

## Article

# Determination of Chemical Kinetic Parameters for Adsorption and Desorption of NH<sub>3</sub> in Cu-Zeolite Used as a DeNO<sub>x</sub> SCR Catalyst of Diesel Engines

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**Abstract:** Ammonia-based selective catalytic reduction is one of the most effective NO<sub>x</sub> reduction technologies for diesel engines, but its low NO<sub>x</sub> reduction efficiency under low-temperature conditions needs further improvement. Previous studies have broadened our understanding of the NH<sub>3</sub> adsorption and desorption that occurs in an SCR catalyst of Cu ion-exchanged zeolite. However, many studies conducted to data on the control of the NH<sub>3</sub> adsorption and desorption in SCR catalysts have considered a simple chemical reaction related to a single acid site. This study demonstrates a detailed process for determining the chemical kinetic parameters of the adsorption and desorption of NH<sub>3</sub> for different types of acid sites of a zeolite catalyst. The determined chemical kinetics parameters will be used for more effective control of the SCR system in future studies.

**Keywords:** selective catalytic reduction; NH<sub>3</sub> temperature-programmed desorption; Cu-SSZ-13; NH<sub>3</sub> adsorption; NH<sub>3</sub> desorption



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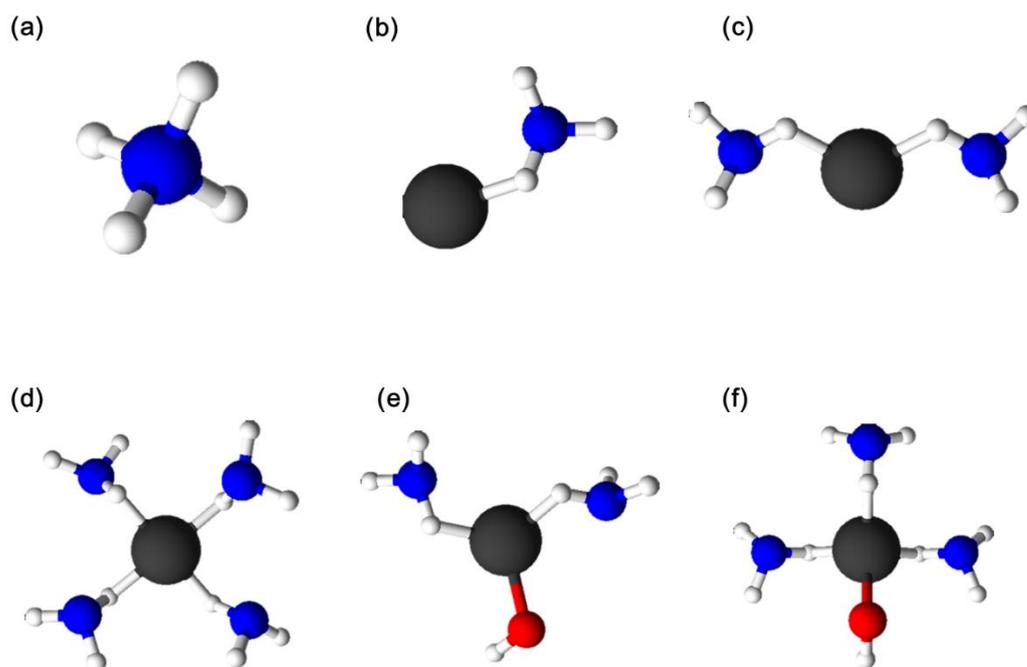


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## 1. Introduction

NO<sub>x</sub> is a major air pollutant emitted from diesel vehicles. To reduce NO<sub>x</sub>, selective catalyst reduction (SCR) systems have been widely used. Catalysts include large and medium pore zeolites such as ZSM-5, MOR, FER, and BEA, and small pore zeolites such as SSZ-13 and SAPO-34 [1]. Among the NH<sub>3</sub>-SCR catalysts, small pore zeolite catalysts such as Cu-SSZ-13 and Cu-SAPO-34 are being actively studied for their excellent NO<sub>x</sub> reduction efficiency and good hydrothermal stability [2–4]. Cu zeolite has a better SCR performance at low temperatures than Fe zeolite. Cu/SSZ-13 and Cu/SAPO are catalysts suitable for a wide temperature range with excellent hydrothermal stability, operating even below 350 °C [1].

Figure 1 shows the various forms of adsorbed NH<sub>3</sub> on Cu-zeolite, which was proposed by Chen et al. [5]. Figure 1a shows the NH<sub>3</sub> molecules bonded to the Brønsted acid site (BAS) in the form of NH<sub>4</sub><sup>+</sup>, and Figure 1b–f represents NH<sub>3</sub> complexes bonded to Cu ions. The bonding form of Cu ions and NH<sub>3</sub> molecules varies depending on the degree of Cu ionization, the presence of OH<sup>-</sup> ions, and the number of adsorbed NH<sub>3</sub> molecules. NH<sub>3</sub> combined with Cu ions has a different SCR reaction pathway depending on the oxidation state of Cu. [6]. The NH<sub>3</sub> bound to the Cu<sup>2+</sup> ion reacts with NO directly to form N<sub>2</sub> and H<sub>2</sub>O via an NO-assisted NH<sub>3</sub> activation pathway, and the NH<sub>3</sub> bound to the Cu<sup>2+</sup> ion is converted to Cu<sup>+</sup>-H<sup>+</sup> in this process. Also, the Cu<sup>+</sup>-H<sup>+</sup> oxidizes to Cu<sup>2+</sup> with a reaction with O<sub>2</sub> and NO<sub>2</sub>. In addition, the NH<sub>3</sub> bound to the Cu ion reacts with NO directly via an NO-assisted NH<sub>3</sub> activation pathway. On the other hand, the NH<sub>3</sub> bound to the Brønsted acid site is much less active under low-temperature steady-state conditions [7]. As such, it is important to understand the binding behavior of NH<sub>3</sub>, because the mechanism of the SCR reaction varies depending on the binding state of NH<sub>3</sub>.



**Figure 1.** Atomic configurations of  $\text{NH}_3$  complexes adsorbed in Cu-SSZ-13 zeolite as  $\text{NH}_3$  molecules. (a)  $\text{NH}_4^+$ , (b)  $[\text{Cu}(\text{I})\text{NH}_3]^+$ , (c) linear  $[\text{Cu}(\text{I})(\text{NH}_3)_2]^+$ , (d) fourfold  $[\text{Cu}(\text{II})(\text{NH}_3)_4]^{2+}$ , (e)  $[\text{Cu}(\text{II})(\text{OH})(\text{NH}_3)_2]^+$ , and (f)  $[\text{Cu}(\text{II})(\text{OH})(\text{NH}_3)_3]^+$ . Atom color codes: copper (gray), nitrogen (blue), oxygen (red), and hydrogen (white) [5].

The adsorption and desorption of  $\text{NH}_3$  in an SCR catalyst are important phenomena which affect the SCR reaction. Many studies have investigated  $\text{NH}_3$  adsorption and desorption by using various measuring techniques, such as  $\text{NH}_3$  temperature-programmed desorption (TPD) and infrared (IR) spectroscopy [8–10]. Recent studies [5,6,11] have shown that there are many peaks of  $\text{NH}_3$  desorption for Cu-zeolite catalysts according to the temperature range at which  $\text{NH}_3$  is desorbed. Lezcano-Gonzalez et al. [10] observed two  $\text{NH}_3$  desorption peaks in H-SSZ-13 and explained their chemical bonding structures. The first peak, called the low-temperature (LT) peak, is a desorption peak at approximately 180 °C. They explained that  $\text{NH}_3$  molecules desorbed in the LT peak were weakly bound to the Lewis acid site (LAS) or solvated to  $\text{NH}_4^+$  ions. The second peak is called the high-temperature (HT) peak, and occurs in the temperature range of approximately 450 °C. It was explained as  $\text{NH}_3$  that is strongly bound to the BAS. Lezcano-Gonzalez et al. [11] compared the  $\text{NH}_3$ -TPD profiles of H-SSZ-13 and Cu-SSZ-13 and confirmed the absence of an intermediate temperature (IT) peak in H-SSZ-13. Further, when the amount of Cu ion exchange increased, the size of the IT peak increased, while that of the HT peak decreased. This indicates that the Cu ions in the catalyst affect the IT peak.

Chen et al. [5] explained these peaks by simulating the  $\text{NH}_3$ -TPD profile of Cu-CHA zeolite using discrete Fourier transform (DFT) calculations. They explained that the LT peak represents the desorption of  $\text{NH}_3$  from LAS, along with  $\text{NH}_3$  desorption from a  $[\text{Cu}(\text{II})(\text{OH})(\text{NH}_3)_3]^+$  complex. The IT peak shown at 250–350 °C was attributed to the decomposition of a linear  $[\text{Cu}(\text{I})(\text{NH}_3)_2]^+$  complex and residual  $[\text{Cu}(\text{II})(\text{OH})(\text{NH}_3)_3]^+$ . The HT peak at 400–500 °C was attributed to  $\text{NH}_3$  in the form of  $\text{NH}_4^+$  adsorbed to the BAS,  $[\text{Cu}(\text{I})(\text{NH}_3)]^+$ , and  $[\text{Cu}(\text{II})(\text{NH}_3)_4]^{2+}$ .

Table 1 compares the  $\text{NH}_3$  bonding mechanisms represented by the studies of Chen et al. [5] and Lezcano-Gonzalez et al. [11]. Chen et al. [5] suggested a more detailed bonding mechanism between Cu ions and  $\text{NH}_3$  molecules. In contrast, Lezcano-Gonzalez et al. mentioned  $\text{NH}_3$  molecules solvating  $\text{NH}_4^+$  ions as a cause of the LT peak, and the extra-framework aluminum (EFAL) as a cause of another HT peak, which was not mentioned by Chen et al.

**Table 1.** NH<sub>3</sub> adsorption form organizing the NH<sub>3</sub> adsorption peak by temperature, as mentioned in various literature and papers.

Classification of NH <sub>3</sub> Desorption Peak	Study of Chen et al. [5]	Study of Lezcano-Gonzalez et al. [11]
Low-Temperature peak	LAS [Cu(II)(OH)(NH <sub>3</sub> ) <sub>3</sub> ] <sup>+</sup>	LAS NH <sub>3</sub> molecules solvating NH <sub>4</sub> <sup>+</sup> ions
Intermediate-Temperature peak	[Cu(I)(NH <sub>3</sub> ) <sub>2</sub> ] <sup>+</sup> remained [Cu(II)(OH)(NH <sub>3</sub> ) <sub>3</sub> ] <sup>+</sup>	NH <sub>3</sub> adsorbed at the Cu <sup>2+</sup> sites
High-Temperature peak	NH <sub>4</sub> <sup>+</sup> (BAS) [Cu(I)(NH <sub>3</sub> ) <sub>2</sub> ] <sup>+</sup> [Cu(II)(NH <sub>3</sub> ) <sub>4</sub> ] <sup>2+</sup>	NH <sub>4</sub> <sup>+</sup> (BAS) EFAL (extra framework aluminum)

Yoshihisa et al. [5] compared the NH<sub>3</sub> adsorption and desorption of H-ZSM-5 and Cu-ZSM-5. Similarly to the study by Lezcano-Gonzalez et al. [11], Yoshihisa et al. observed that H-ZSM-5 had two NH<sub>3</sub> peaks in the LT and HT regions, while Cu-ZSM-5 had an additional peak in the IT region. Additionally, they found that the NO reduction reaction did not occur in the absence of Cu ions in the zeolite. This means that the Cu ion sites are very important for the SCR reaction, and the adsorption and desorption with various forms of NH<sub>3</sub> at the Cu sites should be comprehensively studied.

Gao et al. [12,13] and Paolucci et al. [14] demonstrated the importance of Cu-NH<sub>3</sub> intermediates, such as [Cu(II)(OH)(NH<sub>3</sub>)<sub>3</sub>]<sup>+</sup> and [Cu(I)(NH<sub>3</sub>)<sub>2</sub>]<sup>+</sup>, in the low-temperature SCR reaction. As a starting point for the SCR reaction, they suggested that [Cu(II)(OH)]<sup>+</sup> adsorbs two NH<sub>3</sub> molecules and forms a complex of [Cu(II)(OH)(NH<sub>3</sub>)<sub>3</sub>]<sup>+</sup>. When an NO molecule is introduced, the [Cu(II)(OH)(NH<sub>3</sub>)<sub>3</sub>]<sup>+</sup> changes to intermediates of NH<sub>2</sub>-Cu(I)-NO or NH<sub>3</sub>-Cu(I)-HONO by rearranging the NH<sub>3</sub> and NO ligands. Eventually, N<sub>2</sub> and H<sub>2</sub>O are formed from these intermediates. Then, after the adsorption of another NH<sub>3</sub> molecule onto the Cu ion, [Cu(I)(NH<sub>3</sub>)<sub>2</sub>]<sup>+</sup> is formed. Next, two [Cu(I)(NH<sub>3</sub>)<sub>2</sub>]<sup>+</sup> intermediates and oxygen molecules combine to form [Cu(I)(NH<sub>3</sub>)<sub>2</sub>]<sup>+</sup>-O<sub>2</sub>-[Cu(I)(NH<sub>3</sub>)<sub>2</sub>]<sup>+</sup>. The compound changes again to [Cu(II)(OH)(NH<sub>3</sub>)<sub>3</sub>]<sup>+</sup> via electron transfer from Cu to O and hydration with H<sub>2</sub>O molecules. This means that the adsorption of ammonia to the Cu ion plays an important role in the NO-SCR cycle.

According to previous studies [15,16], NO<sub>x</sub> removal efficiency at low temperatures can be improved by increasing the amount of NH<sub>3</sub> adsorption in the SCR catalyst. It is well known that NH<sub>3</sub> slip can be prevented by careful control of NH<sub>3</sub> adsorption and desorption at high temperatures. However, much of the previous research regarding NH<sub>3</sub> adsorption control for SCR systems of diesel engines considered the catalyst as a single acid site, even though the adsorption of NH<sub>3</sub> in zeolite is influenced by multiple acid sites with different characteristics. As far as we know, there has been no research showing a detailed experimental process to determine the chemical kinetic parameters of adsorption and desorption of NH<sub>3</sub> for different types of acid sites of a zeolite catalyst.

This study investigated the adsorption and desorption of NH<sub>3</sub> on various kinds of acid sites of Cu-SSZ-13 zeolite and attempted to determine their chemical kinetic parameters, which are needed for more precise control of the SCR reaction.

## 2. Results and Discussion

In the SCR reaction modeling, information on both the NH<sub>3</sub> adsorption rate and desorption rate are necessary. In the single-site model, the NH<sub>3</sub> adsorption rate,  $r_{\text{ads}}$ , can be expressed using Equation (1):

$$r_{\text{ads}} = k_{\text{ads}} C_{\text{NH}_3} (1 - \theta_{\text{NH}_3}) \quad (1)$$

where  $k_{\text{ads}}$  is the reaction constant and  $C_{\text{NH}_3}$  is the mole concentration of  $\text{NH}_3$ .  $\theta_{\text{NH}_3}$  is the surface coverage of the catalyst by  $\text{NH}_3$  molecules. It is defined as:

$$\theta_{\text{NH}_3} = \frac{N_{\text{NH}_3}}{N^*_{\text{NH}_3}} \quad (2)$$

where  $N_{\text{NH}_3}$  is the amount of  $\text{NH}_3$  molecules adsorbed on the catalyst and  $N^*_{\text{NH}_3}$  is the maximum amount of  $\text{NH}_3$  molecules adsorbed on the catalyst.

The  $\text{NH}_3$  desorption rate,  $r_{\text{des}}$ , of the single-site model is generally expressed as follows:

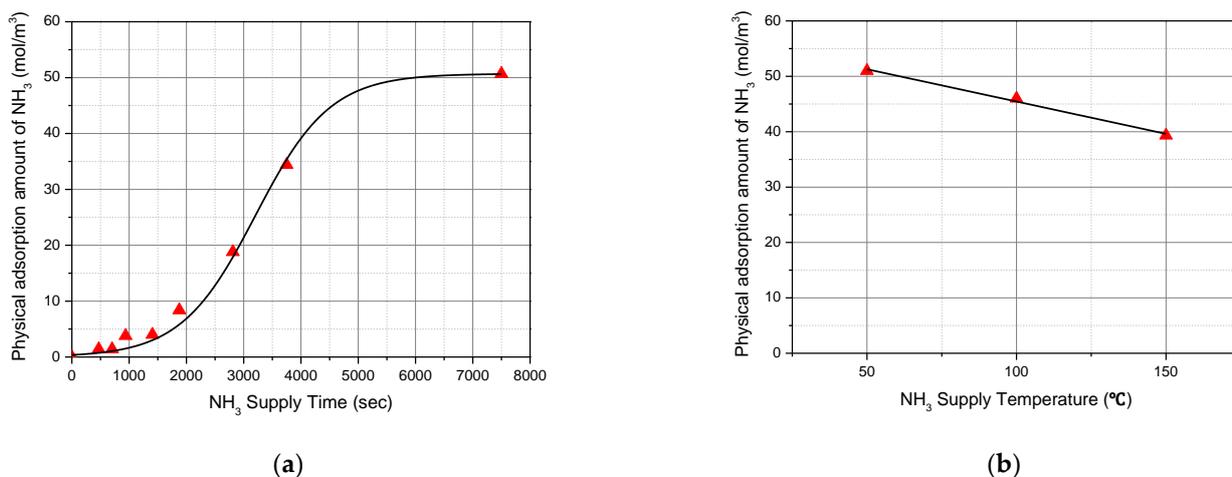
$$r_{\text{des}} = k_{\text{des}} \cdot \exp\left(-\frac{E_{\text{des}}}{RT}\right) \theta_{\text{NH}_3} \quad (3)$$

where  $k_{\text{des}}$  is the reaction constant and  $C_{\text{NH}_3}$  is the mole concentration of  $\text{NH}_3$ .  $E_{\text{des}}$  is the activation energy.  $R$  and  $T$  are the universal gas constant and catalyst temperature, respectively.

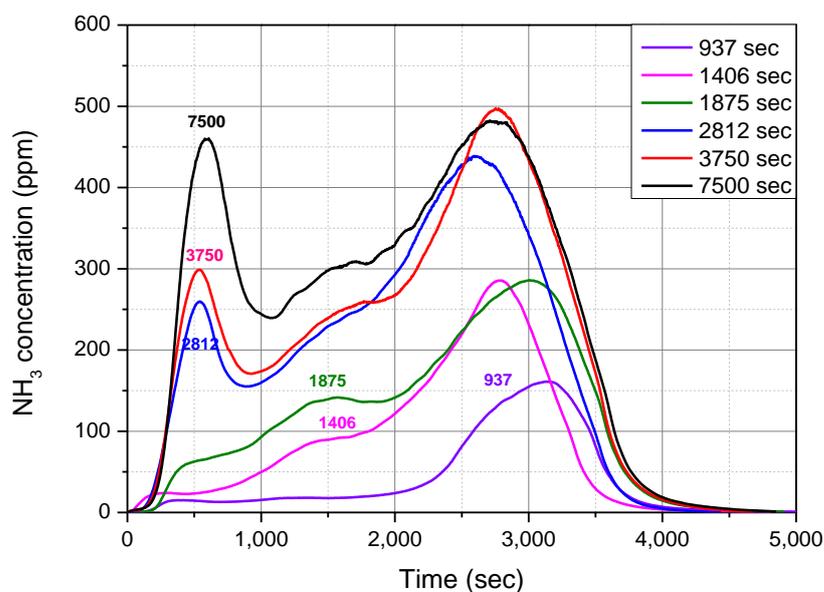
In this study, we attempted to extend the above single-site model to a multi-site model to provide more detailed information on  $\text{NH}_3$  adsorption and desorption rates. In the next section, the modified forms of Equations (2) and (3) are shown for the multi-site model.

In this study, only the chemically adsorbed  $\text{NH}_3$  molecules were considered. Figure 2a shows that the amount of physically adsorbed  $\text{NH}_3$  molecules increased as the  $\text{NH}_3$  supply time increased. At the beginning of the  $\text{NH}_3$  gas supply, the chemical bonds on the acid sites are superior. Therefore, the physical adsorption rate of  $\text{NH}_3$  gas molecules is small. After that, the physical adsorption rate increases, because the number of acid sites available for chemical bonding is decreased. In addition, when a large amount of ammonia molecules are physically adsorbed, the physical adsorption rate decreases again due to the limitation of molecular diffusion. The experimental results also showed that the physical adsorption rate is small at the beginning, then increases rapidly, and decreases at the end. When the ammonia supply in the feed gas is stopped, the physically adsorbed ammonia is desorbed into the feed gas due to the difference between the ammonia concentration in the feed gas and the ammonia concentration on the catalyst surface. Figure 2b show the effect of temperature on the physically adsorbed  $\text{NH}_3$  molecules. It decreases as the  $\text{NH}_3$  supply temperature increases. This is because the attraction surface force, which acts between the catalyst surface and ammonia molecules, becomes smaller than the kinetic energy of the ammonia molecules, which is increased when the feed gas temperature increases. S. J. PALMER [17] presented a mathematical relationship showing that the surface force of water becomes smaller with an increase in temperature, which proves the validity of the results obtained in Figure 2.

Figure 3 shows the variation of  $\text{NH}_3$ -TPD curves with the  $\text{NH}_3$  supply time. The 7500 s curve consisted of three peaks. Many researchers have found the same results from similar experiments. These three peaks have been called the LT peak ( $\sim 200$  °C), IT peak (200–400 °C), and HT peak ( $\sim 400$  °C). The curves below 937 s show that  $\text{NH}_3$  was mainly desorbed at the HT peak of 400 °C or more. This indicates that the initial adsorption of  $\text{NH}_3$  molecules occurred in the acid sites of the HT peak, which had a high bonding energy. When the  $\text{NH}_3$  supply time was increased to 1406 s, the HT peak grew and the smaller IT peak appeared. Further, when the  $\text{NH}_3$  supply time was increased to 1875 s, the LT peak appeared at temperatures below 200 °C. According to studies by several researchers, the HT peak was mainly related to the  $\text{NH}_3$  molecules, which are strongly bonded to BAS, and the IT peak was related to the  $\text{NH}_3$  molecules that were adsorbed to Cu ions. Additionally, it seems that the LT peak comprised weakly bonded  $\text{NH}_3$  molecules in the form of  $[\text{Cu}(\text{II})(\text{OH})(\text{NH}_3)_3]^+$  or solvated to  $\text{NH}_4^+$  ions.

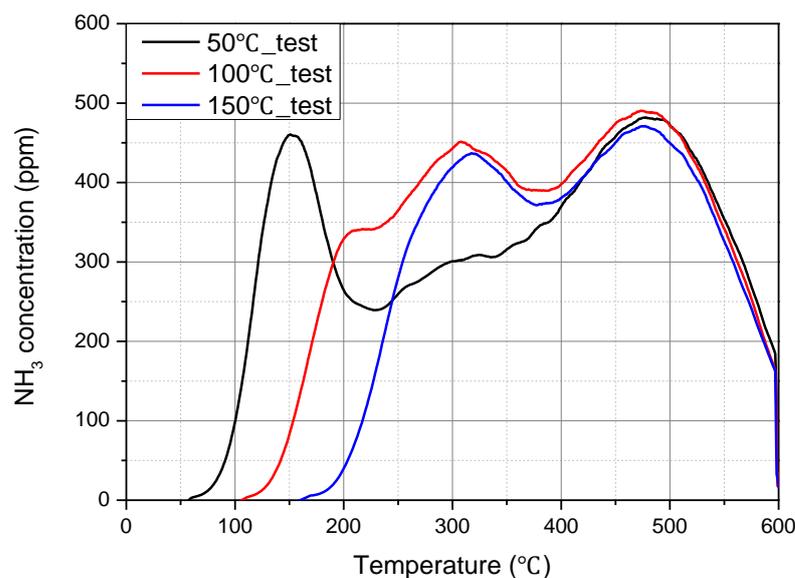


**Figure 2.** Variation of the physically adsorbed NH<sub>3</sub> amount according to the various parameters: (a) Effect of NH<sub>3</sub> supply time (inlet NH<sub>3</sub> concentration: 200 ppm, temperature of NH<sub>3</sub> absorption: 50 °C); (b) effect of NH<sub>3</sub> adsorption temperature (inlet NH<sub>3</sub> concentration: 200 ppm, NH<sub>3</sub> supply time: 7500 s).



**Figure 3.** Variation of NH<sub>3</sub>-TPD curves with respect to the NH<sub>3</sub> supply time (inlet NH<sub>3</sub> concentration: 200 ppm, temperature of NH<sub>3</sub> absorbing: 50 °C).

Figure 4 shows the results of NH<sub>3</sub> TPD tests obtained at different NH<sub>3</sub> adsorption temperatures of 50 °C, 100 °C, and 150 °C. In the three experiments, 200 ppm of NH<sub>3</sub> gas was supplied to the catalyst for 7500 s equally. Therefore, the same amount of NH<sub>3</sub> was supplied. According to the results of these experiments, the shapes of the HT peaks of the three different temperature conditions were nearly the same. However, the LT peak disappeared, and the IT peak increased as the NH<sub>3</sub> adsorption temperature increased from 50 °C to 100 °C and then to 150 °C. The large size of the LT peak and the small size of the IT peak at 50 °C indicate that the LT peak interrupts the growth of the IT peak. This means that the LT peak and IT peak are chemically related. As suggested by Chen et al. [5], the OH of [Cu(II)(OH)(NH<sub>3</sub>)<sub>3</sub>]<sup>+</sup> in the LT peak is separated at 100 °C or higher, and it is changed to [Cu(I)(NH<sub>3</sub>)<sub>2</sub>]<sup>+</sup> and moved to the IT peak.



**Figure 4.** The effect of the  $\text{NH}_3$  adsorption temperature on the  $\text{NH}_3$ -TPD test ( $\text{NH}_3$  supply concentration: 200 ppm,  $\text{NH}_3$  supply time: 7500 s).

Comparing the HT peaks of 2812 and 7500 s in Figure 5 and the HT peaks at 50 °C, 100 °C, and 150 °C in Figure 4, the height and width of the HT peaks are almost the same. This means that when the adsorption time is sufficiently long, the HT peak converges to a certain shape. Therefore, the number of acid sites for the HT peak is finite. Similarly, it seems that the shape of the IT peaks in Figures 3 and 4 eventually converged to that of the IT peak at 150 °C, as shown in Figure 4. To describe the degree of  $\text{NH}_3$  adsorption at the acid sites, the term surface coverage ( $\theta_{\text{NH}_3}$ ) was used in this study. Coverage of the HT and IT peaks is defined in Equations (4) and (5), as follows:

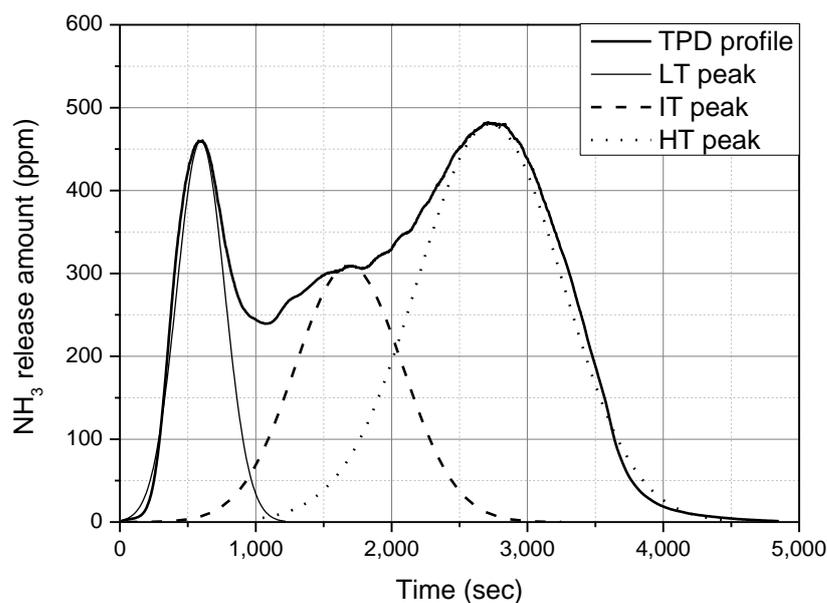
$$\theta_{\text{NH}_3\text{-HT}} = \frac{N_{\text{HT}}}{N_{*\text{HT}}} \quad (4)$$

$$\theta_{\text{NH}_3\text{-IT}} = \frac{N_{\text{IT}}}{N_{*\text{IT}}} \quad (5)$$

where  $N_{\text{HT}}$  and  $N_{\text{IT}}$  are the amounts of  $\text{NH}_3$  molecules adsorbed in the HT and IT peaks, respectively.  $N_{*\text{HT}}$  and  $N_{*\text{IT}}$  are the maximum catalyst adsorption capacities of the HT and IT peaks, respectively.

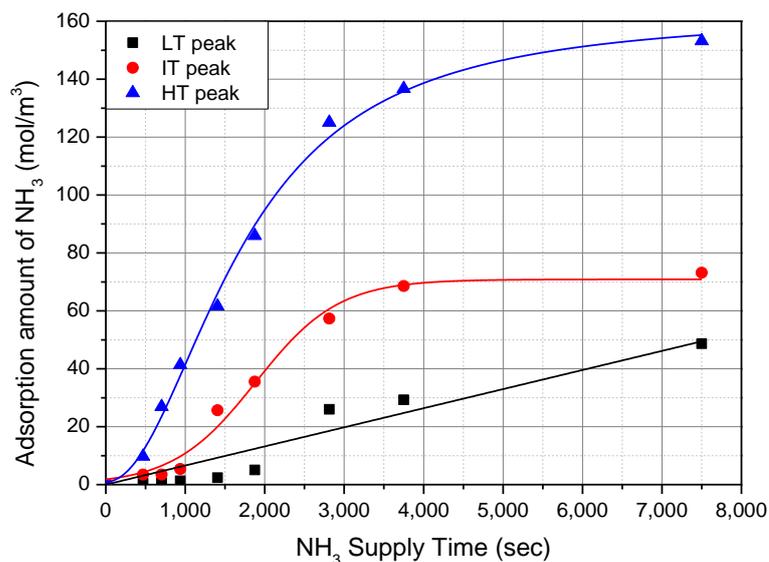
However, the size of the LT peak continued to increase and did not converge, as shown in Figures 3 and 4. This means that the rate of  $\text{NH}_3$  adsorption of the LT peak was not expressed as a function of coverage.

Figure 5 shows an example of curve fitting for the  $\text{NH}_3$  TPD test results. This study assumed that the LT, IT, and HT peaks of the TPD curve can be expressed using standard normal distribution curves. In this example, the difference between the total amount of  $\text{NH}_3$  adsorption obtained by integrating the TPD curve and that obtained by integrating the three standard normal distribution curves was only 0.56%. Thus, it can be said that analysis using curve fitting did not cause a significant error. The integrated amount of  $\text{NH}_3$  of the peaks presented in this paper were obtained from curve fitting with standard normal distribution curves.



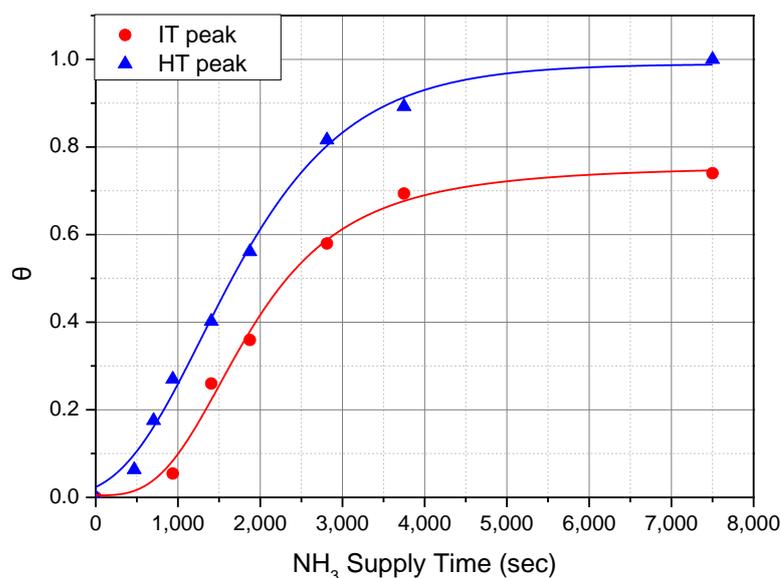
**Figure 5.** An example of curve fitting of TPD curve with three normal distribution curves of the LT, IT, and HT peak (inlet NH<sub>3</sub> concentration: 200 ppm, NH<sub>3</sub> supply time: 7500 s, temperature of NH<sub>3</sub> adsorbing: 50 °C).

Figure 6 shows the change in the NH<sub>3</sub> adsorption amount of each peak with respect to time. It was obtained from the curves shown in Figure 5 by integrating the HT, IT, and LT peaks. The NH<sub>3</sub> adsorption amount of the HT and IT peaks increased rapidly at the beginning and then became saturated at a certain value. However, it seems that the saturation of the LT peak was not clear as the NH<sub>3</sub> supply time increased. Many other studies [11,18,19] have shown that solvation of the ammonium ion (NH<sub>4</sub><sup>+</sup>) by NH<sub>3</sub> can occur under low temperatures. This solvation is independent to acid sites, and quite a large amount of NH<sub>3</sub> molecules attach as a form of NH<sub>4</sub><sup>+</sup>·(NH<sub>3</sub>)<sub>n</sub>. Here, n is the number of NH<sub>3</sub> molecules attached to ammonium ions. Because of this, linear curve fitting was used to describe the development of NH<sub>3</sub> adsorption amount of the LT peak. Additionally, we found that the total amount of NH<sub>3</sub> adsorption of the HT peak was the largest, that of the IT peak was second, and that of the LT peak was the smallest.



**Figure 6.** Change in the amount of NH<sub>3</sub> adsorption of each peak with respect to NH<sub>3</sub> supply time (inlet NH<sub>3</sub> concentration: 200 ppm, temperature of NH<sub>3</sub> adsorbing: 50 °C).

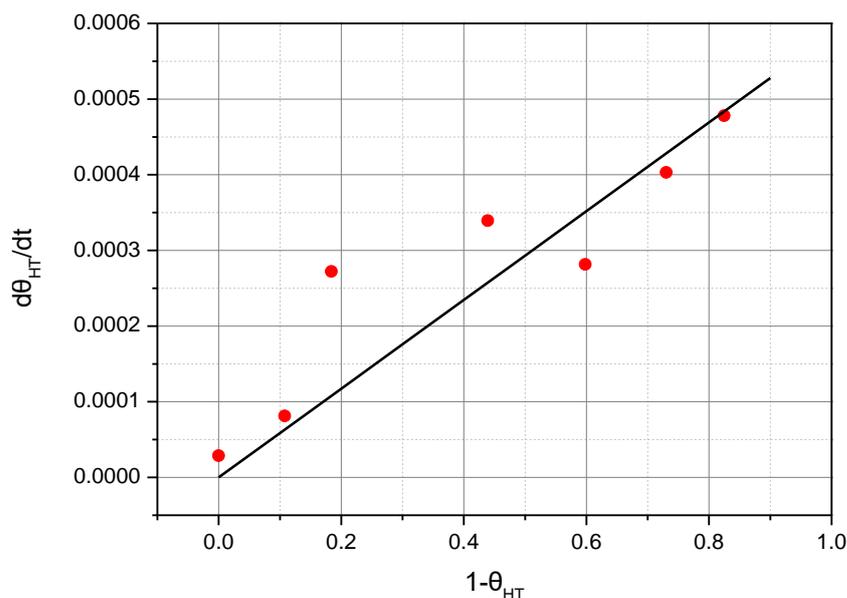
Figure 7 shows the re-plotted graph of Figure 6 with the relationship between  $\theta$  and the  $\text{NH}_3$  supply time. For the calculation of  $\theta$ , the values of  $\Omega_{\text{HT}}^*$  of  $153 \text{ mol/m}^3$  and  $\Omega_{\text{IT}}^*$  of  $99 \text{ mol/m}^3$  were used, respectively. These values were obtained from the integration of the saturated HT and IT peaks shown in Figures 3 and 4, respectively. As already mentioned, the LT peak continued to grow and did not converge to a specific shape, so the  $\text{NH}_3$  adsorption rate cannot be expressed as a function of  $\theta$ , and it is not included in Figure 7.



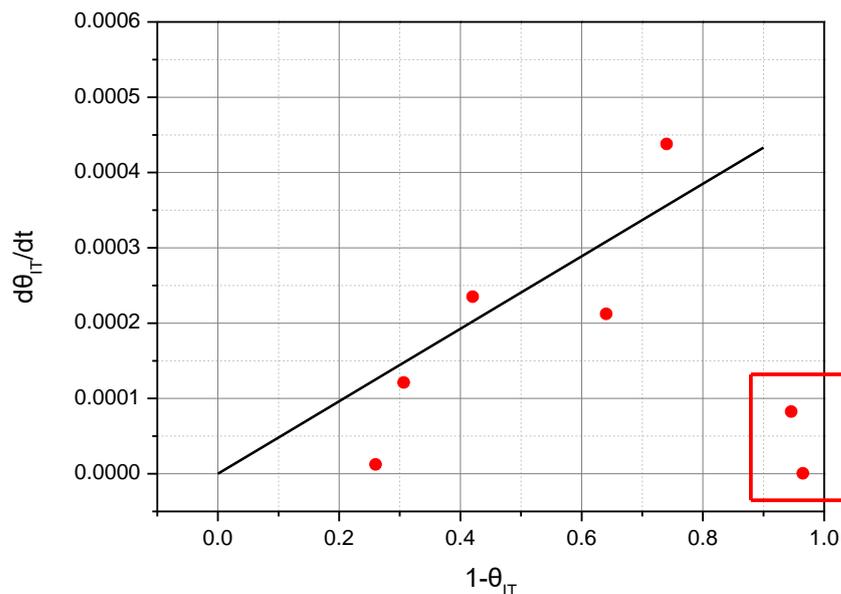
**Figure 7.** Change in  $\theta$  of the HT and IT peaks according to  $\text{NH}_3$  supply time (inlet  $\text{NH}_3$  concentration: 200 ppm, temperature of  $\text{NH}_3$  absorbing:  $50^\circ\text{C}$ ).

Figure 8 shows the correlation between  $d\theta_{\text{HT}}/dt$  and  $(1-\theta_{\text{HT}})$  for  $\text{NH}_3$  adsorption, which was replotted with the data of Figure 7. It seems that  $d\theta_{\text{HT}}/dt$  is proportional to  $(1-\theta_{\text{HT}})$ . This means that the reaction rate of adsorption of  $\text{NH}_3$  molecules on the acid sites constituting the HT peak can be expressed by the first-order equation for  $(1-\theta_{\text{HT}})$ . The reason for some deviations from the linear relationship seem to be due to factors that were not managed precisely during the experiment, such as different external conditions (moisture and temperature) and changes in the catalyst state that occurred during the experiment.

Figure 9 shows the correlation between  $d\theta_{\text{IT}}/dt$  and  $(1-\theta_{\text{IT}})$  for  $\text{NH}_3$  adsorption. Unlike the HT peak in Figure 8, a very small value of  $d\theta_{\text{IT}}/dt$  was observed at the initial stage of  $\text{NH}_3$  adsorption. Subsequently,  $d\theta_{\text{IT}}/dt$  had a maximum value at  $\theta$  of  $\sim 0.2$ , and thereafter, it tended to decrease as  $\theta_{\text{IT}}$  increased. The  $\text{NH}_3$  molecules were first adsorbed to the strong acid sites of the HT peak, and then the acid sites of the IT peak were filled with  $\text{NH}_3$  molecules. This led to a low  $\text{NH}_3$  adsorption rate for the IT peak at the initial stage of  $\text{NH}_3$  adsorption. However, in the absence of the influence of the acid sites of the HT peak, the rate of adsorption of ammonia to the acid sites of IT peak seems to be linearly proportional to  $(1-\theta_{\text{IT}})$ . The deviations from the linear relationship in Figure 9 mean that the rate of  $\text{NH}_3$  adsorption to acid sites in the IT peak was not only affected by  $(1-\theta_{\text{IT}})$ , but also other factors. Additionally, it can be said that these deviations were larger than in Figure 8. This means that the rate of  $\text{NH}_3$  adsorption to acid sites of the IT peak is affected by more factors than the HT peak. In addition to the external air temperature, humidity, and catalyst state described in Figure 8, the influence of acid sites of the HT peak and LT peak are also included in these factors.



**Figure 8.** The relationship of  $d\theta_{HT}/dt$  and  $1-\theta_{HT}$  (inlet  $NH_3$  concentration: 200 ppm, temperature of  $NH_3$  absorbing:  $50\text{ }^\circ\text{C}$ ).



**Figure 9.** The relationship of  $d\theta_{IT}/dt$  and  $(1-\theta_{IT})$  (inlet  $NH_3$  concentration: 200 ppm, temperature of  $NH_3$  absorbing:  $50\text{ }^\circ\text{C}$ ).

To date, many researchers have attempted to calculate the rate of  $NH_3$  adsorption and desorption of a zeolite catalyst as a single-site model. Although the single-site model has the advantage of being simple, it is limited in providing an effective description of the phenomena of  $NH_3$  adsorption and desorption.

This study suggests the modification of Equation (3) to describe the  $NH_3$  adsorption rates as Equation (6) for the acid sites in the HT peak, and Equation (7) for the acid sites in the IT peak.

$$r_{ads\_HT} = k_{ads\_HT}C_{NH_3}(1 - \theta_{HT}) \tag{6}$$

$$r_{ads\_IT} = k_{ads\_IT}C_{NH_3}(1 - \theta_{IT}) \tag{7}$$

The values of  $k_{ads\_HT}$  and  $k_{ads\_IT}$  can be determined from the slopes of Figures 8 and 9, respectively.

To effectively describe the desorption phenomenon of ammonia molecules on the Cu SSZ-13 zeolite catalyst, it is desirable to express the desorption rates of the IT peak and HT peak separately. The NH<sub>3</sub> desorption rate can be described as follows:

$$r_{\text{des\_HT}} = k_{\text{des\_HT}} * \exp\left(-\frac{E_{\text{des\_HT}}}{RT}\right) \theta_{\text{NH}_3\text{-HT}} \tag{8}$$

$$r_{\text{des\_IT}} = k_{\text{des\_IT}} * \exp\left(-\frac{E_{\text{des\_IT}}}{RT}\right) \theta_{\text{NH}_3\text{-IT}} \tag{9}$$

Figures 10 and 11 introduce the process to find  $k_{\text{des\_HT}}$ ,  $k_{\text{des\_IT}}$ ,  $E_{\text{des\_HT}}$ , and  $E_{\text{des\_IT}}$  in Equations (8) and (9).

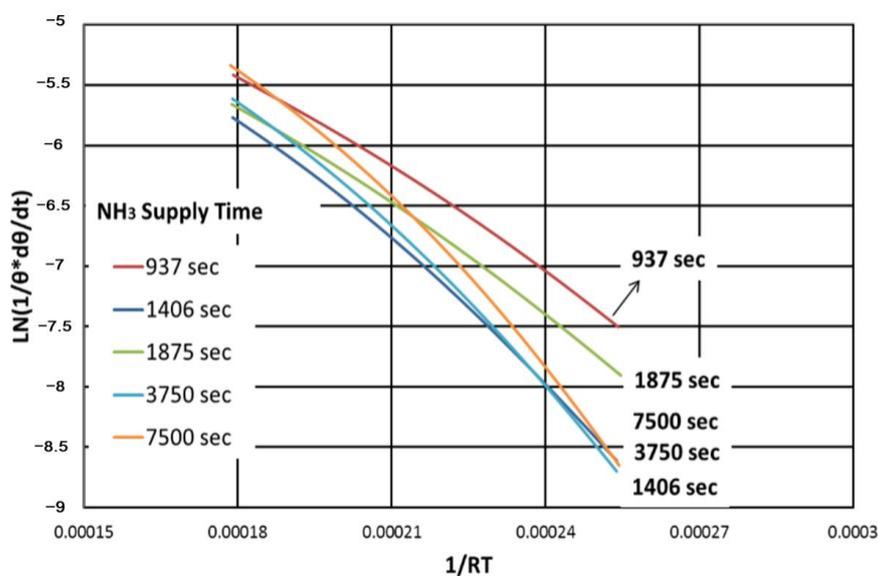


Figure 10. The relationship of the NH<sub>3</sub> desorption rate and temperature for the IT peak.

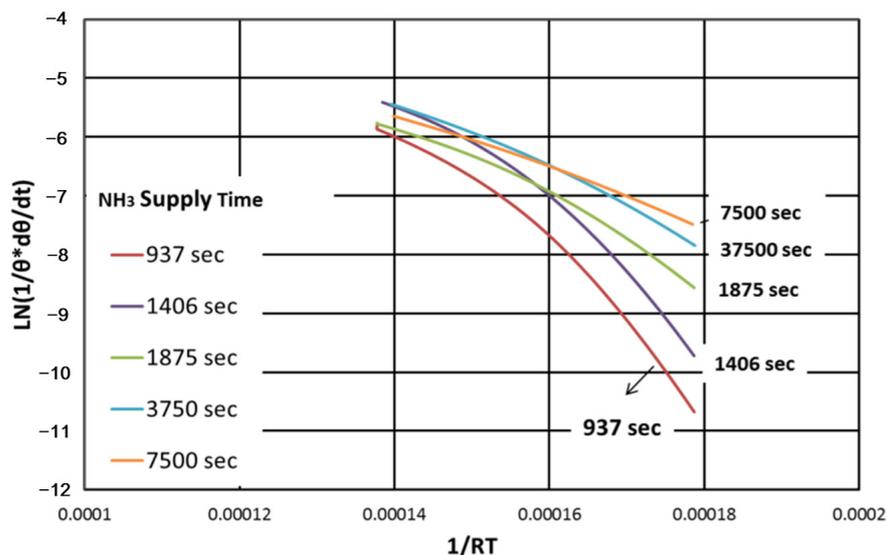


Figure 11. The relationship of the NH<sub>3</sub> desorption rate and temperature for the HT peak.

Figure 10 shows the relationship between  $\ln(1/\theta \cdot d\theta/dt)$  and  $1/(RT)$  of the IT peak. In this graph, the slope represents the value of the activation energy of the reaction, and the log value of the  $y$ -axis intercept indicates the Arrhenius reaction constant. A nearly linear relationship between  $\ln(1/\theta \cdot d\theta/dt)$  and  $1/(RT)$  is shown at each curve. However, the slopes and the values of  $y$ -axis intercept of each curve show some deviations, with no clear trend. The reason for this deviation is uncertain. The deviations may be caused by the experimental method, or by ambient conditions.

Figure 11 shows the  $\text{NH}_3$  desorption rate of the HT peak as a function of  $\ln(1/\theta \cdot d\theta/dt)$  versus  $1/(RT)$ . The slope of the curve, which represents the activation energy, decreased when the  $\text{NH}_3$  supply time was increased. This means that in the SSZ-13 catalyst, various acid sites with different degrees of acidity are widely distributed in the HT peak. These results show that  $\text{NH}_3$  molecules adsorbed early in the reaction had stronger bonding and higher activation energy than  $\text{NH}_3$  molecules adsorbed later.

From the above experimental results, we found that the activation energy and pre-exponential factor of the HT peak and LT peak gradually changed as the process of ammonia desorption proceeded. This study determined the averaged values of activation energy and the pre-exponential factor. It is necessary to find a more effective method to express the change of these values with time. However, the averaged kinetic parameters give the advantage of simple calculation.

Table 2 shows the values of the kinetic parameters for Equations (6)–(9), which were determined from the experimental results for  $\text{NH}_3$  concentrations of 200 ppm. These values can be used effectively to describe the  $\text{NH}_3$  adsorption and desorption of a zeolite catalyst.

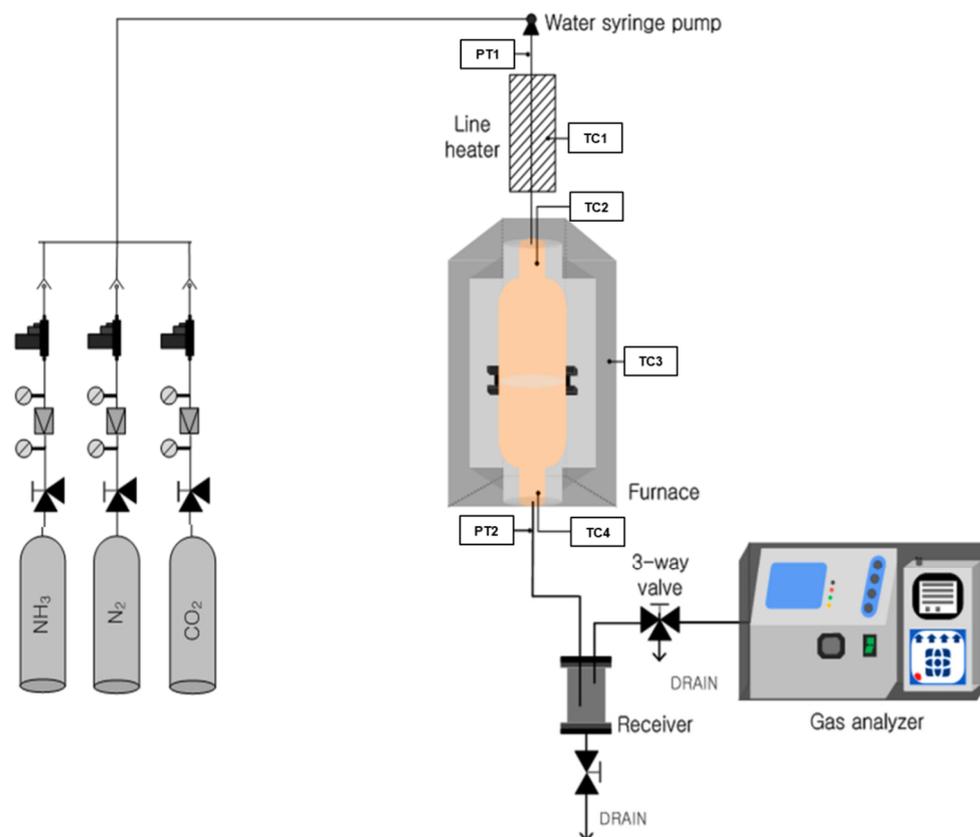
**Table 2.** The values of  $k_{\text{ads}}$ ,  $k_{\text{des}}$ , and  $E_{\text{des}}$  of the HT and IT peaks.

peak	$k_{\text{ads}}$		$k_{\text{des}}$		$E_{\text{des}}$ (kJ/mol)	
	IT	HT	IT	HT	IT	HT
values	$2.4 \times 10^{-6}$	$2.9 \times 10^{-6}$	11.2	$2.5 \times 10^5$	42.7	94.6

### 3. Experimental Equipment and Methods

#### 3.1. Experimental Equipment

A schematic of the experimental setup is shown in Figure 12. It was composed of a gas feeding device, a catalyst, electric heaters to increase the temperature, and a gas analyzer.  $\text{N}_2$ ,  $\text{CO}_2$ , and  $\text{NH}_3$  gases were supplied, and their flow rates were controlled using mass flow controllers (MFC). The catalyst used in this study was Cu-SSZ-13 zeolite, which was commercialized by a motor company for EURO-6 heavy-duty diesel vehicles. The general properties of the Cu-SSZ-13 zeolite can be found in the reference from the manufacturer [20]. The catalyst was coated onto a honeycomb-type ceramic monolith. The diameter and length of the catalyst were 2 cm and 1 cm, respectively. The temperatures of the feeding gas and catalyst were controlled using electric heaters. The gases, including  $\text{NH}_3$ , were measured using FT-IR spectroscopy.



**Figure 12.** Schematic diagram of the experimental setup for the NH<sub>3</sub>-TPD test.

### 3.2. Experimental Method

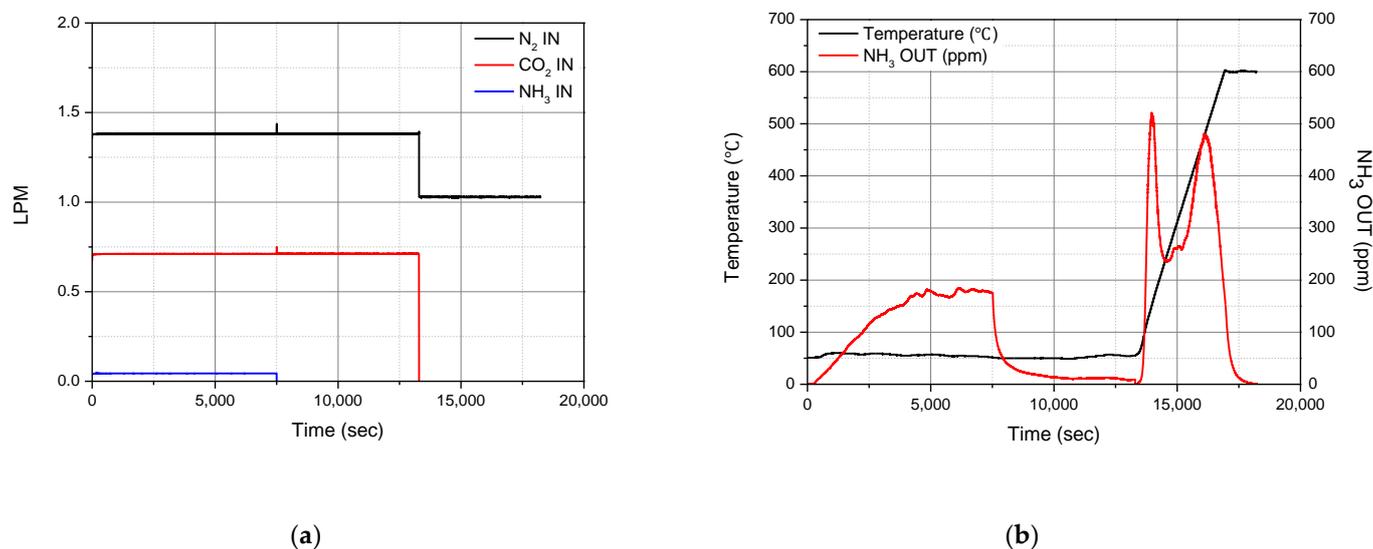
After adsorbing NH<sub>3</sub> to a catalyst at a low temperature, a temperature-programmed desorption (TPD) test was conducted. The experimental conditions are presented in Table 3. The NH<sub>3</sub> supply time, NH<sub>3</sub> concentration, and catalyst temperature during the NH<sub>3</sub> adsorption process were considered as the experimental parameters.

**Table 3.** Experimental conditions.

NH <sub>3</sub> Adsorption Process	
NH <sub>3</sub> concentration (ppm)	200
NH <sub>3</sub> supply time (s)	469, 703, 1406, 1875, 2812, 3750, 7500
Catalyst temperature	50, 100, 150
Space velocity (/h)	40,000
NH <sub>3</sub> Desorption Process	
Temperature range (°C)	50–600
Temperature rise time (°C/min)	9
N <sub>2</sub> gas space velocity (/h)	20,000

Before adsorbing NH<sub>3</sub>, N<sub>2</sub> gas was first supplied to the catalyst and the catalyst was heated to 600 °C to remove any existing impurities. After cooling the catalyst, N<sub>2</sub>, CO<sub>2</sub>, and NH<sub>3</sub> gases were supplied to adsorb NH<sub>3</sub> molecules while maintaining a certain temperature. After supplying a pre-determined amount of NH<sub>3</sub>, the NH<sub>3</sub> supply was stopped, but N<sub>2</sub> and CO<sub>2</sub> were continuously supplied to remove physically adsorbed NH<sub>3</sub> molecules from the catalyst. After that, the catalyst was heated to 600 °C at a rate of 9 °C/min. During the heat-up process, the concentration of NH<sub>3</sub> desorbed from the catalyst

was measured using FT-IR (MKS, Andover, MA, USA). The results shown in this study were the averaged value of three repetitions of the test. The test set-up and procedure used in this study were similar to that already presented by Schiavoni et al. [21] and by Galloni et al. [22]. Figure 13 represents the above mentioned experimental procedure in more detail. It shows the change in the supply amount of various gases and temperature with time. One example of the concentration of  $\text{NH}_3$  gas measured by FT-IR is also shown.



**Figure 13.** Changes in gas supply amount, temperature, and  $\text{NH}_3$  concentration with time, describing the experimental procedure: (a) Gas-feeding amount; (b) temperature and  $\text{NH}_3$  gas concentration.

#### 4. Conclusions

$\text{NH}_3$  adsorption and desorption are important phenomena in  $\text{NH}_3$ -SCR of  $\text{NO}_x$ . Many studies which have tried to control the amount of  $\text{NH}_3$  adsorption and desorption in zeolite catalyst have assumed that it has only one kind of acid site. This simple modeling has limitations, so this study aimed to develop equations of chemical kinetics describing the reaction rates of  $\text{NH}_3$  adsorption and desorption in two important acid sites for  $\text{NH}_3$ -SCR. The following conclusions were obtained:

1. Physically adsorbed  $\text{NH}_3$  molecules are weakly bound to the zeolite surface, not to the acid site, and do not appear to have a significant effect on the  $\text{NO}_x$  SCR reaction. Therefore, the effect of physically adsorbed  $\text{NH}_3$  was excluded in this study.
2. The adsorption and desorption rates of the LT peak cannot be expressed with the  $\text{NH}_3$  coverage ratio of the catalyst. The saturation of the LT peak cannot be confirmed because of solvation of ammonium ions by  $\text{NH}_3$  molecules.
3. The adsorption rate of the HT peak can be expressed as a conventional linear function. The adsorption rates of the HT peak can be described as Equation (6).
4. However, it is not easy to express the rate of  $\text{NH}_3$  adsorption of the IT peak because it is affected by the acid sites of the HT peak and interaction with  $\text{NH}_3$  molecules of the LT peak. In this study, it was found that the rate of  $\text{NH}_3$  adsorption of the IT peak can be expressed by Equation (7) when there is no influence of the acid sites of the HT peak and interaction with the  $\text{NH}_3$  molecules of the LT peak.
5. The desorption rates of  $\text{NH}_3$  molecules of the HT peak and IT peak can be described as Equations (8) and (9). The averaged chemical kinetics parameters describing  $\text{NH}_3$  desorption rates for both the IT and HT peaks were determined.

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supervision, H.K.; project administration, H.K.; funding acquisition, H.K. All authors have read and agreed to the published version of the manuscript.

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