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# Enhanced Broadband Metamaterial Absorber Using Plasmonic Nanorods and Muti-Dielectric Layers Based on ZnO Substrate in the Frequency Range from 100 GHz to 1000 GHz

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**Abstract:** A broadband thin film plasmonic metamaterial absorber nanostructure that operates in the frequency range from 100 GHz to 1000 GHz is introduced and analyzed in this paper. The structure consists of three layers: a 200 nm thick gold layer that represents the ground plate (back reflector), a dielectric substrate, and an array of metallic nanorods. A parametric study is conducted to optimize the structure based on its absorption property using different materials, gold (Au), aluminum (Al), and combined Au, and Al for the nanorods. The effect of different dielectric substrates on the absorption is examined using silicon dioxide (SiO<sub>2</sub>), aluminum oxide (Al<sub>2</sub>O<sub>3</sub>), titanium dioxide (TiO<sub>2</sub>), and a combination of these three materials. This was followed by the analysis of the effect of the distribution of Al, and Au nanorods and their dimensions on the absorption in the microwave range. The optimized structure achieved more than 80% absorption in the ranges 100–280 GHz, 530–740 GHz and 800–1000 GHz. The minimum optimized absorption is more than 65% in the range 100 GHz to 1000 GHz.

**Keywords:** electromagnetic absorbers; metamaterial absorbers; SiO<sub>2</sub>; Al<sub>2</sub>O<sub>3</sub>; TiO<sub>2</sub>; ZnO; microwave absorbers; plasmonic metamaterial absorbers; absorption spectrum; FDTD

# 1. Introduction

Recently, electromagnetic wave absorbers (EMAs) have attracted researchers' intertest due to their varied applications in the field of energy harvesting, avion stealth, sensing as well as suppressing the increasing electromagnetic radiations from electronic devices everywhere around us.

Classical EMAs depend on multireflection and interference of electromagnetic waves and could be divided into three types: Salisbury absorbers, Jaumann absorbers, and circuit analog absorbers. Salisbury absorbers consist of a metal plate separated from a resistive sheet by a dielectric material of a quarter wavelength thickness [1–3]. The interference between the reflected wave from the bottom metal plate and the upper resistive sheet is destructive and hence, the EM wave is trapped, and the energy is dissipated in the resistive sheet. Jaumann absorbers use the same concept as the Salisbury absorbers, but Jaumann absorbers use more than one resistive sheet to broaden the absorption bandwidth (BW) of the device [4,5]. The analog circuit absorbers' design is the same as Salisbury absorbers' design but with the top resistive sheet replaced by a periodic top metallic reactive surface that makes the analog circuit absorbers frequency selective absorbers [6,7]. The main disadvantage of the three types of classical absorbers is the need of a dielectric material of



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quarter wavelength thickness that makes the absorbing device bulky, with limited design flexibility which in turn limits its applicability.

To overcome the drawbacks of classical EMAs, researchers focused on developing new absorbers with thin thickness, light weight, and tunable absorption. In 2008, the first perfect metamaterial absorber (MMA) was proposed by Landy. The unit cell of Landy's absorber consists of two standard split ring resonators connected by an inductive ring parallel to the split wire with a thin dielectric material between them [8]. Generally, MMAs consist of three main layers: ground metal plane, dielectric substrate, and a top metallic periodic patch. The thickness of dielectric layer can be tailored to be much less than the wavelength of the incident electromagnetic wave. Research in the field of EMAs has been accelerated after Landy's perfect absorber due to the prospective applications of the EMAs such as solar energy harvesting, stealth, biological sensors, refractive index sensors, photodetection, photovoltaic devices, and optical switches [9–17].

EMAs can be structured to absorb EM waves in the spectrum range from microwave to visible region. Y. Cheng et al. have reported a metamaterial absorber composed of a single closed-meander-wire resonator structure placed over a metal ground plane separated by a dielectric substrate. They obtained about 90% absorption at different resonance frequencies in the range from 4 to 12 GHz, but this MMA is not suitable for wide bandwidth applications [18]. Using a periodic array of indium tin oxide (ITO) film sandwiched between two polyvinyl chloride layers, Q. Zhou et al. have designed a metamaterial microwave absorber that achieved 90% absorption in the narrow range from 8 to 18 GHz [19]. S. Lai et al. have proposed an MMA with ITO as the top resonance structure array layer, glass as the medium layer, and another ITO as the bottom ground layer. They achieved more than 80% absorption from 15.6 to 39 GHz [20]. J. Ning et al. designed an MMA that operates in the range from 0.4 to 1 GHz with 90% absorption as well, using magnetic nanomaterial and a varactor [21]. Md. Hossain has reported 99.7% to 99.9% EM wave absorption at triple frequencies 5.37, 10.32, and 12.25 GHz using MMA consisting of two split ring copper resonators separated by a dielectric layer [22]. All of these microwave MMAs have a very narrow bandwidth and operate over a narrow range of frequencies.

Recently, thin film MMAs use localized surface plasmon polaritons (LSPPs) to realize small size thin absorber in visible, infrared, and terahertz ranges of the spectrum. W. guo et al. reported infrared MMA using two gold (Au) metallic layers and ZnS dielectric layer sandwiched between them. They got absorption that exceeded 90% in the range from 7.8 to 12.1  $\mu$ m. The absorption range is enlarged (5.3 to 13.7  $\mu$ m) by using double Au-ZnS-Au layers on the top of each other but with only 80% absorption [23]. Terahertz plasmonic MMA is reported by Y. Kang et al. using an Au substrate followed by a dielectric material of a dielectric constant of 1.96, with an Au cylinder on the top of the dielectric layer. They obtained two 99% absorption peaks at 275 and 440 THz [24]. Using a ground Au plate, and an array of Au resonators on top of silicon dioxide (SiO<sub>2</sub>) substrate, D. Katrodiya et al. have achieved metamaterial broadband solar absorber with an average of 89.79% absorption in the frequency range from 155 to 1595 THz [25]. These reported plasmonic MMAs showed high performance in the infrared and terahertz ranges but suffer from degraded performance in the microwave range.

There is an interest in ZnO driven by its prospects in optoelectronics applications owing to its unique properties such as direct wide band gap Eg~3.3 eV at 300 K. It has been widely known as a versatile material for its different applications in the production of green, blue-ultraviolet, and white light-emitting devices, electronics, and optoelectronics devices. Furthermore, ZnO is known for its strong luminescence in the green–white region of the spectrum, strong sensitivity of surface conductivity to the presence of adsorbed species, and high thermal conductivity. The n-type conductivity of ZnO makes it appropriate for different applications such as metamaterial absorbers [26,27]. On the other hand, SiO<sub>2</sub> is a material of considerable technological importance due to its wide applications in electronics devices, with a very wide bandgap of 9.6 eV [28]. TiO<sub>2</sub>, has been widely investigated in environmental and energy research, due to its wide bandgap

of 3.2 eV, which allows it to absorb the UV light [29]. The combination of these materials will play a vital role in affecting the impedance of the proposed metamaterial absorber.

In this work, we introduced an enhanced broadband thin film plasmonic MMA that operates in the frequency range from 100 to 1000 GHz. An absorption above 80% is obtained in the range from 700 to 1000 GHz, while it fluctuates between 60% and 80% in the range below 700 GHz. This proposed absorber is found to be insensitive to light polarization and the direction of incident light. The paper is organized as follows: first, the proposed design of the plasmonic MMA is presented; then the simulation results are illustrated and discussed which yields to an optimized MMA design. Finally, the conclusion summarizes the process and the results of this research.

## 2. Proposed Structure Design and Its Operation Principle

The typical thin film MMA structure has been adopted in this research, which consists of three layers: a metallic Au ground square plate of 200 nm thickness and cross section area of  $1 \times 10^4$  nm<sup>2</sup>, a  $4 \times 4$  array of metallic equally spaced nanorods of height h = 50 nm and radius r = 60 nm, and a dielectric substrate of height  $h_1 = 60$  nm sandwiched between the ground plate and the metallic rods. The schematic diagram of the adopted structure is shown in Figure 1. The gold ground plate acts as a back reflector layer that is used to enhance light trapping and reflects the transmitted light to the structure for more light absorption [30,31]. The spacing (X) between any two successive nanorods could be calculated as:

$$\mathbf{X} = \frac{\mathbf{L}}{4} - 2\mathbf{r} \tag{1}$$

where L is the side length of the square ground metallic plate, and r is the radius of the nanorod. The distance between the center of the outer rod and the edge of the unit cell is assumed X/2.



Figure 1. Schematic diagram of the adopted typical MMA structure.

The principle of operation of MMAs depends on resonance. When an electromagnetic wave at a resonance frequency coincides on the MMA, a pair of anti-parallel oscillating currents are induced in the ground metallic layer and the upper metallic nanorods so, a magnetic resonance is established. Moreover, local surface plasmons are generated at the resonance wavelength, and electric resonance is established between the ground metallic layer and the nanorods. Absorption is a result of this resonance, as the electromagnetic wave will be confined in the MMA unit cell and electromagnetic power at the resonance

frequency is consumed due to losses in the metallic layer and dielectric layer [8,32,33]. Absorptance (A(f)) of the MMA could be calculated from the relation [34]:

$$\mathbf{A}(\mathbf{f}) = \mathbf{1} - \mathbf{R}(\mathbf{f}) - \mathbf{T}(\mathbf{f})$$
(2)

where R(f) and T(f) are the reflectance and transmittance of the absorber, respectively. The reflectance and transmittance could be calculated from the reflection coefficient ( $S_{11}$ ), and transmission coefficient ( $S_{21}$ ):

$$\mathbf{R}(\mathbf{f}) = |\mathbf{S}_{11}|^2 \tag{3}$$

$$\mathbf{T}(\mathbf{f}) = |\mathbf{S}_{21}|^2 \tag{4}$$

Due to the back reflector metallic ground layer, the transmission coefficient is zero and hence, the absorptance A(f) is given by:

$$A(f) = 1 - |S_{11}|^2$$
(5)

The absorptance depends on the input impedance of the MMA structure, and is given by [20]:

$$\mathbf{A}(\mathbf{f}) = \mathbf{1} - \left| \frac{\mathbf{Z}_{in}(\mathbf{f}) - \mathbf{Z}_{o}}{\mathbf{Z}_{in}(\mathbf{f}) + \mathbf{Z}_{o}} \right|$$
(6)

where  $Z_{in}$  is the input impedance of the MMA structure, and  $Z_0 = 377 \Omega$  is the free space impedance. At resonance, the input impedance is matched to the free space impedance, so perfect absorption occurs at the resonance frequency.

Plasmonic nanorods distributed on the substrate layer change the absorbed optical power inside the proposed structure, the absorption depends on the maximum reflectivity. Nanorod shape and size are the main parameters that affect the absorbed optical power in addition to the relative permittivity of the plasmonic nanorods and dielectric constant of the surrounding medium [35]. The maximum absorption occurred at the wavelength known as  $\lambda_{max}$ , the maximum peak of the wavelength, which can be calculated using Equation (7).

$$\lambda_{\max} = \frac{P}{n} \left( \frac{\varepsilon_n \varepsilon_m(\lambda_{\max})}{\varepsilon_m + \varepsilon_n(\lambda_{\max})} \right)^{1/2}$$
(7)

where  $(\varepsilon_m)$  is the permittivity of the surrounding medium,  $(\varepsilon_n)$  is the plasmonic nanorod dielectric constant at corresponding  $(\lambda_{max})$ , (n) is an integer and (P) is the periodicity of the structural.

Hence, the plasmonic nanorod dielectric permittivity can be calculated using a multioscillator Drude-Lorentz model [35] as shown in Equation (8):

$$\varepsilon_{n} = \varepsilon_{\infty} - \frac{\omega_{D}^{2}}{\omega^{2} + j\omega\gamma_{D}} - \sum_{Y=1}^{6} \frac{\delta_{k}\omega_{k}^{2}}{\omega^{2} - \omega_{k}^{2} + 2j\omega\gamma_{k}}$$
(8)

where  $(\varepsilon_{\infty})$  is the nanorod high-frequency dielectric permittivity,  $(\omega_D)$  is the plasma frequency of the free electrons,  $(\gamma_D)$  is the collision frequency of the free electrons,  $(\delta_k)$  is the amplitude of Lorentz oscillator,  $(\omega_k)$  is the resonance angular frequencies and  $(\gamma_k)$  is the damping constants for (Y) value from 1 to 6.

To calculate the absorbed power, the refractive indexes of all used material are given as follows; TiO<sub>2</sub> follows the Devore model [36], however, the value for silicon dioxide is a function of the wavelength and follows Aspnes and Studna model [37], and the refractive index of zinc oxide is considered as given by Kaur et al. [38]. On the other hand, the refractive index of different plasmonic materials is summarized using Equation (8) in Table 1 [39]. The dielectric constants of the used materials are shown in Figures A1–A4 in Appendix A.

Material	Term	Strength	Plasma Frequency	Resonant Frequency	Damping Frequency
Au	0	0.7600	$0.137188  imes 10^{17}$	$0.000000  imes 10^0$	$0.805202  imes 10^{14}$
	1	0.0240	$0.137188  imes 10^{17}$	$0.630488  imes 10^{15}$	$0.366139  imes 10^{15}$
	2	0.0100	$0.137188  imes 10^{17}$	$0.126098  imes 10^{16}$	$0.524141  imes 10^{15}$
	3	0.0710	$0.137188  imes 10^{17}$	$0.451065  imes 10^{16}$	$0.132175  imes 10^{16}$
	4	0.6010	$0.137188  imes 10^{17}$	$0.653885  imes 10^{16}$	$0.378901  imes 10^{16}$
	5	4.3840	$0.137188  imes 10^{17}$	$0.202364  imes 10^{17}$	$0.336362 \times 10^{16}$
Al	0	0.5230	$0.227583  imes 10^{17}$	$0.000000 \times 10^{0}$	$0.714047  imes 10^{14}$
	1	0.2270	$0.227583  imes 10^{17}$	$0.246118  imes 10^{15}$	$0.505910  imes 10^{15}$
	2	0.0500	$0.227583  imes 10^{17}$	$0.234572  imes 10^{16}$	$0.474006  imes 10^{15}$
	3	0.1660	$0.227583  imes 10^{17}$	$0.274680  imes 10^{16}$	$0.205251 \times 10^{16}$
	4	0.0300	$0.227583  imes 10^{17}$	$0.527635  imes 10^{16}$	$0.513810  imes 10^{16}$

**Table 1.** Plasmonic parameters which are used for the metallic materials.

The proposed structure is analyzed and optimized using an electromagnetic wave solver, Lumerical Finite Difference Time Domain (FDTD) solutions software. In the simulation of a unit cell, the boundary conditions are considered as a periodic structure in x and y directions, and the layers are perfectly matched in z-direction. A plane wave source with a frequency band 100–1000 GHz is used as a light source, and the minimum mesh size is 0.5 nm in all directions with an offset time of 7.5 fs is used for the light source. The absorption of the structure is measured at different frequencies.

#### 3. Results and Discussion

In this section, the adopted MMA structure depicted in Figure 1 is optimized to maximize the absorption of the device over a broad spectral band from 100 to 1000 GHz. First, the absorption of the MMA is measured using Lumerical FDTD solution software for different rod materials, then the dielectric substrate material is optimized, and finally, the geometric dimensions of the rod are optimized.

## 3.1. Effect of the Rod Material on the Absorption of the MMA

The MMA is simulated for different nanorod materials to elect the material that maximizes the absorption. Figure 2 shows the absorption of the MMA, with SiO<sub>2</sub> dielectric substrate, measured when all nanorods are made from gold, and Aluminum. Furthermore, the absorption is measured when the nanorods are arranged such that aluminum and gold rows are alternating as shown in Figure 3. The height and radius of the nanorods are h = 50 nm and radius r = 60 nm, respectively, and the height of the dielectric substrate is chosen as  $h_1 = 60$  nm. It is clear from Figure 2 that the absorber with Au nanorods has better absorption than the absorber with Al nanorods in high frequency range from 600 to 1000 GHz, while the opposite behavior is observed in the lower frequency range from 300 to 600 GHz. Using alternating rows of Au, and Al, the absorption is somewhere between that of the two cases.

The absorption of the MMA depends on the material of the nanorods as the resonance frequency depends on the current generated in the metallic nanorods and the generated plasmons which depend on the material. Additionally, according to the RLC model of the MMA, absorption depends on the losses in the dielectric material and ohmic losses of the nanorods [40]. The average absorptions in the three cases are calculated by finding the area under each curve divided by the frequency span (1000–100 GHz). The obtained average absorption values are 72.09%, 69.94%, and 73.56% in case of Au nanorods, Al nanorods, and alternating rows of Au and Al nanorods, respectively. Hence, the design of the typical structure is modified to that shown in Figure 3 with alternating rows of Au, and Al nanorods.



Figure 2. Absorption of the MMA structure.



Figure 3. Schematic diagram of the MMA structure with alternating rows of Au, and Al.

## 3.2. Effect of the Dielectric Substrate Material on the Absorption of the MMA

The absorption of the modified MMA structure shown in Figure 3 is investigated with different dielectric substrate materials of 60 nm fixed thickness. The dimensions of each nanorod in the alternating rows of Au, Al are fixed to h = 50 nm and radius r = 60 nm. Figure 4 shows the absorption of the MMA structure, with Al<sub>2</sub>O<sub>3</sub>, SiO<sub>2</sub>, and TiO<sub>2</sub> substrates. The absorption of the MMA with SiO<sub>2</sub> substrate is the highest in the longer frequency ranging from 600 to 1000 GHz, while the MMA absorber with TiO<sub>2</sub> substrate has the worst absorption over this frequency range. The maximum absorption using SiO<sub>2</sub> substrate exceeds 95%, but the MMA with TiO<sub>2</sub> substrate has the best absorption over the frequency range below 450 GHz with 96% absorption peak at 363 GHz, and another 92% peak at 423 GHz. According to Equation (6), the absorption of the MMA depends on the input impedance of the absorber, which depends on the permittivity, permeability, and refractive index of the dielectric substrate [21].



Figure 4. Absorption of the modified structure using different dielectric substrate materials.

The average power absorbed by the MMA is calculated from the obtained absorption spectrum and the absorbed power is 73.6%, 71%, and 70% for  $SiO_2$ ,  $Al_2O_3$ , and  $TiO_2$  dielectric substrates, respectively.

As MMAs with SiO<sub>2</sub>, or Al<sub>2</sub>O<sub>3</sub>, give a high absorption in the frequency range above 600 GHz, and MMA with TiO<sub>2</sub> substrate has its peak absorption in the frequency range below 450 GHz, in the next stage, the absorption of the absorber is investigated with multi-dielectric layers substrate, as shown in Figure 5.



**Figure 5.** Modified MMA substrate with multi-dielectric layers substrate: (**a**) Two substrates on top of each other; (**b**) two side-by-side substrates.

The performance of the absorber is investigated in two cases. The first case is shown in Figure 5a, where the two substrates are on top of each other, while in the second case shown in Figure 5b, the dielectric substrates are side-by-side, each sharing 50% of the ground plate area. All combinations of SiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub>, and TiO<sub>2</sub> dielectric substrates are tested to elect the substrate that will give better absorption over a wider band. The absorption of the MMA for the first case is shown in Figure 6a, and for second case is shown in Figure 6b. The difference in the absorption of the absorber between case 1 and case 2 is because of the different overall equivalent capacitance of the absorber which in turn changes the input impedance of the absorber and affects its absorption. The minimum absorption, maximum absorption and average absorption are listed in Table 2.



**Figure 6.** Absorption of the multi-dielectric layers MMA structure: (**a**) Two dielectric layers on top of each other; (**b**) Two side-by-side dielectric layers.

	Dielectric Substrate Material	Minimum Absorption	Maximum Absorption	Average Absorption
	SiO <sub>2</sub>	37.6%	90.8%	73.6%
Single dielectric layer	$Al_2O_3$	39.4%	91.4%	71.0%
	TiO <sub>2</sub>	43.7%	96.1%	70.0%
	TiO <sub>2</sub> -SiO <sub>2</sub>	33.2%	99.0%	69.8%
Multi-dielectric lavers	TiO <sub>2</sub> -Al <sub>2</sub> O <sub>3</sub>	33.7%	97.7%	71.0%
on top of each other	SiO <sub>2</sub> -TiO <sub>2</sub>	36.3%	93.5%	72.4%
(The first one is the	SiO <sub>2</sub> -Al <sub>2</sub> O <sub>3</sub>	37.3%	97.7%	72.7%
upper layer)	Al <sub>2</sub> O <sub>3</sub> -TiO <sub>2</sub>	35.6%	94.7%	72.7%
	Al <sub>2</sub> O <sub>3</sub> -SiO <sub>2</sub>	38.5%	96.4%	67.4%
	TiO <sub>2</sub> -SiO <sub>2</sub>	54.8%	92.7%	71.6%
Side-by-side	Al <sub>2</sub> O <sub>3</sub> -SiO <sub>2</sub>	41.5%	92.7%	71.5%
multi diciccule layers -	TiO <sub>2</sub> -Al <sub>2</sub> O <sub>3</sub>	52.6%	93.3%	73.4%

Table 2. Absorption for different dielectric substrates.

The calculated data presented in Table 1 shows that the absorption of the device is affected by the position of the dielectric layer, and the highest absorption is achieved when the multi-dielectric layers are  $TiO_2$ -SiO<sub>2</sub> with SiO<sub>2</sub> is the bottom layer. It's reported that when the top layer is a strong absorber, then the overall absorption of the whole device increases. Small reflection coefficient (S<sub>11</sub>) of the top layer is a crucial requirement [41]. Furthermore, the minimum absorption is enhanced from 37.6%, and 43.7% in case of single SiO<sub>2</sub>, and single TiO<sub>2</sub> layer, respectively, to 54.8% when side-by-side TiO<sub>2</sub>-SiO<sub>2</sub> layers are used. This means that the minimum absorption increases by a factor between 25.4% and 46%. Hence, the TiO<sub>2</sub>-SiO<sub>2</sub> side-by-side multi-dielectric layers structure with 71.6% average absorption is elected for further enhancement.

## 3.3. Effect of the Au, Al Array Distribution and Rod Dimensions on the Absorption of the MMA

The structure is modified for further investigation, the nanorod distribution is changed from the alternating rows of nanorods shown in Figure 5b to alternating Au, Al nanorods, so each nanorod is surrounded by four nanorods of the other material as shown in Figure 7.

The absorption of the structure is shown in Figure 8. As an effect of the new nanorods distribution, average power absorption is elevated to 75.7%, the maximum absorption is increased to 94.2%, while the minimum absorption becomes 59.3%.



Figure 7. MMA side-by-side multi-dielectric layers structure with alternating nanorods distribution.



**Figure 8.** Absorption of the side-by-side multi-dielectric layers MMA structure with alternating rows of nanorods and alternating nanorods.

The distribution of the nanorods changes the distribution of the local surface plasmons induced which affects the electric field in the dielectric material. The absorption of the electromagnetic wave in the dielectric material depends on the magnitude squared ( $|E|^2$ ) of the electric field, which is strongly affected by the design of the structure.

The effect of the radius of the nanorods on the absorption of the MMA is investigated. The radius of the alternating Au, Al nanorods is changed from 40 to 70 nm, while the rod height is fixed to 50 nm, and the absorption is measured in each case. The obtained results are shown in Figure 9a. The effect of the radius is neglected as the maximum absorption is about 94% for all cases and the minimum absorption is between 59.3% and 60%. Moreover, there is a small variation in average absorbed power between 76% and 77%. In addition, the nanorod height is changed from 50 to 80 nm to be optimized. The absorption decreased to almost zero around 400 GHz with nanorods of height 70 nm and 80 nm and increased at the same frequency to 95% with nanorods of height 50 nm then decreased to 55% at 300 GHz, as illustrated in Figure 9b. The optimum nanorod radius and height are 50 nm and 60 nm, respectively.



**Figure 9.** Absorption of the side-by-side multi-dielectric layers MMA structure with alternating nanorods with: (**a**) varying radius from 40 to 70 nm; (**b**) varying heights from 50 to 80 nm.

Finally, a ZnO layer of different thicknesses, 40–70nm, is added on top of the Au ground plate. Recently, ZnO is used to increase the interaction of incident electromagnetic waves and the substrate dielectric layer and thus increase the absorption of the MMA over the operating frequency range [42]. The measured absorption without the ZnO layer and with the ZnO layer of different thicknesses is shown in Figure 10. Adding ZnO layer slightly increases the maximum absorption as illustrated in Table 3. According to the following optimization steps, the optimized structure is shown in Figure 11, where a ZnO layer of thickness 60 nm is added on top of the back reflector. Hence, the optimum design gives an average absorption of 84%, minimum absorption of 65.9% and maximum absorption of 100%.



**Figure 10.** Effect of adding ZnO layer with different thicknesses, 40–70 nm, on the absorption of the absorber.

The enhanced absorption is illustrated in Figure 12 when the ZnO layer is grown on top of the Au layer and used as a base for  $TiO_2$ -SiO<sub>2</sub> materials. The absorption is more than 80% in three different regions, 100–280 GHz, 530–740 GHz and 800–1000 GHz, which represent almost 95% of the band. On the other hand, the obtained absorption is more than 65% in the range from 100 GHz to 1000 GHz.

ZnO Layer Thickness	Minimum Absorption	Maximum Absorption	Average Absorption
Without ZnO layer	59.3%	94.0%	77.0%
$h_3 = 40 \text{ nm}$	60.0%	95.7%	83.3%
$h_3 = 50 \text{ nm}$	55.5%	94.9%	83.5%
$h_3 = 60 \text{ nm}$	65.9%	100%	84.0%
$h_3 = 70 \text{ nm}$	62.4%	95.1%	82.1%

Table 3. Absorption for different dielectric substrates.



Figure 11. MMA side-by-side multi-dielectric layers structure with alternating nanorods distributed on ZnO substrate.



**Figure 12.** The optimum absorption is more than 65% in the range 100–1000 GHz, and with 65.5% of the band over 80% absorption.

The electric field and magnetic field distributions and absorbed optical power are shown in Figure 13 at three different frequencies (230, 450, and 700 GHz). At 450 GHz, there is an electric and magnetic resonance in the  $TiO_2$  layer where the maximum power is absorbed. On the other hand, at 700 GHz, the electric and magnetic field resonance occurs in the  $SiO_2$  and the ZnO layer where the maximum power absorption takes place. Moreover, some power is absorbed by the plasmonic nanorods. The effect the ZnO layer is clear at 700 GHz, as the absorbed power increased due the power absorbed in the ZnO layer. At



450 GHz, where one minimum absorption occurs, Figure 13 shows that no resonance occurs at this frequency which leads to minimum power absorption shown at this frequency.

**Figure 13.** Absorbed optical power, electric field distribution, and magnetic field distribution in the proposed MMA structure at different frequencies.

## 3.4. Effect of the Incidence Angle and Light Polarization on the Absorption of the MMA

The direction of the incident light and its polarization play an important role in the performance the MMA, so this effect is investigated in this section. Figure 14 shows the absorption of the MMA for different incident angles ranging from 0° (normal incidence) to 70° in a step of 10°. Changing the incidence angle, slightly alters the performance of the absorber with some ripples are observed in the absorbed power. The minimum, maximum, and average power absorbed at different angles are shown in Table 4. The maximum absorbed power changes over a range from 100% to 98.6% which represents a 1.4% decrease in maximum absorption. While the average absorption changes from 84% to 93.3% (about 11% increase), the minimum absorption increases from 65.9% to 78.4% at 50°.



the incident wave is far away from the object and angular stability over a  $30^{\circ}$  range is enough to ensure absorber stability [20].

Figure 14. Absorption of the proposed optimized MMA structure for different incident angles.

$\theta = 0^{\circ}$	Minimum Absorption	Maximum Absorption	Average Absorption
Direct	65.9%	100%	84%
$10^{\circ}$	61.8%	99.1%	86.9%
$20^{\circ}$	70.3%	98.8%	89.9%
$30^{\circ}$	72.1%	98.6%	92.1%
$40^{\circ}$	77.5%	98.8%	93.3%
$50^{\circ}$	78.4%	99.1%	93.3%
$60^{\circ}$	63.4%	99.1%	91.5%
$70^{\circ}$	45%	98.8%	84.5%

Table 4. Absorption for different values of incident angle.

The effect of light polarization is investigated by changing the direction of light polarization angle from  $0^{\circ}$  to  $90^{\circ}$  in a step of  $15^{\circ}$ , as shown in Figure 15. Due to the symmetry of the proposed structure, light polarization has no effect on the absorbed power. The effect of light polarization is then investigated for oblique incidence case where the incident angle is  $30^{\circ}$  and the obtained absorption is shown in Figure 16. It is clear from Figure 16 that the proposed structure is insensitive to light polarization in oblique incidence as well.



Figure 15. Absorption of the proposed optimized MMA structure for different light polarization at normal incidence.



**Figure 16.** Absorption of the proposed optimized MMA structure for different light polarization at oblique incidence ( $\theta = 30^{\circ}$ ).

The development of a broadband MMA operating in the wide range of the spectrum has been challenging until now, but comparing our results with the recently reported MMAs shows that the proposed MMA in this work has larger broadband, from 100 to 1000 GHz, with high maximum absorption 100%. The comparison of the absorber's performance is listed in Table 5.

Related Work	Operating Frequency Range	Maximum Absorption	Technique
Ref. [43]	25–37.5 THz	87%	Ti/Ge/Si <sub>3</sub> N <sub>4</sub> /Ti metamaterial structure
Ref. [44]	6-16 GHZ	Exceeds 80%	Metallic strips fabricated with lumped resistors on a FR-4 substrate
	0.79–20.9 GHz		
Ref. [45]	and	90%	Magnetic absorbing material and a multi-layered meta-structure
	25.1–40 GHz		
Ref. [46]	4.2–7.4 THz	98.21%	Split gold and graphene rings over a dielectric and gold plate.
Ref. [47]	7.22-8.84 GHz	90%	Asymmetric section resonator structure with different sizes.
Ref. [48]	10–17 GHz	90%	Array of alternating copper, and FR-4 disks to form a conical frustum
Proposed structure	100–1000 GHz	100%	Au nanorods/TiO2-SiO2/Au ground plate metamaterial structure

Table 5. Comparison of the MMA performance with recently reported MMAs.

# 4. Conclusions

In this work, a metamaterial absorber structure with multi-dielectric layer is introduced. The structure is optimized to maximize the absorption of the MMA and enhance the minimum absorption of it using SiO<sub>2</sub>-TiO<sub>2</sub> side-by-side multi-dielectric layer on top of a ground Au plate, and an alternating Au, Al nanorods on the dielectric substrate. The ZnO layer is added as a substrate on the top of Au back reflector to enhance the absorption. The MMA has an average absorption of 84%%, a maximum absorption of 100%, and a minimum absorption of about 65.9%. The optimized MMA is shown to have good angular stability as the effect of the incident angle of the electromagnetic wave on the MMA absorption is so small and the absorber is insensitive to polarization for both normal and oblique incidence conditions.

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## Appendix A

The real part and imaginary part of the dielectric constant of the used materials are in the material database of the Lumerical software. These dielectric constant values are shown in Figures A1-A4 for  $A1_2O_3$ ,  $SiO_2$ ,  $TiO_2$ , and ZnO, respectively.



**Figure A1.** Dielectric constant of Al<sub>2</sub>O<sub>3</sub>: (**a**) The real part of the dielectric constant; (**b**) The imaginary part of the dielectric constant.



**Figure A2.** Dielectric constant of SiO<sub>2</sub>: (**a**) The real part of the dielectric constant; (**b**) The imaginary part of the dielectric constant.







**Figure A4.** Dielectric constant of ZnO: (**a**) The real part of the dielectric constant; (**b**) The imaginary part of the dielectric constant.

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