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Title A Framework Based on Finite Element Method (FEM) for Modelling and Assessing the Affection of the Local Thermal Weather Factors on the Performance of Anaerobic Lagoons for the Natural Treatment of Swine Wastewater

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Table S1 Biochemical rate coefficients (v_i) and kinetic rate equations (ρ_i) for soluble components ($i=1-12$; $j=1-19$). The matrix comes from the ADM1 Bastone et al. [2]

Component →	i	1	2	3	4	5	6	7	8	9	10	11	12	Rate (ρ_i kgCOD m ⁻³ · d ⁻¹)
j	Process	S_{su}	S_{aa}	S_{fa}	S_{va}	S_{bu}	S_{pro}	S_{ac}	S_{h_2}	S_{ch_4}	S_{ic}	S_{in}	S_i	
1	Disintegration												$f_{sl,xc}$	$k_{dis}X_c$
2	Hydrolysis of carbohydrates	1												$k_{hyd,ch}X_{ch}$
3	Hydrolysis of proteins		1											$k_{hyd,pr}X_{pr}$
4	Hydrolysis of lipids	$1 - f_{fa,li}$		$f_{fa,li}$										$k_{hyd,li}X_{li}$
5	Uptake of sugar	-1				$(1 - Y_{su})f_{bu,su}$	$(1 - Y_{su})f_{pro,su}$	$(1 - Y_{su})f_{ac,su}$	$(1 - Y_{su})f_{h_2,su}$		$-\sum_{i=1-9}^{11-29} C_i v_{i,5}$	$-(Y_{su})N_{bac}$		$k_{m,su} \frac{S_{su}}{K_s + S_{su}} X_{su} I_1$
6	Uptake of amino acids		-1		$(1 - Y_{aa})f_{va,aa}$	$(1 - Y_{aa})f_{bu,aa}$	$(1 - Y_{aa})f_{pro,aa}$	$(1 - Y_{aa})f_{ac,aa}$	$(1 - Y_{aa})f_{h_2,aa}$		$-\sum_{i=1-9}^{11-29} C_i v_{i,6}$	$N_{aa} - (Y_{aa})N_{bac}$		$k_{m,aa} \frac{S_{aa}}{K_s + S_{aa}} X_{aa} I_1$
7	Uptake of LCFA			-1				$(1 - Y_{fa})0.7$	$(1 - Y_{fa})0.3$			$-(Y_{fa})N_{bac}$		$k_{m,fa} \frac{S_{fa}}{K_s + S_{fa}} X_{fa} I_2$
8	Uptake of valerate				-1		$(1 - Y_{c4})0.54$	$(1 - Y_{c4})0.31$	$(1 - Y_{c4})0.15$			$-(Y_{c4})N_{bac}$		$k_{m,c4} \frac{S_{va}}{K_s + S_{va}} X_{c4} I_1 + \frac{1}{S_{bu}/S_{va}} I$
9	Uptake of butyrate					-1		$(1 - Y_{c4})0.8$	$(1 - Y_{c4})0.2$			$-(Y_{c4})N_{bac}$		$k_{m,c4} \frac{S_{bu}}{K_s + S_{bu}} X_{c4} I_1 + \frac{1}{S_{va}/S_{bu}} I$
10	Uptake of propionate						-1	$(1 - Y_{pro})0.57$	$(1 - Y_{pro})0.43$		$-\sum_{i=1-9}^{11-29} C_i v_{i,10}$	$-(Y_{pro})N_{bac}$		$k_{m,pr} \frac{S_{pro}}{K_s + S_{pro}} X_{pro} I_2$
11	Uptake of acetate							-1		$(1 - Y_{ac})$	$-\sum_{i=1-9}^{11-29} C_i v_{i,11}$	$-(Y_{ac})N_{bac}$		$k_{m,ac} \frac{S_{ac}}{K_s + S_{ac}} X_{ac} I_3$
12	Uptake of hydrogen								-1	$(1 - Y_{h_2})$	$-\sum_{i=1-9}^{11-29} C_i v_{i,12}$	$-(Y_{h_2})N_{bac}$		$k_{m,h_2} \frac{S_{h_2}}{K_s + S_{h_2}} X_{h_2} I_1$
13	Decay of X_{su}													$k_{dec,X_{su}} X_{su}$
14	Decay of X_{aa}													$k_{dec,X_{aa}} X_{aa}$
15	Decay of X_{fa}													$k_{dec,X_{fa}} X_{fa}$
16	Decay of X_{c4}													$k_{dec,X_{c4}} X_{c4}$
17	Decay of X_{pro}													$k_{dec,X_{pro}} X_{pro}$
18	Decay of X_{ac}													$k_{dec,X_{ac}} X_{ac}$
19	Decay of X_{h_2}													$k_{dec,X_{h_2}} X_{h_2}$
		Monosaccharides (kgCOD m ⁻³)	Amino acids (kgCOD m ⁻³)	Long chain fatty acids (kgCOD m ⁻³)	Total valerate (kgCOD m ⁻³)	Total butyrate (kgCOD m ⁻³)	Total propionate (kgCOD m ⁻³)	Total acetate (kgCOD m ⁻³)	Hydrogen gas (kgCOD m ⁻³)	Methane gas (kgCOD m ⁻³)	Inorganic carbon (kmoleC m ⁻³)	Inorganic nitrogen (kmoleN m ⁻³)	Soluble inerts (kgCOD m ⁻³)	Inhibition factors: $I_1 = I_{pH} I_{N,lim} I_{h_2}$ $I_1 = I_{pH} I_{N,lim} I_{h_2}$ $I_1 = I_{pH} I_{N,lim} I_{NH_3,ac}$

Table S2 Biochemical rate coefficients ($v_{i,j}$) and kinetic rate equations (p_i) for particulate components ($i=13-24$; $j=1-19$). The matrix comes from the ADM1 Bastone et al. [2]

Component →		i	13	14	15	16	17	18	19	20	21	22	23	24	36	37	38	39	Rate (p_i kg COD m ⁻³ · d ⁻¹)
j	Process _j		X_c	X_{ch}	X_{pr}	X_{li}	X_{su}	X_{aa}	X_{fa}	X_{c4}	X_{pro}	X_{ac}	X_{h2}	X_l	S_{lac}	$X_{lac,f}$	$X_{lac,o}$	S_{ca}	
1	Disintegration		-1	$f_{ch,xc}$	$f_{pr,xc}$	$f_{li,xc}$								$f_{xl,xc}$					$k_{dis} X_c$
2	Hydrolysis of carbohydrates			-1															$k_{hyd,ch} X_{ch}$
3	Hydrolysis of proteins				-1														$k_{hyd,pr} X_{pr}$
4	Hydrolysis of lipids					-1													$k_{hyd,li} X_{li}$
5	Uptake of sugar						Y_{su}												$k_{m,su} \frac{S_{su}}{K_s + S_{su}} X_{su} I_1$
6	Uptake of amino acids							Y_{aa}											$k_{m,aa} \frac{S_{aa}}{K_s + S_{aa}} X_{aa} I_1$
7	Uptake of LCFA								Y_{fa}										$k_{m,fa} \frac{S_{fa}}{K_s + S_{fa}} X_{fa} I_2$
8	Uptake of valerate									Y_{c4}									$k_{m,c4} \frac{S_{va}}{K_s + S_{va}} X_{c4} \frac{1}{1 + S_{hu}/S_{va}}$
9	Uptake of butyrate									Y_{c4}									$k_{m,c4} \frac{S_{bu}}{K_s + S_{bu}} X_{c4} \frac{1}{1 + S_{hu}/S_{bu}}$
10	Uptake of propionate										Y_{pro}								$k_{m,pr} \frac{S_{pro}}{K_s + S_{pro}} X_{pro} I_2$
11	Uptake of acetate											Y_{ac}							$k_{m,ac} \frac{S_{ac}}{K_s + S_{ac}} X_{ac} I_3$
12	Uptake of hydrogen												Y_{h2}						$k_{m,h2} \frac{S_{h2}}{K_s + S_{h2}} X_{h2} I_1$
13	Decay of X_{su}		1				-1												$k_{dec,Xsu} X_{su}$
14	Decay of X_{aa}		1					-1											$k_{dec,Xaa} X_{aa}$
15	Decay of X_{fa}		1						-1										$k_{dec,Xfa} X_{fa}$
16	Decay of X_{c4}		1							-1									$k_{dec,Xc4} X_{c4}$
17	Decay of X_{pro}		1								-1								$k_{dec,Xpro} X_{pro}$
18	Decay of X_{ac}		1									-1							$k_{dec,Xac} X_{ac}$
19	Decay of X_{h2}		1										-1						$k_{dec,Xh2} X_{h2}$
			Composites (kg COD m ⁻³)	Carbohydrates (kg COD m ⁻³)	Proteins (kg COD m ⁻³)	Lipids (kg COD m ⁻³)	Sugar degraders (kg COD m ⁻³)	Amino acid degraders (kg COD m ⁻³)	LCFA degraders (kg COD m ⁻³)	Valerate and butyrate degraders (kg COD m ⁻³)	Propionate degraders (kg COD m ⁻³)	Acetate degraders (kg COD m ⁻³)	Hydrogen degraders (kg COD m ⁻³)	Particulate inerts (kg COD m ⁻³)	Total lactate (kg COD m ⁻³)	Lactate (fermentation) degraders (kg COD m ⁻³)	Lactate (oxidation) degraders (kg COD m ⁻³)	Total calcium (mmole m ⁻³)	Inhibition factors: $I_1 = I_{pH} I_{in,im}$ $I_1 = I_{pH} I_{in,im} I_{h2}$ $I_1 = I_{pH} I_{in,im} I_{NH3,Xac}$

Table S3. Dynamic state variables included in the stoichiometry matrix (Tables A1 and A2).

Name	Description	Name	Description
X_c	composite	S_{bu}	total butyrate
X_{ch}	carbohydrates	S_{pro}	total propionate
X_{pr}	proteins	S_{ac}	total acetate
X_u	lipids	S_{h2}	hydrogen
X_l	particulate inerts	S_{ch4}	methane
S_l	soluble inerts	S_{ic}	inorganic carbon
S_{su}	monosacharides	S_{IN}	inorganic nitrogen
S_{aa}	amino acids	X_{su-h2}	biomass
S_{ta}	total LCFA	S_{cat}	cations
S_{va}	total valerate	S_{an}	anions