

# FDHE-IW: a fast approach for detecting high-order epistasis in genome-wide case-control studies

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## DME models

The DME (**disease loci with marginal effects**) model has both main effects and interaction effects. Twelve disease models (Model 1-Model 12) are composed of multiplicative model, threshold model and concrete model.

**DME 1- DME 4** ( $H^2=0.005$ ,  $MAF=0.05$ ,  $0.1$ ,  $0.2$  and  $0.5$ ) are **multiplicative models** with two disease locus, in which the disease prevalence given the frequency of genotype combination increases multiplicatively with the incremental presence of the disease. The genetic heritability ( $H^2$ ) of DME 1- DME 4 are all equal to  $0.005$ , minor allele frequencies (MAF) of them equal  $0.05$ ,  $0.1$ ,  $0.2$  and  $0.5$ , respectively.

**DME 5- DME 8** ( $H^2=0.02$ ,  $MAF=0.05$ ,  $0.1$ ,  $0.2$  and  $0.5$ ) are the **threshold models** in which the prevalence of genotype frequency does not increase until the number of disease alleles pass the threshold).

**DME 9- DME 12** ( $H^2=0.02$ ,  $MAF=0.05$ ,  $0.1$ ,  $0.2$  and  $0.5$ ) are **concrete model** used to mimic the effect that epistasis has on susceptibility to handedness and the color of swine (Marchini, et al., 2005; Neuman, et al., 1992).

Table S1 presents the **penetrance functions** of three models (**multiplicative models**, **threshold models**, **concrete model**) [1][2]

Table S1. Penetrance functions of the three DME epistasis models [2]

Model 1		Loci 1		
		AA	Aa	aa
Loci 2	BB	$\alpha$	$\alpha$	$\alpha$
	Bb	$\alpha$	$\alpha(1+\beta)^2$	$\alpha(1+\beta)^3$
	bb	$\alpha$	$\alpha(1+\beta)^3$	$\alpha(1+\beta)^4$
Model 2		Loci 1		
		AA	Aa	aa
Loci 2	BB	$\alpha$	$\alpha$	$\alpha$
	Bb	$\alpha$	$\alpha(1+\beta)$	$\alpha(1+\beta)$
	bb	$\alpha$	$\alpha(1+\beta)$	$\alpha(1+\beta)$
Model 3		Loci 1		
		AA	Aa	aa
Loci 2	BB	$\alpha$	$\alpha(1+\beta)$	$\alpha(1+\beta)$
	Bb	$\alpha(1+\beta)$	$\alpha$	$\alpha$
	bb	$\alpha(1+\beta)$	$\alpha$	$\alpha$

Table S2. the parameters ( $H^2$ : genetic heritability, the disease prevalence  $P(D)$ ) and the penetrance values of 12 DME models

DME	$H^2$	MAF	P(D)	AABB	AABb	AAbb	AaBB	AaBb	Aabb	aaBB	aaBb	aabb
DME -1	0.005	0.05	0.1	0.098	0.098	0.098	0.098	0.299	0.522	0.098	0.522	0.912
DME -2	0.005	0.1	0.1	0.096	0.096	0.096	0.096	0.197	0.282	0.096	0.282	0.405
DME -3	0.005	0.2	0.1	0.092	0.092	0.092	0.092	0.144	0.181	0.092	0.181	0.227
DME -4	0.005	0.5	0.1	0.078	0.078	0.078	0.078	0.105	0.122	0.078	0.122	0.142
DME -5	0.02	0.05	0.1	0.096	0.096	0.096	0.096	0.533	0.533	0.096	0.533	0.533
DME -6	0.02	0.1	0.1	0.092	0.092	0.092	0.092	0.319	0.319	0.092	0.319	0.319
DME -7	0.02	0.2	0.1	0.084	0.084	0.084	0.084	0.21	0.21	0.084	0.21	0.21
DME -8	0.02	0.5	0.1	0.052	0.052	0.052	0.052	0.137	0.137	0.052	0.137	0.137
DME -9	0.02	0.05	0.1	0.08	0.192	0.192	0.192	0.08	0.08	0.192	0.08	0.08
DME -10	0.02	0.1	0.1	0.072	0.164	0.164	0.164	0.072	0.072	0.164	0.072	0.072
DME -11	0.02	0.2	0.1	0.061	0.146	0.146	0.146	0.061	0.061	0.146	0.061	0.061
DME -12	0.02	0.5	0.1	0.067	0.155	0.155	0.155	0.067	0.067	0.155	0.067	0.067

## Reference

- [1] Marchini, J., et al. (2005) Genome-wide strategies for detecting multiple loci that influence complex diseases, *Nature genetics*, 37, 413-417.
- [2] Jing P J, Shen H B. MACOED: a multi-objective ant colony optimization algorithm for SNP epistasis detection in genome-wide association studies[J]. *Bioinformatics*, 2015, 31(5):634-641.