



Probabilistic Model for Real-Time Flood Operation of a Dam Based on a Deterministic Optimization Model

Víctor Cuevas-Velásquez ¹,*^D, Alvaro Sordo-Ward ²^D, Jaime H. García-Palacios ²^D, Paola Bianucci ² and Luis Garrote ²^D

- ¹ Civil Engineering Department, Universidad Andres Bello, Santiago 8370106, Chile
- ² Civil Engineering Department: Hydraulics, Energy and Environment, Universidad Politécnica de Madrid, ES28040 Madrid, Spain; alvaro.sordo.ward@upm.es (A.S.-W.); jaime.garcia.palacios@upm.es (J.H.G.-P.); paola.bianucci@upm.es (P.B.); l.garrote@upm.es (L.G.)
- * Correspondence: victor.cuevas@unab.cl

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Abstract: This paper presents a real-time flood control model for dams with gate-controlled spillways that brings together the advantages of an optimization model based on mixed integer linear programming (MILP) and a case-based learning scheme using Bayesian Networks (BNets). A BNet model was designed to reproduce the causal relationship between inflows, outflows and reservoir storage. The model was trained with synthetic events generated with the use of the MILP model. The BNet model produces a probabilistic description of recommended dam outflows over a time horizon of 1 to 5 h for the Talave reservoir in Spain. The results of implementing the BNet recommendation were compared against the results obtained while applying two conventional models: the MILP model, which assumes full knowledge of the inflow hydrograph, and the Volumetric Evaluation Method (VEM), a method widely used in Spain that works in real-time, but without any knowledge of future inflows. In order to compare the results of the three methods, the global risk index (I_r) was computed for each method, based on the simulated behavior for an ensemble of hydrograph inflows. The I_r values associated to the 2 h-forecast BNet model are lower than those obtained for VEM, which suggests improvement over standard practice. In conclusion, the BNet arises as a suitable and efficient model to support dam operators for the decision making process during flood events.

Keywords: real-time reservoir operation; Bayesian networks; reservoir flood control; gate-controlled spillways; mixed integer linear programming (MILP); Monte Carlo simulation framework

1. Introduction

Floods can cause enormous economic damage and human suffering, thence, vulnerable areas require control measures to reduce the impacts [1,2]. In regulated basins, reservoirs play an essential role in mitigating the effects of floods [3–6]. However, the potential conflicts between flood control and the regular operation in multipurpose reservoirs imply a great challenge in the operation decisions [5,7–9]. During floods, dam operators often make decisions based on imperfect and incomplete information (for example, data provided by a limited number of sensors) and, in a partial knowledge of the hydrological response of the contributing basin [10]. In addition, there is still huge uncertainty regarding the proper operation of a reservoir for real-time flood control, that increases the risk in the discharge decision-making process [11,12].

The management of reservoirs for flood control in real-time has been historically addressed through curves derived from predefined rules obtained by means of simulation techniques [8], or by using programmed management methods, such as Volumetric Evaluation Method (VEM) [13], widely used



in Spain. These methods, reactive in nature, have been included in the reservoir regulation rules and help the operators to manage the dam [6]. Other approaches to real-time flood control in reservoirs are based on risk and uncertainty analysis, leaving decision-makers to choose the model to use according to different emergency scenarios and the initial water level of the reservoir [14], or, in the determination of relationships between double-peak floods, reservoir storage capacity and discharge capacity [15]. Currently, advances in optimization and learning techniques have allowed a new approach to the treatment of the problem of reservoir management in real-time, incorporating the uncertainty caused by the stochastic nature of the inflow hydrographs to the reservoir [16]. There is a wide variety of programs and models regarding the forecast of the inflow hydrographs and the optimization of the

dam operation, each with its strengths and weaknesses [17].

The hydrologic dam safety is based on minimizing the risk and consequences of both, the dam infrastructure and downstream discharges [6,18]. In recent decades the use of optimization techniques has attracted the attention of many researchers to develop optimal reservoir operation policies [17,19–21] and taking into account different objectives simultaneously [7,12]. These techniques were mainly based on: Linear Programming (LP), Mixed Integer Linear Programming (MILP), Non-Linear Programming (NLP), Successive Linear Programming (SLP), Dynamic Stochastic Programming (SDP), Genetic Algorithms (GA), Genetic Programming (GP), Optimization of Swarm Particle (PSO), Honey-Bee Crossing (HBM), and Artificial Bee Colony (ABC), as well as hybrid models that combine the previous ones. A detailed description of these techniques is presented by Choong and El-Shafie [17]. Among these methods of optimization, the Mixed Integer Linear Programming (MILP) is widely used. It allows to combine real, integer and binary variables [21,22]. The MILP model has the advantage of simplicity and flexibility [23,24], the guarantee that the solution corresponds to the global optimum [12] and its efficiency in solving reservoir optimization problems [24-26]. It is fairly easy to adapt the model formulation to different cases by adjusting the model parameters [21,24,27,28], to obtain good results [21,29,30]. However, its main disadvantage is that all relations involved (objective functions and constraints) are required to be linear or linearizable. Although the robustness of MILP models, solving them for very large systems may be computationally more expensive than other optimization models (e.g., NLP).

In most cases, the lack of complete and sufficiently long records of precipitation and gauging increases the uncertainty in the estimation of extreme floods [2,31], which, added to a lack of precise flood forecasting techniques, makes it difficult to determine optimal operation of reservoirs [18,32]. Although reservoir management optimization models allow simultaneous reduction of released flows and appropriate storage allocation during floods, their applicability for real-time management is limited by the forecast accuracy. Indeed, for their correct operation, most of these models are coupled to flood forecasting models in order to increase the known length of the hydrograph entering the reservoir [33–35]. If stochastic modeling techniques are additionally considered to quantify the uncertainty about future inputs to the reservoir, the optimization models become excessively complex. This fact limited the practical usefulness of these techniques [36,37]. On the other hand, deterministic optimization models cannot quantify the uncertainty in the parameters of the model or future flows. As an alternative, learning algorithms are characterized by their fundamental ability to deduce behavioral models of a system from measured information, showing in general, good accuracy and a moderate formulation [38].

Bayesian inference stands out among learning techniques. In this approach, uncertainties are expressed in terms of probability distributions [16,36].

Some interesting applications of Bayesian Networks (BNets) include the definition of the optimal shape of double-arch dams, associated with the decrease in the use of concrete [39], the search for the optimal geometric parameters (area and volume) for double-arch dams based on static and dynamic internal stresses [40].

Recent research in the field of hydrology has used BNets to identify the driving factors of flood loss at residential buildings and gaining insight into their relations [41], to develop dynamic predictive

models for annual runoff temporal behavior of high dependence rivers [42], to assess temporally conditioned annual runoff fractions in unregulated rivers [43], to quantify the forecast uncertainty by a model for ensemble flood forecasting [2], to perform the dynamic assessment of flood in urban underground spaces [44], to develop a self-adaptive real-time correction model to reduce uncertainties in flood forecasting [45], and to estimate uncertainty in catchment modelling parameter values and uncertainty in design flow estimates [46].

Regarding real-time flood control reservoir operation, BNets have been built as decision support tools, including, for example, the probabilistic modeling of the behavior of a reservoir to control flash floods [36], the development of monthly operating rules for a cascade reservoir system with the objective of controlling floods and supply irrigation needs [47], the analysis of the risk of a single reservoir dam overtopping and two reservoirs collapsing under the combined action of flood and landslide surge [48], the risk analysis for real-time flood control operation of a multi-reservoir system using a dynamic BNet [49] and the risk analysis of reservoir flood control considering the uncertainty of the inflow to a reservoir and the initial level of the reservoir [50].

All these studies have in common the use of Monte Carlo techniques to simulate the hydrological series that are later used for the training of BNets.

On the other hand, the models used to operate the reservoirs include VEM programmed management model [36], models of predefined operating rules specific to each dam [48,49,51] and an optimization model that minimizes the maximum discharge flow [50].

The MILP model may consider, simultaneously, both objectives: dam safety and downstream protection, during each synthetic flood event generated with Monte Carlo techniques.

In this study, a probabilistic real-time reservoir operation model for flood control was developed, which integrates the advantages of a deterministic reservoir optimization model (MILP) and overcomes its limitations derived from the requirement of full knowledge of the inflow hydrograph. The proposed model is built using a case-based learning scheme (BNets) from an ensemble of synthetic events simulated with the MILP model.

2. Materials and Methods

2.1. The Real-Time Reservoir Operation Problem Approach

The real-time flood control optimization approach was addressed by coupling a MILP model with a BNet model. Additionally, an ensemble of synthetic hydrographs for model training was generated.

The applicability of the MILP model for real-time reservoir operation is limited, because it requires full knowledge of the inflow hydrograph. This limitation is overcome by using the output series produced by the MILP model to train a data-based learning model. The model thus built can be used in real-time to produce management recommendations based on the optimizations, but using only the available information. This approach may lead to a more efficient implementation and easier interpretation compared with other real-time operation frameworks. Formulating the real-time model using a BNet scheme was chosen because it can capture the complex causal relationships among variables during training, but its operation is easy and it can assist the decision-maker in the rapid assessment of the situation [36].

2.2. Formulation of a BNet

A BNet is a specific type of graphical model, composed of nodes and directed links, called a directed acyclic graph (DAG) [52]. The nodes represent the model variables and the links the conditional dependency relationships. In general, knowing the values of the nodes $X = X_1, ..., X_n$, the joint probability function for any BNet [53] is:

$$P(X) = \prod_{i=1}^{n} P(X_i | parents(X_i)),$$
(1)

where, X_i is the i_{th} qualitative value of variable X, P(X) is the joint probability of all of the variables, represented by the product of the probabilities of each variable X_i given its parent's value: $parents(X_i)$. This shows the meaning of the links: they indicate which other variables a given variable is conditioned upon. The links in a BNet are sometimes looked at as causal connections where each parent node causes an effect on its children [53]. For example, if variable F depends on E and variable G depends on E and F, the joint probability would be:

$$P(E, F, G) = P(E) \times P(F|E) \times P(G|E, F),$$
(2)

Inference is the task of computing the probability of each value of a node in a BNet when other values of the variables are known. There are different algorithms for doing inference in a BNet. The learning of a BNet is divided in two types: the learning of the structure and the learning of the parameters (probability distributions). The learning method depends on the knowledge of the structure and the degree of observability of the parameters. The structure can be defined thanks to expert knowledge, but if it is unknown, two tasks must be performed: a metric to compare possible structures and a search algorithm to find potential structures. The cause–effect logical refers to the relationship between the variable represented by parent node (cause) and the variable represented by child node (effect). In the case of parametric learning in a BNet with partial observability, the expectation-maximization (EM) algorithm is used [54].

2.3. Case Study

The proposed methodology was applied to the Talave Dam, located in the Mundo River (southern Spain) and belonging to the Segura River Basin (Figure 1). The mean annual rainfall in the basin is 557 mm and the maximum annual flood was 600 m^3 /s (year 1996).



Figure 1. Location of Talave dam in the Segura River Basin.

Table 1 shows the characteristic levels of the Talave reservoir and the associated volumes.

Table 1. Talave Dam characteristics.	Levels and	l storage capacity.
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Symbol	Description	Water Level (m)	Volume (hm ³)	
TCP	Top of conservation pool (maximum normal operative level)	508.9	31.9	
FCL	Flood control level (top of flood control pool)	509.9	34.8	
DFL	Design flood level	511.3	39.1	
TOP	Top of dam	512.4	42.5	

Analogously, Table 2 presents several characteristic flows related to the downstream river reach capacity.

Symbol	Description	Flow (m ³ /s)
AO	Alert outflow (maximum downstream channel capacity)	100
WO	Warning outflow (mild damage flow)	150
EO	Emergency outflow (moderate damage flow)	300

Table 2. Downstream river characteristic capacity (flows).

The Talave dam is equipped with the following outlets:

- Gated spillway located on the left side, with a threshold level 505.9 m and provided with two bays six meters each. The discharge capacity at DFL (fully open) is 284.9 m³/s.
- Fixed crest spillway (emergency spillway), located on the right side of dam, being the threshold level 510 m. The length of the spillway crest is 13.5 m and the discharge capacity is 41 m³/s.
- Bottom outlet with its axe at 475.8 m. The outlet discharge capacity at DFL is 99.55 m³/s.
- Former intake consists in two conduits at 494.6 m, with a discharge capacity at DFL up to 18 m³/s.
- Newest intake (also two conduits) at 476.12 m, having a discharge capacity of 123 m³/s at DFL.

2.4. Stochastic Generation of Hydrological Forcing

The Monte Carlo simulation technique was used, which is described below, to generate a large number of synthetic episodes that will serve to train the BNet. The inflow flood events were estimated by applying a semi-distributed event-based hydro-meteorological model that modeled the main physical processes from the rainfall generation to the estimation of the inflow floods [55,56]. In order to obtain a set of stochastic rainfall events, a sample of 1000 uniform distributed values corresponding to the probability of exceedance (*p*) were generated. Being the return period Rp = 1/p, the annual maximum daily precipitation was calculated according to the probability distribution function SQRT-ETmax [55,57,58]. The total precipitated volume (*Pt*) for a duration *D* was estimated by applying the intensity-duration-frequency (IDF) curves proposed by the Ministry of Public Works of Spain [59] and recommended by the Spanish Committee of Large Dams [60]. In order to estimate the temporal distribution of each storm event, it was assumed that the episodes generated were random and not correlated. The temporal distribution of each episode was estimated with an autoregressive moving average model (ARMA(2,2)). The model and its orders (*p* and *q*) were selected based on an analysis of rainfall data available for Spain (source: Automatic Hydrological Information System; SAIH) and results found in the literature [61–64].

Many time-series techniques used to model water resources series are based on ARMA linear stochastic processes [62].

A model of this type is denoted by ARMA(p,q) and, it is composed of two parts: AR(p) (autoregressive component) and MA(q) (moving average component), where *p* and *q* are parameters that identify the order of each part. The autoregressive part describes the time series of *p* previous data and the moving average part describes the current and *q* previous values of white noise.

$$x_{t} = \phi_{1} \times (x_{t-1} - \mu_{x}) + \phi_{2} \times (x_{t-2} - \mu_{x}) + \dots + \phi_{p} \times (x_{t-p} - \mu_{x}) + \eta_{t} + \theta_{1} \times \eta_{t-1} + \theta_{2} \times \eta_{t-2} + \dots + \theta_{q} \times \eta_{t-q} + \mu_{x}$$
(3)

where x_t is the time series; η_t is white noise, i.e., a non-correlated, zero-mean random variable that is also not correlated with the past values of x_t ; $\phi_1 \dots \phi_p$ and $\theta_1 \dots \theta_q$ are the auto-regressive and moving-average parameters, respectively; and μ_x is the mean of the time series.

The ARMA(2,2) process was chosen because it has a correlation structure equivalent to the Neyman-Scott rectangular pulses model [62], which has been proved to represent the stochastic structure of rainfall better [65]. Furthermore, the ARMA(2,2) model structure has been used in previous studies to disaggregate daily precipitation, generating synthetic hyetographs, in specific studies of the Segura river basin [21,55,56].

The ARMA(2,2) model parameters were adjusted for 32 rainfall episodes recorded in the basin in the period March 2009 to February 2013, obtaining: $\phi_1 = 0.12$, $\phi_2 = 0.16$, $\theta_1 = 0.33$, $\theta_2 = 0.11$.

The rainfall-runoff transformation was estimated by applying the curve number method [66]. Subsequently, the hydrographs was generated by applying the dimensionless unit hydrograph method of the Soil Conservation Service [66]. 42% of single peak hydrographs, 48% double peak, 9% triple peak and 1% quadruple peak were generated. Muskingum method was used to estimate the routing of the hydrographs [67]. A detailed description of the methodology to generate the flood events was presented in Sordo-Ward et al. [55,56].

The lower *Rp* events can be regulated in the dam by gate operations, however, for higher *Rp* events the gates become fully opened and the operation rules of the gates decreases in importance for regulation purposes. The Monte Carlo simulation process should generate a sufficient number of cases to cover a wide range of combinations of values that can be expected during the operation of the BNet model [36]. Synthetic episodes were generated for three reasons: (1) to train the BNet, (2) to evaluate the learning process of the BNet and (3) to verify the performance of the BNet. In order to train the BNet 30,000 episodes were generated, to evaluate the learning process 20,000 episodes were generated and, to verify its performance, 2000 episodes were generated. Altogether, 52,000 synthetic episodes were generated.

The number of episodes for the various tasks (training, evaluation, and performance verification) was selected based on the stability of the conditional entropy of the BNet [68].

The conditional entropy quantifies the average degree of dispersion of the variable *X* when the state of the variable *Y* is known, and is given by the expression:

$$H(X|Y) = -\sum_{i=1}^{m} p(y_i) \times \left[\sum_{j=1}^{n} p(x_j|y_i) \times \log[p(x_j|y_i)]\right],\tag{4}$$

where H(X|Y) is the conditional entropy, $X = x_1, ..., x_n$ represents the set of values of the child node of the BNet and the variable $Y = y_1, ..., y_m$ is the set of values of the parent nodes of the BNet.

The 50,000 episodes used to train and evaluate the BNet were plotted to determine the number of episodes for which the conditional entropy stabilizes (Figure 2).



Figure 2. Evolution of the conditional entropy for the 50,000 episodes used in the training and evaluation of the BNet.

The conditional entropy stabilizes, approximately, at the value 0.125, for the first 30,000 episodes, remaining relatively constant until reaching 50,000 episodes. For this reason, 30,000 episodes were chosen to train the BNet and the remaining 20,000 to evaluate it.

The conditional entropy of the 2000 episodes used in the performance verification is 0.124, very close to the stable value of the conditional entropy for the set of 50,000 episodes. For this reason, 2000 episodes were considered an adequate number to verify the performance of the BNet. Hyetographs of uniformly distributed duration were considered, with values between 10 and 80 h. This range of values is characteristic of the Segura river basin [69]. The Talave reservoir basin was divided into three homogeneous sub-basins. The semi-distributed hydrological model was calibrated based on 32 hourly rainfall events recorded simultaneously in four rain gauges of the Segura basin and Guadalquivir basin and in the azud de Liétor gauging station, located 8.2 km upstream from the Talave reservoir, in the period March-2009 to February-2013. This hydrological model was used to generate the 52,000 hourly flow hydrographs from the 52,000 previously generated synthetic rainfall hyetographs.

2.5. Optimal Reservoir Management

In order to obtain the optimal reservoir response to hydrographs entering the reservoir, the MILP model proposed by Bianucci et al. [21] was used. The main concepts are briefly presented here. This model transforms (as input signal) the input flood hydrograph into two output time series corresponding to the output hydrograph and the evolution of levels in the reservoir.

The MILP optimization model minimizes a cost or penalty function (*P*) subject to operational and hydraulic constraints. The objective function, *P*, is the weighted sum of two penalty terms (Equation (5)), one corresponding to the reservoir volumes (*PS*) and the other corresponding to the discharged flows (*PO*).

$$\min P = \min(ws \times PS + wo \times PO), \tag{5}$$

where *ws* and *wo* are the corresponding weights. These penalty terms are related to the dam safety and the downstream safety, respectively.

As mentioned, all the relationships must be linear. Consequently, partial penalty functions (*PS* and *PO*) and constraints functions were defined as piecewise linear functions and binary variables were included. Complementarily, these functions were parameterized to represent a specific case study. The main advantage of applying the MILP model is that, for each flood, an optimum solution (minimum penalty) is achieved, representing an envelope situation which is not possible to reach using simulation methods based on traditional reactive operation rules (defined by if-then-else statements). Nevertheless, the main drawback of using the MILP model for real-time operation is its dependency on the flood forecast quality as it requires knowing, beforehand, the flood hydrograph for an efficient optimization. Using MILP, the hydrographs of discharged flow and the series of evolution of volumes in the reservoir were obtained, from the 52,000 episodes generated in the previous section. The volume series was transformed into level series using the storage-level curve of the reservoir. For simulation purpose, the initial level was fixed at the maximum normal operation level (TCP), which is the maximum level that is reached during normal operation of the reservoir (before the flood). This assumption is commonly used in dam design [70,71].

2.6. Construction and Evaluation of a BNet

During a flood, the basic variables involved to characterize the routing process in the Talave reservoir are: inflow to the reservoir, reservoir water level, and outflow from the reservoir. The variables were defined considering their possible cause–effect relationships, and adding the time lag factor between them, with expert knowledge (Table 3).

With these variables and their dependency relationships, the BNet structure was built (Figure 3).

Although the structure of the BNet is unique, the child node O_{t+i} is different depending on the forecast time step. For this reason, to refer to a specific forecast interval of the BNet, the notation was used: BNet_i, where i can take one or more values from 1 to 5 h. Before training the BNet, the variables (or nodes) were discretized in class intervals within the range of values of the synthetic episodes. Later, the subset of 30,000 synthetic episodes generated according to the procedure indicated in the previous

sections was used, to train the BNet, obtaining the Conditional Probability Tables (CPTs) for each node. The trained BNet allow the probabilistic inference of the flow discharged by the reservoir in a forecast time t + i, where *i* varies between 1 and 5 h.

Symbol	Description
It	Inflow to the reservoir at time <i>t</i> hour
I_{t-1}	Inflow to the reservoir at time $t - 1$ h
WL_t	Reservoir water level at time <i>t</i> hour
WL_{t-1}	Reservoir water level at time $t - 1$ h
O_t	Outflow from the reservoir at time <i>t</i> hour
ΔI_t	Variation of the inflow to the reservoir between the time t and $t - 1$ h
ΔWL_t	Variation of the reservoir water level between the time t and $t - 1$ h
O_{t+i}	Outflow from the reservoir at forecast time $t + i$ hour, where i is the forecast time step



Figure 3. BNet structure that forecast the discharge flow of the reservoir at time t + i hours, where i = 1 to 5 h.

In order to evaluate the learning process of the BNet, the attributes of forecast quality, ability, and precision were estimated, with the subset of 20,000 synthetic episodes generated according to the procedure indicated in the previous sections. Table 4 shows the values of the area under the Relative Operating Characteristic (ROC) curve [72], which quantifies the ability, and the Ranked Probability Score (RPS) index [73], which quantifies the precision.

Table 4. Values of the parameter that quantify the forecast quality of the BNet, in a time step from 1 to 5 h.

Demonstra			BNet		
Parameter	i = 1 h	<i>i</i> = 2 h	<i>i</i> = 3 h	i = 4 h	<i>i</i> = 5 h
ROC area RPS index	0.973 0.006	0.966 0.009	0.961 0.012	0.958 0.014	0.956 0.017

The area under the ROC curve of the BNet has values close to 1 that decrease slightly as the forecast interval increases. This means that the BNet ability is close to the maximum possible. The RPS index of the BNet has values close to 0, which increase slightly as the forecast time step is greater. This means that the forecast of the BNet is almost perfect with respect to this attribute.

2.7. BNet Application Strategy

Considering that a BNet returns the probability distribution of values over the class interval of the child node, O_{t+i} can take any value within the class interval. A procedure to select a single value of the flow discharged at each instant of time was developed to facilitate the work of the operator of the dam. It was observed that most of the discharge hydrographs resulting from the application of the MILP method have a plateau shape. In the first hours, the flows discharged are very similar to the inflows in the reservoir, therefore, the level of the reservoir remains practically constant. From a certain point, the outflow decreases with respect to the inflow and the level of the reservoir begins to rise.

This point, located in the ascending branch of the input hydrograph, corresponds to the instant in which the slope ratio between two consecutive time intervals ($k_t = S_t/S_{t-1}$) takes a value less or equal than 1, where S_t is the slope of the input hydrograph at time t. This threshold flow must be identified (TF_j) in all the ascending branches of the input hydrograph, where subscript j represents the last ascending branch up to the current moment (Figure 4).



Figure 4. Slope ratio (k_t) of the input hydrograph to the reservoir between two consecutive time intervals.

Figure 5 shows an example of the input hydrograph zoning to select the discharge flow. Each zone has a single criterion for selecting the discharge flow. If the input hydrograph has more than one peak value, for each ascending branch, there will be a different threshold flow, TF_{j} .



Figure 5. Zoning based on the input hydrograph to the reservoir of a single criterion for selecting the flow discharged in each zone, according to Figure 6 and the following steps:

- If $I_t I_{t-1} \ge 0$, that is, if the input flow is maintained or is increasing.
 - \land If $I_t > \max(I_1, \dots, I_{t-1})$, that is, if a maximum of the input hydrograph has not been reached.
 - □ If $I_t \leq TF_j$, that is, if the input flow is less than the threshold value number *j* [Zone 1].

$$O_{t+i} = I_t, (6)$$

□ If $I_t > TF_j$, that is, if the input flow is greater than the threshold value number *j* [Zone 2].

$$O_{t+i} = \min(I_t, Oav),\tag{7}$$

- ♦ If $I_t \le \max(I_1, ..., I_{t-1})$, that is, if a maximum of the input flow has been reached.
 - □ If $I_t \leq Imr_k$, that is, if the inflow to the reservoir is less than or equal to the largest peak of the registered inflow [Zone 4].

$$O_{t+i} = \min\Big(Imr_k, \max(I_t, Oav)\Big),\tag{8}$$

- □ If $I_t > Imr_k$, that is, if the inlet flow is greater than the highest recorded inlet flow peak.
 - If $I_t \leq TF_j$, that is, if the input flow is less than the threshold value number j [Zone 1].

$$O_{t+i} = I_t, \tag{9}$$

• If $I_t > TF_j$, that is, if the input flow is greater than the threshold value number j [Zone 2].

$$O_{t+i} = \min(I_t, Oav), \tag{10}$$

• If $I_t - I_{t-1} < 0$, that is, if the input flow is decreasing [Zone 3].

$$O_{t+i} = \min\Bigl(\max(I_1, \dots, I_{t-1}), Oav\Bigr),\tag{11}$$

where:

 O_{t+i} : Ouput or discharged flow in the instant t + i, where *i* is the forecast time interval.

*I*_{*t*}: Input flow in the instant *t*.

 TF_j : Threshold flow that corresponds to the value of the input flow when a variation less than 1 is reached in the slope of the input hydrograph, where *j* is the sub-index of the threshold flow recorded up to the current moment.

Imr_k: Higher flow peak of the input hydrograph, registered up to the current analysis time *t*, where *k* is the sub-index of the peak value recorded up to the current moment.

Oav: Average flow of the forecast probability distribution given by the BNet of flow discharged.

2.8. VEM

In order to compare the results of the BNet model, the VEM [13], a method usually used in Spain, was used. VEM is a reactive-type scheduled management method that works in real-time. At each time step, it calculates the discharge flow based on available surcharge pool volume. This method is based on three fundamental principles: (1) While the inflow is increasing, the discharge flow must be less than the inflow to the reservoir, (2) If the inflow to the reservoir increases, the discharge flow must increase as a function of the previous one, (3) The higher the reservoir level, the greater the percentage increase in the discharge flow relative to the inflow.

At each time step, the method calculates the number of time intervals (*n*) remaining for the available surcharge pool volume (S_t^a) to run out. The volume variation in the reservoir in a time interval Δt (ΔS_t) is equal to the difference between the inflow at *t* (I_t) and the discharge flow at *t* – 1 (O_{t-1}). If it is considered that the rate of increase in discharged flow is linear, *n* is:

$$n = \frac{S_t^a}{\Delta S_t} = \frac{S_t^a}{(I_t - O_{t-1}) \cdot \Delta t},\tag{12}$$

If a linear increase in the discharge flow is maintained until the surcharge pool volume is exhausted at time $\Delta t \cdot n$, at which point the discharge flow equals the inflow, the discharge flow must increase the following amount in each time interval Δt :

$$\Delta O_t = \frac{(I_t - O_{t-1})^2 \cdot \Delta t}{S_t^a},\tag{13}$$

The application of the MEV considers 2 parameters: the maximum gradient of discharge flow (MGD) and the activation level (ACT). The MGD is intended to limit damage downstream from the reservoir. In this case, it was assumed equal to the AO. The ACT is an arbitrary value (assumed as 509.3 m [74]), which defines a time interval for the application of the VEM, depending on the zone where the reservoir level is located. If the level is below the TCP, the VEM is applied every 4 h, if it is between the TCP and the ACT level, every 2 h and, if it is above the ACT level, every 1 h.

2.9. Overall Risk Index (I_r)

In order to evaluate the results of the various peak attenuation methods used (VEM, MILP, and BNet), the I_r index [21] was calculated. I_r is the sum of the risk of damage indexes due to the discharge flow, I_0 , and the risk of damage index due to the storage volume, I_S . I_0 is the expected value of damage downstream of the dam, in the areas adjacent to the main water course. I_S is the expected value of damage due to overflow on the dam. For each peak attenuation method, the maximum values of discharge flow, O_{max} , and storage volume, S_{max} , were extracted for each of the N episodes analyzed. Subsequently, the empirical probability of non-exceedance of O_{max} and S_{max} , $F(O_{max})$ and $F(S_{max})$, respectively, was obtained using the Gringorten expression.

 I_0 was calculated using the following expression:

$$I_0 = \sum_{i=1}^{N-1} [F(O_{max,i+1}) - F(O_{max,i})] \cdot D_O\left(\frac{O_{max,i+1} + O_{max,i}}{2}\right),\tag{14}$$

where *N* is the number of episodes, $O_{max,i}$ is the maximum discharged flow in episode *i*, $F(O_{max,i})$, is the empirical probability of non-exceedance of $O_{max,i}$, and D_O , is the damage associated with the maximum discharged flow obtained from the damage curve (Figure 6).

Similarly, I_S was calculated using the following expression:

$$I_{S} = \sum_{i=1}^{N-1} [F(S_{max,i+1}) - F(S_{max,i})] \cdot D_{S} \left(\frac{S_{max,i+1} + S_{max,i}}{2}\right),$$
(15)

where *N* is the number of episodes, $S_{max,i}$, is the maximum volume reached by the reservoir in episode *i*, $F(S_{max,i})$, is the empirical probability of non-exceedance of $S_{max,i}$, and D_S , is the damage associated with the maximum volume reached by the reservoir of the damage curve (Figure 7).

The damage curves of the Talave reservoir as proposed by Bianucci et al. [21] were obtained (Figure 7).



Figure 6. Scheme of the selection procedure of the forecast discharge flow according to the zoning of the input hydrograph.



Figure 7. Damage curves due to (a) discharge flow and (b) storage volume of the Talave reservoir [21].

3. Results and Discussion

Performance of the BNet

In order to evaluate model performance, the BNet model is compared to two standard models for dam flood operation: the Volumetric Evaluation Model (VEM) and the Mixed Integer Linear Programming (MILP) model. The application of VEM model is the standard practice in many dams in Spain. VEM is a reactive model, which is solely based on the evolution of reservoir level and operates without knowledge of the inflow hydrograph. The results of the VEM model set the baseline for comparison: any proposed model should at least improve the performance of the standard practice. MILP, on the other hand, is taken as the upper limit of model performance. MILP produces a mathematical optimization of dam management, but requires full knowledge of the inflow hydrograph, which is a very unrealistic situation. The results of MILP were used to train the BNet model and thus it can be expected that the performance of the BNet model be lower than that of MILP. The two extreme cases provide a reference to evaluate how BNet can improve over VEM and how far below it is from MILP.

For this purpose, 2000 synthetic hydrographs that enter in the reservoir were generated, as indicated in Section 2.4. The hydrographs were used as inputs to the BNet_i (i = 1, ..., 5 h), VEM and MILP models, obtaining, in each case, 2000 time series of reservoir discharge hydrographs and evolution of levels in the reservoir.

When VEM is applied in real-time, the discharge flow and reservoir level are obtained, at each time step of 1 h, during the flood, until reaching TCP level. By applying MILP, a hydrograph of discharge flows and the time series of levels in the reservoir were obtained for each previously known flood. In the case of the BNet, 5 sets of predicted reservoir discharge hydrographs and evolution of levels in the reservoir were obtained, one set for each forecast time interval from 1 to 5 h (Figure 3).

The general procedure to use the BNet requires a brief explanation: First, the BNet_i (i = 1, ..., 5 h) was chosen, which, at each instant of time, forecast a discharge flow O_{t+i} (the procedure proposed in Section 2.7 was used, in order to obtain a single predicted discharge flow value at time t + i). Then, this value was kept until instant t + i - 1 was reached, where it becomes the parent node O_t . In each time interval the variables I_{t-1} and I_t (parent nodes) are known. With these values the variable $\Delta I_t = I_t - I_{t-1}$ (parent node) was calculated. At each time step the variable WL_t (parent node) was calculated using the modified Puls method [75], and, with this value, and WL_{t-1} , the variable $\Delta WL_t = WL_t - WL_{t-1}$ (parent node) was obtained. Figure 8 shows an example of a real-time BNet_i application for i = 3 h.



Figure 8. Real-time application of the BNet_{*i*} (i = 3 h).

Applying the BNet_i (i = 3 h) in real time, 2000 synthetic episodes were obtained.

In order to compare the results of the methods, the maximum values of each one of the time series were extracted, corresponding to the maximum discharge flow and the maximum level reached by the reservoir. Subsequently, the differences of the maximum discharge (ΔO_{max}) and the maximum level reached by the reservoir (ΔWL_{max}) between the BNet_i (i = 1, ..., 5 h) and both, the MILP and VEM comparison methods were calculated. With these results the graphs of Figure 9 and Table 5 were created. On the horizontal axis ΔWL_{max} was plotted and on the vertical axis ΔO_{max} was plotted.

The objective of this analysis was to know how many episodes resulted in lower O_{max} and WL_{max} when using the BNet_i (*i* = 1, ..., 5 h) than when using VEM and MILP methods.

 ΔWL_{max} and ΔO_{max} values can be positive or negative.

If $\Delta O_{max} > 0$, the O_{max} values of the BNet_i are greater than those of the comparison method (MILP or VEM), therefore, the BNet_i generates a smaller peak attenuation. If $\Delta O_{max} < 0$, the opposite happens.

If $\Delta WL_{max} > 0$, the WL_{max} values of the BNet_i are greater than those of the comparison method (MILP or VEM). If $\Delta WL_{max} < 0$, the opposite happens.

The ΔO_{max} and $\Delta W L_{max}$ values can be combined as follows:

If $\Delta O_{max} > 0$ and $\Delta WL_{max} > 0$, the O_{max} and WL_{max} values of an episode that result with the BNet_i are greater than the values obtained from the standard method (VEM or MILP). In this case, the episode analyzed falls into quadrant I of Figure 9.

If $\Delta O_{max} > 0$ and $\Delta W L_{max} < 0$, the analyzed episode belongs to quadrant II of Figure 9.

If $\Delta O_{max} < 0$ and $\Delta W L_{max} < 0$, the analyzed episode belongs to quadrant III of Figure 9.

If $\Delta O_{max} < 0$ and $\Delta W L_{max} > 0$, the analyzed episode belongs to quadrant IV of Figure 9.

Figure 9a (i = 1 h) shows that in 39% of the events, the results of maximum discharge and maximum level reached by the reservoir, when using the BNet_i (i = 1 h), are simultaneously lower than those obtained using the VEM, meanwhile, only 1% are larger. In 57% of the episodes, the maximum flows discharged using the BNet_i (i = 1 h) are greater than those obtained using the VEM, while the maximum levels are lower. In 3% of the episodes, the maximum levels reached using the BNet_i (i = 1 h) are greater than those obtained using the BNet_i (i = 1 h) are greater than those obtained using the BNet_i (i = 1 h) are greater than those obtained using the BNet_i (i = 1 h) are greater than those obtained using the VEM, while the maximum discharges are lower.

Table 5 and Figure 9a show that when comparing the BNet (for 5 forecast time steps) with the VEM, as the BNet forecast time increases, the number of episodes decrease in quadrant III, increase in quadrant II, decrease in quadrant II, and increase in quadrant IV. The decrease in the number of episodes in quadrant III means that O_{max} and WL_{max} calculated with the BNet are increasingly greater than those calculated with VEM. The increase in the number of episodes in quadrant I means that the O_{max} and WL_{max} calculated with the BNet are increasingly greater than those calculated with the BNet are increasingly greater than those calculated with the BNet are increasingly greater than those calculated with the BNet are increasingly greater than those calculated with the BNet are increasingly greater than those calculated with the BNet are increasingly greater than those calculated with the BNet are increasingly greater than those calculated with the BNet are increasingly greater than those calculated with the BNet are increasingly lower than those calculated with the VEM. The increase in the number of episodes in quadrant IV means that the maximum levels calculated with the BNet are increasingly higher than those calculated with the VEM.

Figure 9a shows that in the first three forecast time intervals, i = 1, 2, and 3 h, BNet results are better than VEM, since there are more episodes in quadrant III than in quadrant I. On the contrary, in the forecast time intervals, i = 4 and 5 h, VEM results are better than BNet, since there are more episodes in quadrant I than in quadrant III.

Figure 9b (i = 1 h) shows that 2% of the events of the BNet simultaneously returns lower values of maximum discharge and maximum level than the MILP. On the contrary, in 6% of the cases, the MILP returns higher results of the comparison variables than the BNet. In 90% of the cases, the BNet returns higher values of maximum flow discharged and lower maximum levels, than the MILP. Finally, in 3% of the episodes, the BNet returns lower values of maximum flow discharged and higher levels than the MILP.

Figure 9b shows that in all forecast time intervals, MILP returns better results than VEM.

This result is explained by the fact that the set of values of both the MILP and the VEM methods, which are used to compare with the BNet, is always the same, regardless of the forecast time step. For each episode, both MILP and VEM return a single hydrograph and a single time series of evolution

of levels in the reservoir, from which the maximum values of discharge flow and level reached are extracted, which are then used to compare with the BNet. In the case of MILP, this is possible because the hydrographs entering the reservoir are known before applying this method. On the other hand, the BNet decreases the forecast quality as the forecast time step increases (see Table 4). Given that MILP provides the optimal results with which the BNet is trained, it is expected that its results will be better than the BNet. The BNet, relative to VEM, is always at a "disadvantage", since the predicted future results of the BNet are compared with the results of the VEM, which is unable to forecast. Even so, better results are obtained with the BNet than with the VEM up to i = 3 h, and worse, from i = 4 h.



Figure 9. Comparison of the BNet results for each forecast time step (i = 1 to 5 h) with the Volumetric Evaluation Method (VEM) (**a**) and mixed integer linear programming (MILP) (**b**) for 2000 synthetic episodes of flood.

Table 5. Percentage of episodes classified by quadrants when comparing ΔO_{max} and $\Delta W L_{max}$ between the BNet, from *i* = 1 h to 5 h, and the VEM and MILP methods.

BNet:	<i>i</i> = 1 h		<i>i</i> = 2 h		<i>i</i> = 3 h		<i>i</i> = 4 h		<i>i</i> = 5 h	
Quadrant	VEM	MILP								
Ι	1%	5%	6%	23%	15%	50%	28%	69%	37%	80%
II	57%	90%	53%	73%	50%	48%	43%	30%	38%	19%
III	39%	2%	31%	1%	19%	0%	12%	0%	7%	0%
IV	3%	3%	10%	3%	16%	2%	17%	1%	18%	1%

For the episodes outside of quadrant III, it was analyzed how far the results obtained with the BNet_i (i = 1, ..., 5 h) are from those generated with the VEM. For this, a graph of the probability of non-exceedance of the maximum differences ΔO_{max} and ΔWL_{max} , was created, in each BNet_i (i = 1, ..., 5 h) of the episodes that belong to quadrants I, II, and IV (Figure 10).

Figure 10 shows the percentages of episodes found in quadrants I, II, and IV for different thresholds. The greater the number of episodes under small thresholds, the greater the similarities between the results of both methods (VEM and BNet). In quadrant II, it should be highlighted the difference in maximum discharge (ΔO_{max}), and in quadrant IV the maximum level difference (ΔWL_{max}). In quadrant I it is important to highlight the thresholds corresponding to the difference in maximum discharge (ΔO_{max}) and to the difference in the maximum level reached by the reservoir (ΔWL_{max}).

Figure 10 (i = 1 h) shows that in quadrant II(c), with a probability of non-exceedance of 0.9, the differences in ΔO_{max} do not exceed 21.3 m³/s, which is only the 13% percentile of the O_{max} resulting from the VEM and the BNet_i (i = 1 h). In quadrant IV(d), with a probability of non-exceedance of 0.9, the ΔWL_{max} do not exceed 0.42 m, which is the 36% percentile of the WL_{max} reached by the reservoir resulting from the VEM and the BNet_i (i = 1 h). In quadrant I, which concentrates the results in which the VEM behaves better than the BNet_i (i = 1 h), with a probability of non-exceedance of 0.9, ΔO_{max} (a)

do not exceed 15 m³/s, which is only the 9% percentile, and ΔWL_{max} (b) do not exceed 0.43 m, which is at the 37% percentile.

In quadrant I(a), as the BNet forecast time advances, for the same probability of non-exceedance, ΔO_{max} increases, that is, the value of O_{max} calculated with the BNet increases its difference with respect to the value calculated with the VEM. In quadrant I(b), as the BNet forecast time advances, for the same probability of non-exceedance, ΔWL_{max} increases, that is, the value of WL_{max} calculated with the BNet increases its difference with respect to the value calculated with the VEM. In quadrant II(c), there is no significant difference between the non-exceedance probability curves as the BNet forecast time progresses. In quadrant IV(d), there is also no significant difference between the non-exceedance probability curves as the BNet forecast time progresses.



Figure 10. Probability of non-exceedance of the differences in maximum discharged flows (ΔO_{max}) and the maximum levels reached by the reservoir (ΔWL_{max}), between the VEM and the BNet_i (i = 1, ..., 5 h), in quadrants I, II, and IV.

An analysis of the variables O_{max} and WL_{max} was also performed separately, plotting their probabilities of non-exceedance in each of the forecast time intervals (from i = 1 to 5 h) by applying the BNet, VEM, and MILP methods. Figure 11a shows that the probability of non-exceedance of the O_{max} calculated with the BNet_i (i = 1, ..., 5 h) is lower than that calculated with the VEM and the MILP, up to the AO. Above EO, the probability of non-exceedance of the O_{max} calculated with the BNet is lower than the probabilities of non-exceedance of the VEM and the MILP. Between AO and EO, the values of probability of non-exceedance of the O_{max} calculated with the BNet is lower and MILP values, with a tendency to match the VEM as the BNet forecast interval increases.

Figure 11b shows that as the BNet forecast time increases, the probability of non-exceedance of the WL_{max} tends to decrease. For the BNet_i (*i* = 1 h), the probability of non-exceedance of the WL_{max} is greater than that calculated with the MILP and VEM methods.



Figure 11. Probabilities of non-exceedance of: (**a**) maximum discharge flows (O_{max}) and (**b**) maximum levels (WL_{max}), obtained with the VEM, MILP, and BNet_i (i = 1, ..., 5 h).

In order to compare the BNet results with the VEM, from the point of view of risk reduction, the global risk index (I_r) [21] was calculated, which simultaneously quantifies the overflow risk of the dam (I_S) and the flood risk downstream of the dam (I_O), such as, $I_r = I_S + I_O$ (Table 6).

Symbol	Description	MILP	VEM	BNet				
				<i>i</i> = 1 h	<i>i</i> = 2 h	<i>i</i> = 3 h	<i>i</i> = 4 h	<i>i</i> = 5 h
I _O	release flow risk index	0.247	0.380	0.337	0.345	0.373	0.391	0.406
I_S	storage risk index	0.137	0.171	0.108	0.188	0.280	0.444	0.600
Ir	overall risk index	0.383	0.551	0.445	0.533	0.653	0.834	1.006

Table 6. Talave reservoir risk index (M€). MILP, VEM, and BNet methods.

Table 6 shows that the downstream flood risk (I_O) calculated with the BNet_i (i = 1, ..., 3 h) that forecast the discharged flow from 1 h to 3 h, was lower than the risk of VEM. Likewise, the overflow risk (I_S) obtained with the BNet_i (i = 1 h) that forecast the discharged flow in 1 h, was lower than the risk of VEM. Finally, the overall risk (I_r) calculated with the BNet_i (i = 1 and 2 h) that forecast the discharged flow in an interval of 1 h and 2 h, was lower than the VEM overall risk.

VEM is a reactive method for managing reservoirs in floods that makes a single discharge decision at each instant of time depending on the state of the reservoir. This method works in real-time, but does not forecast. For the 2000 synthetic reservoir input hydrographs, VEM returned a single set of 2000 combinations of maximum discharge flows and maximum levels reached by the reservoir, with which I_r was calculated.

MILP is a method that optimizes the management of the reservoir in floods that requires knowing the entire hydrograph that enters the reservoir before being applied, therefore, its use in real-time is very limited. For the 2000 synthetic reservoir input hydrographs, MILP returned a single set of 2000 combinations of maximum discharge flows and maximum levels reached by the reservoir, with which I_r was calculated.

The BNet was applied for the 2000 synthetic hydrographs entering the reservoir, for 5 forecast time steps (see Figure 8), obtaining, for each forecast time step, a different set of 2000 combinations of maximum discharge flows and maximum levels reached by the reservoir. I_r was calculated for each of the 5 data sets.

The BNet was trained with the results of the MILP, so it is expected that the results of the BNet are worse than those of the MILP, which is consistent with the value of the I_r calculated (Table 6).

On the other hand, the forecast quality of the BNet decreases as the forecast time step increases (Table 4), so I_r increases with the forecast time step. For the first 2 forecast time steps, the I_r of the BNet

is less than the I_r of the VEM (which is unique), but, from the 3-h forecast time step, I_r of theBNet_{*i*} (*i* = 3, ..., 5 h) exceeds that of the VEM. These results are explained because the BNet predicts and VEM does not, so the BNet always compares at a "disadvantage".

In a practical case of real-time application, the BNet could be used to forecast the flow discharged by the dam in all time horizons, from 1 to 5 h, obtaining 5 probable values of future discharge flows, one for each forecast time step, values that the VEM is unable to estimate.

4. Conclusions

The proposed methodology is useful to build a decision-support system for dam operation during floods based on the Bayesian model. The analyses performed showed that the Bayesian model can improve the performance of the VEM model, which is the method of choice for real time operation in many dams in Spain. More sophisticated optimization models, like MILP, cannot be easily applied in real time because they require full knowledge of the inflow hydrograph. These models, however, can be used to produce a large dataset of optimal dam operations that can be used to train the BNet. The Bayesian model can thus be used in real time without the need for a hydrograph forecast module.

The developed BNet model predicts the flow discharged through the reservoir outlets during floods over a time horizon of 1 to 5 h. This model adapted the MILP model that optimizes the management of the reservoir, but it cannot be easily used in real-time. In order to evaluate the learning process of the BNet its quality attributes were calculated: area under the ROC curve and RPS index. The area under the ROC curve varied between 0.973, for 1 h of forecast, and 0.956, for 5 h, values close to 1 that show the ability of the BNet. The RPS index varied between 0.006 and 0.017, for 1 h of forecast and 5 h, respectively, values close to 0, which indicate that the BNet returns good results with respect to this attribute. The values of both attributes show that the BNet learning process was satisfactory.

Since the BNet returns the most probable class interval of the predicted discharge flow, a selection method of a single forecast value at each instant of time was proposed, in order to facilitate the use of the BNet by the dam operator.

The BNet model was compared with the MILP method, which cannot be easily applied in real-time, and with the VEM, which works in real-time, but does not forecast. The values of maximum discharge flow and maximum level reached by the reservoir, calculated by each method, were extracted. Based on these values, the overall risk index (I_r) was estimated, obtaining 0.383 M€ for MILP, which is the lower limit, and 0.551 M€ for VEM. The BNet returned an I_r value of 0.445 M€ for 1 h forecast, 0.533 M€ for 2 h, 0.653 M€ for 3 h, 0.834 M€ for 4 h, and 1.006 M€ for 5 h. Therefore, it was concluded that the BNet presented better results than the VEM, which does not predict, even for BNet forecast time steps of up to 2 h. Finally, this model improves the results from one of the most used methods in Spain, the VEM, and could represent and improvement to the actual dam operation methods.

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