outcome. This is the outcome of an algorithm that was trained on a

prior dataset and is now being applied to new data to assess the likelihood of a certain result in order to generate an output model. Forecasting is the probabilistic version of predicting an event in the future. In this review paper, the terms prediction and forecasting are used interchangeably. ML model predictions can be used to create very accurate estimations of the potential outcomes of a situation based on past data, and they can be about anything. For each record in the new data, the algorithm will generate probability values for an unknown variable, allowing the model builder to determine the most likely value. Prediction models can have either a parametric or non-parametric form; however, most WRM models are parametric. The development steps consist of four phases: data processing, feature selection, hyperparameter tuning, and training. Raw historical operation data are translated to a normalized scale in the data transformation step to increase the accuracy of the prediction model. The feature extraction stage extracts the essential variables that influence the output. These retrieved features are then used to train the model. The model's hyperparameters are optimized to acquire the best model structure. Finally, the model's weights are automatically modified to produce the final forecast model, which is of paramount importance for optimal control, performance evaluation, and other purposes.

3.1.1. Essential Data Processing in ML

For prediction purposes, ML algorithms can be applied to a wide variety of data types and formats, including time series, big data, univariate, and multivariate datasets. Time series are observations of a particular variable collected at regular intervals and in chronological order across time. A feature dataset is a collection of feature classes that utilize the same coordinate system and are connected. Its major purpose is to collect similar feature classes into a single dataset, which can be used to generate a network dataset. Many real-world datasets are becoming increasingly multi-featured because the ability to acquire information from a variety of sources is continuously expanding. Big data was first defined in 2005 as a large volume of data that cannot be processed by typical database systems or applications because of its size and complexity. Big data are extremely massive, complex, and challenging to process with the current infrastructure. Big data can be classified as structured, unstructured, or semi-structured. Structured data are the most well-known among hydrologist researchers because of their easy accessibility; they are usually stored in spreadsheets. Unstructured data such as images, video, and audio cannot be directly analyzed with a machine, whereas semi-structured data such as user-defined XML files can be read by a machine. Big data have five distinguishing characteristics (namely, the five Vs): volume, variety, velocity, veracity, and value. Recent developments in graphics processing units (GPUs) have paved the way for ML and its subset to get the advantage of big data and learn the complex and high dimensional environment. The establishment of a prediction model begins with the assimilation of data. It includes the phases of data collection, cleansing, and processing.

After adequate components have been gathered, any dataset needs to be structured. Predefined programs allow for the application of a variety of data manipulation, imputation, and cleaning procedures to achieve this goal. Anomalies and missing data are common in datasets and require special attention throughout the preprocessing phase. Depending on the goals of the prediction and the techniques selected, the clean data will require further processing. Depending on the type of prediction model being used, a dataset may employ a single labeled category or multiple categories. In ML, there are four types of data: numerical, categorical, time series, and text. The selected data category affects the techniques available for feature engineering and modeling, as well as the research questions that can be posed. Depending on how many variables need to be predicted, a prediction model will either be univariate, bivariate, or multivariate. In the processing phase, the raw data are remodeled, combined, reorganized, and reconstructed to meet the needs of the model.

3.1.2. Algorithms and Metrics for Evaluation

Because the outcomes of various ML approaches are not always the same, their performances are assessed by considering the outcomes acquired. Numerous statistical assessment measures have been proposed to measure the efficacy of the ML prediction technique. Table 3 summarizes some commonly used ML evaluation metrics, classifying them as either magnitude, absolute, or squared error metrics. The mean normalized bias and mean percentage error, which measures the discrepancies between predicted and observed values, fall under the first group. When only the amount by which the data deviate from the norm is of interest, an absolute function can be used to report an absolute error as a positive value, where Y , \hat{Y} , \bar{Y} , and $\bar{\hat{Y}}$ denote the observed, predicted, the mean of the observed, and the mean of the predicted value, respectively.

Table 3. Performance criteria for prediction model evaluation [19,20].

Metric	Equation	Description
Mean normalized bias error	$MBE = \frac{1}{n} \sum_{i=1}^n \frac{Y_i - \hat{Y}_i}{Y_i}$	Estimation of the average bias of the prediction approach used to decide on measures for correcting the approach bias
Mean percentage error	$MPE = \frac{1}{n} \sum_{i=1}^n \frac{Y_i - \hat{Y}_i}{Y_i} \times 100$	The computed average of the percentage errors between a model's forecasts and the actual values of the quantity being forecast
Mean absolute error	$MAE = \frac{1}{n} \sum_{i=1}^n \hat{Y}_i - Y_i $	A statistic to assess the average magnitude of errors in a set of forecasts without considering the direction of the errors
Mean absolute percentage error	$MAPE = \frac{1}{n} \sum_{i=1}^n \left \frac{Y_i - \hat{Y}_i}{Y_i} \right \times 100$	An accuracy rating metric that measures accuracy as a percentage of the average absolute percentage error minus the real amounts divided by the real amounts
Relative absolute error	$RAE = \frac{\sum_{i=1}^n Y_i - \hat{Y}_i }{\sum_{i=1}^n Y_i - \bar{Y} }$	A relative metric for evaluating a prediction model's performance
Weighted mean absolute percentage error	$WMAPE = \frac{\sum_{i=1}^n Y_i - \hat{Y}_i }{\sum_{i=1}^n Y_i }$	A measure of a forecasting method's prediction accuracy that is a weighted version of the MAPE
Normalized mean absolute error	$NMAE = \frac{MAE}{\frac{1}{n} \sum_{i=1}^n Y_i }$	Intended to make it easier to compare datasets with different scales in terms of MAE
Mean squared error	$MSE = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$	Measures the variation between the mean squares of the real amount and forecast values
Root mean square error	$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2}$	An estimation of the mean amount of error
Coefficient of variation	$CV = \frac{\sqrt{\frac{\sum_{i=1}^n (Y_i - \hat{Y}_i)^2}{n}}}{\bar{Y}}$	Known as the relative standard deviation, it is a standardized measurement of the dispersion of a probability distribution
Normalized root mean square error	$NRMSE = \frac{RMSE}{Y_{imax} - Y_{imin}}$	A normalized RMSE to facilitate comparisons between datasets and models with different scales
Coefficient of determination	$R^2 = 1 - \frac{\sum_{i=1}^n (\hat{Y}_i - \bar{Y})^2}{\sum_{i=1}^n (Y_i - \bar{Y})^2}$	Measurement of the variance ratio of a dependent variable using an independent variable

Table 3. Cont.

Metric	Equation	Description
Willmott’s index agreement	$WI = 1 - \left[\frac{\sum_{i=1}^n (Y_i - \hat{Y}_i)^2}{\sum_{i=1}^n (Y_i - \hat{Y}_i + \hat{Y}_i - \bar{Y})^2} \right]$	Measurement of the ratio of the mean square error and the potential error
Legates–McCabe’s	$LM = 1 - \left[\frac{\sum_{i=1}^n Y_i - \hat{Y}_i }{\sum_{i=1}^n Y_i - \bar{Y} } \right]$	A useful alternative goodness-of-fit or relative error that overcomes many of the limitations of correlation-based metrics
Kling–Gupta efficiency	$KGE = \sqrt{[r - 1]^2 + [\alpha - 1]^2 + [\beta - 1]^2}$ $r = \frac{cov(\hat{Y}, Y)}{\sigma(\hat{Y})\sigma(Y)}, \alpha = \frac{\sigma(\hat{Y})}{\sigma(Y)}, \beta = \frac{\bar{\hat{Y}}}{\bar{Y}}$	Measures the model efficiency with accuracy, precision, and consistency components. Here, r , α , and β represent the correlation coefficient, the bias (ratio between the standard deviations of the predicted and observed values), and the ratio of variances, respectively. σ denotes the standard deviation.
Akaike information criterion	$AIC = -2 \log(L(\theta^{\hat{ML}} Y)) + 2i$	A measure of a model performance that accounts for model complexity. $\theta^{\hat{ML}}$ represents the vector of maximum likelihood estimates of the model parameters, and i denotes the number of the observed values.
Probabilistic Metric		
Continuous ranked probability score	$CRPS = \int_{-\infty}^{+\infty} [P(\hat{Y}_i) - H(\hat{Y}_i - Y_i)]^2 d\hat{Y}_i$	A quadratic measure of the difference between forecast and empirical cumulative distribution functions (CDF), $P(\hat{Y}_i)$ is the prediction CDF, and H is the Heaviside step function, which is equal to 0 if $\hat{Y}_i < Y_i$ and 1 otherwise.
Average width of the prediction intervals	$AWPI = \frac{1}{n} \sum_{i=1}^n (\hat{Y}_i^u - \hat{Y}_i^l)$	An estimate of an interval in which a future observation will fall, with a certain confidence level, based on previous observations. u and l denote the upper and lower bounds of the 95 % prediction interval, respectively.
Prediction interval coverage	$PICP = \frac{1}{n} \sum_{i=1}^n c_i, c_i = \begin{cases} 1, & \text{if } Y_i \in [\hat{Y}_i^l, \hat{Y}_i^u] \\ 0, & \text{if } Y_i \notin [\hat{Y}_i^l, \hat{Y}_i^u] \end{cases}$	The percentage of the time the prediction interval covers the actual value in a holdout set
Prediction interval normalized average width	$PINAW = \frac{1}{n} \sum_{i=1}^n \frac{\hat{Y}_i^u - \hat{Y}_i^l}{R}$	Measures the wide degree of the prediction interval. R denotes the range of variation of the observed value.

3.1.3. Applications and Challenges

The metrics used to evaluate the performance of ML models based on the accuracy of the predicted values are presented in Table 3. Choosing the correct metric to evaluate a model is crucial, as some models may only produce favorable results when evaluated using a specific metric. Researchers’ assessments of the significance of various characteristics in the outcomes are influenced by the metrics they use to evaluate and compare the performances of ML algorithms. Each year, a considerable number of papers are published to share the successes and achievements in the vast area of WRM. In the field of hydrology, some studies employ recorded data such as streamflow, precipitation, and temperature data, whereas others employ processed data such as large-scale atmospheric data, which are generated using gauge and satellite data. When it comes to predictions in the field of

WRM, data-driven models perform better than statistical models owing to their higher capability in a complex environment. Table 4 provides a brief overview of some of the recent applications of ML for WRM prediction, with the relevant abbreviations defined in the glossary.

Table 4. Recent applications of ML for prediction in WRM.

Research Field	Algorithm	Goal	Ref.
Streamflow	LSTM, BNN, LSTM-MC, BLSTM	Developing a probabilistic forecasting model that addresses the relevant subproblem of univariate time series models for multistep ahead daily streamflow forecasting in order to quantify both epistemic and aleatory uncertainty.	[19]
Streamflow	SVR, TSVR, ELM, Huber loss function-based ELM	Adopting new data preprocessing techniques to capture the data noise and enhance prediction accuracy.	[21]
Streamflow	Bi-directional LSTM, Stacking of RF and MLP	Introducing a novel streamflow forecasting model.	[22]
Soil Moisture	MLP, RF, SVR	Applying machine learning with novel structures for the estimation of daily volumetric soil water content.	[23]
Water quality in an urban drainage network	EMD-LSTM	Combining a data preprocessing mechanism based on empirical mode decomposition (EMD) with an LSTM neural network prediction module.	[24]
Contamination in water distribution systems	ANN, SVM with linear kernels, SVM with radial basis function kernels (RBF), linear regressor, decision tree, extra trees, gradient boosting regressor, RF, KNN, and uniform weighted KNN	Introducing a new stacking ensemble model for contamination detection based on several water quality metrics.	[25]
Urban water quality	RF, SVM	Creating an integrated decomposition-reclassification-prediction technique for water quality by combining the CEEMDN and RF methods with the genetic algorithm-support vector machine model (GA-SVM).	[26]
Leakage detection	LSTM	Constructing a model using multi-layer perceptron (MLP) and LSTM to predict MNF (minimal night flow).	[27]
Failure rate	ANN	Identifying the most effective serial triple diagram model (STDM) methodologies for predicting the daily failure rates of a water distribution system.	[28]
Water demand	Graph convolutional recurrent neural network (GCRNN)	Building a graph-based model capable of capturing the dependence among the different water demand time series in both spatial and temporal terms.	[29]
Water consumption	ARIMA, LSTM	Developing a water consumption prediction model for individual customers using a deep learning-based LSTM approach.	[30]
Hydropower	SVR, LSTM	Developing a theory-guided ML framework and validating the model's performance for a reservoir located in Southwest China.	[31]

Table 4. Cont.

Research Field	Algorithm	Goal	Ref.
Hydropower	DNN	Exploring if it is desirable to use the known energy production of previous days as a predictor or to predict the day ahead inflows and then simulate the consequent energy production.	[32]
Hydropower	ANN, ARIMA, SVM	Investigating the capabilities of different ML algorithms in predicting the power production of a reservoir in China using data from 1979 to 2016.	[33]
Water levels	LSTM, GRU	Developing an efficient and precise data model for predicting water levels with extreme temporal variations.	[34]
Streamflow	CNN-BAT	Demonstrating the prediction accuracy of a convolutional neural network (CNN) using BAT metaheuristic algorithm.	[35]
Groundwater	ARIMA, a back-propagation artificial neural network (BP-ANN), LSTM	Investigating the accuracy of the model in forecasting the GWL at the monthly and daily scales by using three widely used data-driven models: an autoregressive integrated moving average (ARIMA), a back-propagation artificial neural network (BP-ANN), and an LSTM network.	[36]
Groundwater	Ensemble learning (FFNN, ANFIS, GMDH), LASTM	Forecasting multi-step ahead GWL of each cluster's piezometer centroid.	[37]
Streamflow	LSTM	Integrating meteorological forecasts, land surface hydrological model simulations, and ML to forecast hourly streamflow.	[38]
Precipitation	LSTM	Proposing a combination of the weather research and forecasting hydrological modeling system (WRF-Hydro) and LSTM network to improve streamflow prediction.	[39]
Streamflow	ANN, CNN, LSTM	Evaluating the possibilities of singular spectral analysis (SSA), seasonal-trend decomposition utilizing loess (STL), and attribute selection preprocessing approaches with neural network techniques for predicting monthly streamflow.	[40]
Streamflow	ConvLSTM, LSTMNet, 3D-CNN, TD-CNN, transformer	Enhancing the multi-step ahead prediction capability by using mesoscale hydroclimate data as booster predictors and employing attention-based DNNs.	[20]
Water quality	Deep transfer learning based on transformer (TLT)	Introducing a transfer learning approach to water quality prediction in order to improve prediction performance in data constrained environments.	[41]
Streamflow	ANN, ELM, SVM, EMD, EEMD	Developing a hydrological forecasting model based on parallel cooperation search algorithm (PCSA) and extreme learning machine (ELM).	[42]
Streamflow	BART	Developing a novel hybrid model, GA-BART, that combines a genetic algorithm (GA) and the Bayesian additive regression tree (BART) model for hourly streamflow forecasting.	[43]
Streamflow	DGDNN	Introducing a DL model and directed graph DNN for multi-step streamflow prediction.	[44]

Table 4. Cont.

Research Field	Algorithm	Goal	Ref.
Streamflow	ANFIS-GBO	Improving the accuracy of prediction in a mountainous river basin.	[45]
Streamflow	ELM-PSOGWO	Introducing a hybrid model based on heuristic optimization and extreme learning machine algorithms for monthly runoff prediction.	[46]
Streamflow	ANN-EMPA	Introducing a hybrid model based on extended marine predators algorithm (EMPA)-based ANN	[47]

Today, most countries are putting more pressure on their water resources than ever before. The world's population is growing quickly, and if things stay the same, there will be a 40% gap between how much water is needed and how much is available by 2030. In addition, extreme weather events like floods and droughts are seen as some of the biggest threats to global prosperity and stability. People are becoming more aware of how water shortages and droughts make fragile situations and conflicts worse. Changes in hydrological cycles due to climate change will exacerbate the problem by making water more volatile and increasing the frequency and severity of floods and droughts. Approximately 1 billion people call monsoonal basins home, while another 500 million call deltas home. In this situation, the lives of millions of people are relying on a sustainable integrated WRM plan, which is an essential issue being handled by engineers and hydrologists. To increase water security in the face of increasing demand, water scarcity, growing uncertainty, and severe natural hazards such as floods and droughts, politicians, governments, and all shareholders will be required to invest in institutional strengthening, data management, and hazard control infrastructure facilities. Institutional instruments such as regulatory frameworks, water prices, and incentives are needed for better allocation, governance, and conservation of water resources. Having open access to information is essential for water resources monitoring, decision-making under uncertainty, hydro-meteorological prediction, and early warning. Ensuring the quick spread and appropriate adaptation or use of these breakthroughs is critical for increasing global water resilience and security. However, the absence of appropriate data sets restricts the accuracy of prediction models, especially in complex real-world applications. Moreover, advanced multi-dimensional prediction models are scarce in hydrology and WRM studies. ML algorithms should be able to self-learn and make accurate predictions based on the provided data. It is anticipated that models that integrate various efficient algorithms into elaborate ML architectures will form the groundwork for future research lines. Some of the difficulties currently encountered in hydrological prediction may be overcome by employing newly emerging networks such as graph neural networks. The lack of widespread adaption of cutting-edge algorithms in the water-resource field, such as those used in image and natural language processing, hampers the creation of cutting-edge multidisciplinary models for integrated WRM. Table 4 shows no signs of the implementation of attention-based models, CNNs, or even more compatible models with long sequence time-series forecasting (LSTF), such as informer and conformer. Finding an appropriate prediction model and prediction strategy is the primary difficulty in prediction research. The five initial steps for ML prediction models are shown in Figure 3. If even one of these steps is conducted poorly, it will affect the rest, and as a result, the entire prediction strategy will fail.

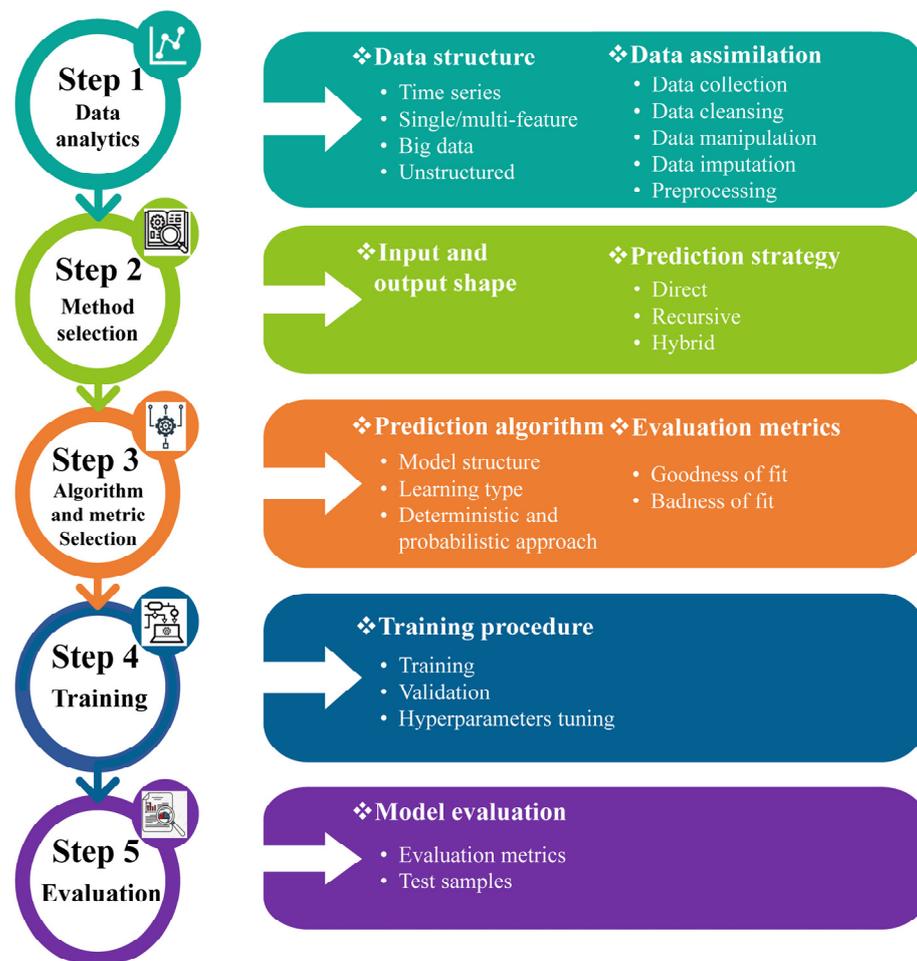


Figure 3. Steps of machine learning–based prediction strategies.

3.2. Clustering

The importance of clustering in hydrology cannot be overstated. The clustering of hydrological data provides rich insights into diverse concepts and relations that underline the inherent heterogeneity and complexity of hydrological systems. Clustering is a form of unsupervised ML that can identify hidden patterns in data and classify them into sets of items that share the most similarities. Similarities and differences among cluster members are revealed by the clustering procedure. The intra-cluster similarity is just as important as inter-cluster dissimilarity in cluster analysis. Different clustering algorithms vary in how they detect different types of data patterns and distances. Classification is distinct from clustering. In other words, a machine uses a supervised procedure called classification to learn the pattern, structure, and behavior of the data that it is fed. In supervised learning, the machine is fed with labeled historical data in order to learn the relationships between inputs and outputs, whereas in unsupervised learning, the machine is fed only input data and then asked to discover the hidden patterns. In this method, data is clustered to make models more manageable, decrease their dimensionality, or improve the efficiency of the learning process. Each of these applications, along with the pertinent literature, is discussed in this section.

3.2.1. Algorithms and Metrics for Evaluation

There are numerous discussions of clustering algorithms in the literature. Some studies classify clustering algorithms as monothetic or polythetic. Members of a cluster share a common set of characteristics in monothetic approaches, whereas polythetic approaches are based on a broader measure of similarity [48]. Depending on the algorithm’s parameters, a

clustering algorithm may produce either hard or soft clusters. Hard clustering requires that an element is either a member of a cluster or not. Soft clustering allows for the possibility of cluster overlap. The structure of the resulting clusters may be flat or hierarchical. While some strategies for clustering produce collections of groups, others benefit from a systematic approach. Algorithms for hierarchical clustering may be agglomerative or divisive [49]. A dataset’s points are clustered by combining them with their neighbors using agglomerative approaches. The desired number of clusters is attained by repeatedly dividing the original unit in divisive approaches.

The well-known clustering algorithms in WRM are shown in Figure 4. Many clustering algorithms fall into the individual branches of the figure. Some of the famous partitioning methods are K-means, K-medians, and K-modes. These algorithms are centroid-based methods that form clusters around known data centroids. Fuzzy sets and fuzzy C-means are soft clustering techniques applied extensively in control systems and reliability studies. The density-based spatial clustering of applications with noise (DBSCAN) and its updated version, distributed density-based clustering for multi-target regression, deals with probabilities while clustering. Divisive clustering analysis (DIANA) and agglomerative nesting (AGNES) are two hierarchical methods and functions that readily visualize the clustering procedure. The performances of these algorithms significantly depend on the distance functions chosen. Distribution-based clustering of large spatial databases (DBCLASD) and Gaussian mixed models are some of the popular distribution-based functions built upon mature experiments. The statistics of support vectors are used by the support vector clustering algorithms to develop data clusters with some margins. Table 5 lists some of the error functions commonly used to assess the performance of clustering algorithms. These metrics can be used to answer both the question of which clustering method performs better and the question of how many clusters should be used in a given dataset. These issues may be addressed in a variety of ways, such as through the use of graphical inspection and the implementation of an optimization algorithm. Nonetheless, this relies on the clustered dataset, and no comprehensive approaches have yet been proposed.

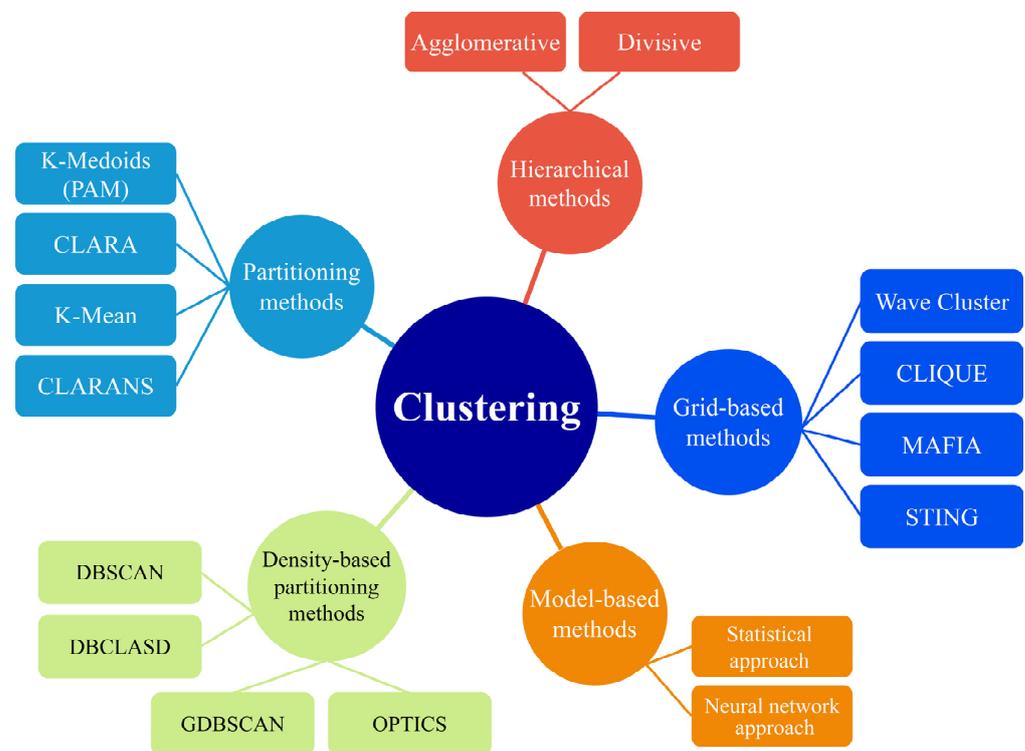


Figure 4. Clustering algorithms organization.

Table 5. Common error functions in clustering.

Metric	Equation	Description	Ref.
Calinski-Harabasz	$CH = \frac{n-k}{k-1} \frac{\sum_{i=1}^k C_i d(v_i, \bar{x})}{\sum_{i=1}^k \sum_{x_j \in C_i} d(v_i, \bar{x})}$	The numerator measures the distance between the cluster centroids and the global centroid, whereas the denominator measures the distances between centroids within each cluster. Clearly, a valid optimal partition is indicated by the largest CH.	[50]
Chou-Su-Lai	$CS = \frac{\sum_{i=1}^k \left\{ \frac{1}{ C_i } \sum_{x_j \in C_i} \max_{x_l \in C_i} d(v_i, \bar{x}) \right\}}{\sum_{i=1}^k \left\{ \min_{j \neq i} d(v_i, \bar{x}) \right\}}$	The numerator is the sum of the average maximum distances between points within each cluster, and the denominator is the sum of the minimum distances between clusters. The partition with the smallest CS is valid and optimal.	[51]
Dunn’s index	$\min_{i \neq j \in [k]} \left\{ \frac{DI = \min\{d(x_u, x_v) x_u \in C_i, x_v \in C_j\}}{\max_{l \in [k]} \max\{d(x_u, x_v) x_u, x_v \in C_l\}} \right\}$	The numerator represents the minimum between-cluster distance, whereas the denominator represents the maximum within-cluster distance. The largest DI indicates an optimally valid partitioning.	[52]
Davies-Bouldin’s index	$DB = \frac{1}{k} \sum_{i=1}^k \max_{j \in [k] \setminus \{i\}} \left\{ \frac{S_{i,q} + S_{j,q}}{(\sum_{s=1}^p v_{i,s} - v_{j,s} ^t)^{\frac{1}{t}}} \right\}$	The partition with the smallest DB is the optimal partition.	[53]
Davies-Bouldin’s Index*	$DB^* = \frac{1}{k} \sum_{i=1}^k \frac{\max_{j \in [k] \setminus \{i\}} \{S_{i,q} + S_{j,q}\}}{\min_{j \in [k] \setminus \{i\}} \left\{ (\sum_{s=1}^p v_{i,s} - v_{j,s} ^t)^{\frac{1}{t}} \right\}}$	The smallest DB* denotes a valid optimal partition, similar to the original DB.	[54]
Silhouette Coefficient	$\frac{1}{N} \sum_{i=1}^n s_i, s_i = \begin{cases} \frac{SC = \frac{b_i - a_i}{\max\{b_i, a_i\}}}{0} & \text{if } C_l > 1, \\ \text{if } C_l = 1 \end{cases}$ $\begin{cases} a_i = \frac{1}{ C_l -1} \sum_{j: x_j \in C_l} d(x_i, x_j) \\ b_i = \min_{s \neq l} \frac{1}{ C_s } \sum_{j: x_j \in C_s} d(x_i, x_j) \end{cases}$	The largest SC denotes an optimal partition which is valid.	[55]
Hybrid validity index	$SCD = \frac{SC}{(0.5CS + 0.5DB)}$	SCD is a collection of three robust measures of cluster validity (SC, CS, and DB).	[37]

3.2.2. Clustering in the Field of WRM

Clustering techniques are extensively applied in different WRM fields. It is up to the discretion of the decision maker (DM) to choose the best strategy for the growth and use of water resources. When the DM has access to relevant data, better decisions should follow. However, as more data become available, the DM will have a harder time compiling relevant summaries and settling on a single decision option. Clustering analysis has proven to be a useful method of condensing large amounts of data into manageable chunks for easier analysis and management in a decision-making environment [56].

Some of the applications of clustering algorithms in hydrology include time series modeling [57], interpolation and data mining [58], delineation of homogenous hydro-meteorological regions [59], catchment classification [60], regionalization of the catchment for flood frequency analysis and prediction [61], flood risk studies [62], hydrological modeling [63], hydrologic similarity [64], and groundwater assessment [65,66]. Clustering is useful in these situations because it simplifies the creation of effective executive plans and maps by reducing the problem diversity. Furthermore, one of the more traditional uses of clustering analysis is in spotting outliers and other anomalies in the dataset. Any clustering approach can be used for anomaly detection, but the choice will depend on the nature and structure of the data. To sum up, cluster analysis is advantageous for complex

projects because it enables accurate dimension reduction for both models and features without compromising accuracy.

3.2.3. Clustering Applications and Challenges in WRM

Some recent applications of clustering algorithms in WRM are summarized in Table 6. Model simplification, ease of learning, and dimensionality reduction are all areas where K-means variants contribute significantly to hydrological research. Moreover, they are easy to change to fit different types, shapes, and distributions of data, and they are easy to apply and available in most commercial data analysis and statistics packages. As shown in Table 6, K-means and hierarchical clustering are the most commonly used methods in WRM. The former can handle big data well, while the later cannot. This is because the time complexity of K-means is linear, whereas that of hierarchical clustering is quadratic [67]. Hierarchical algorithms are predominantly used for dimension reduction [68]. Data imputation and cleaning are two examples of secondary data analytics applications that benefit from density-based algorithms. Furthermore, a recent study by Gao et al. [69] reported the capability of density-based algorithms for clustering a dataset with missing features. Most studies report the number of clusters required for the successful application of a clustering algorithm because conventional clustering algorithms cannot efficiently handle real-world data clustering challenges [70]. As shown in Table 6, the required number of clusters varies considerably based on the nature of the problem. While the optimal method for determining the number of clusters to employ is discussed in the majority of clustering papers, this is still a topic of debate in the ML community.

Table 6. Applications of clustering algorithms in WRM.

Research Field	Cluster No.	Algorithm	Goal	Ref.
Water distribution system	3–5	OPTICS/K-means	Determine different customer patterns based on the geographic locations of households	[71]
Water monitoring system	3	k-means	Monitor water consumption in a household to improve WRM	[72]
Sediment	5	Fuzzy C-means	Classify the Rhône River hydrology according to the main hydrological events	[73]
Hydrological regionalization	6	Hierarchical and K-means	Delineate the homogeneous clusters of watersheds	[74]
Water consumption patterns	-	k-means	Observe the consumption patterns with regard to their variability.	[75]
Hydrological time series clustering	4	Hierarchical/DBSCAN	Develop a clustering framework	[76]
Flood risk	1–3, 5, 7, 10, 20, 50, 100, 200, 500	k-means	Choosing the optimal number of clusters and associated parameter sets for a hydrologic model. model	[62]
Groundwater	2–10	K-Means/hierarchical (WARD)/self-organizing neural network (GNG)	Promote remediation measures for groundwater depletion and contamination	[77]
Groundwater	4, 5, 6	K-means/FCM/GNG/Cluster ensemble	Identify the patterns of groundwater level (GWL) over the Ghorveh-Dehgolan plain (GDP) located in western Iran	[37]

Table 6. Cont.

Research Field	Cluster No.	Algorithm	Goal	Ref.
Watershed zonation	1–7	K-means/hierarchical/Gaussian mixture	Characterize the organization and functions of the watershed in a more tractable manner by integrating multiple spatial data layers	[78]
Groundwater	5	agglomerative hierarchical	Classify wells in the San Joaquin River Basin, California	[79]
Hydrological regionalization	3	K-value	Regionalize lowland rivers using long data series and selected hydrological characteristics based on the example of Lithuanian rivers.	[80]
Karstic aquifers	1–5	K-means, fuzzy logic, fuzzy C-mean genetic K-means	Improve protection in a vulnerable karstic region	[81]
Rainfall	2, 3, 4, 7, 11	K-Means/Fuzzy C-Means	Determining the spatiotemporal patterns of torrential rainfall along the East Coast of Peninsular Malaysia	[82]
Flood	8	K-Means	Design and implementation of real-time monitoring	[83]
Streamflow	3	Hierarchical	Study the collective similarity in periodic phenomena	[84]
River	5	Hierarchical	Identify the primary causes of flow and sediment load variations	[85]
River	4	k-means	Analysis of climatic and physiographic catchment properties	[86]
Catchment hydrologic control	3	Hierarchical	Investigate landscape controls on hydrologic response through catchment classification	[87]
Water scarcity	3	k-means	Investigate how human adaptation affects water scarcity uncertainty	[88]
Flow regime	2–10	k-means	Stream analysis for bias estimation and reduction	[89]
Precipitation	3	k-means	Improve both medium- and long-term precipitation forecasting accuracy	[90]
Aquifer system	11	Hierarchical	Classify non-linear hydrochemical data	[91]

Although unsupervised learning performs well in reducing the dimensions of complicated models, the rate at which new clustering algorithms are created has fallen in recent years. Various neural networks can play a role as clustering algorithms. It is anticipated that new ML algorithms will be required to solve multidisciplinary WRM problems, and data clustering will be an important step in defining a constructive problem. After discovering their hidden patterns, ML algorithms are able to autonomously solve these problems. Clustering ensembles, as opposed to single clustering models, are at the forefront of computer science. The effectiveness of diverse ensemble architectures still needs to be investigated. The reliability of probabilistic clustering algorithms, which are an updated version of classic decision-making tools, have also been investigated in recent research. Unsupervised learning-based predictive models and their accuracy evaluation are a new field of research.

3.3. Reinforcement Learning

This section provides an in-depth introduction to RL, covering all the fundamental concepts and algorithms. After years of being ignored, this subfield of ML has recently

gained much attention as a result of the successful application of Google DeepMind to learning to play Atari games in 2013 (and, later, learning to play Go at the highest level) [92]. This modern subfield of ML is a crowning achievement of DL. RL deals with how to learn control strategies to interact with a complex environment. In other words, RL defines how to interact with the environment based on experience (by trial and error) as a framework for learning. Currently, RL is the cutting-edge research topic in the field of modern artificial intelligence (AI), and its popularity is growing in all scientific fields. It is all about taking appropriate action to maximize reward in a particular environment. In contrast to supervised learning, in which the answer key is included in the training data by labeling them, and the model is trained with the correct answer itself, RL does not have an answer; instead, the reinforcement autonomous agent determines what to do in order to accomplish the given task. In other words, unlike supervised learning, where the model is trained on a fixed dataset, RL works in a dynamic environment and tries to explore and interact with that environment in different ways to learn how to best accomplish its tasks in that environment without any form of human supervision [93,94]. The Markov decision process (MDP), which is a framework that can be utilized to model sequential decision-making issues, along with the methodology of dynamic programming (DP) as its solution, serves as the mathematical basis for RL [95]. RL extends mainly to conditions with known and unknown MDP models. The former refers to model-based RL, and the latter refers to model-free RL. Value-based RL, including Monte Carlo (MC) and temporal difference (TD) methods, and policy-search-based RL, including stochastic and deterministic policy gradient methods, fall into the category of model-free RL. State–action–reward–state–action (SARSA) and Q-learning are two well-known TD-based RL algorithms that are widely employed in RL-related research, with the former employing an on-policy method and the latter employing an off-policy method [90,91].

When it comes to training agents for optimal performance in a regulated Markovian domain, Q-learning is one of the most popular RL techniques [96]. It is an off-policy method in which the agent discovers the optimal policy without following the policy. The MDP framework consists of five components, as shown in Figure 5. To comprehend RL, it is required to understand agents, environments, states, actions, and rewards. An autonomous agent takes action, where the action is the set of all possible moves the agent can take [97]. The environment is a world through which the agent moves and responds. The agent's present state and action are inputs, while the environment returns the agent's reward and its next state as outputs. A state is the agent's concrete and immediate situation. An action's success or failure in a given state can be measured through the provision of feedback in the form of a reward, as shown in Figure 5. Another term in RL is policy, which refers to the agent's technique for determining the next action based on the current state. The policy could be a neural network that receives observations as inputs and outputs the appropriate action to take. The policy can be any algorithm one can think of and does not have to be deterministic. Owing to inherent dynamic interactions and complex behaviors of the natural phenomena dealt with in WRM, RL could be considered a remedy to solve a wide range of tasks in the field of hydrology. Most real-world WRM challenges can be handled by RL for efficient decision-making, design, and operation, as elucidated in this section.

Water resources have always been vital to human society as sources of life and prosperity [98]. Owing to social development and uneven precipitation, water resources security has become a global issue, especially in many water-shortage countries where competing demands over water among its users are inevitable [99]. Complex and adaptive approaches are needed to allocate and use water resources properly. Allocating water resources properly is difficult because many different factors, including population, economic, environmental, ecologic, policy, and social factors, must be considered, all of which interact with and adapt to water resources and related socio-economic and environmental aspects.

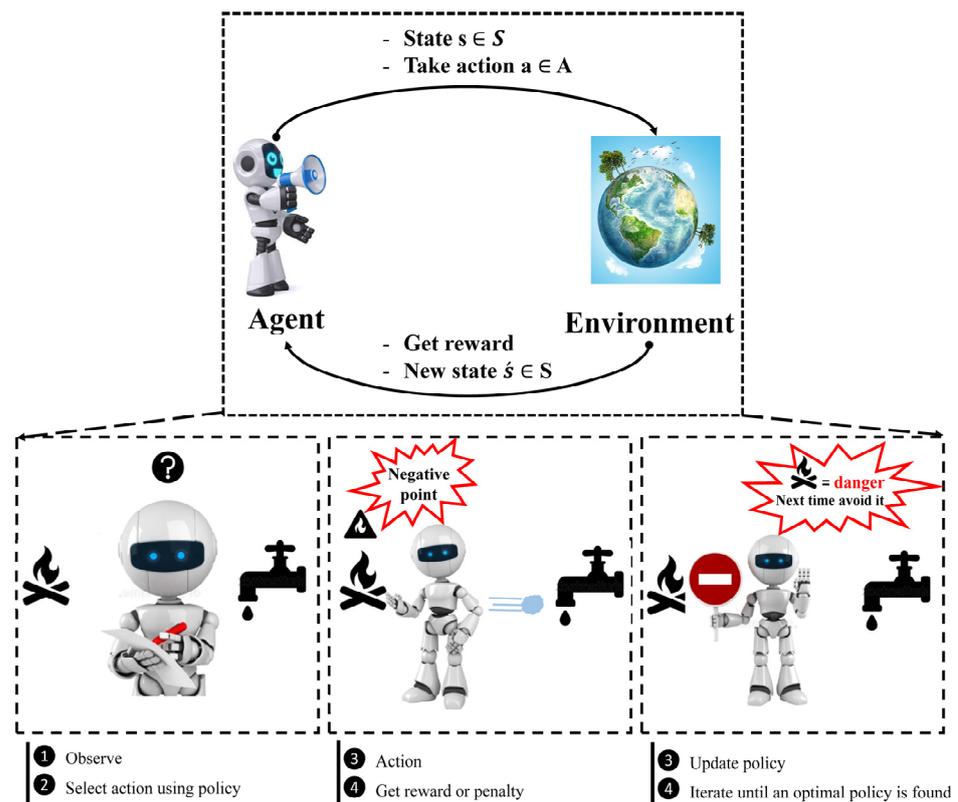


Figure 5. Concept of reinforcement learning (RL).

RL can be utilized to model the behaviors of agents, simplify the process of modeling human behavior, and locate the optimal solution, particularly in an uncertain decision-making environment, to optimize the long-term reward. Simulating the actions of agents and the feedback corresponding to those actions from the environment is the aim of RL-based approaches. In other words, RL involves analyzing the mutually beneficial relationships that exist between the agents and the system, which is an essential requirement in an optimal water resources allocation and management scenario. Another challenging yet less investigated issue in WRM and allocation is shared resource management. Without simultaneously considering the complicated and challenging social, economic, and political aspects, along with the roles of all the beneficiaries and stakeholders, providing an applicable decision-making plan for water demand management is not possible, especially in countries located in arid regions suffering from water crises. Various frameworks have been proposed to analyze and model such a multi-level, complex, and dynamic environment. In the last two decades, complex adaptive systems (CASs) have received much attention because of their efficacy [100].

In the realm of WRM, agent-based modeling (ABM) is a popular simulation method for investigating the non-linear adaptive interactions inherent to a CAS [95]. ABM has been widely used for simulating human decisions when modeling complex natural and socioecological systems. In contrast, the application of ABM in WRM is still relatively new [101], despite the fact that it can be used to define and simulate water resources wherein individual actors are described as unique and autonomous entities that interact regionally with one another and with a shared environment, thus addressing the complexity of integrated WRM [102,103]. In RL water resources-related studies, when addressing water allocation systems, from water infrastructure systems and ecological water consumers to municipal water supply and demand problem management, agents have been conceptualized to represent urban water end-users [104,105].

While RL has shown promise in self-driving cars, games, and robot applications, it has not been given widespread attention related to applications in the field of hydrology.

However, RL is expected to take over an increasingly wide range of real-world applications in the future, especially to obtain better WRM schemes. Over the past five years, numerous frameworks have emerged, including Tensorforce, which is a useful RL open-source library based on TensorFlow [106], and Keras-RL [107]. In addition to these, it is notable that there are now additional frameworks such as TF-agents [108], RL-coach [109], acme [110], dopamine [111], RLlib [112], and stable baselines3 [113]. RL can be integrated with a DNN as a function approximator to improve its performance. Deep reinforcement learning (DRL) is capable of automatically and directly abstracting and extracting high-level features while avoiding complex feature engineering for a specific task. Some trendy DRL algorithms that are modified from Q-learning include the deep Q-network (DQN) [92], double DQN (DDQN) [114], and dueling DQN [115]. Other packages for the Python programming language are available to facilitate the implementation of RL, including the PyTorch-based RL (PFRL) library [116]. Other fundamental, engineering-focused programming languages such as MATLAB (MathWorks), and Modelica (Modelica Association Project) have also been utilized for the development and instruction of RL agents. The application of RL in WRM and planning will simplify the complexity of all the conflicting interests and their interactions. It will also provide a powerful tool for simulating new management scenarios to understand the consequences of decisions in a more straightforward way [95]. The categorization of RL algorithms by OpenAI using [112–129] was utilized to draw the overall picture in Figure 6.

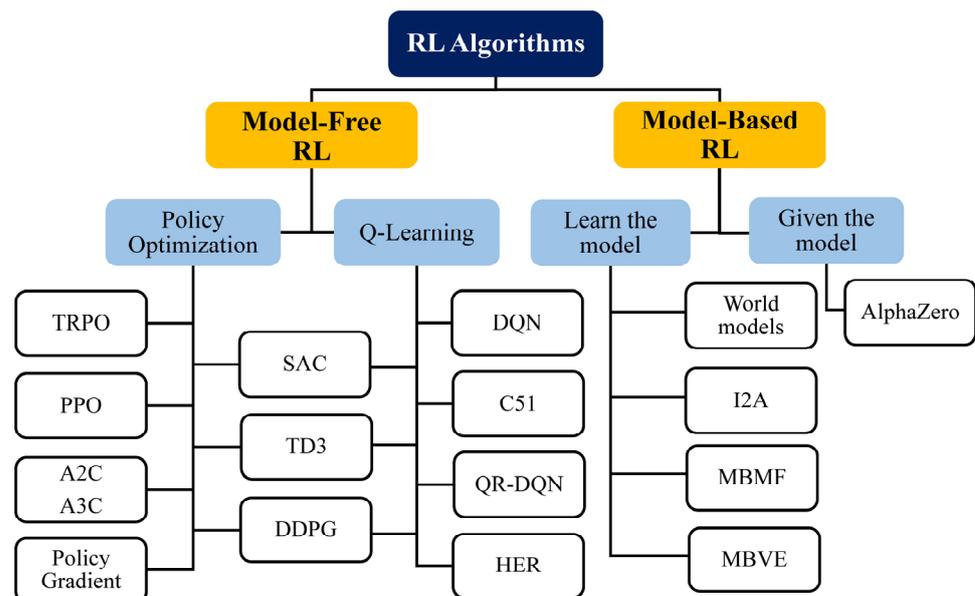


Figure 6. Reinforcement learning (RL) categorization (all the abbreviations are provided in the nomenclature).

4. Less-Studied Areas for ML Applications in WRM

In this section, less-studied areas for ML application, including spatiotemporal, geospatiotemporal, and probabilistic challenges in WRM are reviewed in order of their significance to future research. The following sections review the state-of-the-art applications of ML techniques in the field of WRM, the relevant problems, and a future trend.

Spatiotemporal studies model and analyze simultaneously how phenomena change over space and time. Due to the fact that they construct a one-dimensional picture of a multifaceted problem, they are of the utmost importance for the development of WRM strategies. In recent years, the emphasis on ML-driven spatiotemporal analysis tools has increased significantly. This is mainly due to the significant technical advancements made in the implementation of new assets, such as sensors and online devices that collect geographical and temporal data. At the beginning of the training process for an ML model,

the input data are annotated with geo-spatial and temporal features. This is done in order to model the data's dynamics while the machine is being trained. Various techniques have already been developed and formulated in order to make progress toward this objective. Depending on the geo-spatiotemporal context, time data can be presented as a continuous sequence, as a collection of sets that form an n-dimensional shape, or as a hidden component within the dynamic model itself. In the first, the machine can be trained with a single or multiple time series or the observation time can be recorded alongside the model's other variables as an independent variable. The second type of data includes the date, hour, and minute to facilitate the learning process. In the third scenario, the input data are organized according to the timestamps of the occurrences, increasing the monitoring efficiency. Similarly, geographic coordinates can be used to precisely assign the geo-spatiotemporal characteristics of data. In addition, data inputs can be labeled with geo-spatiotemporal information, or model variables can be explored across discrete cells on different grids. Each of these methods can be used to train a variety of algorithms; the most appropriate method typically depends on the available modeling environment and library resources, as well as the individual's preferences. Overall, the features of spatiotemporal and geo-spatiotemporal frameworks are instructed to consider time and location labels in spatiotemporal and longitude and latitude in geo-spatiotemporal frameworks, as depicted schematically in Figure 7a,b, respectively.

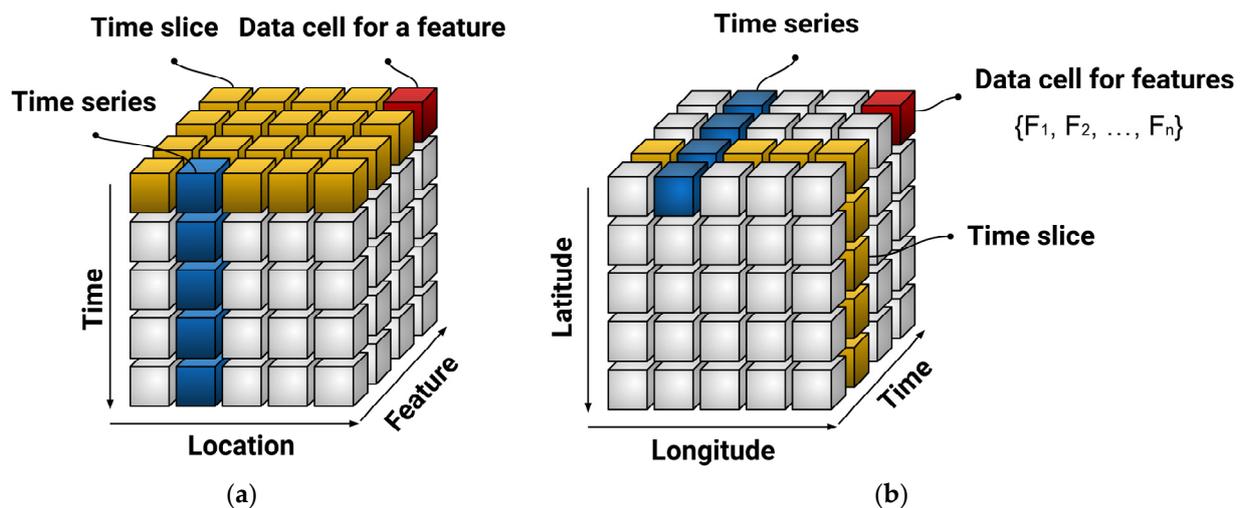


Figure 7. Schematic representation of ML-driven for (a) spatiotemporal model, and (b) geo-spatiotemporal model.

The field of hydrology is characterized by a high degree of epistemic uncertainty and limited knowledge of the inherent complexity. The limited quality and availability of data have been hindrances in both areas. In the field of hydrology, the development of automatic monitoring and surveillance sensors, as well as high-resolution remote sensing data from a variety of sources, has resulted in an abundance of new, high-quality data known as big data. Utilizing large-scale hydrological datasets necessitates the creation and implementation of new geo-spatiotemporal tools for use in computational analytics and hydrological modeling. In particular, technologies that fall under the concept of geospatial and geo-spatiotemporal AI, such as DL and parallel computing, provide the ways to effectively employ this geo-spatiotemporal dataset and improve integrated hydrological system modeling, especially in poorly gauged or even ungauged basins.

The application of newly emerging ML technologies, along with accessible large-scale hydroclimate data, simplifies the existing challenges in WRM due to the intermittent nature of natural phenomena and complexities of the existing correlations and inter-dependencies among them. Future studies must consider not only the complexity of integrated WRM systems, but also the hydrological uncertainties. Probabilistic method is an alternative

to consider the uncertainties in ML applications. A probabilistic approach is a method that considers uncertainty in the data not only to optimize the expected value but also to infer the distribution of such uncertainty. A probabilistic method such as the Bayesian approach can serve as a straightforward illustration of uncertainty investigation. The fitting of stochastic processes and determination of the parameters of distributions are examples of applications of probabilistic methods in WRM. These applications can be utilized for a wide variety of purposes, including streamflow prediction, pollution detection, resource allocation, and groundwater level prediction.

Another less-studied issue in the field of hydrology is considering the complex geo-spatiotemporal interdependencies among the input features in ML-driven models. Some recent spatiotemporal studies are summarized in Table 7. ML tools have been employed in a wide range of WRM fields, from streamflow prediction to pollution detection in a water distribution network. Due to the complexity of hydro-meteorological data's spatiotemporal patterns, predictive models typically require more complex algorithms to detect as many dependencies as possible. Newly emerged DNN algorithms can effectively capture spatiotemporal patterns in data. The type of geo-spatiotemporal problem, chosen algorithm, and the main objective of the simulation all influence the data resolution. Studies of basins at different scales can be conducted from the national to the local scale. Likewise, the temporal resolution can vary from monthly to just a few seconds in WRM studies. Many developed and developing countries throughout the world have used ML algorithms extensively. Prior to attention-based algorithms, which are more capable in handling the geo-spatiotemporal complexities, CNN, and LSTM were the most widely used algorithms in this field.

Table 7. State-of-the-art applications of ML to spatiotemporal studies.

Research Field	Data/Period	Location	Algorithm	Ref.
Hydrological extreme	Satellite rainfall estimates and sea surface temperature (SST) anomalies/1980–2020	Fiji's islands	LSTM	[130]
Flood	Six-hour precipitation based on Himawari-8 and ground station data	Xi County, China	ConvLSTM	[131]
Flood	60 historical events occurred in the area/1995–2020	Venice, Italy	LR, NN, RF	[132]
Droughts	Meteorological data from the openly accessible climate dataset PMD, which contains land-based observations/1980–2020	Cholistan, Punjab, Pakistan	RF	[133]
Droughts	Standardized precipitation index series with timescales of 3, 6, and 12 months during the 1951–2016 period	31 stations in Iran	Maximal overlap discrete wavelet transform (MODWT) and K-means	[134]
Precipitation	Radar station Z9270/2016–2020	Wuhan, China	ST-LSTM-SA	[135]
Groundwater	GWL, rainfall, runoff/1989–2018	Iran	Ensemble learning (FFNN, ANFIS, GMDH), LASTM	[37]

5. Challenges and Future Research

There are still significant limitations, despite the fact that all of the aforementioned studies have achieved great success. First, the majority of previous research focused on conventional ML models, whereas the newly emerging DL attention-based models (i.e., long- and short-term time-series networks (LSTNet), transformer, informer, and conformer) are in their infancy, particularly in the field of WRM. In addition, previous studies focused primarily on one or two aspects of prediction improvement, such as spatial or temporal dependencies, whereas the geo-spatiotemporal studies are still in the early stages. Notably, traditional algorithms often ignore spatiotemporal consistency. Nonetheless, a framework

that can generate 3D input data (i.e., high resolution, high spatiotemporal continuity, and high precision) is urgently required. Even though autocorrelated patterns are frequently identified in recorded datasets, ML algorithms have not been thoroughly utilized to manage geo-spatiotemporal problems in WRM. In this regard, Ghobadi et al. [20] proposed the application of multimedia tensors as inputs in order to extract the complex relationships in a geo-spatiotemporal environment and increase the accuracy of long-term multi-step ahead streamflow prediction. Moreover, in their research, the application of networks comprising different topping and bottoming models, each focusing on different types of interdependencies, was also proposed. Last but not least, attention-based DL, a new generation of ML technology, has been validated as a promising approach in a variety of domains, outperforming conventional ML models with considerable performance improvements.

It is anticipated that geo-spatiotemporal models will be developed as an extension of the current spatiotemporal models. In the absence of sufficient historical data, ML algorithms struggle to make accurate predictions. Therefore, it is anticipated that transfer learning algorithms will be developed in this area to take advantage of the data availability in some areas for use in a location with a lack of sufficient in-situ data. Moreover, the majority of recent nationwide spatiotemporal studies have employed static models that oversimplify the problem. It is anticipated that future research will develop dynamic models with accelerated data extraction. The remaining obstacles in spatiotemporal and geo-spatiotemporal research include the removal of irrelevant information from spatial data frames, the selection of the optimal temporal horizon and resolution, and the simplification of the interface between data mining tools and ML algorithms.

The advent of global hydroclimate data provides a permanent solution to hydrologic prediction at various geo-spatiotemporal scales for regions without sufficient stations or ungauged basins. Several prior studies evaluated the global applicability of hydroclimate data to improve prediction accuracy through spatiotemporal modeling [136,137]. These models form multivariate time series by concatenating time series across columns for each location. The open literature review indicates that the gradient vanishing issues prevent standalone prediction models like LSTM and GRU from providing an accurate long-term prediction, while integrated models can increase prediction accuracy [138]. Self-attention allows for the re-representation of an input sequence by focusing on different positions and capturing precise, long-term, and long-range dependencies. Recent studies suggest that the transformer network can improve long-term multivariate time series (MTS) prediction [20]. To the best of our knowledge, an open challenge in the field of hydrology is a systematic approach to dealing with complex geo-spatiotemporal dependencies to achieve robust long-term prediction. Moreover, another major bottleneck in DL is automatic feature engineering compatible with 3D data. [139]. To sum up, intelligent and cutting-edge integrated networks are necessary to address the existing complex and dynamic long-term dependencies in order to make accurate predictions and manage LSTF.

6. Conclusions

The first part of this review classified the major ML techniques into prediction, clustering, and reinforcement learning categories. Determining an appropriate prediction strategy as the main challenge of prediction studies has been addressed. Moreover, a prediction model procedure has been divided into five main steps to facilitate future studies, including data analytics, method selection, algorithm and metric selection, training, and evaluation. Data have been clustered in order to simplify models, reduce their dimensions, or facilitate the learning procedure in WRM-related studies. Several metrics have been reported to address major clustering challenges, including figuring out the ideal number of clusters and the clustering algorithm that best fits the data. The clustering algorithms were considered according to their goals, overlap, and structure to pave the way for configuring efficient ensembles of clustering algorithms in future studies. The second part of this review introduced spatiotemporal and geo-spatiotemporal views in existing studies that contribute to the design and operation of long-term WRM and planning. In order to solve complex

multiobjective, multiperiod, nonlinear water resources-related problems, this review suggested focusing on the RL method, which could be used to model the decision-making of agents capable of adapting to a dynamic environment by learning from past experiences. The spatiotemporal data resolution varies from miles and monthly values to inches and seconds. Future geo-spatiotemporal studies will develop multidimensional models that go beyond the spatial and temporal dimensions by employing new variants of attention-based networks such as LSTNet, transformer, conformer, and informer. Because integrated WRM and planning gives consideration to stakeholders' cognitive beliefs and values, the circular economy; water demand management; and natural, political, social, and economic disputes that contribute to water management problems count as essential aspects that must be considered. Moreover, owing to the existence of dynamic interactions and adaptations between water resources and related socio-economic and environmental areas, water crises, and resource allocation, this review suggests using RL in dealing with multidimensional research related to integrated WRM. In the near future, it is anticipated that RL agents will focus on this field in order to comprehend the behaviors of integrated hydrological systems, develop policies by employing an integrated pathway, and reveal the optimal management frameworks. Thanks to advancements in ML techniques, the WRM field is anticipated to witness the growth of intelligent control and monitoring infrastructure in the coming years.

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Nomenclature

A2c-A3c	Asynchronous Advantage Actor-Critic
ABM	Agent-based modeling
AGNES	Agglomerative nesting
AI	Artificial intelligence
AR	Autoregressive
ARIMA	AR-integrated moving average
BART	Bayesian additive regression tree
BNN	Bayesian neural network
BP-ANN	Back-propagation artificial neural network
C51	Categorical 51-Atom DQN
CAS	Complex adaptive systems
CLARA	Clustering Large Applications
CLARANS	Clustering Large Applications based on RANdomized Search
CNN	Convolutional neural networks
DBCLASD	Distribution-based clustering of large spatial databases
DBSCAN	Density-based spatial clustering of applications with noise
DDPG	Deep Deterministic Policy Gradient
DDQN	Double DQN
DIANA	Divisive clustering analysis
DL	Deep learning
DM	Data management
DM	Decision maker
DNN	Deep neural networks

DP	Dynamic programming
DQN	Deep Q-Network
DRL	Deep reinforcement learning
ELM	Extreme learning machine
EMD	Empirical mode decomposition
GA	Genetic algorithm
GNG	Growing neural gas
GRU	Gated recurrent unit
GWL	Groundwater level
HER	Hindsight Experience Replay
I2A	Imagination-Augmented Agents
IHP	Intergovernmental Hydrological Programme
KNN	K-nearest neighbors
LSTF	Long sequence time-series forecasting
LSTM	Long and short-term memory
LSTNet	Long- and Short-term Time-series network
MBMF	Model-Based RL with Model-Free Fine-Tuning
MBVE	Model-Based Value Expansion
MC	Monte Carlo
MDP	Markov Decision Process
ML	Machine learning
MLP	multi-layer perceptron
MODWT	Maximal Overlap Discrete Wavelet Transform
MTS	Multivariate time series
PCSA	parallel cooperation search algorithm
PPO	Proximal Policy Optimization
QR-DQN	Quantile Regression DQN
RF	Random forest
RL	Reinforcement learning
RNN	Recurrent neural networks
SAC	Soft Actor-Critic
SARSA	State–action–reward–state–action
STDM	Serial triple diagram model
SVM	Support vector machine
SWOT	Strengths, weaknesses, opportunities, and threats
TD	Temporal Difference
TD3	Twin Delayed DDPG
TRPO	Trust Region Policy Optimization

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