



# High-Entropy FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> Alloy Synthesized by Mechanical Alloying and Spark Plasma Sintering

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**Abstract:** A FeCoNi( $B_{0.5}Si_{0.5}$ ) high-entropy alloy with the face-centered cubic (FCC) crystal structure was synthesized by mechanical alloying and spark plasma sintering (SPS). Phase evolution, microstructure, morphology and annealing behaviors were investigated. It was found that a single FCC solid solution appears after 50 h of milling. The grain size was 10 nm after 150 h of milling. Microstructure parameters were calculated by the Rietveld fitting of the X-ray Diffraction patterns. Magnetic characterizations of milled and annealed powders at 650 °C for 1 h were investigated. The heat treatment improves the magnetic properties of the milled powders by enhancing the saturation magnetization value from 94.31 to 127.30 emu/g and decreasing the coercivity from 49.07 to 29.57 Oe. The cohabitation of the FCC phase with the equilibrium crystalline phases observed after annealing is responsible of this magnetic softening. The as-milled powder was also consolidated by spark plasma sintering at 750 and 1000 °C. The obtained specimen consolidated at 750 °C improved the coercivity to 25.06 Oe and exhibited a compressive strength of 1062 Mpa and Vickers hardness of  $518 \pm 14$  HV, with a load of 2 kN. The nanoindentation technique with the Berkovich indentor gave hardness and indentation elastic modulus of  $6.3 \pm 0.3$  Gpa (~640 HV) and  $111 \pm 4$  Gpa for samples consolidated by SPS at 750 °C.

**Keywords:** HEA alloy; FeCoNi( $B_{0.5}Si_{0.5}$ ), mechanical alloying; SPS consolidation

# 1. Introduction

High-entropy alloys (HEAs) are a new field of metal alloys, discovered by Yeh et al. [1]. It was defined as alloys composed of five or more metallic elements with each elemental concentration ranging from 5 to 35 at.%. HEAs tend to form a single body-centered cubic (BCC) solid solution or a single face-centered cubic (FCC) one, or, a duplex (FCC + BCC). Some other HEAs can exhibit amorphous structure [2]. HEAs were considered as very promising materials for soft magnetic and exceptional mechanical properties like the hardness and wear resistance [3]. The mixing reaction leading to HEAs in the mechanical alloying process is dominated by the entropy, which substantially diminishes the free Gibbs energy ( $\Delta G_{mix} = \Delta H_{mix} - T \Delta S_{mix}$ ), even at low temperatures. Thus,



super-saturated solid solutions can appear rather than ordered phases, which need higher temperatures to be formed. The binary Fe–Co is a soft magnetic alloy, whereas the addition of Ni in Fe enhanced the electrical resistivity and permeability [4]. Hence, the ternary Fe–Co–Ni exhibited good soft magnetic properties, which make this alloy suitable for several technological devices like magnetic recording media and magnetic fluids [5,6]. Very recently, the quinary system Fe<sub>25</sub>Co<sub>25</sub>Ni<sub>25</sub>(B,Si)<sub>25</sub> [7] and the senary Fe<sub>25</sub>Co<sub>25</sub>Ni<sub>25</sub>(P,C,B)<sub>25</sub> [8] high-entropy bulk metallic glasses (HE-BMGs) were synthesized by the copper mold casting method. They exhibited good soft magnetic and mechanical properties. On the other hand, Wei et al. [9] successfully synthesized a senary Fe<sub>26.7</sub>Co<sub>28.5</sub>Ni<sub>28.5</sub>Si<sub>4.6</sub>B<sub>8.7</sub>P<sub>3</sub> (HEA) by the melt spinning method, which formed an amorphous phase at high cooling rate and a FCC solid solution at low cooling rate. From the best of our knowledge, most of the research concentrated on mechanical properties of bulk alloys with limited shapes and sizes, and studied their restricted applications, while HEAs synthesis by the mechanical alloying process is still limited. However, HEAs defined by Yeh et al. [1] are microcrystalline and their properties and applications could be definitely enhanced if they were synthesized in nanocrystalline scale. Furthermore, HEAs synthesis by melting or casting can lead to phase segregation and dendritic structure formation [10]. Otherwise, high-entropy alloys can easily be obtained by the mechanical alloying process without phase segregation and usually lead to the formation of homogenous microstructures [11–14]. As mentioned above, the  $Fe_{25}Co_{25}Ni_{25}(B,Si)_{25}$  system was already synthesized as a high-entropy bulk metallic alloy by the copper mold casting method and it showed excellent mechanical and magnetic properties [7]. Recently, for an in-depth mechanical study, the combination between the mechanical alloying and spark plasma sintering (MA-SPS) was successfully used. Many bulk alloys and bulk high-entropy alloys have been consolidated by spark plasma sintering (SPS) of as-milled powders [15–18].

In this paper, FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> high-entropy alloy powder was prepared by mechanical alloying and spark plasma sintering. We studied the influence of milling time on the morphology, phase composition and microstructure of the alloy. The as-milled powder was also annealed, and the magnetic behaviors were investigated before and after the thermal treatment and SPS consolidation. The mechanical property of the alloy was studied after SPS consolidation. Two temperatures were used in the spark plasma sintering technique. First, a consolidation at high temperature, 1000 °C, was used as a reference indicator for 100% dense solid. Then, a reasonably lower temperature, 750 °C, was used for consolidation in order to conserve the nanostructured powder and the high density of crystallographic defects given by the mechanical alloying. Thus, a high-resistance alloy was obtained.

### 2. Experimental Procedures

Elemental powders of Fe, Co, Ni, B and Si, with purity of higher than 99.6% and particles size of  $\leq$ 30 µm, were mechanically milled in argon atmosphere by using a high-energy planetary ball mill (Fritsh Pulverisette P7, FRITSH GmbH, Idar-Oberstein, Germany). The boron is in amorphous form, while the other elements are crystalline. The milling process was carried out up to 150 h at 600 rpm with a ball-to-powder weight ratio of 4:5. The milling sequence was chosen as 10 min of milling followed by 5 min of pause to avoid heating. The milling process was regularly interrupted, and small quantities of powder were collected for analysis by X-ray diffraction (XRD) and scanning electron microscopy (SEM).

To study the thermal stability of the compound, the as-milled powder was heat-treated for 1 h at 650 °C in a sealed quartz tube under  $10^{-3}$  Pa argon atmosphere. Annealing was performed in a Carbolite furnace with a heating rate of 15 °C/min. The alloys were characterized by X-ray diffraction (XRD) by means of Siemens D500 S (Siemen, Munich, Germany) equipment with Cu K $\alpha$  ( $\lambda$  = 1.54056 Å) radiation. The crystallite size, lattice strain and lattice parameters were determined using the Maud program based on the Rietveld method [19]. The morphology of the alloy powders was observed using scanning electron microscopy (SEM, DSM960A ZEISS, Carl Zeiss GmbH, Oberkochen, Germany) in secondary electron mode operating at a voltage of 15 kV. The saturation magnetization (M<sub>s</sub>), coercive field (H<sub>c</sub>) and squareness ratio (M<sub>r</sub>/M<sub>s</sub>) of the as-milled and heat-treated powders were conducted by

a superconducting quantum interference device from Quantum Design (Caledonia, MI, USA) SQUID MPMS-XL at 300 K with maximum applied field of 20 kOe.

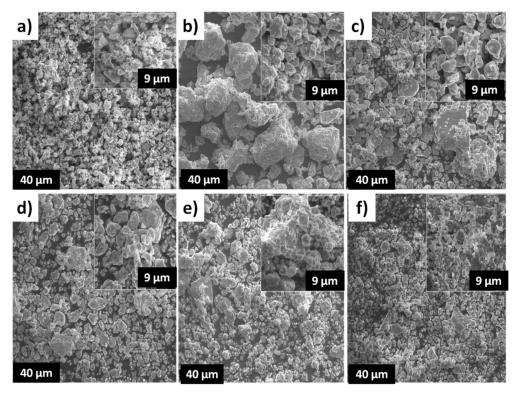
Subsequently, the as-milled powder was consolidated in vacuum atmosphere by SPS (HPD10, FCT Systeme GmbH, Frankenblick, Germany) at 750 and 1000 °C, using a heating rate of 50 °C/min, under a pressure of 50 Mpa, and then free cooled to room temperature for 10 min. For the SPS consolidation at 750 °C, a dwell time of 10 min was used at maximum temperature (750 °C), before the cooling stage. Densities of the as-sintered samples (discs of 10 mm large and almost 3 mm thick) were measured using the Archimede's principle. As for the powders, the as-sintered samples were also characterized by SEM and XRD and their magnetic properties were measured. The samples were mechanically polished using SiC paper for coarse grains, then diamond suspension and super-finished using 50 nm colloidal silica suspension. In order to show eventual porosities, the super-finition stage was long (20 min). Vickers hardness of the polished specimens was measured using a hardness tester (Zwick/Roell) with a load of 200 g at a holding time of 10 s. At least nine measurements were performed to obtain the average value of the hardness. Additionally, micro-hardness tests were realized on the powder grains under 10 g of load hold for 10 s. The powder was mounted by mixing it with resin and subsequently polished. The compressive properties at room temperature were measured by a SHIMADZU AGX-V (Shimadzu Corporation, Kyoto, Japan) testing machine at a speed of 0.1 mm/min, and the corresponding fracture surface features were observed by SEM.

Alternative hardness and elastic modulus were made by nanoindentation techniques in order to characterize the alloy and the constitutive phases. Nanoindentation experiments were performed using an Anton Paar UHT ultra nanoindenter (Anton Paar, Graz, Austria). Berkovich tip has been used. Its shape area function has been calibrated using fused silica. Indentation at constant  $F(t)/F(t) = 0.05 \text{ s}^{-1}$  has been chosen, where F(t) is the load on the indenter at the instant t. Maximum loads of 1 and 45 mN were applied. A sinusoidal signal has been superimposed during the loading stage of the indentation in order to proceed to continuous stiffness measurements [20]. The frequency of the signal is 5 Hz and the amplitude is 10% of the applied load, F(t). Fourteen indentations at 45 mN for global characterization purposes were done. In order to characterize the different phases, 144 indentations at 1 mN were performed and the results were post-processed using statistic methods. Hardness and elastic modulus were evaluated following the Oliver and Pharr method [21]. A Poisson's ratio of 0.3 was considered for these calculations.

## 3. Results and Discussion

### 3.1. Morphological Changes

Figure 1 shows the morphological evolution of the alloyed powders at different stages of milling. The un-milled particles are just mixed, and no notable deformation is observed (Figure 1a). Milling for 5 h (Figure 1b) changes the original morphology completely, due to the severe plastic deformation and sequential force of the ball-powder-ball collisions into the particles. So, the cold-welding effect is dominant. This facilitates the diffusion of atoms and then the alloying process takes place. Up to 25 h of milling, divided particles with more uniform sizes and other flattened ones are observed [22] (see Figure 1c). By prolonging milling time after 50 h, the majority of particles became rounded and the homogeneity of the powder is visible. Therefore, a balance between fracture and cold welding is reached [23] (Figure 1d). With increasing milling time, the particles became smaller (Figure 1e) and reached a finer structure at the end of the milling (Figure 1f).

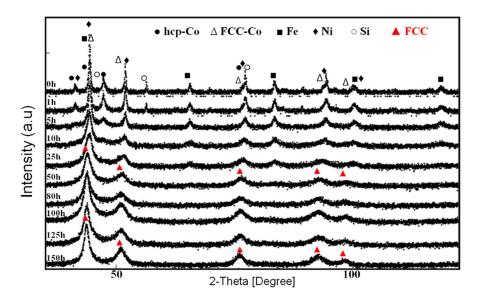


**Figure 1.** Scanning electron micrographs (SEM) of mechanically milled powders: (**a**) 0 h, (**b**) 5 h, (**c**) 25 h, (**d**) 50 h, (**e**) 100 h and (**f**) 150 h.

### 3.2. Structural Changes

Figures 2 and 3 show the XRD patterns of the FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> high-entropy alloy powders after different milling times. All characteristic peaks for elemental powders can be observed in the XRD pattern of the un-milled powder. Cobalt presents two allotropic structures, face-center cubic (FCC) and hexagonal close-packed (HCP). The characteristic peaks for boron are not observed because amorphous boron powder was used in the present work. The peaks' intensity decreased dramatically after 5 h of milling. The disappearance of the FCC-Si and FCC-Co diffraction peaks was observed. Some authors noticed the allotropic transformation of Co from FCC to HCP structure during milling [24,25]. In addition, the FCC–Co becomes unstable when mechanical energy is introduced [26]. Peaks are getting broader and some peaks (HCP–Co phase) disappear after 10 h of milling. After 25 h, the HCP–Co peaks completely vanished. The decrease and the broadening of peaks during milling are due to the crystallites' refinement and to the increase of dislocations density [27]. In addition, the most intense diffraction peak of the primary body-centered cubic BCC-iron phase became asymmetric. The asymmetry of the peak is due to the gradual disappearance of the BCC phase and to the appearance of the FCC solid solution. Shift of the Fe peaks (compared to the reference un-milled powder—0 h) toward smaller angles suggests the increase of the lattice parameter, which can be attributed to the lattice expansion induced by the diffusion of B, Si, Co and Ni into the iron matrix, leading to the cohabitation of BCC and FCC solid solution after 25 h (see Figure 3). On one hand, the interdiffusion of the Ni and Fe leads to the formation of a new FCC phase with a lattice parameter superior to the FCC Ni phase [28]. So, the FCC phase is a result of the diffusion of Fe, Co, B and Si in the Ni matrix. As the milling time reaches up to 50 h, only the peaks characterized by a FCC solid solution phase are evident, while the BCC iron peak vanishes. The significant shift of the peak to  $2\theta = 44.1^{\circ}$  after 50 h indicates the disappearance of the BCC phase (see Figure 3). Thus, the structure of the solid solution can be indicated as supersaturated solid solution. In fact, the solid solubility can be extended due to the interdiffusion between the multiple components, which occurs throughout the prolonged milling. During milling, the grain became refined with nanometric crystallites, and then a large amount of

enthalpy can be stocked in nanocrystals alloy because of the high density of defects and the wide grain boundary domain (high density of grain boundaries) [29]. Hence, the formation of solid solution can be enhanced by the energy stoked in the grain boundaries and distorted crystallographic lattice. In addition, the surface tension of nanometric grains can provoke the distortion of the lattice, which can enhance the solubility.



**Figure 2.** X-ray diffraction (XRD) patterns of FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> powders as a function of mechanical alloying time.

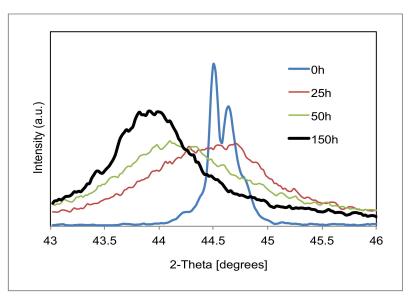


Figure 3. Details of the principal BCC and FCC peaks during milling time.

Chen et al. [30] reported that the alloying rates of elements with similar concentrations are inversely proportional to their melting point. The lower the melting point of the element, the higher its diffusivity in the solid state [31]. For the elements with similar melting point like Cobalt (1768 K) and Nickel (1726 K), the alloying rates are in proportion with the brittleness of the pure element [30]. Moreover, the lower the concentration of the element, the higher its alloying rate [32]. Hence, the diffusion sequence of elements for the FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> HEA should be: Si  $\rightarrow$  B  $\rightarrow$  Co  $\rightarrow$  Ni  $\rightarrow$  Fe.

We can conclude that only a BCC Fe–Co–B–Si supersaturated solid solution (with a slight increase of the lattice parameter compared to BCC–iron) is formed during the first 10 h of milling. After 25 h

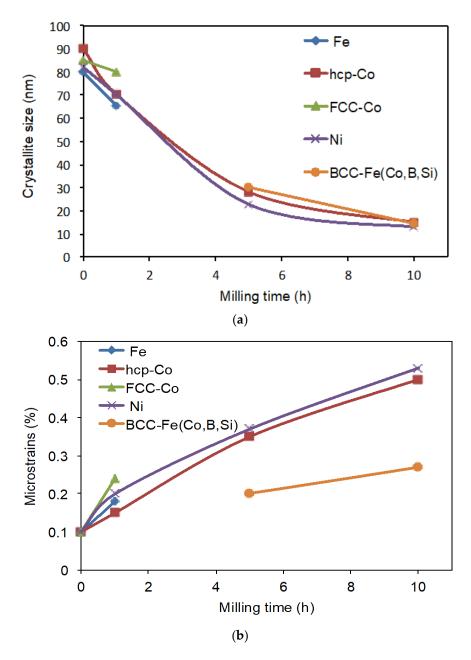
of milling, the inter-diffusion of the Ni and Fe leads to the coexistence of a mixed BCC and FCC supersaturated solid solution [28]. Continuous milling up to 150 h produces shifts of the FCC peaks to smaller angles besides the decrease of their intensity as well their broadening (Figure 3). Thus, we can deduce the formation of supersaturated solid solution at this stage of milling.

The lattice parameters obtained by fitting using Maud software are given in detail in Table 1. The lattice parameter of the BCC phase increases with increasing milling time due to the insertion of B ( $R_B = 0.82$  Å) atoms in the interstitial sites. Izadi et al. [33] noticed similar observations: the substitution of Fe atoms by Si ( $R_{Si} = 1.15$  Å), Co ( $R_{Co} = 1.25$  Å) and Ni ( $R_{Ni} = 1.24$  Å). As for the FCC lattice parameter, its increasing is due to substitution of atoms in the Ni matrix and the inter-diffusion between the Fe and Ni atoms.

Samples	Phases	Lattice Parameter (Å)	Goodness of Fit	Fit Parameters (%)	
	BCC–Fe	2.866(7)			
	FCC-Ni	3.523(0)		Rb: 3.12 Rexp: 3.46	
0 h	НСР-Со	2.507(1)	1 17		
0 N	ncr-co	c = 4.068(5)	1.16	Rwp: 4.019	
	FCC-Co	3.544(2)		-	
	FCC-Si 5.430(3)				
	BCC-Fe(B)	2.867(1)			
	FCC-Ni	3.523(6)			
		2.508(5)		Rb: 2.41	
1 h	HCP–Co	c = 4.065(6)	1.14	Rexp: 2.95 Rwp: 3.39	
	FCC-Co	3.538(2)		I. T. T.	
	FCC-Si	5.430(4)			
	BCC–Fe(Co,B,Si)	2.868(1)			
	FCC-Ni	3.525(3)		Rb: 1.70	
5 h –		2.512(6)	1.06	Rexp: 2.10 Rwp: 2.23	
	HCP–Co	c = 4.079(6)		Kwp. 2.20	
	BCC–Fe(Co,B,Si)	2.868(6)			
	FCC-Ni	3.526(0)		Rb: 1.53	
10 h		2.502(6)	1.12	Rexp: 1.91 Rwp: 2.15	
	HCP-Co				
	PCC.	c = 4.119(3)			
	BCC Fe–Co–Ni(B,Si)	2.869(2)		Rb: 1.59	
25 h	FCC		1.08	Rexp: 1.96 Rwp: 2.13	
	Fe–Co–Ni(B,Si)	3.541(5)		I	
	FCC			Rb: 1.39	
50 h	Fe–Co–Ni(B,Si)	3.601(2)	1.08	Rexp: 1.84	
				Rwp: 2.00	
100 h	FCC	2(2)(0)	1 1 2	Rb: 1.18	
100 h	Fe-Co-Ni(B,Si)	3.626(0)	1.13	Rexp: 1.34 Rwp: 1.52	
				•	
150 h	FCC	3.630(8)	1.07	Rb: 1.55 Rexp: 1.94	
130 II	Fe-Co-Ni(B,Si)	3.030(0)	1.07	Rexp: 1.94 Rwp: 2.09	

Table 1. Lattice parameter, goodness of fit and fit parameters during milling.

Figure 4a shows the crystallite size with respect to the milling time. The crystallite size and microstrain of the alloy powders after different milling times were calculated from the XRD patterns by fitting using Maud software (the goodness of fit and the fit parameters are listed in Table 1). With increasing milling time, the crystallite size of all elements as well as the newly formed BCC–Fe (Co,B,Si) supersaturated solid solution decreases rapidly in the early stages of milling. The segregation of the boron atoms to the grain boundaries hindered the grain growth of the BCC phase [34]. As a result, the dissolution of boron diminishes the crystallite size remarkably.

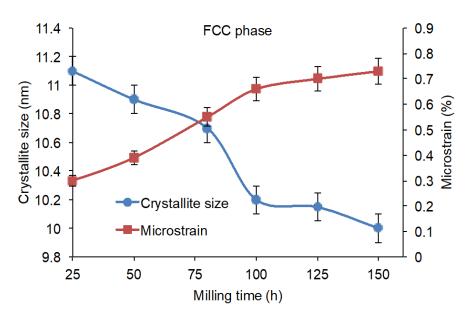


**Figure 4.** Dependence of the microstructure parameters of the Fe, FCC–Co, HCP–Co, Ni and BCC–Fe (Co,B,Si) as a function of milling time. (**a**) crystallite size and (**b**) microstrains.

Figure 4b shows the internal microstrain evolution during the milling. The internal strain increases with the milling time. The micro-stress can come from several sources in crystallites such as vacancies, multiplication of the dislocations and other defects [35]. After 10 h, the BCC phase exhibits a crystal size of 14 nm and a lattice strain of 0.3%. The increasing internal microstrain is due to the size mismatch

between the initial elements, the increase of grain boundary fraction and the high dislocation density produced by the severe plastic deformation [36,37].

Figure 5 shows the evolution of crystallite size and lattice strain of the formed FCC Fe–Co–Ni–B–Si supersaturated solid solution as a function of the milling time. When the FCC solid solution cohabitates with a BCC Fe–Co–Ni–(B,Si) solid solution (after 25 h), the crystallite size is 11 nm for a microstrain of 0.3%. After 50 h, the FCC solid solution remains the single phase with a crystallite size of about 11 nm and a microstrain of 0.4%. The lattice strain of the FCC phase increases with the milling time. The 150-h milled powder reveals a lattice strain of 0.7%. The crystallite size seems to decrease slightly but constantly with the increasing milling time to reach 10 nm at the end of the milling.



**Figure 5.** Dependence of the microstructure parameters of the FCC Fe–Co–Ni–(B,Si) as a function of the milling time.

### Thermodynamic Considerations

From a thermodynamic point of view, the high entropy of mixing  $\Delta S_{mix}$  can notably decrease the Gibbs free energy of mixing  $\Delta G_{mix}$ , even at low temperatures. It has been reported, however, that entropy or free energy considerations only cannot always explain the formation of solid solutions. Indeed, amorphous phases and intermetallics can form as well in HEAs systems [38–40]. Thus, counting on the effect of  $\Delta S_{mix}$  only is not enough to predict the formation of solid solution in HEAs. Based on the mixing entropy  $\Delta S_{mix}$  and the mixing enthalpy  $\Delta H_{mix}$ , Yang and Zhang [41] introduced two parameters to define a criterion for the formation of solid solutions:  $\Omega$  (ratio between the entropy and the enthalpy of mixing) and  $\delta$  (atomic size mismatch). They are defined as follows:

$$\Omega = \frac{T_{\rm m} \Delta S_{\rm mix}}{|\Delta H_{\rm mix}|} \tag{1}$$

$$\delta = \sqrt{\sum_{i=1}^{n} C_i \left(1 - \frac{r_i}{\bar{r}}\right)^2}$$
<sup>(2)</sup>

with

$$\Delta H_{mix} = 4 \sum_{i=1, i \neq j}^{n} \Delta H_{ij} C_i C_j$$
(3)

$$\Delta S_{mix} = -R \sum_{i=1}^{n} (C_i \ln C_i) \tag{4}$$

$$T_m = \sum_{i=1}^n C_i (T_m)_i$$
(5)

where,  $\Delta H_{ij}^{mix}$  represents the enthalpy of mixing of binary liquids i and j alloys, as tabulated in Table 2,  $C_i$  is the atomic percentage of the i-th element respectively,  $r_i$  is the atomic radius of the i-th atoms,  $\bar{r}$  is the average radius of all atoms,  $(T_m)_i$  is the theoretical melting point of the i-th element and R is the gas universal constant. According to Yang and Zhang's method,  $\Omega \ge 1.1$  and  $\delta \le 6.6\%$  should be the criterion for forming solid solution phase. The calculated values of these parameters are given in Table 3. As presented, the condition  $\Omega \ge 1.1$  is not satisfied, while the second condition  $\delta \le 6.6\%$  is fulfilled. Thus, according to this theory, the super-saturated solid solutions are not likely to form, which seems to be contradicted by our mechanical alloying results.

**Table 2.** Enthalpy of mixing ( $\Delta H_{mix}$  (kJ mol<sup>-1</sup>)) in binary equiatomic alloys calculated with Miedema's approach [42].

Element (Atomic Radius, Å)	Fe	Со	Ni	В	Si
Fe (1.24)	-	-1	-2	-26	-35
Co (1.25)	-1	-	0	-24	-38
Ni (1.24)	-2	0	-	-24	-40
B (0.82)	-26	-24	-24		-14
Si (1.15)	-35	-38	-40	-14	-

Table 3. Calculated	parameters for FeCo	$NiB_{0}$ 5 $Si_{0}$ 5	high-entropy	r alloy (HEA).

Alloy	$\Delta H_{mix}$ (kJ mol <sup>-1</sup> )	$\Delta S_{mix}$ (JK <sup>-1</sup> mol <sup>-1</sup> )	T <sub>m</sub> (K)	δ (%)	Ω	VEC *
FeCoNi(B <sub>0.5</sub> Si	<sub>0.5</sub> ) -24.12	12.96	1831.50	0.11	0.98	7.625

\* VEC = valence electron concentration.

On the other side, Guo et al. [2,43] reported that the valence electron concentration (VEC) is an important factor controlling the structure (FCC and/or BCC) of the formed solid solution in HEAs. It is defined as follows:

$$VEC = \sum_{i}^{n} C_{i} (VEC)_{i}$$
(6)

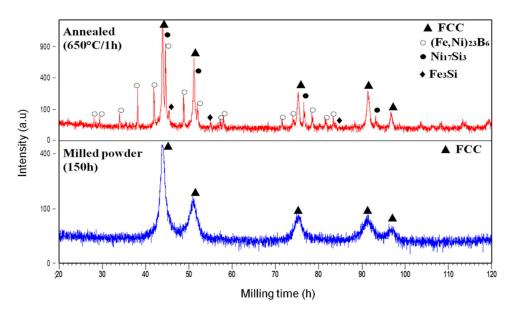
where (VEC)<sub>i</sub> is the valence electron count for the i-th element. According to Guo's method, sole FCC solid solution can exist if VEC  $\geq$  8.0, duplex FCC + BCC structures co-existed when  $6.87 \leq$  VEC  $\leq$  8.00 and single BCC solid solution appears if VEC < 6.87. The calculated VEC for the Fe<sub>25</sub>Co<sub>25</sub>Ni<sub>25</sub>(B<sub>0.5</sub>Si<sub>0.5</sub>)<sub>25</sub> HEA is given in Table 3. In our alloy, the VEC value of the mix indicates the coexistence of mixed (FCC + BCC) solid solutions. This agrees only with the alloy milled for 25 h but does not agree with the phase composition of the alloys obtained after longer milling times. However, from 50 h until the end of the milling (150 h), the XRD patterns reveal the existence of sole FCC structure.

Generally, the binary atom-pairs Fe–Ni and Ni–Co have high mutual solubility. Many researchers confirmed the obtaining of a single FCC structure on HEA systems based on the Fe, Ni and Co [44,45]. Thus, it is highly probable that the thermodynamic parameters may not apply accurately within the FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> HEA case. Thus, the milling time plays a key role in the formation of solid solutions during the mechanical alloying process.

# 3.3. Thermal Analysis

# 3.3.1. Annealing Treatment

In order to understand the effect of heating on structural and magnetic characterization, the 150-h milled high-entropy alloy powder  $FeCoNiB_{0.5}Si_{0.5}$  was annealed for 1 h at 650 °C under argon atmosphere. The XRD patterns before and after annealing are shown Figure 6. An amount of the FCC solid solution is maintained. Its peak intensity increases due to the crystallite size growth during the heating. Moreover, one can see the appearance of some new crystalline phases:  $BCC-(Fe,Ni)_{23}B_6$  (Ref. ICDD Code: 04-001-5987), FCC-Ni<sub>17</sub>Si<sub>3</sub> (Ref. ICDD Code: 03-065-6491) and BCC-Fe<sub>3</sub>Si (Ref. ICDD Code: 04-004-6643) after the annealing. This stable equilibrium phases result from the metastable structure transformation after annealing.



**Figure 6.** X-ray diffraction patterns of mecanically alloyed FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> powders for 150 h of milling and after annealing at 650 °C for 1 h.

### 3.3.2. Consolidation of Powders

In order to understand the effect of heating on structural, magnetic and mechanical characterization, the 150-h milled high-entropy alloy powder  $FeCoNiB_{0.5}Si_{0.5}$  was sintered by SPS at 750 and 1000 °C, under vacuum.

Figure 7 shows the piston displacement as a function of the temperature during the sintering of the powder for both tests. The powder starts to sinter around 500 °C. Sintering is achieved beyond 850 °C. The obtained HEA specimens consolidated at 750 and 1000 °C show densities of 5806 kg/m<sup>3</sup> and 5938 kg/m<sup>3</sup>, respectively. This tends to show that the densification is not complete at 750 °C and that porosities of about 2% seem to be present.

Figure 8 shows the XRD pattern and SEM micrographs in secondary electron (SE) mode of the core of the specimens after SPS consolidation. The samples were mechanically polished down to 50 nm colloidal silica suspension. In order to show eventual porosities, the super-finition stage was long (20 min). It can be seen that no porosity was present in the specimens after SPS sintering and also that they exhibit rough surface after polishing. The use of high temperatures like 1000 °C causes a substantial increase of the grain size. The corresponding energy-dispersive X-ray spectra (EDS) of the two sintered bulks and the alternative dark/light zones are shown in Table 4. The boron is absent from the table because EDS is unable to quantify it. The alternative dark/light zones show the topography of the sample. Given the phase proportion revealed by the XRD patterns, the light zone is very probably the FCC phase.

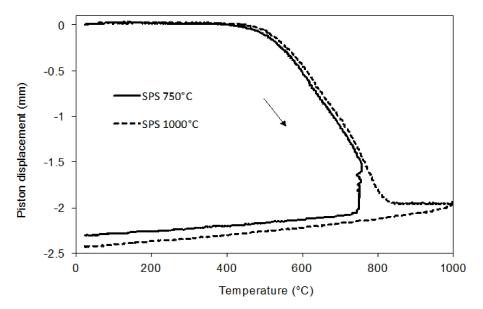


Figure 7. Piston displacement as a function of the temperature during the sintering of the powders.

**Table 4.** Chemical composition (in at. %) of the specimens given by energy-dispersive X-ray spectra(EDS).

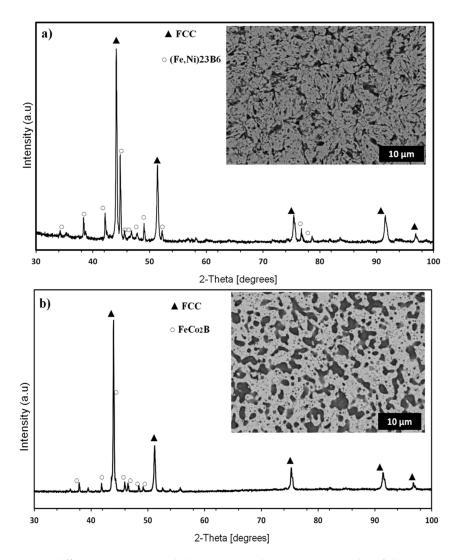
Element	Zone	Fe	Со	Ni	Si	0
SPS at 1000 °C	Black Grey	8.38 25.58	5.17 25.46	5.10 25.11	32.07 23.85	48.65 -
SPS at 750 °C	Black Grey	13.47 25.39	10.55 25.38	10.41 25.23	21.28 24.00	44.29

### 3.4. Magnetic Behavior

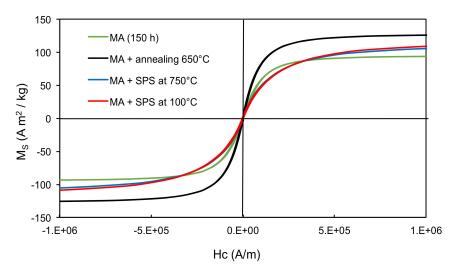
Figure 9 shows the hysteresis curve of the 150-h milled FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> powder before annealing, after annealing at 650 °C for 1 h and after Spark plasma sintering at 750 and 1000 °C. The values of the saturation magnetization ( $M_{s}$ ), the remanence to saturation ratio ( $M_r/M_s$ ) and the coercivity ( $H_c$ ) are listed in Table 5.

The annealed sample shows larger saturation magnetization and lower coercivity than the as-milled powder. The increase in the saturation magnetization can be attributed to the structures of the BCC phases formed during the annealing. In fact, the BCC structure exhibits higher saturation magnetization than the FCC structure. Zhang et al. [46] and Huang et al. [47] also reported similar results for their HEAs FeCoNi(CuAl)<sub>0.8</sub> and FeCrCoNiAl<sub>x</sub>, respectively. The decrease of the coercivity after the heat treatment depends on the increase in crystallite size, the grain size and the decrease of structural strain. Mishra et al. [48] noticed similar observations. The saturation ratio decreases from 0.034 after milling to 0.025 after annealing and to 0.012 after SPS. This decrease is linked to the release of microstrains and the domain wall energy during the elevation for temperature. The saturation ratio also depends on the phases appearance after annealing and SPS sintering.

On the basis of high saturation magnetization,  $M_s$ , and low coercivity,  $H_c$ , measurements, it can be concluded that the heat treatment at 650 °C makes the HEAs magnetically softer. The specimens obtained after SPS exhibit improved coercive field values and smaller saturation ration value compared to the simply annealed samples. Also, the consolidated specimens have a lower coercivity, saturation ratio and higher saturation magnetization values than the as-milled powders that they are made from. As a conclusion, a good combination between the coercivity and the saturation magnetization is obtained after Spark Plasma Sintering at 750 °C.



**Figure 8.** X-ray diffraction pattern and the scanning electron micrographs of the HEA at the two temperatures, (**a**) SPS at 750 °C and (**b**) SPS at 1000 °C.



**Figure 9.** Magnetic hysteresis plots of 150-h milled FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> powders after annealing, MA + SPS at 750 °C and MA + SPS at 1000 °C.

Samples	$M_s$ (A m <sup>2</sup> /kg)	H <sub>c</sub> (A/m)	M <sub>r</sub> /M <sub>s</sub>
As-milled	94.31	3905	0.034
Annealed at 650 °C	127.30	2353	0.025
MA + SPS at 750 °C	110.91	1994	0.012
MA + SPS at 1000 °C	115.84	2220	0.012

**Table 5.** Magnetic characteristics of the milled  $FeCoNiB_{0.5}Si_{0.5}$  HEA powder before and after annealing.

The value of coercivity of the HEA presented here is higher than the coercivity measured by Tianlong et al. [7] on the same chemical composition obtained by the copper cast method. The coercivity  $(H_c)$  reflects the degree of freedom for the movement of magnetic domain walls. It can be influenced by several factors in alloys like microstructure, grain size and crystal defects. In the current case, the coercivity has a relation with the crystallite size and the dislocations [49]. Specifically, the high grain boundaries fraction and the dislocations induced by the mechanical alloying process may significantly hinder the movement of magnetic domain walls, giving different coercivity values for the two methods.

Table 6 presents the results of the present study and summarizes the magnetic characteristics of some alloys and HEA compounds presented in the literature (prepared by mechanical alloying). The FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> shows higher magnetization and lower coercivity compared to most of the mechanically alloyed compounds and HEAs. Hence, this comparison shows that the synthesized FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> HEA exhibits good soft magnetic properties, especially after consolidation by spark plasma sintering at 750 °C.

Alloy	Phase	M <sub>s</sub> (Am <sup>2</sup> /kg)	H <sub>c</sub> (A/m)	Reference
$Fe_{42}Ni_{28}Zr_8Ta_2B_{10}C_{10}$ (198 h MA)	Amorphous + BCC	93.91	2654	[50]
NiCoAlFe (MA)	FCC + BCC	89.50	1732	[51]
FeSiBAlNi (260 h MA)	Amorphous	1	23,077	[52]
FeSiBAlNiNb HEA (100 h MA)	BCC + FCC + Amorphous	~10	~27,852	[52]
Co <sub>60</sub> Fe <sub>5</sub> Ni <sub>5</sub> Ti <sub>25</sub> B <sub>5</sub> (7 h MA)	Amorphous	53.4	605	[53]
(Fe <sub>65</sub> Co <sub>35</sub> ) <sub>95</sub> Cr <sub>5</sub> (100 h MA)	BCC	~205	~5570	[54]
FeSiBAlNiCo HEA (140 h MA)	Amorphous	~2	~18,303	[55]
FeSiBAlNiCe HEA (MA)	Amorphous	1	18,303	[56]
TiFeNiCrCo HEA (MA)	FCC	24.44	11,900	[48]
(Fe <sub>67</sub> Ni <sub>33</sub> ) <sub>70</sub> Ti <sub>10</sub> B <sub>20</sub> HEA (120 h MA)	Amorphous + nanocrystalline phase	105.38	2925	[57]
Fe <sub>70</sub> Ta <sub>5</sub> Si <sub>10</sub> C <sub>15</sub> (150 h MA)	Amorphous/nanocrystalline	-	2720	[58]
FeCoNiB <sub>0.5</sub> Si <sub>0.5</sub> (150 h MA)	FCC	94.31	3905	This work
FeCoNiB <sub>0.5</sub> Si <sub>0.5</sub> (150 h MA + 1 h 650 °C annealing)	FCC + BCC phases	127.30	2353	This work
FeCoNiB <sub>0.5</sub> Si <sub>0.5</sub> (150 h MA + SPS at 750 °C)	$FCC + (Fe,Ni)_{23}B_6$	110.91	1994	This work
FeCoNiB <sub>0.5</sub> Si <sub>0.5</sub> (150 h MA + SPS at 1000 °C)	$FCC + FeCo_2B$	115.84	2220	This work

Table 6. Comparison of magnetic characteristics of some reported HEAs with the present work.

### 3.5. Mechanical Properties

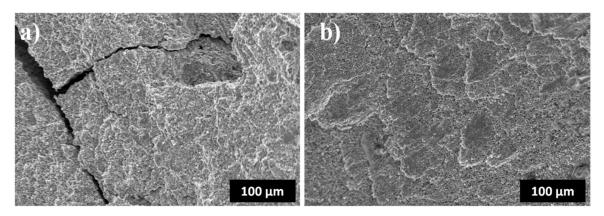
Room-temperature compressive tests and hardness measurements were realized after SPS consolidation. Moreover, microhardness Vickers tests were made on the powder grains using 10 g of load applied for 10 s. The results are shown in Table 7. With increasing SPS temperature, the compressive strength ( $\sigma_{max}$ ) decreases by about 12%, while the yield strength ( $\sigma_y$ ) decreases by 20%. The sample sintered at 750 °C showed crack noises during the compression test, which suggests

that the final strength of 1062 MPa is under-evaluated. Supplementary tests must be realized to measure the ultimate compressive strength. The sample sintered at 750 °C is significantly harder (518 HV) than the one processed at 1000 °C (176 HV). Micro-hardness tests made on grains of as-milled powder (mounted by mixing with resin) showed powder gains hardness of about 626 HV. This shows that the major part of the defects introduced by the milling process, which are responsible for the hardening, still persist after sintering at 750 °C. The high value of hardness obtained after SPS at 750 °C depends on the dislocation strengthening and the ultrafine grains. As shown in SEM examination of SPS-consolidated specimens, the increase of temperature causes an increase of the grain size. According to the Hall-Petch relationship, the increase of the grain size results in a clear decrease in the compression yield strength [59]. The HEA consolidated by SPS at 750 °C exhibits a hardness of 518 HV, which is higher than that reported for some HEAs fabricated by SPS or casting methods [11,60–63] and slightly higher than that of the Stellite commercial alloy which is a commercial hard facing alloy that exhibits a hardness of 500 HV.

Table 7. Mechanical proper	erties: compressive strength ( $\sigma_{\rm m}$	$_{max}$ ), yield strength ( $\sigma_{y}$ ) and Vickers has	ardness.
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Alloy	Process	σ <sub>y</sub> (MPa)	σ <sub>max</sub> (MPa)	Hardness ( $H_V$ )
FeCoNiB <sub>0.5</sub> Si <sub>0.5</sub> FeCoNiB <sub>0.5</sub> Si <sub>0.5</sub>	MA (powder) MA + SPS at 1000 °C	- 722	926	626 176
FeCoNiB <sub>0.5</sub> Si <sub>0.5</sub>	MA + SPS at 750 °C	913	1062	518

Figure 10 shows the corresponding fractographic images after the compressive strength tested alloy consolidated in two different temperatures. As shown Figure 10a, the samples consolidated by SPS at 750 °C show cracks, which explains the intergranular fracture observed with a dimpled texture all over the surface, suggesting that the fracture mode is brittle fracture. On the other hand, the plastic-slipping plane observed with the sample consolidated by SPS at 1000 °C (Figure 10b) suggested that the mode of fracture is a ductile fracture. This suggests that the optimum consolidation temperature should be above 750 °C, in order to make the bulk more ductile.

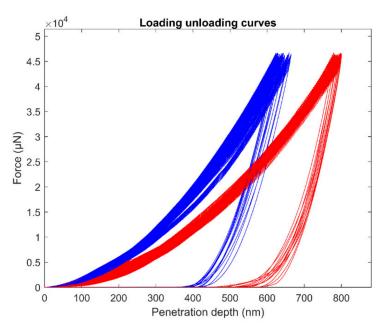


**Figure 10.** Fractography by SEM of the fracture surfaces of the specimens consolidated by SPS, (**a**) SPS at 750 °C and (**b**) SPS at 1000 °C.

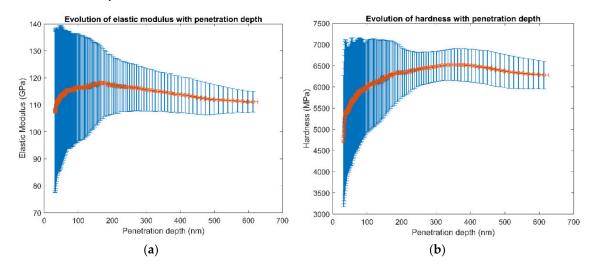
The value of the elastic modulus cannot be directly measured by compression tests since the dies deformation is not negligible in the vicinity of the contact with the sample. Thus, an alternative method for hardness and elastic modulus measurements was deployed—nanoindentation.

The nanoindentation method can also give information about the constitutive phases in the alloy. Nanoindentation experiments allow the evaluation of hardness, H, and indentation elastic modulus, E, as a function of the penetration depth (h). Figure 11 shows the load-displacement curves for both SPS consolidate samples (at 750 and 1000 °C) for indentation loads of 45 mN. Given the microstructure of these alloys, indentations performed at lower loads give very scattered results, as usually observed

for multi-phased materials [64]. The evolution of indentation modulus and hardness withdrawn from the data presented in Figure 11, for the sample consolidated at 750 °C, are shown in Figure 12. Indentations performed at 45 mN allow determining average values of E and H, representative of the global behavior of the sample, as shown on the graphs presented in Figure 12. Parameters H(h) and E(h) show that once a given penetration depth,  $h_d$ , is reached, the values of E and H tend to stabilize. The depth,  $h_d$ , depends on the typically microstructure length scale. Table 8 summarizes the obtained mechanical properties for the two temperatures of consolidation (750 and 1000 °C).



**Figure 11.** Loading-unloading indentation curves with maximum load of 45 mN for the samples consolidated by SPS at 750 °C (blue) and 1000 °C (red).



**Figure 12.** Elastic modulus and hardness curves with the depth for the SPS 750 °C sample, (**a**) Elastic modulus (**b**) Hardness.

**Table 8.** Hardness (H), Elastic modulus (E) and ratios H/E and  $H^3/E^2$  for consolidated powders at 750 °C and 1000 °C.

	Hardness (GPa)	Indentation Elastic Modulus (GPa)	H/E	H <sup>3</sup> /E <sup>2</sup>
MA + SPS at 750 °C	$6.3 \pm 0.3$	$111 \pm 4$	0.057	0.02
MA + SPS at 1000 $^{\circ}$ C	$3.6 \pm 0.08$	$102 \pm 4$	0.035	0.0045

In order to evaluate the wear resistance of the two specimens after SPS, we calculated the H/E ratio, which is also called the elastic strain to failure, or plasticity index, first introduced by Oberle [65]. The high value for this ratio, explained by a combination between the low modulus of elasticity and high hardness, would give the material improved fracture toughness. Furthermore, the  $H^3/E^2$  is a second ratio that gives information on the resistance of the material to the plastic deformation. High values of this ratio mean improved resistance to plastic deformation.

Table 8 also presents the H/E and  $H^3/E^2$  ratio of the SPS-consolidated samples. One can conclude that the MA + SPS at 750 °C is characterized by higher fracture toughness and high resistance to plastic deformation compared to the MA + SPS at 1000 °C.

SEM as well as optical micrography and XRD patterns clearly show the presence of at least two phases in both SPS sintered materials. To deconvolute the mechanical properties of each phase would be very interesting. In order to perform such type of measure, a statistical approach has been envisaged. As it is classically realized for multi-composed materials, a high number of indentation (144) at low load (1 mN) was performed on both materials. The values of indentation modulus and hardness were used to establish a cumulative density function (cdf). Assuming the presence of 2 phases, and in order to identify the mechanical properties (E and H) of each of them, this experimental cdf was fitted with the following function [66]:

$$f_{\rm E} = \frac{\omega_1}{2} \left( 1 + \operatorname{erf}\left(\frac{\mathbf{x} - \mathbf{E}_1}{\sqrt{2}\Delta_{\rm E1}}\right) \right) + \frac{(1 - \omega_1)}{2} \left( 1 + \operatorname{erf}\left(\frac{\mathbf{x} - \mathbf{E}_2}{\sqrt{2}\Delta_{\rm E2}}\right) \right)$$
(7)

where  $\omega_n$  and  $E_n$  are the surface fraction and indentation elastic modulus of the n-th phase, respectively. The term  $\Delta_{En}$  is the standard deviation on the indentation elastic modulus. The same kind of function can be used for the hardness. Then,  $H_n$  and  $\Delta_{Hn}$  can replace  $E_n$  and  $\Delta_{En}$  in Equation (7) as hardness and its standard deviation of the n-th phase.

Table 9 summarizes the values of the extracted data. One can observe that the FCC phase is much softer, as expected, after sintering at higher temperature. At the opposite, the minor phase is much harder after sintering at 1000 °C.

**Table 9.** Extracted values of indentation modulus and hardness from the statistical study of the 144 dynamic nanoindentation tests at 1 mN.

	Surface Fraction	Hardness (GPa)	Indentation Modulus (GPa)
SPS 750 (FeNi) <sub>23</sub> B <sub>6</sub> phase	0.25 ± 0.07	$2.3 \pm 0.6$	$65 \pm 13$
SPS 750 FCC phase	balance	$8.2 \pm 2$	192 ± 59
SPS 1000 FeCo <sub>2</sub> B phase	0.30 ± 0.07	$7.4 \pm 1.4$	38 ± 11
SPS 1000 FCC phase	balance	$2.3 \pm 1.2$	177 ± 72

## 4. Conclusions

The FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> HEA alloy was successfully synthesized by mechanical alloying with a single solid solution structure, while the thermo-dynamic criteria for obtaining such a phase were not respected. After 25 h of milling, one major BCC supersaturated solid solution and a minor supersaturated FCC solid solution were formed. After 150 h of milling, a homogenous FCC structure with a grain size of about 10 nm was present. The increasing milling time led to peak shifts and broadening caused by the lattice expansion, strains and grain refinement. The heat treatment of the as-milled FeCoNiB<sub>0.5</sub>Si<sub>0.5</sub> HEA produced a material with softer magnetic properties. We believe that the structural modification obtained by the decomposition of the supersaturated FCC HEA alloy into more stable equilibrium phase is the main factor responsible for the magnetic softness. After SPS, the metastable FCC phase decomposed into FCC and a minor (Fe,Ni)<sub>23</sub>B<sub>6</sub> after 750 °C, and into FCC and a minor FeCo<sub>2</sub>B phase after 1000 °C. The mechanical properties of the alloy consolidated at a temperature of 750 °C are good but can be optimized by rising the temperature of consolidation in order to find the best compromise

between ductility and strength. Also, a consolidation under a higher compression pressure (here, 50 MPa) can be tested in order to enhance the sintering efficiency. Thus, consolidation optimum conditions seem to be located above 750 °C and with compression pressures higher than 50 MPa. A specific study will be devoted to the optimization of the SPS consolidation conditions.

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