



# Article Multi-Ion-Based Modelling and Experimental Investigations on Consistent and High-Throughput Generation of a Micro Cavity Array by Mask Electrolyte Jet Machining

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**Abstract:** The controllability and consistency in the fabrication of micro-textures on large-scale remains a challenge for existing production processes. Mask electrolyte jet machining (MEJM) is an alternative to Jet-ECM for controllable and high-throughput surface microfabrication with more consistency of dimensional tolerances. This hybrid configuration combines the high-throughput of masked-ECM and the adjustable flow-field of jet-ECM. In this work, a duckbill jet nozzle was introduced to make MEJM more capable of batch micro-structuring. A multiphysics model was built to simulate the distribution of electrochemical reaction ions, the current density distribution, and the evolution of the shape of the machined cavity. Experimental investigations are presented showing the influence of the machining voltage and nozzle moving speed on the micro cavity. Several 35 × 35 micro cavity arrays with a diameter of 11.73–24.92  $\mu$ m and depth of 7.24–15.86  $\mu$ m are generated on 304 stainless steel.

Keywords: micro surface structures; mask electrolyte jet machining; electrochemical micro machining

# 1. Introduction

Micro cavity arrays, as a typical surface microstructure, are broadly applied for heat exchangers [1,2], friction and wear [3], anti-fouling [4,5], etc. Recently, it has been reported that cutting tools [6,7] textured with micro cavities could reduce the cutting force, average friction coefficient, and cutting tool wear, which is useful for machining difficult-to-machine materials. Currently, several technologies have been introduced to manufacture micro cavities on metallic surfaces, such as femtosecond laser micromachining [8], micro-milling [9] and micro-electrical discharge machining [10].

Compared to the aforementioned methods, electrochemical micromachining (EMM) [11] is a promising method for preparing micro cavities [12], as it has unique advantages such as a good control on cavity profile, the potential for multi-response optimization [13], independence of material hardness [14] and toughness [15], absence of a heat-affected layer, lack of process related tool wear and burrs, and a high-throughput capability. Through-mask electrochemical micromachining (TMEMM) is a promising method for generating array-like surface microstructures. In this method, the workpiece surface is covered by a patterned mask, and the machining region is exposed. Subsequent electrochemical micromachining dissolves the exposed area to create the surface texture. With this method, several kinds of surface textures can be prepared, such as micro cavity arrays and micro groove arrays [16]. Wang et al. [17] reported fabrication of a micro cavity array with a diameter of 40  $\mu$ m on a metallic cylindrical surface by using TMEMM. In the work of



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**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). Qu et al. [18], a dry-film photoresist was used as a mask during through-mask electrochemical micromachining to successfully fabricate micro cavity arrays (each cavity about 94  $\mu$ m in diameter and 22.7  $\mu$ m deep) on inner cylindrical surfaces. Qu [19] proposed a modified micro-scale pattern transfer without involving photolithography of substrates. In their work, a through movable dry-film mask electrochemical micromachining was employed for fabrication of micro cavities of 109.4  $\mu$ m in diameter and 15.1  $\mu$ m in depth.

Besides the aforementioned masked-ECM methods, Jet electrochemical machining (Jet-ECM) has also been shown to be an effective approach for generating deep micro cavities [20]. The unique characteristic of this technology is that the electrolyte is ejected from the metallic nozzle to the workpiece with high velocity, which is helpful for preparing deep micro cavities as the electrolyte in the micro cavity can be renewed rapidly [21]. Jet-ECM has been used to fabricate micro-grooves and micro cavities, showing that it is a flexible method [22]. Hackert et al. [23] employed Jet-ECM for generating micro cavities by using a metallic nozzle with an inner diameter of 100  $\mu$ m. As the depth increased from 37  $\mu$ m to 90  $\mu$ m, the diameter of the micro cavity was enlarged from 173  $\mu$ m to 220  $\mu$ m, and the machining localization was reduced. Because the workpiece surface is exposed to jet without side insulation, it often leads to undercutting and stray corrosion at the edge of the micro cavity, and the phenomenon is worsening with an increase in depth, which reduces the machining accuracy and surface quality. Yan [24] presented a reciprocating electrolyte jet machining technology with prefabricated mask (REJP) which was used to generate a circular cavity array of about 43  $\mu$ m in depth and 822  $\mu$ m in diameter on a cast-iron cylinder liner.

These aforementioned methods exhibit a rather low machining efficiency and do not meet the requirements of mass-fabrication of micro cavity like micro-structures. For efficient electrochemical machining of micro cavity array structures, enhanced electrolyte renewal can be helpful for machining high aspect ratio cavities, and reducing the undercutting can improve the machining localization. Mask electrolyte jet machining (MEJM) is an alternative to Jet-ECM/TMEMM for surface microfabrication with more consistency of dimensional variation [25,26]. MEJM is a hybrid configuration which combines the advantages of through-mask electrochemical machining, which is a high-throughput process, and of jet electrochemical machining, with its adjustable flow field.

In the present work, a duckbill jet nozzle is introduced to make MEJM more capable of batch micro-structuring. A multiphysics model is developed to simulate the electric field distribution and micro cavity forming process of the electrolyte. Experimental investigations regarding the influences of machining voltage and nozzle moving speed on the micro cavity are presented. Optimization of the experimental parameters is performed. Finally, the efficient machining of a large number of micro cavities on a stainless-steel plate is demonstrated.

# 2. Process Principle and Theoretical Analysis

## 2.1. Process Principle

The schematic view of MEJM using a duckbill nozzle is shown in Figure 1a. During the machining process, the high-speed electrolyte is sprayed from the metallic nozzle and the nozzle scans on the workpiece. Meanwhile, the high-speed electrolyte flow reaches the exposed workpiece through the micro holes in the mask. Finally, a micro cavity array can be generated when a sufficient voltage is applied between the metallic nozzle and the workpiece. More specifically, a metallic nozzle was employed to provide a stable and high-speed jet flow for workpiece and the renewal of electrolyte in the small machining area, which was useful for generating deep micro cavities. This method is highly flexible and enables machining of large areas.



**Figure 1.** (a) MEJM process schematic view (not to scale). In this work, the lithographic mask array holes are 5  $\mu$ m in diameter. The center–to–center distance of these micro–holes is 50  $\mu$ m, and they are distributed as several 35  $\times$  35 square arrays; (b) The 2D model diagram of MEJM (not to scale); (c) FEM simulation geometry and mesh.

A finite element model (FEM) is developed to investigate the electric field and current density distribution on the workpiece. The profile evolution of the micro cavities can be predicted by this FEM. A 2D diagram of this process configuration is shown in Figure 1b, the geometric and simulation parameters of the model are listed in Table 1.

Table 1. The parameters and initial conditions for the simulation.

| Model Parameters                                      | Value                 |
|---|-----------------------|
| Diameter of the dimple in the mask, $D_0$             | 5 μm                  |
| Thickness of the mask, $T_0$                          | 1.2 μm                |
| Inter-electrode gap, IEG                              | 3.5 mm                |
| Duckbill nozzle slit length,                          | 16 mm                 |
| Duckbill nozzle slit width,                           | 2 mm                  |
| Density of electrolyte, $\rho$                        | $1100  \text{kg/m}^3$ |
| Electrolyte temperature, T                            | 298 K                 |
| Electrolyte conductivity, $\sigma$                    | 10S/m                 |
| Faraday constant, F                                   | 96,486 C/mol          |
| Applied voltage, U                                    | 10 V                  |
| Nozzle moving speed, v                                | 2 mm/s                |
| Molar gas constant, R                                 | 8.314472 J/(K · mol)  |
| Electrolyte pressure                                  | 20 kPa                |
| Initial concentration of Na <sup>+</sup>              | 1 mol/L               |
| Initial concentration of NO <sub>3</sub> <sup>-</sup> | 1 mol/L               |
| Initial concentration of H <sup>+</sup>               | 0 mol/L               |
| Initial concentration of OH <sub>3</sub> <sup>-</sup> | 0 mol/L               |
| Initial concentration of Fe <sup>3+</sup>             | 0 mol/L               |

During machining, the electrolytic products and joule heat will be rapidly removed from the machining area by a high velocity flow of electrolyte. Therefore, the heat effects in the electrochemical reactions do not need to be considered in this case. One of the most significant features of MEJM is the electrolyte flow direction that is changing over time, which refers to a changing concentration gradient in the bulk electrolyte. The current density  $\vec{J}$  in the electrochemical cell can be represented by the ion transportation:

$$\vec{r} = F \sum z_i \vec{N}_i \tag{1}$$

where  $z_i$  is the valence for species *i*, and  $\vec{N}_i$  is the flux of ions which is the result from:

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1 Diffusion:  $\vec{N}_D$ 

$$N_D = -D_i \nabla c_i \tag{2}$$

where  $D_i$  is the diffusion coefficient,  $c_i$  the concentration. Here, H<sup>+</sup>, OH<sup>-</sup>, Na<sup>+</sup>, NO<sub>3</sub> and Fe<sup>3+</sup> were the ions taking part in the electrochemical reactions, the diffusion coefficients are shown in Table 2.

Table 2. Diffusion coefficients at 293.15 K.

| Species <i>i</i>  | Diffusion Coefficient $D_i$ (10 <sup>-9</sup> m <sup>2</sup> /s) |
|-------------------|--|
| Na <sup>+</sup>   | 1.33   |
| NO <sub>3</sub> - | 1.90   |
| $\mathrm{H}^{+}$  | 9.31   |
| OH-               | 5.26   |
| Fe <sup>3+</sup>  | 1.24   |

2 Convection:  $\vec{N}_C$ 

$$N_{\rm C} = \vec{u}c_i \tag{3}$$

where  $\vec{u}$  is the velocity field. In this case, the electrolyte flow rate is considered as laminar flow and can hence be represented by the Navier–Stokes equations:

$$\rho \frac{\partial \vec{u}}{\partial t} + \rho(\vec{u} \cdot \nabla)\vec{u} = -\nabla p + \mu \Delta \vec{u} + \rho \vec{g}$$

$$\frac{\partial \rho}{\partial t} + \rho \nabla \vec{u} = 0$$
(4)

3 Electric migration:  $\vec{N}_E$ 

$$N_E = -\frac{FD_i z_i ci}{RT} \nabla \phi \tag{5}$$

where *F* is the Faraday constant, *R* the ideal gas constant, *T* the temperature and  $\phi$  the electric potential in the interelectrode gap, which can be described by Laplace's equation with a number of certain boundary conditions:

$$\nabla^{2}\phi = \frac{\partial^{2}\phi}{\partial x^{2}} + \frac{\partial^{2}\phi}{\partial y^{2}} = 0$$

$$\phi \mid_{\Gamma_{1}} = 0 \text{ V (Cathode boundaries)}$$

$$\phi \mid_{\Gamma_{2}} = 10 \text{ V (Anode boundaries)}$$

$$\frac{\partial\phi}{\partial \vec{n}} \mid_{\Gamma_{5,6}} = 0 \text{ V (Insulation boundaries)}$$
(6)

where  $\vec{n}$  is the normal phase vector of the boundary.

Therefore, the flux  $\vec{N}_i$  of species in the electrolyte can be given by Equation (7):

$$\vec{N}_{i} = \vec{N}_{D} + \vec{N}_{C} + \vec{N}_{E}$$

$$= -D_{i}\nabla c_{i} + \vec{u}c_{i} - \frac{FD_{i}z_{i}ci}{RT}\nabla\phi$$
(7)

The boundary conditions for the ion transportation are as follows:

• Inflow(inlet):

$$\vec{u} = \vec{u}_0 
c_i = c_{i,0}$$
(8)

• Outflow(outlet):

$$\begin{cases} p = 0\\ \vec{n} \cdot D_i \nabla c_i = 0 \end{cases}$$
(9)

- Open boundary:
  - As no viscous stress is set for the laminar flow, it does not impose any constraint on the pressure:

$$\mu(\nabla \vec{u} + (\nabla \vec{u})^T) \cdot \vec{n} = 0 \tag{10}$$

For the ion transportation:

$$\begin{cases} -\vec{n} \cdot \vec{N}_i = 0, & \vec{n} \cdot \vec{u} \ge 0\\ c_i = c_{i,0}, & \vec{n} \cdot \vec{u} < 0 \end{cases}$$
(11)

• Anode:

$$Fe + 2H_2O \longrightarrow Fe^{3+} + O_2 + 4H^+ + 7e^-$$
(12)

Cathode:

$$2 H_2 O + 2 e^- \longrightarrow H_2 + 2 O H^-$$
(13)

According to Faraday's law, the normal dissolution velocity  $\vec{v_n}$  on the anode boundary can be given by:

$$\vec{v}_n = \eta \frac{M}{zF} \vec{J} \tag{14}$$

where *M* is the molar mass of the workpiece material,  $\eta$  is the coefficient of material removal efficiency weighted by the pulse current and is set to 62.56% in this model.

By solving Equations (2), (3), (5), (6) and (14), the electric field, current density distribution and the material removal process can be calculated.

To make the model applicable, the following simplifying assumptions are made.

- The deformation of the workpiece domain and subsequently the moving boundary is often addressed using the Arbitrary Lagrangian–Eulerian (ALE) finite element technique, in which the "elements" may be modified but cannot be produced or destroyed during the simulation process. To describe the workpiece material removal process that occurs between the workpiece and photoresist mask, however, there must be an interface where the workpiece and photoresist mask may deform in their respective directions, which makes the creation of a gap between them essential. In this work, a virtual gap with 0.1 µm is set between mask and workpiece to ensure the anode boundary to move properly.
- Theoretically, the fabricated micro features will influence the shape of the moving electrolyte jet column. However, it is assumed that, in practice, because of the low moving speed of the nozzle (1–4 mm/s) and the micrometer scale of the features generated, the electrolyte column remains unchanged across the machining process. The bulk electrolyte layer over the workpiece is assumed to be constant because the electrolyte flow pressure is too low (20 kPa) to cause a hydraulic jump associated with the flow pressure used in conventional Jet-ECM (500 kPa). The slit width of the duckbill nozzle in this work is the

same as the diameter of the cylindrical nozzle used in Ref. [25], and the *IEG* is likewise the same. Therefore, the geometry shape of the electrolyte domain from Ref. [25] is used to develope the multiphysics model in this work.

The numerical simulation model is built as shown in Figure 1b,c. The model was built using a free triangular mesh, and the deformed region was refined to improve the calculation accuracy. In this work, the numerical simulations were performed by COMSOL<sup>®</sup> Multiphysics software.

## 2.2. Simulation Results

The profile evolution and corresponding distribution of current density norm, which is the absolute magnitude of the current density vector, on the reaction interface can be seen in Figure 2, the diameter and depth of the machined cavity increased as the electrochemical reaction progressed. Because of the "edge effect" in the electric field, at t = 0 s, the current density norm was slightly higher in the boundary between the photoresist and workpiece than that in the center of micro cavity.



Figure 2. The profile evolution and corresponding current density norm on the reaction interface.

Later in the process, the distribution is inverted, the current density is then always higher in the center than that in the boundary. This will lead to a concave-like profile, i.e., a micro cavity. The detailed simulation results at different machining times (t = 0 s: Figure A1; t = 1 s: Figure A2; t = 2 s: Figure A3; t = 3 s: Figure A4) are provided in Appendix A. As the electrochemical dissolution reaction progressed, the depth of micro cavity increased, causing an increasing distance between the cathode and the anodic area on the workpiece. In the meantime, the distance between the reaction interface and the nozzle, i.e., the cathode, is first reduced and then becomes longer again, the shortest distance between them was at the nozzle moving right above the reaction interface. In the presented simulation, the nozzle was right above the reaction interface at t = 2 s, as shown in Figure A3, and the current density norm reached its peak value and then was reduced.

As shown in Figure 3, the moving nozzle also changes the electrolyte flow direction both around and inside the machined cavity. The variation of the flow field and electric field will cause a variation of the ion distribution. According to Equation (5), positive ions will be repelled and negative ions will be attracted to the reaction interface since it is located at the surface of anode. Significantly more  $OH^-$  than  $H^+$  around the reaction area, which refers to electrochemical reactions occur under an extreme alkaline environment. Similarly, more  $NO_3^-$  than  $Na^+$  ions were present in the reaction area. Due to the water depletion in Equation (12),  $H^+$  ions are produced at the anode surface and contribute to a rising trend of H<sup>+</sup> concentration around the machining area. However, the electric migration caused by the potential gradient not only cancels this increasing concentration trend, but also inverts it into a lowering concentration trend; the concentration of H<sup>+</sup> around the machined cavity is even lower than that of the bulk electrolyte. Since no Na<sup>+</sup> ions are created at the anode surface, the concentration of Na<sup>+</sup> around the machined cavity is even lower than the concentration of  $H^+$ . The produced  $Fe^{3+}$  ions were also expelled from the reaction interface. In the meantime, the neutral byproducts, such as  $Fe(NO_3)_3$  cannot be removed from the reaction area by the electric migration effect. These neural byproducts can be driven out by convection and diffusion. Here, the varying flow field makes the byproducts less prone to accumulate, which is what MEJM envisages.

Pulsed power supplies can reduce stray current corrosion and provide more precise machining than DC power supplies. Due to time step limitations, however, it is impractical to incorporate high-frequency pulsed electric current (2 kHz in the present experimental studies) into a multi-physical model, the cost of computation will be excessive. As a result, a simplification in practice is to build the ECM model with a coefficient ( $\eta$  in Equation (14)) to calculate the material removal rate rather than taking the pulse current into account at each time step [27]. In Figure 4, the profiles of the cavity from simulation and experiment are shown; the experimental processing parameters are identical to those of the simulations, with the exception of the pulse current. For additional information, please refer to Section 3.1) are presented. The shape and depth of the features from the simulation demonstrated a good agreement with that from the experiments. However, the simulated and experimental micro cavity diameters are 12 µm and 16.26 µm, respectively. This indicates that the depth of the micro cavity for experiments is higher than the simulation result. This may be because of the absence of pulsed current in our simulation, which can increase the localization of electrochemical reactions. In this study, a coefficient of material removal efficiency weighted by the pulse current is employed to fine-tune the simulation to match the results. However, only a linear correction is made for the material removal rate using this method. For instance, if the coefficient is increased in this study, the calculated cavity depth will match the real data, but the simulated diameter will expand. Thus, the simulated undercutting is larger than the experimental value. This indicates that a coefficient weighted by the pulse current is insufficient to capture the improvement in machining accuracy driven by the pulse current. Further work will focus on modelling of pulsed current and its effects on the electrical double layer.



**Figure 3.** Simulation results at t = 4 s. (**a**<sub>1</sub>): velocity field of the electrolyte flow; (**b**<sub>1</sub>): velocity field of electrolyte flow in the machined cavity; (**a**<sub>2</sub>) electric potential distribution in the MEJM; (**b**<sub>2</sub>) electric potential distribution (V) in the machined cavity; (**c**<sub>1</sub>) normal current density distribution around the machined cavity; (**d**<sub>1</sub>): normal current density distribution on the reaction interface; (**c**<sub>2</sub>-**c**<sub>6</sub>): concentration (mol/m<sup>3</sup>) of Fe<sup>3+</sup>, H<sup>+</sup>, OH<sup>-</sup>, Na<sup>+</sup>, and NO<sub>3</sub><sup>-</sup> around the machined cavity; (**d**<sub>2</sub>-**d**<sub>6</sub>): concentration (mol/m<sup>3</sup>) of Fe<sup>3+</sup>, H<sup>+</sup>, OH<sup>-</sup>, Na<sup>+</sup>, and NO<sub>3</sub><sup>-</sup> on the reaction interface.



Figure 4. The cross sectional profile of cavities from simulation and experiments.

### 3. Experimental Studies

# 3.1. Materials and Metrics

The workpiece material for experimental investigations was 304 stainless steel, and it was polished to mirror-surface levels (surface roughness <0.8  $\mu$ m) to have uniform contact with the mask. The lithographic mask array holes are 5  $\mu$ m in diameter. These micro-holes are distributed as a 35  $\times$  35 square array, and the hole center-distance is 50  $\mu$ m. The jet nozzle is implemented as a duckbill shaped nozzle with a slit length of 16 mm and a slit width of 2 mm. The experimental parameters used are listed in Table 3.

Table 3. Experimental parameters.

| Parameters                      | Value                             |  |  |  |  |
|---------------------------------|-----------------------------------|--|--|--|--|
| Applied voltage                 | 10, 20, 30, 40 V                  |  |  |  |  |
| Pulse frequency                 | 2 kHz                             |  |  |  |  |
| Pulse duty cycle                | 50%                               |  |  |  |  |
| Nozzle moving speed             | 1, 2, 3, 4 mm/s                   |  |  |  |  |
| Inter-electrode-gap             | 3.5 mm                            |  |  |  |  |
| Electrolyte concentration       | 10 % (wt.%) aq. NaNO <sub>3</sub> |  |  |  |  |
| Electrolyte temperature         | 25 °C                             |  |  |  |  |
| Electrolyte pressure            | 20 kPa                            |  |  |  |  |
| Diameter of cavitys in the mask | 5 µm                              |  |  |  |  |
| Mask thickness                  | 1.2 μm                            |  |  |  |  |
| Workpiece material              | Stainless steel 304               |  |  |  |  |

The surface topography of the micro cavity structure was obtained with a scanning electron microscope (S-3400N(II)). The size of micro cavity was measured by a laser scanning confocal microscope (Olympus OLS-4100). From the upper left corner to the lower right corner of the workpiece, 35 positions along the diagonal were uniformly selected for measurements. The diameter (*D*) and depth (*H*) of micro cavities were measured. The aspect ratio AR Equation (15), the etch factor *EF* Equation (16), and the standard deviation of diameter and depth *std*<sub>D</sub> Equation (17) and *std*<sub>H</sub> Equation (18) were calculated.

$$AR = \frac{H_i}{D_i} \tag{15}$$

$$EF = \frac{2H_i}{D_i - D_0} \tag{16}$$

$$\begin{cases} S_{W} = \sqrt{\frac{1}{N-1} \sum_{i=1}^{N} (D_{i} - \overline{D})} \\ \overline{D} = \frac{1}{N} \sum_{i=1}^{N} D_{i} \end{cases}$$

$$\begin{cases} S_{W} = \sqrt{\frac{1}{N-1} \sum_{i=1}^{N} (H_{i} - \overline{H})} \\ \overline{H} = \frac{1}{N} \sum_{i=1}^{N} H_{i} \end{cases}$$

$$(17)$$

$$(17)$$

$$(18)$$

where *N* the total number of measurements,  $D_0$  is the diameter of cavities in the mask,  $D_i$  the diameter of the *i*-th measured machined cavities *D*,  $H_i$  the depth of *i*-th measured machined cavities.

#### 3.2. Results and Discussion

## 3.2.1. Influence of Applied Voltage

Voltages ranging from 10 V to 40 V were applied to investigate their effect on shape accuracy of micro cavity fabrication. A typical profile of a micro cavity array with good shape consistency (the standard deviation for diameter and depth are  $std_D < 0.8 \mu m$  and  $std_H < 0.4 \mu m$ , respectively) and single micro cavity at different applied voltages (10 V and 40 V) are shown in Figure 5.

The dimensions of micro cavities generated with different applied voltage, with a pulse duty cycle of 50%, pulse frequency of 1 kHz, and a nozzle moving speed of 1 mm/s are shown in Figure 6 and Table 4. The violin plot, as shown in Figure 6, is presented for a better understanding of the processing pattern. The diamond-shaped areas generated by the multivariate KDE-based probabilistic density function are used to construct the violin plot, which examines the distribution of the results with different processing parameters. This data visualization method provides a statistical and intuitive way of interpreting the data. For more details, please refer Figure A5 in Appendix B.

| Voltage<br>(V) | 10    |      | 20    |      | 30    |       | 40    |       |
|----------------|-------|------|-------|------|-------|-------|-------|-------|
|                | D     | H    | D     | H    | D     | H     | D     | H     |
| mean           | 18.47 | 8.08 | 19.27 | 9.15 | 21.90 | 10.58 | 23.29 | 11.04 |
| std            | 0.56  | 0.20 | 0.60  | 0.26 | 0.69  | 0.32  | 0.74  | 0.39  |
| min            | 17.11 | 7.58 | 17.88 | 8.68 | 20.23 | 9.85  | 21.37 | 10.12 |
| 25% †          | 18.11 | 7.99 | 18.88 | 8.98 | 21.55 | 10.31 | 22.77 | 10.78 |
| 50% ‡          | 18.52 | 8.13 | 19.33 | 9.10 | 21.92 | 10.61 | 23.38 | 11.02 |
| 75% <b>*</b>   | 18.80 | 8.20 | 19.66 | 9.32 | 22.44 | 10.87 | 23.62 | 11.34 |
| max            | 19.53 | 8.53 | 20.64 | 9.77 | 23.50 | 11.10 | 24.92 | 11.73 |

Table 4. Diameter and depth of machined cavities with different applied voltage.

† 25th percentile ; ‡ 50th percentile (median); \* 75th percentile.

It can be seen that the diameter of micro cavities increased from  $18.47 \pm 0.56 \,\mu\text{m}$  (standard deviation) to  $23.29 \pm 0.74 \,\mu\text{m}$  as the voltage increased from  $10 \,\text{V}$  to  $40 \,\text{V}$ . Furthermore, the depth increased from  $8.08 \pm 0.02 \,\mu\text{m}$  to  $11.04 \pm 0.39 \,\mu\text{m}$  with an increase in voltage, thereby showing a similar trend as for the diameter. With an increase in voltage, the current density becomes higher. Therefore, the amount of material removal in a given machining time also increased. As a result, the diameter and depth of the micro cavities gradually increased, and the removal rate follows the general law of Faraday dissolution as shown in Equation (14).



(a) Applied voltage=10 V, frequency=1 kHz, plus duty cycle=50%, nozzle moving speed=2 mm/s.

(b) Applied voltage=40 V, frequency=1 kHz, plus duty cycle=50%, nozzle moving speed=2 mm/s.



**Figure 5.** The typical profile of micro cavities at different applied voltage: (**a**): 10 V; (**b**): 40 V; (**a**<sub>1</sub>,**b**<sub>1</sub>): SEM images of machined cavities; (**a**<sub>2</sub>,**b**<sub>2</sub>): Confocal laser scanning microscope images of machined cavities; (**a**<sub>3</sub>,**b**<sub>3</sub>): Cross-sectional images of corresponding machined cavities.

The values of the etch factor (*EF*) and the aspect ratio (*AR*) of the micro cavity at different voltages are shown in Figure 6 and Table 5. As the voltage increased, the value of *EF* is around 1.202 and the aspect ratio of micro cavity ranges from 0.438 to 0.475. This shows that the presented MEJM process generates an aspect ratio that is higher than others described in the literature.

| Voltage<br>(V) | 10   |      | 10 20 |      | 3    | 0    | 4    | 40   |  |
|----------------|------|------|-------|------|------|------|------|------|--|
|                | EF   | AR   | EF    | AR   | EF   | AR   | EF   | AR   |  |
| mean           | 1.20 | 0.44 | 1.29  | 0.48 | 1.25 | 0.48 | 1.21 | 0.47 |  |
| std            | 0.06 | 0.02 | 0.07  | 0.02 | 0.07 | 0.02 | 0.07 | 0.02 |  |
| min            | 1.11 | 0.41 | 1.14  | 0.43 | 1.14 | 0.44 | 1.06 | 0.42 |  |
| 25% †          | 1.14 | 0.42 | 1.24  | 0.46 | 1.21 | 0.47 | 1.16 | 0.46 |  |
| 50% ‡          | 1.20 | 0.44 | 1.27  | 0.48 | 1.25 | 0.48 | 1.22 | 0.48 |  |
| 75% *          | 1.25 | 0.45 | 1.33  | 0.49 | 1.29 | 0.50 | 1.26 | 0.49 |  |
| max            | 1.36 | 0.48 | 1.42  | 0.51 | 1.46 | 0.55 | 1.35 | 0.52 |  |

**Table 5.** *EF* and *AR* value of machined cavities with different applied voltage.

† 25th percentile; ‡ 50th percentile (median); \* 75th percentile.



Figure 6. The effect of voltage on the dimensions of micro cavities.

It is worth mentioning that the standard deviations of diameter and depth slightly increased as the voltage increased. This indicates that the machining stability was reduced as the amount of removed material increased.

## 3.2.2. Influence of Nozzle Moving Speed

A nozzle moving speed ranging from 1 mm/s to 4 mm/s was employed to investigate their effect on the shape accuracy of micro cavity fabrication. The typical profile of a micro cavity array with good shape consistency and single micro cavity at a different nozzle moving speed (2 mm/s and 4 mm/s) are shown in Figure 7.

The diameter and depth of the micro cavities generated at different nozzle moving speeds with an applied voltage of 30 V, a pulse duty cycle of 50%, and a pulse frequency of 2 kHz are shown in Figure 8 and Table 6. It can be seen that the diameter of the micro cavities decreased from  $22.07 \pm 0.71 \,\mu\text{m}$  to  $17.21 \pm 0.52 \,\mu\text{m}$  with an increase in nozzle moving speed from  $1 \,\text{mm/s}$  to  $4 \,\text{mm/s}$ . Furthermore, the depth decreases from  $10.16 \pm 0.31 \,\mu\text{m}$  to  $7.70 \pm 0.20 \,\mu\text{m}$  with an increase in nozzle moving speed increases, it is equivalent to reducing the processing time, and thus the diameter and depth of the micro cavities have been reduced.



(a) Applied voltage=30 V, frequency=1 kHz, plus duty cycle=50%, nozzle moving speed=2 mm/s.

(b) Applied voltage=30 V, frequency=1 kHz, plus duty cycle=50%, nozzle moving speed=4 mm/s.



**Figure 7.** The typical profile of micro cavities at different nozzle moving speed: (a): 2 mm/s; (b): 4 mm/s; ( $\mathbf{a}_1$ ,  $\mathbf{b}_1$ ): SEM images of machined cavities; ( $\mathbf{a}_2$ ,  $\mathbf{b}_2$ ): Confocal laser scanning microscope images of machined cavities; ( $\mathbf{a}_3$ ,  $\mathbf{b}_3$ ): Cross-sectional images of corresponding machined cavities.

| Speed (mm/s) | 1     |       | 2     |       | 3     |      | 4     |      |
|--------------|-------|-------|-------|-------|-------|------|-------|------|
|              | D     | H     | D     | H     | D     | H    | D     | Н    |
| mean         | 22.07 | 10.16 | 20.91 | 10.16 | 19.55 | 9.10 | 17.21 | 7.70 |
| std          | 0.71  | 0.31  | 0.66  | 0.26  | 0.60  | 0.23 | 0.52  | 0.20 |
| min          | 20.37 | 9.40  | 19.38 | 9.68  | 18.08 | 8.58 | 15.86 | 7.24 |
| 25% †        | 21.63 | 10.02 | 20.48 | 9.99  | 19.24 | 8.92 | 16.84 | 7.57 |
| 50% ‡        | 22.13 | 10.24 | 20.98 | 10.10 | 19.56 | 9.13 | 17.27 | 7.69 |
| 75% <b>*</b> | 22.48 | 10.33 | 21.35 | 10.33 | 20.02 | 9.31 | 17.44 | 7.85 |
| max          | 23.40 | 10.83 | 22.43 | 10.78 | 20.96 | 9.48 | 18.36 | 8.04 |

Table 6. Diameter and depth of machined cavities with different nozzle moving speed.

† 25th percentile; ‡ 50th percentile (median); \* 75th percentile.

The values of *EF* and *AR* of the micro cavities using different nozzle moving speeds are shown in Figure 8 and Table 7. Even at different nozzle moving speeds, the value of *EF* is around 1.2, showing the same trend as that for the voltage. The aspect ratio of the micro cavities ranges from 0.461 to 0.448. In this case, the *EF* of this MEJM technology is comparable to those observed in the literatures. Qu et al. [18] used a 50  $\mu$ m thick dry-film photoresist as a mask during the TMEMM process to fabricate a micro cavity with an *EF* of 1.03 and 94  $\mu$ m in diameter on a cylindrical inner surface, when the original mask aperture is 50  $\mu$ m in diameter.



Figure 8. The effect of nozzle moving speed on the dimensions of micro cavities.

| Speed (mm/s) | 1.00 |      | 2.00 |      | 3.00 |      | 4.00 |      |
|--------------|------|------|------|------|------|------|------|------|
|              | EF   | AR   | EF   | AR   | EF   | AR   | EF   | AR   |
| mean         | 1.19 | 0.46 | 1.28 | 0.49 | 1.25 | 0.47 | 1.26 | 0.45 |
| std          | 0.07 | 0.02 | 0.06 | 0.02 | 0.06 | 0.02 | 0.07 | 0.02 |
| min          | 1.10 | 0.43 | 1.14 | 0.44 | 1.15 | 0.43 | 1.12 | 0.41 |
| 25% †        | 1.13 | 0.44 | 1.23 | 0.47 | 1.21 | 0.45 | 1.21 | 0.43 |
| 50% ‡        | 1.20 | 0.46 | 1.27 | 0.48 | 1.25 | 0.47 | 1.28 | 0.45 |
| 75% <b>*</b> | 1.25 | 0.48 | 1.33 | 0.50 | 1.29 | 0.48 | 1.31 | 0.46 |
| max          | 1.35 | 0.51 | 1.41 | 0.52 | 1.45 | 0.52 | 1.42 | 0.48 |

Table 7. *EF* and *AR* of machined cavities with different nozzle moving speed.

† 25th percentile; ‡ 50th percentile (median); \* 75th percentile.

The standard deviations of diameter and depth were slightly decreased ( $std_D$ : from 0.71 to 0.52,  $std_H$ ) as the nozzle moving speed increased. This shows that the machining reliability was slightly improved as the amount of removed material decreased. This is probably because the deceased total machining time will decrease the risk of mask failure provoked by electrolyte flow flush.

## 4. Conclusions

In this study, a method of mask-based electrolyte jet machining with a duckbill nozzle was proposed for mass fabrication of a micron-sized micro cavity array on the surface of metal parts. The micro cavity shape evolution process and electric-field/current density distribution were simulated using the COMSOL<sup>®</sup>® Multiphysics software. A micro cavity array structure with a good shape consistency (the standard deviation for machined cavity diameter and depth can be as small as 0.52 and 0.2, respectively) was fabricated by MEJM. The design of experiments explored the influence of applied voltage and nozzle moving speed on the size and topography of the micro cavities. It can be concluded that the simulations showed good agreement with the experimental profile. However, there was less machining depth in simulated profiles, possibly because of the absence of considering a pulsed current.

It was observed in experiments that with an increase in process-voltage, the dimensions of micro cavities and depth-to-diameter ratios gradually increased. The diameter and depth increased by 26.08% and 36.57%, respectively, as the voltage increased from 10 V to 40 V. When the processing voltage is 40 V, the size of the micro cavities is highest. At low voltages, the micro cavities are shallow. Therefore, preference should be given to medium voltage. When the applied voltage is 20 V, the *EF* and *AR* values are the highest.

With an increase in the nozzle moving speed, the diameter and depth of the micro cavities decrease. The diameter and depth decreased by 22.04% and 24.23%, respectively, as the nozzle moving speed increased from 1 mm/s to 4 mm/s.

Overall, micro cavity structures were successfully fabricated using the proposed MEJM technology and a duckbill nozzle. This work is an initial step towards using MEJM technology for deterministic and efficient fabrication of micro-structures such as cavity/grooves on large workpieces. The technology can be further changed to textured, curved and free-form surfaces using flexible masks. The technology has potential applications in the texturing of bearings for improved lubrication, mimicking of artificial bearing defects and micro-structuring of mould surfaces for improved ceramic/polymer injection molding. The machining precision is mainly dependent on the resolution of the lithographic mask, rather than the size of the tool; limitations on tool dimensions are overcome with this technology. The holes in the masks can be fabricated down to a nanometer scale using state-of-the-art lithography techniques. With improved electrolyte recycling systems, this technology can be a cost effective technology as it does not involve capital costs such as those of a laser texturing process using femto-second lasers, expensive optics and beam manipulation peripherals.

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# Appendix A. Simulation Results of Ion Distribution at Different Processing Time

**Figure A1.** Simulation results at *t* = 0 s. (**a**<sub>1</sub>): velocity field of the electrolyte flow; (**b**<sub>1</sub>): velocity field of electrolyte flow in the machined cavity; (**a**<sub>2</sub>) electric potential distribution in the MEJM; (**b**<sub>2</sub>) electric potential distribution (V) in the machined cavity; (**c**<sub>1</sub>) normal current density distribution around the machined cavity; (**d**<sub>1</sub>): normal current density distribution on the reaction interface; (**c**<sub>2</sub>-**c**<sub>6</sub>): concentration (mol/m<sup>3</sup>) of Fe<sup>3+</sup>, H<sup>+</sup>, OH<sup>-</sup>, Na<sup>+</sup>, and NO<sub>3</sub><sup>-</sup> around the machined cavity; (**d**<sub>2</sub>-**d**<sub>6</sub>): concentration (mol/m<sup>3</sup>) of Fe<sup>3+</sup>, H<sup>+</sup>, OH<sup>-</sup>, Na<sup>+</sup>, and NO<sub>3</sub><sup>-</sup> on the reaction interface.

a1 Velocity field of the electrolyte flow

05

a2 Electric potential distribution in the MEJM

0.5

c1 Current density distribution around the machined cavity

5000

1

1

 $\times 10^4 \mu m$ 

 $10^4 \mu m$ 

5

0

**V** 0

μm

5020

▲ 8.27×10<sup>5</sup> ×10<sup>5</sup>

A/m<sup>3</sup>

100

50 0

1

0.5

μm

0.5

10 V

5

μm

 $\mu$ m

4000 2000

-2000

 $\mu$ m

μm

μm

1

-10 -15

10

4940

0

10

0

-10 -15 -20 4940

4960

4960

4980

 $c_2$  Concentration of  $\mathsf{Fe}^{3^+}$  around the machined cavity

4980

c3 Concentration of H<sup>+</sup> around the machined cavity

5000

4000

2000

0 -2000

-0.5

0





**Figure A2.** Simulation results at t = 1 s. (**a**<sub>1</sub>): velocity field of the electrolyte flow; (**b**<sub>1</sub>): velocity field of electrolyte flow in the machined cavity; (a2) electric potential distribution in the MEJM;  $(b_2)$  electric potential distribution (V) in the machined cavity;  $(c_1)$  normal current density distribution around the machined cavity;  $(d_1)$ : normal current density distribution on the reaction interface;  $(c_2-c_6)$ : concentration (mol/m<sup>3</sup>) of Fe<sup>3+</sup>, H<sup>+</sup>, OH<sup>-</sup>, Na<sup>+</sup>, and NO<sub>3</sub><sup>-</sup> around the machined cavity;  $(d_2-d_6: \text{concentration } (\text{mol}/\text{m}^3) \text{ of } \text{Fe}^{3+}, \text{H}^+, \text{OH}^-, \text{Na}^+, \text{ and } \text{NO}_3^- \text{ on the reaction interface.}$ 



**Figure A3.** Simulation results at t = 2 s. (**a**<sub>1</sub>): velocity field of the electrolyte flow; (**b**<sub>1</sub>): velocity field of electrolyte flow in the machined cavity; (**a**<sub>2</sub>) electric potential distribution in the MEJM; (**b**<sub>2</sub>) electric potential distribution (V) in the machined cavity; (**c**<sub>1</sub>) normal current density distribution around the machined cavity; (**d**<sub>1</sub>): normal current density distribution on the reaction interface; (**c**<sub>2</sub>-**c**<sub>6</sub>): concentration (mol/m<sup>3</sup>) of Fe<sup>3+</sup>, H<sup>+</sup>, OH<sup>-</sup>, Na<sup>+</sup>, and NO<sub>3</sub><sup>-</sup> around the machined cavity; (**d**<sub>2</sub>-**d**<sub>6</sub>): concentration (mol/m<sup>3</sup>) of Fe<sup>3+</sup>, H<sup>+</sup>, OH<sup>-</sup>, Na<sup>+</sup>, and NO<sub>3</sub><sup>-</sup> on the reaction interface.

μm

μm

4000

2000

-2000

 $\mu$ m

μm

μm

 $\mu$ m

μm

 $\mu$ m

0

10

0

-10

-20

10

C

-10

-20

10

-10

-20

1

(

-10 -20

10

-10

-20

10

-10

-20

0

С

4000

2000

0 -2000

-0.5

-0.5

4950



**Figure A4.** Simulation results at t = 3 s. (**a**<sub>1</sub>): velocity field of the electrolyte flow; (**b**<sub>1</sub>): velocity field of electrolyte flow in the machined cavity;  $(a_2)$  electric potential distribution in the MEJM;  $(b_2)$  electric potential distribution (V) in the machined cavity;  $(c_1)$  normal current density distribution around the machined cavity;  $(d_1)$ : normal current density distribution on the reaction interface;  $(c_2-c_6)$ : concentration (mol/m<sup>3</sup>) of Fe<sup>3+</sup>, H<sup>+</sup>, OH<sup>-</sup>, Na<sup>+</sup>, and NO<sub>3</sub><sup>-</sup> around the machined cavity;  $(d_2-d_6)$ : concentration (mol/m<sup>3</sup>) of Fe<sup>3+</sup>, H<sup>+</sup>, OH<sup>-</sup>, Na<sup>+</sup>, and NO<sub>3</sub><sup>-</sup> on the reaction interface.



## Appendix B. Explanation of Vionlin Plot

Figure A5. Explanation of violin plot.

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