

# Supplementary Information: 3-Dimensional Plasmonic Substrates Based on Chicken Eggshell Bio-Templates for SERS Based Bio-Sensing

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## I. Finite difference time domain (FDTD) method.

FDTD method solves Faraday's law and Ampere's law, Equations 1 and 2, in differential form over a grid-based domain (where field components are defined only at the grid points) using Taylor expansions for the derivatives.

$$\frac{\epsilon \partial \mathbf{E}}{\partial t} = \nabla \times \mathbf{H} - \mathbf{J} \quad (1)$$

$$\frac{\epsilon \partial \mathbf{H}}{\partial t} = \nabla \times \mathbf{E} \quad (2)$$

The most popular discretization is based on Yee's algorithm and computes the E (electric field) and H (magnetic field) components at half grid points relative to each other and central spatial and leapfrog time differences are used for the derivatives [1]. A simple version of this can be generated for a 2D system in which the electric field only has x and y components, and the magnetic field has a z component. If the time step is denoted by  $\tau$ , then the following equations are used:

$$E_x^{n+1/2} = E_x^{n-1/2} + \frac{\tau}{\epsilon} \left( \frac{\partial H_z^n}{\partial y} - J_x^n \right) \quad (3)$$

$$E_y^{n+1/2} = E_y^{n-1/2} + \frac{\tau}{\epsilon} \left( \frac{\partial H_z^n}{\partial x} - J_y^n \right) \quad (4)$$

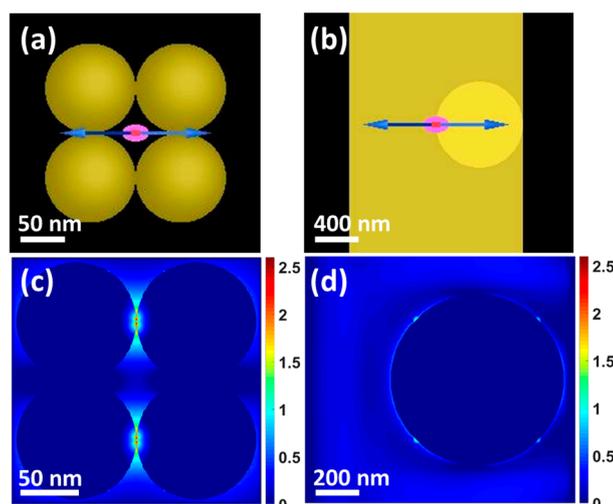
$$H_z^{n+1} = H_z^n + \frac{\tau}{\mu} \left( \frac{\partial E_y^{n+1/2}}{\partial x} - \frac{\partial E_x^{n+1/2}}{\partial y} \right) \quad (5)$$

## II. FDTD simulation setup.

The FDTD simulation domain was  $1.6 \mu\text{m} \times 1.6 \mu\text{m} \times 1.6 \mu\text{m}$  and  $6 \mu\text{m} \times 6 \mu\text{m} \times 6 \mu\text{m}$  for OS and SM, respectively. Perfectly matched layers (PMLs) were used on all the boundaries. However, anti-symmetric and symmetric boundary conditions were used for x-min and y-min for OS simulation. The effect of staircase approximation was addressed by reducing the mesh size around the features to  $2 \text{ nm} \times 2 \text{ nm} \times 2 \text{ nm}$ . The simulations were performed on a computer with 8-core calculation nodes, each carrying 4 GB memory. Gold dielectric constants were obtained from the literature [2].

## III. Calculated electric field (E-field) distributions.

Figure S1 presents the calculated E-field distributions for the representative OS and SM architectures. Figure S1a depicts 4 Au nanospheres (100 nm diameter) touching each other with an in-between empty space of dimension 100 nm (along the E-field direction). Figure S1b shows the characteristic SM architecture, where a  $0.8 \mu\text{m}$  diameter Au disk (corresponds to knobs) is sitting on an infinite Au fiber of diameter  $1.5 \mu\text{m}$ .



**Figure S1.** Representative (a) OS and (b) SM architectures. Calculated E-field distribution for (c) OS and (d) SM architectures. The incident wavelength is 785 nm.

As shown in Figure S1c and S1d, the E-field enhancement is larger for the aggregated nanospheres than that for the disk/fiber architecture. This qualitatively defends the better SERS performance of OS/IS region than the SM.

#### IV. Calculation of SERS enhancement factor (EF).

SERS EF is estimated according to the references 3 and 4 by comparing the  $1575\text{ cm}^{-1}$  peak in the SERS spectrum to the  $1585\text{ cm}^{-1}$  peak in normal Raman spectrum of the benzenethiol (BT) [3,4]. The EF can be written as

$$EF = \left( \frac{I_{\text{SERS}}}{I_{\text{normal}}} \right) \times \left( \frac{C_{\text{normal}}}{C_{\text{SERS}}} \right) \quad (6)$$

Here,  $I_{\text{SERS}}$  and  $I_{\text{normal}}$  represent the normalized (to power and integration time) count rates of the SERS and normal Raman signal, respectively. To obtain  $I_{\text{normal}}$ , BT is drop-casted on bare OS, IS, and SM regions without any Au coating.  $C_{\text{SERS}}$  and  $C_{\text{normal}}$  are the concentrations of the BT molecules in the SERS and normal Raman measurements. Table S1 enlists the calculated EF values for OS, IS, and SM regions.

**Table S1.** Calculation of SERS EF for egg OS, IS, and SM regions.

Region	$C_{\text{normal}}$ (M)	Sample Power (mW)	Integration Time (s)	$I_{\text{normal}}$ (photons $\text{s}^{-1} \text{mW}^{-1}$ )	EF
OS	$4 \times 10^{-2}$	50	30	90	$2.6 \times 10^6$
IS	$4 \times 10^{-2}$	50	30	86	$1.8 \times 10^6$
SM	$4 \times 10^{-1}$	15	30	1040	$1.5 \times 10^5$

#### References

1. Yee, K. Numerical solution of initial boundary value problems involving maxwell's equations in isotropic media. *IEEE Trans. Antennas* **1966**, *14*, 302–307.
2. Johnson, P.B.; Christy, R.-W. Optical constants of the noble metals. *Phys. Rev. B* **1972**, *6*, 4370.
3. Chen, J.; Su, H.; You, X.; Gao, J.; Lau, W.M.; Zhang, D. 3D  $\text{TiO}_2$  submicrostructures decorated by silver nanoparticles as SERS substrate for organic pollutants detection and degradation. *Mater. Res. Bull.* **2014**, *49*, 560–565.
4. Lin, P.Y.; Hsieh, C.W.; Tsai, P.C.; Hsieh, S. Porosity-controlled eggshell membrane as 3D SERS-active substrate. *ChemPhysChem* **2014**, *15*, 1577–1580.