

*Supplementary Materials*

*for*

**Computational Insight into Defective Boron Nitride Supported  
Double-Atom Catalysts for Electrochemical Nitrogen Reduction**

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**Table S1.** Computed cohesive energy ( $E_{\text{coh}}$ ) and adsorption energy ( $E_{\text{a}}$ ) of TM dimer (TM= Ti, Fe, Mo and Ru) anchored on the B-vacancy.

	$E_{\text{coh/TM1}}$	$E_{\text{coh/TM2}}$	$E_{\text{ads}}$	$E_{\text{coh}}$	$E_{\text{ads}}-E_{\text{coh}}$	$E_{\text{f}}$
<b>Fe-Fe</b>	-4.86	-4.86	-10.88	-4.86	-0.58	-1.18
<b>Fe-Mo</b>	-4.86	-6.29	-11.45	-5.58	-0.15	-1.15
<b>Fe-Ru</b>	-4.86	-6.76	-12.02	-5.81	-0.20	-1.15
<b>Fe-Ti</b>	-4.86	-5.45	-12.71	-5.16	-1.20	-1.20
<b>Mo-Mo</b>	-6.29	-6.29	-12.62	-6.29	-0.02	-1.10
<b>Mo-Ru</b>	-6.29	-6.76	-13.25	-6.53	-0.10	-1.12
<b>Mo-Ti</b>	-6.29	-5.45	-12.30	-5.87	-0.28	-1.16
<b>Ru-Ru</b>	-6.76	-6.76	-13.76	-6.76	-0.12	-1.12
<b>Ru-Ti</b>	-6.76	-5.45	-13.67	-6.11	-0.73	-1.18
<b>Ti-Ti</b>	-5.45	-5.45	-14.12	-5.45	-1.61	-1.22

**Table S2.** Calculated the amount of the transferred electrons from the anchored TM atoms to the  $V_{\text{B}}\text{-BN}$  ( $Q$  in  $e$ ) of  $\text{TM}_1\text{-TM}_2@V_{\text{B}}\text{-BN}$ .

	$Q$
<b>Fe-Fe</b>	1.61
<b>Fe-Mo</b>	1.54
<b>Fe-Ru</b>	1.53
<b>Fe-Ti</b>	1.75
<b>Mo-Mo</b>	1.59
<b>Mo-Ru</b>	1.53
<b>Mo-Ti</b>	1.77
<b>Ru-Ru</b>	1.15
<b>Ru-Ti</b>	1.71
<b>Ti-Ti</b>	1.97

**Table S3.** Calculated bond lengths of adsorbed  $^*\text{N}_2$  ( $d_{\text{N-N}}$  in Å) and the amount of charge that  $^*\text{N}_2$  gained from the  $\text{TM}_1\text{-TM}_2@V_{\text{B}}\text{-BN}$  catalysts ( $Q$  in  $e$ ).

	$Q/\text{end-on}$	$d_{\text{N-N}}/\text{end-on}$	$Q/\text{side-on}$	$d_{\text{N-N}}/\text{side-on}$
<b>Fe-Fe</b>	0.35	1.143	0.48	1.180
<b>Fe-Mo</b>	0.43	1.145	0.55	1.189
<b>Fe-Ru</b>	0.41	1.143	0.51	1.184
<b>Fe-Ti</b>	0.41	1.146	0.56	1.190
<b>Mo-Mo</b>	0.48	1.150	0.86	1.263
<b>Mo-Ru</b>	0.52	1.154	0.84	1.255
<b>Mo-Ti</b>	0.52	1.153	0.72	1.230
<b>Ru-Ru</b>	0.39	1.141	0.52	1.195
<b>Ru-Ti</b>	0.41	1.145	0.48	1.179
<b>Ti-Ti</b>	0.53	1.153	0.82	1.220
<b>Ti-Ru</b>	0.48	1.149	0.63	1.210
<b>Ti-Mo</b>	0.50	1.151	0.74	1.230
<b>Ti-Fe</b>	0.51	1.152	0.72	1.220
<b>Ru-Mo</b>	0.39	1.145	0.52	1.194
<b>Ru-Fe</b>	0.39	1.144	0.46	1.180
<b>Mo-Fe</b>	0.52	1.154	0.84	1.253

**Table S4:** Calculated free energy changes of the first hydrogenation step ( $\Delta G^{*N_2 \rightarrow *N_2H}$ ) and the last hydrogenation step ( $\Delta G^{*NH_2 \rightarrow *NH_3}$ ) for 16 TM<sub>1</sub>-TM<sub>2</sub>@V<sub>B</sub>-BN catalysts. "/" indicates that TM atoms cannot adsorb intermediate  $*N_2H$ .

	Fe-Fe	Fe-Mo	Fe-Ru	Fe-Ti	Mo-Mo	Mo-Ru	Mo-Ti	Ru-Ru
$*N_2 \rightarrow *N_2H/e$	0.94	0.91	1.10	0.81	0.38	0.29	/	0.54
$*N_2 \rightarrow *N_2H/s$	-	1.1	0.80	0.99	0.52	-0.25	0.15	0.58
$*NH_2 \rightarrow *NH_3$	0.32	0.24	0.23	0.29	0.80	0.63	1.00	0.14

	Ru-Ti	Ti-Ti	Ti-Ru	Ti-Mo	Ti-Fe	Ru-Mo	Ru-Fe	Mo-Fe
$*N_2 \rightarrow *N_2H/e$	0.53	0.45	-	-	-0.22	0.47	0.93	/
$*N_2 \rightarrow *N_2H/s$	0.40	0.28	0.27	0.24	0.23	0.53	/	0.26
$*NH_2 \rightarrow *NH_3$	-0.08	1.03	1.02	1.16	1.00	0.05	0.22	1.10

**Table S5:** The magnetic moments( $M_{\mu B}$ ) of TMs in TM<sub>1</sub>-TM<sub>2</sub>@V<sub>B</sub>-BN catalysts.

	$M_1(Ru)$	$M_2(Mo/Ru/Ti)$
<b>Ru-Mo@V<sub>B</sub>-BN</b>	1.548	2.250
<b>Ru-Ru@V<sub>B</sub>-BN</b>	1.079	1.044
<b>Ru-Ti@V<sub>B</sub>-BN</b>	1.595	0.422

**Table S6:** The Gibbs free energies changes for each intermediate on Ru-Mo@V<sub>B</sub>-BN via distal, alternating and enzymatic mechanisms at 298.15 K (in eV).

Ru-Mo (Distal)	$\Delta G(eV)$
$*+ N_2 \rightarrow *N_2$	-1.05
$*N_2+H^++e^- \rightarrow *N_2H$	0.47
$*N_2H+H^++e^- \rightarrow *N_2H_2$	-0.06
$*N_2H_2+H^++e^- \rightarrow *N+NH_3$	-0.48
$*N_2+H^++e^- \rightarrow *NH$	-0.26
$*NH+H^++e^- \rightarrow *NH_2$	-0.24
$*NH_2+H^++e^- \rightarrow *NH_3$	0.05

Ru-Mo (Alternating)	$\Delta G(eV)$
$*+ N_2 \rightarrow *N_2$	-1.05
$*N_2+H^++e^- \rightarrow *NNH$	0.47
$*NNH+H^++e^- \rightarrow *NHNH$	0.92
$*NHNH+H^++e^- \rightarrow *NHNH_2$	-0.43
$*NHNH_2+H^++e^- \rightarrow *NH_2NH_2$	-1.01
$*NH_2NH_2+H^++e^- \rightarrow *NH_2+NH_3$	-0.52
$*NH_2+H^++e^- \rightarrow *NH_3$	0.05

Ru-Mo (Enzymatic)	$\Delta G(eV)$
$*+ N_2 \rightarrow *N_2$	-0.70
$*N_2+H^++e^- \rightarrow *NNH$	0.53
$*NNH+H^++e^- \rightarrow *NHNH$	0.07
$*NHNH+H^++e^- \rightarrow *NHNH_2$	-0.32
$*NHNH_2+H^++e^- \rightarrow *NH_2NH_2$	-1.13
$*NH_2NH_2+H^++e^- \rightarrow *NH_2+NH_3$	-0.10
$*NH_2+H^++e^- \rightarrow *NH_3$	0.09

**Table S7:** Computed vibrational frequencies, zero-point energies and entropy of reaction intermediates on Ru-Mo@V<sub>B</sub>-BN, where \* denotes the adsorption site.

Reaction Intermediates	Vibrational Frequencies (cm <sup>-1</sup> )						ZPE (eV)	TS (eV)
*N <sub>2</sub>	2107.12	417.67	406.77	398.43	62.59	47.39	0.21	0.15
*N <sub>2</sub> H	3233.30	1685.80	1107.83	534.11	436.35	397.75	0.49	0.16
	390.32	45.58	27.81					
*N <sub>2</sub> H <sub>2</sub>	3512.72	3346.95	1552.70	1321.20	1180.83	608.77	0.81	0.17
	459.51	364.69	357.16	298.08	84.51	49.29		
*NHNH	3363.45	3241.89	1327.46	1118.70	1024.25	823.28	0.79	0.15
	667.11	454.15	388.08	207.47	99.80	89.12		
*N	1043.11	123.60	118.88				0.08	0.08
*NH	3277.22	859.21	672.44	626.26	112.18	105.81	0.35	0.10
*NH <sub>2</sub>	3464.65	3380.44	1512.27	640.43	634.89	585.07	0.67	0.13
	460.58	118.53	44.05					
*NH <sub>3</sub>	3491.58	3482.26	3389.81	1608.27	1601.25	1140.12	1.01	0.13
	546.92	509.10	336.12	99.85	60.85	36.32		
*NHNH <sub>2</sub>	3450.19	3363.38	3353.46	1577.09	1339.37	1081.41	1.15	0.18
	1018.78	901.47	670.18	624.36	451.54	409.33		
	138.65	94.69	57.53					
*NH <sub>2</sub> NH <sub>2</sub>	3479.48	3477.35	3385.93	3383.53	1499.78	1493.69	1.31	0.20
	748.18	745.28	598.92	544.45	526.22	414.91		
	311.43	191.88	128.77	119.81	102.29	48.75		
*H	1999.04	610.06	570.74				0.20	0.02

**Table S8:** The Gibbs free energies changes for each intermediate on Ru-Ru@V<sub>B</sub>-BN via distal, alternating and enzymatic mechanisms at 298.15 K (in eV).

Ru-Ru (Distal)	ΔG(eV)
*+ N <sub>2</sub> →*N <sub>2</sub>	-1.12
*N <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*N <sub>2</sub> H	0.54
*N <sub>2</sub> H+H <sup>+</sup> +e <sup>-</sup> →*N <sub>2</sub> H <sub>2</sub>	0.31
*N <sub>2</sub> H <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*N+NH <sub>3</sub>	-1.26
*N <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NH	0.31
*NH+H <sup>+</sup> +e <sup>-</sup> →*NH <sub>2</sub>	-0.56
*NH <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NH <sub>3</sub>	0.14
Ru-Ru (Alternating)	ΔG(eV)
*+ N <sub>2</sub> →*N <sub>2</sub>	-1.12
*N <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NNH	0.54
*NNH+H <sup>+</sup> +e <sup>-</sup> →*NHNH	0.59
*NHNH+H <sup>+</sup> +e <sup>-</sup> →*NHNH <sub>2</sub>	-0.08
*NHNH <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NH <sub>2</sub> NH <sub>2</sub>	0.39
*NH <sub>2</sub> NH <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NH <sub>2</sub> +NH <sub>3</sub>	-2.10
*NH <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NH <sub>3</sub>	0.14
Ru-Ru (Enzymatic)	ΔG(eV)
*+ N <sub>2</sub> →*N <sub>2</sub>	-0.68
*N <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NNH	0.58

$*NNH+H^++e^- \rightarrow *NHNH$	-0.04
$*NHNH+H^++e^- \rightarrow *NHNH_2$	-0.26
$*NHNH_2+H^++e^- \rightarrow *NH_2NH_2$	0.82
$*NH_2NH_2+H^++e^- \rightarrow *NH_2+NH_3$	-2.20
$*NH_2+H^++e^- \rightarrow *NH_3$	0.14

**Table S9:** Computed vibrational frequencies, zero-point energies and entropy of reaction intermediates on Ru-Ru@V<sub>B</sub>-BN, where \* denotes the adsorption site.

Reaction Intermediates	Vibrational Frequencies (cm <sup>-1</sup> )						ZPE (eV)	TS (eV)
*N <sub>2</sub>	2120.32	381.68	316.86	314.88	41.68	29.24	0.20	0.18
*N <sub>2</sub> H	3238.89	1396.32	1136.18	591.75	468.09	370.16	0.47	0.17
	208.62	79.32	52.73					
*N <sub>2</sub> H <sub>2</sub>	3490.15	3359.23	1567.99	1312.66	1170.58	553.60	0.79	0.21
	422.11	305.33	279.11	230.75	31.05	13.20		
*NHNH	3290.06	3250.63	1378.05	1147.33	1015.21	901.94	0.81	0.15
	732.07	534.86	433.14	194.44	98.44	91.07		
*N	1078.67	134.44	131.53				0.08	0.08
*NH	3341.41	840.12	441.65	296.04	105.60	103.52	0.32	0.12
*NH <sub>2</sub>	3493.43	3398.43	1506.55	673.68	591.49	493.03	0.66	0.14
	332.02	103.50	44.74					
*NH <sub>3</sub>	3477.26	3475.56	3383.58	1602.96	1601.68	1143.19	1.01	0.19
	535.45	534.07	354.81	132.27	48.39	42.53		
*NHNH <sub>2</sub>	3448.34	3358.66	3351.79	1583.77	1332.65	1086.24	1.14	0.17
	1014.74	896.92	666.04	560.93	451.47	382.40		
	90.82	64.35						
*NH <sub>2</sub> NH <sub>2</sub>	3386.20	3383.03	3306.45	3304.82	1591.83	1571.85	1.47	0.20
	1334.03	1064.12	1051.77	1001.89	932.81	554.61		
	426.11	303.64	284.63	118.83	94.08	76.08		
*H	1822.17	430.87	360.30				0.16	0.03

**Table S10:** The Gibbs free energies changes for each intermediate on Ru-Ti@V<sub>B</sub>-BN via distal, alternating and enzymatic mechanisms at 298.15 K (in eV).

Ru-Ti (Distal)	ΔG(eV)
*+ N <sub>2</sub> →*N <sub>2</sub>	-1.20
*N <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*N <sub>2</sub> H	0.53
*N <sub>2</sub> H+H <sup>+</sup> +e <sup>-</sup> →*N <sub>2</sub> H <sub>2</sub>	0.33
*N <sub>2</sub> H <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*N+NH <sub>3</sub>	-0.67
*N <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NH	-0.19
*NH+H <sup>+</sup> +e <sup>-</sup> →*NH <sub>2</sub>	-0.43
*NH <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NH <sub>3</sub>	-0.08
Ru-Ti (Alternating)	ΔG(eV)
*+ N <sub>2</sub> →*N <sub>2</sub>	-1.20
*N <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NNH	0.53
*NNH+H <sup>+</sup> +e <sup>-</sup> →*NHNH	0.85
*NHNH+H <sup>+</sup> +e <sup>-</sup> →*NHNH <sub>2</sub>	-0.37
*NHNH <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NH <sub>2</sub> NH <sub>2</sub>	-0.75
*NH <sub>2</sub> NH <sub>2</sub> +H <sup>+</sup> +e <sup>-</sup> →*NH <sub>2</sub> +NH <sub>3</sub>	1.45

$*\text{NH}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_3$	-0.08
<hr/>	
<b>Ru-Ti (Enzymatic)</b>	<b><math>\Delta G(\text{eV})</math></b>
$* + \text{N}_2 \rightarrow * \text{N}_2$	-0.89
$* \text{N}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NNH}$	0.40
$* \text{NNH} + \text{H}^+ + \text{e}^- \rightarrow * \text{NHNH}$	0.30
$* \text{NHNH} + \text{H}^+ + \text{e}^- \rightarrow * \text{NHNH}_2$	-0.58
$* \text{NHNH}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_2\text{NH}_2$	-0.97
$* \text{NH}_2\text{NH}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_2 + \text{NH}_3$	0.11
$* \text{NH}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_3$	-0.06

**Table S11:** Computed vibrational frequencies, zero-point energies and entropy of reaction intermediates on Ru-Ti@V<sub>B</sub>-BN, where \* denotes the adsorption site.

Reaction Intermediates	Vibrational Frequencies (cm <sup>-1</sup> )						ZPE (eV)	TS (eV)
*N <sub>2</sub>	1866.94	456.23	346.86	182.48	69.03	64.36	0.19	0.16
*N <sub>2</sub> H	3226.17	1693.91	1112.10	533.82	473.61	414.45	0.49	0.17
	386.53	50.50	41.79					
*N <sub>2</sub> H <sub>2</sub>	3474.90	3360.86	1556.31	1243.89	1161.16	586.85	0.79	0.15
	554.95	372.39	371.79	106.06	31.91	45.35		
*NHNH	3262.46	3234.06	1490.72	1368.86	1274.10	1046.76	0.82	0.20
	553.94	487.70	298.14	117.70	57.15	40.99		
*N	1036.61	149.83	137.31				0.08	0.07
*NH	3191.15	850.46	639.47	633.04	51.74	45.34	0.34	0.14
*NH <sub>2</sub>	3457.87	3373.42	1517.11	663.21	649.58	578.04	0.68	0.13
	489.40	128.18	58.95					
*NH <sub>3</sub>	3473.71	3455.43	3365.88	1613.83	1597.40	1156.67	1.02	0.16
	603.15	567.83	357.82	120.71	107.01	74.60		
*NHNH <sub>2</sub>	3483.88	3355.74	3320.19	1588.52	1428.92	1165.03	1.14	0.20
	1090.56	783.59	683.60	534.50	337.48	294.68		
	184.80	68.32	21.86					
*NH <sub>2</sub> NH <sub>2</sub>	3514.43	3371.47	3331.33	1952.63	1582.64	1452.44	1.37	0.18
	1191.06	1113.59	803.51	782.77	745.19	669.31		
	572.87	367.52	318.96	232.44	91.35	71.56		
*H	1930.02	631.48	534.22				0.19	0.01

**Table S12:** Charge variations of Ru-Ti dimer, V<sub>B</sub>-BN substrate and N<sub>x</sub>H<sub>y</sub> species on Ru-Ti@V<sub>B</sub>-BN.

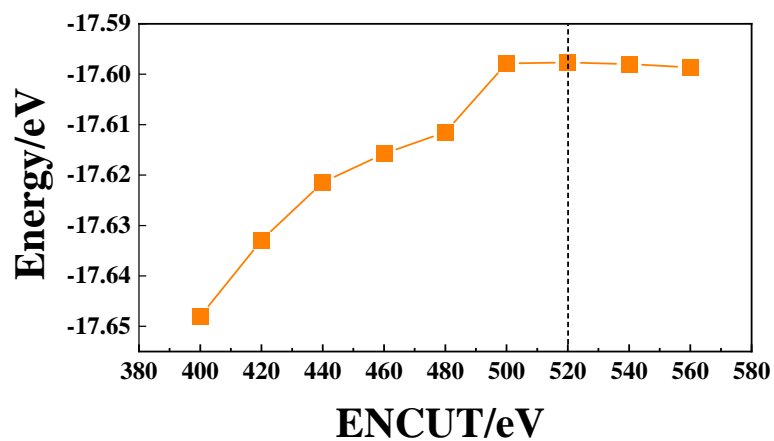
	Ru-Ti	Substrate	N <sub>x</sub> H <sub>y</sub>
<b>Slab</b>	1.71	-1.71	0.00
*N <sub>2</sub>	2.10	-1.62	-0.48
*N <sub>2</sub> H	2.10	-1.68	-0.42
*NHNH	2.19	-1.64	-0.55
*NH <sub>2</sub> NH	2.01	-1.79	-0.22
*NH <sub>2</sub> NH <sub>2</sub>	2.37	-1.61	-0.76
*NH <sub>2</sub>	2.00	-1.66	-0.34
*NH <sub>3</sub>	1.70	-1.83	0.12

**Table S13:** Bond lengths of Ru-Ti, N-N and Ru-N on Ru-Ti@V<sub>B</sub>-BN.

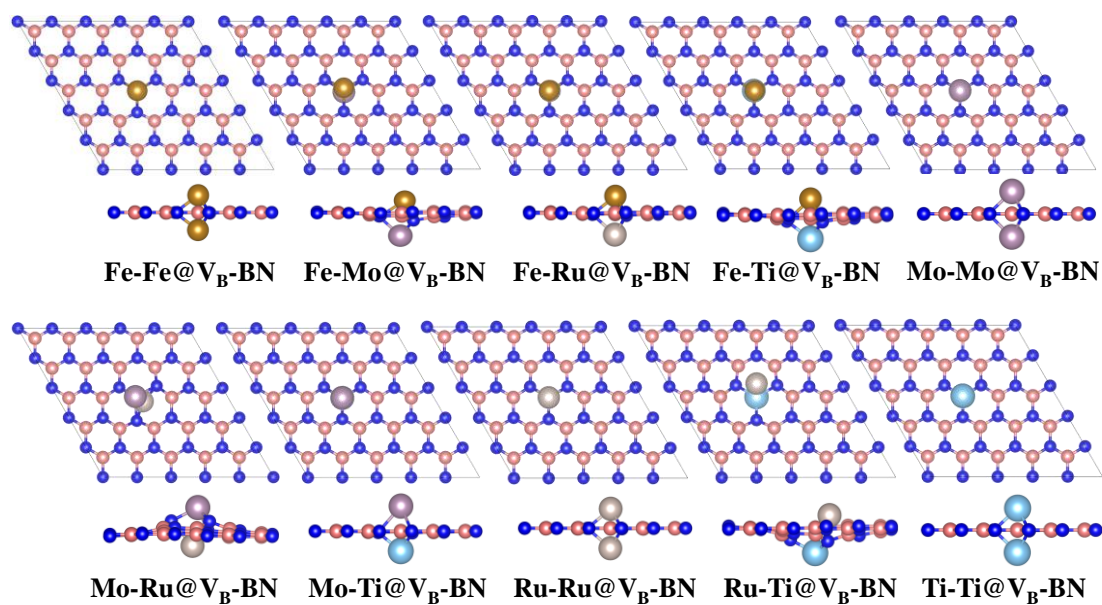
	Ru-Ti	N-N	Ru-N
<b>slab</b>	2.66	-	-
*N <sub>2</sub>	2.54	1.17	2.04
*N <sub>2</sub> H	2.46	1.25	1.93
*NHNH	2.53	1.38	2.00
*NH <sub>2</sub> NH	2.36	1.42	2.03
*NH <sub>2</sub> NH <sub>2</sub>	2.54	3.03	1.96
*NH <sub>2</sub>	2.90	-	1.90
*NH <sub>3</sub>	2.82	-	2.17

**Table S14:** The calculated total energies (Energy-DFT), zero-points energy (ZPE) and entropy corrections (TS), in eV, for the gas phase N<sub>2</sub>, H<sub>2</sub>, NH<sub>3</sub> species of NRR (T = 298.15 K, P = 1 bar). In comparison, the experimental entropies (TS<sub>exp</sub>) of the gas phase N<sub>2</sub>, H<sub>2</sub>, NH<sub>3</sub> species are also shown, which are from NIST standard reference database.

Species	Energy-DFT	ZPE	TS	Gibbs	TS <sub>exp</sub>
H <sub>2</sub> (g)	-6.77	0.27	0.40	-6.90	0.41
N <sub>2</sub> (g)	-16.64	0.15	0.59	-17.08	0.59
NH <sub>3</sub> (g)	-19.54	0.91	0.60	-19.23	0.60

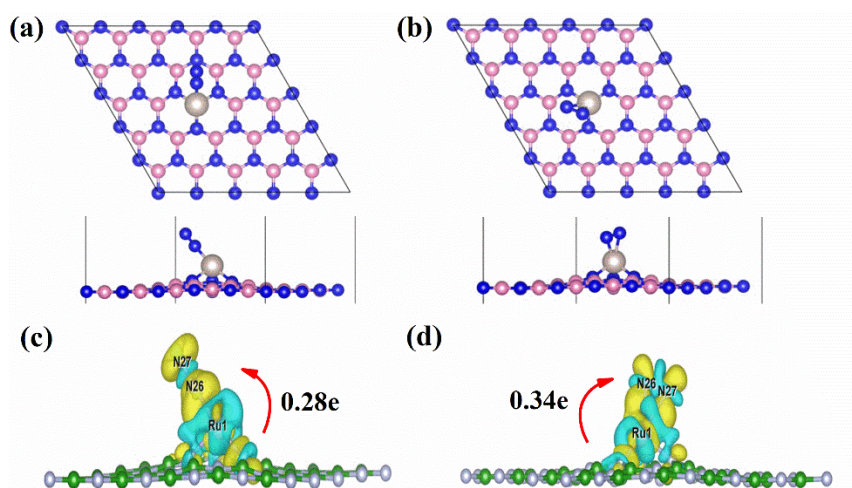


**Figure S1.** Convergence test on the ENCUT value for the BN primitive cell.

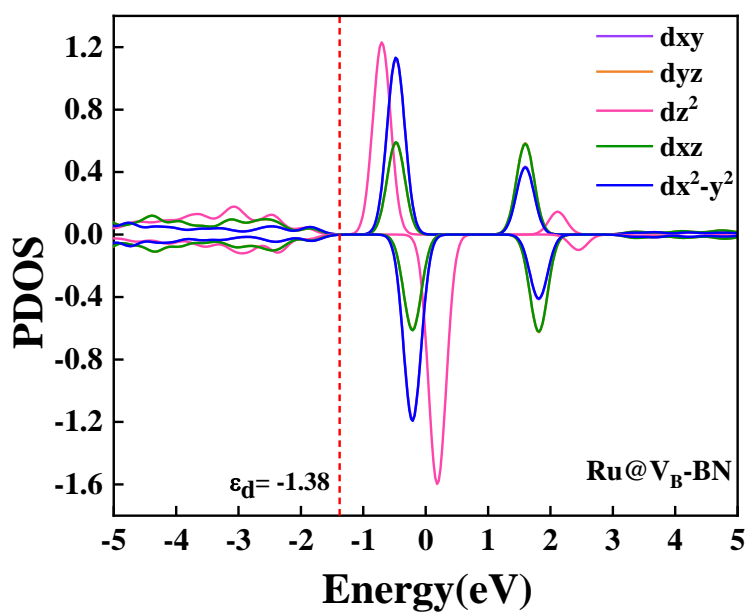


**Figure S2.** Schematic diagrams of the fully relaxed structures of TM<sub>1</sub>-TM<sub>2</sub>@V<sub>B</sub>-BN (TM=Fe, Mo, Ru and Ti).

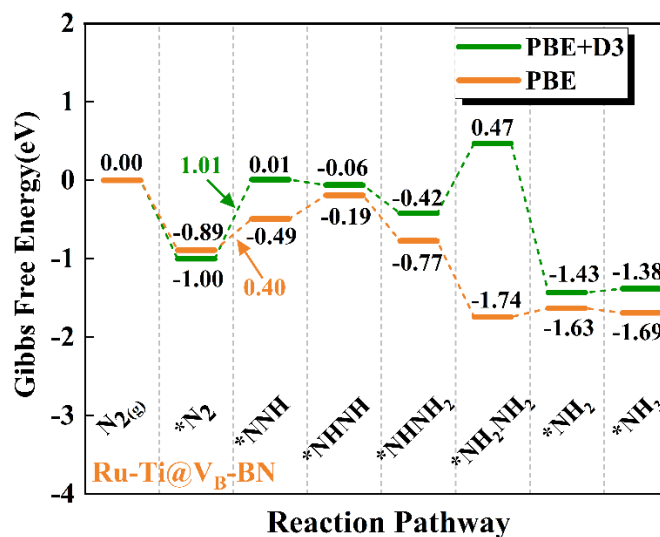




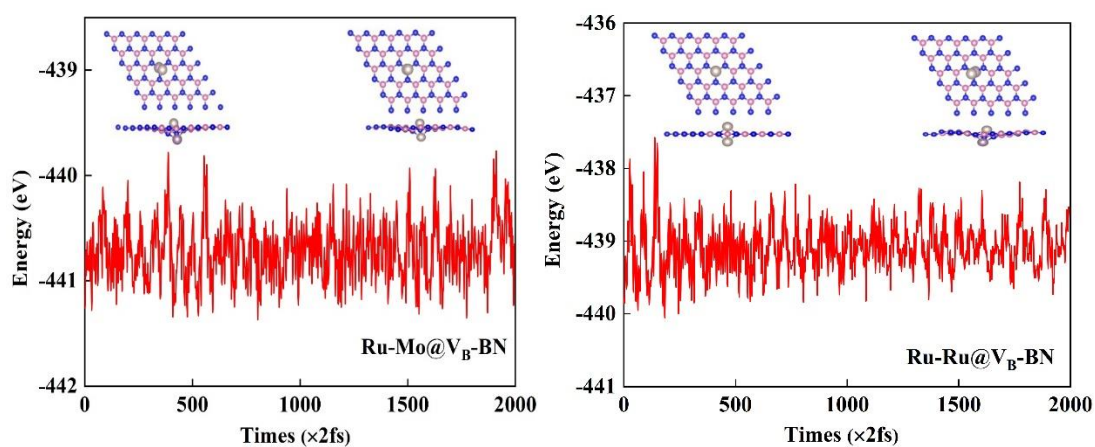
**Figure S3.** Top and side views of N<sub>2</sub> molecule adsorbed on a single Ru atom in (a) end-on and (b) side-on configuration, respectively. Change density differences of N<sub>2</sub> adsorption on Ru@V<sub>B</sub>-BN monolayer for (c) end-on and (d) side-on configurations.



**Figure S4.** Projected density of states (PDOS) of Ru *d* orbitals in Ru@V<sub>B</sub>-BN. The red dotted line represents the position of the *d*-band center.



**Figure S5.** Gibbs free energy diagram for  $N_2$  electroreduction on Ru-Ti@V<sub>B</sub>-BN with and without consideration of vdW interaction.



**Figure S6.** Variations of the total energy against the time for the AIMD simulation for Ru-Mo@V<sub>B</sub>-BN and Ru-Ru@V<sub>B</sub>-BN under 400K.