

Article

A Multiple-Iterated Dual Control Model for Groundwater Exploitation and Water Level Based on the Optimal Allocation Model of Water Resources

Junqiu Liu ^{1,2} , Xinmin Xie ^{1,3,*}, Zhenzhen Ma ^{1,3}, Guohua Fang ², Huaxiang He ^{1,4} and Mingyue Du ⁵

¹ Department of Water Resources, China Institute of Water Resources and Hydropower Research, Beijing 100038, China; ljqlrh1986@163.com (J.L.); mazz@iwhr.com (Z.M.); he6680145@sina.com (H.H.)

² College of Hydrology and Water Resources, Hohai University, Nanjing 210098, China; hhufanggh@163.com

³ State Key Laboratory of Simulation and Regulation of Water Cycle in River Basin, China Institute of Water Resources and Hydropower Research, Beijing 100038, China

⁴ Department of Hydraulic Engineering, Tsinghua University, Beijing 100084, China

⁵ Changchun Institute of Urban Planning and Design, Changchun 130000, China; mingyuedudu@126.com

* Correspondence: xiexm@iwhr.com; Tel.: +86-10-6878-5708

Received: 18 January 2018; Accepted: 29 March 2018; Published: 5 April 2018



Abstract: In order to mitigate environmental and ecological impacts resulting from groundwater overexploitation, we developed a multiple-iterated dual control model consisting of four modules for groundwater exploitation and water level. First, a water resources allocation model integrating calculation module of groundwater allowable withdrawal was built to predict future groundwater recharge and discharge. Then, the results were input into groundwater numerical model to simulate water levels. Groundwater exploitation was continuously optimized using the critical groundwater level as the feedback, and a groundwater multiple-iterated technique was applied to the feedback process. The proposed model was successfully applied to a typical region in Shenyang in northeast China. Results showed the groundwater numerical model was verified in simulating water levels, with a mean absolute error of 0.44 m, an average relative error of 1.33%, and a root-mean-square error of 0.46 m. The groundwater exploitation reduced from 290.33 million m³ to 116.76 million m³ and the average water level recovered from 34.27 m to 34.72 m in planning year. Finally, we proposed the strategies for water resources management in which the water levels should be controlled within the critical groundwater level. The developed model provides a promising approach for water resources allocation and sustainable groundwater management, especially for those regions with overexploited groundwater.

Keywords: groundwater numerical model; multiple-iterated; optimal allocation of water resources; dual control; groundwater exploitation and water level; critical groundwater level

1. Introduction

Groundwater is being overexploited in many regions of the world due to increasing demand for water resources brought about by rapid economic development and population growth [1,2]. It causes a variety of problems such as drawdown of groundwater levels, drying up of aquifers [3], increase in the groundwater cones of depression [4], and land subsidence [5]. Intensive irrigation can lead to the development of salinity problems, and the extraordinary rise of piezometric surface in aquifers may induce groundwater inundation [6], resulting in several damage processes such as building foundation destabilization, groundwater infiltration and pollutant remobilization [7]. Thus, considerable attempts have been made to control groundwater exploitation and water level [8].

In China, the State Council stipulated the implementation of controlled groundwater exploitation in those groundwater overexploited regions [9].

Many models have been developed to optimize groundwater exploitation and address the impact of groundwater overexploitation. Commonly used methods for groundwater simulation include finite difference method, finite element method, boundary element method and finite volume method. Mehl and Hill [10] proposed a new method of local grid refinement for two-dimensional block-centered finite-difference meshes in the context of steady-state groundwater flow modeling. Wang et al. [11] proposed a groundwater flow domain decomposition model coupling the boundary and finite element methods. However, Anderson and Woessner [12] pointed out the accuracy and reliability of groundwater numerical models depended critically not only on the simulation method but also on the properly generalized conceptual hydrogeological model. Recent decades have also witnessed significant progress in the development of groundwater simulation software based on the conceptual hydrogeological model, such as the groundwater simulation modeling system (GMS) [13], modular three-dimensional finite difference groundwater flow model (MODFLOW) [14], finite element groundwater flow modeling software (FEMWATER) [15], and finite element subsurface flow system (FEFLOW) [16]. These models have achieved remarkable success in investigating groundwater levels [17], groundwater mass balance [18], salt transport in coastal aquifers [19,20], groundwater quantity balance [21], impact of predicted climate changes on groundwater flow systems [22], sustainable groundwater management [23,24], and groundwater irrigation [25]. However, given the “natural-artificial” dualistic characteristics of the water cycle system [26], water resources allocation can have significant impacts on the groundwater recharge and discharge, resulting in significant changes in groundwater exploitation and consequently changes in water level. Thus, groundwater numerical models coupled with optimal allocation of water resources can provide a more effective way to simulate groundwater in complex regions.

Artificial fish swarm algorithm [27], multi-objective optimization [28–30], interval-parameter multi-stage stochastic programming model [31], ant colony optimization [32], support vector machines and genetic algorithms [33] have often been used in coupling groundwater-surface water models. These models make it possible for the dynamic allocation of water resources in different regions in reference year [34]. Lu et al. [35] showed that the coupling of water resources allocation models and groundwater numerical models reduced the allowable and overexploitable quantity of groundwater for quantifying the groundwater allowable withdrawal accurately in planning years.

Groundwater level can be indicative of groundwater quantity and underflow, and thus, it is an important index in groundwater management. Knowledge of spatial and temporal changes in groundwater levels following the optimal allocation of water resources is essential to better understand the stability of groundwater environment [36]. Jang et al. [37] quantified the recovery of groundwater levels in townships when groundwater for drinking and agricultural demands was replaced by surface water based on the groundwater-surface water coupled model. In order to more accurately control the groundwater level in the canal-well irrigation district, Su et al. [38] simulated the spatiotemporal groundwater depth in planning year using the optimal allocation model of water resources coupled with the groundwater numerical model. Stefania et al. [39] modeled groundwater/surface-water interactions in an Alpine valley (the Aosta Plain, NW Italy) to investigate the effects of groundwater abstraction on surface-water resources.

In summery, previous studies have focused mainly on the modification of numerical modeling and groundwater exploitation calculation [40–42], while changes in future groundwater levels were seldom considered. Thus, this study aims to consider changes in future groundwater levels, as well as changes in groundwater exploitation in water resources allocation. A water resources allocation model is constructed to predict future groundwater recharge and discharge, and the results are input into the groundwater numerical model to forecast changes in water levels. The established groundwater numerical model will be adopted to feedback the allocation results. Groundwater exploitation and water level are quantified by using multiple-iterated technique to achieve dual

control. Also, groundwater allowable withdrawal and critical groundwater level are used as feedback factors to optimize the model. However, changes of groundwater exploitation and water level will affect the natural equilibrium state of groundwater system and environment. Thus, the proposed multiple-iterated dual control model makes contributions to hydrogeology.

The groundwater over-exploited region in Shenyang of northeast China is selected as the study area. The main purposes of this study are to (1) evaluate the performance of groundwater numerical model in simulating water level and calculate the critical groundwater level; (2) simulate spatial and temporal changes in groundwater levels and propose a scheme for sustainable groundwater management; (3) investigate spatial and temporal changes in groundwater levels under different precipitation conditions in the future; and (4) evaluate the performance of the multiple-iterated dual control model in controlling groundwater exploitation and water level.

2. Study Area and Methods

2.1. Study Area

The groundwater over-exploited region in Shenyang, the capital city of Liaoning Province in northeastern China, is selected as the study area (geographical coordinates, $41^{\circ}11'51''$ – $43^{\circ}02'13''$ N and $122^{\circ}25'09''$ – $123^{\circ}48'24''$ E, see Figure 1). It is a plain area administratively divided into Urban District, Shenbei New District, Sujiatun District, Hunnan New District, Yuhong District and Development Zone with a total area of 2318 km². There are a total of 36 municipal water sources in the study area, as shown in Figure 1, which are the main source of groundwater.

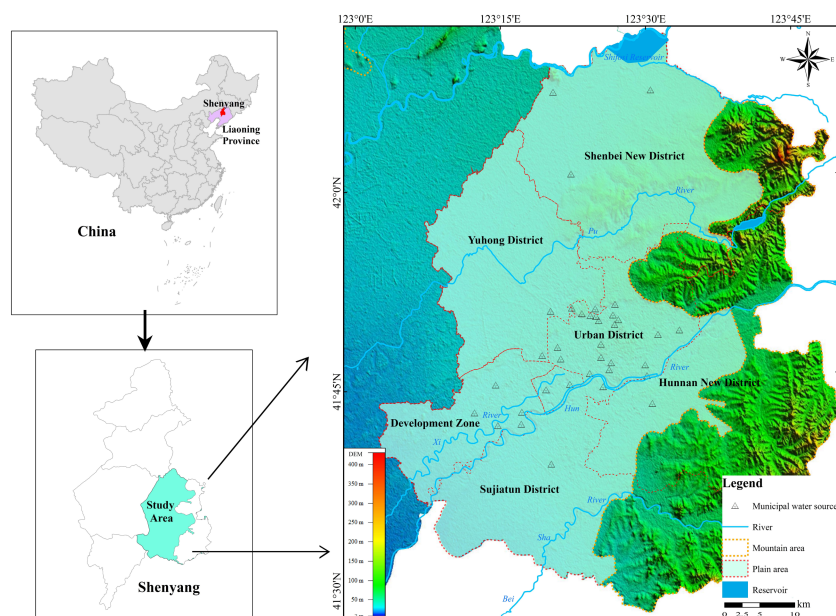


Figure 1. Geographical location of the study area and distribution of municipal water sources.

Figure 2a shows changes in groundwater exploitation and average water level in the study area over the period 2004–2013. Clearly, groundwater exploitation increases from 2005 to 2007 and then decreases from 2007 to 2009. However, it is noted that groundwater exploitation increases again to a maximum of 403.01 million m³ in 2010. Groundwater level decreases to a minimum of 31.07 m in 2010, after which it increases continuously. Two water transfer projects (Dahuofang and Liaoxibei) were constructed in 2011, and the government of Liaoning Province had taken measures to close many groundwater sources to stop decline of water level due to groundwater overexploitation. Now the transferred water are used instead of groundwater since 2012.

Figure 2b shows spatial distribution of groundwater level and location of monitoring wells in 2013. The spatial distribution of groundwater level is plotted based on the monitored groundwater level by the 114 monitoring wells. Due to the influence of topography, groundwater level is generally high in the northeast but low in the southwest. It is important to note that despite the decrease in groundwater exploitation quantity, groundwater overexploitation remains a serious problem in 2013, resulting in the formation of three cones of depression with a maximum groundwater depth of 20.77 m.

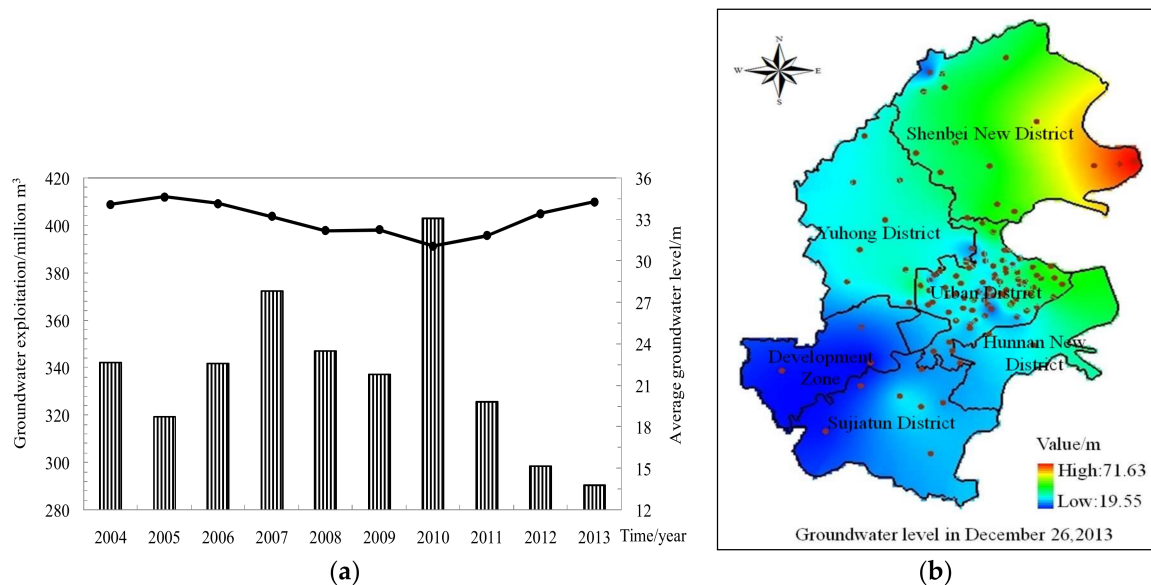


Figure 2. (a) Changes in groundwater exploitation and average water level in 2004–2013; (b) Spatial distribution of groundwater level and location of monitoring wells in 2013.

2.2. Research Framework and Simulation Model

Figure 3 shows the multiple-iterated dual control model for groundwater exploitation and water level, which consists of the following four modules, including optimal allocation module of water resources, groundwater allowable withdrawal calculation module, groundwater simulation module, and groundwater level control module. This study focuses mainly on the dual control for groundwater exploitation and water level and the interactions of the four modules, so the procedures for development of water resources allocation model can be referred to Zhou [43]. The details are provided in the Appendix A.

The model focuses on the coupling of water resources allocation and groundwater numerical simulation. The surface water supply and groundwater exploitation are coupled in the water resources allocation model to calculate field infiltration and well irrigation regression recharge of the groundwater numerical model. Water supply, demand and deficit are analyzed by different water demand schemes, and the rational allocation of water resources is put forward. The future groundwater level can be predicted by data extraction and interaction, and dual control for groundwater exploitation and water level can be achieved based on groundwater allowable withdrawal and critical groundwater level.

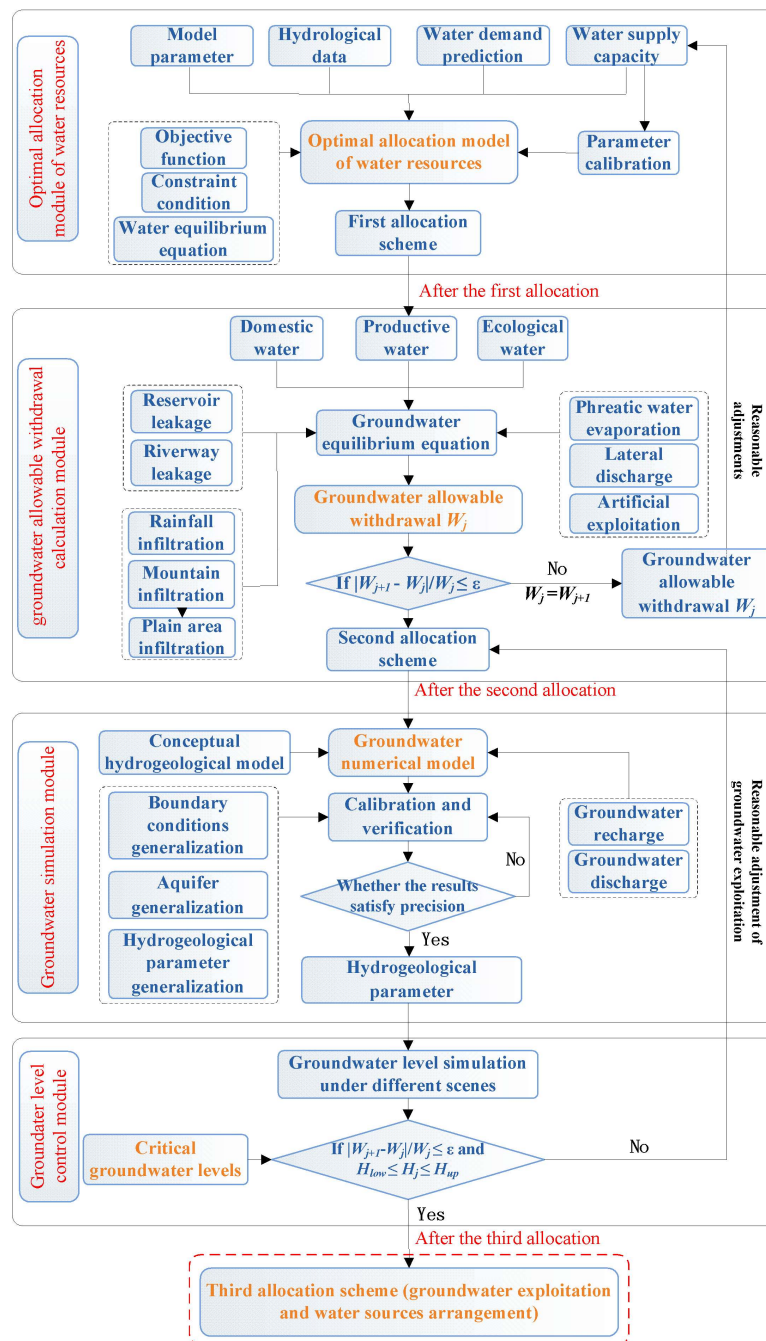


Figure 3. Study framework for multiple-iterated dual control model for groundwater exploitation and water level.

2.2.1. Optimal Allocation Module of Water Resources

The optimal allocation model of water resources consists of a number of objective functions, constraints and water balance equations. In the model long-time series hydrological and economic data and ecological water requirements in different years serve as the inputs. The calculation unit is based on the geographical locations of water resources and administrative regions. The constraints are the water balance constraints, and the objective is to maximize the net benefit of water supply and minimize water loss. The model is solved by the mathematical planning. In this study, the General Algebraic Modeling System (GAMS 2.5) [44] is used to establish and solve the model.

(1) Objective function

The objective is to maximize the net benefit, minimize water loss, and ensure the precedence of water sources for water supply, as described in Equation (1).

$$\max(\min)Z = \{f_1(\bar{x}), f_2(\bar{x}), \dots, f_n(\bar{x})\}^T, \bar{x} \in S \quad (1)$$

where \bar{x} is the vector composed of decision variables; S is the feasible set of decision variables composed of different constraints; and $f_n(\bar{x})$ is the objective for the development of society and economy, ecological environment and water resources.

(2) Constraints and water balance equations

The constraints and water balance equations are described in Wei et al. [45]. The groundwater supply constraints and balance equations in the calculation unit are shown in Equation (2).

$$XZGC_{tm}^j + XZGI_{tm}^j + XZGE_{tm}^j + XZGA_{tm}^j + XZGR_{tm}^j \leq PZGTU^j PZGW_{tm}^j \quad \forall tm, j \quad (2)$$

where $XZGC$, $XZGI$, $XZGE$, $XZGA$, and $XZGR$ are the groundwater supply for urban domestic use, industrial use, urban ecological use, agricultural use, and rural domestic use (million m^3), respectively; $PZGTU$ is the exploitable coefficient of groundwater in the calculation period; $PZGW$ is the annual groundwater availability (million m^3); tm is the calculation period; and J is the calculation unit.

In general, the main data of this module include the predicted water demand, water supply of municipal water sources, and model parameter. The supplemental materials and the first water allocation scheme are listed in Tables A1–A10.

2.2.2. Groundwater Allowable Withdrawal Calculation Module

Groundwater allowable withdrawal is used to judge whether groundwater in a given region is exploited reasonably. It is used as a feedback of the water resources allocation model. In the study area, the shallow groundwater is the main water source and it is phreatic water. The allowable withdrawal of shallow groundwater is defined as the maximum quantity of groundwater that can be extracted from the aquifer without causing environmental and geologic impacts on the premise of economic and technical feasibility. It can be calculated by mining coefficient method based on groundwater balance method [46] (Equation (3)).

$$W = \rho W_r = \rho(W_e \pm \mu F \frac{\Delta S}{\Delta t}) \quad (3)$$

where W is the groundwater allowable withdrawal (million m^3); W_r is the quantity of groundwater recharged by precipitation infiltration, mountain and plain area infiltration, reservoir and riverway leakage, and other recharges (million m^3); W_e is the discharge of groundwater resulting from lateral discharge, artificial exploitation, phreatic water evaporation, and other discharges (million m^3); ΔS is the changes in groundwater level (m); μ is the specific yield of phreatic water aquifer; F is the area of equilibrium region (km^2); Δt is the time span of equilibrium period; ρ is the exploitable coefficient, which is related to the long-term series groundwater data, aquifer type, and mining conditions. The calculation of ρ is described in our previous study, and the iterative calculation of groundwater allowable withdrawal is listed in Table A11.

2.2.3. Groundwater Simulation Module

GMS 7.1 consisting of several modules such as MODFLOW, FEMWATER, and MODPATH is used in this study to develop the groundwater simulation model, and the equations are composed of fundamental differential equations describing the three-dimensional unsteady groundwater flow in porous media, boundary conditions, and initial constraints (Equation (4)). The MODFLOW module is used for groundwater simulation in this study.

$$\begin{cases} \frac{\partial}{\partial x} \left(K_x \frac{\partial H}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_y \frac{\partial H}{\partial y} \right) + \frac{\partial}{\partial z} \left(K_z \frac{\partial H}{\partial z} \right) + W = \mu \frac{\partial H}{\partial t} \\ H|_{\Gamma_1} = H(x, y, t) \\ K(H - B) \frac{\partial H}{\partial n} |_{\Gamma_2} = q(x, y, t) \\ H|_{t=0} = H_0(x, y) \end{cases} \quad (4)$$

where K is the aquifer permeability coefficient; K_x , K_y , and K_z are the component of the permeability coefficient along the x , y and z directions, respectively (m/d); W is the source term per unit volume (m³/d); μ is the specific yield of the phreatic water aquifer; H is the groundwater level (m); H_0 is the initial water level (m); B is the aquifer floor elevation (m); q is the discharge per unit width under the second type boundary conditions (m³/d/m); x , y and z are the coordinates (m); n is the inner normal on the boundary; and Γ_1 and Γ_2 are the first and second type boundary, respectively.

The accuracy of groundwater simulation is determined based on the average relative error (ARE), mean absolute error (MAE), and root-mean-square error (RMSE) (Equations (5)–(7)).

$$ARE = \frac{1}{n} \sum_{i=1}^n \left| \frac{H_i - H'_i}{H_i} \right| \quad (5)$$

$$MAE = \frac{1}{n} \sum_{i=1}^n |H_i - H'_i| \quad (6)$$

$$RMSE = \sqrt{\frac{\sum_{i=1}^n (H_i - H'_i)^2}{n}} \quad (7)$$

where H_i and H'_i are the observed and calculated groundwater level (m), respectively, and n is the length of sample series.

2.2.4. Groundwater Level Control Module

A critical groundwater level H_c is set in this study in order to prevent potential environmental and geological impacts resulting from too high or too low groundwater levels, and it is established according to the function of different groundwater systems in different areas. The upper and lower limits of the critical groundwater level (H_{up} and H_{low}) are determined for each region to control groundwater exploitation and water level more reasonably (Equations (8) and (9)).

$$H_{up} = \min \begin{cases} H_1 = H_{frost} \\ H_2 \\ H_3 \\ H_4 = \begin{cases} H_{uph} + 1\text{m, important buildings} \\ H_{upl}, \text{ general buildings} \end{cases} \end{cases} \quad (8)$$

$$H_{low} = h - 2/3M \quad (9)$$

where H_1 is the critical groundwater level for frost heaving and boiling (m), H_{frost} is the frost line (m), H_2 is the critical groundwater level for soil salinization (m), H_3 is the anti-floating design water level for underground orbit traffic (subway) (m), H_4 is the waterproof design water level for underground structures (m), H_{uph} is the historical maximum water level (m), H_{upl} is the maximum water level in the recent 3–5 years (m), M is the aquifer thickness (m), and h is the ground elevation (m), respectively.

The average critical groundwater level is calculated from groundwater levels of all monitoring wells by the Thiessen Polygons method described in Equation (10) [47].

$$\overline{H_c} = \frac{1}{A} \sum_{i=1}^n H_{ci} a_i \quad (10)$$

where $\overline{H_c}$ and A are the average critical groundwater level (m) and area (km^2) for different regions, respectively; a_i is the area of the i th calculation unit of the i th Thiessen polygon, $i = 1, 2, \dots, n$ (km^2); H_{ci} is the critical groundwater level of the i th calculation unit of the i th Thiessen polygon, $i = 1, 2, \dots, n$ (m); and n is the number of Thiessen polygons.

2.3. Multiple Iteration Processes

The multiple-iterated dual control model is derived from the coupling of the optimal allocation model of water resources and the groundwater numerical model:

Step 1: The topological and recharge-discharge relations among different water systems, water conservancy projects, and water users in reference year are analyzed. The objective functions and constraints are determined, and the optimal allocation model of water resources is established for the calculation of water demand-supply balance in planning year, which is referred to as the “first allocation scheme” in this study.

Step 2: The results obtained from the first allocation scheme are substituted into Equation (3) to calculate the groundwater allowable withdrawal W_j (where j is the number of iterations, $j = 0, 1, 2, \dots, n$). If $|W_{j+1} - W_j|/W_j \leq \rho$ ($\rho = 0.02$), go to Step 3; otherwise let $j = j + 1$ and return to Step 1. This process is repeated until satisfactory results are obtained, which is referred to as the “second allocation scheme” in this study.

Step 3: The aquifer, boundary conditions, and hydrogeological parameters in the study area are generalized, and the conceptual hydrogeological model and groundwater numerical model are established. Subsequently, groundwater levels are calibrated and verified, and hydrogeological parameters are determined.

Step 4: The results obtained from the second allocation scheme are input into the verified groundwater numerical model to simulate changes in groundwater levels H_j (where j is the number of iterations, $j = 1, 2, \dots, n$). If $H_{low} \leq H_j \leq H_{up}$ and $|W_{j+1} - W_j|/W_j \leq \rho$, stop calculation; otherwise, adjust groundwater exploitation Q_j and optimize water resources allocation again until the following three requirements are met: (1) the total groundwater supply is lower than groundwater allowable withdrawal and the total water consumption is lower than that mandated by government regulations, (2) water supply-demand balance and groundwater recharge-discharge balance are realized; and (3) the water deficit ratio of each unit is no more than 5%. This scheme is referred to as the “third allocation scheme” in this study.

2.4. Data Collection

The input data of the optimal allocation model of water resources include corrected monthly precipitation and runoff in 1956–2013, river flow data, groundwater recharge in 1980–2013, and social and economic data in water demand. The input data of the groundwater numerical model include water levels of monitoring wells, groundwater exploitation of municipal water sources, and groundwater recharge and discharge in 2007–2013. These data are provided by the water management institutes of Shenyang. Main model parameters include river parameters, water supply channel parameters, irrigation water use efficiency parameters, and reservoir parameters, which are determined by field research and expert consultation. Hydrogeological parameters and recharge coefficients of river and field infiltration are calibrated by the model.

3. Results and Discussion

3.1. Establishment and Verification of the Groundwater Simulation Model

In this section, the groundwater simulation model will be described sententiously, and the readers are referred to our previous paper for details [48].

3.1.1. Hydrogeological Conceptual Model

- (1) Conceptualization of aquifer: The geological structure of the study area is simple, and the aquifer is single pore phreatic water of Quaternary period. The aquifer thickness ranges from 19 to 140 m, with an average of 66.01 m. Groundwater resources are abundant in the study area. Basically, the grains are finer in the top layer of the aquifer but coarser in the bottom layer. The top layer is composed of coarse, medium, and fine sands, the middle layer is composed of thin clayey soil, and the bottom layer is composed of sand gravel. The 3D geological structure of the study area is shown in Figure A1. The groundwater flow is conceptualized as a 3D unsteady flow according to the Darcy's law, as the flow field is relatively flat.
- (2) Conceptualization of boundary conditions: (a) Lateral boundary conditions: the northern and southern boundaries with rivers are conceptualized as the first water level boundary; the western boundary in which water is exchanged with neighboring regions is conceptualized as the pervious boundary, while the boundaries of other areas are conceptualized as the second flow boundary; (b) Vertical boundary conditions: the top of the phreatic water aquifer is conceptualized as the water exchange boundary, which receives groundwater recharge and discharge, while the aquifer floor is conceptualized as the impervious boundary because it contacts with bedrock.

3.1.2. Discretization and Solution of Numerical Model

The study area is divided into 18,180 grids (200 rows and 200 columns) by MODFLOW module. Each grid has a length of 300 m, a width of 425 m and an area of 0.1275 km². To reflect the change of groundwater flow during several hydrological years, model calibration is carried out using a series of observed data from 26 April 2007 to 26 April 2013. Model verification is carried out using a series of observed data from 26 April 2013 to 26 September 2013. Calculations are conducted on a monthly basis. There are 72 and 5 stress periods for calibration and validation, respectively.

3.1.3. Calibration and Verification of Groundwater Simulation Model

- (1) Calculation of groundwater recharge and discharge

In this study, groundwater is recharged mainly by precipitation infiltration, lateral recharge, reservoir and riverway leakage, field infiltration, and well irrigation regression, and it is discharged mainly by lateral discharge, artificial exploitation, phreatic water evaporation, and riverway discharge. The specific methods of groundwater recharge and discharge can be referred to Ning et al. [49]. Groundwater equilibrium items are used as input to the groundwater numerical model in the form of area recharge intensity. The results are shown in Table A12.

- (2) Calibration and verification

The observed data from 26 April 2007 to 26 April 2013 is used for calibration of parameters; while that from 26 April 2013 to 26 September 2013 is used for verification. There are about 114 groundwater monitoring wells over the period 2007–2013, and ten representative wells in the subareas are selected in this study. The results of two representative wells, Yuhong and Railway Machinery School wells located near the Yuhong and Bainiao water sources respectively, are shown in Figure 4. Clearly, there is a good agreement between calculated and observed groundwater levels for both wells over the period 2007–2012. Specifically, the MAE is 0.44 and 0.61 m, the ARE is 2.16% and 1.89%, and the RMSE is 0.48 m and 0.66 m for the Yuhong well in the calibration and verification periods, respectively. The MAE is 0.53 m and 0.36 m, the ARE is 1.98% and 0.99%, and the RMSE is 0.61 m and 0.37 m for the Railway Machinery School well in the calibration and verification periods, respectively.

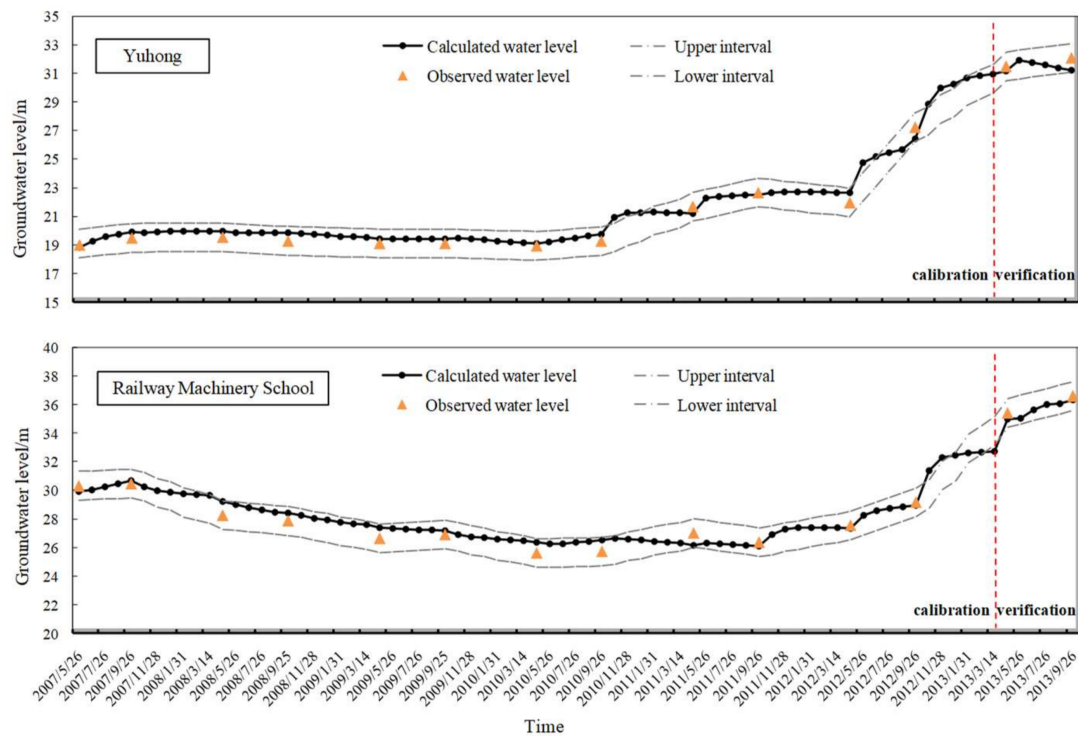


Figure 4. Annual changes of groundwater levels for Yuhong and Railway Machinery School wells in the calibration and verification periods, respectively.

The spatial distribution of groundwater levels in calibration and verification periods is shown in Figure 5. Due to the influence of concentrated groundwater exploitation in the urban district, the spatial distribution of groundwater levels is very complex with some fitting errors. However, the groundwater levels in the other five districts with less groundwater exploitation are basically regular, and the model fits well.

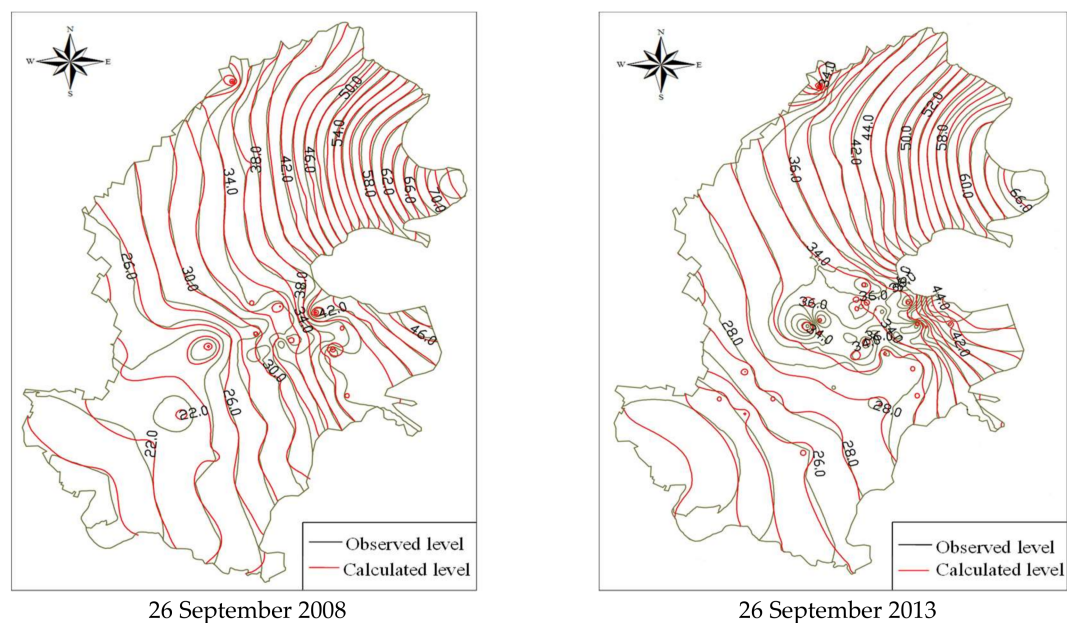


Figure 5. Spatial distribution of groundwater levels in calibration and verification periods.

Table 1 shows that the MAE of average groundwater levels of the 10 monitoring wells is 0.29 m and 0.44 m, the ARE is 0.98% and 1.33%, and the RMSE is 0.30 m and 0.46 m in calibration and verification periods, respectively, indicating a good agreement between observed and calculated groundwater levels.

To conclude, the MAE, ARE, and RMSE are relatively low, indicating high fitting precision of the model. The established groundwater numerical model can be used for quantitating and forecasting the dynamic future trend of groundwater levels.

Table 1. The fitting precision of the average groundwater levels of representative monitoring wells in the calibration and verification periods.

Monitoring Well	Calibration Period					Verification Period				
	Observed Water Level (m)	Calculated Water Level(m)	MAE (m)	ARE	RMSE (m)	Observed Water Level(m)	Calculated Water Level(m)	MAE (m)	ARE	RMSE (m)
Huangjia	40.60	40.25	0.29	0.98%	0.30	41.57	41.03	0.44	1.33%	0.46
Yuhong	19.04	18.82				31.62	31.94			
Tutaizi	21.06	20.75				30.78	30.40			
Zhangshabucun	40.81	40.36				33.22	32.66			
Gongrencun	23.35	23.64				35.20	34.85			
Shashan	29.85	29.61				35.71	35.57			
Urban Oasis	46.26	46.01				39.02	38.55			
Shagangzi	29.30	28.93				30.93	30.34			
Jinbaotai	26.28	26.11				25.62	26.16			
Railway Machinery School	30.30	30.10				35.65	36.17			

3.1.4. Analysis of Parameter Sensitivity and Uncertainty

A total of 68 boreholes and initial values of hydrogeological parameters are determined by field test data and empirical data (Table A13). However, due to the complex heterogeneity of the groundwater system and subjective cognizance, the parameters of groundwater numerical model have uncertainty. Therefore, it is necessary to analyze parameter sensitivity and reduce uncertainty. The permeability coefficient (K) and specific yield (μ) can reflect the permeability of aquifer and declining of groundwater levels, respectively, which are important hydrogeological parameters in groundwater resource evaluation and simulation.

The transforming factor method is used to analyze sensitivity (a parameter as a variable factor and other parameters as invariable factors) [50,51]. The groundwater levels of typical monitoring wells at the end of verification period are output, and changes in groundwater levels are used to reflect parameter sensitivity. The larger change in groundwater levels, the larger effect of parameter on the model. Because the aquifer in the study area is composed of sand and sand gravel, K is 20–150 m/d and μ is 0.1–0.35. After model calibration, K and μ are 50–100 m/d and 0.1–0.2, and thus, K and μ are set to $\pm 20\%$ of initial values. Changes in groundwater levels during parameter variation are shown in Table 2.

Table 2. The water level changes during parameter variation (units: m).

Parameters	Water Level Changes				
	−20%	−10%	0	10%	20%
Permeability coefficient (K)	0.71	0.43	0.00	0.33	0.44
specific yield (μ)	0.17	0.08	0.00	0.06	0.12

Table 2 indicates that as K and μ increase, changes in groundwater levels decrease. K has a more significant effect on the model than μ . Therefore, the permeability coefficient is sensitive to the model.

3.2. Critical Groundwater Level

The upper limit of groundwater level in the Urban District with various underground structures and subways is determined primarily based on the anti-floating design water level of subways and the waterproof design water level of underground structures; while that in the other five districts with large well-canal irrigation regions is determined primarily based on the critical groundwater level for soil salinization [52]. According to the hydrogeological conditions of phreatic water aquifer, the maximum drawdown should not exceed 2/3 of aquifer thickness, and the lower limit of groundwater level is the difference between ground elevation and 2/3 of aquifer thickness [53]. The critical groundwater levels for different subareas are calculated by Equations (8)–(10) (Table 3). Table 3 shows that the average upper limit of water levels is 37.72 m, the average lower limit of water levels is −3.18 m, and the average aquifer thickness is 66.01 m. The minimum aquifer thickness is observed in the Urban District, indicating that the aquifer is thin with low water abundance, and thus it is imperative to control groundwater level within the critical groundwater level.

Table 3. The average critical groundwater level and aquifer thickness of subareas (units: m).

Subarea	Average Upper Limit	Average Lower Limit	Average Aquifer Thickness
Urban District	40.40	17.94	42.69
Shenbei New District	46.47	18.19	45.61
Hunnan New District	48.68	19.56	50.47
Yuhong District	34.12	−10.82	70.41
Sujiatun District	29.43	−33.65	97.63
Development Zone	27.20	−30.30	89.24
Average	37.72	−3.18	66.01

3.3. Optimal Allocation of Water Resources and Groundwater Exploitation Scheme

In this study, the year 2013 is selected as the reference year, while the years 2020 and 2030 are selected as the planning years. Given the rare occurrence of extreme climate events in the history of study area, we focus on the optimal allocation of water resources and changes in groundwater levels in normal years with a precipitation frequency of 50%. The precipitation frequency in 1956–2013 is analyzed and the precipitation in normal years is calculated. The precipitation in 2014–2019, 2020–2029, and 2030–2035 is forecasted by the climate natural variability method [54,55].

3.3.1. Water Supply-Demand Balance

Tables 4 and 5 show water supply and demand in 2020 and 2030 obtained from the second allocation scheme. The results show that the total water supply in 2020 and 2030 is 2266.26 and 2504.74 million m³, whereas the total water demand is 2273.75 and 2506.23 million m³, respectively, thus indicating a good balance between water supply and demand. According to survey data provided by the water management institute of Shenyang, wastewater treatment plants have been established and operated at the end of 2013. Thus, there is an increase in recycled water supply and transferred water supply but a decrease in groundwater supply in 2020 and 2030, indicating that more surface water is used instead of groundwater, which can contribute to improve groundwater environment. The increased supply of recycled water is from wastewater treatment plants.

Table 4. Water demand and supply in 2020 (units: million m³).

Subarea	Water Demand	Water Supply					Water Deficit	Water Deficit Ratio (%)
		Surface Water	Groundwater	Recycled Water	Transferred Water	Total		
Urban District	870.06	17.17	54.01	72.27	726.61	870.06	0.00	0.00
Sujiatun District	223.16	88.76	96.87	9.23	27.44	222.30	0.86	0.39
Development Zone	370.63	76.95	58.99	13.11	221.42	370.47	0.16	0.04
Hunnan New District	219.88	46.72	140.20	11.07	19.98	217.97	1.91	0.87
Shenbei New District	322.59	96.42	155.94	21.42	45.27	319.05	3.54	1.10
Yuhong District	267.43	55.77	161.37	10.56	38.71	266.41	1.02	0.38
Total	2273.75	381.79	667.38	137.66	1079.43	2266.26	7.49	0.35

Table 5. Water demand and supply in 2030 (units: million m³).

Subarea	Water Demand	Water Supply				Total	Water Deficit	Water Deficit Ratio (%)
		Surface Water	Groundwater	Recycled Water	Transferred Water			
Urban District	1026.98	10.69	76.74	185.94	753.14	1026.91	0.07	0.01
Sujiatun District	230.12	85.40	96.35	14.50	33.66	229.91	0.21	0.09
Development Zone	382.11	78.70	58.98	52.92	191.47	382.07	0.04	0.01
Hunnan New District	236.63	47.54	140.18	16.19	32.67	236.58	0.05	0.02
Shenbei New District	350.42	88.59	155.96	14.67	90.55	349.77	0.65	0.19
Yuhong District	279.97	54.69	161.19	16.07	47.55	279.50	0.47	0.17
Total	2506.23	365.61	689.40	300.29	1149.04	2504.74	1.49	0.06

Table 6 shows the calculated groundwater exploitation and groundwater allowable withdrawal after the optimal allocation of water resources. The groundwater exploitation reduces from 290.33 million m³ in 2013 to 87.05 million m³ in 2020 and 109.05 million m³ in 2030, respectively. However, the groundwater exploitation of Hunnan New District remains unchanged in 2020 and 2030 due to extremely high water demand of the national hi-tech industrial development zone. In the first allocation (Tables A9 and A10), the water deficit of Urban District is 68.93 million m³ in 2030, and therefore the groundwater exploitation in 2030 should be increased to 51.20 million m³, resulting in a decrease of water deficit to 0.07 million m³. However, the overexploitation of Urban District in 2013 is 27.95 million m³, while no overexploitation occurs in other districts, indicating that the controlled measure of groundwater exploitation results in effective mitigation of groundwater overexploitation.

Table 6. Calculated groundwater exploitation and groundwater allowable withdrawal under the controlled measure of groundwater exploitation (units: million m³).

Subarea	Groundwater Exploitation			Groundwater Allowable Withdrawal
	2013	2020	2030	
Urban District	104.07	29.20	51.20	76.12
Shenbei New District	55.43	14.78	14.78	153.92
Hunnan New District	18.25	18.25	18.25	211.59
Yuhong District	44.35	17.52	17.52	176.53
Sujiatun District	14.60	7.30	7.30	151.35
Development Zone	53.63	0.00	0.00	57.58
Total	290.33	87.05	109.05	827.09

3.3.2. Spatial and Temporal Changes in Groundwater Levels

The recharge and discharge of groundwater obtained from the second allocation scheme and precipitation in normal years are put into the groundwater numerical model to simulate changes in groundwater levels. We assign 22 stress periods for future prediction from 1 January 2014 to 1 January 2036. Time step is one year. Figure 6 shows that the groundwater levels of water sources (201, Libayan, Songjiang and Beiling) are higher than the upper limit of water level in 2014–2030, and the average groundwater level is increased by 2.52 m. At the beginning of 2034, the groundwater level of Libayan is expected to be 2.1 m higher than the upper limit of water level, whereas that of other water sources is expected to lower than the upper limit of water level. It is also noted that the groundwater levels of all water sources in simulation period are higher than the lower limit of water level. The increase and then decrease in groundwater level coincide well with the decrease and then increase in groundwater exploitation.

Under the second allocation scheme, the groundwater levels decrease from the northeast to the southwest (Figure 7a). Figure 7b shows the spatial distribution of elevation. However, due to controlled groundwater exploitation, the cones of depression observed in 2013 disappear in 2035, and the average groundwater level increases from 34.27 m in 2013 to 34.81 m in 2035. The highest and lowest groundwater level are 73.53 m and 18.32 m, and the average groundwater depth is recovered to 4.92 m. Although the average groundwater level of study area does not exceed the upper limit of water

level, there are some water sources with a groundwater level higher than the upper limit of water level, indicating the need to consider the effect of groundwater exploitation on local water sources.

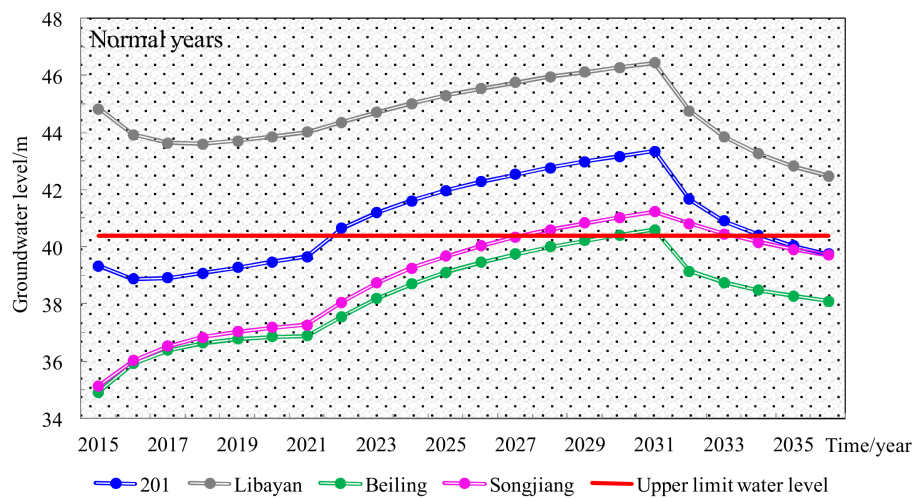


Figure 6. Temporal changes in groundwater levels of water resources obtained by the second allocation scheme.

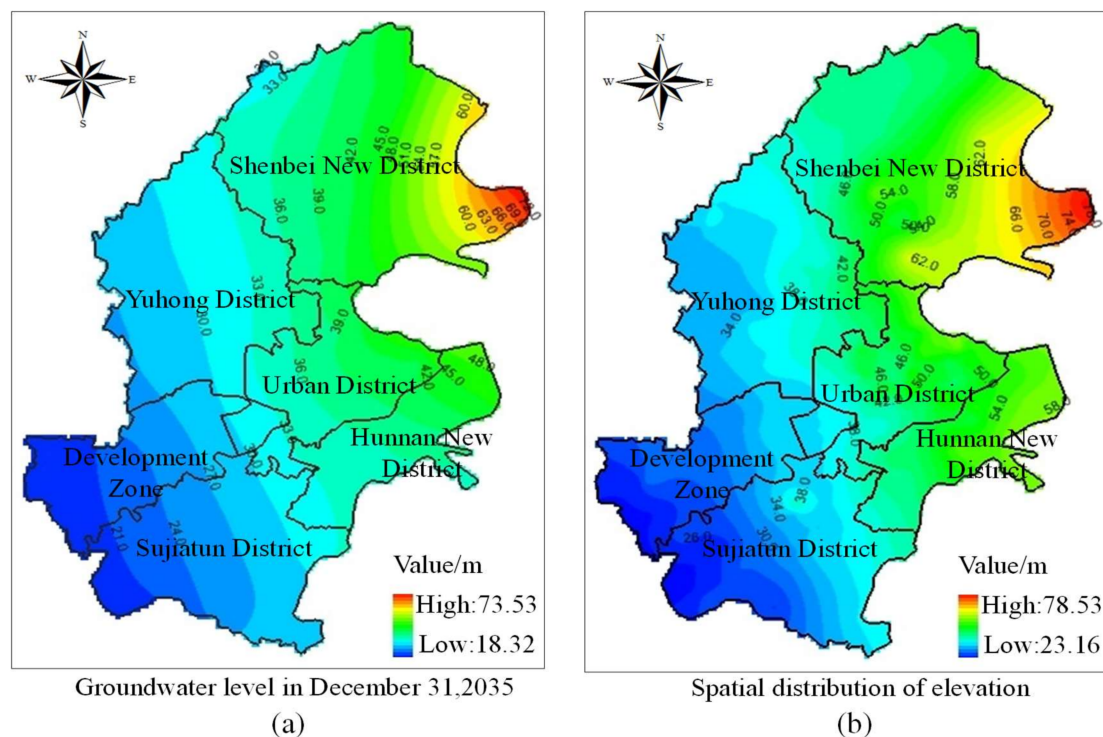


Figure 7. (a) Spatial distribution of groundwater levels under the second allocation scheme at the end of 2035; (b) Spatial distribution of elevation.

3.3.3. Groundwater Exploitation Schemes and Water Sources Arrangement

In China, for controlling groundwater overexploitation, the government sets a restrictive groundwater exploitation for each city every year. However, we do not know how the groundwater level will change with this restrictive groundwater exploitation and whether this value is reasonable. So we want to search an appropriate groundwater exploitation that does not exceed the restrictive value for water resources optimal allocation. Then put the appropriate value into groundwater numerical

model and simulate the groundwater level. If the water level is between the upper and lower limits of water level, the groundwater exploitation is reasonable. The reasonable value is considered as the recommended groundwater exploitation.

Considering that the groundwater level of Libayan is expected to exceed the upper limit of water level at the end of simulation period, it is necessary to calculate the groundwater exploitation of the Urban District in 2030 on the premise of ensuring groundwater recharge-discharge balance in 2020. Finally, groundwater exploitation of Urban District in 2030 is recommended by reasonably adjusting groundwater exploitation. The average groundwater level is 34.72 m and the groundwater levels of all municipal water sources are within critical groundwater level in 2035. Thus, the recommended groundwater exploitation is obtained.

Figure 8 shows the recommended arrangement of municipal water sources at the end of simulation period. There are a total of eleven municipal water sources in the study area, including six water sources in Urban District (20.86, 11.44, 10.04, 9.12, 6.57 and 0.88 million m^3 for Xinnanta, Shashan, Libayan, Beiling, 201, and Songjiang, respectively), two water sources in Shenbei New District (12.23 and 2.55 million m^3 for Huangjia and Shifosi, respectively), one water source in Yuhong District (17.52 million m^3 for Jingsai), one water source in Sujiatun District (7.3 million m^3 for Suxi), and one water source in Hunnan New District (18.25 million m^3 for Hunnan). The total groundwater exploitation is 116.76 million m^3 , with a decrease of about 173.57 million m^3 compared with that in 2013. According to the “closing scheme of groundwater source implemented by government”, most of groundwater sources are closed and few are reserved. On the one hand, water sources are located close to rivers and allow for the recharge of groundwater from river water. On the other hand, the water levels of some areas have trends that exceed the upper limit. Water sources of these areas need to be reserved.

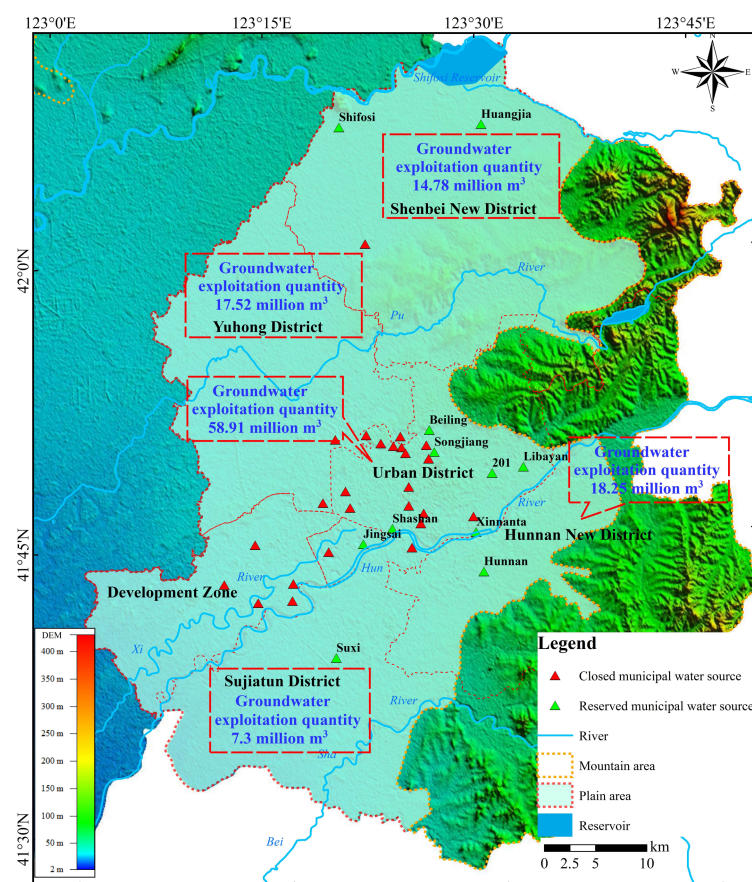


Figure 8. Recommended arrangement of municipal water sources at the end of simulation period.

3.4. Spatial and Temporal Changes in Groundwater Levels under Different Precipitation Conditions

The groundwater levels obtained by the recommended scheme in wet (precipitation frequency is 25%) and dry (precipitation frequency is 75%) years are shown in Figures 9 and 10. Figure 9 shows the spatial distribution of groundwater levels in wet and dry years, respectively. The average groundwater level increases from 34.27 m in 2013 to 36.63 m in 2035 in wet years and reduces to 31.77 m in dry years, with a change of 2.36 m and -2.50 m, respectively. The average groundwater depth is 2.52 m and 7.93 m in wet and dry years, respectively. The precipitation is higher in wet years, resulting in an increase in surface water supply. Consequently, the precipitation infiltration and groundwater level increase. However, the groundwater level reduces significantly in dry years. Figure 9 indicates that the influence of precipitation and groundwater exploitation on groundwater level is very obvious in the same region.

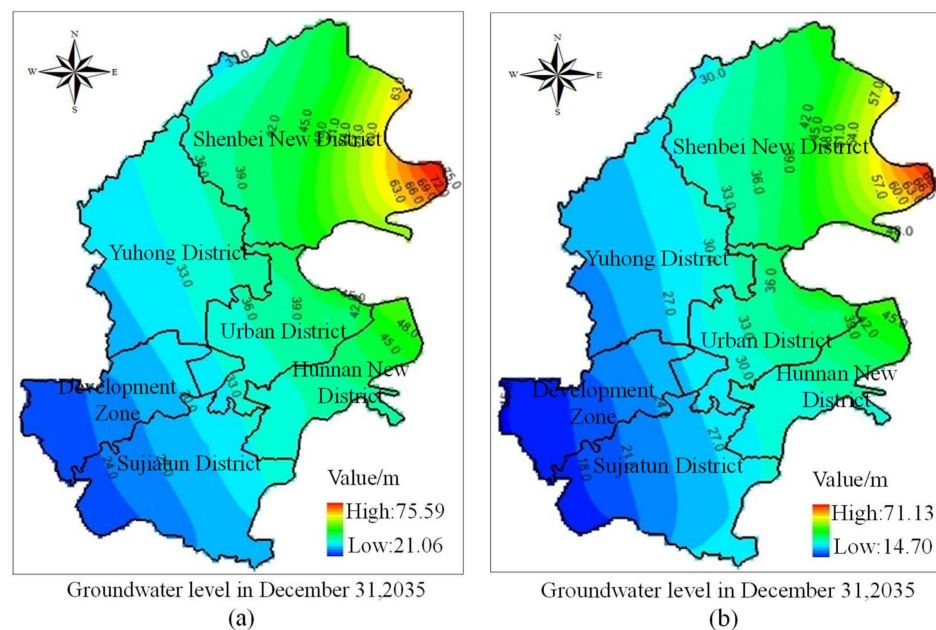


Figure 9. Spatial distribution of groundwater levels in wet and dry years. (a) Spatial distribution of groundwater levels at the end of 2035 in wet years; (b) Spatial distribution of groundwater levels at the end of 2035 in dry years.

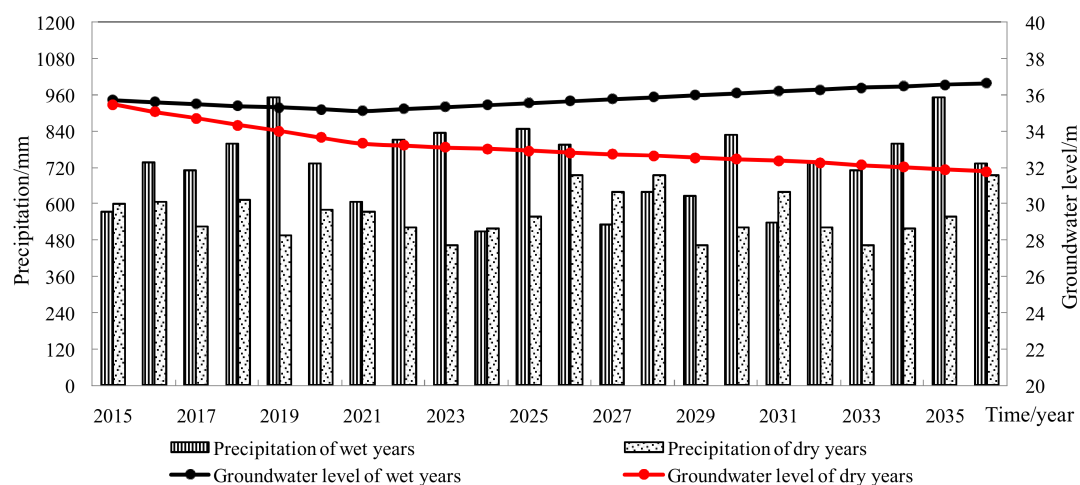


Figure 10. Temporal changes in groundwater levels in wet and dry years, respectively.

Figure 10 shows temporal changes in groundwater levels in wet and dry years. The groundwater levels in wet years show a decreasing and then increasing trend, whereas that in dry years show a decreasing trend. The differences in groundwater levels between dry and wet years range from 0.27 m to 4.86 m with an average of 0.92 m and 3.33 m in 2015–2020 and 2020–2035, respectively. Changes in precipitation in different hydrologic years can have significant effects on the groundwater level, and the decrease rate of groundwater level is higher than the increase rate. Figures 9 and 10 indicate that precipitation is still a significant factor affecting groundwater level under the recommended scheme of groundwater exploitation. Climate change plays an important role in affecting groundwater level.

3.5. Evaluation of the Multiple-Iterated Dual Control Model

In order to evaluate the performance of the recommended scheme, we compared recommended groundwater exploitation, maximum groundwater exploitation stipulated by government, and average groundwater allowable withdrawal, as shown in Table 7. It shows that the recommended groundwater exploitation is 87.05 and 116.76 million m³ in 2020 and 2030, respectively, which is lower than the maximum groundwater exploitation (259.66 million m³) and average groundwater allowable withdrawal (812.48 million m³). The groundwater exploitation of each subarea is also within the range of maximum groundwater exploitation and average groundwater allowable withdrawal.

Table 7. Evaluation of the recommended groundwater exploitation (units: million m³).

Subarea	Recommended Groundwater Exploitation		Maximum Groundwater Exploitation	Average Groundwater Allowable Withdrawal
	2020	2030		
Urban District	29.20	58.91	123.88	77.26
Shenbei New District	14.78	14.78	70.08	133.07
Hunnan New District	18.25	18.25	18.25	212.10
Yuhong District	17.52	17.52	32.85	178.69
Sujiatun District	7.30	7.30	14.60	152.65
Development Zone	0.00	0.00	0.00	58.71
Total	87.05	116.76	259.66	812.48

Table 8 shows that at the end of simulation period, the groundwater levels of all water sources in normal and dry years are within the average critical groundwater level, whereas that of three water sources in Urban District are above the upper limit of water level in wet years. However, the average groundwater level is within the average critical groundwater levels (3.18–37.72 m). Thus, the recommended scheme can satisfy water demand and realize rational utilization of water resources. However, for those water sources with a groundwater level higher than the upper limit in wet years, it is necessary to take appropriate measures to develop groundwater, so that the groundwater level can be kept in the appropriate range, such as constructing water conservation and utilization system and establishing landscape fountains. These methods are suggested measures for realizing this purpose.

Table 8. Groundwater levels in different hydrologic years and average critical groundwater levels (units: m).

Subarea	Water Sources	Groundwater Level in Wet Years	Groundwater Level in Normal Years	Groundwater Level in Dry Years	Average Upper Limit	Average Lower Limit
Urban District	Xinnanta	37.79	37.50	34.49	40.40	17.94
	Shashan	33.36	32.71	29.47		
	Libayan	44.74	40.26	39.16		
	201	41.97	38.47	35.94		
	Beiling	39.37	36.65	33.29		
Shenbei New District	Songjiang	41.42	38.37	35.65	46.47	18.19
	Huangjia	41.94	40.64	39.19		
	Shifosi	35.35	33.79	31.93		
Yuhong District	Jingsai	33.96	31.08	27.13	34.12	−10.82
Sujiatun District	Suxi	29.39	27.05	23.96	29.43	−33.65
Hunnan New District	Hunnan	37.70	36.19	33.16	48.68	19.56

3.6. Discussion of Model Applicability

Groundwater overexploitation has triggered a series of ecological and environmental problems in north China. In 2012, the State Council of China developed a policy to “implement the strictest water resources management system”, which suggested that both total groundwater exploitation and water level should be properly controlled. However, this policy has not been strictly enforced in many regions due to lack of effective management policies and measures. The multiple-iterated dual control model proposed in this study can contribute significantly to reducing groundwater overexploitation in Shenyang, which can also provide important insights into control of groundwater exploitation and water level in other regions. In the study area, the groundwater storage and level have recovered in 2016 [56]. This model has been used to control groundwater depth and realize rational utilization of water resources in other canal-well irrigation regions of China, such as Shanxi [38], and to control groundwater exploitation in Beijing by setting up underground reservoir and allocating irrigation schemes [57]. However, this model is still in the exploratory stage and needs to be further improved to expand its applicability. At present, we attempt to make this model applicable to other groundwater overexploitation areas in China or in the world.

4. Conclusions

In this study, a multiple-iterated dual control model is proposed for short-term and long-term groundwater resources management. This model integrates the optimal allocation model of water resources and the groundwater numerical model, thus making it possible to achieve dual control of groundwater exploitation and water level. It has been successfully applied to the groundwater simulation in Shenyang of Liaoning Province, China. The following conclusions could be drawn:

There is a good agreement between calculated and observed groundwater levels for Yuhong and Railway Machinery School wells over the period 2007–2012, indicating that the groundwater numerical model performs well in simulating groundwater levels with high accuracy.

The optimal allocation of water resources makes it possible for the attainment of water supply–demand balance and groundwater recharge–discharge balance. As a result, the groundwater exploitation reduces from 290.33 million m³ in 2013 to 87.05 million m³ in 2020 and 116.76 million m³ in 2030, respectively.

The controlled exploitation of groundwater results in a disappearance of cones of depression and a rapid recovery of groundwater levels in normal years. The average groundwater level increases from 34.27 m in 2013 to 36.63 m in 2035 in wet years, recovers to 34.72 m in normal years, and reduces to 31.77 m in dry years, respectively. The groundwater exploitation is controlled between the groundwater allowable withdrawal and the maximum groundwater exploitation, and the groundwater levels are controlled within the critical groundwater level.

Water demand predictions of social economy development and ecological environment consider sustainable development in the economy. The optimal allocation model of water resources realizes water supply–demand balance. Regional water resources are rationally allocated in order to achieve better economic and social development. When groundwater is overexploited, it recovers slowly. The multiple-iterated dual control model can be used in overexploitation areas in which surface and transferred water can be used to replace groundwater, and it contributes significantly to economic development, environmental protection, and sustainable groundwater exploitation.

However, there are some limitations in this model. For instance, although future precipitation changes and groundwater exploitation schemes have been considered in this model, some other uncertainties, such as temperature and groundwater quality, are not considered. This deserves further research in future studies.

Acknowledgments: This study was funded by the Critical Patented Projects in the Control and Management of the National Polluted Water Bodies (No. 2012ZX07201-006), the Scientific Research Special Fund Project of Public Welfare by Ministry of Water Resources, China (No. 201401003), the National Science Foundation for

Distinguished Young Scholars of China (No. 51709274), and Special Funds for Scientific Research of Public Welfare in the Ministry of Water Resources (No. 201501013).

Author Contributions: All authors made a substantial contribution to this paper. Junqiu Liu, Guohua Fang, Xinmin Xie, and Zhenzhen Ma conceived and designed the methods and model; Junqiu Liu and Huaxiang He performed the calculations and analyzed the results; Junqiu Liu wrote the paper and submitted it; Junqiu Liu, Zhenzhen Ma, and Mingyue Du modified the manuscript.

Conflicts of Interest: The authors declare no conflict of interest.

Appendix A

Tables A1–A5 are the main predicted results of water demand that need to input the optimal allocation module of water resources.

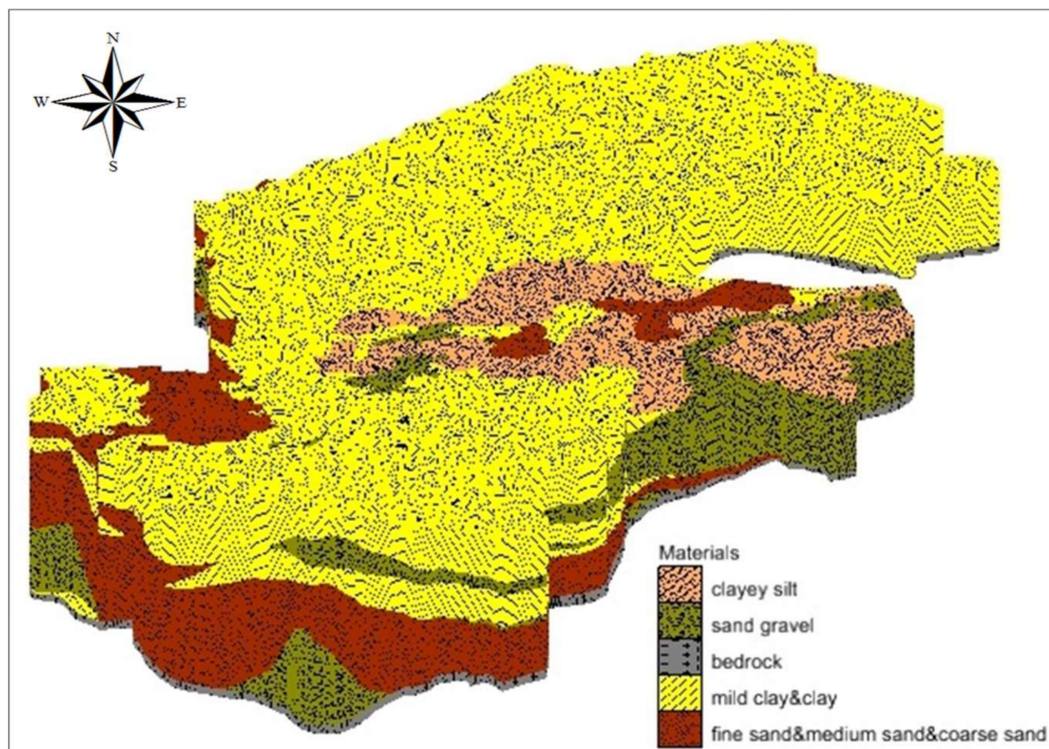


Figure A1. The 3D geological structure of study area.

Table A1. Prediction of population development (units: million persons).

Subarea	Urban Population			Rural Population			Total Population		
	2013	2020	2030	2013	2020	2030	2013	2020	2030
Urban District	4.17	4.99	6.07	0.00	0.00	0.00	4.17	4.99	6.07
Development Zone	0.14	0.24	0.32	0.12	0.07	0.06	0.26	0.31	0.38
Sujiatun District	0.32	0.38	0.57	0.16	0.20	0.12	0.48	0.58	0.69
Hunnan New District	0.17	0.37	0.58	0.16	0.13	0.08	0.33	0.50	0.66
Shenbei New District	0.31	0.49	0.66	0.12	0.16	0.14	0.43	0.65	0.80
Yuhong District	0.57	0.68	0.82	0.06	0.07	0.07	0.63	0.75	0.89
Total	5.68	7.15	9.02	0.62	0.63	0.47	6.30	7.78	9.49

Table A2. Prediction of gross domestic product (GDP) (units: million yuan).

Area	GDP			Per Capita GDP		
	2013	2020	2030	2013	2020	2030
Shenyang	715,860	1,980,830	4,063,500	0.09	0.20	0.34

Table A3. Prediction of economic development.

Subarea	Industrial Value Added (Billion Yuan)			Construction and Tertiary Industry Value Added (Billion Yuan)			Effective Irrigation Area of Farmland (Million Mu)		
	2013	2020	2030	2013	2020	2030	2013	2020	2030
Urban District	54.10	149.32	301.63	237.92	759.47	1476.92	0.00	0.00	0.00
Development Zone	82.01	249.10	548.34	15.35	44.7	81.16	0.17	0.21	0.21
Sujiatun District	19.71	50.89	102.86	13.06	35.58	64.49	0.24	0.28	0.28
Hunnan New District	32.25	88.22	182.85	16.21	42.38	77.80	0.10	0.11	0.11
Shenbei New District	38.72	110.11	230.12	13.73	36.4	67.74	0.25	0.33	0.33
Yuhong District	29.73	69.95	152.42	17.13	44.48	82.03	0.19	0.20	0.20
Total	256.52	717.59	1518.22	313.4	963.01	1850.14	0.95	1.13	1.13

Table A4. Water demand prediction of social economy development (units: million m³).

Subarea	Living			Industry			Construction and Tertiary Industry			Agriculture		
	2013	2020	2030	2013	2020	2030	2013	2020	2030	2013	2020	2030
Urban District	212.85	281.87	363.20	70.29	150.72	147.61	157.86	392.58	457.76	0.00	0.00	0.00
Development Zone	10.02	15.03	19.87	116.67	257.22	264.62	9.90	23.36	26.13	75.55	69.30	64.94
Sujiatun District	20.35	26.44	36.39	29.49	57.81	57.19	9.00	18.96	21.35	128.89	110.73	104.57
Hunnan New District	13.52	24.38	35.90	47.80	99.87	99.12	11.59	23.57	28.13	55.74	51.70	51.53
Shenbei New District	18.41	30.80	41.78	59.63	126.61	142.65	8.01	18.77	25.39	138.90	135.40	127.83
Yuhong District	30.08	39.57	50.37	43.12	76.96	80.82	11.95	24.48	27.02	111.53	93.89	87.72
Total	305.23	418.09	547.51	367.00	769.19	792.01	208.31	501.72	585.78	510.61	461.02	436.59

Table A5. Water demand prediction of ecological environment (units: million m³).

Subarea	2013	2020	2030
Urban District	30.36	44.89	58.41
Development Zone	0.90	2.83	3.41
Sujiatun District	2.10	5.20	6.22
Hunnan New District	15.07	18.47	19.91
Shenbei New District	2.05	5.89	7.26
Yuhong District	25.70	28.74	30.07
Total	76.18	106.02	125.28

Table A6. Designed water supply capacity of municipal water sources.

Subarea	Name of Municipal Water Source	Designed Water Supply Capacity (m ³ /d)	Water Supply of 2013 (Million m ³)
Urban District	Gongrencun	4000	0.00
	Tiexi	4000	0.00
	Beiling	25,000	0.00
	Bainiao	10,000	3.21
	Zhongshan	16,000	1.45
	Zhongyi	9000	2.02
	Songjiang	2000	0.91
	Taiyuan	5000	1.60
	Libayan	54,000	13.38
	Henan	3000	4.65
	Dizhi	3000	0.00
	Jiuheli	2000	0.00
	Longjiang	2000	0.00
	Wanquan	17,000	4.65
	201	18,000	5.62
	Donggong	6000	0.25
	Sanhao	6000	0.26
	Xinnanta	155,000	52.56
Yuhong District	Changbai	12,000	0.00
	Shashan	85,000	13.51
	Liguan	106,000	0.33
	Yuhong	25,000	2.54
	Dingxiang	26,000	5.44
	Hebei	45,000	16.14
Shenbei New District	Jingsai	114,000	17.52
	Fangshi	15,000	2.38
	Yinjia	54,000	19.00
	Shifosi	72,000	24.22
Development Zone	Huangjia	34,000	12.21
	Langjia	60,000	0.00
	Zhaijia	90,000	19.07
	The first water plant of Shengke		11.52
	The second water plant of Shengke	95,000	11.52
	The third water plant of Shengke		11.52
Sujiatun District	Suxi	40,000	14.60
Hunnan New District	Hunnan	50,000	18.25

Table A7. The large reservoir for participating water resources allocation model.

Name	Controlled Area (km ²)	Normal High Water Level (m)	Normal Storage (Million m ³)	Dead Water Level (m)	Deadl Storage (Million m ³)	Monthly Leakage Coefficient
Shifosi	164,786	66.2	140.0	59.7	30.0	0.003

Table A8. The main parameter and actual values of water resources model in calculation units.

Water Resources Division	Administrative Division	Annual Groundwater Availability (Million m ³)	Monthly Exploitable Coefficient	Irrigation Utilization Coefficient of Surface Water	Coefficient of Canal into River
Region above Shifosi	Shenbei New District	0.67	0.15	0.59	0.23
Region from Shifosi	Shenbei New District	45.52	0.15	0.59	0.22
	Yuhong District	7.89	0.15	0.59	0.22
Region from Dahuofoang reservoir	Shenbei New District	70.31	0.15	0.54	0.13
	Yuhong District	114.98	0.15	0.54	0.13
	Urban District	157.71	0.15	0.54	0.13
	Hunnan New District	40.53	0.15	0.54	0.13
	Sujiatun District	27.57	0.15	0.54	0.13
Taizi River region	Hunnan New District	1.27	0.14	0.54	0.13
	Sujiatun District	22.44	0.14	0.54	0.13

Annotation: Annual groundwater availability of Development Zone is included in Urban District in the allocation process.

Table A9. Water demand and supply in reference year (2013) (units: million m³).

Subarea	Water Demand	Water Supply					Water Deficit	Water Deficit Ratio (%)
		Surface Water	Groundwater	Recycled Water	Transferred Water	Total		
Urban District	471.36	4.34	224.06	6.88	236.08	471.36	0.00	0.00
Sujiatun District	194.14	86.29	101.06	4.73	0.00	192.08	2.06	1.06
Development Zone	215.92	64.18	61.47	0.00	82.25	207.90	8.02	3.71
Hunnan New District	145.61	20.06	118.31	0.00	7.24	145.61	0.00	0.00
Shenbei New District	231.98	91.18	112.32	0.00	0.00	203.50	28.48	12.28
Yuhong District	226.08	46.07	129.98	0.00	32.14	208.19	17.89	7.91
Total	1485.09	312.12	747.20	11.61	357.71	1428.64	56.45	3.80

Table A10. Water demand and supply in 2030 (the first allocation result) (units: million m³).

Subarea	Water Demand	Water Supply					Water Deficit	Water Deficit Ratio (%)
		Surface Water	Groundwater	Recycled Water	Transferred Water	Total		
Urban District	1026.98	10.69	54.74	167.48	725.14	958.05	68.93	6.71
Sujiatun District	230.12	85.40	96.35	14.50	33.66	229.91	0.21	0.09
Development Zone	382.11	78.70	58.98	52.92	191.47	382.07	0.04	0.01
Hunnan New District	236.63	47.54	140.18	16.19	32.67	236.58	0.05	0.02
Shenbei New District	350.42	88.59	155.96	14.67	90.55	349.77	0.65	0.19
Yuhong District	279.97	54.69	161.19	16.07	47.55	279.50	0.47	0.17
Total	2506.23	365.61	667.4	281.83	1121.04	2435.88	70.35	2.81

Table A11. The iterative calculation of groundwater allowable withdrawal (unit for W_j : million m³).

Subarea	Initial Value		Initial Allocation		Multiple Loop Iteration							Final Result
			The First Iteration		The Second Iteration		The Third Iteration		The Fourth Iteration			
	Recharge Amount	ρ	W_0	W_1	$\frac{ W_0 - W_1 }{W_0}$	W_2	$\frac{ W_1 - W_2 }{W_1}$	W_3	$\frac{ W_2 - W_3 }{W_2}$	W_4	$\frac{ W_3 - W_4 }{W_3}$	
Urban District	84.89	0.98	83.19	80.68	3.0%	77.25	4.3%	76.12	1.5%	76.12	1.5%	76.12
Development Zone	64.52	0.96	61.94	60.34	2.6%	56.10	7.0%	58.71	4.7%	57.58	1.9%	57.58
Shenbei New District	200.03	0.88	176.03	168.48	4.3%	161.54	4.1%	156.18	3.3%	153.92	1.4%	153.92
Yuhong District	192.76	0.96	185.05	179.93	2.8%	178.69	0.7%	176.53	1.2%	176.53	1.2%	176.53
Hunnan New District	259.77	0.89	231.20	225.53	2.5%	220.43	2.3%	213.01	3.4%	211.59	0.7%	211.59
Sujiatun District	189.46	0.86	162.94	158.41	2.8%	153.46	3.1%	151.35	1.4%	151.35	1.4%	151.35

Notes: The recharge amount is the multi-year average of groundwater recharge from 1980 to 2013. ρ is the exploitable coefficient.

Table A12. Calculated results of groundwater balanced items (2007–2013) (units: million m³).

Balanced Item	2007	2008	2009	2010	2011	2012	2013
Precipitation infiltration recharge	224.72	307.49	317.68	427.08	212.96	417.92	357.99
Riverway leakage recharge	241.87	291.73	201.61	259.70	219.14	224.80	213.58
Lateral recharge	19.11	20.39	20.39	23.18	14.26	24.12	23.79
Field infiltration recharge	145.25	191.79	145.38	234.82	131.60	170.29	43.08
Well irrigation regression recharge	50.71	44.60	38.95	45.65	50.68	45.44	57.76
Total	681.66	856.00	724.01	990.43	628.64	882.57	696.20
Artificial exploitation	694.16	654.01	644.82	667.25	747.11	711.49	607.32
Phreatic water evaporation	2.21	2.52	1.94	2.30	1.67	2.00	1.97
Lateral discharge	23.46	22.79	22.79	26.53	19.38	29.07	28.46
Riverway discharge	67.12	55.30	47.27	72.11	88.58	57.59	71.52
Total	786.95	734.62	716.82	768.19	856.74	800.15	709.27

Table A13. Initial value of hydrogeological parameters in study area.

Subarea	Permeability Coefficient (m/d)	Specific Yield	Precipitation Infiltration Coefficient	Phreatic Water Evaporation Coefficient	Paddy Field Infiltration Coefficient	Dry Field Infiltration Coefficient	Riverway Leakage Coefficient	Canal Infiltration Coefficient
Urban District	100	0.11	0.19	0.06	0.22	0.13	0.09	0.12
Shenbei New District	70	0.11	0.26	0.07	0.22	0.13	0.14	0.12
Hunnan New District	70	0.12	0.21	0.06	0.22	0.13	0.13	0.12
Yuhong District	70	0.12	0.21	0.06	0.22	0.13	0.13	0.12
Sujiatun District	70	0.11	0.17	0.05	0.23	0.14	0.13	0.12
Development Zone	70	0.11	0.21	0.06	0.22	0.13	0.12	0.12

Annotation: The permeability coefficient and specific yield are calibrated by groundwater numerical model. The other coefficients have been calculated and referred to empirical values in our previous reports of project.

References

1. Foster, S.S.D.; Perry, C.J. Improving groundwater resource accounting in irrigated areas: A prerequisite for promoting sustainable use. *Hydrogeol. J.* **2010**, *18*, 291–294. [CrossRef]
2. Mulligan, K.B.; Brown, C.; Yang, Y.C.E.; Ahlfeld, D.P. Assessing groundwater policy with coupled economic-groundwater hydrologic modeling. *Water Resour. Res.* **2014**, *50*, 2257–2275. [CrossRef]
3. Matthew, J.C.; Dioni, I.C.; Cheng, X. Erratum: Analysis of environmental isotopes in groundwater to understand the response of a vulnerable coastal aquifer to pumping: Western Port Basin, south-eastern Australia. *Hydrogeol. J.* **2013**, *21*, 1413–1427. [CrossRef]
4. Zhu, B. Management Strategy of Groundwater Resources and Recovery of Over-Extraction Drawdown Funnel in Huaibei City, China. *Water Resour. Res.* **2013**, *27*, 3365–3385. [CrossRef]
5. Pacheco-Martínez, J.; Hernández-Marín, M.; Burbey, T.J.; González-Cervantes, N.; Ortiz-Lozano, J.Á.; Zermeno-De-León, M.E.; Solís-Pintoc, A. Land subsidence and ground failure associated to groundwater abstraction in the Aguascalientes Valley, Mexico. *Eng. Geol.* **2013**, *164*, 172–186. [CrossRef]
6. Benyamini, Y.; Mirlas, V.; Marish, S.; Gottesman, M.; Fizik, E.; Agassi, M. A survey of soil salinity and groundwater level control systems in irrigated fields in the Jezre'el Valley, Israel. *Agric. Water Manag.* **2005**, *76*, 181–194. [CrossRef]
7. García-Gil, E.; Vázquez-Suñe, J.A.; Sánchez-Navarro, J.; Lázaro, M.; Alcaraz, M. The propagation of complex flood-induced head wave fronts through a heterogeneous alluvial aquifer and its applicability in groundwater flood risk management. *J. Hydrol.* **2015**, *527*, 402–419. [CrossRef]
8. Zhang, M.L.; Hu, L.T.; Yao, L.L.; Yin, W.J. Surrogate Models for Sub-Region Groundwater Management in the Beijing Plain, China. *Water* **2017**, *9*, 766. [CrossRef]
9. State Council. Opinions of the Implementation of the Strictest Water Resources Management Regulations. 12 January 2012. Available online: http://szy.mwr.gov.cn/zd gz/zygszyglzd/201406/t20140610_566891.html (accessed on 15 December 2017). (In Chinese)
10. Mehl, S.; Hill, M.C. Development and evaluation of a local grid refinement method for block-centered finite-difference groundwater models using shared nodes. *Adv. Water Resour.* **2002**, *25*, 497–511. [CrossRef]
11. Wang, H.R.; Zhu, G.R.; Zhao, J.X. A Groundwater Flow Domain Decomposition Model Coupling the Boundary and Finite Element Methods. *Geol. Rev.* **2003**, *49*, 48–52. (In Chinese)
12. Anderson, M.P.; Woessner, W.W. *Applied Groundwater Modeling: Simulation of Flow and Advective Transport*; Academic Press Inc.: New York, NY, USA, 1992; pp. 145–152.
13. Environmental Modeling Research Laboratory (EMRL). *Groundwater Modeling System*; Environmental Modeling Research Laboratory, Brigham Young University: Provo, UT, USA, 1999.
14. McDonald, M.G.; Harbaugh, A.W. *A Modular Three-Dimensional Finite-Difference Ground-Water Flow Model*; U.S. Geological Survey Open-File Report; U.S. Geological Survey: Washington, DC, USA, 1988.
15. Lin, H.C.; Richards, D.R.; Yeh, G.T.; Cheng, J.R.; Jones, N.L. *FEMWATER: A Three-Dimensional Finite Element Computer Model for Simulating Density-Dependent Flow and Transport in Variably Saturated Media*; Technical Report CHL-97-12; Waterways Experiment Station, U.S. Army Corps of Engineers: Vicksburg, MS, USA, 1997.
16. Diersch, H.J.G. *FEFLOW: User's Manual*; WASY-Institute for Water Resources Planning and Systems; Research Ltd.: Berlin, Germany, 1998.
17. Milzow, C.; Kinzelbach, W. Accounting for subgrid scale topographic variations in flood propagation modeling using MODFLOW. *Water Resour. Res.* **2010**, *46*, 219–233. [CrossRef]
18. Zghibi, A.; Zouhri, L.; Tarhouni, J. Groundwater modelling and marine intrusion in the semi-arid systems (Cap-Bon, Tunisia). *Hydrol. Process.* **2011**, *25*, 1822–1836. [CrossRef]
19. Roy, D.K.; Datta, B. Fuzzy C-Mean Clustering Based Inference System for Saltwater Intrusion Processes Prediction in Coastal Aquifers. *Water Resour. Manag.* **2017**, *31*, 1–22. [CrossRef]
20. Karatzas, G.P. Developments on Modeling of Groundwater Flow and Contaminant Transport. *Water Resour. Manag.* **2017**, *31*, 3235–3244. [CrossRef]
21. Li, J.; Mao, X.M.; Li, M. Modeling hydrological processes in oasis of Heihe River Basin by landscape unit-based conceptual models integrated with FEFLOW and GIS. *Agric. Water Manag.* **2017**, *179*, 338–351. [CrossRef]
22. Havril, T.; Tóth, Á.; Molson, J.W.; Galsa, A.; Mádl-Szőnyi, J. Impacts of predicted climate change on groundwater flow systems: Can wetlands disappear due to recharge reduction? *J. Hydrol.* **2017**. [CrossRef]

23. Sahoo, S.; Jha, M.K. Numerical groundwater-flow modeling to evaluate potential effects of pumping and recharge: Implications for sustainable groundwater management in the Mahanadi delta region, India. *Hydrogeol. J.* **2017**, *25*, 1–23. [[CrossRef](#)]
24. Islam, M.B.; Firoz, A.B.M.; Foglia, L.; Marandi, A.; Khan, A.R.; Schüth, C.; Ribbe, L. A regional groundwater-flow model for sustainable groundwater-resource management in the south Asian megacity of Dhaka, Bangladesh. *Hydrogeol. J.* **2017**, *25*, 617–637. [[CrossRef](#)]
25. Gebreyohannes, T.; De Smedt, F.; Walraevens, K.; Gebresilassie, S.; Hussien, A.; Hagos, M.; Amare, K.; Deckers, J.; Gebrehiwot, K. Regional groundwater flow modeling of the Geba basin, Northern Ethiopia. *Hydrogeol. J.* **2017**, *25*, 639–655. [[CrossRef](#)]
26. Wang, H.; Jia, Y.W. Theory and study methodology of dualistic water cycle in river basins under changing conditions. *J. Hydraul. Eng.* **2016**, *47*, 1219–1226. (In Chinese)
27. Gao, Y.F.; Zhang, Z.Y. Chaotic artificial fish-swarm algorithm and its application in water use optimization in irrigated areas. *Trans. Chin. Soc. Agric. Eng.* **2007**, *23*, 7–11. (In Chinese)
28. Yang, C.C.; Chang, L.C.; Chen, C.S.; Yeh, M.S. Multi-objective planning for conjunctive use of surface and subsurface water using genetic algorithm and dynamics programming. *Water Resour. Manag.* **2009**, *23*, 417–437. [[CrossRef](#)]
29. Mohammad, R.T.M.; Soltani, J. Multi-objective optimal model for conjunctive use management using SGAs and NSGA-II models. *Water Resour. Manag.* **2013**, *27*, 37–53.
30. Wu, X.; Zheng, Y.; Wu, B.; Tian, Y.; Han, F.; Zheng, C.M. Optimizing conjunctive use of surface water and groundwater for irrigation to address human-nature water conflicts: A surrogate modeling approach. *Agric. Water Manag.* **2016**, *163*, 380–392. [[CrossRef](#)]
31. Fu, Q.; Liu, Y.F.; Liu, D.; Li, T.X.; Liu, W.; Amgad, O. Optimal allocation of multi-water resources in irrigation area based on interval-parameter multi-stage stochastic programming model. *Trans. Chin. Soc. Agric. Eng.* **2016**, *32*, 132–139. (In Chinese)
32. Safavi, H.R.; Enteshari, S. Conjunctive use of surface and ground water resources using the ant system optimization. *Agric. Water Manag.* **2016**, *173*, 23–34. [[CrossRef](#)]
33. Safavi, H.R.; Esmikhani, M. Conjunctive use of surface water and groundwater: Application of support vector machines (SVMs) and genetic algorithms. *Water Resour. Manag.* **2013**, *27*, 2623–2644. [[CrossRef](#)]
34. Emin, C.D.; Charles, F.B.; Tariq, N.K. Groundwater Modeling in Support of Water Resources Management and Planning under Complex Climate, Regulatory, and Economic Stresses. *Water* **2016**, *8*, 592. [[CrossRef](#)]
35. Lu, H.Y.; Xie, X.M.; Guo, K.Z.; Wang, J. Study on groundwater allowable withdrawal of groundwater based on water resources optimal allocation. *J. Hydraul. Eng.* **2013**, *44*, 1182–1188. (In Chinese)
36. Dušan, P.; Zoran, G.; Dragoljub, B.; Čedomir, C. A Hybrid Model for Forecasting Groundwater Levels Based on Fuzzy C-Mean Clustering and Singular Spectrum Analysis. *Water* **2017**, *9*, 541. [[CrossRef](#)]
37. Jang, C.S.; Chen, C.F.; Liang, C.P.; Chen, J.S. Combining groundwater quality analysis and a numerical flow simulation for spatially establishing utilization strategies for groundwater and surface water in the Pingtung Plain. *J. Hydrol.* **2016**, *533*, 541–556. [[CrossRef](#)]
38. Su, X.L.; Song, Y.; Liu, J.M.; Dang, Y.R.; Tian, Z. Spatiotemporal optimize allocation of water resources coupling groundwater simulation model in canal-well irrigation district. *Trans. Chin. Soc. Agric. Eng.* **2016**, *32*, 43–51. (In Chinese)
39. Stefania, G.A.; Rotiroti, M.; Fumagalli, L.; Simonetto, F.; Capodaglio, P.; Zanotti, C.; Bonomi, T. Modeling groundwater/surface-water interactions in an Alpine valley (the Aosta Plain, NW Italy): The effect of groundwater abstraction on surface-water resources. *Hydrogeol. J.* **2018**, *26*, 147–162. [[CrossRef](#)]
40. Yang, Y.S.; Kalin, R.M.; Zhang, Y.; Lin, X.; Zou, L. Multi-objective optimization for sustainable groundwater resource management in a semiarid catchment. *Hydrol. Sci. J.* **2009**, *46*, 55–72. [[CrossRef](#)]
41. Yue, W.F.; Yang, J.Z.; Zhan, C.S. Coupled model for conjunctive use of water resources in the Yellow River irrigation district. *Trans. Chin. Soc. Agric. Eng.* **2011**, *27*, 35–40. (In Chinese)
42. Wang, T.; Fang, G.H.; Xie, X.M.; Liu, Y.; Ma, Z.Z. A Multi-Dimensional Equilibrium Allocation Model of Water Resources Based on a Groundwater Multiple Loop Iteration Technique. *Water* **2017**, *9*, 718. [[CrossRef](#)]
43. Zhou, X.N. Research on Multi-Dimensional Coordinated Allocation Model of Water Resources and Its Application. Ph.D. Thesis, China Institute of Water Resources and Hydropower Research, Beijing, China, 2015. (In Chinese)
44. Bussieck, M.R.; Meeraus, A. General Algebraic Modeling System (GAMS). *Appl. Optim.* **2004**, *88*, 137–158.

45. Wei, C.J.; Han, J.S.; Han, S.H. *Key Technology and Demonstration of Basin or Regional Water Resources Total Factor Optimal Allocation*; China Water Power Press: Beijing, China, 2012. (In Chinese)
46. Li, R.Z.; Wang, J.Q.; Qian, J.Z. Unascertained risk analysis of groundwater allowable withdrawal evaluation. *J. Hydraul. Eng.* **2004**, *35*, 54–60. (In Chinese)
47. Thomas, I.I.; Hartmann, H.C. Resolving Thiessen polygons. *J. Hydrol.* **1985**, *76*, 363–379.
48. Liu, J.Q.; Xie, X.M. Numerical simulation of groundwater and early warnings from the simulated dynamic evolution trend in the plain area of Shenyang, Liaoning Province (P.R. China). *J. Groundw. Sci. Eng.* **2016**, *4*, 367–376.
49. Ning, L.B.; Dong, S.G.; Ma, C.M. *Theory and Practice of Groundwater Numerical Simulation*; China University of Geosciences Press: Wuhan, China, 2010. (In Chinese)
50. Lenhart, T.; Eckhardt, K. Comparison of two different approaches of sensitivity analysis. *Phys. Chem. Earth* **2002**, *27*, 645–654. [[CrossRef](#)]
51. Crosetto, M.; Tarantola, S. Uncertainty and sensitivity analysis: Tools for GIS-based model implementation. *Int. J. Geogr. Inf. Sci.* **2001**, *15*, 415–437. [[CrossRef](#)]
52. Nosetto, M.D.; Acosta, A.M.; Jayawickreme, D.H.; Ballesteros, S.I.; Jackson, R.B.; Jobbagy, E.G. Land-use and topography shape soil and groundwater salinity in central Argentina. *Agric. Water Manag.* **2013**, *129*, 120–129. [[CrossRef](#)]
53. Xie, X.M.; Chai, F.X.; Yan, Y.; Zhang, J.Q.; Yang, L.L. Preliminary Study on Critical Depth of Ground Water Table. *Ground Water*. **2007**, *29*, 47–50. (In Chinese)
54. Arnell, N.W. Relative effects of multi-decadal climatic variability and changes in the mean and variability of climate due to global warming: Future streamflows in Britain. *J. Hydrol.* **2003**, *270*, 195–213. [[CrossRef](#)]
55. Prudhomme, C.; Jakob, D.; Svensson, C. Uncertainty and climate change impact on the flood regime of small UK catchments. *J. Hydrol.* **2003**, *277*, 1–23. [[CrossRef](#)]
56. Liaoning Provincial Department of Water Resources. Liaoning Provincial Bulletin of Water Resources in 2016. Available online: http://www.lnwater.gov.cn/jbgb/szygb/201703/t20170324_2821392.html (accessed on 21 February 2018). (In Chinese)
57. Zhao, Y. The Research on Storage and Storage Capacity of Groundwater Reservoir-Take Beijing Mihuaishun Groundwater Reservoir Study Area as an Example. Master's Thesis, North China University of Water Resources and Electric Power, Zhengzhou, China, 2014. (In Chinese)



© 2018 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (<http://creativecommons.org/licenses/by/4.0/>).