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Integrated UAV-Based Multi-Source Data for Predicting Maize Grain Yield Using Machine Learning Approaches

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Abstract: Increases in temperature have potentially influenced crop growth and reduced agricultural yields. Commonly, more fertilizers have been applied to improve grain yield. There is a need to optimize fertilizers, to reduce environmental pollution, and to increase agricultural production. Maize is the main crop in China, and its ample production is of vital importance to guarantee regional food security. In this study, the RGB and multispectral images, and maize grain yields were collected from an unmanned aerial vehicle (UAV) platform. To confirm the optimal indices, RGB-based vegetation indices and textural indices, multispectral-based vegetation indices, and crop height were independently applied to build linear regression relationships with maize grain yields. A stepwise regression model (SRM) was applied to select optimal indices. Three machine learning methods including: backpropagation network (BP), random forest (RF), and support vector machine (SVM) and the SRM were separately applied for predicting maize grain yields based on optimal indices. RF achieved the highest accuracy with a coefficient of determination of 0.963 and root mean square error of 0.489 (g/hundred-grain weight). Through the grey relation analysis, the N was the most correlated indicator, and the optimal ratio of fertilizers N/P/K was 2:1:1. Our research highlighted the integration of spectral, textural indices, and maize height for predicting maize grain yields.

Keywords: maize grain yield; unmanned aerial vehicle (UAV); vegetation indices and textural indices; machine learning



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1. Introduction

Climate change has significantly influenced the growth of crops, thus reducing agricultural yields and threatening food security [1–3]. Maize is one of the three staple foods, and timely prediction of maize grain yield is essential for ensuring food security [4]. Farmers usually apply more fertilizers to improve agricultural production per unit of arable land, and therefore, reduce the negative impacts from climate change. Currently, the main challenge in agriculture is to feed the present and future generations by increasing agricultural production while caring for the valuable environment [5]. Excessive application of fertilizers does not improve agricultural production, and it does increase environmental risks and reduce the biodiversity of agricultural environments [6]. Therefore, timely prediction of maize grain yields is essential for selecting new cultivars for breeding, for optimizing fertilizer applications, and further, for guaranteeing regional food security by timely allocating food [7]. Optimizing the proper amounts of fertilizers and adjusting in-season fertilization would help to achieve sustainable agriculture.

So far, the common approaches for yield predictions are destructive sampling, the use of a deterministic crop simulation model, and the use of empirical relationships built using remote sensing platforms [8]. Destructive sampling is the most precise method for yield prediction, but it is labor intense since it is difficult to perform at a large scale within a limited time period. A crop simulation model can simulate the soil–plant–climate–agronomy interactions and can help to quantify factors impacting crop production with accurate climatic forecasts [9]. A simulation model also needs detailed site-specific input data such as soil property, cultivar, and daily weather information, which are very difficult to collect [10]. Alternatively, empirical methods based on satellite-based remote sensing (SRS) have achieved a good level of yield prediction. However, SRS is often limited by weather conditions, coarse spatial resolutions, and its limited applicability beyond the year in which the empirical relationship is developed [11,12]. Images of important phenological stages are hard to acquire as the limitation of traditional satellite remote sensing such as long-time revisit and coarse spatial resolution [13]. Fortunately, with the development of light sensors and wireless communication technology, unmanned aerial vehicle (UAV) platforms have attracted great attention due to their advantages of light weight, ease of deployment, and cloudless, and therefore, they have become alternatives to SRS [14–17].

UAVs mounted with multi-sensors can be applied to acquire images covering the entire growth stages of maize in a short time period. The high-throughput data can be used to analyze the impacts of climate and management practices on crop yield.

Vegetation indices (VIs) are commonly applied for monitoring growth conditions and predicting agricultural yields. For example, the normalized difference vegetation index (NDVI), ratio of vegetation index (RVI), and difference index (DI) have been commonly applied for predicting rice grain yields [18]. Varieties of VIs calculated from both RGB images and multispectral images have been evaluated to confirm the optimal applications of N [19]. The currently applied VIs have commonly been influenced by the problem of saturation, and thus, they have failed to detect crop sensitivity to dynamic environmental and climatic changes. Especially, the most commonly applied VIs have low accuracies in monitoring growth conditions during the reproductive stages [20]. In addition, the potentials of textural indices (TIs) such as contrast, correlation, energy, and homogeneity for predicting maize grain yield have been less reported [21,22]. Therefore, there is a need to investigate the potential ability of VIs, TIs, and crop phenotype for timely and precise maize yield predictions.

Machine learning methods have commonly been applied in remote sensing domains for image classification and regression. The SPAD values of maize have been precisely monitored using machine learning methods, namely, support vector machine (SVM) and random forest (RF) [23]. The MRBVI has been proposed to estimate SPAD values, and the index with other commonly applied indices has performed well for predicting maize grain yield using backpropagation neural network model (BP), SVM, RF, and extreme learning machine (ELM) [7]. Various machine learning methods including ridge regression (RR), SVM, RF, Gaussian process (GP), and K-neighbor network (K-NN) have been applied for predicting the leaf area index, as well as the fresh weight and dry weight of maize, and the results have shown relatively high accuracy [24]. Multi-source environmental data applied with machine learning methods (i.e., SVM and RF) have been adopted to predict wheat yield in China, and the results indicated that the RF achieved the highest accuracy [25].

To date, only a few studies have explored the integration of multi-indicators (i.e., RGB-based VI, multispectral-based indices, RGB-based textural indices, and crop height) for predicting maize grain yields. In this paper, RGB-based VIs, RGB-based TIs, multispectral-based VIs, and maize height were innovatively applied to predict maize grain yield using traditional regression method and machine learning approaches. The main objectives were: (1) to evaluate the potential ability of VIs, TIs, and crop phenotype (maize height) for predicting maize grain yields; (2) to confirm optimal indices for predicting maize grain yield prediction; (3) to predict maize grain yields based on the integrated indices using

machine learning methods; (4) to confirm the most optimal amounts and ratios of N, P, and K for achieving sustainable agriculture.

2. Materials and Methods

2.1. Study Area

The data collection was conducted in Nanpi Eco-Agricultural Experimental Station (NEES) (38.00°N , 116.40°E) in 2019 (Figure 1). The maize cultivar (Zhengdan 958) was planted on 22 June 2019, and different amounts N, P, and K were applied on 20 plots to optimize the usage of different varieties of fertilizers. One-third of the fertilizers were treated ten days after emergence, another one-third of the fertilizers were treated at booting date, and the remaining fertilizers were treated at heading date (Table A1).

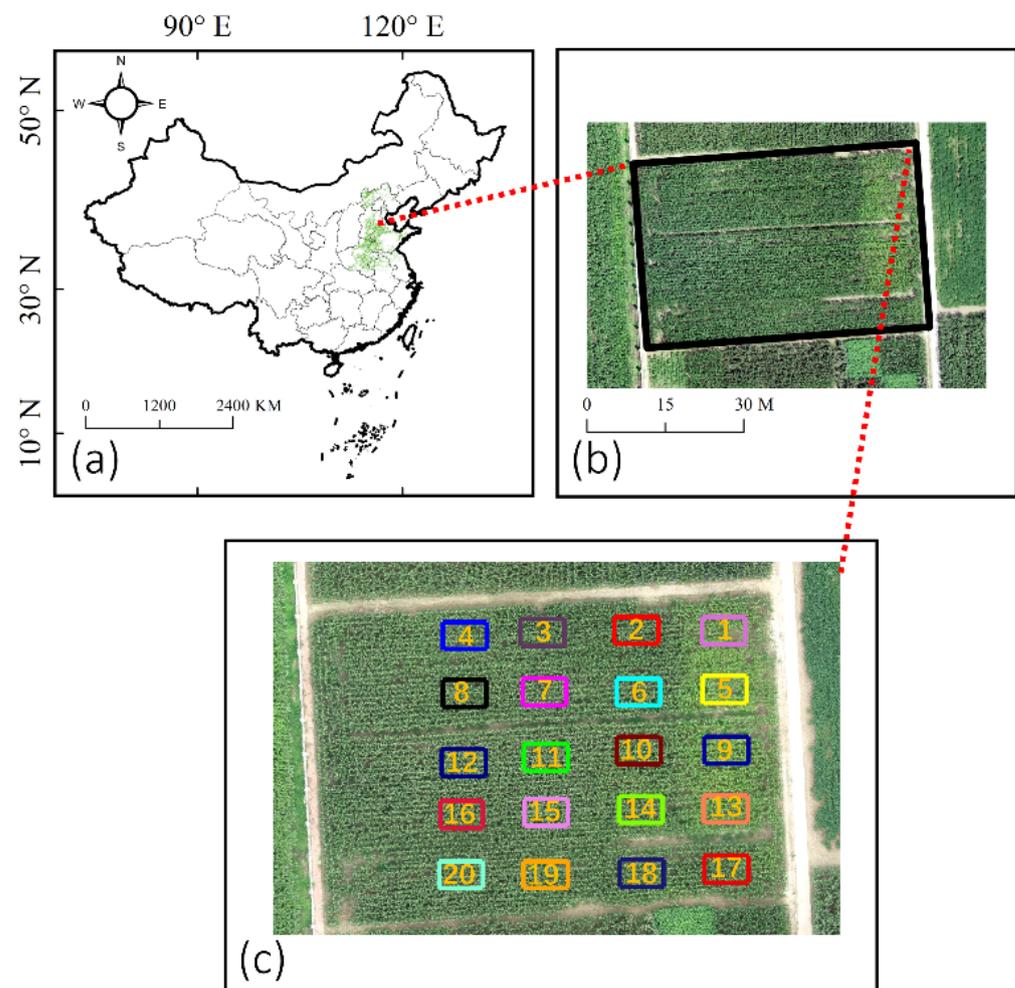


Figure 1. The geo-location of the Nanpi Eco-Agricultural Experimental Station (NEES) and the detailed setting of 20 plots with different treatments of fertilizers. (a) the geographical location of experimental station, (b) the study area from UAV view, (c) the 20 plots for image clipping.

In this study, a DJI Phantom 4 Pro V2.0 was applied for collecting RGB images, and a Mini MCA 6 Camera (MMC) mounted on a DJI M600 Pro UAV platform was conducted to collect multispectral images (Figure 2). The detailed information of the cameras and the deployment of data collection were introduced in previous studies [7,14,26].

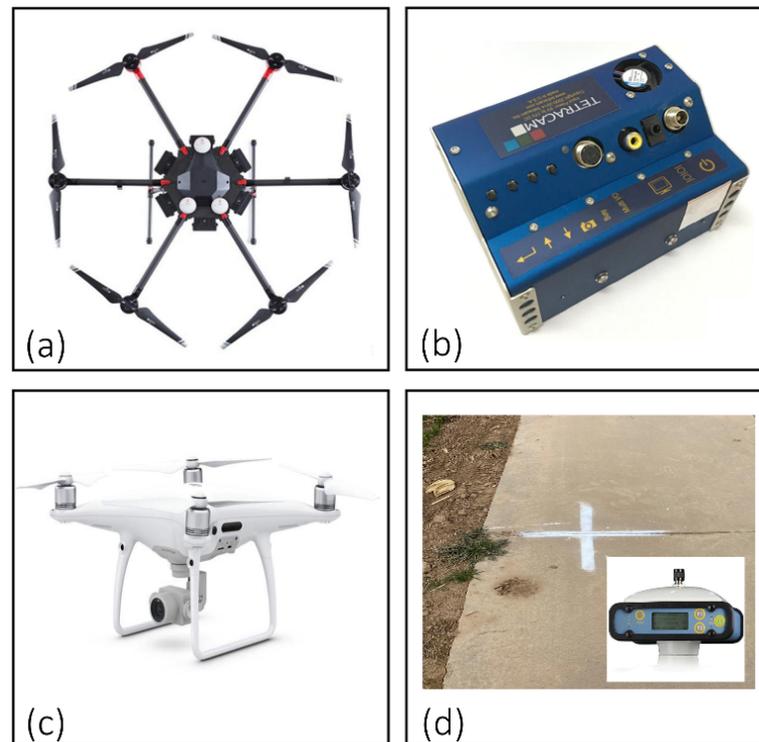


Figure 2. The UAV and cameras applied for data collection: (a) DJI M600 Pro UAV; (b) Mini MCA 6 Camera; (c) DJI Phantom 4 Pro V2.0; (d) ground control points.

2.2. Data Collection and Preprocessing

During the entire growth stages of maize, the images were collected on cloudless weather conditions between 11:30 and 12:30 (local time). The maize was seeded on 22 June 2019 and harvested on 5 October 2019; 173 and 278 were the corresponding day of year (DOY), respectively. For the UAV image collection, data collection of the DJI Phantom 4 Pro V2.0 were applied on 188, 195, 203, 209, 230, 237, 244, 250, 257, 264, and 273 DOY and data collection of the MMC were applied on 230, 237, 250, 258, 264, and 273 DOY. To ensure high quality of image acquisition, the forward and side overlaps were set as 85 and 80% for the RGB images acquisition, and 80 and 70% were set for the multispectral image acquisition. Four ground control points (GCPs) were pre-set before the growing season, and the precise locations were obtained using a real-time kinematic (RTK) S86T system (Figure 2d) [23,27]. The single RGB images and multispectral images of each flight were independently mosaicked and processed within Pix4D Mapper under a standard procedure (Lausanne, Switzerland) [28,29]. The images were clipped within IDL (version 8.5) [30]. The spatial resolution of RGB images and multispectral images were 1 and 5 cm, respectively.

Maize grain yields of 20 plots were measured using the format of hundred-grain weight. To reduce the accidental errors of measurement, maize grain yields in each plot were measured three times to avoid accidental errors, and marked as maize grain yield1, maize grain yield2, and maize grain yield3 (Table A1). The final maize grain yield of each plot was obtained as the average of maize grain yield1, maize grain yield2, and maize grain yield3. Through long-time ground observations, it was confirmed that the tasseling dates of most plots happened from 230 to 237 DOY.

2.3. Methods

The workflow was divided into parts: (1) calculating RGB-based VIs, RGB-based TIs, multispectral-based VIs, and maize height; (2) selecting optimal indices and optimal stages for predicting maize grain yields; (3) predicting maize yield using integrated optimal indices and machine learning and statistical approaches, i.e., BP, SVM, RF, and stepwise

regression model (SRM); (4) optimizing the amounts and varieties of fertilizers using a grey relation analysis. The detailed information is shown in Figure 3.

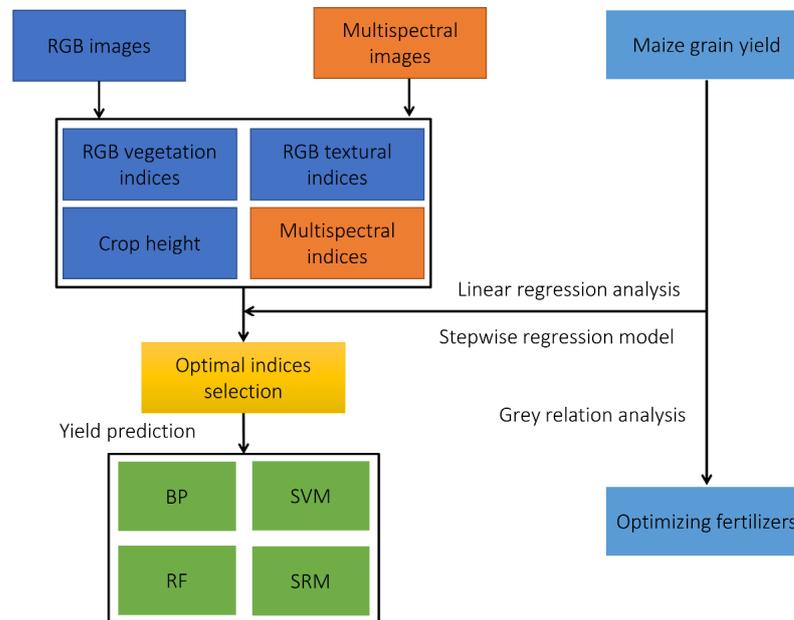


Figure 3. The workflow for predicting maize grain yield and optimizing fertilizers.

2.3.1. The Extractions of Spectral Indices/Textural Indices and Maize Height

The RGB images were independently applied to extract the RGB-based VIs, and the first step was to extract the pure pixels only containing maize. Commonly, the D-values between the excess green vegetation index (EXG) and the excess red vegetation index (EXR) have been applied to differentiate maize and soil [31]. The positive D-values were assigned as maize, and the remainder were assigned as soil.

$$\text{EXG} = 2 \times G - R - B \quad (1)$$

$$\text{EXR} = 1.4 \times R - G \quad (2)$$

where R, G, and B denote the original red, green, and blue bands, respectively, of the RGB images. Then, the commonly applied RGB-based VIs were calculated based on RGB images only containing maize (Table 1).

Table 1. The commonly applied RGB-based vegetation indices.

Indices	Formulations	Reference
CIVE	$0.441 \times R - 0.881 \times G + 0.385 \times B + 18.78$	[32]
RGRI	R/G	[33]
GLI	$(2 \times G - R - B)/(2 \times G + R + B)$	[34]
GRAY	$0.2898 \times R + 0.5870 \times G + 0.1140 \times B$	[35]
VARI	$(G - R)/(G + R - B)$	[36]
RGDI	$(R - G)/(R + G)$	[37]
IKAW	$(R - B)/(R + B)$	[37]
NGRDI	$(G - R)/(G + R)$	[38]
NGBDI	$(G - B)/(G + B)$	[37]
GBDI	$G - B$	[37]
GRI	G/R	[39]
GCC	$R/(G + B + R)$	[40]

Table 1. *Cont.*

Indices	Formulations	Reference
MRBVI	$(R \times R - B \times B)/(R \times R + B \times B)$	[7]
COM	$0.25 \times (2 \times G - R - B) + 0.3 \times ((2 \times G - R - B) - 1.4 \times R - G) + 0.33 \times (0.441 \times R - 0.881 \times G + 0.385 \times B + 18.787)$	[41]

Similarly, commonly applied multispectral-based VIs were extracted (Table 2). The reflectance of soil was quite different from the reflectance of maize in the red band (720 nm) and the near-infrared band (800 nm) [42–44]. Then, the pixels that only contained maize and the pixels that only contained soil were sampled, and the reflectance of each was obtained using IDL. It was found that the reflectance lower than 0.04 in the red band and higher than 0.4 in the near-infrared band were defined as maize, and the remaining pixels were defined as soil. Then, various multispectral-based VIs were calculated based on pixels that only contained maize.

Table 2. The commonly applied multispectral-based vegetation indices. B, G, R, edge, and n800 each represented blue, green, red, red edge, and near infrared bands of the Mini MCA 6 Camera.

Name	Formulations	Reference
MCARI1	$((n800 - edge) - 0.2 \times (n800 - R)) \times n800/edge$	[45]
MEVI	$2.5 \times (n800 - edge)/(n800 + 6 \times edge - 7.5 \times G + 1)$	[46]
NRI	$R/(edge + n800 + R)$	[47]
NREI	$edge/(edge + n800 + G)$	[46]
NGI	$G/(edge + n800 + G)$	[48]
GRDVI	$(n800 - G)/\sqrt{(n800 + G)}$	[46]
GOSAVI	$(1 + 0.16) \times (n800 - G)/(n800 + G + 0.16)$	[49]
NDVI	$(n800 - R)/(n800 + R)$	[50]
SAVI	$(n800 - R) \times (1 + 0.5)/(n800 + R + 0.5)$	[51]
OSAVI	$(n800 - R \times (1 + 0.16))/(n800 + R + 0.16)$	[49]
IPVI	$(n800)/(n800 + R)$	[52]
RDVI	$\frac{(n800-R)}{\sqrt{(n800+R)}}$	[53]
TNDVI	$\sqrt{(n800 - R)/((n800 + R) + 0.5)}$	[54]
VIOPT	$(1.45 \times (n800 \times n800 + 1))/(R + 0.45)$	[55]
MTCI	$(n800 - edge)/(edge - R)$	[56]
RVI	$n800/R$	[55]
NDVI*RVI	$((n800 - R)/(n800 + R)) \times (n800/R)$	[57]
GSAVI	$1.5 \times (n800 - G)/(n800 + G + 0.5)$	[58]
GRVI	$n800/G$	[59]
GDVI	$n800 - G$	[60]
GWDRVI	$(0.12 \times n800 - G)/(0.12 \times n800 + G)$	[46]

The commonly applied TIs such as contrast, correlation, energy, and homogeneity can be extracted from the gray level co-occurrence matrix (GLCM) [61,62], and the red band has been reported to contain slightly more information than the green and blue bands. Therefore, we only applied the red band for extracting the textural information [63]. Since the spatial resolutions of RGB images were higher than multispectral images, the GLCM was calculated using the red bands from RGB images [44,63]. The digital height model (DHM) was obtained using D-values of digital surface model (DSM), to be more specific, the maize height was obtained by subtracting DSM at later growth stages and DSM at earlier stage of growth stage. Thus, the average values of the DHM in each plot were obtained for different growth stages.

2.3.2. The Selection of Indices and Optimal Growth Stages

The linear regression model (LRM) was separately applied between multi-indicators, namely RGB-based VIs, multispectral-based VIs, RGB-based textural indices, DHM, and maize yields. The indices with higher values of coefficients of determination (R^2) were confirmed using the stepwise regression model (SRM). The SRM was applied to select the suitable indices for maize yield prediction with high R^2 (p -values significant). Then, the selected indices of all categories were integrated for predicting maize yields. The main purpose of the LRM was to confirm the optimal indices. Evaluating the performance of different indices was not easy, since there was only a limited number of datasets, and to fairly evaluate these indices the selected datasets should be the same for different indices and growth stages. Therefore, we applied all datasets for indice selection, and all sample numbers were used.

2.3.3. The Maize Grain Yield Prediction Using Machine Learning Approaches and Stepwise Regression Model

A backpropagation network (BP) is a typical artificial neural network (ANN) that builds maps between independent and dependent variables iteratively. It has been widely applied to solve problems such as pattern recognition and classification, nonlinear feature extraction, prediction, and function approximation [64]. During the training phase, the BP adjusted the weights while mapping the model output and actual output by minimizing the errors [65,66]. A support vector machine (SVM) that contains linear, polynomial, splines, and radial basis function networks can be applied to handle nearly all problems of regression [67]. Random forest (RF) can automatically measure the contribution of independent variables and adjust the tree structure of the model. A RF classifier can build massive and multi-layers of trees for simulating (regression and classification), and it can also test the relatively importance of independent variable.

In this study, the selected indices were integrated for predicting maize grain yields using advanced machine learning methods and the traditional stepwise regression model (SRM) method. To be more specific, the optimal indices were treated as the independent variables and the corresponding maize grain yields of each plot were treated as the dependent variables. In order to fully use the dataset, a 10-fold cross-validation was applied. The whole dataset was divided into 10 parts, i.e., 9 parts for training the model and 1 part for model validating. For the BP, the parameters were set as: maximum training times, 10,000; minimum error of training target, $1e-6$; learning rate, 0.001; and maximum number of confirmation failures, 1000. For the RF, the number of trees was set as default 500, the bootstrap was set as true, and the number of variables used for the binary tree in the node was set as max of floor ($D/3$). For the SVM, the kernel-type was set as linear, u^*v ; c cost and g gamma were optimized using the grid search method (x and y each ranged from -5 to 5 with an interval of 0.1); the SVM type was set as epsilon-SVR; and the p epsilon was set as 0.01 [68,69]. For the SRM, the multiple linear regression method was applied.

The commonly applied indicators R^2 and root mean square error (RMSE) were adopted to evaluate model performance [23]. The built-in model with the lowest RMSE and highest R^2 was retained for further maize grain yield mapping. For different sources of data, the RGB images were resized to the same resolution of the multispectral images. The coefficients in the well-built models were each applied to predict the maize grain yield using the selected indices at optimal growth stages.

2.3.4. The Confirmation of Optimal Amounts and Combinations of Fertilizers

The different amounts and combinations of N, P, and K and maize grain yields were applied for further analysis to confirm the optimal amounts and combinations of fertilizers. A grey relation analysis (GRA) is commonly conducted in agriculture for assessing the relationships of correlated variables [70,71]. In particular, a GRA is an excellent method for calculating the grey relational degree and determining the contribution measure of the main behavior of a system or the influence degree between system factors. A GRA

was applied to assess the relative importance of fertilizers to maize grain yields. The independent variables were the amounts of fertilizers of 20 plots in sequences, and the dependent variables were the corresponding maize grain yields in sequences. The values of the GRCs for the fertilizer were compared, and the most important fertilizers were obtained. The ratios of fertilizers were applied and the suggested usages of fertilizers were confirmed.

3. Results

3.1. The Linear Regression Analysis between Indices and Maize Grain Yields

The RGB images and multispectral images acquired at different growth stages of maize were processed under a standard procedure using the approach introduced in the Methods section (Figures A1 and A2). To better show the difference between different growth stages, the images were all shown in the RGB color system for comparison. The tasseling dates of maize in all plots mostly happened from 230 to 237 DOY.

The RGB-based VIs of 20 plots during the entire growth stages of maize were regressed with maize grain yields. The RGB-based VI with regression equations, R^2 and p -values are shown in Table 3. It can be obtained that R^2 ranged from 0.748 to 0.809, indicating that RGB-based VIs were closely correlated with maize grain yields. It can be deduced that the RGB-based VIs may have great potential for predicting maize grain yields.

Table 3. The linear regression analysis of RGB-based VIs and maize grain yields during the entire growth stages.

Indices	Regression Equations	R^2	p -Values
CIVE	$Y = 0.036X + 34.025$	0.769	$p = 0.108$
GRAY	$Y = 0.001X + 32.416$	0.755	$p = 0.130$
NGBDI	$Y = 26.132X + 44.874$	0.796	$p = 0.075$
GBDI	$Y = -0.046X + 39.382$	0.748	$p = 0.141$
GCC	$Y = 15.204X + 23.992$	0.764	$p = 0.117$
IKAW	$Y = -37.040X + 33.304$	0.807	$p = 0.063$
MRBVI	$Y = -18.541X + 33.241$	0.809	$p = 0.059$

The multispectral-based VIs during the entire growth stages was also linear regressed with maize grain yields. The multispectral-based VIs with regression equations, R^2 , and p -values are shown in Table 4. It can be obtained that the R^2 of multispectral-based VIs ranged from 0.780 to 0.826, and these values were slightly higher than those of RGB-based VIs.

Table 4. The linear regression analysis of multispectral-based VIs and maize grain yields using data of 20 plots during the entire growth stages.

Indices	Regression Equations	R^2	p -Values
NDVI	$Y = 72.072X - 42.252$	0.826	$p < 0.001$
SAVI	$Y = 39.965X - 29.690$	0.781	$p < 0.001$
OSAVI	$Y = 44.018X - 38.885$	0.798	$p < 0.001$
IPVI	$Y = 144.143X - 124.006$	0.822	$p < 0.001$
GRVI	$Y = 40.699X - 29.189$	0.781	$p < 0.005$
GDVI	$Y = 170.356X - 198.655$	0.824	$p < 0.001$
VILOT	$Y = 9.475X - 62.144$	0.786	$p < 0.050$
NDVI*RVVI	$Y = 27.987X + 4.711$	0.780	$p < 0.050$

The TIs including contrast, correlation, energy, homogeneity and the DHM were independently extracted from the RGB images, and a linear regression analysis was conducted between these indices and maize grain yields. The linear regression results using textural indices and DHM are shown in Table 5. It can be observed that the R^2 values ranged from 0.779 to 0.901, and the R^2 values were larger than the values of the multispectral-based

VI_s, except for energy. Thus, the textural indices were closely correlated with maize grain yields. The DHM also had a close relationship with the yield, of which the R^2 was 0.857.

Table 5. The linear regression analysis of textural indices, DHM, and maize grain yields during the entire growth stages.

Indices	Regression Equations	R^2	p -Values
Contrast	$Y = -12.589X + 32.348$	0.833	$p < 0.050$
Correlation	$Y = 3.682X + 33.892$	0.901	$p < 0.050$
Energy	$Y = -6.335X + 33.495$	0.779	$p = 0.095$
Homogeneity	$Y = 13.150X - 47.351$	0.878	$p < 0.050$
DHM	$Y = -0.477X + 24.012$	0.857	$p < 0.050$

3.2. The Selection of Optimal Growth Stage for Maize Grain Yield Prediction

The RGB-based VI_s of 20 plots at each growth period were linearly regressed with maize grain yields (Figure 4). It can be observed that the R^2 using data collected from 230 to 273 DOY were commonly larger than those during the period from 188 to 209 DOY. The data acquired on 250 DOY achieved the highest R^2 , of which the value was 0.71 for NGBDI and GBDI. The data collected from 230 to 273 DOY were more correlated with maize grain yields than the data collected from 188 to 209 DOY. The RGB-based VI_s from 230 to 273 DOY were selected for maize grain yield prediction.

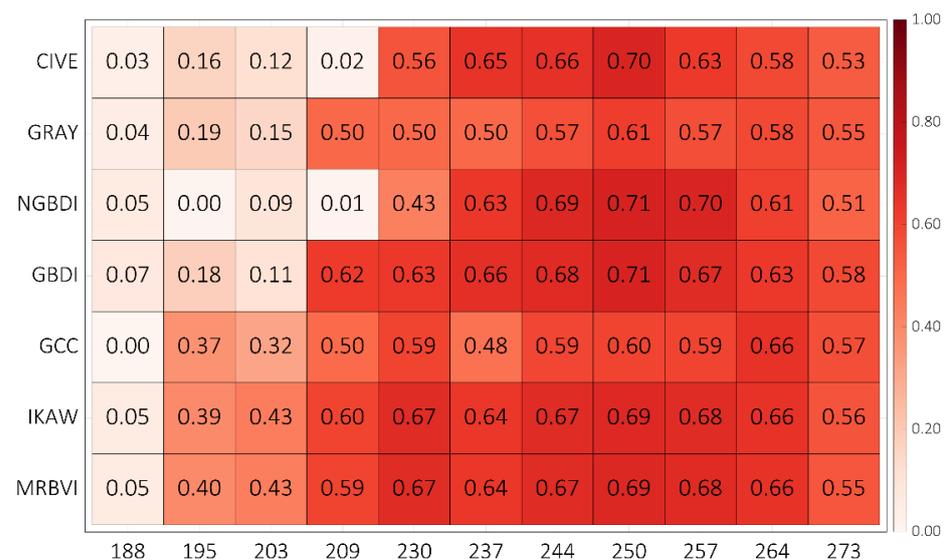


Figure 4. The R^2 between the RGB-based VI_s and maize grain yields using data at each growth stage using the linear regression method. The x-axis represents the DOY and the y-axis represents the different indices.

The multispectral-based VI_s of 20 plots at different growth periods were separately linearly regressed with maize grain yields (Figure 5). The data collected on 237 DOY were more correlated with maize grain yields. The tasseling dates ranged from 230 to 237 DOY for 20 plots, and the higher R^2 values achieved from 230 DOY indicated that the accuracy of yield prediction using data collected from tasseling date to maturity date was higher. The multispectral-based VI_s from 230 to 273 DOY were selected for further predicting maize grain yields.

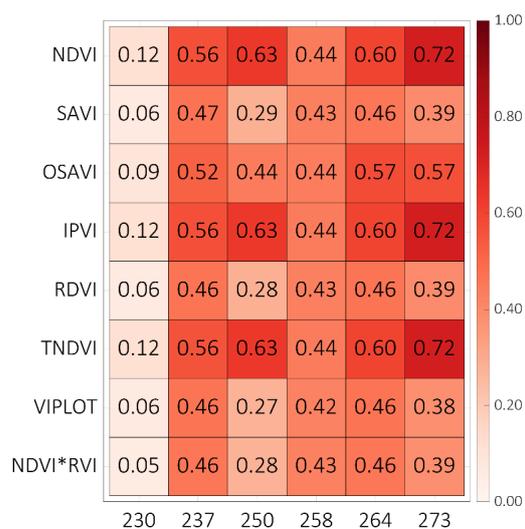


Figure 5. The R^2 values between the multispectral-based VIs and maize grain yields using data of 20 plots at each growth stage using the linear regression method. The x-axis represents the DOY and the y-axis represents the different indices.

3.3. The Maize Grain Yield Prediction of Maize Using Machine Learning Methods and Traditional Regression Method

The selected RGB-based VIs, multispectral-based VIs, RGB-based textural indices, and DHM at optimal growth stages were integrated to predict maize grain yields using three machine learning methods, i.e., BP, SVM, RF, and a traditional regression method, i.e., SRM. Each model was independently applied to build the relationships between these integrated indices and maize grain yields. The comparison of measured and predicted maize grain yields are shown in Figure 6.

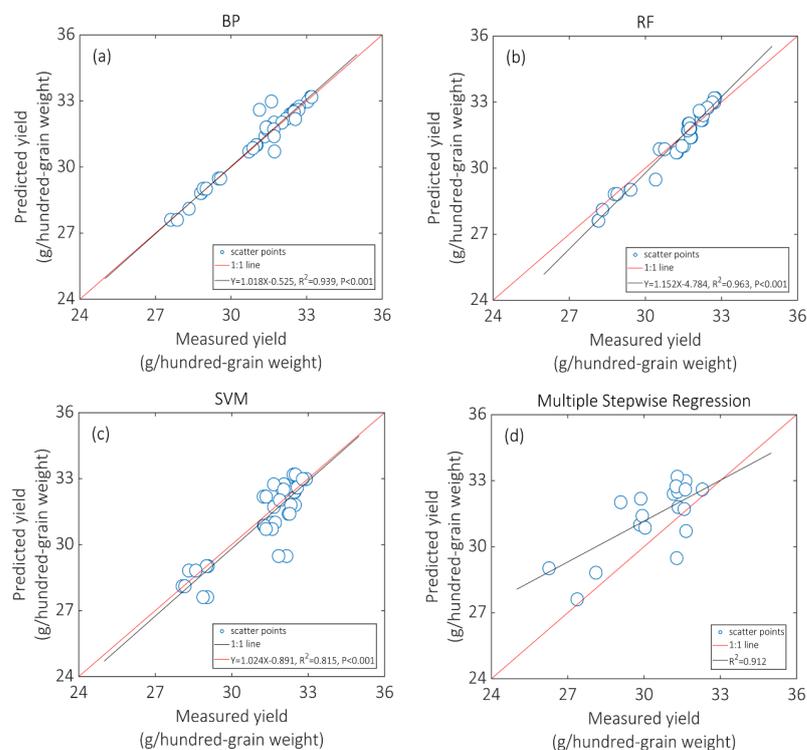


Figure 6. The comparison of measured and predicted maize grain yields using three machine learning methods and the stepwise regression model (SRM). Note: (a–d) represent the results using BP, RF, SVM and SRM, respectively.

For the machine learning-based methods, the R^2 values using BP, RF, and SVM were 0.939, 0.963, and 0.815, respectively. Similarly, the RMSE values using BP, RF, and SVM were 0.496, 0.489, and 0.823 g/hundred-grain weight, respectively. The BP and RF both performed better than SVM, with higher R^2 values and lower RMSE values. For the results using SRM, the R^2 was 0.912, and the RMSE was 1.772 g/hundred-grain weight. Therefore, the machine learning-based methods have greater potential for predicting maize grain yield, and the RF achieved the highest accuracy. The optimized parameters of the machine learning-based models were applied for mapping maize grain yields (pixel-based optimal indices collected at optimal growth stages) (Figure 7).

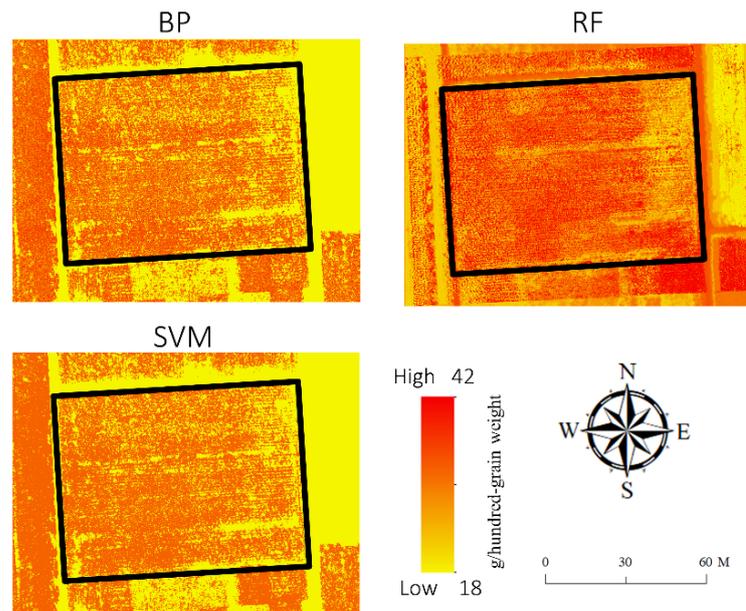


Figure 7. The mapping of maize grain yields using three machine learning methods with optimized parameters.

3.4. The Optimization of Combinations and Ratios for Fertilizers

The grey relation coefficients (GRCs) between each type of fertilizer and yields calculated using the grey relation analysis (GRA) are shown in Figure 8. The GRC values were 35.707, 34.435, and 29.857% for the maize grain yield1, 36.417, 32.606, 30.975% for maize grain yield2, and 35.926, 33.084, and 30.989% for maize grain yield3. The results show that N is the dominating influencing factor for the growth of maize.

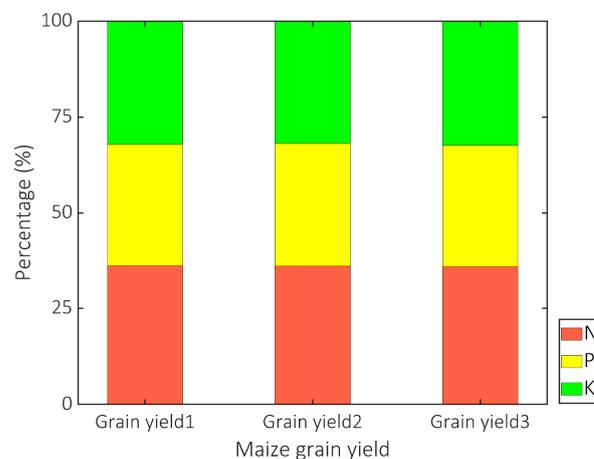


Figure 8. The grey relation coefficients (GRC) of N, P, and K for maize grain yields using grey relation analysis (GRA).

The changes in N, K, and P fertilizers with the corresponding variations of maize grain yields are shown in Figure 9. It can be clearly noted that the impacts of different ratios of fertilizer to maize grain yields varied significantly. For N, the maize grain yields increased with the addition of N, until the ratios increased between 2 and 3 (Figure 9a–c). The optimal application ratio of N was 2. For P and K, the maize grain yields merely changed with the adding of these two fertilizers. Most of the circumstances in subplots from Figure 9d to Figure 9i showed decreased maize grain yields due to the increased usage of P and K. The optimal application ratios for P and K was 1. It can be deduced that the optimal combination ratio of N/P/K is 2:1:1.

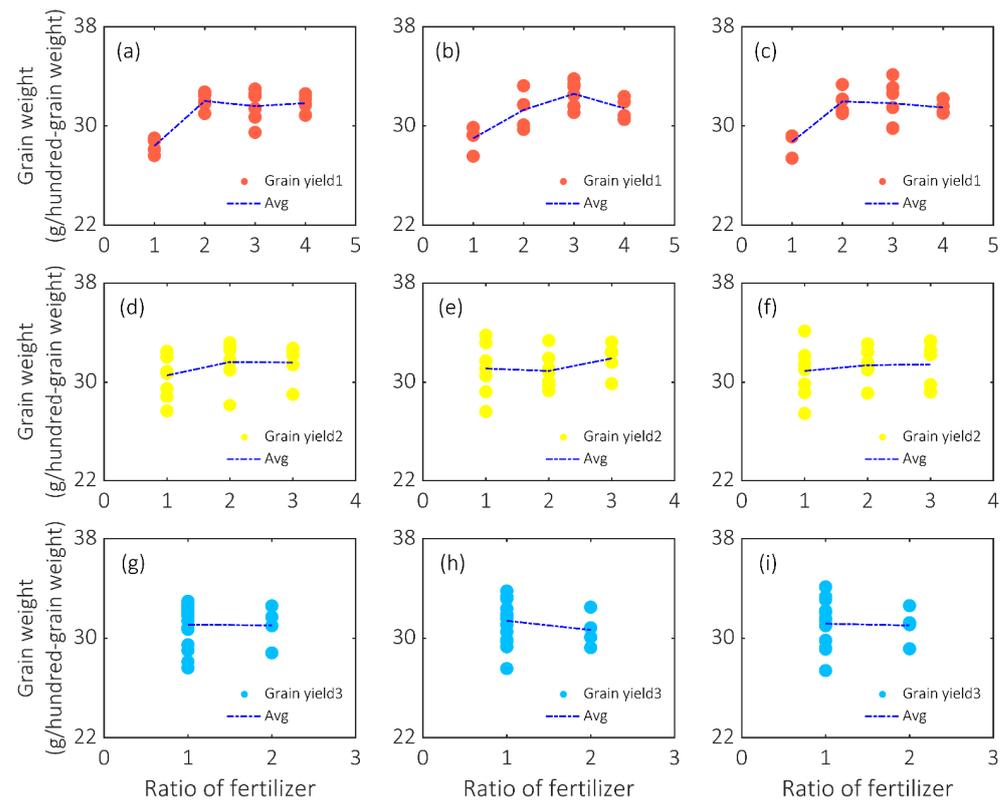


Figure 9. The dynamic changes in ratios of N, P, and K and the corresponding variations of maize grain yields. Note: (a–c) Represent the effects of N on maize grain yield1; (d–f) represent the effects of P on maize grain yield2; (g–i) represent the effects of K on maize grain yield3.

4. Discussion

4.1. Yield Prediction Using Multi-Source Data from a UAV Platform

In this study, the RGB images and multispectral images covering the entire growth stages of maize were collected from a UAV platform. The selected RGB-based VIs, TIs, and DHM from RGB images, and the multispectral-based VIs were integrated for predicting maize grain yields. The R^2 values of yield prediction only using RGB-based VIs ranged from 0.748 to 0.809 during the growing season. The RGB-based VIs were closely correlated with maize grain yields. The results were consistent with previous studies, where RGB-based VIs from RGB images were proven to have great potential for agricultural yield predictions [7]. The multispectral-based VIs performed slightly better than the RGB-based VIs. This was also consistent with previous studies, where multispectral-based VIs were found to have greater potential than RGB-based VIs in predicting agricultural yields [72–74]. Unlike the satellite-based images, the UAV-based RGB and multispectral images were commonly at the centimeter level, and were merely influenced by the mixed pixels. The high-resolution images from a UAV can be applied to derive high-resolution textural indices. We found the TIs with the DHM also improved the accuracy of maize grain yield prediction, with

R^2 values ranging from 0.779 to 0.901. The TIs actually expressed the dynamic changes of maize in a different way from spectral indices [75–77]. The DHM was actually the crop phenotype, and it was found to be very useful for predicting crop yields [78–80].

The R^2 values between maize grain yields and indices were totally different for different growth stages. The higher R^2 values occurred from 230 to 237 DOY; this stage (tasseling date) was in accordance with previous studies, and was found to be closely correlated with maize grain yields [81–83]. Therefore, tasseling date is an important phenology for yield prediction, and the data collected during this period are important for assessing maize grain yields. Meanwhile, tasseling date has been widely proven to be an important period for management practices such as the application of fertilizers [84–87]. Therefore, it was recommended to integrate RGB-based VIs, RGB-based TIs, multispectral-based VIs, and DHM (maize height) acquired from tasseling date to maturity date for predicting maize grain yields.

N was found to be the most important fertilizer to increase maize grain yields. This finding was in accordance with previous studies where the application of N was correlated with maize grain yields [88–90]. Increasing the ratios of P and K was also greatly correlated with maize grain yields. Therefore, it was suggested that the optimal ratio of N/P/K was 2:1:1. Excessive application of fertilizers to agricultural land can cause uneven distribution of resources, and can reduce the potential application of fertilizers to other fields where materials are needed [91–94]. In addition, excessive application of fertilizers can cause serious land degradation, endangering the environmental and ecological system, and lead to a reduction in agricultural yields. There is a need to reduce the potential usage of P and K, since the added P and K will reduce agricultural yields and also destroy valuable cultivated land. This is very important to meet the requirement of sustainable agriculture.

4.2. The Limitations

Multi-sources of UAV images were applied for predicting maize grain yields using traditional regression and advanced machine learning approaches. The data quality was strictly controlled, but there were uncertainties that still remained from the data source and data processing. First, there was a mismatch between the geometric registration between the RGB images (1 cm) and multispectral images (5 cm), even though the RGB images were resampled to the same spatial resolution as the multispectral images. This would influence the extraction of various VIs, and would further influence the maize grain yield predictions. Second, the images covering the entire growth of maize were collected under similar imaging conditions, but there were slight differences in the solar radiation, wind, air pressure, and atmospheric effects. These differences in environmental conditions would influence the image collection. In addition, the long working time of cameras and the hot temperature would create inevitable noise, especially in summer [95,96]. Third, the applied machine learning methods were commonly used methods; more advanced machine learning and deep learning methods that would certainly achieve high accuracy in yield predictions could be explored in future analysis [97–99]. Finally, the number of sampling plots was limited in this study, which may cause an overfitting problem. A larger number of plots for exploring different amounts and combinations of fertilizers on maize grain yield could be conducted in future analysis. Machine learning-based approaches using more datasets may realize more reasonable and convincing results.

5. Conclusions

In this study, the multi-indicators, namely RGB-based VIs, RGB-based TIs, multispectral-based VIs, and maize height from UAV data were applied for predicting maize grain yields. The RGB-based VIs and multispectral-based VIs were proven to be closely correlated with maize grain yields. The innovation of integration of commonly applied VIs, TIs, and crop height for maize grain yield prediction significantly improved the accuracy. The data collected from tasseling date to maturity date were more correlated with the maize grain yield than other phenological growth stages. The tasseling date is an important phenology

of maize that would promote the accuracy of yield prediction of summer maize. The multi-indicators were integrated to predict maize grain yields using traditional regression and advanced machine learning approaches. The machine learning approaches were commonly better than the traditional regression method, and R gained the highest accuracy ($R^2 = 0.963$ and $RMSE = 0.489$ g/hundred-grain weight). It is recommended to adopt multi-data (spectral, textural indices, and maize height) from tasseling date to maturity date for predicting maize grain yields based on RF.

Author Contributions: Conceptualization, Y.G. and X.Z.; methodology, Y.G. and X.Z.; software, Y.G. and S.C.; validation, Y.G., X.Z., S.C. and H.W.; formal analysis, H.W. and S.J.; investigation, S.J. and D.C.; resources, Y.G., X.Z. and Y.F.; data curation, Y.G., X.Z., D.C. and Y.F.; writing—original draft preparation, Y.G.; writing—review and editing, Y.G., X.Z. and Y.F.; visualization, Y.G.; supervision, X.Z. and Y.F.; project administration, X.Z.; funding acquisition, X.Z. and Y.F. All authors have read and agreed to the published version of the manuscript.

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Data Availability Statement: Data will be made available on request.

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Conflicts of Interest: The authors declare no conflict of interest.

Appendix A

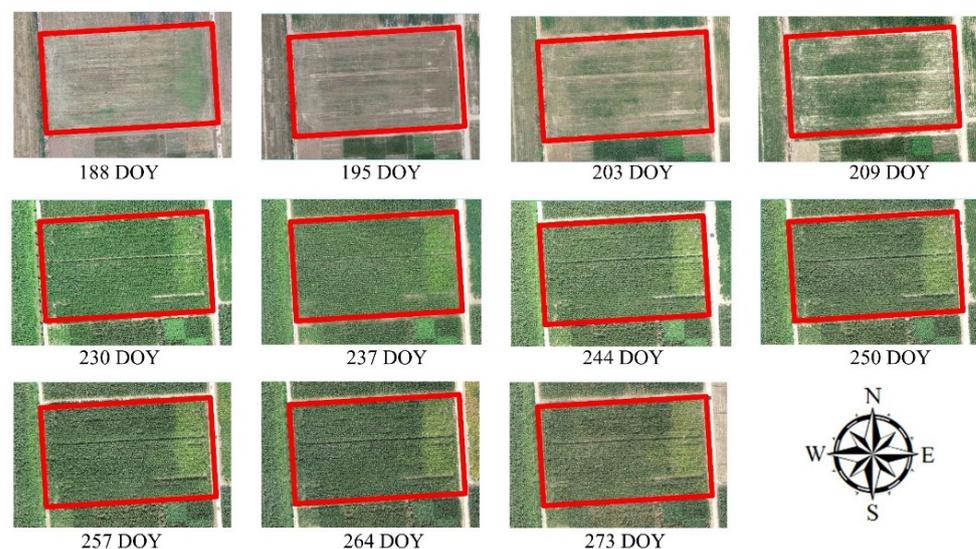


Figure A1. The RGB images at different growth stages of maize.

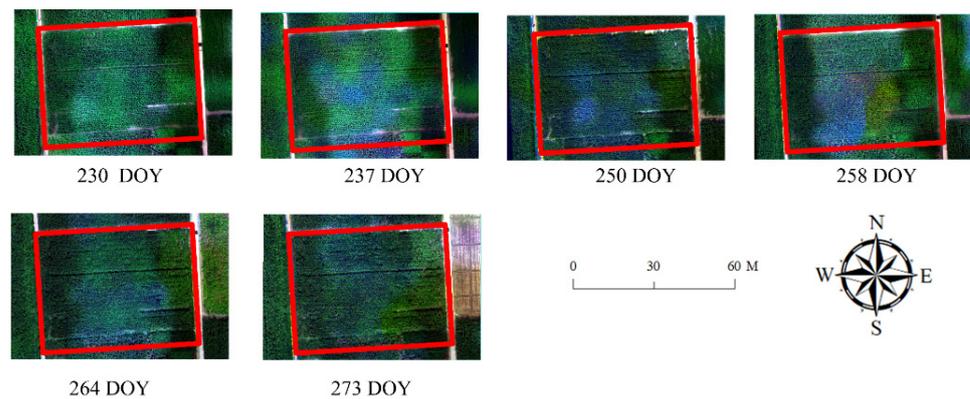


Figure A2. The multispectral images at different growth stages of maize.

Table A1. The application of fertilizers in 20 plots. The number after NPK represents the actual multiple applications of fertilizers. The plots correspond to the plots shown in Figure 1. The 1, 2, and 3 each represent 0.7, 1.4, and 2.1 kg of the elements, respectively.

Plots	Combinations	Grain Yield 1	Grain Yield 2	Grain Yield 3
1	N1P1K2	28.82	29.24	29.15
2	N3P1K1	29.48	31.08	29.84
3	N3P3K1	31.4	31.6	29.8
4	N2 + wheat-straw	32.02	31.7	32.1
5	N1P1K1	27.61	27.56	27.4
6	N3P3K2	32.6	32.5	32.62
7	N3P2K1	32.98	33.36	33.1
8	N2 + Organic material	33.18	31.1	32.44
9	N1P2K1	28.11	29.31	29.12
10	N2P2K2	31	30.08	31.25
11	N4P3K1	32.18	32.38	32.21
12	N3+ wheat-straw	30.71	33.8	31.48
13	N1P3K1	29.02	29.88	29.2
14	N2P1K1	32.5	31.72	32.16
15	N4P2K1	32.6	31.94	31.6
16	N3 + Organic material	32.4	33.18	34.13
17	N2P3K1	32.74	33.24	33.34
18	N2P2K1	31.8	29.72	31
19	N4P1K1	30.86	30.52	31.02
20	N4P2K2	31.71	30.84	31.09

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