

Article



# Simulation of Daily Mean Soil Temperatures for Agricultural Land Use Considering Limited Input Data

Philipp Grabenweger <sup>1</sup>, Branislava Lalic <sup>2</sup>, Miroslav Trnka <sup>3,4</sup>, Jan Balek <sup>3,4</sup>, Erwin Murer <sup>5</sup>, Carmen Krammer <sup>5</sup>, Martin Možný <sup>3,6</sup>, Anne Gobin <sup>7,8</sup>, Levent Şaylan <sup>9</sup> and Josef Eitzinger <sup>1,\*</sup>

- <sup>1</sup> Institute of Meteorology and Climatology, University of Natural Resources and Life Sciences, Gregor-Mendel-Straße 33, A-1180 Vienna, Austria; philipp.grabenweger@outlook.at
- <sup>2</sup> Faculty of Agriculture, University of Novi Sad, Dositej Obradovic Sq. 8, 21000 Novi Sad, Serbia; branislava.lalic@polj.edu.rs
- <sup>3</sup> CzechGlobe–Global Change Research Institute, Czech Academy of Sciences, Bělidla986, 4a, 60300 Brno, Czech Republic; miroslav.trnka@mendelu.cz (M.T.); jan.balek.83@seznam.cz (J.B.); martin.mozny@chmi.cz (M.M.)
- <sup>4</sup> Institute of Agriculture Systems and Bioclimatology, Mendel University in Brno, Zemědělská 1, 61300 Brno, Czech Republic
- <sup>5</sup> Federal Agency for Water Management (BAW), Pollnbergstraße 1, A-3252 Petzenkirchen, Austria; erwin.murer@baw.at (E.M.); carmen.krammer@baw.at (C.K.)
- <sup>6</sup> Czech Hydrometeorological Institute, Agrometeorological Observatory, Doksany, 14306 Prague, Czech Republic
- <sup>7</sup> Flemish Institute for Technological Research (VITO), Boeretang 200, 2400 Mol, Belgium; anne.gobin@vito.be
  <sup>8</sup> Department of Farth and Environmental Sciences, Faculty of Bioscience Engineering, University of Leuven
- Department of Earth and Environmental Sciences, Faculty of Bioscience Engineering, University of Leuven, Celestijnenlaan 200E, 3001 Heverlee, Belgium
- Department of Meteorology, Faculty of Aeronautics and Astronautics, Istanbul Technical University, Maslak, Sarıyer, 34469 Istanbul, Turkey; saylan@itu.edu.tr
- Correspondence: josef.eitzinger@boku.ac.at

Abstract: A one-dimensional simulation model that simulates daily mean soil temperature on a daily time-step basis, named AGRISOTES (AGRIcultural SOil TEmperature Simulation), is described. It considers ground coverage by biomass or a snow layer and accounts for the freeze/thaw effect of soil water. The model is designed for use on agricultural land with limited (and mostly easily available) input data, for estimating soil temperature spatial patterns, for single sites (as a stand-alone version), or in context with agrometeorological and agronomic models. The calibration and validation of the model are carried out on measured soil temperatures in experimental fields and other measurement sites with various climates, agricultural land uses and soil conditions in Europe. The model validation shows good results, but they are determined strongly by the quality and representativeness of the measured or estimated input parameters to which the model is most sensitive, particularly soil cover dynamics (biomass and snow cover), soil pore volume, soil texture and water content over the soil column.

**Keywords:** agrometeorology; soil temperature; simulation model; soil climate; soil freezing and thawing; soil cover effects; agricultural soils

# 1. Introduction

Soil temperature plays an important role in many soil processes and is related to atmospheric, soil and surface conditions. Temperature as one of the driving factors of soil genesis was recognized in the late 19th century by Dokuchaev [1] and independently by Hilgard [2], who listed climate, plants and organisms, the parent material and time as key soil-forming factors. Later, for example, Ellenberg [3] and Gray et al. [4] showed there is a dominant influence of climate and parent material on numerous soil properties. The soil properties, in turn, influence the water and energy transfer, which directly affect the soil temperature, then directly determine the activity levels and survival of soil fauna and



Citation: Grabenweger, P.; Lalic, B.; Trnka, M.; Balek, J.; Murer, E.; Krammer, C.; Možný, M.; Gobin, A.; Şaylan, L.; Eitzinger, J. Simulation of Daily Mean Soil Temperatures for Agricultural Land Use Considering Limited Input Data. *Atmosphere* **2021**, *12*, 441. https://doi.org/10.3390/ atmos12040441

Academic Editor: Francesc Castellví

Received: 22 January 2021 Accepted: 20 March 2021 Published: 29 March 2021

**Publisher's Note:** MDPI stays neutral with regard to jurisdictional claims in published maps and institutional affiliations.



**Copyright:** © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). flora [5]. Soil temperature measurements are critical for calibrating many soil temperature response functions in simulation models [6], since soil temperature and water content affect physical, chemical and soil biological processes [7,8]. A good performance of soil temperature simulation is therefore very important, especially for crop models, which include nutrient balance or models simulating leaching processes and gas emissions from soils. For example, the soil carbon (C) and nitrogen (N) balance is determined by soil temperature and water content [9-11], because they regulate the rate of N-mineralization and, further, the emission of gases from soils [12,13]; C/N balance models are a critical part of most crop growth models, e.g., [14,15]. Many related phenomena are related closely to soil temperatures, such as the effects on soil properties [16], the soil carbon balance under climate change [17], etc. As soil properties and surface conditions vary significantly over space, this creates a big challenge for representative site-specific soil temperature simulations [18,19] as well as for spatial applications of soil temperature models, as shown by, e.g., [6]. Most of the data on near-ground atmospheric conditions are available from in situ weather stations, which are irregularly distributed, creating substantial uncertainties about the spatial distribution, especially for precipitation. However, soil properties and important surface conditions, such as snow cover and plant canopy characteristics [20,21] that influence soil temperatures, are much more difficult to estimate due to their even stronger spatial variability.

Regarding agricultural land use, management factors such as irrigation, soil cultivation and crop management (i.e., harvest, cutting, and mulching) influence soil physical properties and/or soil surface characteristics, affecting soil temperature and wetness [22–24] and can add significant spatial and temporal changes compared to natural or undisturbed land. In conclusion, agricultural management strongly affects the dynamics of soil heat flux and needs to be considered in soil temperature modeling to get the most accurate results for soil processes such as soil respiration [25,26], decomposition rates [27,28], and the microbiological or biotic activity [29,30] of arable lands—all affecting final crop productivity [31,32].

Impact of seasonal snow cover and soil freezing on soil temperature is well documented [33–35] but not sufficiently captured by soil-vegetation-atmosphere-transfer (SVAT) models and most crop models. Neglecting snow cover and freezing effects can lead to significant error in the assessment of the soil temperature's impact on winter crops' development in crop models or the calculation of canopy micrometeorological conditions (canopy air temperature and humidity, leaf temperature and wetness, for example), commonly performed by SVAT models. Currently, numerical weather prediction (NWP) models and climate models [36] implement treatment of snow presence based on the energy balance of the surface (surface albedo) [37], but horizontal spatial grid spacing of these models (particularly the vegetation/land use maps) cannot satisfy the needs for simulations at the field or farm level [38]. However, NWP model outputs can be used as input weather data for more sophisticated soil temperature models, which can operate as standalones or as part of SVAT, crop, or other agrometeorological models.

Inventory of different soil temperature (sub)models of SVAT models offer comprehensive modeling of physical processes by describing soil surface-atmosphere energy transfer and simulating the soil temperature on different levels [39–41]. Due to the time scales of the driving processes (surface exchange of short-wave and long-wave radiation), hourly meteorological data are used. On the other hand, for the process-oriented models used in crop production (such as crop growth and yield models, pest models, irrigation models, agrometeorological models) and for site-specific or spatial applications, only limited sets of hourly input data are available [42]. However, these are not necessary because a daily simulation time step is sufficient for most of these applications [43]. For example, the daily course of temperatures can be assessed from daily extremes of air temperatures. In regard to soil conditions, short-term variations in precipitation, air temperature, or radiation and their impact on soil temperature and wetness are buffered in the soil column, averaging out short-term variations that could affect simulated ecological processes. Therefore, the main objective of our study is the development and validation of a robust and tailored soil temperature model for applications with limited input data requirements (including daily time step of weather data and surface conditions as well as easily available or measurable soil physical data). In this context, reduced uncertainty can be achieved by an optimized balance between model complexity and input data requirements. Furthermore, the model is designed for low computational requirements, allowing for applications for decision-making in crop production as well as applications over larger scales (e.g., using GIS).

The AGRIcultural SOil TEmperature Simulation (AGRISOTES) model developed in our study, is based on model approaches with limited complexity [44–46] in order to calculate daily soil temperatures on different flexible depths using daily weather data and temporal changes of soil surface characteristics as well as soil pore volume, which allows for a consideration of the soil cultivation effects. Considering the specific needs of agricultural applications (such as the living conditions for soil-borne pests), particular attention is further devoted to the parameterization of processes in the presence of soil cover (snow and vegetation) and ice in the soil. AGRISOTES is designed as a tool for a wide range of possible combinations with other ecosystem models or algorithms, measured datasets as well as model implementations.

#### 2. Materials and Methods

#### 2.1. Model Description

In this section, the developed AGRISOTES model will be described. The main model inputs addressing variable temporal conditions (Figure 1) on a daily time step are meteorological elements (mean, maximum and minimum dry-bulb air temperature, solar radiation, and actual evapotranspiration), soil characteristics in order to address soil cultivation events (soil-layer-specific pore volume and soil water content), and soil cover characteristics (snow cover and soil surface biomass), which will allow us to simulate sudden changes of snow or crop cover. Static input parameters include soil texture and configuration parameters, such as simulated soil depth, number of layers and layer thickness, etc. (Figure 1). In general, all input data can be either based on measured data or estimated through other models or simplified algorithms. However, the final selection of input data sources depends on the accuracy and representativeness for the specific application. Our model input scheme allows for maximum flexibility in model application, but it is up to the decision of the model users if a specific type of dataset is suitable for a relevant application. The notations and units of input/output or processed parameters can be found in the Appendix D.

The model consists of two parts: (i) the soil surface temperature module and (ii) the subsurface soil temperature module, which includes heat transport and freezing and thawing of soil water (Figure 2). These two modules are coupled with the ground heat flow at the soil surface. In the soil surface temperature module of AGRISOTES, with respect to snow cover, three different conditions will be described: without snow cover, with dense snow cover and with partial snow cover (limits to be defined as calibrated input).

#### 2.1.1. Soil Surface Temperature: Vegetated Soil Surface without Snow Cover

The calculation of soil surface temperature is based on Best's canopy model [47], which is a simplification of the model proposed by Deardorff (1978), [48]. The plant canopy is treated as a single foliage layer covering a fraction  $v_f$  of the ground surface area. The vegetation cover (or fractional cover)  $v_f$  must be between 0 and 1 and has to be chosen to be representative of the type and amount of aboveground biomass CV (kg ha<sup>-1</sup>).



Soil pore volume: Total soil pore volume in the different soil depths (as specified in configuration parameters)

Figure 1. The AGRIcultural SOil TEmperature Simulation (AGRISOTES) model structure.

The heat balance equation for the soil surface is formulated in the AGRISOTES model in a similar way to that in Herb et al. (2006) [49], as follows:

$$h_{net,g} = \left(1 - \nu_f\right) \left(\left(1 - \alpha_g\right)h_s + \varepsilon_g h_{l,ac}\right) + h_{l,fg} - h_{l,ga} - h_{evap,g} - h_{conv,g}$$
(1)

where  $h_{net,g}$  is the net ground heat flow (W m<sup>-2</sup>),  $\alpha_g$  is the soil surface albedo,  $h_s$  is the observed solar radiation per unit area of the ground surface (W m<sup>-2</sup>),  $\varepsilon_g$  is the soil emissivity,  $h_{l,ac}$  is the incoming atmospheric long-wave radiation (W m<sup>-2</sup>),  $h_{l,fg}$  is the net long-wave radiation from the foliage to the ground (W m<sup>-2</sup>),  $h_{l,ga}$  is the outgoing long-wave radiation emitted from the bare soil (W m<sup>-2</sup>),  $h_{evap,g}$  is the evaporative heat transfer from the soil surface to the atmosphere (W m<sup>-2</sup>) and  $h_{conv,g}$  is convective heat transfer from the soil surface to the atmosphere (W m<sup>-2</sup>).



Figure 2. Heat flow and heat exchange roadmap of AGRISOTES model.

Ì

The convective and evaporative heat flux components between the ground and the canopy are neglected, as in Best's model. As indicated by [49], this simplification is only suitable in the presence of a dense canopy. Therefore, partial canopies are treated here by linearly combining the dense canopy model and the model for bare soil using the vegetation cover factor  $v_f$  in a similar manner as that described by [49].

The soil surface albedo  $\alpha_g$  and soil emissivity  $\varepsilon_g$  are calculated from the surface wetness, as proposed by Van Bavel and Hillel (1976) [50]. The incoming atmospheric long-wave radiation,  $h_{l,ac}$ , is according to [51], expressed as follows:

$$h_{l,ac} = \varepsilon_{ac} \sigma (T_a + 273.15)^4 \tag{2}$$

where  $T_a$  is the air temperature (°C),  $\sigma$  is the Stefan-Boltzmann constant ( $\approx 5.67 \times 10^{-8}$  W m<sup>-2</sup> K<sup>-4</sup>), and  $\varepsilon_{ac}$  is the atmospheric emissivity (Appendix A).

For the calculation of  $h_{l,fg'}$  the soil surface and vegetation layer are considered as two parallel plates for which the net radiation exchange is calculated and scaled with vegetation cover  $v_f$ . Following [52], using air temperature in the vicinity of plants as an approximation for canopy temperature leads to an expression for  $h_{l,fg}$  in the form

$$\mu_{l,fg} = \nu_f \mu_{fg} \sigma \left( (T_a + 273.15)^4 - (T_g + 273.15)^4 \right)$$
(3)

where  $T_g$  is the soil surface temperature (°C) and  $\mu_{fg}$  is the degree of radiation exchange defined as [53]:

$$\mu_{fg} = \frac{1}{1/\varepsilon_f + 1/\varepsilon_g - 1},\tag{4}$$

where  $\varepsilon_f$  is the foliage emissivity. The outgoing long-wave radiation emitted from the bare soil  $h_{l,ga}$  is calculated as

$$h_{l,ga} = \left(1 - \nu_f\right)\varepsilon_g \sigma \left(T_g + 273.15\right)^4.$$
(5)

The evaporative heat transfer  $h_{evap,g}$  from the ground to the atmosphere is roughly approximated to be a fraction  $(1 - v_f)$  of the total evaporative heat transfer (ground + foliage)  $h_{evap}$  (W m<sup>-2</sup>):

$$h_{evap,g} \approx \left(1 - \nu_f\right) h_{evap}.\tag{6}$$

It should be pointed out that Equation (6) is not based on physical principles, but is just a simple approximation using the vegetation cover  $v_f$  to interpolate linearly between two limit cases: the case of bare soil, in which  $v_f = 0$  and  $h_{evap,g} = h_{evap}$ , and the case of full vegetation cover, in which  $v_f = 1$  and the assumption is made that soil evaporation can be neglected ( $h_{evap,g} = 0$ ). This approximation allows the AGRISOTES model to perform its calculations when only actual daily evapotranspiration is provided as input, without knowledge of the splitting up between ground and foliage of the total evaporative heat transfer. In contrast to this, in applications where daily ground evaporation is available as an input, the model accuracy could probably be improved by keeping  $h_{evap,g}$  as a direct model input instead of using the approximation in Equation (6). However, this will, in general, require recalibration of the model, so that the calibration results presented afterwards no longer remain valid.

The convective heat flow from the soil surface to the atmosphere is assumed to occur only from the uncovered fraction of the soil surface (for the covered fraction, convective heat flow is assumed to occur only between the foliage and air) and is expressed by a ground convective heat transfer  $h_{conv,g}$  in the form

$$h_{conv,g} = \left(1 - \nu_f\right) k_{cg} (T_g - T_a) \tag{7}$$

where  $k_{cg}$  is the convective heat transfer coefficient between soil surface and air (W m<sup>-2</sup> K<sup>-1</sup>), which is dependent on the bare soil surface roughness length and the wind speed. In the model,  $k_{cg}$  is considered a direct model input parameter and must either be chosen to be representative of the average wind speed and surface characteristics in the considered region or be determined by model calibration. Combining Equations (1)–(3) and (5)–(7), the heat balance equation for the vegetated soil surface can be written in the form:

$$h_{net,g} = \left(1 - \nu_f\right) \left( (1 - \alpha_g) h_s + \varepsilon_g \sigma \left(\varepsilon_{ac} (T_a + 273.15)^4 - (T_g + 273.15)^4\right) - h_{evap} - k_{cg} (T_g - T_a) \right) + \nu_f \mu_{fg} \sigma \left( (T_a + 273.15)^4 - (T_g + 273.15)^4 \right).$$
(8)

Equation (8) is highly nonlinear with respect to temperature. To calculate  $T_g$  from Equation (8), it is linearized using a first-order Taylor series approximation:

$$\sigma (T_g + 273.15)^4 \approx \sigma (T_a + 273.15)^4 + 4\sigma (T_a + 273.15)^3 \Delta T_g = h_{l0} + k_{l0} \Delta T_g, \qquad (9)$$

where the following abbreviations are introduced:

$$\Delta T_g = T_g - T_a, h_{l0} = \sigma (T_a + 273.15)^4, k_{l0} = 4\sigma (T_a + 273.15)^3, h_{l,g0} = \varepsilon_g h_{l0}, k_{l,g0} = \varepsilon_g k_{l0}.$$

This transforms the heat balance equation into the form

$$h_{net,g} = (1 - \nu_f) \left( (1 - \alpha_g) h_s - (1 - \varepsilon_{ac}) h_{l,g0} - h_{evap} \right) - (\bar{(1 - \nu_f)} (k_{l,g0} + k_{cg}) + \nu_f \mu_{fg} k_{l0}) \Delta T_g.$$
(10)

Equation (10) establishes a relationship between the output variables  $T_g$  and  $h_{net,g}$  and the input parameters of the model. It provides a basis to derive a top boundary condition

for the simulation of soil temperatures within the soil column during snow-free periods. To aggregate the input model variables, the following abbreviations are introduced:

$$k_1 = (1 - \nu_f) (k_{l,g0} + k_{cg}) + \nu_f \mu_{fg} k_{l0},$$
(11)

$$h_{t,1} = \left(1 - \nu_f\right) \left( \left(1 - \alpha_g\right) h_s - (1 - \varepsilon_{ac}) h_{l,g0} - h_{evap} \right).$$
(12)

So, Equation (10) can be rewritten as

$$h_{net,g} = h_{t,1} - k_1 \Delta T_g,\tag{13}$$

or in the form

$$\Delta T_g = \Delta T_1 - R_1 h_{net,g},\tag{14}$$

where  $R_1 = 1/k_1$  and  $\Delta T_1 = h_{t,1}/k_1$ .

To calculate the daily mean soil surface temperature  $T_{g,mean}$ , a daily time averaging procedure is applied to Equation (13) (see in Appendix B) in order to obtain the difference between the daily mean soil surface temperature  $T_{g,mean}$  and the daily mean air temperature  $T_{a,mean}$  in the form

$$\Delta T_{g,mean} = \Delta T_{1,mean} - R_{1,mean} h_{net,g,mean}, \tag{15}$$

which will be used as the top boundary condition for the simulation of soil temperature during snow-free periods.

## 2.1.2. Soil Surface Temperature: Soil Surface with Dense Snow Cover

Dense snow cover affects temperature and soil moisture on a daily basis. In the AGRISOTES model, the calculation of the daily mean soil surface temperature  $T_{g,mean}$  with dense snow cover, is implemented in a similar way to that of the soil surface temperature module of the DAYCENT model [54] as

$$T_{g,mean} = \begin{cases} 0 \ ^{\circ}C & \text{for } T_{a,mean} \ge 0 \ ^{\circ}C, \\ 0.3 \cdot T_{a,mean} \cdot k_{snow} & \text{for } T_{a,mean} < 0 \ ^{\circ}C, \end{cases}$$
(16)

where  $k_{snow}$  is defined as

$$k_{snow} = \max(-0.015 \cdot SNO + 1.0, 0) \tag{17}$$

and *SNO* is the snow water equivalent of the snow layer (mm). By subtracting  $T_{a,mean}$  from Equation (16), it may also be written in the form of Equation (15):

$$\Delta T_{g,mean} = \Delta T_{2,mean} - R_{2,mean} \cdot h_{net,g,mean}, \tag{18}$$

where

$$R_{2,mean} = 0 \text{ m}^2 \text{ K W}^{-1}$$
(19)

and

$$\Delta T_{2,mean} = \begin{cases} -T_{a,mean} & \text{for } T_{a,mean} \ge 0 \,^{\circ}\text{C}, \\ 0.3 \cdot T_{a,mean} \cdot k_{snow} - T_{a,mean} & \text{for } T_{a,mean} < 0 \,^{\circ}\text{C}. \end{cases}$$
(20)

2.1.3. Soil Surface Temperature: Soil Surface with Partial Snow Cover (General Case)

For a given *SNO* value, which is designated as an input to the AGRISOTES model, the snow coverage factor  $v_{sn}$  is calculated as

$$\nu_{sn} = \begin{cases} 0 & \text{for } SNO \leq SNO_{limit,1}, \\ \frac{SNO-SNO_{limit,1}}{SNO_{limit,2}-SNO_{limit,1}} & \text{for } SNO_{limit,1} < SNO < SNO_{limit,2}, \\ 1 & \text{for } SNO \geq SNO_{limit,2}, \end{cases}$$
(21)

where *SNO*<sub>*limit*,1</sub> is the lower limit of *SNO* below which the snow layer is neglected, and *SNO*<sub>*limit*,2</sub> is the upper limit of *SNO* beyond which snow cover is treated as dense (completely covered soil surface).

For partial snow cover, the soil surface is considered to be a surface consisting of patches of vegetated soil surface and soil with dense snow cover. The ground heat flow  $h_{net,g,mean}$  is assumed to be homogeneous with respect to the horizontal surface, whereas the soil surface temperature difference  $\Delta T_{g,mean}$  is assumed to vary according to the local snow cover. Therefore, to obtain an approximation for a horizontally averaged difference in soil surface temperature, a linear combination of Equations (15) and (18) can be used in the form

$$\Delta T_{g,mean} = (1 - \nu_{sn}) \left( \Delta T_{1,mean} - R_{1,mean} h_{net,g,mean} \right) + \nu_{sn} \left( \Delta T_{2,mean} - R_{2,mean} h_{net,g,mean} \right)$$

so that the definitions

$$\Delta T_{mean} = (1 - \nu_{sn})\Delta T_{1,mean} + \nu_{sn}\Delta T_{2,mean}$$
(22)

$$R_{mean} = (1 - \nu_{sn})R_{1,mean} + \nu_{sn}R_{2,mean}$$
(23)

can be used to obtain the following equation, which will be used as top boundary condition for soil temperature simulation when snow cover is present:

$$\Delta T_{g,mean} = \Delta T_{mean} - R_{mean} \cdot h_{net,g,mean}.$$
(24)

2.1.4. Subsurface Soil Temperature: Soil Temperature Equation in Finite-Difference Form

The soil temperatures at different depths are calculated by spatial and temporal discretization of the differential equations for a soil heat flow. The simulated layers are aligned to soil horizon boundaries and thin near the soil surface, with gradually increasing thickness towards the bottom boundary [49]. We applied Fourier's law of heat conduction (Equation (25)) and the energy conservation law in differential form (Equation (26)), including a term accounting for the latent heat of the freezing or thawing of soil water, both tailored for a one-dimensional heat flow:

$$h(z,t) = -\lambda(z,t)\frac{\partial T_s(z,t)}{\partial z},$$
(25)

$$C(z,t)\frac{\partial T_s(z,t)}{\partial t} - F_{H2O}\frac{\partial \theta_{ice}(z,t)}{\partial t} = -\frac{\partial h(z,t)}{\partial z}.$$
(26)

Here, *h* is the soil heat flow (W m<sup>-2</sup>), *T<sub>s</sub>* is the soil temperature (°C),  $\lambda$  is the thermal conductance of soil (W m<sup>-1</sup> K<sup>-1</sup>), *C* is the volumetric heat capacity of soil (J m<sup>-3</sup> K<sup>-1</sup>), *F*<sub>H2O</sub> is the latent heat of ice fusion related to the volume of liquid water ( $\approx 3.34 \times 10^8$  J m<sup>-3</sup>),  $\theta_{ice}$  is the volumetric ice content (cm<sup>3</sup> cm<sup>-3</sup>) in the soil (neglecting volume expansion of frozen water), *z* is the depth (m) and *t* is time (s).

The equations above assume negligible water migration, which can lead to short-term deviations, e.g., after heavy precipitation and on strongly draining soils. An implicit, semidiscrete finite difference scheme to solve these partial differential equations approximately is derived. The simulation domain for the depth *z* in the soil profile is defined as  $[0, z_{max}]$ , where  $z_{max}$  is the depth of the bottom of the simulated soil profile (m). The simulation time step  $\Delta t$  is one day ( $\Delta t = 86400$  s), while every time point  $t_j$  is defined as  $t_j = j\Delta t$ . The evaluation of quantities at time point  $t_j$  will further be denoted by an upper index *j*.

In the further derivations, time averaging will be used in the form  $\widehat{C}^{l}(z)$ , where the bar (<sup>-</sup>) indicates the averaging of variable *C* over the 24-h period [t,  $t + \Delta t$ ], with  $t = t_j$  in this example, while the caret (<sup>^</sup>) indicates approximated quantities. If the soil thermal properties  $\lambda$  and *C* as well as the time-averaged heat flow gradient  $\overline{\partial_z h}$  do not vary significantly during a 24-h period and  $\partial_z h$  is continuous, by applying daily averaging on Equation (25) once and

on Equation (26) twice, it can be concluded that the following semidiscrete finite difference equations hold approximately:

$$\hat{\overline{h}}^{j}(z) = -\hat{\overline{\lambda}}^{j}(z) \cdot \partial_{z} \overline{T}^{j}_{s}(z), \qquad (27)$$

$$\hat{\overline{C}}^{j}(z)\frac{\overline{T}_{s}^{j}(z)-\overline{T}_{s}^{j-1}(z)}{\Delta t}-F_{H2O}\frac{\overline{\theta}_{ice}^{j}(z)-\overline{\theta}_{ice}^{j-1}(z)}{\Delta t}=-\partial_{z}\hat{\overline{h}}^{j}(z).$$
(28)

In Equations (27) and (28), values  $\hat{C}^{j}(z)$  and  $\hat{\lambda}^{j}(z)$  are approximations for  $\overline{C}^{j}(z)$  and  $\overline{\lambda}^{j}(z)$ , defined as

$$\hat{\overline{C}}^{j}(z) = C\left(VP_{sand}(z), VP_{clay}(z), \overline{\theta}^{j}_{sat}(z), \overline{\theta}^{j}(z), \hat{\overline{\zeta}}^{j-1}(z)\right)$$
(29)

and

$$\hat{\overline{\lambda}}^{j}(z) = \lambda \left( VP_{sand}(z), VP_{clay}(z), \overline{\theta}^{j}_{sat}(z), \overline{\theta}^{j}(z), \hat{\overline{\zeta}}^{j-1}(z) \right),$$
(30)

where  $\overline{\zeta}$  is the approximate daily mean ice fraction, defined as

$$\hat{\overline{\zeta}}^{j}(z) = \frac{\overline{\theta}^{j}_{ice}(z)}{\overline{\theta}^{j}(z)},$$
(31)

with  $\theta$  denoting the volumetric water content (cm<sup>3</sup> cm<sup>-3</sup>), while the five-parametric  $C(VP_{sand}, VP_{clay}, \theta_{sat}, \theta, \zeta)$  and  $\lambda(VP_{sand}, VP_{clay}, \theta_{sat}, \theta, \zeta)$  functions denote the soil thermal property calculation procedures, which are additionally dependent on the volume percentages of clay  $VP_{clay}$  (%) and sand  $VP_{sand}$  (%) relative to the total solid matter and the saturated volumetric water content  $\theta_{sat}$  [55]. To calculate the thermal properties of the soil, the method described for the model SWAP version 3.2 [55], which is based on [56–60] was used, together with some enhancements to treat the case of partially or totally frozen soil.

The application of the finite difference method to solve partial differential equations generally requires sufficient differentiability of the involved space- and time-dependent quantities. Therefore, regularization techniques have been used for the numerical solution of Equations (27) and (28). In particular, the ideally discontinuous dependence of  $\zeta$  on  $T_s$  (see Section 2.1.6) has been replaced by a smoothed function that does not differ significantly from the idealized behavior but is sufficiently often differentiable to allow the application of the finite difference method for the spatial discretization of Equations (27) and (28). Spatial discontinuities of soil texture properties at the boundary between soil horizons, as long as they are not moving and their depths are known, are allowed in our model and have been appropriately accounted for in the numerical implementation.

#### 2.1.5. Subsurface Soil Temperature: Top and Bottom Boundary Conditions

To formulate the top boundary condition for the finite difference scheme approximation of soil heat flow, the soil surface heat balance (Equation (24)) must be incorporated, which is approximated for the finite-difference scheme using the formulation

$$\overline{T}_{s}^{j}(0) = T_{a,mean}^{j} + \Delta T_{mean}^{j} - R_{mean}^{j} \cdot \overline{h}^{j}(0).$$
(32)

.

For the bottom boundary condition, three different modes are available for the soil temperature model:

- (i) To set the approximated daily mean heat flux  $\hat{h}'(z_{max})$  at the bottom of the simulated soil profile to zero;
- (ii) To fix the temperature at the bottom of the soil profile to the annual mean air temperature  $T_{AA}$  (°C), which is an input to the model; and

(iii) To assume that the soil thermal properties  $\lambda$  and C and the ice content  $\theta_{ice}$  near the bottom of the soil profile are constant over z and t for depths  $z \ge z_{max}$  and that the temperature at the bottom of the soil profile varies sinusoidally with a one-year period around a mean value of  $T_{AA}$ . With the angular frequency of a year  $\omega_a$  (rad s<sup>-1</sup>) and the approximated damping depth at the bottom of the soil profile  $d_a^j(z_{max})$  (m) for annual frequency, this leads to the following bottom boundary condition (detailed derivation can be found in Appendix C):

$$-\partial_{z}\overline{T}_{s}^{j}(z_{max}) = \frac{1}{d_{a}^{j}(z_{max})} \left( \left(1 - \tan\left(\frac{\omega_{a}\Delta t}{2}\right)\right) \left(\overline{T}_{s}^{j}(z_{max}) - T_{AA}\right) + \frac{\overline{T}_{s}^{j}(z_{max}) - \overline{T}_{s}^{j-1}(z_{max})}{\sin(\omega_{a}\Delta t)} \right).$$
(33)

Simulations at site Groß-Enzersdorf, which is located northeast of Vienna, Austria (see Section 2.2), representing a Central European semihumid climate, have shown that the first two modes for bottom boundary conditions were only applicable to depths greater than approximately 10 m. The third mode for the bottom boundary condition was applicable even at lower depths of approximately 2.5 m. Therefore, when simulation results of the soil temperature at depths between 2.5 m and 10 m are not required, the third bottom boundary condition mode can be used to reduce the computing time of the soil temperature simulation.

#### 2.1.6. Subsurface Soil Temperature: Treatment of Freezing/Thawing of Soil Water

Figure 3 shows an idealized graph for some fixed depth *z* (neglecting freezing-point depression) of the dependence of soil temperature and ice content on heat energy density w (J m<sup>-3</sup>). The zero-point of *w* is defined as the state where  $T_s = 0$  °C and  $\theta_{ice} = 0$ . It can be seen what occurs if the soil at first has a temperature  $T_{s,1}$  and ice content  $\theta_{ice,1}$  and the heat energy density changes by  $\Delta w$ , so that afterwards, the soil has temperature  $T_{s,2}$  and ice content  $\theta_{ice,2}$ .



Figure 3. Dependence of soil temperature and ice content on heat energy density.

As can be seen, during time periods in which the soil is partially frozen ( $0 < \theta_{ice} < \theta$ ), the temperature stays constant at 0 °C. For  $T_s > 0$  °C, the soil is unfrozen, so  $\theta_{ice} = 0$  and the derivative of  $T_s$  with respect to w is given as  $1/C_{unfrz}$ , where  $C_{unfrz}$  is the volumetric heat capacity for unfrozen soil. For  $T_s < 0$  °C, the soil is completely frozen, so  $\theta_{ice} = \theta$  and the derivative of  $T_s$  with respect to w is given as  $1/C_{frz}$ , where  $C_{frz}$  is the volumetric heat capacity for completely frozen soil. It should be noted that the shape of the curves in Figure 3 depends on the soil water content  $\theta$ , as well as on soil composition and pore volume.

Considering the daily mean soil temperature  $\overline{T}_s$  and ice content  $\overline{\theta}_{ice}$ , their behavior is comparable to, but not the same as that shown in Figure 3 for  $T_s$  and  $\theta_{ice}$ . Due to the diurnal variation of  $T_s$  and  $\theta_{ice}$ , on some days  $\overline{T}_s > 0$  °C, but during some night hours, freezing may occur so that, nevertheless,  $\overline{\theta}_{ice} > 0$ . Since it is not possible to take into account precisely such effects in a model that is only dealing with daily averaged quantities, the following assumptions are introduced:

$$\overline{T}_{s}^{j}(z) > 0 \,^{\circ}\mathrm{C} \Rightarrow \overline{\theta}_{ice}^{j}(z) = 0, \tag{34}$$

$$\overline{T}_{s}^{j}(z) < 0 \,^{\circ}\mathrm{C} \Rightarrow \overline{\theta}_{ice}^{j}(z) = \overline{\theta}^{j}(z).$$
(35)

The above approach is an approximation and, therefore, in the simulation, particularly during those days on which soil water freezing starts or ends (considering some fixed depth z), greater deviations of simulated daily mean soil temperature and ice content from the real values can occur (see validation results in Figure 6). As has already been mentioned in Section 2.1.4, the discontinuous dependence of  $\hat{\zeta}$  on  $\overline{T}_s$  resulting from Equations (34) and (35) was replaced by a similar smoothed function for the numerical implementation of the model. In summary, the applied simplifications as described above can lead to short-term deviations, especially due to sudden changes in surface conditions (e.g., timing of snow or vegetation cover), extreme weather impacts such as heavy precipitation, which can influence additionally heat transport in soils, and deviations of the freezing status of soil layers.

## 2.2. Calibration and Validation Sites

AGRISOTES was calibrated and validated at different sites with various climates, soils and agricultural land uses in Austria, Belgium, Turkey and the Czech Republic (Table 1). Table 1 presents an overview and comparison of the primary sites, from which measured daily soil temperature time series were available. Site conditions and measured/estimated/simulated model input parameters are indicated. Further details on site conditions are presented with the results.

For all sites, the measured physical soil properties (texture and soil pore volume) were available from up to four depths over the vertical soil profile, which were used as direct inputs and assumed to represent the full soil column. As a daily input, soil pore volume at all soil layers was assumed to be constant over the validation periods due to lack of temporal data. In some cases, the soil water content was simulated (S) using the data of on-site or nearby weather stations by the FAO model approach [61]. In all cases, daily actual evapotranspiration was simulated for AGRISOTES input using the FAO model approach as well. The daily input of soil surface dry matter dynamics was estimated (E) at most validation sites based on reported biomass at harvest and according to linear interpolation between phenological development stages [61] or by direct measurements during the growth period (M).

**Table 1.** Main characteristics of site conditions used for generating representative inputs for the AGRIcultural SOil TEmperature Simulation (AGRISOTES) model for the calibration and validation periods (all sites characterized by no or only negligible slope inclination and no shading from larger structures).

Site	Soil and Surface Management	Station Type	Annual Means of Temperature and Precipitation (1981–2010)	Main Soil Type	AGRISOTES Model Inputs M: Measured at Site E: Indirectly Estimated S: Simulated from Measured Weather Data				
					Met <sup>1</sup>	Soil <sup>2</sup>	θ <sup>3</sup>	CV <sup>4</sup>	
Groß-Enzersdorf Northeast Austria (Calibration)	Arable – Bare soil and straw mulch	Field experiment station	10.3 °C – 516 mm	Para-chernosem	М	E/M <sup>5</sup>	М	М	
Goggendorf Northeast Austria (Validation)	Arable – Bare soil and fallow after winter wheat	Field experiment station	9.2 °C – 519 mm	Chernosem	М	М	S	Е	
Doksany Northwest Czech Republic (Validation)	Permanent short grass	Long term field experiment station	9.5 °C – 466 mm	Chernosem	М	М	М	Е	
Pucking Northwest Austria (Validation)	Arable – Crop rotation	Lysimeter	9.1 °C – 790 mm	Cambisol	М	М	S	Е	
Kirklareli, Thrace region, Turkey (Validation)	Winter wheat/Bare soil and fallow after winter wheat	Field experiment station	13.3 °C – 570 mm	Vertisol Cambisol	М	М	М	М	
Hamme, Belgium (Validation)	Permanent short grass	Field experiment station	10.6 °C – 852 mm	Eutric Fluvic Gleyic Cambisol	М	М	Е	Е	
Purbach East Austria (Validation)	Arable – Vineyard	Field experiment station	10.4 °C – 758 mm	Chernosem	М	М	S	Е	
Grafendorf Southeast Austria (Calibration of snow cover effect/Validation)	Permanent grassland (3–cut)	Field experiment station	9.4 °C – 716 mm	Cambisol	М	E/M <sup>6</sup>	М	Е	
Obersiebenbrunn Northeast Austria (Validation)	Natural grassland		10.3 °C – 516 mm	Chernosem	М	М	S	Е	

<sup>1</sup> Meteorological input parameters: Daily mean, maximum and minimum temperature, and solar radiation (global radiation), <sup>2</sup> Soil: Sand and clay content ( $VP_{sand}$ ,  $VP_{clay}$ ) and total soil pore volume (measurement samples from up to four soil depths), <sup>3</sup>  $\theta$ : Volumetric soil water content (measurements based on 1–2 soil depths), <sup>4</sup> CV: Total above ground dry biomass, <sup>5</sup> Soil texture estimated from soil map (mean value over soil profile), <sup>6</sup> Estimated for calibration of snow cover effect, but measured for validation.

# 3. Results and Discussion

#### AGRISOTES Model Calibration, Validation and Sensitivity Analysis on Daily Mean Soil Temperatures

A calibration of two important model parameters was performed based on measured soil temperatures in a field trial (Groß-Enzersdorf, Austria). Calibration was carried out for arable (plowed) land with bare soil and with different straw mulch coverage to estimate the dampening effect of total aboveground dry matter biomass, CV (Table 2) as well as the convective heat transfer coefficient ( $k_{cg}$ ) for bare soil (Table 3).

**Table 2.** Calibrated cover effect factor ( $v_f$ ) for total aboveground dry matter biomass (CV; based on straw mulch).

$CV$ (kg ha $^{-1}$ )	$v_f$ (Dimensionless)
0	0
2500	0.848
4000	0.933
5000	0.965

Table 3. Model parameters based on the calibration sites.

Parameter	Unit	Calibrated Value	First Estimate (Value Used in Subsequent Simulations)
k <sub>cg</sub>	${ m W}~{ m m}^{-2}~{ m K}^{-1}$	42.0	41.0
β	ha kg $^{-1}$	0.000729	0.000663
ε <sub>f</sub>	1	0.95	0.95
SNO <sub>limit,1</sub>	mm H <sub>2</sub> O	0.3	0.4
SNO <sub>limit,2</sub>	$mm H_2O$	13.8	13.8

Taking the form of Equation (2) in [62], a simple exponential curve was fitted for the data in Table 2. The resulting relationship was

$$\nu_f(CV) = 1 - \exp(-\beta \cdot CV),\tag{36}$$

with  $\beta$  given in Table 3. This relationship can be used to interpolate for values of *CV* other than the calibrated ones, but care needs to be taken for very low values, i.e., less than 2000 kg ha<sup>-1</sup>, because gaps can occur in canopies under these conditions. For other types of biomass coverage (e.g., living crops), different values of  $v_f$  (in relation to *CV*) may apply depending on the canopy structure; however, the validation showed good results in our case for grassland and wheat canopy (see Table 4 and Table 6).

The value for  $k_{cg}$  (convective heat transfer coefficient from the soil surface to air) was first optimized for bare soil with  $v_f$  set to zero (for the obtained value of  $k_{cg}$  see Table 3). Then,  $k_{cg}$  was fixed, and optimal values for  $v_f$  were estimated for the mulch-covered trial.

In Table 3, the calibrated model parameters are given. The value of  $\varepsilon_f$  was not optimized, but taken from [49]. The values of  $SNO_{limit,1}$  and  $SNO_{limit,2}$  were taken from parameter optimizations from a grassland site with regular snow cover occurrence (Grafendorf), since the calibration at the other site (Groß-Enzersdorf) was performed only during snow-free periods.

Location	Surface Conditions	Simulation Period	Available Days	Soil Depth (cm)	R	σ₀ (°C)	σ <sub>s</sub> (°C)	RMSE (°C)	RRMSE (%)	IA (0–1)
Groß- Enzersdorf Calibration	$4 \times 4$ m plot bare soil after seedbed preparation	1 April–24 May 2012	54	10	0.98	4.45	4.59	0.89	6.3	0.99
Goggendorf Validation	$4 \times 4$ m plot bare soil in winter wheat stand since 22 June; soil water content simulated	22 June–9 December 2016	116 116 109 117	5 10 20 40	0.999 0.999 0.99 0.99	8.87 8.79 8.07 6.73	8.63 8.31 7.75 6.66	1.21 1.17 1.01 0.59	8.2 7.9 7.2 4.1	0.99 0.99 0.99 0.99
	Winter wheat, 15 August harvest –stubble field – 20 September soil mulching– Soil water cont. simulated	22 June–9 December 2016	123 123 123	5 20 40	0.999 0.999 0.999	7.47 6.71 5.87	7.55 6.77 5.71	0.69 0.55 0.42	5.2 4.1 3.1	0.99 0.99 0.99

Table 4. Soil temperature model calibration/validation on study specific field experiments.

The goal of the optimizations was to reduce the root-mean-square-difference between simulated and measured daily mean soil temperatures near the soil surface. However, the presented calibration result can be understood as a first guess only, because our available calibration data sets are based on field measurements, which are related to inherent uncertainties, especially due to the nature of inhomogeneous physical properties of soils. Extended model calibrations are therefore recommended for other different sites to ensure the maximum accuracy of simulation results (where the number of measured parameters and measurement quality are considered as suitable, including soil physical parameters, daily LAI, canopy or snow cover gaps, and biomass measurements). In our case, a correction for the value of volumetric heat capacity of air has been made in the soil thermal property calculation routine of the model after a first parameter estimation. This caused a change in the calibrated model parameter values compared with their first estimates (Table 3), which were determined before the model correction. The parameter change, however, showed only very marginal effects on the simulation results. Therefore, all simulation results shown subsequently were generated using the corrected model version but with the first estimates of the model parameters since they were available earlier. The main limitation, however, is the limited availability of calibration data sets of suitable quality.

The quality of model calibration and validation was tested using: (a) R—the coefficient of determination between observed and simulated values; (b)  $\sigma$ —the standard deviation of observed ( $\sigma_0$ ) and simulated values ( $\sigma_s$ ); (c) RMSE—the root mean square error; (d) RRMSE—the relative RMSE and e) IA—the index of agreement [63]. According to [64], the simulation is performed more realistic if: (a) RMSE is less than the standard deviation of observed values,  $\sigma_0$ , and (b) the standard deviation of simulated values,  $\sigma_s$ , is close to the standard deviation of observed values,  $\sigma_0$ . Also, good model performance is indicated if the index of agreement is close to 1 [63]. Furthermore, the model accuracy is considered excellent when RRMSE < 10%, good if 10% < RRMSE < 20%, fair if 20% < RRMSE < 30%, and poor if RRMSE > 30% [65].

Results of the model for bare soil for Groß-Enzersdorf and Goggendorf are shown in Figures 4 and 5, and related statistics are shown in Table 4.



**Figure 4.** Measured and simulated daily mean soil temperatures at a soil depth of 10 cm in Groß-Enzersdorf (Austria) under bare soil conditions (prepared seedbed) from 1 April to 24 May 2012 (DOY = Day Of Year).



**Figure 5.** Measured and simulated daily mean soil temperatures at a soil depth of 20 cm in Goggendorf (Austria) under bare soil conditions and a winter wheat canopy from 22 June until 31 December 2016 (DOY = Day of Year).

Calibration site statistics over the whole simulation period for Groß-Enzersdorf (Table 4) indicate good model performance: R and IA are close to 1, the RMSE is far below  $\sigma_o$  and  $\sigma_s$  is just 0.14 °C higher than  $\sigma_o$ . RRMSE is well below 10%, indicating excellent model performance.

Validation using a controlled experiment was carried out for a site with arable soil (Goggendorf), with similar conditions to the site of Groß-Enzersdorf. Two stations were placed within a wheat field, representing bare soil and wheat field surface biomass dynamics. The aboveground biomass of the full canopy of standing wheat was estimated from measured yield (set as 7000 kg ha<sup>-1</sup> dry matter biomass), and soil porosity and texture at three soil depths were measured once (kept constant during the simulation period), while the daily soil water content and actual evapotranspiration were simulated using the FAO approach [61]. The FAO approach is based on calculating the actual evapotranspiration of crop canopies from grass reference evapotranspiration by using correction factors, which depend on soil water content and crop development. Stubble after wheat harvest was set to 1000 kg ha<sup>-1</sup> (straw was removed from field after harvest). Table 4 shows similar performance statistics for Goggendorf for R and IA as at the Groß-Enzersdorf site. For both variants,  $\sigma_0$  and  $\sigma_s$  decreased with depth, following the temperature trend. For both bare soil and vegetated surface simulations in Goggendorf, the RRMSE was slightly higher for bare soil, decreased with depth, and was always well below 10%.

These results, further supported by Figure 5 for the 20 cm soil depth, show that the model can represent soil temperatures within a deviation range of 2 °C on a daily basis at a 20 cm soil depth, considering the existing uncertainties in inputs on soil surface biomass and soil characteristics (simulated soil water content, constant porosity, and soil texture).

As solar radiation interception into canopies and related energy transfer to the soil surface vary not only by canopy structure but also between diffuse and direct solar radiation, Table 5 shows a comparison of AGRISOTES performance for days with high versus low solar radiation. Due to the simplified approach used in AGRISOTES (Equation (1)), some differences in model behavior can be expected. Using our database, including four different sites with different canopy conditions (Table 1), we found that on the simulation days with a higher radiation level (7–15 MJ m<sup>-2</sup> d<sup>-1</sup> vs. > 20 MJ m<sup>-2</sup> d<sup>-1</sup>), the model performance is slightly lower (in the range of 0.09 °C to 0.52 °C in RMSE) for both grassland and arable land. However, in order to better calibrate this function, detailed canopy characteristics and light interception data would be necessary.

Site Name	Soil Depth		$7-15 MJ m^{-2} d^{-1}$		>20 MJ m <sup>-2</sup> d <sup>-1</sup>
	cm	n	RMSE (°C)	n	RMSE (°C)
Doksany, CZ	5	1366	1.36	1207	1.88
Kirklareli, TR	20	724	1.25	560	1.71
Hamme, BE	15	1000	1.85	837	2.15
Grafendorf, AT	10	1717	1.15	1630	1.24

**Table 5.** Model performance (measured as RMSE,  $^{\circ}$ C) in response to daily solar radiation level (global radiation of 7–15 MJ m<sup>-2</sup> d<sup>-1</sup> vs. > 20 MJ m<sup>-2</sup> d<sup>-1</sup>) for four simulation sites as described in Table 1 (n = number of affected days).

For the Goggendorf site, we carried out a model sensitivity analysis of the most important parameters for soil temperature simulation dynamics, including surface biomass, soil layer specific soil water content, soil porosity, and soil texture. We defined an artificial simple stepwise change with the most likely realistic ranges for these parameters in agricultural soils, as shown in Table 6.

The model sensitivity analysis demonstrates that uncertainties in the soil water content may have less impact on model performance than soil porosity and sand content within the often observed vertical and horizontal variations in the soil column of soils under field conditions. The highest impact on soil temperature and its simulation is from the dynamics of soil surface biomass cover under common field conditions (see also Figure 5). The sensitivity to the changing sand content increases with soil depth, whereas the sensitivity to the soil surface biomass affects all depths to the same extent (Table 6).

Finally, for the model validation on a wider range of soil and surface conditions, independent datasets of several years at different sites were used to demonstrate the model performance under various conditions of input data availability and quality. The selected sites include different climates, agricultural soils, and land use, where for model parameterization the local available data were used (such as annual temperature and soil characteristics). The sites are located in Austria, the Czech Republic, Belgium, and Turkey. In all cases, the model input "actual evapotranspiration" was calculated based on the Penman-Monteith equation according to the FAO approach [61]. If measured data were not available, the soil water content input was also calculated by the FAO approach [61]. Snow cover was calculated by the model Snow Mouse [66] when measured data were not available. The statistics of model performance at all validation sites are shown in Table 7.

It can be seen that the various uncertainties and indirect estimates of critical soil temperature model inputs are reflected in the performance of results. As expected, most errors can occur when the dynamics of surface biomass are not measured or are difficult to estimate. For example, in the vineyard and permanent grassland sites in Purbach and Obersiebenbrunn, respectively, an increase in the RRMSE, accompanied by a higher deviation between  $\sigma_0$  and  $\sigma_s$  (e.g., 6.88 and 7.66, respectively at 10 cm soil depth in Obersiebenbrunn), is caused by temporal deviation of simulated near soil surface temperatures from measurements (not shown). It seems that known grassland cutting dates and related calculated biomass dynamics contribute to a better performance, such as at sites Doksany and Grafendorf, where the RRMSE values are mostly well below 15. Even at site Pucking, where there was rotation of various crops, and the biomass dynamics were calculated using a simple linear approach based on [61] according to exact dates of growing periods of the different crops, an acceptable result was achieved. Conversely, soil parameter uncertainty and their variation over the vertical soil profile led to deviations, especially in deeper soil layers, such as those at Purbach and Grafendorf. In fact, the physical soil properties for the deeper soil layer of these two sites were extrapolated from the next shallower soil layer. Furthermore, we found that soil conditions beyond the common range for agricultural soils, such as gravel, are not well represented by the current model parameterization (data not shown).

# Atmosphere 2021, 12, 441

Reference Simulation <sup>1</sup>	Reference Conditions	Soil Depth (cm)	Soil Water Content +10 vol %	Soil Water Content –10 vol %	Porosity +10 vol %	Porosity -10 vol %	SBM <sup>2</sup> +1000 kg ha <sup>-1</sup>	SBM <sup>2</sup> -1000 kg ha <sup>-1</sup>	Sand +55% (Ref: 10%)					
		$\Delta$ °C—July 2016 mean deviation from reference												
		5	0.06	-0.09	-0.04	0.05	-0.15	-0.19	-0.07					
		10	0.05	-0.09	0.00	0.02	-0.15	-0.17	-0.17					
		20	0.01	-0.08	0.04	-0.04	-0.14	-0.12	-0.33					
	Fallow after winter	40	-0.02	-0.08	0.11	-0.11	-0.15	-0.07	-0.57					
	wheat–15 August	60	-0.03	-0.09	0.13	-0.14	-0.18	-0.04	-0.75					
Simulation period:	harvest – straw	100	-0.02	-0.11	0.10	-0.13	-0.23	0.00	-0.90					
1 January 2016 till 31	mulch – 20				$\Delta \circ C$ —Octob	er 2016 mean devia	ation from reference							
December 2016	September soil	5	-0.10	0.07	0.05	-0.07	-0.35	0.58	-0.02					
	mulching	10	-0.08	0.06	0.01	-0.03	-0.34	0.57	0.10					
		20	-0.04	0.04	-0.05	0.03	-0.35	0.53	0.26					
		40	0.03	0.00	-0.17	0.16	-0.35	0.47	0.58					
		60	0.08	-0.02	-0.27	0.26	-0.33	0.41	0.91					
		100	0.15	-0.06	-0.41	0.42	-0.31	0.29	1.45					

Table 6. Basic model sensitivity analysis of the effect of the main important model input parameters on simulated soil temperature at the Goggendorf validation site (see also Table 4).

<sup>1</sup> All sensitivity test input factors modified in respect to the reference. <sup>2</sup> SBM: Surface dry biomass change, reference in July = 4000 kg ha<sup>-1</sup>, in October = 1000 kg ha<sup>-1</sup> (straw-soil mulch).

Table 7. Model validation results based on available data sets (see Table 1 for site characteristics).

Location and Soil Surface	Not Directly Measured Settings/Inputs	Simulation Period	Available Days	Soil Depth (cm)	R	σ <sub>ο</sub> (°C)	σ <sub>s</sub> (°C)	RMSE (°C)	RRMSE (%)	IA (0–1)
Doksany – Permanent short grass	Constant surface biomass assumed	Full years 2001–2004	1454 1454 1454	5 50 100	0.98 0.99 0.99	8.42 6.75 5.17	8.41 6.70 5.24	1.65 0.97 0.87	15.0 9.2 8.2	0.99 0.99 0.99
Kirklareli – Winter wheat/fallow	Constant pore volume assumed	Full years 2010–2011	714 714	5 20	0.99 0.99	8.23 7.57	8.69 8.11	1.57 1.45	10.7 10.0	0.99 0.99
Hamme – Permanent Short grass	Constant soil water content and surface biomass assumed	Full years 2012–2014	1096	15	0.96	5.60	5.64	1.94	15.5	0.97

lable 7. Cont.											
Location and Soil Surface	Not Directly Measured Settings/Inputs	Simulation Period	Available Days	Soil Depth (cm)	R	σ <sub>0</sub> (°C)	σ <sub>s</sub> (°C)	RMSE (°C)	RRMSE (%)	IA (0–1)	
Pucking – Cultivated soil on lysimeter	Constant pore volume Crop rotation related surface biomass and soil	Sept 1996–Feb 1999	745 854	10 30	0.97 0.99	6.32 6.86	6.36 6.32	1.59 1.25	21.7	0.98	
	water content calculated		001		0.77	0.00	0.02				
			941	10	0.99	7.67	7.72	2.20	23.8	0.98	
Purbach – Cultivated soil under	Constant pore volume and surface biomass (3000 kg ha <sup>-1</sup> ) Soil water content calculated	July 1999–May 2002	941	20	0.99	7.66	7.30	1.19	11.4	0.99	
vineyard			941	40	0.99	7.43	6.49	1.30	12.1	0.99	
			941	70	0.99	7.22	5.45	2.06	19.0	0.97	
			1714	10	0.98	7.11	6.98	1.45	12.9	0.99	
Grafendorf – 3–cuts	Surface biomass		1744	20	0.98	6.88	6.52	1.24	11.1	0.99	
Permanent	calculated	Years	1744	30	0.99	6.59	6.09	1.13	10.2	0.99	
grassland	according to	2004-2007	1739	40	0.99	6.37	5.69	1.13	10.3	0.99	
0	reported cuts-Snow cover simulated		1744	60	0.99	5.26	5.16	0.91	8.3	0.99	
Obersieben-brunn – Permanent	Constant surface biomass assumed (3000 kg ha <sup><math>-1</math></sup> )	Years	2557	10	0.98	6.88	7.66	2.56	28.9	0.97	
natural grassland	Soil water content calculated	2000-2009	2557	50	0.99	5.80	5.23	1.11	10.2	0.99	

Table 7 Co

From the weather inputs, the existence of snow cover is the most critical component for a representative simulation of soil temperatures during the winter period. This is especially clear for Grafendorf and Doksany, in Figures 6 and 7, respectively. The site Grafendorf is characterized by a semihumid climate, with regular snow cover during the winter. Figure 6 shows the model performance for the selected soil depth of 10 cm over a four-year period. The overall performance is good, but there are temporal underestimations of simulated soil temperatures during the growing periods, which result from the fact that the grassland surface biomass was calculated according to the reported cutting dates. The largest short-term deviations occur during the winter period and are caused by inadequate (simulated) snow cover duration, which is an input to the soil temperature model. The majority of the daily variation range is below 1 °C.



**Figure 6.** Measured and simulated daily mean soil temperatures at the 10-cm soil depth in Grafendorf (Austria) under a grassland three-cut regime from 2004 to 2007.



# a) Daily mean soil temperatures at 5 cm soil depth

Figure 7. Cont.



Figure 7. Cont.



**Figure 7.** (**a**–**d**). Comparison of measured and simulated daily mean soil temperatures at three climatologically different sites in Belgium, the Czech Republic, and Turkey over the full measured temperature ranges (statistics shown in Table 7).

Figure 6 demonstrates the performance of the simulations over a four-year period for the Grafendorf site, including information on snow cover duration. A strong effect of snow cover on the underlying soil temperatures and a freeze/thaw effect (soil temperatures stay close to zero during ongoing freezing or thawing) can be seen; however, it is difficult to meet the conditions of a not fully frozen or fully frozen state, so that deviations occur more frequently. The impact of snow cover and soil freezing on simulated soil temperature is, as expected, much more pronounced at the upper layer than in deeper soil layers, leading to better model performance in deeper soil layers, e.g., decreasing RMSE and RRMSE (see Table 7 for statistical results). Furthermore, the greatest deviations between measured and simulated soil temperatures are related to sites with periods of snow cover occurrence and/or soil freezing events (see Figure 7a—a site with regular soil frost versus Figure 7c—a site without significant soil frost). Especially at the freezing point (around 0 °C), deviations occur (see also Figures A1–A18 of nine validation sites in Appendix E).

In general, also the representation of surface dry biomass (SBM) can contribute to deviations and uncertainties (see sensitivity analysis, Table 6), where a deviation of about 1000 kg ha<sup>-1</sup> SBM leads to a change of up to 0.6 °C in mean monthly soil temperature. Especially during the crop growing period, this parameter is continuously changing and deviations increase when it is assessed and/or kept constant in the simulation (as at Doksany and Hamme, Figure 7a,b, and other sites, as statistically presented in Table 7, when, e.g., RRMSE values in the top soil layers rise above 15%). The effect of solar radiation levels on model performance is presented statistically in Table 5 and visually for the wellmonitored site in Kirklareli, Turkey in Figure 7c,d. It can be seen that, with increasing radiation, the model performance declines, e.g., for levels above 20 MJ m<sup>-2</sup>, yielding RMSE values of 1.24-2.15 °C, depending on the site.

Additional validation results for nine independent Czech soil temperature measurement sites for 10 cm and 50 cm soil depth, respectively, are presented in Appendix E (Figures A1–A18). These sites are characterized by grass cover that is kept at or below 10 cm. At these sites, the soil physical characteristics (especially soil pore volume, wilting point and field capacity) were derived from FAO soil map and soil type description (Table A1, Appendix E). Therefore, larger biases can be expected for these sites due to larger input data uncertainty as other AGRISOTES inputs (e.g., soil water content and evapotranspiration) were simulated by the FAO approach based on these data as well. These additional uncertainties lead to higher RMSE values (overall in the range of 1-2 °C; Table A2, Appendix E) compared to our other validation sites (Table 7) where mostly in situ-based soil characteristics were available (Table 1). However, the overall performance of the simulation results are satisfactory over the whole temperature range in view of these uncertainties, and useable for many applications in crop management (e.g., assessing optimum sowing time, soil born pest activities, N-mineralization rates, etc.). Accepted applicability for farmers, however, depends on the specific use cases, which need to be tested before implementation.

## 4. Conclusions

According to the results of the AGRISOTES model validation performed for different European climatic conditions, land use, soil type, biomass development, snow presence and freezing conditions, it can be concluded that the model:

- (a) is able to produce a smooth transition between bare soil and vegetated surface at the beginning of the vegetation period, as well as after sudden surface condition changes such as harvest;
- (b) represents the influence of surface biomass dynamics on soil temperatures with acceptable accuracy for many agricultural applications;
- (c) RMSE is higher for bare soil than for vegetated surfaces and intensively decreases with depth, indicating that the model is more sensitive to atmospheric forcing (a stronger effect on bare soil) than to the given soil characteristics and the parameterization of the energy transport over the whole profile;
- (d) is highly sensitive to the presence of snow cover; and
- (e) reflects well the most determining soil physical factors such as porosity, soil texture and soil water content. Soil surface conditions, however, remain the greatest influence under agricultural land use.

However, currently, there are still potential limitations on the application of AGRISOTES in different climate zones and under various types of surface conditions. For example, under tropical and other climates and surface conditions such as in wetlands, deserts or forests, AGRISOTES should be evaluated on extended suitable data sets. If the model applicability seems to be given, at least a validation should be carried out first. Based on these validation results, if necessary, a recalibration of the model should be considered, especially of the  $v_f(CV)$ -relationship. In general, we recommend testing with highly accurate measured input datasets for calibration that reflect the greater variability of canopy structure and crop types.

Author Contributions: Conceptualization, J.E.; methodology, J.E., P.G., B.L.; software, P.G.; calibration and validation, J.E., J.B., P.G., B.L.; resources, J.E., M.T.; data curation, J.E., M.T., J.B., E.M., C.K., M.M., A.G., L.Ş.; writing—original draft preparation, P.G., J.E.; writing—review and editing, P.G., J.E., B.L., M.T.; visualization, P.G., J.E.; supervision, J.E.; project administration, J.E.; funding acquisition, J.E., B.L., M.T. All authors have read and agreed to the published version of the manuscript.

Funding: See Acknowledgement.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

**Data Availability Statement:** Available data sets used for this study can be requested from the corresponding author.

Acknowledgments: The research work described in the paper was carried out through support from several projects. The database, model development, simulations, and results analysis were supported by projects CLIMSOIL and AGROFORECAST of the Austrian Climate Research Program (ACRP). The authors acknowledge the financial support of the Ministry of Education, Science and Technological Development of the Republic of Serbia (Grant No. 451-03-68/2020-14/200125). Results analysis and manuscript development were supported by project H2020-TWINNING-SERBIA FOR EXCELL, which has received funding from the European Union's Horizon 2020 research and innovation program under grant agreement no. 691998. The database and simulations were also supported by the SustES project—Adaptation strategies for sustainable ecosystem services and food security under adverse environmental conditions (CZ.02.1.01/0.0/0.0/16\_019/0000797).

Conflicts of Interest: The authors declare no conflict of interest.

# Appendix A. Incoming Atmospheric Longwave Radiation

The incoming atmospheric long-wave radiation is calculated via Equation (2), where the atmospheric emissivity  $\varepsilon_{ac}$  is calculated as follows [67,68]:

$$\varepsilon_{ac} = (1-s) + s \left( 1 - 0.261 \exp\left( -7.77 \cdot 10^{-4} T_a^2 \right) \right),$$
 (A1)

where *s* is defined according to [68] as the ratio of the measured solar radiation  $h_s$  and clear-sky irradiance  $h_{s,clr}$  (W m<sup>-2</sup>)

$$s = \frac{h_s}{h_{s,clr}}.$$
 (A2)

The reason for *s* appearing in Equation (A1) is that it should represent the changes of  $\varepsilon_{ac}$  due to cloud cover, which in turn is estimated from solar radiation measurements. This means, however, that the usage of Equation (A1) is restricted to daytime observations [68]. Clear-sky irradiance  $h_{s,clr}$  is estimated using the algorithm described in [69] for the calculation of solar radiation under cloudless skies.

#### Appendix B. Averaging Calculations for Top Boundary Condition during Snow-Free Periods

Applying daily time-averaging to Equation (13) leads to

$$h_{net,g,mean} = h_{t,1,mean} - k_1 \Delta T_g, \tag{A3}$$

where  $h_{t,1,mean}$  and  $h_{net,g,mean}$  denote the daily mean values of  $h_{t,1}$  and  $h_{net,g}$ , respectively. Using Equation (12),  $h_{t,1,mean}$  is in this study is calculated as follows:

$$h_{t,1,mean} = \left(1 - \nu_f\right) \left( \left(1 - \alpha_g\right) h_{s,mean} - \left(1 - \varepsilon_{ac}\right) h_{l,g0,mean} - h_{evap,mean} \right), \tag{A4}$$

where  $h_{s,mean}$  is the daily mean observed solar radiation per unit area of ground surface,  $h_{evap,mean}$  is the daily mean total evaporative heat transfer to the atmosphere and  $h_{l,g0,mean}$  is calculated by applying a daily averaging procedure to the previously introduced  $h_{l,g0}$  flux (Equation (9) and below) and neglecting higher-order terms:

$$h_{l,g0,mean} = \overline{\epsilon_g \sigma (T_a + 273.15)^4} \approx \epsilon_g \sigma (T_{a,mean} + 273.15)^4.$$
(A5)

The values of  $v_f$ ,  $\alpha_g$ ,  $\varepsilon_{ac}$  and  $\varepsilon_g$  used in Equations (A4) and (A5) are assumed to stay constant over the day, where  $\varepsilon_{ac}$  is calculated from Equations (A1) and (A2) approximatively by inserting daily mean values  $T_{a,mean}$ ,  $h_{s,mean}$  and  $h_{s,clr,mean}$  for  $T_a$ ,  $h_s$ , and  $h_{s,clr}$ , respectively. Furthermore,  $h_{s,mean}$  is obtained directly from daily observed solar radiation input to the model, while  $h_{evap,mean}$  is calculated from the daily actual evapotranspiration *ETa* which is obtained using the FAO-56 method [61]. The following approximation is used (neglecting the correlation term) in deriving the daily average of the second term on the RHS of Equation (A3):

$$k_1 \Delta T_g \approx k_{1,mean} \cdot \Delta T_{g,mean},$$
 (A6)

where  $\Delta T_{g,mean}$  is defined as the difference between the daily mean soil surface temperature  $T_{g,mean}$  and the daily mean air temperature  $T_{a,mean}$ 

$$\Delta T_{g,mean} = T_{g,mean} - T_{a,mean}. \tag{A7}$$

The value of  $k_1$ , as defined in Equation (11), changes during the day because of  $k_{l0}$  air temperature dependence. The daily mean value of  $k_1$  is calculated as follows:

$$k_{1,mean} = \left(1 - \nu_f\right) \left(k_{l,g0,mean} + k_{cg}\right) + \nu_f \mu_{fg} k_{l0,mean},\tag{A8}$$

using the approximation

$$k_{10,mean} = 4\sigma (T_a + 273.15)^3 \approx 4\sigma (T_{a,mean} + 273.15)^3$$
(A9)

and

$$k_{l,g0,mean} = \varepsilon_g k_{l0,mean},\tag{A10}$$

where  $T_{a,mean}$  is the daily mean air temperature (°C). Now, Equation (A3) can be written, approximately, in the form

$$h_{net,g,mean} = h_{t,1,mean} - k_{1,mean} \Delta T_{g,mean} , \qquad (A11)$$

or in the form of Equation (15), which is more convenient for further calculations, where

$$R_{1,mean} = \frac{1}{k_{1,mean}},\tag{A12}$$

$$\Delta T_{1,mean} = \frac{h_{t,1,mean}}{k_{1,mean}}.$$
(A13)

## Appendix C. Derivation of Bottom Boundary Equations

Combining Equations (25) and (26) (neglecting  $\theta_{ice}$  change, because the bottom layer of the simulated soil profile is assumed to be deep enough that  $\theta_{ice}$  does not change there) and assuming constant thermal conductance  $\lambda$  and heat capacity *C* yields

$$C \cdot \partial_t T_s(z, t) = \lambda \cdot \partial_z^2 T_s(z, t).$$
(A14)

The solution to Equation (A14) for sinusoidal variation with annual angular frequency  $\omega_a$  and amplitude  $T_{ampl}$  around a mean value of  $T_{AA}$  is known as [70]:

$$T_s(z,t) = T_{AA} + T_{ampl} \exp\left(-\frac{z}{d_a}\right) \cos\left(\omega_a(t-t_0) - \frac{z}{d_a}\right),\tag{A15}$$

where the angular frequency of a year  $\omega_a$  (rad s<sup>-1</sup>) is defined as

$$\omega_a = \frac{2\pi}{365 \cdot 86400} \tag{A16}$$

and the damping depth  $d_a$  for annual frequency is given as [70]:

$$d_a = \sqrt{\frac{2\lambda}{\omega_a C}}.$$
(A17)

Using Equations (25) and (A15) and the trigonometric addition theorems it can be verified that the following equation for the heat flow is true:

$$h(z,t) = -\lambda \partial_z T_s(z,t) = \frac{\lambda}{d_a} \left( \left( 1 - \tan\left(\frac{\omega_a \Delta t}{2}\right) \right) (T_s(z,t) - T_{AA}) + \frac{T_s(z,t) - T_s(z,t - \Delta t)}{\sin(\omega_a \Delta t)} \right).$$
(A18)

Time-averaging yields ( $\partial_z T_s$  is assumed to be continuous)

$$\overline{h}(z,t) = -\lambda \partial_z \overline{T}_s(z,t) = \frac{\lambda}{d_a} \left( \left( 1 - \tan\left(\frac{\omega_a \Delta t}{2}\right) \right) \left( \overline{T}_s(z,t) - \overline{T}_{AA} \right) + \frac{\overline{T}_s(z,t) - \overline{T}_s(z,t - \Delta t)}{\sin(\omega_a \Delta t)} \right).$$
(A19)

From Equation (A19) now follows the bottom boundary condition Equation (33), where the approximated damping depth  $d_a^j(z)$  (m) for annual frequency has been defined as follows [70]:

$$d_a^j(z) := \sqrt{\frac{2\hat{\lambda}^j(z)}{\omega_a \hat{\overline{C}}^j(z)}}.$$
 (A20)

# Appendix D. Notations and Units

Quantity Part I	Unit	Description
С	$J m^{-3} K^{-1}$	volumetric soil heat capacity
CV	kg ha <sup>-1</sup>	total aboveground biomass
$d_a$	m	damping depth for annual frequency
ETa	mm H <sub>2</sub> O	actual daily evapotranspiration
Fuzo	$Im^{-3}$	latent heat of ice fusion related to volume of liquid water ( $\approx 3.34 \cdot 10^8$ I m <sup>-3</sup> )
- 1120 h	$W m^{-2}$	soil heat flow
hcong a	$\mathrm{W}\mathrm{m}^{-2}$	convective heat transfer from the soil surface to the atmosphere
hevan	$W m^{-2}$	total evaporative heat transfer to the atmosphere per ground area
heven a	$\mathrm{W}\mathrm{m}^{-2}$	evaporative heat transfer from the soil surface to the atmosphere
	2	daily mean total evaporative heat transfer to the atmosphere per ground
h <sub>evap,mean</sub>	$W m^{-2}$	area
$h_{l0}$	$\mathrm{W}\mathrm{m}^{-2}$	long-wave radiation for a black body at air temperature
$h_{l,ac}$	$\mathrm{W}\mathrm{m}^{-2}$	incoming atmospheric long-wave radiation
$h_{1 f \alpha}$	${ m W}~{ m m}^{-2}$	net long-wave radiation from the foliage to the ground (per total ground
*//S	<b>T</b> 17 2	area)
$h_{l,g0}$	$W m^{-2}$	long-wave radiation from soil surface at air temperature
h <sub>l,g0,mean</sub>	$W m^{-2}$	daily mean long-wave radiation from soil surface at air temperature
$h_{l,ga}$	$W m^{-2}$	outgoing thermal long-wave radiation emitted from the bare soil
h <sub>net,g</sub>	$W m^{-2}$	net ground heat flow
h <sub>net,g,mean</sub>	$W m^{-2}$	daily mean net ground heat flow
$h_s$	$W m^{-2}$	observed solar radiation per unit area of ground surface
h <sub>s,clr</sub>	$W m^{-2}$	clear-sky irradiance
h <sub>s,clr,mean</sub>	$W m^{-2}$	daily mean clear-sky irradiance
h <sub>s,mean</sub>	$W m^{-2}$	daily mean observed solar radiation per unit area of ground surface
$h_{t,1}$	$W m^{-2}$	net incoming heat flux for snow-free periods
h <sub>t,1,mean</sub>	$W m^{-2}$	daily mean net incoming heat flux for snow-free periods
$k_1$	$W m^{-2} K^{-1}$	net heat transfer coefficient for snow-free periods
$k_{1,mean}$	$W m^{-2} K^{-1}$	daily mean net heat transfer coefficient for snow-free periods
$k_{cg}$	${ m W}~{ m m}^{-2}~{ m K}^{-1}$	convective heat transfer coefficient from the soil surface to air
<i>k</i> <sub>10</sub>	${\rm W} ~{\rm m}^{-2} ~{\rm K}^{-1}$	derivate of black-body long-wave radiation with respect to temperature,
1.	147 - 2 - 2 - 1	
к <sub>10,mean</sub>	wm-ĸ-	daily mean value of $k_{l0}$
<i>k</i> <sub><i>l,g</i>0</sub>	${\rm W}{\rm m}^{-2}{\rm K}^{-1}$	temperature, evaluated at air temperature
k <sub>l.e0.mean</sub>	${ m W}~{ m m}^{-2}~{ m K}^{-1}$	daily mean value of $k_{l,g0}$
ksnow	1	damping factor for snow coverage
$R_1$	$\mathrm{m}^2~\mathrm{K}~\mathrm{W}^{-1}$	thermal resistance respective ground heat flow for snow-free periods
R <sub>1,mean</sub>	$\mathrm{m}^2\mathrm{K}\mathrm{W}^{-1}$	thermal resistance respective ground heat flow for snow-free periods, applicable to daily mean data
R <sub>2,mean</sub>	$\mathrm{m}^2\mathrm{K}\mathrm{W}^{-1}$	thermal resistance respective ground heat flow for dense snow cover, applicable to daily mean data
R <sub>mean</sub>	$\mathrm{m}^2~\mathrm{K}~\mathrm{W}^{-1}$	thermal resistance respective ground heat flow for partial snow cover, applicable to daily mean data
SNO	$mm H_2O$	snow water equivalent of snow layer
SNO <sub>limit,1</sub>	mm H <sub>2</sub> O	lower limit for SNO below which the snow layer is ignored
SNO <sub>limit,2</sub>	mm H <sub>2</sub> O	upper limit for SNO beyond which the snow layer is treated as dense
S	1	ratio of measured solar radiation to clear-sky irradiance
$T_{AA}$	°C	annual mean air temperature
$T_a$	°C	air temperature (2 m height)

Quantity	Unit	Description
T <sub>a,mean</sub>	°C	daily mean air temperature (2 m height)
$T_{q}$	°C	soil surface temperature
$T_{g,mean}$	°C	daily mean soil surface temperature
$T_s$	°C	soil temperature
t	s	time
VP <sub>clay</sub>	vol %	volume percentage of total solid soil matter that is clay
VPsand	vol %	volume percentage of total solid soil matter that is sand
w	$\mathrm{J}~\mathrm{m}^{-3}$	heat energy density
z	m	depth in soil profile ( $z = 0$ at soil surface, $z > 0$ inside the soil)
$Z_{max}$	m	maximum simulation depth (bottom of soil profile)
Part II		
αg	1	soil surface albedo (0–1)
β	ha kg $^{-1}$	parameter in $\nu_f(CV)$ -relation
$\Delta T_1$	°C	difference between soil surface and air temperature during snow-free periods for zero ground heat flow
$\Delta T_{1,mean}$	°C	difference between daily mean soil surface and air temperature during snow-free periods for zero ground heat flow
$\Delta T_{2,mean}$	°C	difference between daily mean soil surface and air temperature for dense snow cover and zero ground heat flow
$\Delta T_g$	°C	difference between soil surface and air temperature
$\Delta T_{g,mean}$	°C	difference between daily mean soil surface and air temperature
$\Delta T_{mean}$	°C	difference between daily mean soil surface and air temperature for partial snow cover and zero ground heat flow
$\Delta t$	S	simulation time step (= $86,400 \text{ s}$ )
Eac	1	atmospheric emissivity (0–1)
ε <sub>f</sub>	1	foliage emissivity (0–1)
έ	1	ground (soil surface) emissivity (0–1)
ζ	1	ice fraction (0–1)
θ	${\rm cm}^3~{\rm cm}^{-3}$	volumetric total soil water content (liquid + ice, but neglecting volume expansion of frozen water)
$\theta_{ice}$	$\rm cm^3~cm^{-3}$	volumetric ice content in soil, but neglecting volume expansion of frozen water
$\theta_{sat}$	$\rm cm^3 \ cm^{-3}$	saturated volumetric water content or total soil pore volume
λ	${ m W}~{ m m}^{-1}~{ m K}^{-1}$	soil thermal conductivity
$\mu_{fg}$	1	radiation exchange degree between foliage and ground
v <sub>f</sub>	1	vegetation cover (0–1)
v <sub>sn</sub>	1	snow coverage factor (0–1)
σ	${ m W}~{ m m}^{-2}~{ m K}^{-4}$	Stefan-Boltzmann constant ( $\approx$ 5.67 $\cdot$ 10 <sup>-8</sup> W m <sup>-2</sup> K <sup>-4</sup> )
$\omega_a$	$\rm rad~s^{-1}$	angular frequency of the year

# Appendix E.

Table A1. Description of nine validation sites in the Czech Republic (related to Figures A1–A18).

Station Name	Station Code	Long	Lat	Altitude	Soil Description
		0	0	m	
KROMĚŘÍŽ	B1KROM01	17.3653	49.2847	233	0–100 cm loamy soil, chernozem
LEDNICE	B2LEDN01	16.7989	48.79262	177	0–100 cm loamy soil, chernozem
KOCELOVICE	C1KOCE01	13.83861	49.46722	519	0–25 cm sandy loam, 25–50 cm loam 50–100 cm sandy, Cambisol
UPICE	H1UPIC01	16.01162	50.50642	413	0–70 cm loamy-sand
BĚLOTÍN	O1BELO01	17.8042	49.5869	306	0–100 cm loamy soil, luvisol
LUČINA	O1LUCI01	18.4425	49.7308	300	0–100 cm loam. Pseudogleyic luvisol
LUKÁ	O2LUKA01	16.95333	49.65222	510	0–30 cm sandy-loam 30–100 cm loam, Cambisol
USTÍ NAD LABEM	U1ULKO01	14.04111	50.68333	375	0–30 cm sandy loam 30–100 cm loam, typical Cambisol with strong human influence
LIBEREC	U2LIBC01	15.02389	50.76972	398	0–22 cm sandy-loam 22–100 cm loam, gleyic soil

**Surface conditions:** All measurement sites are characterized by no or only negligible slope inclination (flat area) and grass cover with regular mowing; AGRISOTES simulations were carried out with constant surface biomass of 1000 kg ha<sup>-1</sup> (representing short grass).

Station Name	Station Code	Soi	l Depth 10	cm	Soil Depth 50 cm			
		R <sup>2</sup>	R <sup>2</sup> RMSE MBE		<b>R</b> <sup>2</sup>	RMSE	MBE	
			°C	°C		°C	°C	
KROMĚŘÍŽ	B1KROM01	0.98	1.26	0.52	0.99	1.10	0.72	
LEDNICE	B2LEDN01	0.97	1.43	-0.08	0.98	1.16	0.44	
KOCELOVICE	C1KOCE01	0.96	1.67	0.45	0.96	1.57	0.65	
UPICE	H1UPIC01	0.95	1.83	0.78	0.95	1.83	0.82	
BĚLOTÍN	O1BELO01	0.95	1.82	-0.06	0.95	1.65	0.04	
LUČINA	O1LUCI01	0.94	1.95	0.20	0.94	1.96	0.36	
LUKÁ	O2LUKA01	0.97	1.60	0.70	0.97	1.64	0.72	
USTÍ NAD LABEM	U1ULKO01	0.96	1.58	0.37	0.94	1.74	0.31	
LIBEREC	U2LIBC01	0.95	1.98	1.08	0.95	1.84	1.14	

**Table A2.** Statistical validation results of AGRISOTES (measured vs. simulated soil temperatures) for nine validation sites (see Table A1) in the Czech Republic (related to Figures A1–A18).

Figures A1–A18 show the validation results of AGRISOTES (measured vs. simulated soil temperatures in °C) for nine validation sites (see Table A1) of Czech Republic (graphical representation).



Figure A1. Validation at site B1KROM01 for 10 cm soil depth.



Figure A2. Validation at site B1KROM01 for 50 cm soil depth.



Figure A3. Validation at site B2LEDN01 for 10 cm soil depth.



Figure A4. Validation at site B2LEDN01 for 50 cm soil depth.



Figure A5. Validation at site C1KOCE01 for 10 cm soil depth.



Figure A6. Validation at site C1KOCE01 for 50 cm soil depth.



**Figure A7.** Validation at site H1UPIC01 for 10 cm soil depth.



Figure A8. Validation at site H1UPIC01 for 50 cm soil depth.



Figure A9. Validation at site O1BELO01 for 10 cm soil depth.



Figure A10. Validation at site O1BELO01 for 50 cm soil depth.



Figure A11. Validation at site O1LUCI01 for 10 cm soil depth.



Figure A12. Validation at site O1LUCI01 for 50 cm soil depth.



Figure A13. Validation at site O2LUKA01 for 10 cm soil depth.



Figure A14. Validation at site O2LUKA01 for 50 cm soil depth.



Figure A15. Validation at site U1ULKO01 for 10 cm soil depth.



Figure A16. Validation at site U1ULKO01 for 50 cm soil depth.



Figure A17. Validation at site U2LIBC01 for 10 cm soil depth.



Figure A18. Validation at site U2LIBC01 for 50 cm soil depth.

# Appendix F. Software/Data Availability of AGRISOTES

Name of software: AGRISOTES

Developer and contact: Authors as in the paper, use the corresponding author as contact: Prof. DI Dr. Josef Eitzinger, University of Natural Resources and Life Sciences, Institute of Meteorology and Climatology, Gregor-Mendel-Str. 33, A-1180 Vienna, Tel.: +43 1 47654 81422, E-Mail: josef.eitzinger@boku.ac.at.

Year of First Availability: 2019

Hardware required: Standard PC

Software required: GNU Octave 4.0.3 (or higher versions, if fully backward compatible regarding used program language features)

Availability: software and user manual, including example input files; on request, no costs AGRISOTES software:

Program language: GNU Octave

Program size: <100 KB

Input and output data format: MS Excel compatible comma-separated values (CSV).

## References

- 1. Dokuchaev, V.V. Russian Chernozem—Selected Works of V.V. Dokuchaev; Israel Program for Scientific Translations: Jerusalem, Israel, 1967.
- 2. Fanning, D.S.; Fanning, M.C.B. Soil Morphology, Genesis, and Classification; John Wiley and Sons: New York, NY, USA, 1989; 395p, ISBN 0471892483.
- 3. Ellenberg, H. Zeigerwerte der Gefäßpflanzen Mitteleuropas. Scr. Geobot. 1974, 9, 1–97.
- 4. Gray, J.M.; Humphreys, G.S.; Deckers, J.A. Relationships in soil distribution as revealed by a global soil database. *Geoderma* **2009**, 150, 309–323. [CrossRef]
- 5. Larcher, W. Physiological Plant Ecology, 4th ed.; Springer: Berlin, Germany, 2003; 513p, ISBN 978-3-540-43516-7.
- Trnka, M.; Kersebaum, K.C.; Eitzinger, J.; Hayes, M.; Hlavinka, P.; Svoboda, M.; Dubrovský, M.; Semerádová, D.; Wardlow, B.; Pokorný, E.; et al. Consequences of climate change for the soil climate in Central Europe and the central plains of the United States. *Clim. Chang.* 2013, *120*, 405–418. [CrossRef]
- 7. Davis, P.M.; Brenes, N.; Allee, L.L. Temperature dependent models to predict regional differences in corn rootworm (Coleoptera: Chrysomelidae) phenology. *Environ. Entomol.* **1996**, *25*, 767–775. [CrossRef]
- 8. Orchard, V.A.; Cook, F.J. Relationship between soil respiration and soil moisture. Soil Biol. Biochem. 1983, 15, 447–453. [CrossRef]
- 9. Parton, W.J.; Schimel, D.S.; Cole, C.V.; Ojima, D.S. Analysis of factors controlling soil organic matter levels in Great Plains grasslands. *Soil Sci. Soc. Am. J.* **1987**, *51*, 1173–1179. [CrossRef]
- 10. Parton, W.J.; Stewart, J.W.B.; Cole, C.V. Dynamics of C, N, P and S in grassland soils: A model. *Biogeochemistry* **1988**, *5*, 109–131. [CrossRef]
- 11. Parton, W.J.; Mosier, A.R.; Ojima, D.S.; Valentine, D.W.; Schimel, D.S.; Weier, K.; Kulmala, A.E. Generalized model for N<sub>2</sub> and N<sub>2</sub>O production from nitrification and denitrification. *Glob. Biogeochem. Cycles* **1996**, *10*, 401–412. [CrossRef]
- 12. Peterjohn, W.T.; Melillo, J.M.; Steudler, P.A.; Newkirk, K.M.; Bowles, F.P.; Aber, J.D. Responses of trace gas fluxes and N availability to experimentally elevated soil temperatures. *Ecol. Appl.* **1994**, *4*, 617–625. [CrossRef]

- Fu, C.; Lee, X.; Griffis, T.J.; Wang, G.; Wei, Z. Influences of root hydraulic redistribution on N<sub>2</sub>O emissions at AmeriFlux sites. *Geophys. Res. Lett.* 2018, 45, 5135–5143. [CrossRef]
- 14. Rodrigo, A.; Recous, S.; Neel, C.; Mary, B. Modelling temperature and moisture effects on C–N transformations in soils: Comparison of nine models. *Ecol. Modell.* **1997**, *102*, 325–339. [CrossRef]
- 15. Franko, U.; Oelschlägel, B.; Schenk, S. Simulation of temperature-, water- and nitrogen dynamics using the model CANDY. *Ecol. Modell.* **1995**, *81*, 213–222. [CrossRef]
- 16. Qin, Y.; Bai, Y.; Chen, G.; Liang, Y.; Li, X.; Wen, B.; Lu, X.; Li, X. The effects of soil freeze–thaw processes on water and salt migrations in the western Songnen Plain, China. *Sci. Rep.* **2021**, *11*, 3888. [CrossRef]
- Wang, J.; Quan, Q.; Chen, W.; Tian, D.; Ciais, P.; Crowther, T.W.; Mack, M.C.; Poulter, B.; Tian, H.; Luo, Y.; et al. Increased CO<sub>2</sub> emissions surpass reductions of non-CO<sub>2</sub> emissions more under higher experimental warming in an alpine meadow. *Sci. Total Environ.* 2021, 769, 144559. [CrossRef]
- 18. Bogomolov, V.Y.; Dyukarev, E.A.; Stepanenko, V.M.; Drozdov, E.D. Modeling the temperature and humidity conditions of mineral soils in an active layer model taking into account in depth changes in the thermodynamic properties of the soil. *IOP Conf. Ser. Earth Environ. Sci.* **2020**, *611*, 012012. [CrossRef]
- 19. Kiselev, M.V.; Voropay, N.N.; Dyukarev, E.A.; Preis, Y.I. Temperature regimes of drained and natural peatlands in arid and water-logged years. *IOP Conf. Ser. Earth Environ. Sci.* 2019, *386*, 012029. [CrossRef]
- Koçak, K.; Şaylan, L.; Eitzinger, J. Nonlinear prediction of near-surface temperature via univariate and multivariate time series embedding. *Ecol. Modell.* 2004, 173, 1–7. [CrossRef]
- 21. Tanaka, K.; Hashimoto, S. Plant canopy effects on soil thermal and hydrological properties and soil respiration. *Ecol. Modell.* 2006, 196, 32–44. [CrossRef]
- 22. Sepaskhah, A.R.; Boersma, L. Thermal conductivity of soils as a function of temperature and water content. *Soil Sci. Soc. Am. J.* **1979**, 43, 439–444. [CrossRef]
- Dhanush, K.V.; Patil, D.R. Effect of mulches on soil moisture, temperature, weed suppression and estimation of cost benefit ratio of grape (*Vitis vinifera* L.) 'Kishmish Rozavis White' in northern dry zone of Karnataka, India. *Acta Hortic.* 2020, 1299, 61–66. [CrossRef]
- 24. Gupta, S.C.; Larson, W.E.; Allmaras, R.R. Predicting soil temperature and soil heat flux under different tillage-surface residue conditions. *Soil Sci. Soc. Am. J.* **1984**, *48*, 223–232. [CrossRef]
- Zapata, D.; Rajan, N.; Mowrer, J.; Casey, K.; Schnell, R.; Hons, F. Long-term tillage effect on with-in season variations in soil conditions and respiration from dryland winter wheat and soybean cropping systems. *Sci. Rep.* 2021, *11*, 2344. [CrossRef] [PubMed]
- 26. Du, K.; Li, F.; Qiao, Y.; Leng, P.; Li, Z.; Ge, J.; Yang, G. Influence of no-tillage and precipitation pulse on continuous soil respiration of summer maize affected by soil water in the North China Plain. *Sci. Total Environ.* **2021**, *766*, 144384. [CrossRef] [PubMed]
- 27. Huang, F.; Ding, X.; Li, W.; Jia, H.; Wei, X.; Zhao, X. The effect of temperature on the decomposition of different parts of maize residues in a solonchak. *Catena* **2021**, *201*, 105207. [CrossRef]
- Von Haden, A.C.; Marín-Spiotta, E.; Jackson, R.D.; Kucharik, C.J. Soil microclimates influence annual carbon loss via heterotrophic soil respiration in maize and switchgrass bioenergy cropping systems. *Agric. For. Meteorol.* 2019, 279, 107731. [CrossRef]
- Al-Maliki, S.; Al-Taey, D.K.A.; Al-Mammori, H.Z. Soil microbes, organic carbon protection and plant production in consideration with earthworms: A review. *Plant Cell Biotechnol. Mol. Biol.* 2020, 21, 99–125.
- 30. Johnson, S.N.; Zhang, X.; Crawford, J.W.; Gregory, P.J.; Young, I.M. Egg hatching and survival time of soil-dwelling insect larvae: A partial differential equation model and experimental validation. *Ecol. Modell.* **2007**, 202, 493–502. [CrossRef]
- 31. Dai, Z.; Hu, J.; Fan, J.; Fu, W.; Wang, H.; Hao, M. No-tillage with mulching improves maize yield in dryland farming through regulating soil temperature, water and nitrate-N. *Agric. Ecosyst. Environ.* **2021**, *309*, 107288. [CrossRef]
- 32. Liu, Z.; Lei, N. Effect of different tillage managements on soil physicochemical properties and crop yield. *IOP Conf. Ser. Earth Environ. Sci.* **2019**, 384, 012175. [CrossRef]
- 33. Eitzinger, J.; Parton, W.J.; Hartman, M. Improvement and validation of a daily soil temperature submodel for freezing/thawing periods. *Soil Sci.* 2000, *165*, 525–534. [CrossRef]
- 34. Zhang, T. Influence of the seasonal snow cover on the ground thermal regime: An overview. *Rev. Geophys.* 2005, 43, RG4002. [CrossRef]
- 35. Ren, J.P.; Vanapalli, S.K.; Han, Z. Soil freezing process and different expressions for the soil-freezing characteristic curve. *Sci. Cold Arid Reg.* **2017**, *9*, 221–228.
- Balsamo, G. Land surface processes. In Proceedings of the ECMWF Workshop on Sub-Seasonal Predictability, Reading, UK, 2–5 November 2015. Available online: https://www.ecmwf.int/sites/default/files/elibrary/2015/14483-land-surface-processes.pdf (accessed on 9 March 2021).
- 37. Dutra, E.; Balsamo, G.; Viterbo, P.; Miranda, P.M.A.; Beljaars, A.; Schär, C.; Elder, K. An improved snow scheme for the ECMWF land surface model: Description and offline validation. *J. Hydrometeorol.* **2010**, *11*, 899–916. [CrossRef]
- 38. Trigo, I.F.; Boussetta, S.; Viterbo, P.; Balsamo, G.; Beljaars, A.; Sandu, I. Comparison of model land skin temperature with remotely sensed estimates and assessment of surface-atmosphere coupling. *J. Geophys. Res. Atmos.* **2015**, *120*, 12096–12111. [CrossRef]
- 39. Sellers, P.J.; Mintz, Y.; Sud, Y.C.; Dalcher, A. A simple biosphere model (SiB) for use within general circulation models. *J. Atmos. Sci.* **1986**, *43*, 505–531. [CrossRef]

- 40. Ek, M.; Mahrt, L. A User Guide to OSU1DPBL Version 1.0.4: A One-Dimensional Planetary Boundary Layer Model with Interactive Soil Layers and Plant Canopy; Department of Atmospheric Sciences, Oregon State University: Corvallis, OR, USA, 1991.
- 41. Grünhage, L.; Haenel, H.-D. Detailed documentation of the PLATIN (PLant-ATmosphere INteraction) model. *Landbauforsch. Völkenrode Sonderh.* 2008, *319*, 1–85.
- 42. Walker, B.H.; Langridge, J.L. Modelling plant and soil water dynamics in semi-arid ecosystems with limited site data. *Ecol. Modell.* **1996**, *87*, 153–167. [CrossRef]
- Jones, L.M.; Koehler, A.-K.; Trnka, M.; Balek, J.; Challinor, A.J.; Atkinson, H.J.; Urwin, P.E. Climate change is predicted to alter the current pest status of Globodera pallida and G. rostochiensis in the United Kingdom. *Glob. Chang. Biol.* 2017, 23, 4497–4507. [CrossRef]
- 44. Dzotsi, K.A.; Basso, B.; Jones, J.W. Development, uncertainty and sensitivity analysis of the simple SALUS crop model in DSSAT. *Ecol. Modell.* **2013**, *260*, 62–76. [CrossRef]
- 45. Petersen, B.M.; Olesen, J.E.; Heidmann, T. A flexible tool for simulation of soil carbon turnover. *Ecol. Modell.* **2002**, 151, 1–14. [CrossRef]
- 46. White, J.W.; Hoogenboom, G.; Kimball, B.A.; Wall, G.W. Methodologies for simulating impacts of climate change on crop production. *Field Crops Res.* 2011, 124, 357–368. [CrossRef]
- 47. Best, M.J. A model to predict surface temperatures. Bound.-Layer Meteorol. 1998, 88, 279–306. [CrossRef]
- Deardorff, J.W. Efficient prediction of ground surface temperature and moisture, with inclusion of a layer of vegetation. J. Geophys. Res. 1978, 83, 1889–1903. [CrossRef]
- Herb, W.R.; Janke, B.; Mohseni, O.; Stefan, H.G. All-Weather Ground Surface Temperature Simulation; Project report no. 478; St. Anthony Falls Laboratory, University of Minnesota: Minneapolis, MN, USA, 2006. Available online: https://hdl.handle.net/1129 9/113684 (accessed on 10 March 2021).
- 50. Van Bavel, C.H.M.; Hillel, D.I. Calculating potential and actual evaporation from a bare soil surface by simulation of concurrent flow of water and heat. *Agric. Meteorol.* **1976**, *17*, 453–476. [CrossRef]
- 51. Campbell, G.S.; Norman, J.M. An Introduction to Environmental Biophysics, 2nd ed.; Springer: New York, NY, USA, 1998; ISBN 978-0-387-94937-6.
- 52. Luo, Y.; Loomis, R.S.; Hsiao, T.C. Simulation of soil temperature in crops. Agric. For. Meteorol. 1992, 61, 23–38. [CrossRef]
- 53. DIN EN ISO 6946. Bauteile—Wärmedurchlasswiderstand und Wärmedurchgangskoeffizient—Berechnungsverfahren; Beuth Verlag: Berlin, Germany, 2018. [CrossRef]
- 54. Parton, W.J.; Hartman, M.; Ojima, D.; Schimel, D. DAYCENT and its land surface submodel: Description and testing. *Glob. Planet. Chang.* **1998**, *19*, 35–48. [CrossRef]
- 55. Kroes, J.G.; Van Dam, J.C.; Groenendijk, P.; Hendriks, R.F.A.; Jacobs, C.M.J. SWAP Version 3.2. Theory Description and User Manual; Alterra report 1649; Alterra: Wageningen, The Netherlands, 2008; ISSN 1566-7197.
- De Vries, D.A. Thermal Properties of Soils. In *Physics of Plant Environment*; Van Wijk, W.R., Ed.; North-Holland Publishing Company: Amsterdam, The Netherlands, 1963; pp. 210–235, 1566-7197.
- 57. De Vries, D.A. Heat transfer in soils. In *Heat and Mass Transfer in the Biosphere. Part 1. Transfer Processes in Plant Environment;* De Vries, D.A., Afgan, N.H., Eds.; Scripta Book Company: Washington, DC, USA, 1975; pp. 5–28.
- 58. Hillel, D. Fundamentals of Soil Physics; Academic Press: San Diego, CA, USA, 1980.
- 59. Ten Berge, H.F.M. Heat and Water Transfer at the Bare Soil Surface: Aspects Affecting Thermal Imagery. Ph.D. Thesis, Wageningen Agricultural University, Wageningen, The Netherlands, 1986.
- 60. Ashby, M.; Dolman, A.J.; Kabat, P.; Moors, E.J.; Ogink-Hendriks, M.J. SWAPS Version 1.0. Technical Reference Manual; Technical document 42; DLO Winand Staring Centre: Wageningen, The Netherlands, 1996.
- 61. Allen, R.G.; Pereira, L.S.; Raes, D.; Smith, M. Crop Evapotranspiration—Guidelines for Computing Crop Water Requirements—FAO Irrigation and Drainage Paper 56; Food and Agriculture Organization: Rome, Italy, 1998; ISBN 92-5-104219-5.
- 62. Pronk, A.A.; Goudriaan, J.; Stilma, E.; Challa, H. A simple method to estimate radiation interception by nursery stock conifers: A case study of eastern white cedar. *NJAS-Wagen. J. Life Sci.* **2003**, *51*, 279–295. [CrossRef]
- 63. Willmott, C.J. Some comments on the evaluation of model performance. Bull. Am. Meteorol. Soc. 1982, 63, 1309–1313. [CrossRef]
- 64. Pielke, R.A. Mesoscale Meteorological Modeling; Academic Press: New York, NY, USA, 1984; ISBN 0125548206.
- 65. Li, M.-F.; Tang, X.-P.; Wu, W.; Liu, H.-B. General models for estimating daily global solar radiation for different solar radiation zones in mainland China. *Energy Convers. Manag.* **2013**, *70*, 139–148. [CrossRef]
- Trnka, M.; Kocmánková, E.; Balek, J.; Eitzinger, J.; Ruget, F.; Formayer, H.; Hlavinka, P.; Schaumberger, A.; Horáková, V.; Možný, M.; et al. Simple snow cover model for agrometeorological applications. *Agric. For. Meteorol.* 2010, 150, 1115–1127. [CrossRef]
- 67. Idso, S.B.; Jackson, R.D. Thermal radiation from the atmosphere. J. Geophys. Res. **1969**, 74, 5397–5403. [CrossRef]
- 68. Crawford, T.M.; Duchon, C.E. An improved parameterization for estimating effective atmospheric emissivity for use in calculating daytime downwelling longwave radiation. *J. Appl. Meteorol.* **1999**, *38*, 474–480. [CrossRef]
- Neitsch, S.L.; Arnold, J.G.; Kiniry, J.R.; Williams, J.R. Soil and Water Assessment Tool Theoretical Documentation Version 2009; Technical report no. 406; Texas Water Resources Institute: College Station, TX, USA, 2011. Available online: http://hdl.handle.net/1969.1/1 28050 (accessed on 10 March 2021).
- 70. Hillel, D. Introduction to Soil Physics; Academic Press: San Diego, CA, USA, 1982; ISBN 0123485207.