

**Table S1.** The content of phosphorus of P modified supports.

Supports	Synthesis Method	The Load of P (wt.%)
0P $\theta$ -Al <sub>2</sub> O <sub>3</sub>	-	0
0.1P $\theta$ -Al <sub>2</sub> O <sub>3</sub>		0.11
0.3P $\theta$ -Al <sub>2</sub> O <sub>3</sub>		0.31
0.6P $\theta$ -Al <sub>2</sub> O <sub>3</sub>	incipient wetness impregnation	0.6
1P $\theta$ -Al <sub>2</sub> O <sub>3</sub>		1.02
1.5P $\theta$ -Al <sub>2</sub> O <sub>3</sub>		1.43
3P $\theta$ -Al <sub>2</sub> O <sub>3</sub>		2.67

**Table S2.** The specific surface area and pore volume of the supports.

Supports	S <sub>BET</sub> (m <sup>2</sup> ·g <sup>-1</sup> )	Percentage of Decline Relative to θ-Al <sub>2</sub> O <sub>3</sub>	Volume (cm <sup>3</sup> ·g <sup>-1</sup> )	Percentage of Decline Relative to θ-Al <sub>2</sub> O <sub>3</sub>
0P $\theta$ -Al <sub>2</sub> O <sub>3</sub>	111.44	0.0	0.442	0.0
0.1P $\theta$ -Al <sub>2</sub> O <sub>3</sub>	111.08	0.3	0.438	1.0
0.3P $\theta$ -Al <sub>2</sub> O <sub>3</sub>	105.74	4.3	0.424	4.3
0.6P $\theta$ -Al <sub>2</sub> O <sub>3</sub>	103.93	6.7	0.413	6.6
1P $\theta$ -Al <sub>2</sub> O <sub>3</sub>	103.49	7.1	0.413	6.6
1.5P $\theta$ -Al <sub>2</sub> O <sub>3</sub>	102.63	7.9	0.395	10.6
3P $\theta$ -Al <sub>2</sub> O <sub>3</sub>	100.41	9.9	0.371	16.1

**Table S3.** Quantitative results of TGA test of supports.

<b>Supports</b>	<b>The Amount of Desorbed Water (mmol·g<sup>-1</sup>)</b>
0Pθ-Al <sub>2</sub> O <sub>3</sub>	1.49
0.1Pθ-Al <sub>2</sub> O <sub>3</sub>	1.18
0.3Pθ-Al <sub>2</sub> O <sub>3</sub>	1.33
0.6Pθ-Al <sub>2</sub> O <sub>3</sub>	1.37
1Pθ-Al <sub>2</sub> O <sub>3</sub>	1.60
1.5Pθ-Al <sub>2</sub> O <sub>3</sub>	1.63
3Pθ-Al <sub>2</sub> O <sub>3</sub>	1.87

**Table S4.** Quantitative results of NH<sub>3</sub>-TPD test of supports.

<b>Sample</b>	<b>Peak1 Temperature (°C)</b>	<b>Amounts of NH<sub>3</sub> Desorption at Peak1 (umol·g<sup>-1</sup>)</b>	<b>Relative Surface Hydroxyl Density <sup>(1)</sup></b>
0Pθ-Al <sub>2</sub> O <sub>3</sub>	152	116.28	1.00
0.1Pθ-Al <sub>2</sub> O <sub>3</sub>	156	91.57	0.79
0.3Pθ-Al <sub>2</sub> O <sub>3</sub>	158	95.17	0.82
0.6Pθ-Al <sub>2</sub> O <sub>3</sub>	154	109.16	0.94
1Pθ-Al <sub>2</sub> O <sub>3</sub>	155	127.12	1.09
1.5Pθ-Al <sub>2</sub> O <sub>3</sub>	152	139.77	1.20
3Pθ-Al <sub>2</sub> O <sub>3</sub>	154	211.03	1.82

(1) Relative surface hydroxyl density: the surface hydroxyl density of θ-Al<sub>2</sub>O<sub>3</sub> was set as 1, and the relative values of other samples with respect to θ-Al<sub>2</sub>O<sub>3</sub> were defined as the relative surface hydroxyl density of the support.

**Table S5.** Binding energy of P 2p.

<b>Supports</b>	<b>P 2p Binding Energy (eV)</b>
0.1Pθ-Al <sub>2</sub> O <sub>3</sub>	—
0.3Pθ-Al <sub>2</sub> O <sub>3</sub>	133.1
0.6Pθ-Al <sub>2</sub> O <sub>3</sub>	133.34
1Pθ-Al <sub>2</sub> O <sub>3</sub>	133.6
1.5Pθ-Al <sub>2</sub> O <sub>3</sub>	133.8
3Pθ-Al <sub>2</sub> O <sub>3</sub>	134.0
PO <sub>4</sub> <sup>3-</sup>	130.2
HPO <sub>4</sub> <sup>2-</sup>	133.4
H <sub>2</sub> PO <sub>4</sub> <sup>-</sup>	133.8

**Table S6.** Element content of Pd catalysts.

<b>Samples</b>	<b>Content of P (wt.%)</b>	<b>Content of Pd (wt.%)</b>
Pd/0Pθ-Al <sub>2</sub> O <sub>3</sub>	0	0.79
Pd/0.1Pθ-Al <sub>2</sub> O <sub>3</sub>	0.11	0.81
Pd/0.3Pθ-Al <sub>2</sub> O <sub>3</sub>	0.31	0.80
Pd/0.6Pθ-Al <sub>2</sub> O <sub>3</sub>	0.6	0.82
Pd/1Pθ-Al <sub>2</sub> O <sub>3</sub>	1.02	0.78
Pd/1.5Pθ-Al <sub>2</sub> O <sub>3</sub>	1.43	0.81
Pd/3Pθ-Al <sub>2</sub> O <sub>3</sub>	2.67	0.82

**Table S7.** Quantitative results of TGA test of samples.

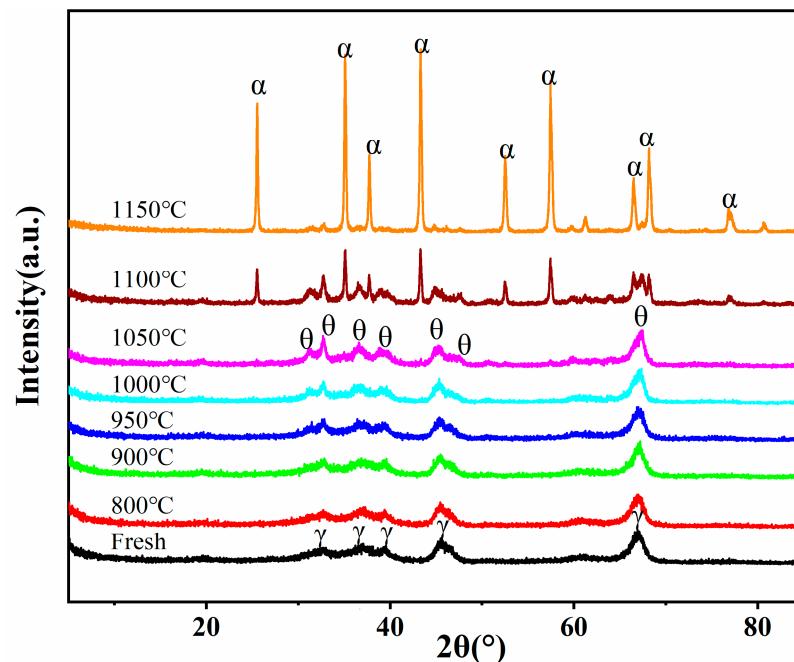
Samples	The Amount of Desorbed Water (mmol/g)
Pd/0Pθ-Al <sub>2</sub> O <sub>3</sub>	1.69
Pd/0.1Pθ-Al <sub>2</sub> O <sub>3</sub>	0.95
Pd/0.3Pθ-Al <sub>2</sub> O <sub>3</sub>	1.33
Pd/0.6Pθ-Al <sub>2</sub> O <sub>3</sub>	1.59
Pd/1Pθ-Al <sub>2</sub> O <sub>3</sub>	1.80
Pd/1.5Pθ-Al <sub>2</sub> O <sub>3</sub>	1.92
Pd/3Pθ-Al <sub>2</sub> O <sub>3</sub>	2.05

**Table S8.** Quantitative results of NH<sub>3</sub>-TPD test of samples.

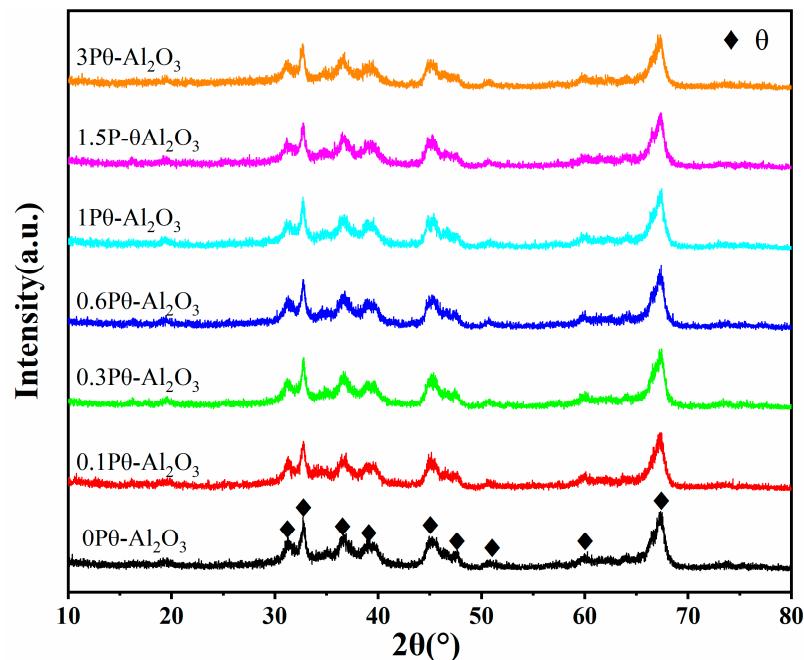
Samples	Peak1 Temperature (°C)	The Desorption of NH <sub>3</sub> at Peak 1 (μmol/g)	Relative Surface Hydroxyl Density
Pd/0Pθ-Al <sub>2</sub> O <sub>3</sub>	154	120.67	1.000
Pd/0.1Pθ-Al <sub>2</sub> O <sub>3</sub>	160	78.13	0.647
Pd/0.3Pθ-Al <sub>2</sub> O <sub>3</sub>	156	97.95	0.812
Pd/0.6Pθ-Al <sub>2</sub> O <sub>3</sub>	151	110.29	0.914
Pd/1Pθ-Al <sub>2</sub> O <sub>3</sub>	148	124.31	1.030
Pd/1.5Pθ-Al <sub>2</sub> O <sub>3</sub>	148	136.45	1.131
Pd/3Pθ-Al <sub>2</sub> O <sub>3</sub>	148	198.10	1.642

**Table S9.** Apparent activation energy of samples in the presence 8% water.

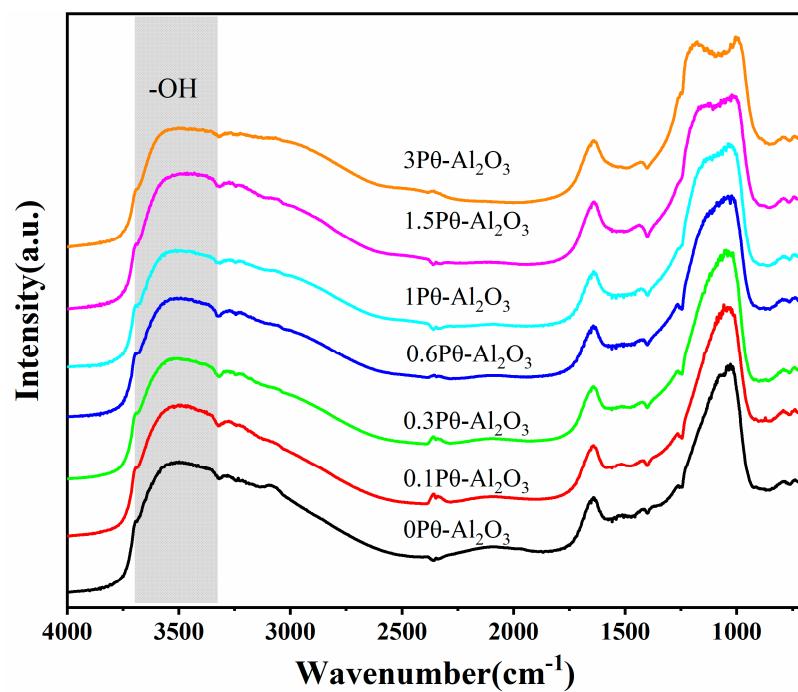
Samples	Apparent Activation Energy (kJ·mol <sup>-1</sup> )
Pd/0Pθ-Al <sub>2</sub> O <sub>3</sub>	172.81
Pd/0.1Pθ-Al <sub>2</sub> O <sub>3</sub>	170.24
Pd/0.3Pθ-Al <sub>2</sub> O <sub>3</sub>	171.14
Pd/0.6Pθ-Al <sub>2</sub> O <sub>3</sub>	170.41
Pd/1Pθ-Al <sub>2</sub> O <sub>3</sub>	172.07
Pd/1.5Pθ-Al <sub>2</sub> O <sub>3</sub>	172.05
Pd/3Pθ-Al <sub>2</sub> O <sub>3</sub>	177.60



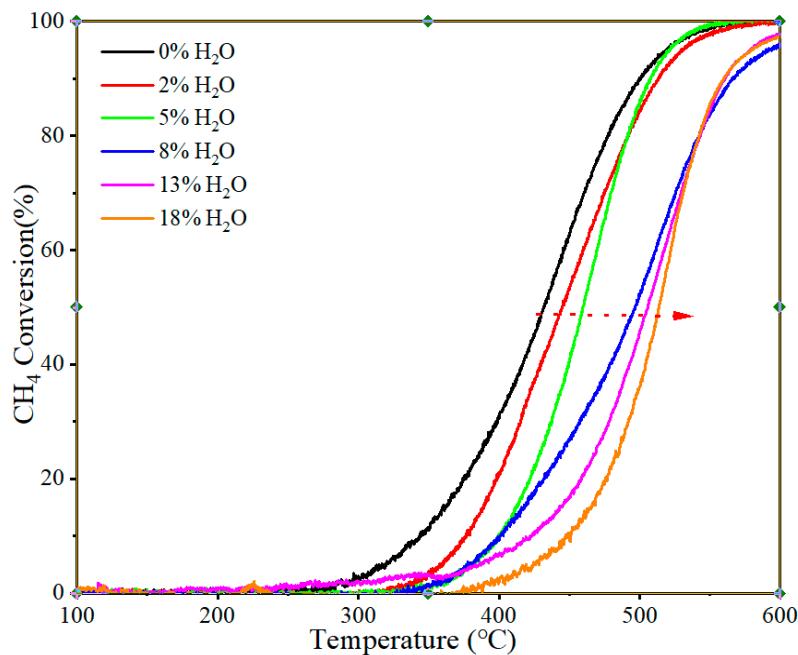
**Figure S1.** XRD patterns of the commercial  $\gamma$ - $\text{Al}_2\text{O}_3$  calcined at different temperature.



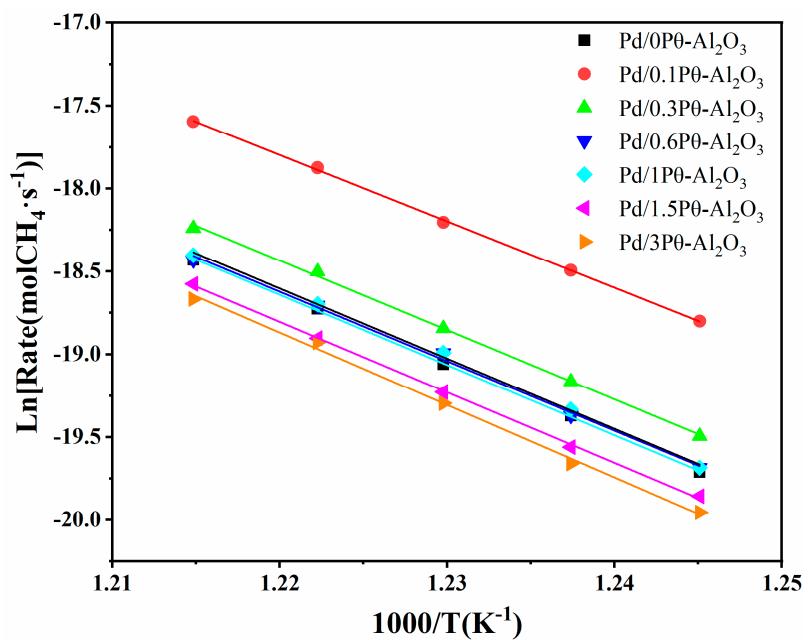
**Figure S2.** XRD patterns of the  $x$ P0- $\text{Al}_2\text{O}_3$  supports.



**Figure S3.** FT-IR profiles of supports.



**Figure S4.** Catalytic combustion of methane over Pd/ $\gamma$ - $\text{Al}_2\text{O}_3$  with different amounts of water Conditions: 2000 ppm CH<sub>4</sub>, 5 vol.% O<sub>2</sub>, 0–18 vol.% H<sub>2</sub>O, N<sub>2</sub> balance; GHSV=36,000 h<sup>-1</sup>.



**Figure S5.** The Arrhenius curve of the samples in the presence of 8% water. (Conditions: 2000ppm CH<sub>4</sub>, 5%O<sub>2</sub>, 8%H<sub>2</sub>O and N<sub>2</sub> as balance gas, GHSV=180,000h<sup>-1</sup>).