



# Article Coherent-on-Receive Synthesis Using Dominant Scatterer in Millimeter-Wave Distributed Coherent Aperture Radar

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Abstract: The target signal-to-noise ratio (SNR) can be notably improved by coherent-on-receive synthesis (CoRS) in distributed coherent aperture radar (DCAR). A core challenge of CoRS is to estimate the coherent parameters (CPs), including time, frequency, and phase, in order to cohere the multi-radar within DCAR. Conventional methods usually rely on the target's own information to estimate the CPs, which is not available in highly dynamic environments. Additionally, the CPs of different targets, especially the phase, are unequal in high-frequency systems. This means that we cannot directly use the CPs of one target to compensate for others. To address these issues, an adaptive CoRS method using the dominant scatterer is proposed for millimeter-wave (MMW) DCAR in this paper. The basic idea is to correct the CPs of the dominant scatterer to compensate for other targets. The novelty lies in the adaptive phase compensation based on the estimated CPs. This phase compensation depends on a series of discrete phase values, which are derived from the limit of synthesis loss within a given configuration. Hence, this method avoids the requirement of prior information or massive searches for the possible locations of other targets. Moreover, the dominant scatterer in this work is an unknown target with strong scattering points in radar detection scenarios, and we focus on analyzing its selection criteria. To validate the proposed method, a prototype system has been fabricated and evaluated through experiments. It is demonstrated that the multi-target can realize CoRS effectively, thus enhancing the target SNR.

**Keywords:** coherent-on-receive synthesis; distributed coherent aperture radar; coherent parameters; dominant scatterer

# 1. Introduction

Distributed coherent aperture radar (DCAR), which is composed of several independent unit radars, has potential for radar detection, tracking, and recognition [1–3]. These unit radars can be placed in different positions and used together in a coherent and cooperative way to enhance the target energy significantly.

A typical mode of DCAR is coherent-on-receive synthesis (CoRS) [4–6]. With this mode, DCAR could promote the target signal-to-noise ratio (SNR) by  $M^2$  times, where M is the number of unit radars. In CoRS, the multiple-unit radars rely on hardware for synchronization and transmit orthogonal signals [7–9]. This hardware allows the target echoes to be separated at each receiver. By analyzing these echoes, we can estimate the coherent parameters (CPs) between different unit radars, including transmission time, frequency, and phase [10,11]. The estimated CPs can then be used to carefully adjust the echoes so that the echoes can be added together at the same time and phase. The synthesis performance



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**Copyright:** © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). of DCAR depends on high-accuracy CP estimations. Moreover, the demands for estimation accuracy also increase with the radar carrier frequency and bandwidth. Therefore, the majority of the research on CoRS is focused on the low-frequency system [12–14].

To align the time and phase between unit radars, hardware-based methods have been investigated in the literature [15–18]. They utilize wired or wireless connections to obtain high-precision synchronization. However, these methods commonly require highly complex hardware. Additionally, even with almost ideal synchronization, realtime monitoring and calibration are still required in practical applications because of hardware instability.

Estimating the CPs based on observed target echoes is an effective way to solve the above problems. Existing estimation methods can be roughly divided into two categories. One is detecting the target's own peak in returns for estimations [19,20], and the other is utilizing a cooperative target with prior information, called the dominant scatterer [21,22]. However, these methods are quite limited in highly dynamic scenarios. The former will fail when all scattering points of the target are undetectable, and the premise of the latter, requiring prior information, is hardly valid in many applications. Furthermore, using the estimated CPs of one target, the phases of other targets may still not be aligned in multiple-unit radars. This is caused by the spatial phase between different targets, which can be neglected in previous low-frequency systems. In high-frequency systems, such as millimeter-wave (MMW), the spatial phase may vary significantly, so we cannot directly use the estimated CPs of one target to compensate for the others.

In this paper, a novel CoRS method is proposed to solve the above issues for MMW DCAR. The basic idea is to correct the CPs of the dominant scatterer to compensate for other targets. Unlike the previous works that use a pre-positioned corner reflector or active backscatter transponder as the dominant scatterer, the proposed method employs an unknown target with strong scattering points to estimate the CPs in radar detection scenarios. For the dominant scatterer, we focused on analyzing its selection criteria and procedure. Furthermore, an adaptive phase compensation approach was explored to correct the estimated CPs of the dominant scatterer. This approach can compensate for the phases of different targets using a series of discrete phase values. Different from the general approaches that compensate the phases by searching for the possible positions of other targets point-by-point, the determination of discrete phase values in this approach is derived by the limit of synthesis loss within a given MMW DCAR configuration. This approach can simultaneously align the phase of targets located in a certain region based on the phase relationship between multiple unit radars. Hence, it can significantly reduce the number of phase compensations searches and remove the need for the spatial position of other targets. Finally, a prototype system composed of three MMW radars with a common trigger was fabricated, and the proposed concepts were confirmed via measurements with this prototype system. The main contributions in this work can be summarized as follows:

- We first introduce the coherent-on-receive synthesis into the millimeter-wave distributed coherent aperture radar. This method can be widely used in millimeter-wave radar applications, such as autonomous driving and precision guidance;
- 2. An adaptive compensation approach is proposed to correct the estimated CPs of the dominant scatterer. On the one hand, prior information about the dominant scatterer is not required, and we can choose an unknown target with strong scattering points to estimate the CPs in radar detection scenarios. On the other hand, there is also no need for the spatial position of other targets as prior information;
- 3. The proposed MMW DCAR can be adaptively cohered based on observed target echoes, thus reducing the hardware demands for high-accuracy synchronization.

The remainder of this paper is organized as follows. In Section 2, we introduce the workflow and signal model of CoRS in DCAR. In Section 3, the proposed method is described and derived in detail. Moreover, its constraints are also analyzed to present the selection criteria of the dominant scatterer. In Section 4, the proposed method's evaluation via simulations is reported. Section 5 illustrates the real-data results with a prototype system to verify the feasibility of the proposed method. Finally, we conclude this paper with a summary of the main outcomes in Section 6.

#### 2. Background

# 2.1. Workflow of CoRS in DCAR

The distributed coherent aperture radar (DCAR) is composed of M unit radars. An  $M^2$  SNR gain could be obtained over a unit radar when coherence-on-receive synthesis (CoRS) is realized, which makes it capable of attaining the equivalent performance compared with a large aperture radar.

There are three steps, including system hardware synchronization, coherent parameters estimation, and cohere-on-receive synthesis, in the operation procedure of CoRS, as displayed in Figure 1. The workflow can be illustrated as follows:

- 1. The multiple-unit radars within DCAR rely on wired or wireless connections to ensure that they can operate at the same time.
- 2. Due to the imperfect synchronization and the unequal range between different unit radars and targets, there are multidimensional differences between any two radars, called coherent parameters (CPs). To solve this problem, the multiple unit radars transmit the orthogonal waveforms with the same time base, which allows the target echoes to be separated at each receiver's matched filter output. By detecting the target peaks in different echoes, the CPs can be estimated.
- 3. The estimated CPs are used to adjust the echoes of multiple unit radars, and then the adjusted echoes are added together with the same time and phase to obtain the SNR gain.



Figure 1. The workflow diagram of CoRS in DCAR.

## 2.2. Signal Model

Multiple-unit radars transmit the orthogonal waveforms to guarantee that mixed echoes can be separated at the receivers. The basis waveform in this work is the fast chirp sequence [23–27], where a series of chirp signals is successively transmitted in one coherent processing interval (CPI). With the basis waveform, various orthogonal techniques have been reviewed in [28], such as time division, frequency division, and code division.

The frequency-division method limits the available bandwidth for each transmitter as well as the range resolution [29,30]. Moreover, its intermediate frequency (IF) should have a large bandwidth to hold the mixer output, resulting in high hardware costs. The codedivision method modulates different phase sequences on the transmission pulses [31–33]. Due to its imperfect orthogonality, this waveform will have relatively high sidelobes in the spectrum. The high sidelobes may reduce the estimation accuracy of coherent parameters, resulting in an overall loss of synthesis. Considering the above issues, we recommend using the time-division method. This method is simple, but the unambiguous Doppler range will be reduced. To solve this problem, staggered PRT or multiple PRT approaches can be used to estimate the ambiguity number [34,35]. These approaches have a good performance in resolving velocity ambiguity, yet have a relatively low data rate. Additionally, the time-division method will also receive interference signals from other radars in many applications, such as traffic scenarios. Although the parameters of the signals may be different, they may produce non-phase-referenced interference, which will limit the performance of CoRS. In this regard, interference mitigation approaches [36–39] can be employed to solve this issue. Based on these approaches, we can first estimate the interfering signal. Then, after removing the estimated interference, the radar echoes can be restored with sparsity-based techniques.

Utilizing the time-division method, as shown in Figure 2, in a single chirp duration, only one unit radar transmits a linear chirp of the form:

$$s(t) = exp\left[j2\pi\left(f_0t + \frac{1}{2}kt^2\right)\right],\tag{1}$$

with carrier frequency  $f_0$ , frequency slope k = B/T, where *B* is the sweep bandwidth and *T* represents pulse repetition time (PRT).



Figure 2. The fast chirp sequence waveform used in the MMW DCAR with time-division method.

Since the proposed MMW DCAR only relies on a common trigger for synchronization, it leads to multidimensional synchronization errors between any two unit radars. Assuming that the synchronization errors of the *m*-th radar, compared with the reference radar (the first radar), include time synchronization error  $\Delta T_m$ , frequency synchronization error  $\Delta f_m$ , and phase synchronization error  $\Delta \varphi_m$ , the echo of the *m*-th transmitting radar and the *n*-th receiving radar can be expressed as

$$s_{mn}(t) = \exp\left[j2\pi\left((f_0 + \Delta f_{mn})(t - \tau_{mn}) + \frac{1}{2}k(t - \tau_{mn})^2\right) + j\Delta\varphi_{mn}\right],$$
 (2)

with

$$\tau_{mn} = \frac{R_{mn} + v_{mn}t}{c} + \Delta T_{mn} \tag{3}$$

$$\Delta T_{mn} = \Delta T_m - \Delta T_n \tag{4}$$

$$\Delta f_{mn} = \Delta f_m - \Delta f_n \tag{5}$$

$$\Delta \varphi_{mn} = \Delta \varphi_m - \Delta \varphi_n \tag{6}$$

where  $R_{mn}$  and  $v_{mn}$  represent the sum of the propagation distance and radial velocity of the target, and *c* is the speed of light.

Further, the beat signal can be obtained with de-chirp processing as

$$s_{beat,mn}(t) = exp\left[j2\pi\left((f_0 + \Delta f_{mn})\tau_{mn} + k\tau_{mn}t - \frac{1}{2}k(\tau_{mn})^2\right) + j\Delta\varphi_{mn}\right].$$
(7)

Supposing  $t = t_s + t_p$ , where  $t_s$  is the sampling time in PRT and  $t_p = p \times PRT$  denotes the velocity dimension sampling time, the beat signal can be modified as

$$s_{beat,mn}(t_s,t_p) = exp \left\{ j2\pi \left[ \begin{array}{c} \left(\frac{kR_{mn}+f_0v_{mn}+\Delta f_{mn}v_{mn}-kv_{mn}\Delta T_{mn}+kv_{mn}t_s}{c} + k\Delta T_{mn} - \Delta f_{mn}\right)t_s \\ + \left(\frac{f_0v_{mn}+\Delta f_{mn}v_{mn}-kv_{mn}\Delta T_{mn}+kv_{mn}t_s}{c}\right)t_p \\ + \left(\frac{(f_0+\Delta f_{mn}+k\Delta T_{mn})R_{mn}}{c} + (f_0+\Delta f_{mn})\Delta T_{mn} - \frac{k\Delta T_{mn}^2}{2}\right) - \frac{k}{2}\left(\frac{R_{mn}+v_{mn}t_s+v_{mn}t_p}{c}\right)^2 \right] + j\Delta\varphi_{mn} \right\}.$$
(8)

Note that the quadratic phase terms within the beat signal have been neglected because their contribution to the phase change is small, referring to [22]. Further, the beat signal can be simplified as

$$s_{beat,mn}(t_s, t_p) = exp[j2\pi(\Phi_s t_s + \Phi_p t_p + \Phi_C)] \cdot exp[j\Delta\varphi_{mn}], \tag{9}$$

where

$$\Phi_s = k\Delta T_{mn} - \Delta f_{mn} + \frac{kR_{mn} + f_0 v_{mn}}{c}$$
(10)

$$\Phi_p = \frac{f_0 v_{mn} + \Delta f_{mn} v_{mn} - k v_{mn} \Delta T_{mn}}{c} \tag{11}$$

$$\Phi_{C} = \frac{f_0 R_{mn} + \Delta f_{mn} R_{mn} - k R_{mn} \Delta T_{mn}}{c} + (f_0 + \Delta f_{mn}) \Delta T_{mn}.$$
 (12)

The classical signal model with the time-division method was derived. Usually, the sampled data are stacked together in a cube according to the fast time and slow time. Hence, the range and velocity of the targets are separately extracted with a two-dimensional fast Fourier transform (2D-FFT) from this data cube, which can be expressed as

$$S_{mn}(f_r, f_v) = \mathcal{F}[s_{beat,mn}(t_s, t_p)] \\ = sinc(f_r - \Phi_s) \cdot sinc(f_v - \Phi_p) \cdot exp[j2\pi(\Phi_C)] \cdot exp[j\Delta\varphi_{mn}],$$
(13)

where  $\mathcal{F}[\cdot]$  represents the 2D-FFT processing.

Clearly, the target can be focused on the range–Doppler spectrum; however, there is an uncertain deviation caused by the synchronization errors. To estimate the deviations in range or the Doppler spectrum, we can detect the target peak in different echoes. However, the phase deviation, as in Equation (12), which is proportional to the radar carrier frequency, is related to the target's spatial position and the synchronization errors. Therefore, it may vary significantly for different targets in high-frequency systems. This means that the available region for estimating CPs of phases is quite limited. When we compensate the phases using the CPs of one target, the phases of other targets cannot be aligned, leading to a great CoRS loss.

## 3. Proposed Method

To solve the above problem, a novel coherent-on-receive synthesis method using the dominant scatterer is proposed, and its processing flow is presented in Figure 3.



Figure 3. The processing flow of the proposed method using the dominant scatterer.

First, the proposed method uses the dominant scatterer to estimate CPs, in which the dominant scatterer is realized as an unknown strong target in radar detection scenarios.

Second, the echoes of multiple unit radars can be compensated with the estimated CPs of the dominant scatterer. In this way, the range and velocity of different targets in multiple unit radars can be aligned, but the phase requires further adjustment.

Third, an adaptive compensation approach was explored to align the phases of various targets in multiple unit radars. The phases of different targets are compensated with discrete phase values. Unlike the general approaches that compensate the phases by searching for the possible positions of other targets point-by-point, the determination of discrete phase values in this work is derived by the limit of synthesis loss within a given MMW DCAR configuration. This approach can simultaneously align the phase of targets located in a certain region based on the phase relationship between multiple unit radars. Hence, it can significantly reduce the number of phase compensation searches, and there is no need for the spatial position of other targets.

Furthermore, we derived the constraints of the proposed method and focused on analyzing the selection criteria and procedure of the dominant scatterer. The theoretical CoRS gain is also deduced to evaluate the performance of the proposed method in practice.

## 3.1. CP Estimation Using Dominant Scatterer

According to the focusing positions, we can estimate the CPs using the dominant scatterer. In previous works, the dominant scatterer was realized as a pre-positioned corner reflector or active backscatter transponder, which is hardly valid in high-dynamic scenarios. Instead, the dominant scatterer in this work is defined as an unknown target with strong scattering points in radar detection scenarios, such as vehicles, signs, etc.

The specific estimation method is similar to conventional methods. Assuming that channel 1T1R is the reference channel, which consists of the first transmitting and receiving radar, according to Equation (9), the beat signal in channel 1T1R without synchronization errors can be derived and simplified as

$$s_{beat,11}(t_s, t_p) = exp\left\{j2\pi \left[\left(\frac{f_0v_{11}}{c} + \frac{kR_{11}}{c}\right)t_s + \frac{f_0v_{11}}{c}t_p + \frac{f_0R_{11}}{c}\right]\right\}.$$
 (14)

Correspondingly, the estimated CPs for time can be obtained as

$$\Delta \hat{T}_{mn} = \Delta T_{mn} - \frac{\Delta f_{mn}}{k} + \frac{R_{mn} - R_{11}}{c} + \frac{f_0(v_{mn} - v_{11})}{ck}.$$
(15)

Similarly, the estimated CPs for velocity can be calculated as

$$\Delta \hat{V}_{mn} = \frac{v_{mn} - v_{11}}{2} + \frac{\Delta f_{mn} v_{mn}}{2f_0} - \frac{k v_{mn}}{2f_0} \Delta T_{mn}.$$
(16)

Moreover, the CPs for phase can also be estimated as

$$\Delta\hat{\varphi}_{mn} = 2\pi \left[ (f_0 + \Delta f_{mn})\Delta T_{mn} + \frac{f_0(R_{mn} - R_{11})}{c} + \frac{(\Delta f_{mn} - k\Delta T_{mn})R_{mn}}{c} \right] + \Delta\varphi_{mn}.$$
 (17)

3.2. Echoes Compensation and Analysis

Using the estimated CPs, as in Equations (15) to (17), the beat signal can be compensated as

$$s'_{beat,mn}(t_s,t_p) = s_{beat,mn}(t_s,t_p) \cdot exp(-j2\pi k\Delta \hat{T}_{mn} \cdot t_s) \cdot exp(-j2\pi k f_0 \Delta \hat{V}_{mn} \cdot t_p) \cdot exp(-j\Delta \hat{\varphi}_{mn}).$$
(18)

After compensation, the multidimensional parameters can be aligned with the reference channel. This means that the echoes can be added together to enhance the SNR of the dominant scatterer. However, due to the spatial difference, the compensated signal of other weak targets may have deviations. These deviations may lead to a great synthesis loss of weak targets. Therefore, we carefully derive the deviations and present an analysis thereof in the following.

Assuming that the CPs of a weak target can be estimated, the ideal compensated signal can be aligned to the reference channel and is expressed as

$$s'_{beat,mn}(t_s, t_p)\big|_{DS \to WT} = exp\Big[j2\pi\Big(\Big(\frac{f_0 v_{11}|_{WT}}{c} + \frac{kR_{11}|_{WT}}{c}\Big)t_s + \frac{f_0 v_{11}|_{WT}}{c}t_p + \frac{f_0 R_{11}|_{WT}}{c}\Big)\Big],\tag{19}$$

where  $R_{11}|_{WT}$  and  $v_{11}|_{WT}$  denote the range and velocity of the weak target in reference channel.

Due to the lack of the estimated CPs of the weak target, we can only utilize the CPs of the dominant scatterer to compensate for the beat signal. In this way, the compensated signal can be derived as

$$s'_{beat,mn}(t_s,t_p)\big|_{DS \to WT} = s_{beat,mn}(t_s,t_p)\big|_{WT} \cdot exp(-j2\pi k\Delta \hat{T}_{mn} \cdot t_s) \cdot exp(-j2\pi k f_0 \Delta \hat{V}_{mn} \cdot t_p) \cdot exp(-j\Delta \hat{\varphi}_{mn})$$

$$= exp \left\{ j2\pi \left[ \begin{array}{c} \left( \frac{k(R_{mm}|_{WT} - R_{mn}|_{DS} + R_{11}|_{DS})}{c} + \frac{f_0(v_{mn}|_{WT} - v_{mn}|_{DS} + v_{11}|_{DS})}{c} - \frac{k(v_{mn}|_{WT} - v_{mn}|_{DS})\Delta T_{mn}}{c} \right) t_s \\ + \left( \frac{f_0(v_{mn}|_{WT} - v_{mn}|_{DS} + v_{11}|_{DS})}{c} + \frac{(\Delta f_{mn} - k\Delta T_{mn})(v_{mn}|_{WT} - v_{mn}|_{DS})}{c} \right) t_p \\ \frac{f_0(R_{mn}|_{WT} - R_{mn}|_{DS} + R_{11}|_{DS})}{c} + \frac{(\Delta f_{mn} - k\Delta T_{mn})(R_{mn}|_{WT} - R_{mn}|_{DS})}{c} \right] \right\}.$$
(20)

Comparing Equations (19) and (20), it is apparent that the results including range, velocity, and phase are shifted. Specifically, the deviations can be calculated as

$$\Delta R_{mn}|_{DS \to WT} \approx \frac{R_{mn}|_{WT} - R_{mn}|_{DS} + R_{11}|_{DS} - R_{11}|_{WT}}{2},$$
(21)

$$\Delta V_{mn}|_{DS \to WT} \approx \frac{v_{mn}|_{WT} - v_{mn}|_{DS} + v_{11}|_{DS} - v_{11}|_{WT}}{2},$$
(22)

$$\Delta \varphi_{mn}|_{DS \to WT} = 2\pi \left( \frac{f_0(R_{mn}|_{WT} - R_{mn}|_{DS} + R_{11}|_{DS} - R_{11}|_{WT})}{c} + \frac{(\Delta f_{mn} - k\Delta T_{mn})(R_{mn}|_{WT} - R_{mn}|_{DS})}{c} \right).$$
(23)

Herein, the range and velocity deviations are simplified because the neglected terms are much smaller than the reserved ones, which can be expressed as follows.

$$\frac{f_0(v_{mn}|_{WT} - v_{mn}|_{DS} + v_{11}|_{DS} - v_{11}|_{WT})}{c} - \frac{k(v_{mn}|_{WT} - v_{mn}|_{DS})\Delta T_{mn}}{c} \ll \frac{k(R_{mn}|_{WT} - R_{mn}|_{DS} + R_{11}|_{DS} - R_{11}|_{WT})}{c},$$
(24)

$$\frac{k(v_{mn}|_{WT} - v_{mn}|_{DS})\Delta T_{mn}}{c} \ll \frac{f_0(v_{mn}|_{WT} - v_{mn}|_{DS} + v_{11}|_{DS} - v_{11}|_{WT})}{c}.$$
 (25)

Obviously, the deviations in range and velocity are caused by the geometry of the target relative to multiple unit radars. It is difficult to further compensate them due to the lack of a weak target position. In this regard, we define the constraints for dominant scatterer compensation so that these two deviations cannot exceed half a resolution cell after compensation. The specific derivation and analysis are presented in Section 3.4.

The phase deviation, as in Equation (23), is composed of two terms. The former is only determined by multi-target spatial positions, and the latter is a coupling term with the spatial positions and the synchronization errors. Similarly, it is difficult to accurately compensate for the phases due to the lack of weak target information. Moreover, the phase deviation is proportional to the radar carrier frequency. It will vary significantly for different targets in the MMW system, and hence is required to be adjusted for effective CoRS.

## 3.3. Adaptive Compensation for Phases

To align the phases of different targets in multi-channels, an adaptive compensation method is proposed. Considering that the phase deviation is composed of two terms, we performed two-step compensations to align the phases in multi-channels.

First, we utilized the information and CPs of the dominant scatterer to compensate for the coupling term, which is composed of the spatial positions and the synchronization errors. Thereafter, due to the lack of weak target information, we propose to compensate the phase adaptively with discrete phase values. The determination of discrete phase values is derived from the limit of synthesis loss within a given MMW DCAR configuration. Hence, this approach can simultaneously align the phase of targets located in a certain region based on the phase relationship between multiple unit radars. It can significantly reduce the compensation number and remove the need of the spatial position of weak targets.

# 3.3.1. Compensation for Coupling Term

To eliminate the coupling term of phase deviation, the signal of each channel can be compensated with the CPs of the dominant scatterer and can be expressed as

$$S_{corr}(f_r, f_v) = \mathcal{F}\left[s'_{beat,mn}(t_s, t_p)\big|_{DS \to WT}\right] \cdot exp\left(-j2\pi\left(\frac{k(\mathbf{R}_{unit} - R_{mn}|_{DS})\Delta\hat{T}_{mn}}{c}\right)\right).$$
(26)

where  $\mathbf{R}_{unit} = [R_1, R_2, \cdots, R_{max}]$  represents the cells in range spectrum.

After compensating for the coupling term, the phase deviation of the weak target can be derived as

$$\Delta \varphi'_{mn}|_{DS \to WT} = \Delta \varphi_{mn}|_{DS \to WT} - 2\pi \left[ \frac{k(R_{mn}|_{WT} - R_{mn}|_{DS})\Delta \hat{T}_{mn}}{c} \right]$$
  
$$= 2\pi \left[ \frac{f_0(R_{mn}|_{WT} - R_{mn}|_{DS} + R_{11}|_{DS} - R_{11}|_{WT})}{\frac{k(R_{mn}|_{WT} - R_{mn}|_{DS})^2}{c^2}} + \frac{f_0(R_{mn}|_{WT} - R_{mn}|_{DS})(v_{mn}|_{WT} - v_{mn}|_{DS})}{c^2} \right]$$
  
$$\approx 2\pi \left[ \frac{f_0(R_{mn}|_{WT} - R_{mn}|_{DS} + R_{11}|_{DS} - R_{11}|_{WT})}{c} \right].$$
(27)

Herein, it is apparent that the compensated phase deviation only relies on the multitarget spatial positions.

## 3.3.2. Compensation for Spatial Phase

Although the compensated phase deviation is only related to the multi-target positions, aligning the phases of weak targets is a challenging task. On the one hand, we cannot obtain prior information on weak targets to compensate the phase directly. On the other hand, compensating via searching for the possible positions of the weak targets leads to a large number of compensations. To this end, we propose to compensate the phase adaptively with discrete phase values, which are derived by the limit of synthesis loss within a given MMW DCAR configuration.

First, in a given configuration, the relative relationships of the compensated phase deviations of the weak targets within multi-channel are derived. Second, we define the acceptable synthetic gain loss and construct an inequality equation from this loss. Finally, the phase tolerance is deduced by solving the inequality equation. The phase tolerance is a discrete phase value, which can be defined as the maximum acceptable phase difference between any two channels. According to this tolerance, we can adjust the phases of multi-channel adaptively with the relative relationship. The specific derivation of this approach is described as follows.

The compensated phase deviation in channel mTnR in Equation (27) can be rewritten as

$$\Delta \varphi'_{mn}|_{DS \to WT} = 2\pi \left( \frac{f_0 \left( R_m|_{WT} + R_n|_{WT} - R_m|_{DS} - R_n|_{DS} + 2R_1|_{DS} - 2R_1|_{WT} \right)}{c} \right), \tag{28}$$

where  $R_i|_{DS}$  and  $R_i|_{WT}$  represent the one-way propagation range from dominant scatterer and weak target to *i*-th radar.

In a given MMW DCAR configuration, the relative relationship of the compensated phase deviations can be derived as

$$\begin{cases}
\Delta \varphi'_{1n}|_{DS \to WT} = \Delta \varphi'_{n1}|_{DS \to WT} \\
\Delta \varphi'_{mn}|_{DS \to WT} = \Delta \varphi'_{1m}|_{DS \to WT} + \Delta \varphi'_{1n}|_{DS \to WT} \\
\Delta \varphi'_{nn}|_{DS \to WT} = 2 \times \Delta \varphi'_{1n}|_{DS \to WT}.
\end{cases}$$
(29)

Thereafter, we analyzed and derived the signal power after CoRS. Herein, it is assumed that multi-channel signals after compensation have the same amplitude and only the phase deviations. For the MMW DCAR composed of N unit radars, the signal power of  $N^2$  channels after CoRS can be expressed as

$$P_{CoRS} = \left[exp(j\Delta\varphi'_{11}|_{DS \to WT}) + \dots + exp(j\Delta\varphi'_{mn}|_{DS \to WT}) + \dots + exp(j\Delta\varphi'_{NN}|_{DS \to WT})\right]^{2}$$

$$= \left[\sum_{m=1}^{N} \sum_{n=1}^{N} exp(j\Delta\varphi'_{mn}|_{DS \to WT})\right]^{2}$$

$$= \left|\left[\sum_{m=1}^{N} exp(j\Delta\varphi'_{1m}|_{DS \to WT})\right] \times \left[\sum_{n=1}^{N} exp(j\Delta\varphi'_{1n}|_{DS \to WT})\right]\right|^{2}$$

$$= \left[\sum_{m=1}^{N} exp(j\Delta\varphi'_{1m}|_{DS \to WT})\right]^{4}.$$
(30)

Correspondingly, the theoretical signal power after synthesis, in which each channel is aligned to the reference channel, can be denoted as

$$P_{Opt} = \left[\sum_{m=1}^{N} \sum_{n=1}^{N} \left[ exp(j\Delta \varphi'_{11}|_{DS \to WT}) \right] \right]^2 = N^4.$$
(31)

Due to the phase deviations, there is a certain gain loss. We define the acceptable synthetic gain loss as  $P_{GL}$ , which can be expressed as

$$P_{CoRS} \ge P_{Opt} - P_{GL}$$

$$\Leftrightarrow \left[\sum_{m=1}^{N} exp(j\Delta \varphi'_{1m}|_{DS \to WT})\right]^{4} \ge \left(10^{-P_{GL}/10}\right) \times N^{4}$$

$$\Leftrightarrow \left[\sum_{m=1}^{N} exp(j\Delta \varphi'_{1m}|_{DS \to WT})\right]^{2} \ge \left(10^{-P_{GL}/20}\right) \times N^{2}.$$
(32)

According to the Euler formula, it can be rewritten as

$$\left[\sum_{m=1}^{N} exp(j\Delta\varphi'_{1m}|_{DS\to WT})\right]^{2} \ge \left(10^{-P_{GL}/20}\right) \times N^{2}$$

$$\Leftrightarrow \left[\left(\sum_{m=1}^{N} \cos(\Delta\varphi'_{1m}|_{DS\to WT})\right) + j\left(\sum_{m=1}^{N} \sin(\Delta\varphi'_{1m}|_{DS\to WT})\right)\right]^{2} \ge \left(10^{-P_{GL}/20}\right) \times N^{2}$$

$$\Leftrightarrow N + \sum_{m=1}^{N} \sum_{n\neq m}^{N} \cos(\Delta\varphi'_{1m}|_{DS\to WT} - \Delta\varphi'_{1n}|_{DS\to WT}) \ge \left(10^{-P_{GL}/20}\right) \times N^{2}.$$
(33)

By solving the inequality equation, Equation (33), we can obtain a certain phase tolerance. This tolerance is defined as the maximum acceptable phase difference between any two channels and can be derived as

$$\forall m, n, (N^2 - N) \cos(\Delta \varphi'_{1m}|_{DS \to WT} - \Delta \varphi'_{1n}|_{DS \to WT}) \ge (10^{-P_{GL}/20}) \times N^2 - N$$
  
$$\Rightarrow \quad \forall m, n, |\Delta \varphi'_{1m}|_{DS \to WT} - \Delta \varphi'_{1n}|_{DS \to WT}| \le \arccos\left(\frac{(10^{-P_{GL}/20}) \times N^{-1}}{N^{-1}}\right) = \varphi_{Tole}.$$
(34)

This phase tolerance is a discrete phase value, that is used to guide the compensation of each channel. For an arbitrary channel, we can cyclically compensate a phase value to satisfy

the derived tolerance. Within the phase region  $[-\pi, \pi]$ , the number of compensations can be denoted as

$$Num_{correct} = \lceil \pi / \varphi_{Tole} \rceil, \tag{35}$$

and the value for each compensation can be expressed as

Ν

$$\varphi_{correct} = \frac{2k_{\varphi}\pi}{\left\lceil \pi/\varphi_{Tole} \right\rceil}, k_{\varphi} = 0, 1, \cdots, \left\lceil \pi/\varphi_{Tole} \right\rceil - 1.$$
(36)

It should be noted that only the channels from 1T2R to 1TNR are required to be compensated. Owing to the relationship, as in Equation (29), the remaining channels can be compensated adaptively. Therefore, the total number of compensations for *N* unit radars can be deduced as

$$Num_{All} = (Num_{correct})^{N-1} = (\lceil \pi / \varphi_{Tole} \rceil)^{N-1}.$$
(37)

Utilizing the proposed method, the phases of the weak target can be aligned in one of the sets of compensations. This method can simultaneously align the phase of targets located in a certain region based on the phase relationship between multiple unit radars. Hence, it can significantly reduce the number of compensations, and there is no need for the spatial position of other targets.

## 3.4. Selection of Dominant Scatterer

The dominant scatterer in this work is defined as an unknown target with strong scattering points in radar detection scenarios, such as vehicles, signs, etc. Its selection may directly affect the synthetic performance of other targets. Therefore, we focused on analyzing the selection criteria and procedure of the dominant scatterer.

The constraints of the proposed method will vary with the positions of the dominant scatterer, and the synthetic gain of weak targets also relies on the dominant scatterer's SNR. In this regard, we defined the constraints using the dominant scatterer and performed the simulations on the influence of the dominant scatterer position and SNR. The selection criteria and procedure can be obtained from the results.

# 3.4.1. Analysis of Constraints

In Section 3.2, we derived and analyzed the deviations in range and velocity after compensation using the dominant scatterer. These two deviations may lead to the failure of the proposed method. This means that the compensations using the dominant scatterer are valid for a certain region, as depicted in Figure 4. Specifically, we defined the constraint that the deviations could not exceed half of a resolution cell after compensation.



Figure 4. Conceptual diagram of constraints for the compensation using the dominant scatterer.

For the purpose of simplification, the MMW DCAR used in this work was considered a rigid system. Namely, the relative motion states of multi-unit radars can be considered constant. On this basis, a typical scenario composed of the MMW DCAR and two targets is displayed in Figure 5. The specific constraints in this scenario are derived as follows.



Figure 5. Geometric diagram of the DCAR and multi-target.

The compensated signals of the weak target should be focused on the same range cell in each channel, which can be expressed as

$$\Delta R_{mn} \Big|_{DS \to WT} = \left| \frac{R_{mn}|_{WT} - R_{mn}|_{DS} + R_{11}|_{DS} - R_{11}|_{WT}}{2} \right| \le \frac{R_{res}}{2},$$
(38)

where  $R_{res}$  represents the range resolution. As shown in Figure 5, the coordinates of the weak target are required to meet the first constraint, which can be further deduced as

$$\begin{vmatrix} \sqrt{(R_{x2}-l_1)^2 + R_{y2}^2} + \sqrt{(R_{x2}-l_2)^2 + R_{y2}^2} - 2\sqrt{R_{x2}^2 + R_{y2}^2} \\ -\sqrt{(R_{x1}-l_1)^2 + R_{y1}^2} - \sqrt{(R_{x1}-l_2)^2 + R_{y1}^2} + 2\sqrt{R_{x1}^2 + R_{y1}^2} \end{vmatrix} \le R_{res}.$$
 (39)

Similarly, the compensated signal must be focused on the same velocity cell, which can be denoted as

$$\Delta V_{mn}|_{DS \to WT} = \left| \frac{v_{mn}|_{WT} - v_{mn}|_{DS} + v_{11}|_{DS} - v_{11}|_{WT}}{2} \right| \le \frac{V_{res}}{2}, \tag{40}$$

where  $V_{res}$  represents the velocity resolution. Then, we can derive the second constraint for the weak target as

$$\left(\frac{R_{y2}}{\sqrt{(R_{x2}-l_{1})^{2}+R_{y2}^{2}}}+\frac{R_{y2}}{\sqrt{(R_{x2}-l_{2})^{2}+R_{y2}^{2}}}-\frac{2R_{y2}}{\sqrt{R_{x2}^{2}+R_{y2}^{2}}}\right)v_{2} \\
-\left(\frac{R_{y1}}{\sqrt{(R_{x1}-l_{1})^{2}+R_{y1}^{2}}}+\frac{R_{y1}}{\sqrt{(R_{x1}-l_{2})^{2}+R_{y1}^{2}}}-\frac{2R_{y1}}{\sqrt{R_{x1}^{2}+R_{y1}^{2}}}\right)v_{1}\right| \leq V_{res}.$$
(41)

Furthermore, due to the shift of the range spectrum caused by the synchronization errors, the proposed method requires that the multi-target in all channels must be within the observation region after translation, which can be denoted as

$$\forall m, n, 0 < \hat{R}_{mn} < R_{max}, \tag{42}$$

where  $R_{max}$  is the maximum observation in the range spectrum. Hence, the third constraint can be derived as

$$\forall m, n, \begin{cases} R - \left| \frac{c\Delta T_{mn}}{2} - \frac{c\Delta f_{mn}}{2k} \right| > 0\\ R + \left| \frac{c\Delta T_{mn}}{2} - \frac{c\Delta f_{mn}}{2k} \right| < R_{max} \end{cases} \Leftrightarrow \left| \frac{c\Delta T_{mn}}{2} - \frac{c\Delta f_{mn}}{2k} \right| < R < R_{max} - \left| \frac{c\Delta T_{mn}}{2} - \frac{c\Delta f_{mn}}{2k} \right|. \tag{43}$$

In summary, the compensations for weak targets are valid for a certain region that relies on the position and velocity of the dominant scatterer. We performed the simulations on this in the next subsection to analyze the selection criteria for the dominant scatterer.

# 3.4.2. Selection Criteria

We performed the simulations to determine the influence of the dominant scatterer position and SNR. The selection criteria and procedure can be obtained from the results.

The comparison tests are composed of four scenarios in which the dominant scatterer is located in different positions, as given in Table 1. Moreover, the parameters of the MMW DCAR configuration and the weak target traversal region are presented in Table 2.

Table 1. Parameters of the dominant scatterer position.

Parameters	Test 1	Test 2	Test 3	Test 4
Cross range	0 m	-10  m	0 m	0 m
Radial range	60 m	60 m	150 m	60 m
Velocity	20 m/s	20 m/s	20 m/s	-5  m/s

**Table 2.** Parameters of the MMW DCAR configuration and weak target.

	Parameter	Value
	Carrier frequency	77 GHz
	Range resolution	0.5 m
MMW DCAR	Velocity resolution	0.3 m/s
	Number of radars	3
	Radar spacing	0.3 m/0.2 m
	Traversal region in cross range	[-15 m 15 m]
	Traversal region in radial range	[10 m 210 m]
Weak Target	Traversal region in velocity	[-10  m/s 10  m/s]
weak larget	Traversal interval in cross range	0.15 m
	Traversal interval in radial range	1 m
	Traversal interval in velocity	0.2 m/s

According to Equations (21) and (22), the deviations in range and velocity are calculated and depicted in Figures 6–9. The effective regions, satisfying the constraint that the deviations cannot exceed half of a resolution cell after compensation, are also presented. The part marked in red corresponds to the effective region, which covers the majority of radar detection scenarios. This means that the proposed method can be effectively adapted to many applications.



**Figure 6.** The simulation results of Test 1. (**a**,**b**) display the range and velocity deviations. (**c**) represents radar detection scenario, including effective region (red) and ineffective region (gray).



**Figure 7.** The simulation results of Test 2. (**a**,**b**) display the range and velocity deviations. (**c**) represents radar detection scenario, including effective region (red) and ineffective region (gray).



**Figure 8.** The simulation results of Test 3. (**a**,**b**) display the range and velocity deviations. (**c**) represents radar detection scenario, including effective region (red) and ineffective region (gray).



**Figure 9.** The simulation results of Test 4. (**a**,**b**) display the range and velocity deviations. (**c**) represents radar detection scenario, including effective region (red) and ineffective region (gray).

As shown in Figures 6–9, it is apparent that the radial range and velocity of the dominant scatterer have a negligible impact on the effective region. On the contrary, the deviations will increase with the cross range, and the corresponding effective region will reduce significantly, as shown in Table 3. Therefore, the first criterion is that the dominant scatterer should be close to the normal direction of MMW DCAR, i.e., its azimuth should be relatively small.

Table 3. The proportion satisfying the constraints.

	Test 1	Test 2	Test 3	Test 4
Proportion	93.58%	89.84%	93.57%	93.58%

The dominant scatterer in this work is a non-cooperative target, which may have multiple scattering points at a short range [40]. The CP estimations require scattering point matching; the multiple scattering points can lead to mismatching and a negative estimation. Thus, we recommend choosing a target with a medium- or long-range as the dominant scatterer, which is the second selection criterion.

Furthermore, the dominant scatterer's SNR determines the accuracy of the CP estimations, which potentially has an essential impact on the synthetic performance of weak targets. In this regard, we performed the simulations on the synthetic gain loss of the weak target with respect to the dominant scatterer's SNR. The dominant scatterer SNR was set from 10 dB to 25 dB with a 1 dB interval, and 1000 Monte Carlo simulations were performed for each SNR.

The simulation results are displayed in Figure 10. As the dominant scatterer's SNR increases, the synthetic performance of the weak target is enhanced. In particular, the synthetic performance tends to be stable with an SNR higher than 13 dB. Hence, the third criterion is to choose one of the targets with a higher SNR as the dominant scatterer. For a scenario containing multiple high SNR targets, these targets can all be used as the dominant scatterer, and can then be further refined using the above two criteria.





In summary, the dominant scatterer in the paper can be defined as a medium- or long-range target that is close to the radar's normal direction. Moreover, its SNR should be as higher than 13 dB as possible. According to these selection criteria, the selection procedure of the dominant scatterer in practice is illustrated in Figure 11.



Figure 11. The selection procedure of the dominant scatterer, where *Th* is set to 13 dB in this paper.

## 3.5. Derivation of Theoretical Synthetic SNR

SNRs in multiple unit radars may be different due to the influence of noise. Hence, to evaluate the proposed method, the theoretical synthetic SNR is required to be derived as follows.

Assuming that the signal amplitude and noise power in channel mTnR are  $K_{mn}$  and  $P_{mn}$ , the target SNR can be expressed as

$$SNR_{mn} = K_{mn}^2 / P_{mn}.$$
(44)

Thereafter, the theoretical signal amplitude after CoRS is the sum of the signal amplitude in each channel, which is expressed as

$$A_{sig} = \sum_{m=1}^{N} \sum_{n=1}^{N} K_{mn}$$
(45)

Similarly, the accumulated noise power after CoRS can be denoted as

$$P_{Noise} = \sum_{m=1}^{N} \sum_{n=1}^{N} P_{mn}.$$
(46)

Therefore, the theoretical SNR can be obtained as

$$SNR_{theory} = A_{sig}^2 / P_{Noise} = \left(\sum_{m=1}^N \sum_{n=1}^N K_{mn}\right)^2 / \sum_{m=1}^N \sum_{n=1}^N P_{mn}.$$
 (47)

Let  $\gamma_{mn} = P_{mn}/P_{11}$ , which indicates the noise power ratio of the channel *m*T*n*R to the reference channel. Thereby, we can rewrite Equation (47) as

$$SNR_{Theory} = \frac{1}{\sum\limits_{m=1}^{N}\sum\limits_{n=1}^{N}\gamma_{mn}} \times \frac{1}{P_{mn}} \times \left(\sum\limits_{m=1}^{N}\sum\limits_{n=1}^{N}K_{mn}\right)^{2}$$

$$= \frac{1}{\sum\limits_{m=1}^{N}\sum\limits_{n=1}^{N}\gamma_{mn}} \times \left(\sum\limits_{m=1}^{N}\sum\limits_{n=1}^{N}\sqrt{\gamma_{mn}} \times \sqrt{SNR_{mn}}\right)^{2}.$$
(48)

## 4. Simulations

We assessed the proposed method via simulations and present an analysis thereof. A typical scenario composed of one dominant scatterer and two weak targets was set up. The synthetic performance of all targets in continuous CPIs is presented, and the specific results are discussed within a single CPI. Moreover, the proposed method is also compared with the noncoherent integration method in terms of detection improvement.

## 4.1. CoRS for Multiple Targets

The simulation scenario is composed of three targets, the parameters of which are given in Table 4. The used MMW DCAR consists of three unit radars. It is important to note that the acceptable synthetic gain loss is defined as 3 dB in simulation. Therefore, the phase tolerance can be calculated as 27.9° according to Equation (34). Additionally, the compensation number for each channel and the MMW DCAR can be deduced as 7 times and 49 times, respectively.

#### 4.1.1. Synthetic Results in Continuous CPIs

Utilizing the proposed method, the synthetic results of different targets in continuous CPIs are illustrated in Figure 12. Herein, the theoretical SNR, as in Equation (48), was used as a guideline for evaluation.

Since the multidimensional parameters of the dominant scatterer can be aligned with its own estimated CPs, the synthetic results in Figure 12a are consistent whether adaptive phase compensation is employed or not. However, due to the phase deviation, the synthetic performance of weak targets will decline significantly when using the dominant scatterer compensation only, as illustrated in Figure 12b,c. Instead, the synthetic results of weak targets can be effectively improved with the proposed method. Particularly, the maximum gain loss of these targets is 1.9 dB, which satisfies the definition.

Table 4. Parameters of multiple targets.

Target Classification	Parameters	Value		
	Cross range	-3 m		
	Radial range	45 m		
Dominant Scatterer	Radial velocity	-9  m/s		
	SNR	15 dB		
	Cross range	0 m		
First West Target	Radial range	30 m		
Flist Weak larget	Radial velocity	3 m/s		
	SNR	4 dB		
	Cross range	3 m		
Second Week Target	Radial range	55 m		
Second Weak Target	Radial velocity	-2  m/s		
	SNR	3 dB		



**Figure 12.** Multi-target coherent-on-receive synthesis results in consecutive CPIs. (**a**) Results of the dominant scatterer. (**b**) Results of the first weak target. (**c**) Results of the second weak target.

# 4.1.2. Synthetic Results within a Single CPI

To demonstrate the synthetic performance, the simulation results of the 10th CPI are presented in Figures 13–15. Due to the synchronization errors, these targets focused on different range cells in multi-channel, as illustrated in Figure 13. The echoes can be calibrated with the estimated CPs of the dominant scatterer. Figure 14 shows that the deviations caused by the synchronization errors were eliminated, and thereby the multi-target was aligned in the range spectrum. From Figure 15a, the dominant scatterer can be synthesized effectively, while the weak targets suffer a great loss due to the phase deviation. Utilizing the proposed method, the weak targets can achieve CoRS with adaptive phase compensation, as shown in Figure 15b,c.

To specifically verify the effectiveness of the proposed method, Table 5 gives the numerical comparison results. Since the signal discreteness in FFT processing causes a fence effect, the targets' SNRs have a slight variation after compensation using estimated CPs. It is verified that the targets' SNRs in multi-channels do not change significantly, and thus their impact can be neglected in the actual processing.



**Figure 13.** The range spectra of the original beat signal in multi-channel. (**a**–**i**) are the channels 1T1R to 3T3R, respectively.



Figure 14. The range spectra after dominant scatterer compensation.



Figure 15. Multi-target CoRS results via the proposed method. (a) Results of the dominant scatterer.(b) Results of the first weak target. (c) Results of the second weak target.

Tab	le 5.	The nur	nerical c	omparison	results	(dB)	of simul	lations.
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	Description	Channels								
	Parameters	1T1R	1T2R	1T3R	2T1R	2T2R	2T3R	3T1R	3T2R	3T3R
	Noise power	30.2	29.1	30.0	29.9	30.0	30.0	30.1	29.1	29.9
Original	Dominant scatterer SNR	16.4	16.2	15.1	16.3	14.3	15.7	15.2	16.1	14.9
signal	First weak target SNR	2.9	5.3	4.1	4.0	3.7	3.8	3.2	5.7	4.2
-	Second weak target SNR	2.4	3.0	1.8	4.3	3.5	2.7	2.2	4.8	2.0
	Noise power	30.2	29.4	30.0	29.5	30.0	29.6	29.8	29.1	29.9
Compensated	Dominant scatterer SNR	16.4	15.9	15.1	16.7	14.3	16.1	15.5	16.1	14.9
signal	First weak target SNR	2.9	5.0	4.1	4.4	3.7	4.2	3.5	5.7	4.2
	Second weak target SNR	2.4	2.7	1.8	4.7	3.5	3.1	2.5	4.8	2.0
The second second	Dominant scatterer					25.1				
Ineoretical	First weak target	13.6								
SNK	Second weak target	12.5								
Proposed method	Dominant scatterer	24.9 (Gain loss: 0.2 dB)								
	First weak target	11.7 (Gain loss: 1.9 dB)								
	Second weak target	10.8 (Ga					oss: 1.7 dB)			

For the dominant scatterer, its synthetic SNR is 24.9 dB, with a gain loss of 0.2 dB compared to the theoretical result. Additionally, with the proposed method, the SNR gain losses of two weak targets are 1.9 dB and 1.7 dB, respectively. In summary, it is demonstrated that these targets can match the defined acceptable synthetic gain loss well. Namely, multi-target can be effectively synthesized, thus improving the target SNR and enhancing the radar detection performance significantly.

## 4.2. Detection Performance Comparison

The feasibility of the proposed method was further evaluated with the constant false alarm detection (CFAR) algorithm [41–43]. We compared it with the noncoherent integration method based on the square law detector [44,45]. Herein, the dominant scatterer with SNR = 20 dB was fixed, and a weak target was randomly generated in the radar detection region that satisfies the constraints, with the weak target's SNR in a single channel set from 0 dB to 20 dB. We performed the Monte Carlo simulations 1000 times via different methods, which are demonstrated in Figure 16.

Compared with using a single channel, using two types of synthesis methods can improve the detection performance. However, the noncoherent integration method suffers a great loss in the case of a low SNR. As the SNR increases, this method can enhance target detection, with a maximum gain of approximately 3.5 dB. On the contrary, the proposed method is stable at both high and low SNR conditions. With an equivalent detection probability, the proposed method improves by approximately 9 dB.



Figure 16. Detection performance utilizing CFAR algorithm with 1000 Monte Carlo simulations.

#### 5. Experiments

The proposed CoRS method using the dominant scatterer was verified by measurements in a typical urban environment. The prototype system was fabricated, and the hardware components of the MMW DCAR are presented.

The prototype system in this work is composed of three radars with an operating frequency range of 76.0 GHz to 81.0 GHz. It employs a wired trigger, which is generated by a separate signal source and provides a trigger pulse to the radars with cables of equal length. An overview of the basic parameters of these radars is given in Table 6.

Table 6. Parameters of the test radars.

Parameter	Value
Center frequency	77.0 GHz
Bandwidth	200 MHz
Chirp duration	40 µs
Pulse repetition time	48 µs
IF bandwidth	12.5 MHz
Clock frequency	80 MHz

In the prototype system, a certain timing difference between the high levels of the trigger pulse at the radars is unavoidable because of the imperfect electrical length of the lines. Since each radar is independent, there may be an uncertain timing difference when their internal clocks detect the trigger pulse. The combined timing difference is the main factor that contributes to the arbitrary initial time delay. Furthermore, these independent unit radars are also subject to random deviations in carrier frequency and phase.

The prototype system, which contains three MMW radars and a wired trigger, is displayed in Figure 17. The test scenario consisted of a vehicle as the dominant scatterer and a pedestrian as the weak target.

With the time-division method, the multi-channel signals can be separated at each receiver. The range–Doppler spectra are presented in Figure 18. Clearly, due to the system synchronization errors, the focus positions are offset, which can be calibrated with the dominant scatterer.



Figure 17. The prototype system and the test scenario consisting of a vehicle and a pedestrian.



**Figure 18.** The range–Doppler spectra of multi-channel with real data. (**a**–**i**) are the channels 1T1R to 3T3R, respectively.

In the real-data experiment, the vehicle had two strong scattering points. We chose the stronger scattering point as the dominant scatterer of the proposed method. The optimal synthetic results for the vehicle and the pedestrian are demonstrated in Figure 19a,b, respectively.



**Figure 19.** The optimal CoRS results in multiple-phase compensation groups. (**a**) Results of the vehicle. (**b**) Results of the pedestrian.

The numerical comparison results from the real-data experiment are given in Table 7. The theoretical SNR of the stronger scattering point after synthesis is calculated at 33.2 dB, while the actual SNR can be improved to 32.0 dB. For weak scattering points, the CoRS can be realized by using the estimated CPs only. Its theoretical and actual SNR after synthesis are 27.2 dB and 26.2 dB, respectively. The pedestrian is also synthesized with the proposed method, and its theoretical and actual SNR after synthesis can be calculated as 23.8 dB and 21.6 dB. Additionally, it should be noted that several stationary targets including signs and streetlights can also be effectively synthesized, as shown in Figure 19. To sum up, the proposed method satisfies the defined acceptable synthetic gain loss (3 dB) for each target, which can enhance the target SNR effectively.

	<b>D</b> (		Channels							
	Parameters	1T1R	1T2R	1T3R	2T1R	2T2R	2T3R	3T1R	3T2R	3T3R
	Noise power	89.2	88.6	87.8	89.8	89.4	88.5	88.8	89.0	87.9
Original	Vehicle Point 1 SNR	21.3	22.3	23.9	23.8	24.3	23.5	24.4	23.5	25.4
signal	Vehicle Point 2 SNR	16.1	13.3	15.6	19.8	19.3	16.5	12.8	20.4	20.8
	Pedestrian SNR	14.4	12.6	12.5	16.5	16.6	14.1	11.6	13.8	14.8
	Vehicle Point 1	33.2								
Theoretical	Vehicle Point 2	27.2								
SNR	Pedestrian	23.8								
Proposed method	Vehicle Point 1	32.0 (Gain loss: 1.2 dB)								
	Vehicle Point 2	26.2 (Gain loss: 1.0 dB)								
	Pedestrian	21.6 (Gain loss: 2.2 dB)								

Table 7. The numerical comparison results (dB) with real data.

Furthermore, the power near the zero frequency in the Doppler spectrum is higher than that at other frequencies. This is caused by the ground clutter and some stationary targets (e.g., trees, curbs, etc.) in the urban environment. As illustrated in Figures 18a and 19a, the signal power in this part is 97.9 dB and 109.1 dB, with 11.2 dB of gain. It is well known that the ideal synthetic gain for targets is approximately 19.0 dB, while the gain for noise is 9.5 dB. Consequently, the gain of clutter is intermediate between the noise and the target, which may have a negative impact on the improvement of the proposed method for stationary targets.

# 6. Conclusions

This paper describes a millimeter-wave distributed coherent aperture radar that can be used to improve the target SNR by coherent-on-receive synthesis. The synchronization errors are calibrated with the estimated coherent parameters of the dominant scatterer, which can be defined as an unknown strong target in radar detection scenarios. We focused on the selection criteria of the dominant scatterer by analyzing the constraints of the proposed method. Furthermore, an adaptive compensation approach was further explored to expand the available region for the estimated CPs of the dominant scatterer. This approach can compensate for the phases of different targets within multiple-unit radars using discrete phase values. The determination of discrete phase values is derived from the limit of synthesis loss within a given MMW DCAR configuration. Hence, this approach avoids massive searches for possible locations of other targets and the requirement of prior information.

The presented theory and the corresponding method were evaluated via extensive simulations and experiments. The constraints and limitations of the system were verified to meet the application requirements. Utilizing the proposed method, multi-target can achieve the desired synthetic results in sequential CPIs. Compared with the noncoherent integration method, the proposed method is stable at both high and low SNR conditions, yet with a higher SNR gain. Furthermore, a prototype system was fabricated and used to verify the proposed method. The experiment results match well with the simulations, showing the efficacy of the proposed method.

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