

1. Equation used in the RclimDex

CDD

It is the consutive number of days with precipitation amount i for j period of time, where $RR_{ij} < 1\text{mm}$

CWD

It is the consutive number of days with precipitation amount i for j period of time, where $RR_{ij} > 1\text{mm}$

PRCPOT

Let RR_{ij} is the daily precipitation amount i in j time period and I is the number of wet days during this time span, then

$PRCPOT_j =$

27. PRCPTOT

Let RR_{ij} be the daily precipitation amount on day i in period j . If I represents the number of days in j , then

$$PRCPOT = \sum_{i=1}^I RR_{ij}$$

R10mm

Suppose the RR_{ij} is the precipitation amount on day I in a specific period j . Then it is the total number of days in specific period of time with precipitation amount $RR_{ij} > 10\text{mm}$

R20mm

Suppose the RR_{ij} is the precipitation amount on day I in a specific period j . Then it is the total number of days in specific period of time with precipitation amount $RR_{ij} > 20\text{mm}$

R25mm

Suppose the RR_{ij} is the precipitation amount on day I in a specific period j . Then it is the total number of days in specific period of time with precipitation amount $RR_{ij} > 25\text{mm}$

R95p

Suppose the RR_{ij} is the precipitation amount on wet day i ($RR > 1\text{mm}$) in a specific period j and $R95p$ is the 95th percentile of wet days during 1961-2014.

$$R95p = \sum_{i=1}^j RR_{ij} \text{ where } RR_{ij} > RR_{95^{\text{th}} \text{ percentile}}$$

R99p

Suppose the RR_{ij} is the precipitation amount on wet day i ($RR > 1\text{mm}$) in a specific period j and $R95p$ is the 99th percentile of wet days during 1961-2014.

$$R95p = \sum_{i=1}^j RR_{ij} \text{ where } RR_{ij} > \text{RR 99th percentile}$$

RX1day

Suppose the RR_{ij} is the precipitation amount on day i in a specific period j . Then it is the maximum precipitation amount in specific period of time $Rx1day = \max(RR_{ij})$.

RX5day

Suppose the RR_{ij} is the precipitation amount for five day interval ending with i in a specific period j . Then it is the maximum value for precipitation amount in specific period of time $Rx5day = \max(RR_{ij})$.

SDII

Suppose the RR_{ij} is the wet days precipitation amount ($RR \geq 1\text{mm}$) in a specific period j . And if I represents the count of wet days in j , then

$$SDII_j = \frac{\sum_{i=1}^j RR_{ij}}{I}$$

2. Autocorrelation test

The autocorrelation test has been employed to remove the correlation effects in the data. For the sample data (x_1, x_2, \dots, x_n) used in this study, the following steps were followed;

- i. Salas et al (1980) applied lag-1 serial coefficient on data to eliminate the effect of correlation from the data as presented in Equation (S1)

$$r_1 = \frac{\frac{1}{n-1} \sum_{i=1}^{n-1} (x_i - E(x_i))(x_{i+1} - E(x_{i+1}))}{\frac{1}{n} \sum_{i=1}^n (x_i - E(x_i))^2} \quad (S1)$$

$$E(x_i) = \frac{1}{n} \sum_{i=1}^n x_i \quad (S2)$$

Where the number of observation and mean of the data are represented by n and $E(x_i)$, respectively.

- ii. For testing the time series Equation (S3) was applied at the time series

$$\frac{-1 - 1.645\sqrt{(n-2)}}{n-1} \leq r_1 \leq \frac{-1 + 1.645\sqrt{(n-2)}}{n-1} \quad (S3)$$

For independent data sets the r_1 value must be between the above mentioned intervals otherwise it is correlated if the value is not within the said intervals. The pre-whitening test must be applied to eliminate the effects of correlation as described below

$$(x_2 - r_1 x_1, x_3 - r_1 x_2, \dots, x_n - r_1 x_{n-1})$$

3. Mann-Kendall Trend Test

The most used non parametric approach for trend analysis named as Mann-Kendall trend test is used to analyse the time-series data in this study.

The 'S' statistic of the Mann-Kendall test can be obtained by applying the Equation (S4),

$$S = \sum_{i=1}^{n-1} \sum_{j=i+1}^n \text{sgn}(x_j - x_i) \quad (\text{S4})$$

where x_i and x_j are yearly values for i and j years, respectively, with $j > i$, n represents the number of data points and $\text{sgn}(x_j - x_i)$ is the sign function.

The variance of Mann Kendall can be computed as

$$V(S) = \frac{n(n-1)(2n+5) - \sum_{k=1}^m t_k(t_k-1)(2k+5)}{18} \quad (\text{S5})$$

where n represents the number of data points; whilst number of tied groups can be represented by m with the ties of extent k . A data group with the same values represents the tied group. The test statistics is computed using the below Equation (S6) for a sample size with $n > 10$.

$$Z_s = \begin{cases} \frac{s-1}{\sqrt{V(S)}} & \text{if } S > 0 \\ 0 & \text{if } S = 0 \\ \frac{s+1}{\sqrt{V(S)}} & \text{if } S < 0 \end{cases} \quad (\text{S6})$$

Positive/negative values of Z_s represents the increasing/decreasing trend. The null hypothesis (H_0) is rejected if $Z_s > Z_{1-\alpha/2}$, where the values of $Z_{1-\alpha/2}$ is achieved from a standard normal cumulative distribution table. The presented MK test is generally used to identify the significance of the data at 99.99% and/or 99% confidence interval of time series data for $|Z_s| > 2.57$ and $|Z_s| > 1.96$, respectively, with the H_0 of no trend is rejected.

4. Theil-Sen approach (TSA)

Sen (1968) presented the non-parametric approach to estimate the trends slope for N pairs of the data samples. Equally distributed time series should be arranged in ascending order and the below given formula applied to compute the trend slope.

$$Q_k = \frac{(x_j - x_i)}{j - i}, \text{ for } k=1 \dots N \quad (\text{S7})$$

where x_i and x_j are data points of time series i and j , respectively, with $(j > i)$. The $N = \frac{n(n-1)}{2}$ values of Q slopes are computed if there are n values of x_i are presents in the time series. All N values are arranged in ascending order to obtain the Sen's slope estimator, that is the median of these N values, with the help of Equation (S8)

$$Q_{med} = \begin{cases} Q_{(N+1)/2} & \text{if } N \text{ is odd} \\ \frac{Q_{N/2} + Q_{N/2+1}}{2} & \text{if } N \text{ is even} \end{cases} \quad (\text{S8})$$

The steepness of the slope is obtained from the magnitude of Q_{med} while its positive/negative sign represents the direction of increasing / decreasing trend.