

Polarization Weather Radar Development from 1970–1995: Personal Reflections

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Abstract: The modern era of polarimetric radar begins with radiowave propagation research starting in the early 1970s with applications to measurement and modeling of wave attenuation in rain and depolarization due to ice particles along satellite–earth links. While there is a rich history of radar in meteorology after World War II, the impetus provided by radiowave propagation requirements led to high-quality antennas and feeds. Our journey starts by describing the key institutions and personnel responsible for development of weather radar polarimetry. The early period was dominated by circularly polarized radars for propagation research and at S band (frequency near 3 GHz) for hail detection. By the mid to late 70s, a paradigm shift occurred which led to the dominance of linear polarizations with applications to slant path attenuation prediction as well as estimation of rain rates and inferences of precipitation physics. The period from the early 1980s to 1995 can be considered as the “golden” period of rapid research that brought in meteorologists, cloud physicists, and hydrologists. This article describes the evolution of this technology from the vantage point of the authors. Their personal reflections and “behind the scenes” descriptions offer a glimpse into the inner workings at several key institutions which cannot be found elsewhere.

Keywords: radar; dual-polarization; precipitation

1. Introduction

The electromagnetic wave is defined by amplitude, frequency, and polarization state. These properties change because of interaction with precipitation, and relating these changes to particle microphysical states including Doppler velocity and spectrum width is the main purpose of dual-polarized Doppler weather radar. The electromagnetic theory rooted in Maxwell’s equations has played a central role in the development and application of polarimetric weather radar. There is a rich history of radar in meteorology since World War II for which we defer to the Battan Memorial Conference Proceedings published in *Radar in Meteorology* [1] edited by the late David Atlas. Our objective in this article is much less ambitious in that we describe the early years of dual-polarization research in meteorology and related radiowave propagation starting from the mid-1970s to about the early 1990s. In the mid-70s the number of papers on dual-polarized radar presented in the American Meteorological Society (AMS) Radar Meteorology conferences was < 5 while by the mid-90s this number reached 50. Thus, this period was chosen, albeit subjectively, as it marks the beginning of the modern era of radar polarimetry to the point beyond which the accelerated pace of research and applications probably reached its peak but not mature enough to be adopted by the operational weather services. The authors were closely involved with, and had intimate knowledge of, the principal players and institutions active during this period so this article reflects their opinions from

that vantage point. Also, much of the research during this period is described in detail in several books [2,3]. For convenience a table of abbreviations is given at the end of this article.

The modern era of polarimetric radar began in the early 1970s driven largely by the radiowave propagation scientists who were characterizing attenuation and depolarization of electromagnetic (EM) waves due to rain and ice particles along satellite-earth links at microwave and millimeter wavelengths. Related advances in accurate dual-polarization antenna feed design, precise reflector manufacturing methods, and microwave circuits were driven by stringent earth station antenna requirements on sidelobes and on-axis cross-polarization levels. This also contributed significantly to weather radar polarimetry. Much of this early work involved researchers with strong backgrounds in electromagnetic scattering theory, microwave engineering, and signal processing. Their work led to a wider recognition of the intrinsic value of polarimetry in radar meteorology and in the next two decades inspired strong contributions by meteorologists and nonspecialists alike. This was aided by the ready availability of numerical scattering software tools and reliable and high quality data from polarimetric radars, as well as advances in cloud and precipitation physics. Currently, the operational deployment of polarimetric Doppler weather radars by nearly all weather service agencies worldwide has led to research advancements scarcely foreseen by the early pioneers. It continues to grow with advances in numerical microphysical models of precipitation growth and evolution that predict the physical properties needed by advanced scattering models.

The first workshop on dual-polarization radar lead by Metcalf and Humphries [4] was held the day before the AMS Radar Meteorology Conference in Miami Beach in 1980 where all of eight conference papers on dual-polarization topics were presented. The workshop had 21 attendees, mainly from the US, Canada, and the UK. The goal was to assess the meteorological applications of dual-polarization and system design considerations as well as experimental procedures used at that time. Short presentations were made based on the experiences at the relevant institutions such as New Mexico Tech, Rutherford Appleton Laboratory, National Research Council of Canada, Alberta Research Council, and NOAA-Wave Propagation Laboratory. It was recognized that the different institutions were proceeding along their own lines of research but there was strong support for a coherent polarization agile dual-receiver system. Polarization agility is defined here as the capability of the radar to transmit polarization states that alternate between two orthogonal states (e.g., horizontal and vertical) from pulse-to-pulse (“fast”-switched) with typically only a single receiver that receives the copolar signal. Polarization diversity refers to transmitting a specified polarization state and receiving the copol and cross-pol signals using two receivers.

To make this article tractable, we describe the seminal or landmark papers that provided ideas and impetus for research sometimes occurring decades later. In addition to the role of EM theory we include processing and statistical analysis of signals. We start with the work by McCormick and Hendry at the National Research Council of Canada in the early 1970s. They were able to make more accurate dual-pol radar measurements than possible hitherto, with high performance antennas, feeds, and polarizer networks using circular polarization basis. In parallel they guided the upgrade of the Alberta Research Council S-band radar to circular polarization for hail detection. The next sections describe the nature of how some of the early work using horizontal-vertical polarization basis developed at the institutions and laboratories that the authors worked in or had close associations with, giving a personal historical and “behind the scenes” look that is often left out in the archival journal articles but is useful to record. Any important work we may have missed or overlooked is entirely unintentional.

2. Brief Overview of Electromagnetics in Dual-Polarization Radar and Related Topics

The radar range equation for single linear polarization is well known to the radar meteorological community but less well known is the voltage form of this equation for dual-polarization radars. Our notation is bold face for vectors and bold face italic with underbar for matrices. We use mixed vector-matrix equations and exclude constants for simplicity. The voltage equation is given as $V = \mathbf{h} \cdot \mathbf{E}_s$, where \mathbf{h} describes the effective antenna “height” defined as $\mathbf{h} = \lambda G^{1/2} \mathbf{e}_h$ and \mathbf{E}_s is the backscattered wave from the particle [5]. The wavelength is λ , G is the gain, and \mathbf{e}_h is the unit vector which describes

the radiated polarization state. In general, \mathbf{e}_h could be elliptically polarized (described by the ellipticity angle τ and orientation angle Φ of the ellipse) but most common is the linear antenna polarization state (defined by convention when the antenna is radiating with $\tau = 0$ and $\Phi = 0, 90^\circ$ corresponding to H and V polarizations, respectively). The 2×2 scattering matrix $\underline{\mathbf{S}}$ describes the interaction between the wave incident on the particle and the wave that is scattered back, $\mathbf{E}_s = \underline{\mathbf{S}} \mathbf{E}_{inc}$ [6]. Thus, the voltage equation takes the bilinear form $V = \mathbf{h} \cdot [\underline{\mathbf{S}} \mathbf{E}_{inc}]$ and the received power is $|\mathbf{h} \cdot [\underline{\mathbf{S}} \mathbf{E}_{inc}]|^2$ [7]. From the expression for the received power, the generalized form of the radar cross-section takes the more familiar form $\sigma(\mathbf{e}_h, \mathbf{e}_{inc}) = 4\pi |\mathbf{e}_h \cdot [\underline{\mathbf{S}} \mathbf{e}_{inc}]|^2$ where the unit polarization vector for the antenna is \mathbf{e}_h and that of the incident wave is \mathbf{e}_{inc} . Note that the copolar radar cross-section is defined when $\mathbf{e}_h = \mathbf{e}_{inc}$ whereas for cross-pol \mathbf{e}_h is orthogonal to \mathbf{e}_{inc} . From [2], for a sphere whose scattering matrix is for simplicity given by $S_{hh} = S_{vv} = 1$, $S_{hv} = 0$, the $\sigma_{co} = 4\pi(2\cos^2\tau_{inc} - 1)^2$ and $\sigma_{cx} = 4\pi(4\cos^2\tau_{inc} \sin^2\tau_{inc})$.

The voltage form of the radar range equation in the circular polarization ($\tau = 45^\circ$) basis was derived in [8]. From this, the elements of the 2×2 coherency matrix (two real power terms and one complex correlation) follow, the complex correlation being one of the central elements of their theory [8]. However, the coherency matrix is not complete for partially polarized backscatter as evidenced by the nine real terms of the Mueller matrix [9]. To achieve completeness, the 3×3 Hermitian covariance matrix is needed which has three real (power) terms and three complex correlation terms [10]. The early dual-pol radars [11,12] were polarization agile but measured only two power terms (HH,VV) using a single receiver.

Matrosov [13], using a 35 GHz radar, proposed transmitting a slightly elliptical polarized wave (ellipticity angle τ of 40°). For drizzle (spherical droplets) the elliptical depolarization ratio (σ_{co}/σ_{cx}) or Elliptical Depolarization Ratio (EDR) turns to be -14 dB independent of elevation angle and forms a reference against which to compare the elevation angle dependence of EDR for other types of ice crystals, e.g., branched planar dendrites or irregular graupel. RHI scans in horizontally homogeneous winter precipitation showed dramatic swings of (8 dB) in EDR for plate-like crystals with elevation angle from 0 to 90° whereas irregular graupel showed EDR about 1 dB higher than for drizzle with no elevation angle dependence.

Coherent propagation of dual-polarized EM waves in precipitation media was formulated in [14] in the form of a complex 2×2 transmission matrix ($\underline{\mathbf{T}}$) which enters into the voltage form of the radar range equation as $V = \mathbf{h} \cdot [\underline{\mathbf{T}}^t \mathbf{S} \mathbf{T}]$ where superscript (t) is the matrix transpose. This complicates the separation of backscatter from propagation effects such as differential attenuation and differential phase shift which causes depolarization of the transmitted wave even at long wavelengths (S-band). In [15], McCormick and Hendry showed that when propagation effects dominate the signal returns then a complex plane plot of what they term as W/W_2 (W is the complex correlation and W_2 is the power in the main signal channel) as a function of increasing range can be used to measure differential attenuation and differential phase (as path averages over homogeneous sections). From these complex plane plots they were able to determine the anisotropy of the propagation medium and the first measurements in rain and snow were at Ku-band and later at X-band in [16], which, additionally, used “slow” switching between right-hand and left-hand circular polarizations. Some years later Hendry confided to one of the authors (V.N.B) that one personal highlight of their Ku-band measurements in snow was the recognition that the particles responsible for the circular depolarization ratio (i.e., the larger nonspherical aggregates with large variance of shapes) were different from those that contributed most to the differential propagation phase (i.e., horizontally oriented plate-like ice crystals). As described in the Canadian work, a principal conclusion was that raindrops form a highly oriented anisotropic propagation medium with symmetry axis near vertical. They also determined that differential phase shift due to oriented ice crystals aloft in thunderstorms could reveal changes that correlate with lightning discharges [17]. Later, using real-time displays of differential propagation phase shifts based on polarization agile (H, V)-basis data, the aforementioned changes could be easily identified by rapid RHI scans through thunderstorm cores aloft. There the differential propagation phase would decrease with range as electrostatic fields oriented the crystals vertically. The lightning discharge that followed relaxed the crystals into

horizontal orientation and the differential phase would start increasing with range [18,19]; the process repeated at regular intervals. One of the authors (V.N.B) witnessed this repetitive “charge” and “discharge” phenomena by observing real-time displays on the Colorado State University–University of Chicago and Illinois State Water Survey (CSU-CHILL) radar RHI scans with chief engineer David Brunkow and it was a thrilling moment to see electromagnetic theory at work in nature and to observe it so easily.

In collaboration with NRC Canada, an S-band circularly polarized radar funded by the Alberta Research Council was built for hail detection using a combination of reflectivity, circular depolarization ratio, and cross-correlation [20,21]. However, effects of the transmission matrix on circular polarization radar observables resulted in depolarization of the transmitted wave due to pure differential phase shift in heavier rain that made it difficult to separate the backscatter effects from the effects due to propagation, as modelled in [22]. It was not until a decade later when Anthony Holt and David Bebbington from the UK re-analyzed the Alberta Research Council (ARC) data and devised a method for “correcting” the differential propagation phase that enabled recovery of the “intrinsic” backscatter elements of the coherency matrix [23]. In a follow-up article [24], Holt gave a simpler derivation and, in addition, provided algorithms to retrieve differential propagation phase and differential reflectivity (Z_{DR}). In [25] the ARC radar data were “corrected” and re-analyzed to show that combined use of reflectivity, Z_{DR} and to some extent the “degree of orientation” could identify hail and rain-hail mixtures.

It is noteworthy that the prototype and 13 preproduction units of the Weather Surveillance Radar 88 Doppler (WSR-88D) had circular polarization (WSR-88D is the US National Weather Service Doppler radar). However, unlike the Canadian radars, they were not configured to measure the full coherency matrix, but rather only one element (e.g., transmit right-hand circular (RHC) and coherently receive the “main” signal in the left-hand circular (LHC) port). This and other technical details of the future WSR-88D were confidential to protect the intellectual property of the bidding companies. Istar Zawadzki and Martin Hall were among the first ones to find out and they alerted researchers in the USA, including Dusan Zrnic (D.Z.). Differential propagation phase measurements in rain with the Cimarron dual-polarization radar (see Section 7) was reported in [26]. They proposed a relation between the specific differential phase (K_{DP}) and rain rate. From this relation and the Marshall Palmer $R(Z)$ relation, D.Z. quickly computed the differential phase along some radials of reflectivity. The results indicated that the differential propagation phase could easily reach 180° in strong convective rain. The voltage in the intended LHC port can be simply expressed as $V_L = \cos(K_{DP} \bullet r)$ where r is the range to the resolution volume [2]. Since it is assumed that two-way differential propagation phase (defined as $2K_{DP} \bullet r$) reaches 180° or $K_{DP} \bullet r$ reaches 90° , the LHC port receives no signal whereas the returned signal would be terminated at the RHC port. Recognizing that this “artificial” loss in the return signal would be devastating, D.Z. wrote a memo about this loss to Dr. Vernon Derr, the director of the Environmental Research Laboratories (National Severe Storms Laboratory is one of these laboratories), who informed the National Weather Service (NWS). The transmit polarization was soon changed to linear horizontal. This issue raised awareness among the NWS personnel about the impact of radar polarimetry.

Meanwhile scientists from the National Center for Atmospheric Research (NCAR) (Rit Carbone) and Illinois State Water Survey (Gene Muller) lead by Thomas Seliga (Ohio State) approached the NWS with a request to include dual-polarization in the forthcoming Weather Surveillance Radar 1988 Doppler (WSR-88D) or Next Generation Weather Radar (NEXRAD). The NWS postponed the decision about dual-polarization but insisted in the procurement specifications that contractors furnish technical/conceptual details on how they would upgrade to dual-polarization in the future. Ultimately, Andrew Canada, the antenna subcontractor to the winner of the award, manufactured a dual-polarization feed with orthomode transducer (OMT) (their proprietary design) and measured the patterns at the two polarizations. Their feed-OMT was later installed on the NEXRAD antenna for proof-of-concept of the dual-polarization upgrade [27].

An important development occurred in 1990 when the CHILL (University of Chicago-Illinois State Water Survey) S-band radar was relocated to Colorado State University as a national facility

funded by the National Science Foundation (NSF) for both education and research with close cooperation between the Departments of Atmospheric Science (Steven Rutledge) and Electrical Engineering (V.N.B., the lead author of this review; later joined by V. Chandrasekar). Under the leadership of the late Gene Mueller and engineer David Brunkow, the CSU-CHILL radar was continuously upgraded and in 1995 was configured with two transmitters (the second transmitter was a spare from the Norman radar at NSSL) and dual-receivers which allowed for a number of operating modes. In particular, the two transmitters could be “fired” either alternately or simultaneously (with equal power to approximate slant 45° linear state), and receiving the H and V components of the backscattered field. Comparing polarimetric data from these two modes in rain and demonstrating their consistency [28] was an important initial result that assisted the proof-of-concept of the dual-pol upgrade alluded to above.

Calculations of the scattering matrix (both back and forward directions) for a single particle at low frequencies (Rayleigh scattering) and higher frequencies (non-Rayleigh scattering) is an important application of EM theory. It models the expected values of radar observables as functions of size, shape, orientation, and dielectric constant, as well as the incidence angle. The radar observables are obtained from averages of the covariance matrix elements (i.e., second order temporal moments) whereas the transmission matrix elements ensue from coherent integration of the forward scatter amplitudes [14]. Typical “bulk” assumptions are (1) particle size distributions based on gamma *pdf*, (2) equivalent spheroidal shapes with mean axis ratios either fixed or specified as a function of size, (3) Gaussian orientation distributions with mean and standard deviation fixed or dependent on tumbling/wobbling or degree of melting or riming, and (4) effective medium approximations for the dielectric constant of particles, e.g., low-density or mixed-phase.

Substantial literature exists for Rayleigh scattering, either analytical such as Gans’ method for spheroids (as derived in [29]) or numerical (for arbitrary shapes) that solve the quasistatic surface integral equation for the electric potential using method of moments [29,30]. The range of shapes for which the equivalent spheroid assumption is reasonable is given in [30] for Rayleigh scattering. They found that for convex shapes (e.g., cylinders, cones) especially with an axis of symmetry, the equivalent spheroid is reasonable, but shapes that have concave surfaces or are multiply-connected (e.g., torus) cannot be approximated by spheroids. In the mid-1970s, Gans’ method was frequently used for rain drops, solid ice “plates” (oblates with axis ratios of 0.05 or less), and needles (prolates with axis ratios of 20 or higher). The effective medium approximations for the dielectric constants of inhomogeneous particles such as snow aggregates (ice–air mixture) or wet snow (ice–water–air mixtures) or spongy hail (ice–water mixture) are generally based on [31] but they are valid only if the inclusions or “grains” within the matrix material (e.g., ice inclusions in water) are small so that they can be treated as dipoles. The formulas do account for interaction between dipoles as in the Clausius–Mossotti equation (see [32]) so are valid for dense packing of the inclusions within the matrix. Thus, Gans’ method for spheroids combined with effective medium approximations were often used to model observed polarimetric signatures [13].

For non-Rayleigh scattering, numerical methods such as T-matrix for rotationally symmetric shapes have been available since the mid-1970s [33,34]. Charles Warner later mentioned to V.N.B. that by chance he and A. Hizal were sharing office space and Hizal casually mentioned to him that he had developed T-matrix code for scattering by spheroids and asked whether there was any application for it. Warner recognized its value, to the best of V.N.B.’s recollection, rewrote the code, and used it to calculate scattering by oblate rain drops [34]. The two-layer T-matrix [35,36] has been used for water-coated spheroidal hail or melting conical graupel [37,38]. The scattering by arbitrary shaped particles using the method of moments solution of the surface electric field integral equation was used for disks (solid ice plate-like crystals) [39]. For inhomogeneous particles the method of moments solution of the volume integral equation was well-developed in the electrical engineering community by the mid-1970s but not used by the radar meteorology community. However, the Fredholm integral equation method used by the radiowave propagation community is based on the volume integral equation for the electric field interior to the particle [40]. Both volume and surface integral formulations fall in the class of Fredholm integral equations of the second kind involving the

tensor free space Green's function which is singular due to the self-term which is usually evaluated analytically. The method in [40] uses a Fourier transform approach in which the transformed volume integral equation is nonsingular. The case of the ellipsoid afforded some simplifications so the code developed was restricted to spheroids and ellipsoids and was applied to ice crystal scattering by [41]. Perhaps this restriction limited more widespread use of this method. This is unfortunate as it was shown to satisfy the Schwinger variational principle and is thus known to be convergent and numerically stable [40].

The discrete dipole approximation (DDA) [42]), which also falls in the class of volume integral equations (but formulated using the concept of the "exciting field"), was used for *mm*-wave scattering by complex-shaped ice crystals and rimed aggregates but not frequently during the period covered in this article [43]. A comparison of DDA for hexagonal plates and columns (of solid ice found in cirrus clouds) with volume-equivalent oblate and prolate spheroids was done by [44]. Using the DDA as reference, they showed that errors in backscatter cross-sections at H and V-polarizations computed with spheroid approximations were <15% at 35 GHz (for typical sizes of crystals in cirrus clouds).

Whereas polarization agility and/or diversity were nascent in radar meteorology, in parallel significant work was ongoing in the remote sensing community. Specifically, airborne polarimetric synthetic aperture radar observations of ground features including cities, fields, and forests were made. Moreover, theoretical works aimed at studies of rigid bodies with possible tactical applications were in progress. Wolfgang Boerner, from the University of Illinois at Chicago, organized a NATO-sponsored workshop in 1998 in Bad Windsheim, Germany. He invited representatives from the three communities to facilitate exchange of information. The presentations were published in a two-volume book edited by Wolfgang Boerner [45]. This book contains two hundred pages on radar polarimetry for meteorological observations.

3. Ohio State-Illinois Water Survey Collaboration

Thomas Seliga (T.S.) was Director of the Atmospheric Sciences Program within the Electrical and Computer Engineering department at Ohio State University (OSU) at the time when one of the authors (V.N.B.) joined him as a graduate student in 1973. The problem that T.S. posed was the measurement of rain rate without invoking $R(Z)$ power laws but via estimation of the intercept (N_0) and median volume diameter (D_0) of an assumed exponential drop size distribution. At that time T.S. and V.N.B. were aware of (1) the wind-tunnel data of [46], which gave a simple linear expression for drop axis ratio (b/a) versus D in the form $b/a = 1 - \beta D$ and (2) the conclusions in [47] that rain drops formed an anisotropic propagation medium with high degree of orientation. T.S. suggested a simplistic view of Rayleigh scattering by oblates arguing that an H-polarized wave would induce an electric dipole moment and related radar cross-section varying as a^6 (a being the major axis) whereas a V-polarized wave induced moment and related cross-section as b^6 (b the minor axis). Thus, small deviations in axis ratio would be amplified if the ratio $(b/a)^6$ were considered. A colleague suggested we use Gans' method, as in [48], for scattering by oblate spheroids. Subsequently, the differential reflectivity technique for estimating R was presented by V.N.B. at an URSI conference in Boulder in 1974 followed by [49] where Z_{DR} versus D_0 and $\log(Z_h/N_0)$ versus D_0 were given on the same plot to emphasize the retrieval of (N_0 , D_0) and hence R . T.S. also included two block diagrams to measure Z_{DR} . The first was based on polarization agility or pulse-to-pulse switching between H and V polarizations and sequential reception of the H and V polarized components of the backscattered wave via the same receiver. The second was polarization diversity, whereby the transmitted wave was fixed at slant linear 45° polarization and simultaneous reception of the H and V-polarized components were made via two receivers. T.S. knew from his prior research on wave propagation in the ionosphere at Penn State that receivers could be built that measure small differential amplitude (and differential phase shifts) very accurately, hence the assumption in [49] was made that Z_{DR} could be measured to within 0.2–0.5 dB.

While taking an advanced EM class at OSU, V.N.B. was introduced to Waterman's T-matrix method of scattering by conducting bodies of revolution, and realized that it could be applied to oblate raindrops. A fortuitous event led Peter Barber to send his T-matrix code to OSU for this

application [33]. The National Hail Research Experiment (NHRE) was ongoing and there appeared to be interest in scattering by nonspherical melting hail (i.e., water-coated hail) which could be solved using a two-layer T-matrix approach [36,37,50]. At about the same time, Humphries' PhD thesis [51] on depolarization effects of rain on circular polarized waves inspired [52] to suggest that differential propagation phase termed as $\Delta\Phi$ normalized by N_0 could be related to D_0 which together with differential reflectivity might provide better accuracy in estimation of R . The simple formula in [43] for coherent wave propagation was used along with T-matrix calculations for the forward scatter amplitudes. However, at that time an algorithm to estimate $\Delta\Phi$ using pulse-to-pulse switching data was not available (that appeared later in a conference paper by Mueller) [53].

In 1977, Ramesh Srivastava, who was Principal Investigator for the CHILL facility, arranged a science meeting at the University of Chicago where Gene Mueller thought it feasible to use "slow" switching (0.5 s switch time) between alternate batches of (1500) H and (1500) V pulses to measure Z_{DR} . In the mid-1950s, Gene had already worked on drop shapes and scattering by spheroids, which appears to have played a role in his enthusiasm. The CHILL antenna had a feed/OMT for dual-pol capability but unused as yet. The feed/OMT was sent to OSU where the E/H-plane patterns were measured at the Electrosience Laboratory. The feed was a dual-mode Potter horn that gave well-matched E/H-plane patterns and the OMT had good port-to-port isolation. The antenna engineering staff indicated the feed was good for our application. It might be of interest to know that T.S. consulted with the famous antenna expert John Kraus (inventor of the helical antenna and Big Ear Radio Telescope, who was retired but still at OSU at that time) about dual-polarization radar measurements and Kraus' response was "to keep it simple". In retrospect, this was sound advice as there is no simpler concept than the two systems for measuring Z_{DR} outlined by T.S. in [49]. In the summer of 1977 and during the waning days of the Severe Environmental Storms and Mesoscale Experiment (SESAME) project in Oklahoma (OK), the first "slow"-switched Z_{DR} data in rain were obtained which showed that it could be measured and fell in the range predicted from theory [11]. In 1981, the first high-power switchable ferrite circulator (from an NSF grant awarded to Ohio State) was installed on the CHILL radar enabling measurement of "fast"-switched Z_{DR} . Seliga and Mueller presented these data in 1982 at a URSI conference in the UK [64].

A series of articles on the microphysical interpretation of Z_{DR} , CDR, and specific differential phase in terms of, respectively, the reflectivity-weighted mean axis ratio, the mean and variance of the latter, and the product of W (rain water content) and the deviation of the mass-weighted mean axis ratio from unity were published in [54,55]. The axis ratio distributions from Jones' [56] camera data which are extreme and not supported by later drop shape studies were used. Nevertheless, the interpretations are, in essence, applicable given the *pdf* of axis ratios. Assuming a linear relation of the form $b/a = 1 - \beta D$, the Z_{DR} and specific differential phase were related to the ratio of 7th to 6th moments of the drop size distribution (DSD), and to the product of W , β , and the ratio of the 4th to 3rd moments (caveat is that β from Jones' data is too low and biased to mean drop axis ratios closer to sphericity) [54,55].

4. Ohio State and Appleton Laboratory Collaboration

In 1977 a fortuitous meeting between Martin Hall of the Appleton Laboratory in the UK and Thomas Seliga at an URSI conference in La Baule, France, led to "fast" pulse-to-pulse switched Z_{DR} measurements. A surplus air-surveillance S-band radar had been installed on the 25 m reflector antenna at Chilbolton, UK, for studies of rain attenuation along slant paths as part of radiowave propagation experiments. It was recognized that the parameters of the DSD were needed to estimate attenuation (which could then be scaled to Ku-band) so the decision was taken by Martin Hall and the chief engineer, Steve Cherry, to build a motor-driven rotary vane switch integrated with a turnstile polarizer coupled to a scalar feed as one unit. A small NATO grant enabled collaboration between Appleton and OSU. In 1978, Martin and Steve came to OSU with time series of power samples at H and V polarizations with antenna stationary and from a single movable range gate. OSU was tasked with deriving the statistics of the normalized amplitude ratio of the H and V signals (the radar was incoherent) as a function of the correlation between the pulse pairs in the simpler case of

uncorrelated sequence of (H,V)-pairs. An article on the bivariate chi distribution presented sufficient information to obtain the *pdf* of the normalized amplitude ratio with the correlation coefficient as a parameter. The agreement between theory and time-series analysis was unexpectedly good especially for correlation coefficients close to 1. The analysis was written up in a conference paper which was presented at a URSI conference organized by Profs. Riedler and Randeu in Graz, Austria [57]. At that conference, McCormick wrote down a formula for Z_{DR} in terms of the elements of the coherency matrix at circular polarization [58]. As mentioned earlier, [24] derived the same after “correcting” for differential propagation shift in rain (see, also) [59].

During a visit by V.N.B. to Appleton Labs in 1982, Steve Cherry had collected a substantial set of time-series data which enabled a more detailed study of the statistical fluctuations of Z_{DR} and the “optimal” estimator for Z_{DR} starting from the 4×4 correlation matrix of the complex voltages. The expressions for mean and variance of Z_{DR} were adapted from [60,61] resulting in the article [62].

5. Rutherford-Appleton Laboratory/Chilbolton Radar

A landmark article in *Nature* describes in more spatial detail (afforded by the narrow 0.25° beam) the application of Z_{DR} [12]. It included detection of ice (graupel) melting to rain in convection, snow aggregates melting to rain in stratiform events (with bright-band), and the spatial variability of the DSD parameters (N_0 , D_0). This and the table of particle type classification based on (Z_H , Z_{DR}) were largely responsible for rapid acceleration of polarization agile radar development in the US [63] and in Europe (initially France, then Russia, Italy, and Germany, see Section 8). In 1982, an URSI Commission F symposium on Multiple-Parameter Radar Measurements of Precipitation [64] was held in Bournemouth, UK, with Martin Hall as the Symposium Chair. Seventy-nine attendees from 15 countries participated in ushering a new chapter in weather radar polarimetry. Subsequently, the conference papers were published in a Special Issue of *Radio Science* in 1984, edited by Martin Hall [65].

The article by [66] in that special issue again stands out for providing details of the vertical profile of Z_H and Z_{DR} with height in stratiform rain with bright-band. A layer of positive Z_{DR} up to 4 dB at -10°C was inferred to be caused by horizontally oriented plates (-10°C being a growth region of dendritic crystals by vapor deposition). At lower heights to -5°C , aggregation was inferred by increasing Z_H (larger maximum sizes) but lower Z_{DR} (lower bulk density and irregular shapes). The peak in Z_{DR} (around 1.3 dB) due to partially melting snow was located near the base of bright-band just prior to the rapid transition to fully melted smaller rain drops. Another important example (which they termed as a “rare” occurrence) was a narrow column of high Z_H and Z_{DR} extending to 1.5 km above the melting level in convection and interpreted as supercooled rain drops carried up in the updraft. The above two examples, just based on (Z_H , Z_{DR}), inspired substantial research on the microphysical origins of the full complement of polarimetric signatures in winter storms and in positive Z_{DR} columns in convective storms that is still ongoing.

In the same special issue, Chilbolton radar data were used to construct a frequency distribution of (Z_H , Z_{DR})-pairs in rain and a rain–ice separation boundary was identified [67]. Data pairs that fell outside the rain area were inferred to be graupel/hail depending on the Z_H values. This led to defining the quantitative HDR hail signature in [68] but, more importantly, to defining two-dimensional membership functions for rain in fuzzy-logic schemes [69–71].

Another article in the same special issue described the use of optical array probes on the University of Wyoming King Air [72]. Based on Thomas Seliga’s suggestion, one of the probes was oriented in the conventional manner with vertical optical axis (giving the top view) and another with horizontal axis (side view). When penetrating light rain shafts, the top-view images were circular while the side-view images were elliptical. Careful analysis of the axis ratios using the side view images by William Cooper showed good agreement on average with the axis ratios from Green’s theory for $2 < D < 4$ mm [73]. The mean axis ratio versus D relation is vital for Z_{DR} estimation of D_0 and subsequently much research has been done to establish this on a firmer basis including wind-tunnel measurements [74] and 2D-video disdrometer measurements [75] as well as the numerical prediction of equilibrium shapes [76]. A curve fitting approach using available axis ratio data from a

variety of somewhat uncertain experimental and laboratory results (perhaps with compensating errors) has since been widely used [77].

Using the Chilbolton radar, a seminal paper on observations of Z_{DR} in the ice region of a stratiform rain event with aircraft-mounted particle imaging probes was published [78] which largely corroborated the inferences in [66]. Large positive Z_{DR} were found in layers of “plate-like” crystals with low Z_H , but when mixed with larger snow aggregates they found a “masking” effect, i.e., Z_{DR} tended to 0 dB as Z_H increased due to aggregation [78]. The shapes of snow aggregates (which dominates the Z_{DR}) are highly irregular with effective permittivity much lower than solid ice, both of which cause Z_{DR} to be close to 0 dB. Their paper spurred substantial polarimetric applications in winter precipitation using S, C, and X-band systems.

At about 1985, Anthony Illingworth (University of Manchester UK) infused new energy to the Chilbolton radar research by encouraging a steady stream of students interact with the RAL staff (John Goddard and Jon Eastment) and by focusing on cloud physics. A seminal article describes the possible microphysical origin of (Z_H , Z_{DR}) signatures in isolated echoes from initial stage (low concentration of large drops formed by coalescence processes) to vigorous updraft stage where positive Z_{DR} columns extend to about -10 °C; this indicates lofting of rain into the cold part of the cloud [79]. They also describe the dissipating stage where (Z_H , Z_{DR}) in the rainshaft are consistent with exponential DSDs. The ultragraining aerosol hypothesis in [80] and a simple coalescence growth model was used to predict the (Z_H , Z_{DR}) [81]. The evolution from initial echo stage where low concentrations of large drops formed via coalescence was compared with radar measurements and found to be in good agreement [81].

Sometime in 1986–1987, a second receiver was added to the radar by Jon Eastment permitting linear depolarization ratio (LDR) measurements. Statistics of ΔZ_H , which is the difference between the peak value of Z_H in the bright-band (BB) and the rain below, was given in [82]. The mode of ΔZ_H was about 10 dB which occurred with large LDR values of about -15 dB indicating wet snow. In contrast, in stratiform rain with weak embedded convection the $\Delta Z_H \approx 0$ dB with lower LDR < -20 dB indicative of more compact rimed snow or graupel melting (with weak or no BB signature) to form rain. The engineering modifications to the Chilbolton radar circa 1994 are described in [83], which includes Doppler velocity and differential phase with all variables displayed in real-time.

6. Colorado State-NCAR-Ohio State/Penn State Collaboration

In 1983, the Army Research Office funded three institutions (listed above) for continuing polarimetric studies using the NCAR CP2 dual-wavelength radar. Earlier in 1981, J. Vivekanandan joined CSU as a PhD student, V. Chandrasekar in 1982, Joseph Turk in 1986 and John Hubbert in 1988, all under VNB. Thomas Seliga provided the second high-power switchable ferrite circulator, which was installed on the CP2 radar under the leadership of Charles Frush, who was able to “tune” the transmit and receive port-to-port isolation to better than 30 dB (the manufacturer’s specification was minimum 20 dB of isolation). The field program MAYPOLE (May Polarization Experiment ‘83) had the NCAR Wyoming King Air with cloud and precipitation probes mounted with H and V optical axes (4 probes in all) for in-situ validation.

In 1984, Frush also led the installation of a second X-band antenna and receiver on the CP2 pedestal to measure the cross-pol reflectivity and thus LDR (the copol reflectivity was measured by the original X-band part of the dual-wavelength system). This second antenna was rotated by 90° relative to the original antenna. Both antennas were military surplus coaxial Cassegrain design with a polarization twist sub-reflector, which greatly reduced blockage, resulting in low side lobes (< -30 dB). The two-way integrated cross-polar ratio was around -32 dB based on antenna pattern measurements at the National Bureau of Standards. However, the S-band antenna had high close-in side lobe levels (around -23 dB) in the principal planes due to blockage by the 4 support struts which were located in these planes. Apart from the side lobe levels, the mismatch in the close-in side lobe levels between H and V-polarizations caused large Z_{DR} errors in the presence of even modest spatial gradients of Z_H [84,85]. At the suggestion of Thomas Seliga, the support struts were rotated by 45° in late 1986, which resulted in much better Z_{DR} data quality in the presence of gradients [86].

The first article on hail detection using Z_{DR} hail signature in strong convective storms was published in 1984 [87]. In a two-part series of articles [88,89], Part 1 used the detailed melting model of graupel [90] together with T-matrix (and two-layer T-matrix) scattering calculations, CP2 radar measurements, and aircraft data to show good agreement in the vertical profiles of Z_H , Z_{DR} and LDR between radar and model in two convective cases. This was perhaps the first such coupling of microphysical model output to EM scattering model specifically for melting graupel (the “dry” graupel size distribution aloft and sounding for the melting model were initialized with aircraft data). In the Part 2 article [89], CP2 radar data were used to compare the spatial distribution of Z_{DR} , LDR, and dual-wavelength signatures in several hail storms. They showed very good spatial overlap of the signatures as well as consistency with scattering model predictions. The vertical structure of dual-wavelength hail signatures (>5 dB) above 0°C level, enhanced LDR (> -20 dB), due to wet hail aloft and prominent Z_{DR} hail signatures below the melting level demonstrated the value of combining polarimetric and dual-wavelength radar data.

In 1986, V. Chandrasekar and Peter Brockwell of the Statistics Department at CSU devised a method to simulate polarimetric radar signal fluctuations assuming the Doppler spectra at HH and VV polarizations were Gaussian with specified correlation coefficient [91]. This procedure simulates the statistical fluctuations in Z_H , Z_{DR} and differential phase more realistically (depending on wavelength, spectral width, number of sample pairs, and pulse repetition time as compared to simply assuming ad hoc Gaussian errors for the radar variables. The goal was to understand, using simulations, the error structure of polarimetric radar estimation of rain rate using different algorithms based on $[Z_H, Z_{DR}, K_{DP}]$ [92]. For disdrometer simulations, the DSD was modelled as the product of N_T and the *pdf* (D) where N_T is the total number of drops per unit volume assumed to be Poisson distributed and the *pdf* (D) was assumed to be the gamma *pdf* [93]. This form involves “double” random variables so the mean and variance of moments of the DSD, and correlation between moments, involved random sums over random number of total drop counts and random drop sizes. In [93], simulations of disdrometer-induced fluctuations in Z-R were compared with simulations of radar Z fluctuations with R (with full range of expected physical variations included). They showed quantitatively that disdrometer Z-R correlations would be much higher relative to radar-based Z-R correlations under ideal conditions [93]. A three-part series of papers followed on the error structure of radar and disdrometer measurements of rainfall using Z_{DR} , X-band specific attenuation, and differential propagation phase [94–96].

In 1986, the CP2 radar was moved to Huntsville, AL, with two NCAR C-band radars as part of a triple Doppler network for the Microburst and Severe Thunderstorm (MIST) project headed by the late Theodore Fujita. The PIs for the CP2 radar were V.N.B. and Gregory Forbes from Penn State while Roger Wakimoto was in charge of radar operations. The South Dakota School of Mines and Technology (SDSM&T), T-28, and University of North Dakota (UND) Citation aircraft also participated for in situ measurements of precipitation in the interior of >50 dBZ convective cells. MIST provided the first opportunity to deploy a polarimetric dual-wavelength radar in a subtropical climate. Very quickly it was apparent that warm rain processes in early echoes (low Z_H and positive Z_{DR}) were ubiquitous as were positive Z_{DR} columns extending to -10°C in more vigorous convective updrafts. It was David Johnson who alerted V.N.B. (via Roy Rasmussen) to look for positive Z_{DR} in early echoes (with warm cloud bases) and their evolution based on his ultragrantic aerosol hypothesis. The freezing of supercooled rain as inferred from the disappearance of the positive Z_{DR} columns was almost always followed by a lightning discharge which was monitored in real time by Steve Goodman from NASA/Marshall to his great excitement. Dusan Zrnic happened to visit the CP2 radar during MIST and he, too, was greatly impressed by the real-time observations of positive Z_{DR} column evolution. The time evolution of an isolated microburst-producing storm was described in [97] from early echo stage to vigorous growth stage to heavy precipitation loading by small wet hail in the dissipating stage along with cloud photos of the evolution on which contours of Z_H were overlaid (true to the Fujita style of analysis and hand-drawn graphics by Roger). In a landmark article, the same storm was analyzed using triple Doppler synthesis in addition to Z_{DR} , specific attenuation at X-band (A_x), and dual-wavelength ratio (DWR) hail signatures from early echo to dissipating stage [98].

The time–height cross-sections of multiple radar observables (Z_H , Z_{DR} , A_x , DWR, and updraft speeds) gave an excellent opportunity to synthesize the “bulk” microphysical evolution of the storm. The co-authors, Harold Orville and Fred Kopp of SDSM&T, used their two-dimensional time-dependent cloud model initialized with the morning sounding to compare with the radar observations [98]. By and large, the model microphysical evolution was consistent with radar observations during the vigorous growth and microburst-producing phases.

Around 1987, the Battan Memorial Conference with a commemorative volume of review papers on Radar in Meteorology was being planned by David Atlas, Robert Serafin, and Rit Carbone, which was published by the AMS in 1990. The early years of dual-polarization radars were reviewed in [99]. The status of dual-polarization radar research, at that time including circular and linear polarization configurations, was also reviewed [100]. Hendry built a comprehensive table listing the system characteristics of nearly all of the dual-polarized radars which were in use or had just been decommissioned [100].

The microphysical inferences of polarimetric signatures using CP2 radar data especially positive Z_{DR} columns extending several km above the 0 °C level and the enhanced LDR “cap” at the column top signifying mixed phase region (supercooled rain and wet ice) which can rapidly evolve into severe hailstorms were reviewed in [101]. They also showed the vertical structure of dual-wavelength and LDR signatures in a hailstorm and discuss the different scattering aspects, i.e., non-Rayleigh scattering at X-band versus depolarization due to wet, non-spherical hail.

One of the last deployments of the CP2 radar in the US was in Florida in 1991 for the Convective and Precipitation/Electrification (CaPE) project which involved the NOAA P-3 and T-28, as well as the NCAR and Wyoming King Airs. Multiple Doppler synthesis, radar observables [Z_H , Z_{DR} , A_x , LDR], and in situ microphysical and electric field mill data were used to study the evolution of thunderstorm cells [102]. The mixed phase region inferred by overlapping enhanced LDR “cap” and a core of enhanced specific attenuation on top of positive Z_{DR} columns (at about −10 °C) was validated by aircraft penetrations. Storm electrification was positively correlated with the first appearance of the mixed phase signatures aloft [103].

In 1994, a Workshop on Weather Radar Polarimetry for Research and Operations was held at NCAR with 29 scientists in attendance [104]. To set the stage and to foster discussion, 16 short presentations were made highlighting the progress made so far and future avenues needing research prior to operational systems development. There was good motivation for improved quantitative precipitation estimation (QPE) from the weather agencies and for hydrological applications represented by Bob Saffie. The need for validation of rainfall algorithms using a dense network of gages was emphasized, including the use of differential propagation phase when rain is mixed with hail in strong convection. However, the important agenda was to replace the CP2 system with a new, easily transportable S-band radar without radome, with a high-quality antenna and feed and new digital intermediate frequency (IF) receivers and real-time displays of all the polarimetric variables.

In 1995, the CSU-CHILL radar with a new parabolic reflector antenna and two transmitter system with dual-receivers was able to deliver high quality polarimetric data including LDR with system limit approaching −34 dB. In addition, measurements of the correlation between the copol and cross-pol signals were available. Thus, the full covariance matrix (three real powers and three complex correlations) data were available with high accuracy for the first time. Among the first articles that followed [105] was a description of the distinct polarimetric signatures in a supercell storm. A chase van equipped for manual collection of hail, and instrumented with a rain gauge, intercepted the storm core for 50 min. The loud pounding of golf ball-sized hail while trying to take notes on changing hydrometeor types as well as collecting hail every few minutes in plastic bags with time stamps, chilling them in hexane, and bagging them in dry ice was an unforgettable experience for the two nonmeteorologists, V.N.B. and John Hubbert. Locations of peak horizontal convergence (from dual-Doppler synthesis) were found to be centered on well-defined positive Z_{DR} columns. An enhanced LDR “cap” area on top of the positive Z_{DR} column was interpreted as a region of large drops mixed with partially frozen and frozen hydrometeors, consistent with [101]. A positive K_{DP} column on the western fringe of the main updraft was

hypothesized to be the result of copious numbers of small drops (1–2 mm) shed by wet hailstones. Swaths of large hail at the surface (inferred from LDR signatures) and positive Z_{DR} at 3.5 km AGL suggested that potential frozen drop embryos were favorably located for growth into large hailstones.

The microphysics and kinematic evolution of convective storms studied so far with CP2 and CSU-CHILL radars took a major leap towards understanding the electrical characteristics [106]. The dual-pol radar-inferred graupel volume suspended in a vigorous updraft in upper portions of the storm was strongly correlated with in-cloud (IC) lightning flash rate. In addition, the radar-inferred maxima in the hail rate were related to peaks in the cloud-to-ground (CG) lightning flash rate. Both correlations were consistent with the non-inductive charging mechanism, which is caused by collisions between graupel/hail particles and ice crystals in the presence of supercooled water. The research published in [106] led to substantial further research on application of polarimetric radar for storm electrification studies.

7. National Severe Storms Laboratory

The NSSL is the research arm of the US National Weather Service (NWS) with the mission of advancing the understanding of weather processes, research to improve forecasting and warning techniques, and development of operational applications. NSSL is NOAA's primary radar laboratory for advancing radar technology, the prime example being NSSL's role leading up to the deployment of the WSR-88D Doppler systems (NEXRAD) by the NWS. The next technology to attract the attention of Richard Doviak (R.D., leader of the Advanced Techniques Group) was dual-polarization, the potential of which was not explored as yet by NSSL. One of the authors (D.Z.) joined NSSL in 1978 and was assigned to lead dual-polarization radar studies. Both R.D. and D.Z. attended the first Workshop on Dual-Polarization Radar in 1980 chaired by Metcalf and Humphries. In 1979, R.D. and D.Z. visited with Humphries in Alberta to evaluate their S-band circularly polarized radar. They concluded that the coherency matrix using circular basis could not be easily related to bulk precipitation properties and decided in favor of dual-linear polarizations.

In 1981, NSSL placed an order with Raytheon for the same ferrite switchable circulator as installed on CHILL and CP2 radars. The ferrite phase shifters were known to be especially sensitive to temperature and it took Raytheon three trials to meet the specifications, but fell short. The switch was delivered in 1983 and its characteristics were measured in the laboratory and later reported in [107]. NSSL chief engineer Dale Sirmans, with John Carter and Mike Schmidt, "tuned" the switch for stable and near optimal performance and installed it on the NSSL radar in Cimarron, OK. At that time D.Z. did not realize the full potential of polarization agile "fast"-switched data. He had the foresight to decide that time series of the complex voltages ($I+jQ$) at H and V-polarizations gave the most flexibility in signal processing for computing polarimetric variables other than Z_{DR} . At slow antenna scan speeds, it was possible to acquire data from tens of kilometers in range.

In 1983, M. Sachidananda (M.S.) from India came to NSSL as an NRC associate to work with D.Z. A landmark article by M.S. and D.Z. [108] was published in 1985 where they (1) computed the var (Z_{DR}) in the "fast"-switched mode accounting for correlation between all the samples in the H,V sequences (a generalization) of [62]), (2) where they related the zero-lag correlation coefficient $|Q_{hv}(0)|$ to physical properties of the scatterers, and (3) computed the var (Z_{DR}) in the mode where slant linear 45° polarization is transmitted with simultaneous reception of H and V-polarized components of the elliptically polarized backscattered electric field (suggested) in [49]. In this case, the 2×2 coherency matrix has 2 power terms and one complex correlation which by definition is at zero lag or Q_{hv} . The var (Z_{DR}) in this mode involves the term $1 - |Q_{hv}|^2$ which implies that if $|Q_{hv}|^2$ is sufficiently close to 1, then the var (Z_{DR}) will reduce correspondingly. They estimated that $|Q_{hv}|^2$ due to raindrop shape variations (e.g., oscillations) or drop canting would be 0.99 or larger. Any decorrelation due to mixture of particle types such as rain-hail or wet snow shapes or tornado debris or even ground clutter would lower $|Q_{hv}|^2$ pointing to its utility as a useful radar measureable.

Another important paper [109] was published in 1986 where they compute the variance of differential propagation phase (Φ_{dp}) based on two estimators of which the better one was given by [53] and used in polarization agile "fast"-switched radars. The derivation for the var (Φ_{dp}) is

complicated but the end result is that it can be measured with standard deviation of a few degrees. In both [108,109] the authors drew on important works concerning pulse pair estimators of Doppler velocities [110–113] to obtain the statistics of the polarimetric variables (Z_{DR} , Φ_{dp}). In [109] they define $\Delta\Phi$ as the range derivative of Φ_{dp} and show that rain rate (R) derived from $\Delta\Phi$ is less sensitive to DSD variations than Z – R relations. In a follow-up article, the field of $\Delta\Phi$ from sector PPI scans were used to illustrate the range of values and their spatial variability [26]. Later, the specific differential phase (K_{DP}) was defined as one-half the range derivative of Φ_{dp} to be consistent with the radiowave propagation literature. In 1986, M.S. departed but details of algorithms used for mean Doppler velocity, differential phase, and correlation coefficient were contained in the notes of M.S. and D.Z. Soon thereafter, D.Z. assembled these notes into a Cooperative Institute for Mesoscale Meteorological Studies (CIMMS) report [114], which was widely distributed in the US and overseas with the aim of accelerating dual-polarization research. The specific algorithms for Doppler spectral width and the decoupling of mean Doppler velocity from Φ_{dp} were given in [115]. For the record, NSSL produced reports many of which are on its Web site.

N. Balakrishnan (N.B.), from the premier Indian Institute of Science (IISc) in Bangalore where he was a faculty member in Aerospace Engineering, joined NSSL as a NRC associate from 1987–1989. Both M.S. and N.B. obtained their PhD from IISc and were fellow graduate students. Soon after N.B. joined NSSL, he requested the T-matrix and two-layer T-matrix codes from V.N.B., who knew him well from past visits to IISc. Using his strong background in EM and scattering theory, N.B. made full use of these codes in innovative ways. In a seminal conference paper in 1989, a method was proposed for correcting for path integrated attenuation (PIA) using differential propagation phase especially at higher frequencies such as C- and X-bands [116]. They recognized that both the specific attenuation (A) and the specific differential phase (K_{DP}) were approximately related to the fourth moment of the DSD from which linear relations of the form $A = \alpha K_{DP}$ were formulated. In a similar manner, they also formulated a linear relation between specific differential attenuation between H and V polarized waves (A_{DP}) and K_{DP} . Simulations based on gamma DSDs were used to show the accuracy of these linear relations [117]. The latter article also provided experimental data from the polarimetric dual-wavelength CP2 radar by collecting time-series data in heavier rainfall from which X-band PIA was shown to be highly correlated with S-band Φ_{dp} . After range filtering they showed that specific attenuation (A_x) was linearly related to S-band K_{DP} which confirmed the theoretical predictions. The straightforward correction of measured reflectivity and differential reflectivity, which are strongly attenuated due to propagation in rain, invigorated the use of polarimetric X-band weather radars (and network of X-bands) in the next two decades.

In another landmark article, time series data from the S-band NSSL radar in Cimmaron, OK, (or, CIM) were processed to simultaneously derive [Z_H , Z_{DR} , K_{DP}] in a hailstorm [118]. They made a keen inference that in a precipitation shaft composed of rain-hail mixtures, the hailstones due to tumbling or irregular shapes could be considered “isotropic” thus not contributing to the $Re(f_{h-v})$ whereas the highly oriented oblate rain drops were the main contributors to $Re(f_{h-v})$. This follows from coherent addition of the forward scattered waves from the rain and hail. Thus, hail was “transparent” to K_{DP} and this permitted the estimation of the rain water content in the precipitation shaft. RHI scans through the main precipitation shaft showed the height profiles of K_{DP} as well as the separation of hail and rain amounts [118]. The descent of the hail and heavy rain to the surface (precipitation loading in the downdraft) was reflected by a lowering (or depression) of the height of the K_{DP} column. They also described examples of interesting positive K_{DP} above the 0 °C level, which was interpreted as possible supercooled drops lofted upwards in the updraft [118]. Substantial research in the next two decades on this topic followed, especially in tornadic supercells.

The use of the correlation coefficient for hail detection and possible separation of small hail (<2 cm) from larger hail was explored in [119] using scattering simulations (including backscatter differential phase δ) and comparing them with measurements by the CIM radar. While processing of time-series data from the CIM radar was tedious, it led to further insights of the utility of polarimetric variables. For example, RHI scan data in the stratiform region of a mesoscale convective system were used to show a “dip” in the correlation coefficient (<0.90) at the base of the bright-band [120]. They

also derived the variable δ by examining the range profiles of Φ_{dp} and noting locations where there were localized deviations from the usual monotonic range profiles. Comparing the measured δ ($\approx 5^\circ$) with a forward scattering model they were able to infer 10 mm wet aggregates at the base of the bright-band. For Rayleigh scattering the $\delta \approx 0$ so the onset of non-Rayleigh scattering at S-band is about 10 mm or so for wet ice. The “dip” in the correlation coefficient was largely ascribed to non-zero values of δ as opposed to variance of shapes occurring at the base of the bright-band. The statistics of one estimator of $|Q_{hv}(0)|$ was given in the Appendix of [120] in the form of plots of the standard deviation and bias versus number of (H,V)-pairs with Doppler spectrum width as a parameter. The standard deviation varied from 0.03–0.06, which was considered sufficient for detection of hail and bright-band. The statistics of $|Q_{hv}(0)|$ under low signal-to-noise ratio (SNR), non-Gaussian spectra and both simultaneous and alternate sampling can be found in [121]. They found that simultaneous sampling (slant 45° transmit with simultaneous reception of H and V) gave much lower standard deviation in the range 0.003–0.006.

In the early 1990s, real-time calculations and displays of $\{Z_H, Z_{DR}, K_{DP}, Q_{hv}\}$ were not yet implemented on CIM radar or any other S-band radar in the US. Hence, a number of scientists in the US visited NSSL to collaborate with D.Z. on “slow” scanning time-series data which were unique at that time. They included V.N.B., V. Chandrasekar, and John Hubbert (from Colorado State) and K. Aydin from Penn State. One example was a hailstorm with supercell characteristics that was moving in the direction of the CIM radar. V.N.B., K.A., and the technician Mike Schmidt barely made it on time to start the radar as the leading edge of the storm approached. There was only time to set up RHI scans on the fly (i.e., “blind”) without knowing where the storm core was located. The intense hailstorm with golf ball-sized hail and intense rain rate went overhead and lightning brought the radar “down” after 30 min of data collection. Polarimetric data analysis from this hail storm, and based on the range of values of the four radar variables and scattering simulations, a schematic of three vertical cross-sections depicting hydrometeor classification for three periods were shown in [122]. The classification showed the varying height of the mixed-phase or melting level; light, medium, and intense rain rates; large hail; rain-hail mixture; graupel; oriented ice crystals and bright-band along with single Doppler-based up and down drafts. While subjective, the schematic synthesized much of the knowledge available at that time in terms of self-consistency of the radar variables, scattering calculations, and melting models. D.Z. constructed a classification Table with input from NSSL staff (Burgess and Doviak) and other scientists which was included in Chapter 8 (2nd edition) of [123].

Real-time calculations and displays of all the polarimetric variables and Doppler moments were completed by Allen Zahrai in 1992 including remote control of the CIM radar. It was a “first” for any polarization agile “fast”-switched system in the US. These advances, together with the exact equations for calculating the radar variables, were described in detail [124] and have been used by many organizations. Real-time data from CIM (no longer limited by “slow” antenna scan rates) over the entire unambiguous range have been used to analyze the evolution of a supercell storm [125] providing much more temporal and spatial detail than was possible in [122] including vertical cross-sections through the hail core and relative locations of updraft and downdrafts. Decades later, the microphysical origin of polarimetric signatures in tornadic supercells are still being studied.

In an innovative article [126], a method using polarization agile radar was proposed for measuring the three real and three complex terms of the covariance matrix by appropriately controlling the high power “fast”-switch (assuming high port-to-port isolation >40 dB in both transmit and receive states). The copolar and cross-polar signals are sequentially routed to a single receiver [126]. The trade-off is between parallel processing with two receivers versus sequential processing with one receiver. Most advanced radar systems have, however, been designed with polarization agility on transmit with dual-channel receivers.

8. France, Russia, Italy, and Germany

The S-band radar at the University of Clermont-Ferrand in France was modified for pulse-to-pulse switching between H and V-polarizations using a high power ferrite switchable circulator and

a single receiver [127]. To the best of our knowledge, the first article that correlated (Z_H , Z_{DR}) signatures in hail with a hail pad network is [128]. Specifically, they showed the time variation of Z_H and Z_{DR} over periods ranging from 6–30 minutes over the hail pad locations. From the hail pad data, the total number per m^2 and maximum size of hail were estimated for the duration of each event. They found negative Z_{DR} values in the range -0.4 to -1 dB with Z_H peaks of 60 dBZ during the very heavy hail intensity. For less intense hail events, the peak Z_H was about 54 dBZ with Z_{DR} in the range 0.6–2 dB. The correlation between maximum hail size and Z_H alone was low at 0.68 but when Z_{DR} was included the correlation improved to 0.86.

The Russian production incoherent X-band radar was modified for Z_{DR} measurements using a high-power switchable ferrite circulator and a single logarithmic receiver [129]. The transmit pulse sequence was either alternating [HVHV...] or the sequence [HHVV...]. The second sequence was used to estimate the correlation at zero lag from 1-lag estimators but from amplitude samples from the output of a logarithmic receiver. They show (Z_H , Z_{DR}) data from summertime convection near the St. Petersburg area collected in 1990 and largely confirm the prior inferences on positive Z_{DR} columns extending, in one example, a staggering 8 km above the melting layer. They estimated severe differential attenuation at X-band at 0.3–0.4 dB/km, which is about a factor of 10 larger than predicted in [117]. Features such as positive Z_{DR} layers aloft in winter stratiform cold rain events, the peak in Z_{DR} at the base of the bright-band, and a “dip” in the zero lag correlation coefficient were consistent with prior results [129]. They also report on the expected values of the latter coefficient to distinguish between ground clutter and precipitation echoes.

The Italian and German C-band dual-pol radar development began in the early–mid-1980s [130,131]. Both radar systems opted for an offset feed reflector antenna (without radome) for low side lobes (<-32 dB) but the two linear cross-polar lobes can be high in the azimuthal plane (peaks of -27 dB located off boresight but within the main beam) and vanishingly small in the elevation plane. Consequently, the two-way integrated cross-polar ratio was estimated (at best) to be -35 dB. The Italian system (Polar 55C) was designed for polarization agility (pulse-to-pulse switching between H and V-polarizations) for Z_{DR} measurements using a high-power switchable ferrite circulator but the ferrite circulator limited the isolation to 20–25 dB or so. The radar was installed near Florence in 1990 as part of a real-time integrated Arno River flood forecasting system. The first operational dual-pol radars (network of three) appears to have been for the Emilia Romagna weather service and they are still operational (1991–present). These C-band dual-pol systems featured dual-offset Cassegrain reflector antennas for simultaneously achieving excellent side lobes and cross-pol performance with polarization agility capability using high power ferrite circulator switches.

The German system was built by Enterprise Electronics Corporation in 1986 with the signal processors provided by SIGMET. The polarizer microwave network was unique in that a variable ratio power divider and latching ferrite phase shifters under software control could be configured for transmission of any elliptical polarization state. After transmission, the receive polarization state could be configured for receiving any two orthogonal polarizations (generally copol and cross-pol to the transmitted state). They had two receivers, one for each state. A detailed description of this radar system is given in [131]. Examples of range profiles of the various polarimetric variables are in [132] focusing on iterative filtering of Φ_{dp} to derive K_{DP} and δ

In 1987, the NCAR King Air was flown to Germany (German Aerospace Research Establishment (DFVLR) near Munich) for in situ measurements of particles in coordination with radar observations. In one stratiform event, the aircraft flew in a layer of pristine crystals (dendrites) where Z_{DR} was large in the range 3–4 dB with low Z_H (10–20 dBZ) and then flew into a region of rimed dendrites and aggregates of dendrites where the Z_{DR} was reduced (<0.5 dB) with higher Z_H (30 dBZ) confirming the earlier results in [78] but with a better suite of optical array probes and cloud water measurements. The particle images were analyzed and classified manually into pristine crystals, rimed crystals, and aggregates, and quantitative frequency of occurrences of these types were calculated which confirmed the radar inferences.

An organized line of convective cells was observed by [133] with the feeder cells ahead of the line convection showing low Z_H and large Z_{DR} (4–5 dB) consistent with active coalescence processes

whereas in the heavier precipitation within the convective line the Z_H was about 60–65 dBZ with large Z_{DR} values of up to 7 dB. These large Z_{DR} values occur at C-band due to resonant scattering of 6–7 mm drop sizes. The vertical profiles of [Z_H , Z_{DR} , K_{DP} , and δ] showed values consistent with two-layer T-matrix calculations of water-coated hail, especially the measurements of large backscatter differential phase shift (δ) of 10–20°. The precipitation shaft was inferred to contain heavy rain and small melting hail with water torus (<10 mm).

9. Conclusions

It has taken nearly 35 years from the mid-70s to 2011 for dual-polarization to be given the go-ahead for operations in the US. It is the most major and complex upgrade to occur since the WSR-88Ds were deployed in the mid-1990s. This article has documented the research and institutions that spearheaded the way from circular polarized radars in the mid-70s to the polarization agile “fast”-switched radars that dominated until the mid-90s. While the seminal contributions have been summarized, perhaps too succinctly, it is our hope that the next generation of radar meteorologists will come to appreciate the early history (at least from the mid-1970s) and imbibe the flavor of the kinds of articles appearing largely (but not entirely) in the *Trans. IEEE* or *Radio Science* journals. We hope that some of the “behind the scenes” descriptions of interactions between the authors and their colleagues or serendipitous events has enlivened the article and kept the reader engaged. In the nearly two decades since 1994 the applications of radar polarimetry to meteorology has expanded way beyond what the early pioneers could have reasonably imagined including nontraditional applications such as tornado debris, volcano eruptions, insect/bird migration patterns, or smoke plumes from forest fires (this issue).

While the role of electromagnetics in dual-polarization radar is fundamental, we have taken an expansive view in this article by documenting the work that has spawned further research often many years or even decades later. The references we chose to mention are, of course, subjective to some degree but were highly regarded and cited during the period covered and continue to be cited.

Concerning polarization basis, we have come full circle, starting with circular and then agile linear (H,V) followed by the “hybrid” mode radars (such as WSR-88D). In it, the transmitted polarization state has unknown ellipticity but known H and V components, and measured is the coherency matrix of the elliptically polarized backscattered wave in the (H,V) basis using two receivers. This mode is now standard for operational weather radars and the major radar manufacturers offer this in their product line.

The microphysical inferences from polarimetric radar data during the period of this article were largely based on an observational approach with supporting scattering calculations using simple models of particle shape, orientation, or dielectric mixture formulas and at times using a 1-D detailed graupel/hail melting model. Validation was often sparse except during dedicated field programs involving aircraft-based instrumentation or surface disdrometers and rain gages. Dual-pol was often considered as an esoteric topic by most meteorologists and cloud physicists but that changed significantly by the early-90s with hydro-meteorologists also being entrained by prospects for more accurate QPE using [Z_H , Z_{DR} , K_{DP}] in some “optimized” form. We seem to have also come full circle in QPE to using specific attenuation alone as an operational algorithm for the WSR-88D (the specific attenuation being a by-product from constrained attenuation-correction algorithms using Φ_{dp}).

In the abstract of the recent article by Zhang and co-authored by 27 leading scientists, the comment is made that “The potential impact of PRD (polarimetric radar data) has been limited by their oftentimes subjective and empirical use. More importantly, the community has not begun to regularly derive from PRD the state parameters, such as water mixing ratios and number concentrations, used in numerical weather prediction (NWP) models” [134]. While there is some merit in their statement, the polarimetric radar community, by and large, has used rigorous theory, carefully conducted experiments, and solid data analysis without which the operational agencies of many countries and especially the NWS would not have gone ahead with the WSR-88D upgrade.

Most numerical microphysical schemes predict the number concentration and mass but do not predict what is important for forward modelling the polarimetric variables, e.g., shape, orientation,

or particle density. Some recent schemes predict bulk physical properties such as mean density, rime mass fraction, liquid fraction on mixed phase particles, and even ice crystal aspect ratios which are closer to what is needed for forward modelling [135–137]. There has been a recent push for Lagrangian particle-based approach where the evolution of the particle size distribution is described in a truly multidimensional microphysical phase space by predicting physical properties such as ice mass, rime mass and rime volume, and liquid water fraction, as well as all warm rain processes [138,139]. This major shift in numerical microphysical models bodes well for forward modelling the polarimetric variables and ultimately to assimilation of radar data in NWP.

Dual-polarization radar topics specific to meteorology were first covered in Chapter 8 of [123]. Seventeen years later a book devoted entirely to polarimetric Doppler weather radar was published [2]. Since then, the book by Rauber and Nesbitt [140] starts with the treatment of EM waves and later devotes 50 pages to dual-polarized radar while the book by Zhang [141] is entirely on radar polarimetry covering both fundamentals and applications with rigor. The most recent book by Ryzhkov and Zrnic [3] covers the fundamentals but also offers the most comprehensive treatment of the applications of radar polarimetry to meteorology available to date. These books bode well for the next generation who can come up to speed very quickly and make original contributions to the field.

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Abbreviations

The following abbreviations are used in this manuscript:

AMS	American Meteorological Society
ARC	Alberta Research Council
CIM	Cimarron, Oklahoma
CIMMS	Cooperative Institute for Mesoscale Meteorological Studies
CSU-CHILL	Colorado State University-University of Chicago and Illinois State Water Survey
DDA	Discrete Dipole Approximation
DFVLR	German Aerospace Research Establishment
DWR	Dual-Wavelength Ratio
EDR	Elliptical Depolarization Ratio
EM	Electromagnetics
HDR	Hail Detection
LHC	Left Hand Circular
MIST	Microburst and Severe Thunderstorm (Project)

NCAR	National Center for Atmospheric Research
NEXRAD	Next Generation Weather Radar
NOAA	National Oceanic and Atmospheric Administration
NSF	National Science Foundation
NSSL	National Severe Storms Laboratory
NWS	National Weather Service
OMT	Orthomode Transducer
OSU	Ohio State University
PIA	Path Integrated Attenuation
PPI	Plan Position Indicator
RAL	Rutherford Appleton Laboratory
RHC	Right Hand Circular
RHI	Range Height Indicator
SDSM&T	South Dakota School of Mines and Technology
SESAME	Severe Environmental Storms and Mesoscale Experiment
UND	University of North Dakota
URSI	International Union of Radio Science
WSR-88D	Weather Surveillance Radar 88 Doppler

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