

Supplementary materials

This section collects obtained results from the applied methodology for analysis of pumping control systems on the case studies used in this article. Specifically, pumping station (PS4) of TF network and E1 network were used as case studies. The attached information corresponds from several pumping configurations of PS4 in TF network evaluated in reduced energy terms for each flow reduced rate. The other attached information corresponds from the optimal number of FSD and VSD pumps in operation and its respective consumed power (PT) of every pump model analyzed in E1 network.

Table S1. Pumping configurations evaluated in reduced energy terms (TF Network-PS4)

Pumping Configurations	No. of FSD	No. of VSD
0FSD-1VSD	0	1
0FSD-2VSD	0	2
0FSD-3VSD	0	3
1FSD-1VSD	1	1
1FSD-2VSD	1	2
0FSD-4VSD	0	4
2FSD-1VSD	2	1

Table S2. Results of the evaluation of the different configurations (rotation speed of the VSDs, α , reduced performance ϑ_c and reduced energy π_T) in the TF Network-PS4.

q	Pumping Configurations											
	0FSD-1VSD			0FSD-2VSD			0FSD-3VSD			1FSD-1VSD		
	α	ϑ_c	π_T	α	ϑ_c	π_T	α	ϑ_c	π_T	α	ϑ_c	π_T
0.00	0.52	0.00	0.11	0.52	0.00	0.21	0.52	0.00	0.32	0.52	0.00	0.11
0.06	0.52	0.18	0.13	0.52	0.09	0.24	0.52	0.06	0.36	0.52	0.18	0.13
0.13	0.53	0.34	0.14	0.53	0.18	0.25	0.52	0.12	0.37	0.53	0.34	0.14
0.19	0.53	0.48	0.15	0.53	0.26	0.26	0.53	0.18	0.38	0.53	0.48	0.15
0.25	0.54	0.59	0.16	0.53	0.34	0.27	0.53	0.24	0.39	0.54	0.59	0.16
0.31	0.55	0.68	0.17	0.53	0.41	0.28	0.53	0.29	0.40	0.55	0.68	0.17
0.38	0.56	0.75	0.19	0.54	0.47	0.30	0.53	0.34	0.42	0.56	0.75	0.19
0.44	0.58	0.80	0.21	0.54	0.53	0.31	0.54	0.39	0.43	0.58	0.80	0.21
0.50	0.59	0.84	0.23	0.55	0.59	0.33	0.54	0.43	0.44	0.59	0.84	0.23
0.57	0.61	0.87	0.25	0.56	0.63	0.34	0.55	0.47	0.46	0.61	0.87	0.25
0.63	0.62	0.88	0.28	0.56	0.68	0.36	0.55	0.51	0.48	0.62	0.88	0.28
0.69	0.64	0.89	0.31	0.57	0.71	0.38	0.56	0.55	0.50	0.64	0.89	0.31
0.75	0.66	0.89	0.34	0.58	0.75	0.40	0.56	0.58	0.52	0.66	0.89	0.34
0.82	0.69	0.88	0.38	0.59	0.78	0.42	0.57	0.62	0.54	0.69	0.88	0.38
0.88	0.71	0.87	0.42	0.60	0.80	0.45	0.57	0.64	0.56	0.71	0.87	0.42
0.94	0.73	0.85	0.46	0.61	0.83	0.48	0.58	0.67	0.59	0.73	0.85	0.46
1.01	0.76	0.83	0.51	0.62	0.85	0.51	0.59	0.70	0.61	0.76	0.83	0.51
1.07	0.78	0.81	0.57	0.63	0.86	0.54	0.60	0.72	0.64	0.78	0.81	0.57
1.13	0.81	0.79	0.63	0.64	0.88	0.57	0.61	0.74	0.67	0.81	0.79	0.63
1.19	0.83	0.77	0.69	0.65	0.89	0.60	0.61	0.77	0.70	0.83	0.77	0.69
1.26	0.86	0.75	0.77	0.67	0.90	0.64	0.62	0.78	0.74	0.86	0.75	0.77
1.32	0.89	0.73	0.84	0.68	0.91	0.68	0.63	0.80	0.77	0.89	0.73	0.84
1.38	0.91	0.71	0.93	0.69	0.91	0.72	0.64	0.82	0.81	0.91	0.71	0.93

q	Pumping Configurations											
	0FSD-1VSD			0FSD-2VSD			0FSD-3VSD			1FSD-1VSD		
	α	ϑ_c	π_T	α	ϑ_c	π_T	α	ϑ_c	π_T	α	ϑ_c	π_T
1.44	0.94	0.69	1.02	0.71	0.92	0.77	0.65	0.83	0.85	0.94	0.69	1.02
1.51	0.97	0.67	1.12	0.72	0.92	0.82	0.66	0.85	0.89	0.97	0.67	1.12
1.57	1.00	0.65	1.23	0.73	0.92	0.87	0.67	0.86	0.93	1.00	0.65	1.23
1.61	0.00	0.00	0.00	0.74	0.92	0.91	0.68	0.87	0.97	0.62	0.13	1.38
1.65	0.00	0.00	0.00	0.75	0.92	0.94	0.69	0.87	1.00	0.63	0.25	1.39
1.70	0.00	0.00	0.00	0.76	0.92	0.98	0.69	0.88	1.03	0.64	0.36	1.40
1.74	0.00	0.00	0.00	0.77	0.92	1.02	0.70	0.89	1.06	0.65	0.46	1.41
1.78	0.00	0.00	0.00	0.78	0.92	1.06	0.71	0.89	1.10	0.66	0.55	1.43
1.82	0.00	0.00	0.00	0.79	0.92	1.11	0.72	0.90	1.14	0.67	0.62	1.44
1.86	0.00	0.00	0.00	0.80	0.92	1.15	0.72	0.90	1.17	0.68	0.69	1.46
1.90	0.00	0.00	0.00	0.81	0.92	1.20	0.73	0.91	1.21	0.69	0.75	1.48
1.94	0.00	0.00	0.00	0.82	0.92	1.25	0.74	0.91	1.25	0.70	0.80	1.50
1.99	0.00	0.00	0.00	0.83	0.92	1.30	0.75	0.92	1.29	0.71	0.84	1.52
2.03	0.00	0.00	0.00	0.84	0.91	1.35	0.76	0.92	1.34	0.73	0.87	1.54
2.07	0.00	0.00	0.00	0.85	0.91	1.40	0.76	0.93	1.38	0.74	0.90	1.57
2.11	0.00	0.00	0.00	0.87	0.91	1.46	0.77	0.93	1.43	0.76	0.92	1.60
2.15	0.00	0.00	0.00	0.88	0.91	1.51	0.78	0.93	1.47	0.78	0.93	1.63
2.19	0.00	0.00	0.00	0.89	0.90	1.57	0.79	0.94	1.52	0.79	0.94	1.67
2.23	0.00	0.00	0.00	0.90	0.90	1.64	0.80	0.94	1.57	0.81	0.95	1.71
2.28	0.00	0.00	0.00	0.91	0.90	1.70	0.80	0.94	1.62	0.83	0.95	1.75
2.32	0.00	0.00	0.00	0.92	0.90	1.76	0.81	0.94	1.68	0.85	0.95	1.80
2.36	0.00	0.00	0.00	0.93	0.89	1.83	0.82	0.95	1.73	0.87	0.94	1.85
2.40	0.00	0.00	0.00	0.94	0.89	1.90	0.83	0.95	1.79	0.89	0.93	1.90
2.44	0.00	0.00	0.00	0.95	0.89	1.97	0.84	0.95	1.85	0.91	0.93	1.96
2.48	0.00	0.00	0.00	0.97	0.89	2.05	0.85	0.95	1.91	0.93	0.92	2.02
2.52	0.00	0.00	0.00	0.98	0.88	2.12	0.86	0.95	1.97	0.95	0.90	2.09
2.57	0.00	0.00	0.00	0.99	0.88	2.20	0.87	0.95	2.03	0.98	0.89	2.16
2.61	0.00	0.00	0.00	1.00	0.88	2.28	0.87	0.95	2.09	1.00	0.88	2.24
2.63	0.00	0.00	0.00	0.00	0.00	0.00	0.88	0.95	2.13	0.00	0.00	0.00
2.65	0.00	0.00	0.00	0.00	0.00	0.00	0.88	0.96	2.17	0.00	0.00	0.00
2.67	0.00	0.00	0.00	0.00	0.00	0.00	0.89	0.96	2.20	0.00	0.00	0.00
2.70	0.00	0.00	0.00	0.00	0.00	0.00	0.89	0.96	2.24	0.00	0.00	0.00
2.72	0.00	0.00	0.00	0.00	0.00	0.00	0.90	0.96	2.28	0.00	0.00	0.00
2.74	0.00	0.00	0.00	0.00	0.00	0.00	0.90	0.96	2.32	0.00	0.00	0.00
2.76	0.00	0.00	0.00	0.00	0.00	0.00	0.91	0.96	2.35	0.00	0.00	0.00
2.79	0.00	0.00	0.00	0.00	0.00	0.00	0.91	0.96	2.39	0.00	0.00	0.00
2.81	0.00	0.00	0.00	0.00	0.00	0.00	0.92	0.96	2.43	0.00	0.00	0.00
2.83	0.00	0.00	0.00	0.00	0.00	0.00	0.92	0.96	2.47	0.00	0.00	0.00
2.85	0.00	0.00	0.00	0.00	0.00	0.00	0.93	0.96	2.51	0.00	0.00	0.00
2.87	0.00	0.00	0.00	0.00	0.00	0.00	0.93	0.96	2.56	0.00	0.00	0.00
2.90	0.00	0.00	0.00	0.00	0.00	0.00	0.94	0.96	2.60	0.00	0.00	0.00
2.92	0.00	0.00	0.00	0.00	0.00	0.00	0.94	0.96	2.64	0.00	0.00	0.00
2.94	0.00	0.00	0.00	0.00	0.00	0.00	0.95	0.96	2.68	0.00	0.00	0.00
2.96	0.00	0.00	0.00	0.00	0.00	0.00	0.95	0.96	2.73	0.00	0.00	0.00
2.99	0.00	0.00	0.00	0.00	0.00	0.00	0.96	0.96	2.77	0.00	0.00	0.00
3.01	0.00	0.00	0.00	0.00	0.00	0.00	0.96	0.96	2.82	0.00	0.00	0.00

Pumping Configurations												
q	0FSD-1VSD			0FSD-2VSD			0FSD-3VSD			1FSD-1VSD		
	α	ϑ_c	π_T	α	ϑ_c	π_T	α	ϑ_c	π_T	α	ϑ_c	π_T
3.03	0.00	0.00	0.00	0.00	0.00	0.00	0.97	0.96	2.86	0.00	0.00	0.00
3.05	0.00	0.00	0.00	0.00	0.00	0.00	0.97	0.96	2.91	0.00	0.00	0.00
3.07	0.00	0.00	0.00	0.00	0.00	0.00	0.98	0.96	2.95	0.00	0.00	0.00
3.10	0.00	0.00	0.00	0.00	0.00	0.00	0.98	0.96	3.00	0.00	0.00	0.00
3.12	0.00	0.00	0.00	0.00	0.00	0.00	0.99	0.96	3.05	0.00	0.00	0.00
3.14	0.00	0.00	0.00	0.00	0.00	0.00	0.99	0.96	3.10	0.00	0.00	0.00
3.16	0.00	0.00	0.00	0.00	0.00	0.00	1.00	0.96	3.15	0.00	0.00	0.00

Pumping Configurations									
Δq	1FSD-2VSD			0FSD-4VSD			2FSD-1VSD		
	α	ϑ_c	π_T	α	ϑ_c	π_T	α	ϑ_c	π_T
0.00	0.52	0.00	0.21	0.52	0.00	0.42	0.52	0.00	0.11
0.06	0.52	0.09	0.24	0.52	0.05	0.48	0.52	0.18	0.13
0.13	0.53	0.18	0.25	0.52	0.09	0.49	0.53	0.34	0.14
0.19	0.53	0.26	0.26	0.53	0.14	0.50	0.53	0.48	0.15
0.25	0.53	0.34	0.27	0.53	0.18	0.51	0.54	0.59	0.16
0.31	0.53	0.41	0.28	0.53	0.22	0.52	0.55	0.68	0.17
0.38	0.54	0.47	0.30	0.53	0.26	0.54	0.56	0.75	0.19
0.44	0.54	0.53	0.31	0.53	0.30	0.55	0.58	0.80	0.21
0.50	0.55	0.59	0.33	0.54	0.34	0.57	0.59	0.84	0.23
0.57	0.56	0.63	0.34	0.54	0.37	0.58	0.61	0.87	0.25
0.63	0.56	0.68	0.36	0.55	0.41	0.60	0.62	0.88	0.28
0.69	0.57	0.71	0.38	0.55	0.44	0.62	0.64	0.89	0.31
0.75	0.58	0.75	0.40	0.56	0.47	0.64	0.66	0.89	0.34
0.82	0.59	0.78	0.42	0.56	0.50	0.66	0.69	0.88	0.38
0.88	0.60	0.80	0.45	0.57	0.53	0.69	0.71	0.87	0.42
0.94	0.61	0.83	0.48	0.57	0.55	0.71	0.73	0.85	0.46
1.01	0.62	0.85	0.51	0.58	0.58	0.74	0.76	0.83	0.51
1.07	0.63	0.86	0.54	0.59	0.60	0.77	0.78	0.81	0.57
1.13	0.64	0.88	0.57	0.59	0.62	0.80	0.81	0.79	0.63
1.19	0.65	0.89	0.60	0.60	0.65	0.83	0.83	0.77	0.69
1.26	0.67	0.90	0.64	0.61	0.67	0.87	0.86	0.75	0.77
1.32	0.68	0.91	0.68	0.62	0.69	0.90	0.89	0.73	0.84
1.38	0.69	0.91	0.72	0.62	0.70	0.94	0.91	0.71	0.93
1.44	0.71	0.92	0.77	0.63	0.72	0.98	0.94	0.69	1.02
1.51	0.72	0.92	0.82	0.64	0.74	1.02	0.97	0.67	1.12
1.57	0.73	0.92	0.87	0.65	0.75	1.07	1.00	0.65	1.23
1.61	0.62	0.07	1.57	0.66	0.76	1.10	0.62	0.13	1.38
1.65	0.63	0.13	1.58	0.66	0.77	1.13	0.63	0.25	1.39
1.70	0.63	0.19	1.59	0.67	0.78	1.16	0.64	0.36	1.40
1.74	0.64	0.25	1.61	0.67	0.79	1.20	0.65	0.46	1.41
1.78	0.65	0.31	1.62	0.68	0.80	1.23	0.66	0.55	1.43
1.82	0.65	0.36	1.64	0.69	0.80	1.27	0.67	0.62	1.44
1.86	0.66	0.41	1.66	0.69	0.81	1.31	0.68	0.69	1.46
1.90	0.67	0.46	1.67	0.70	0.82	1.35	0.69	0.75	1.48
1.94	0.67	0.50	1.69	0.71	0.83	1.39	0.70	0.80	1.50

Δq	Pumping Configurations								
	1FSD-2VSD			0FSD-4VSD			2FSD-1VSD		
	α	ϑ_c	π_T	α	ϑ_c	π_T	α	ϑ_c	π_T
1.99	0.68	0.54	1.71	0.71	0.83	1.43	0.71	0.84	1.52
2.03	0.69	0.58	1.74	0.72	0.84	1.47	0.73	0.87	1.54
2.07	0.70	0.62	1.76	0.73	0.85	1.51	0.74	0.90	1.57
2.11	0.71	0.65	1.78	0.74	0.85	1.56	0.76	0.92	1.60
2.15	0.71	0.68	1.81	0.74	0.86	1.60	0.78	0.93	1.63
2.19	0.72	0.71	1.84	0.75	0.86	1.65	0.79	0.94	1.67
2.23	0.73	0.74	1.87	0.76	0.87	1.70	0.81	0.95	1.71
2.28	0.74	0.77	1.90	0.76	0.87	1.75	0.83	0.95	1.75
2.32	0.75	0.79	1.93	0.77	0.88	1.80	0.85	0.95	1.80
2.36	0.76	0.81	1.96	0.78	0.88	1.86	0.87	0.94	1.85
2.40	0.77	0.83	2.00	0.79	0.89	1.91	0.89	0.93	1.90
2.44	0.78	0.85	2.04	0.79	0.89	1.97	0.91	0.93	1.96
2.48	0.79	0.86	2.07	0.80	0.89	2.03	0.93	0.92	2.02
2.52	0.80	0.88	2.12	0.81	0.90	2.09	0.95	0.90	2.09
2.57	0.81	0.89	2.16	0.82	0.90	2.15	0.98	0.89	2.16
2.61	0.83	0.90	2.21	0.83	0.90	2.21	1.00	0.88	2.24
2.63	0.83	0.91	2.23	0.83	0.91	2.25	0.76	0.09	2.52
2.65	0.84	0.92	2.26	0.83	0.91	2.28	0.77	0.18	2.53
2.67	0.84	0.92	2.29	0.84	0.91	2.32	0.77	0.26	2.54
2.70	0.85	0.93	2.31	0.84	0.91	2.35	0.78	0.33	2.55
2.72	0.86	0.93	2.34	0.85	0.91	2.39	0.78	0.40	2.56
2.74	0.86	0.93	2.37	0.85	0.91	2.42	0.79	0.47	2.57
2.76	0.87	0.94	2.40	0.86	0.92	2.46	0.79	0.53	2.58
2.79	0.88	0.94	2.43	0.86	0.92	2.50	0.80	0.59	2.59
2.81	0.88	0.94	2.47	0.86	0.92	2.54	0.81	0.64	2.61
2.83	0.89	0.95	2.50	0.87	0.92	2.58	0.82	0.69	2.62
2.85	0.90	0.95	2.53	0.87	0.92	2.62	0.82	0.73	2.64
2.87	0.90	0.95	2.57	0.88	0.92	2.66	0.83	0.77	2.66
2.90	0.91	0.95	2.60	0.88	0.92	2.70	0.84	0.80	2.68
2.92	0.92	0.96	2.64	0.89	0.92	2.74	0.85	0.83	2.70
2.94	0.92	0.96	2.68	0.89	0.93	2.78	0.86	0.86	2.72
2.96	0.93	0.96	2.71	0.89	0.93	2.82	0.87	0.88	2.75
2.99	0.94	0.96	2.75	0.90	0.93	2.87	0.89	0.90	2.77
3.01	0.94	0.96	2.79	0.90	0.93	2.91	0.90	0.92	2.80
3.03	0.95	0.96	2.84	0.91	0.93	2.95	0.91	0.93	2.83
3.05	0.96	0.96	2.88	0.91	0.93	3.00	0.92	0.94	2.87
3.07	0.97	0.96	2.92	0.92	0.93	3.04	0.94	0.95	2.90
3.10	0.97	0.96	2.97	0.92	0.93	3.09	0.95	0.96	2.94
3.12	0.98	0.96	3.01	0.93	0.93	3.14	0.96	0.96	2.98
3.14	0.99	0.96	3.06	0.93	0.94	3.18	0.98	0.96	3.02
3.16	1.00	0.96	3.11	0.93	0.94	3.23	0.99	0.96	3.07

Table S3. Consumed Power of every pump model (E1 Network)

Q (l/s)	Model A			Model B			Model B		
	N_{FSD}	N_{VSD}	P_T (kw)	N_{FSD}	N_{VSD}	P_T (kw)	N_{FSD}	N_{VSD}	P_T (kw)
0.00	0	1	6.12	0	1	11.21	0	1	11.27
5.16	0	1	7.05	0	1	12.32	0	1	12.10
10.32	0	1	7.51	0	1	12.96	0	1	12.64
15.48	0	1	8.05	0	1	13.69	0	1	13.25
20.64	0	1	8.66	0	1	14.51	0	1	13.93
25.81	0	1	9.35	0	1	15.43	0	1	14.68
30.97	0	1	10.14	0	1	16.45	0	1	15.51
36.13	0	1	11.03	0	1	17.60	0	1	16.44
41.29	0	1	12.03	0	1	18.87	0	1	17.45
46.45	0	1	13.15	0	1	20.28	0	1	18.57
51.61	0	1	14.40	0	1	21.84	0	1	19.79
56.77	0	1	15.80	0	1	23.56	0	1	21.13
61.93	0	1	17.34	0	1	25.45	0	1	22.59
67.09	0	1	19.06	0	1	27.52	0	1	24.18
72.25	0	1	20.95	0	1	29.79	0	1	25.92
77.42	0	1	23.04	0	1	32.26	0	1	27.80
82.58	0	2	24.74	0	1	34.96	0	1	29.83
87.74	0	2	25.93	0	1	37.90	0	1	32.04
92.90	0	2	27.20	0	1	41.09	0	1	34.42
98.06	0	2	28.54	0	1	44.54	0	1	36.98
103.22	0	2	29.97	0	2	46.94	0	1	39.74
108.38	0	2	31.47	0	2	49.02	0	1	42.70
113.54	0	2	33.06	0	2	51.22	0	1	45.88
118.70	0	2	34.74	0	2	53.53	0	2	47.72
123.86	0	2	36.52	0	2	55.97	0	2	49.66
129.03	0	2	38.39	0	2	58.54	0	2	51.68
133.56	0	2	40.12	0	2	60.53	0	2	53.17
138.08	0	2	41.92	0	2	62.60	0	2	54.71
142.61	0	2	43.81	0	2	64.74	0	2	56.31
147.14	0	3	45.44	0	2	66.97	0	2	57.95
151.67	0	3	46.88	0	2	69.27	0	2	59.65
156.20	0	3	48.36	0	2	71.66	0	2	61.41
160.73	0	3	49.90	0	2	74.14	0	2	63.22
165.26	0	3	51.50	0	2	76.70	0	2	65.09
169.79	0	3	53.15	0	2	79.36	0	2	67.02
174.32	0	3	54.86	0	2	82.10	0	2	69.01
178.85	0	3	56.63	0	2	84.94	0	2	71.06
183.38	0	3	58.46	0	2	87.88	0	2	73.18
187.91	0	3	60.35	0	2	90.91	0	2	75.36
192.44	0	3	62.30	0	2	94.04	0	2	77.60
196.97	0	3	64.32	0	2	97.28	0	2	79.91
201.50	0	3	66.41	0	3	100.32	0	2	82.29
206.03	0	3	68.56	0	3	103.00	0	2	84.74
210.56	0	3	70.79	0	3	105.75	0	2	87.25
215.08	0	3	73.08	0	3	108.58	1	1	89.72

219.61	0	4	75.03	0	3	111.49	1	1	91.87
224.14	0	4	77.02	0	3	114.48	1	1	94.17
228.67	0	4	79.07	0	3	117.55	1	1	96.62
233.20	0	4	81.18	0	3	120.70	1	1	99.25
237.73	0	4	83.34	0	3	123.94	1	1	102.04
242.26	0	4	85.56	0	3	127.26	1	1	105.02
245.05	0	4	86.96	0	3	127.98	0	3	108.08
247.84	0	4	88.38	0	3	128.70	0	3	109.10
250.63	0	4	89.83	0	3	129.43	0	3	110.12
253.42	0	4	91.30	0	3	130.16	0	3	111.15
256.21	0	4	92.79	0	3	130.90	0	3	112.19
259.00	0	4	94.31	0	3	131.64	0	3	113.24
261.79	0	4	95.85	0	3	132.38	0	3	114.30
264.58	0	4	97.42	0	3	133.13	0	3	115.37
267.37	0	4	99.01	0	3	133.88	0	3	116.45
270.16	0	4	100.63	0	3	134.64	0	3	117.54
272.95	0	4	102.27	0	3	135.40	0	3	118.64
275.74	0	4	103.94	0	3	136.16	0	3	119.75
278.53	0	4	105.63	0	3	136.93	0	3	120.87
281.31	0	4	107.35	0	3	137.70	0	3	122.00
284.10	0	4	109.10	0	3	138.48	0	3	123.15
286.89	0	4	110.88	0	3	139.26	0	3	124.30
289.68	0	4	112.68	0	3	140.04	1	2	125.42
292.47	0	4	114.51	0	3	140.83	1	2	126.43
295.26	0	4	116.37	0	3	141.63	1	2	127.45
298.05	0	4	118.25	0	3	142.42	1	2	128.49
300.84	0	5	120.03	0	3	143.22	1	2	129.55
303.63	0	5	121.76	0	3	144.03	1	2	130.63
306.42	0	5	123.52	0	3	144.84	1	2	131.72
309.21	0	5	125.30	0	3	145.65	1	2	132.83
312.00	0	5	127.10	0	3	146.47	1	2	133.96



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