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Wide Bandwidth Silicon Nitride Strip-Loaded Grating Coupler on Lithium Niobate Thin Film

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Abstract: In this research, a vertical silicon nitride strip-loaded grating coupler on lithium niobate thin film was proposed, designed, and simulated. In order to improve the coupling efficiency and bandwidth, the parameters such as the SiO₂ cladding layer thickness, grating period, duty cycle, fiber position, and fiber angle were optimized and analyzed. The alignment tolerances of the grating coupler parameters were also calculated. The maximum coupling efficiency and the −3 dB bandwidth were optimized to 33.5% and 113 nm, respectively. In addition, the grating coupler exhibited a high alignment tolerance.

Keywords: grating coupler; integrated optics; lithium niobate thin film; 3D-FDTD



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1. Introduction

The emergence of lithium niobate on an insulator (LNOI) has greatly promoted the development and progress of integrated optics devices [1,2]. The high refractive index contrast between LN and SiO₂ in LNOI can shrink the photonic devices/circuits and enhance the remarkable optical properties of LN [3–6]. Due to its extraordinary nonlinearity and excellent electrooptical properties, LNOI can be used in a variety of expandable on-chip devices to provide nonlinear wavelength conversion and high-speed optical modulation [7–9]. At present, it is very important to improve the coupling efficiency between an LNOI waveguide and fiber. However, the mode mismatch between optical fiber mode and thin film material makes direct alignment coupling inefficient. A grating coupler is an effective way to solve the coupling problem between an LNOI waveguide and optical fiber [10–12]. A grating coupler has many advantages, such as being able to be positioned anywhere on the chip, a large alignment tolerance, and no requirement for end face polishing.

Silicon nitride (Si₃N₄) has a wide transparent spectrum and high compatibility with the standard complementary metal oxide semiconductor technology [13,14]. It is difficult to etch directly on LN. However, this situation can be avoided by using Si₃N₄ strip loading. Si₃N₄ strip-loaded LNOI can make use of the properties of Si₃N₄ and LN, leading to heterogeneous photonic devices. Various photonic devices have been reported in Si₃N₄ strip-loaded LNOI, including a multiplexer [15], a micro-ring resonator [16], and an electrooptic modulator [17]. A large bandwidth can be obtained by using Si₃N₄ grating couplers, such as Si₃N₄-on-SOI grating couplers [18,19]. Modeling and simulation are indispensable steps in preparing high-quality grating.

In this study, an Si₃N₄ strip-loaded grating coupler on LNOI was studied and simulated based on the three-dimensional finite-difference time-domain method (3D-FDTD). The important parameters affecting the coupling efficiency of the grating coupler, including the grating period (Λ), duty cycle ($DC = \omega / \Lambda$, where ω is the ridge width), the thickness

of the SiO_2 cladding layer (T), the fiber position x (distance between the grating edge and the fiber core in the x -axis, L_x), the fiber position y (distance between the center line of the grating and the fiber core in the y -axis, L_y), and the fiber angle (θ), were optimized, which provided guidance for improving the coupling efficiency of the grating couplers. The tolerance of the grating coupler was also carefully studied due to its great importance for the practical implementation of such a device.

2. Device Design and Methods

The structure of the Si_3N_4 strip-loaded grating coupler on LNOI that was studied from the top to bottom layers included a $0.3\text{-}\mu\text{m}$ -thick Si_3N_4 strip, a $0.5\text{-}\mu\text{m}$ -thick x -cut single-crystal LN thin film, an amorphous SiO_2 cladding layer, and an LN substrate. The cross-sectional diagrams of the grating coupler are shown in Figure 1. The fiber fundamental transverse electric mode (TE_0) was used as the light source to simulate the coupling process between the grating coupler and the optical fiber. Considering the single-mode operation, the small mode effective area, the optical power in the LN thin film, and the bending loss, the thickness of the Si_3N_4 strip-loaded grating coupler was selected as $0.3\text{ }\mu\text{m}$ [20], and it was fully etched. The thickness of the LN film was set to $0.5\text{ }\mu\text{m}$. The parameters Λ , DC , T , L_x , L_y , and θ were varied to maximize the light coupling in the waveguide from the single-mode fiber.

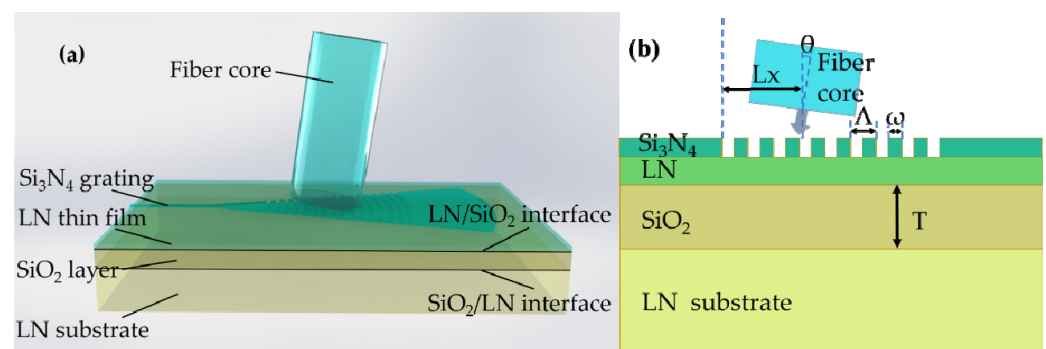


Figure 1. (a) The structure diagram, and (b) schematic cross-section of an Si_3N_4 strip-loaded grating coupler on LNOI.

The mechanism of the grating coupler is as follows: the light of a single-mode fiber was coupled to the grating structure because of the diffraction effect of the grating coupler. When the input field mode was matched to the waveguide mode, the light could be effectively coupled from the single-mode fiber to the waveguide plane. The overlap integral between the input field mode and the waveguide mode could be increased with the optimization of the parameters of the grating coupler to reduce the mode mismatch between the waveguide optical device and the single-mode fiber [21]. The coupling efficiency was defined as the percentage of power converted from the source power to the waveguide plane.

After diffracting through the grating coupler, part of the beam from the fiber was reflected back to the fiber, and part was scattered to the LN cladding. At the LN/SiO₂ interface, part of the power was transmitted to the SiO₂ cladding layer, and part of the power was reflected upwards and transmitted to the grating through the LN cladding layer again. The power was transmitted into the SiO₂ cladding layer. At the SiO₂/LN interface, part of the power that was lost was transmitted into the LN substrate, and part of the power was reflected and propagated upward through the SiO₂ cladding to the LN cladding layer. Based on the commercial software Lumerical FDTD Solutions (Version: 8. 9.1584, ANSYS Inc., South Pittsburg, PA, USA) [22], the 3D-FDTD method under the condition of mesh accuracy of 10 ppw (the number of mesh points per wavelength) was used for simulation and optimization, and the perfectly matched layer (PML) boundary conditions were used to absorb the light emitted from the simulation area. For the FDTD solutions [23], based on the solution of the vector three-dimensional Maxwell equations, the

FDTD method was used to grid the space step-by-step in time based on the time-domain signal to obtain the steady-state continuous wave, resulting in a wide band, and the unique material model could accurately describe the dispersion characteristics of the material in a wide band with embedded high speed. A high-performance computing engine could be used to obtain wide band multiwavelength results in one calculation, simulate any three-dimensional shape, and provide an accurate dispersion material model. For the PML [22], due to the limitations of the computer memory capacity and the calculation speed, the FDTD calculation could only be carried out in a limited area. In order to simulate the propagation process of an ultrasonic wave in a larger area, it was necessary to set the absorption boundary conditions at the boundary of the area to absorb the incident waves and avoid reflecting waves as much as possible. The most common absorption boundary condition was the PML absorption boundary, which could theoretically achieve complete absorption.

3. Results and Discussion

According to the Bragg phase matching condition, the resonant excitation of the coupled mode is carried out when Equation (1) is satisfied [24]:

$$k \sin \theta = \beta + \frac{q \times 2\pi}{\Lambda} \quad (1)$$

In the expression, $k = \frac{2\pi}{\lambda}$ is the wave number, q is the diffraction order ($q = -1$), θ is the incident angle, $\beta = \frac{2\pi n_{eff}}{\lambda}$ is the real part of the propagation constant, and n_{eff} is the effective refractive index of the guided mode. The range of the grating period can be estimated by using the above equation.

The grating coupler is sensitive to the effective refractive index, which has to fulfill the inequality $n_{SiO_2} \leq n_{eff} \leq n_{LN}$, where n_{LN} and n_{SiO_2} are the refractive indices of SiO_2 (1.444) and LN (2.138) [25], respectively. The fiber angle θ , selected as 8° , can effectively avoid the second-order reflection that greatly reduces the coupling efficiency of the vertical grating coupler [26]. By substituting the inequality into Equation (1), the estimated range of Λ for the optical fiber angle can be obtained as $\frac{\lambda}{2.138 - \sin \theta} \leq \Lambda \leq \frac{\lambda}{1.989 - \sin \theta}$. The range of Λ is estimated to be $0.775 \mu m \leq \Lambda \leq 1.188 \mu m$.

In order to improve the coupling efficiency, the parameters of the grating coupler are analyzed and optimized. The thickness and the etching depth of the Si_3N_4 strip-loaded grating coupler are set to $0.3 \mu m$. Due to the polarization sensitivity of the grating coupler, the fundamental TE mode is used in the simulation. The parameters of the TE polarized grating coupler are simulated and optimized. The results are shown in Table 1. The optimized coupling efficiency at a wavelength of $1.55 \mu m$ is 33.5%.

Table 1. The optimized parameters of the Si_3N_4 strip-loaded grating coupler at a wavelength of $1.55 \mu m$.

Λ (μm)	DC	T (μm)	Lx (μm)	Ly (μm)	θ ($^\circ$)
1.166	0.54	2	4.8	1	8

The relationship between the coupling efficiency and the wavelength is shown in Figure 2. The coupling efficiency is half of the peak value when the wavelengths of light are 1.494 and $1.607 \mu m$. The -3 dB bandwidth is 113 nm. The simulation results show that the Si_3N_4 strip-loaded grating coupler on LNOI has a larger -3 dB bandwidth compared with the silicon strip-loaded grating coupler on LNOI [27].

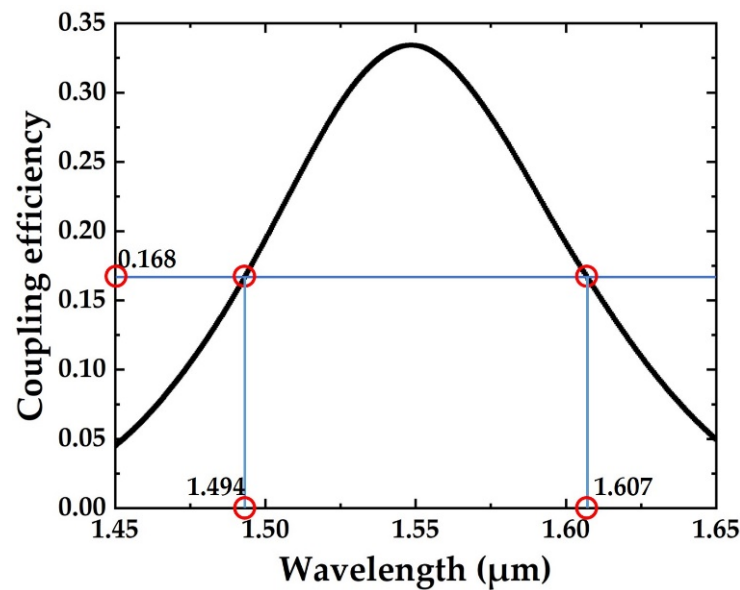


Figure 2. Coupling efficiency as a function of wavelength.

In this simulation, the influence of each parameter on the performance of the grating coupler is studied using the control variable method. During the simulation, except for the modification of the studied parameter, the other parameters are fixed at their optimized values.

The relationship between the coupling efficiency and the grating period is shown in Figure 3a. When the grating period varies to 1.166 μm , the coupling efficiency reaches its maximum value. The coupling efficiency remains above 30% when the grating period deviates by 0.022 μm . The relationship between the coupling efficiency and the wavelength at different periods is shown in Figure 3b. The coupling efficiency at a wavelength of 1.55 μm corresponds to the red circles in Figure 3a. The peak of the coupling efficiency is red-shifted when the period increases, and it moves in the opposite direction when the period decreases.

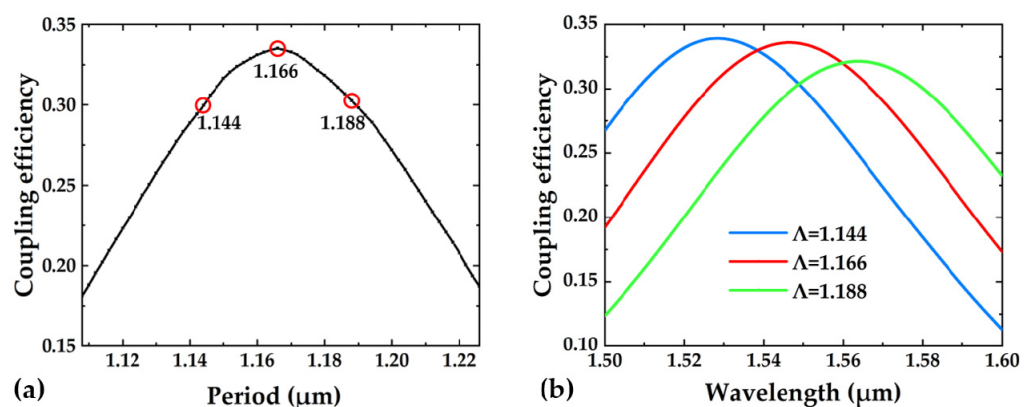


Figure 3. (a) Coupling efficiency as a function of the period. (b) Coupling efficiency as a function of the wavelength at different periods.

The relationship between the coupling efficiency and the duty cycle is shown in Figure 4a. The coupling efficiency reaches a peak when the duty cycle varies to 0.54. When the duty cycle deviates by 0.08, it retains a coupling efficiency of more than 30% at a wavelength of 1.55 μm . Figure 4b shows the variation of the coupling efficiency with wavelengths for different duty cycles. The coupling efficiency at a wavelength of 1.55 μm in Figure 4b corresponds to the red circles in Figure 4a. The peak of the coupling efficiency

is red-shifted when the duty cycle increases, and it moves in the opposite direction when the duty cycle decreases.

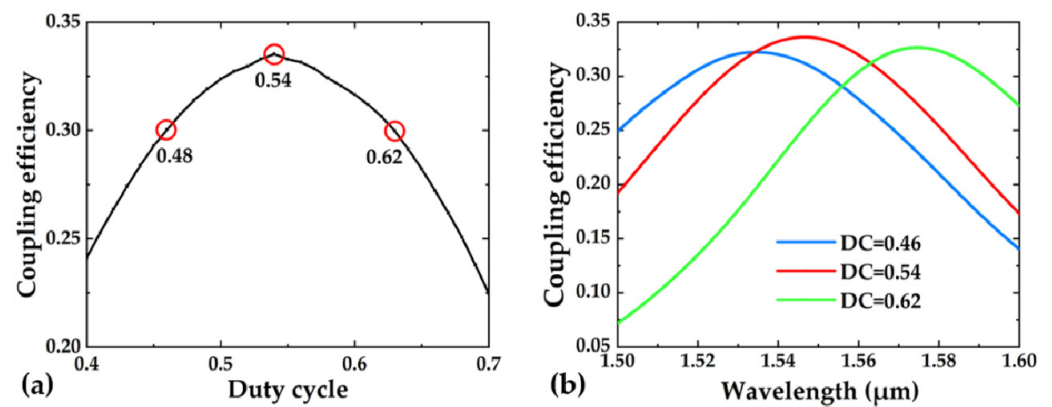


Figure 4. (a) Coupling efficiency as a function of the duty cycle. (b) Coupling efficiency as a function of the wavelength at different duty cycles.

The relationship between the coupling efficiency and the SiO₂ cladding layer thickness is shown in Figure 5. The curve of the coupling efficiency oscillates periodically between the maximum and the minimum as the thickness of the SiO₂ cladding layer increases. The periodic variation of the coupling efficiency stems from the constructive or destructive interference between the upward reflected light from the LN/SiO₂ interface and the SiO₂/LN interface.

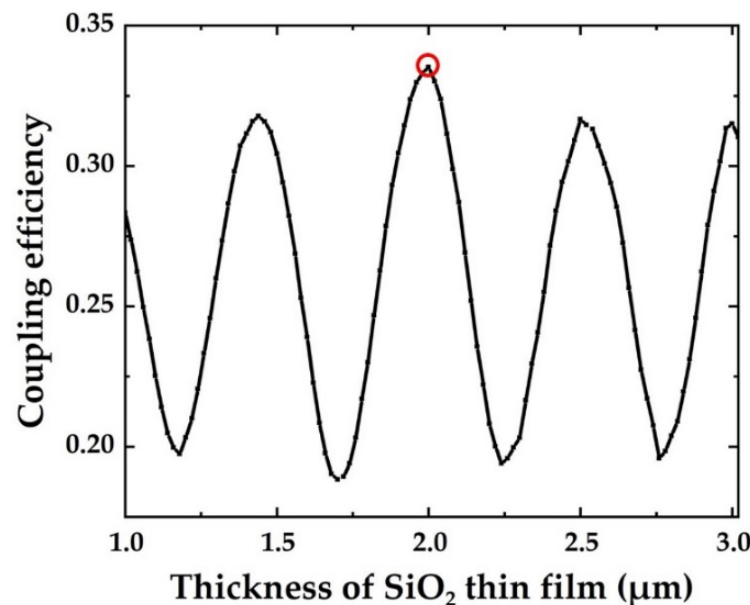


Figure 5. Coupling efficiency as a function of the SiO₂ cladding thickness.

Figure 6a,b shows the coupling efficiencies as functions of L_x and L_y , respectively. Since the grating coupler is symmetrical in the y -direction, only half of L_y is simulated. The coupling efficiencies reach their peaks when L_x and L_y are set at 4.8 μm and 1 μm, respectively. The coupling efficiency decreases faster when L_x decreases than when L_x increases. The coupling efficiency decreases to 30% when L_x is 3 μm and 7.2 μm. When L_y is less than 5 μm, the coupling efficiency is almost unchanged. However, the coupling efficiency begins to decrease rapidly when L_y is 6 μm, while the coupling efficiency decreases sharply to 29%.

Figure 7a shows the relationship between the coupling efficiency and the fiber angle. The coupling efficiency is very sensitive to the change of the fiber angle. The coupling efficiency decreases very little when the fiber angle deviates by 1° . However, the coupling efficiency decreases rapidly when the fiber angle deviates by 2° . The peak of the coupling efficiency is red-shifted when the fiber angle decreases, and it moves in the opposite direction when the fiber angle increases.

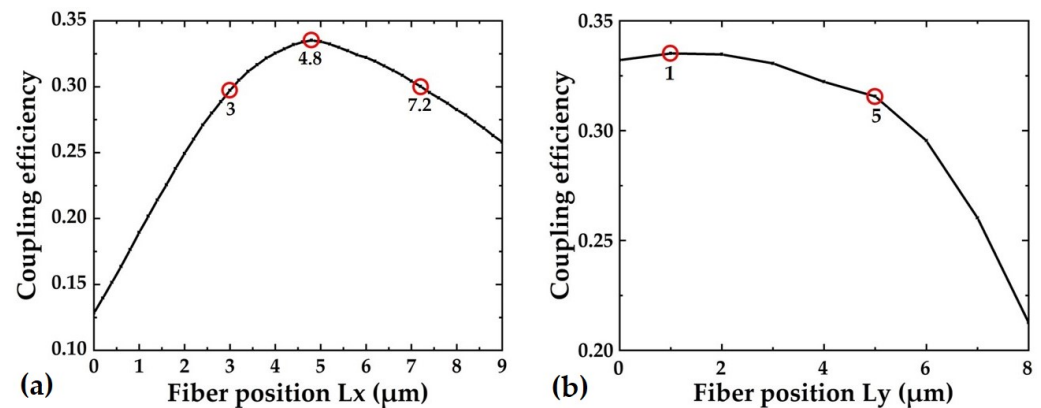


Figure 6. (a) Coupling efficiency as a function of L_x . (b) Coupling efficiency as a function of L_y .

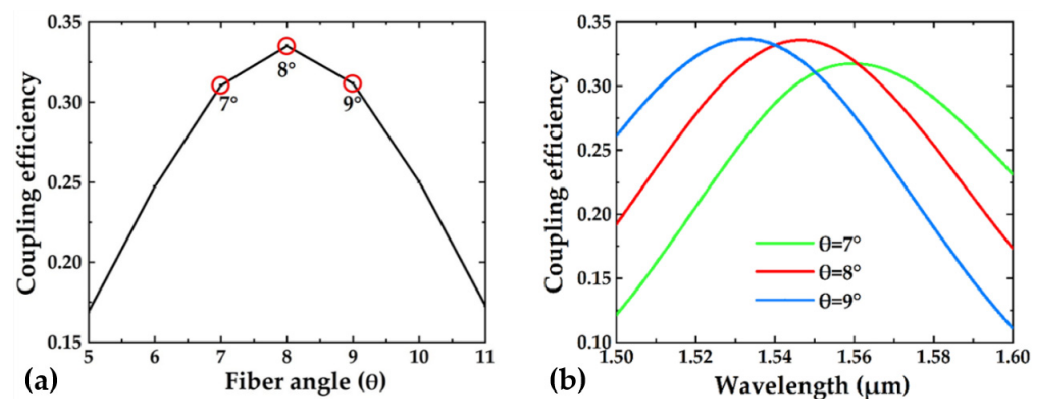


Figure 7. (a) Coupling efficiency as a function of the fiber angle. (b) Coupling efficiency as a function of the wavelength at different fiber angles.

Figure 8 shows the electric field distribution of the light wave. The in-coupled light formed an angle (8°) relative to the normal of the LN substrate. This angle allows the grating coupler to achieve near-vertical coupling in the waveguide plane at wavelengths of around $1.55 \mu\text{m}$ while avoiding second-order reflection. The light from the optical fiber is mainly divided into three parts: some scatter upwards into the air due to reflection, some are coupled into the waveguide, and others are lost in the substrate.

Table 2 lists a comparison of the different types of grating couplers previously reported on and the coupler in this work. The chirped grating couplers and grating couplers using the bottom or top reflectors have higher coupling efficiencies than uniform grating couplers. In this work, the maximum coupling efficiency of the LNOI coupler using uniform Si_3N_4 strip loading is 33.5%, and the -3 dB bandwidth is 113 nm. It can be confirmed that the grating coupler is a reliable method for solving the coupling between the chip and the single-mode fiber, and a wide -3 dB bandwidth can be obtained by using Si_3N_4 strip loading.

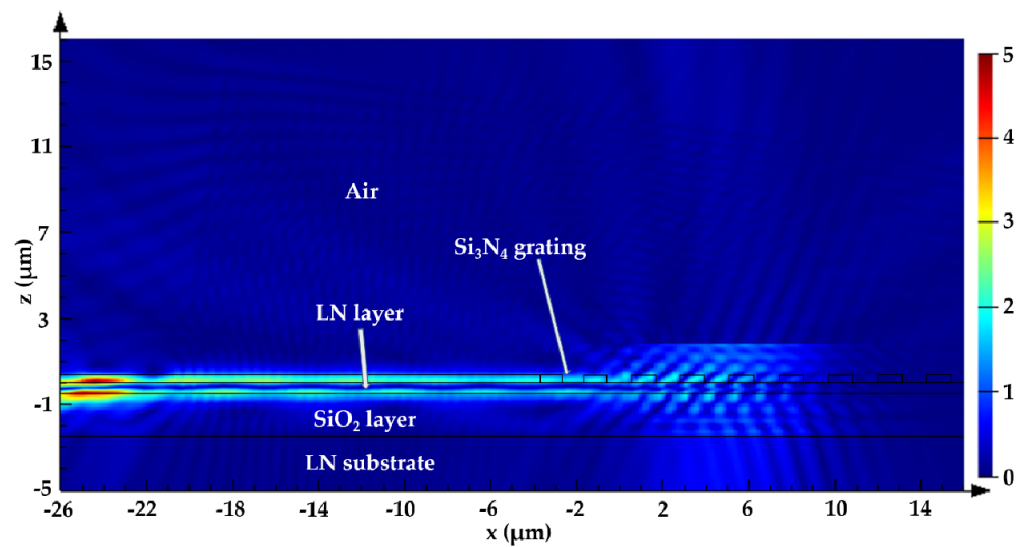


Figure 8. Electric field distribution of the light wave.

Table 2. A comparison of the reported grating couplers in this work.

Grating Coupler Type	Features	Coupling Efficiency (%)	Bandwidth (nm)	Ref
LN-on-SiO ₂	Chirped grating coupler	43.7 (TE) (1550 nm)	48 (−3 dB)	[10]
Si ₃ N ₄ -on-SOI	Apodized grating coupler	79.4 (TE) (1550 nm)	80 (−1 dB)	[16]
Si-on-LNOI	Polarization-independent	50.1 (TE) (1550 nm)	86 (−3 dB)	[17]
LN-on-SiO ₂	Chirped and apodized grating coupler	83.2 (TE) (1536 nm)	82 (−3 dB)	[28]
LN-on-SiO ₂	Integrated coupler and filter	14.5 (TE) (1550 nm)	80 (−3 dB)	[29]
Si-SiO ₂ -LN	Fully etched grating	53.7 (TE) (1550 nm)	102 (−3 dB)	[30]
LN-on-SiO ₂	Metal bottom reflector	45.7 (TE) (1553.5 nm)	30 (−1 dB)	[31]
Si-on-SiO ₂	Uniform grating with upper reflector	89.4 (TE) (~1550 nm)	96 (−3 dB)	[32]
Si ₃ N ₄ -on-LNOI	Strip-loaded uniform grating	33.5 (TE) (1550 nm)	113 (−3 dB)	This work

4. Conclusions

In this work, a 3D-FDTD simulation technique was used to systematically study the performance of an Si₃N₄ strip-loaded grating coupler on LNOI. The light was coupled vertically into the LNOI waveguide from a single-mode fiber. The parameters Λ , DC , T , Lx , Ly , and θ were analyzed and optimized to be 1.166 μm , 0.54, 2 μm , 4.8 μm , 1 μm , and 8°, respectively. At wavelengths of around 1.55 μm , the maximums of the coupling efficiency and the −3 dB bandwidth were 33.5% and 113 nm, respectively. The relationship between the parameter tolerance and the coupling efficiency of the grating couplers was discussed. Larger tolerances greatly reduced the requirements for manufacturing accuracy. Our simulation results for the grating couplers will provide useful guidance for the fabrication of similar optical devices.

Author Contributions: H.H. conceived the original idea; F.Y. carried out the simulations and wrote the manuscript; and H.F. and B.X. contributed the useful and deep discussions, analyzed the data, and modified the manuscript. All authors have read and agreed to the published version of the manuscript.

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Conflicts of Interest: The authors declare no conflict of interest.

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