

## Article

# GNSS-IR Snow Depth Retrieval from Multi-GNSS and Multi-Frequency Data

Jinsheng Tu <sup>1</sup>, Haohan Wei <sup>2,\*</sup> , Rui Zhang <sup>3,4</sup> , Lei Yang <sup>5</sup> , Jichao Lv <sup>3</sup> , Xiaoming Li <sup>6</sup>, Shihai Nie <sup>1</sup>, Peng Li <sup>1</sup> , Yanxia Wang <sup>1</sup> and Nan Li <sup>1</sup>

- <sup>1</sup> College of Geographic Information and Tourism, Chuzhou University, Chuzhou 239000, China; tujinsheng@chzu.edu.cn (J.T.); nsh1017@chzu.edu.cn (S.N.); lipeng@chzu.edu.cn (P.L.); lidarcenter@chzu.edu.cn (Y.W.); linan@chzu.edu.cn (N.L.)
- <sup>2</sup> College of Civil Engineering, Nanjing Forestry University, Nanjing 210037, China
- <sup>3</sup> Faculty of Geosciences and Environmental Engineering, Southwest Jiaotong University, Chengdu 611756, China; zhangrui@swjtu.edu.cn (R.Z.); lvjichao@my.swjtu.edu.cn (J.L.)
- <sup>4</sup> State-Province Joint Engineering Laboratory of Spatial Information Technology for High-Speed Railway Safety, Southwest Jiaotong University, Chengdu 611756, China
- <sup>5</sup> College of Information Science and Engineering, Shandong Agricultural University, Tai'an 271018, China; yanglei@sdau.edu.cn
- <sup>6</sup> College of Surveying and Geoinformatics, Tongji University, Shanghai 200092, China; lxmch@tongji.edu.cn
- \* Correspondence: weihaoan@njfu.edu.cn; Tel.: +86-139-5185-6853



**Citation:** Tu, J.; Wei, H.; Zhang, R.; Yang, L.; Lv, J.; Li, X.; Nie, S.; Li, P.; Wang, Y.; Li, N. GNSS-IR Snow Depth Retrieval from Multi-GNSS and Multi-Frequency Data. *Remote Sens.* **2021**, *13*, 4311. <https://doi.org/10.3390/rs13214311>

Academic Editors: Serdjo Kos, José Fernández and Juan F. Prieto

Received: 3 October 2021

Accepted: 25 October 2021

Published: 26 October 2021

**Publisher's Note:** MDPI stays neutral with regard to jurisdictional claims in published maps and institutional affiliations.



**Copyright:** © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (<https://creativecommons.org/licenses/by/4.0/>).

**Abstract:** Global navigation satellite system interferometric reflectometry (GNSS-IR) represents an extra method to detect snow depth for climate research and water cycle managing. However, using a single frequency of GNSS-IR for snow depth retrieval is often found to be challenging when attempting to achieve a high spatial and temporal sensitivity. To evaluate both the capability of the GNSS-IR snow depth retrieved by the multi-GNSS system and multi-frequency from signal-to-noise ratio (SNR) data, the accuracy of snow depth retrieval by different frequency signals from the multi-GNSS system is analyzed, and a joint retrieval is carried out by combining the multi-GNSS system retrieval results. The SNR data of the global positioning system (GPS), global orbit navigation satellite system (GLONASS), Galileo satellite navigation system (Galileo), and BeiDou navigation satellite system (BDS) from the P387 station of the U.S. Plate Boundary Observatory (PBO) are analyzed. A Lomb–Scargle periodogram (LSP) spectrum analysis is used to compare the difference in reflector height between the snow-free and snow surfaces in order to retrieve the snow depth, which is compared with the PBO snow depth. First, the different frequency retrieval results of the multi-GNSS system are analyzed. Then, the retrieval accuracy of the different GNSS systems is analyzed through multi-frequency mean fusion. Finally, the joint retrieval accuracy of the multi-GNSS system is analyzed through mean fusion. The experimental shows that the retrieval results of different frequencies of the multi-GNSS system have a strong correlation with the PBO snow depth, and that the accuracy is better than 10 cm. The multi-frequency mean fusion of different GNSS systems can effectively improve the retrieval accuracy, which is better than 7 cm. The joint retrieval accuracy of the multi-GNSS system is further improved, with a correlation coefficient (R) between the retrieval snow depth and the PBO snow depth of 0.99, and the accuracy is better than 3 cm. Therefore, using multi-GNSS and multi-frequency data to retrieve the snow depth has a good accuracy and feasibility.

**Keywords:** GNSS-IR; snow depth; signal-to-noise ratio; multi-GNSS; multi-frequency; mean fusion

## 1. Introduction

Snow is an important part of the land hydrological cycle and global climate system. Accurate real-time snow depth data are an important reference indicator for water resource management and climate disaster warning [1,2]. Among the existing snow depth detection

methods, in situ snow sensor measurement lacks time resolution, and global navigation satellite system interferometric reflectometry (GNSS-IR), as a new microwave sensing technology, has proven to be able to realize snow depth detection [3]. GNSS-IR is a kind of satellite remote sensing technology that uses GNSS signals as the transmitting source to realize the retrieval of the physical parameters of surface targets by receiving and processing the interference effect of GNSS signals formed by direct and surface reflection [4–6]. At present, this technology is mainly employed to retrieve the soil moisture content (SMC), snow depth, and vegetation parameters [7–12].

In recent years, researchers have made remarkable achievements in GNSS-IR snow depth detection. Larson et al. first proposed to extend the application of signal-to-noise ratio (SNR) data observed by the traditional geodetic global positioning system (GPS) receiver in order to detect snow depth [3]. Larson et al. conducted snow depth retrieval using SNR data of a GPS L2C signal at multiple stations of the Plate Boundary Observatory (PBO) and further verified the feasibility of this technology [13]. Later, Larson et al. developed a snow depth retrieval algorithm based on GPS L1 SNR data, compared it with the snow depth results of L2C signal retrieval, and found that the accuracy was improved [14]. Tabibi et al. evaluated the value of GPS L5 SNR data in snow depth detection, compared the results with the L2C signal, and found that there was no detectable deviation in the L5 retrieval results [15]. Tabibi et al. proposed the global orbit navigation satellite system multipath reflectometry (GLONASS-MR) SNR retrieval model, which extended GPS-MR to multiple GNSS, and showed a strong correlation by comparing the retrieval results of GPS L2C and GLONASS R2-coarse acquisition (C/A) signals [16]. Later, Tabibi et al. used simulation and field measurements to evaluate the accuracy of GPS and GLONASS combined multi-GNSS-MR snow depth retrieval. At the same time, the variance factor was used to form the optimal multi-GNSS combined snow depth daily sequence retrieval. Compared with the single signal snow depth retrieval results, the accuracy was significantly improved [17]. Jin et al. used GPS L2P SNR data to retrieve the snow depth, and compared it with GPS L1 C/A code results, which showed a high correlation, indicating that using L2P SNR data can better estimate the snow depth [18]. Zhou et al. used GLONASS L1 SNR data for snow depth detection, and the accuracy reached centimeter-level and showed a strong correlation with the measured data [19]. Zhou et al. also studied the retrieval of different signal combinations and proposed using GPS L1, L2, and L5 signal multipath reflection and SNR combination for the retrieval of snow depth. The results showed that this method can be effectively used for snow depth detection [20].

The above scholars' research on snow depth retrieval is based on GPS and GLONASS observation data and has not been extended to other GNSS systems. To further analyze the potential of other GNSS systems in snow depth detection, Wang et al. used the SNR data of GPS L1 and BeiDou navigation satellite system (BDS) B1I signals to retrieve the snow depth, finally reaching an accuracy of 5 cm in a day [21]. Wang et al. used multi-GNSS system data to retrieve the snow depth and found that the trend of single signal retrieval results of multi-GNSS system constellations was in good agreement, except for the GPS precise code (P-code) signal. Then, the multi-GNSS system combination method based on robust regression was used to combine the signal retrieval between constellations. The results showed that the accuracy, availability, and time sampling of multi-GNSS system combination retrieval were improved [22].

From the current research status, snow depth retrieval is mainly concentrated in single or dual GNSS systems and single frequency SNR data, which is often found to be challenging when attempting to meet the accuracy and time resolution requirements of snow depth detection. Therefore, based on previous studies, this article conducts snow depth retrieval using multi-GNSS and multi-frequency SNR data. For the case that the antenna height of the GNSS receiver is unknown, the mean value of the multi-day Lomb-Scargle periodogram (LSP) spectrum analysis results in the snow-free surface is used as the initial reference reflector height of the multi-GNSS and multi-frequency GNSS-IR in the

article. Then, the snow depth retrieval capability of the Galileo satellite navigation system (Galileo) and BDS multi-frequency signal, which are rarely used to retrieve the snow depth, except the GPS and GLONASS signal, are evaluated. A mean fusion of multi-frequency retrieval results of different GNSS systems is proposed to improve the accuracy compared with different frequencies of multi-GNSS system retrieval results. Finally, the multi-GNSS system retrieval results are fused to further evaluate the accuracy of the GNSS combination retrieval of snow depth. In this article, through the above process, the feasibility and accuracy of multi-GNSS and multi-frequency GNSS-IR snow depth retrieval are evaluated.

## 2. Materials and Methods

### 2.1. GNSS-IR Snow Depth Retrieval Principle

The snow depth retrieval method used in the article is based on SNR data processing of traditional geodetic GNSS receivers. The SNR is an indicator used to measure the signal strength of global navigation satellites, which is mainly affected by antenna gain, satellite transmission power, and multipath [23–25]. The multipath effect of the SNR decreases with increasing satellite elevation angle. The direct and surface reflected signals will have obvious interference effects at the receiver antenna when the satellite is at low elevation angle. At the same time, the frequency of the reflected signal will also change with the change in antenna height. The snow depth parameter can be obtained by comparing the vertical distance difference between the reflection surface and the receiver antenna phase center under snow-free and snow conditions.

Figure 1 shows that direct signal and reflected signal generate corresponding interference effects at the receiver to form a composite interference signal, which can be expressed as [24]:

$$\text{SNR} = A_d^2 + A_r^2 + 2A_d A_r \cos \varphi, \quad (1)$$

where  $A_d$  and  $A_r$  are the amplitudes of the direct signal and the reflected signal, and  $\varphi$  is the difference between the phases of the direct signal and the phases of the reflected signal (the unit is rad), which can be expressed as [26]:

$$\varphi = \frac{4\pi h}{\lambda} \sin \theta, \quad (2)$$

where  $\lambda$  is the wavelength of the signal;  $\theta$  is the elevation angle of the satellite;  $h$  is the vertical distance from the reflector to the antenna phase center; and the full text is uniformly called the reflector height.

Because the change in snow depth parameters is only related to the reflected signal in the composite SNR data, it is necessary to eliminate the direct signal in the composite SNR to obtain the reflected signal part. In the article, the composite SNR data are fitted by a cubic low-order polynomial, and the composite SNR is linearized before fitting [27]:

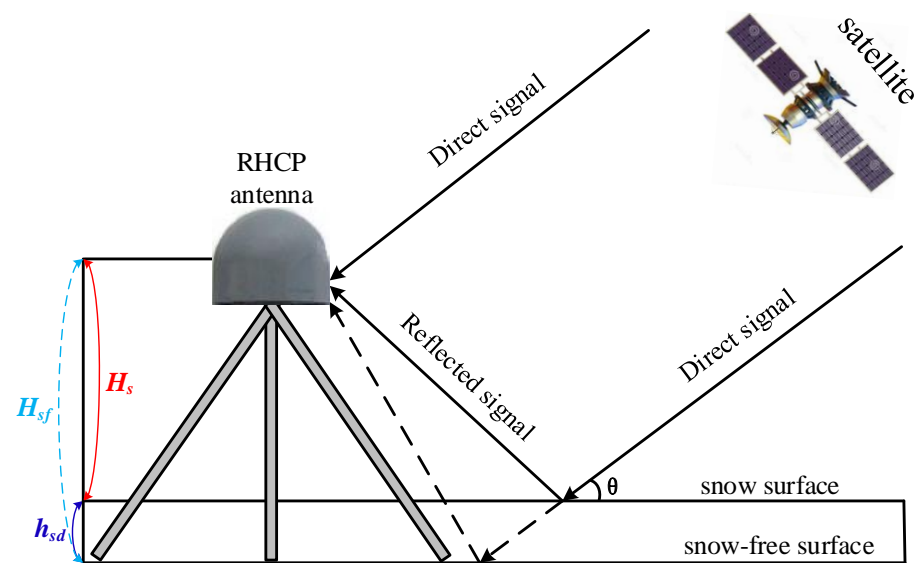
$$\text{SNR}(\text{volts/volts}) = 10^{\frac{\text{SNR}(\text{dB-Hz})}{20}}, \quad (3)$$

After the trend of the direct signal sequence is fitted, the SNR sequence of the reflected signal that removes the influence of the direct signal can be obtained, which can be expressed as  $\text{SNR}_r$  [28]:

$$\text{SNR}_r = A_r \cos\left(\frac{4\pi h}{\lambda} \sin \theta + \varphi\right), \quad (4)$$

$f$  is the signal frequency of the multipath effect part in the SNR. After simplification, the relationship reflector height and the satellite signal wavelength can be obtained as follows:

$$f = \frac{2h}{\lambda} \quad h = \frac{\lambda f}{2}, \quad (5)$$



**Figure 1.** Schematic diagram of GNSS-IR snow depth retrieval. After the satellite sends the signal, the right-handed circular polarized (RHCP) antenna receives the direct signal and the surface reflected signal, and produces interference effect at the receiver. The snow surface reflector height ( $H_s$ ) and snow-free surface reflector height ( $H_{sf}$ ) are calculated, respectively, by analyzing the oscillation effect, and the snow depth ( $h_{sd}$ ) is calculated by comparing the differences between them.  $\theta$  is the elevation angle of the satellite.

In the article, the LSP method is used to analyze  $\text{SNR}_r$ , obtain  $f$ , and extract  $h$  [3,29,30]. As shown in Figure 1, the snow depth parameter is calculated by using the above method by comparing reflector height in the case of snow-free and snow surfaces:

$$h_{sd} = H_{sf} - H_s, \quad (6)$$

where  $H_{sf}$  and  $H_s$  are the snow-free and snow surface reflector height, and  $h_{sd}$  is the snow depth.

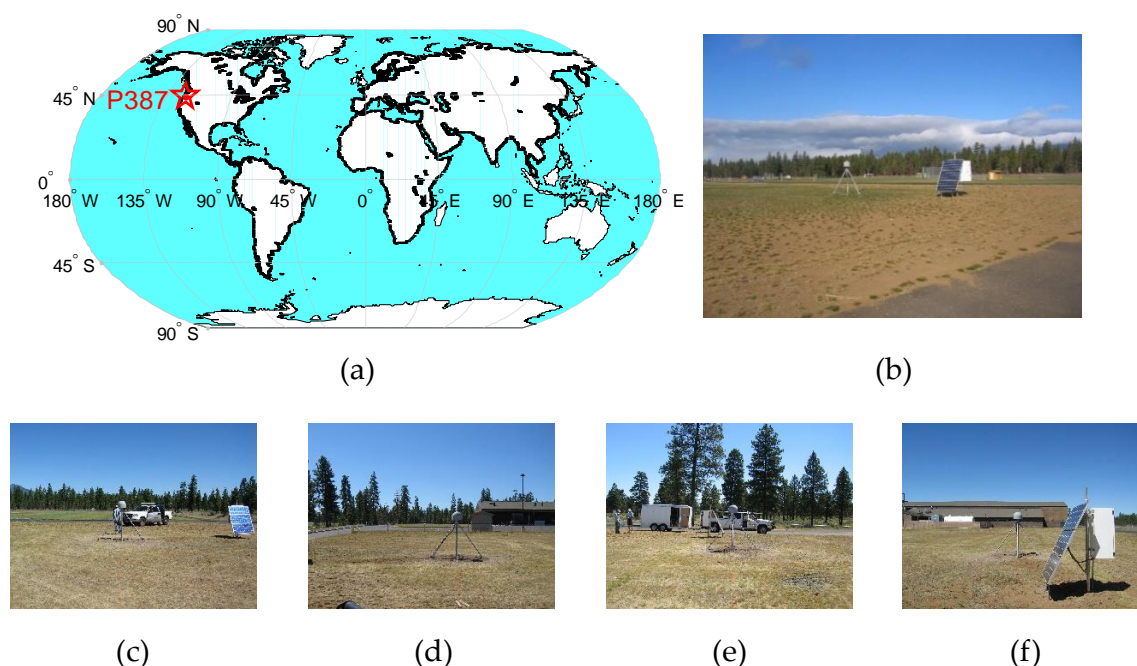
Snow depth retrieval is mainly determined by snow and snow-free surface reflector height. Wang et al. mentioned that non-planar reflecting surface and atmospheric refraction in GNSS-IR techniques can lead to errors in reflector height. These two errors are mainly considered in the sea level height retrieval, but rarely in the snow depth, as the snow depth changes slowly, and the reflector height to snow depth is usually smaller than that to the sea level [22]. The purpose of the article is to evaluate the ability of multi-GNSS and multi-frequency GNSS-IR snow depth retrieval, without focusing on the actual error impact caused by these two factors.

## 2.2. Data Source

### 2.2.1. Station Location and Surrounding Environment

This article selects GNSS observation data and snow depth data collected at the P387 station (Figure 2) of the PBO, which is located in Sisters, Oregon, the U.S., with an altitude of 963.041 m. The specific location of the station is  $44.29675^\circ\text{N}$  and  $121.57446^\circ\text{W}$ . The data of the P387 station is collected by SEPTENTRIO (SEPT) POLARX5 receivers and TRM59800.80 antennas pointing toward the zenith with a sampling frequency of 15 s. The terrain around this station is flat without trees, and the signal acquisition conditions are good.

Figure 2 shows that, regarding the P387 site location and surrounding environment, the terrain around P387 is flat. The ability of multi-GNSS and multi-frequency GNSS-IR snow depth retrieval is key to the article. In order to reduce the influence of terrain on the reflector height, the experimental region with small surface fluctuation is selected.



**Figure 2.** P387 station conditions: (a) station location in the world; (b) site vision; (c) site north; (d) site south; (e) site east; (f) site west.

At the same time, it can be seen that the vegetation around the P387 site is rare, and that the vegetation type is lawn. The surface can be defined as bare soil in winter snow stage. Therefore, with the melting of snow, the surface is gradually exposed, and the signal reflected by the surface is less affected by vegetation attenuation. The surface should be selected to be close to the bare soil in the subsequent analysis of snow-free reflection, so as to reduce the influence of vegetation error caused by the reflector height of snow-free and snow surface.

The roughness of snow surface will also lead to a retrieval error. In the article, the snow surface is regarded as a plane when extracting the reflector height, and it is not corrected temporarily.

For the above description, the calculation results of the reflector height in the snow-free and snow surfaces will not cause significant errors due to the change in the position of the mirror point. Therefore, the rise and fall stages of the satellite can be used as a signal source when selecting the experimental data. Nevertheless, it is necessary to determine whether it is a continuous observation period in advance in order to select the available arc segment.

## 2.2.2. Selection and Analysis of Experimental Data

Figure 3 shows the PBO snow depth data between days of year (DOYs) 024 and 065 of 2017. The article also selects GNSS observation data at this time, and the observation period selected in the article is when the snow has reached the deepest state, followed by the process of ablation. The feasibility and accuracy of snow depth retrieval using multi-GNSS and multi-frequency SNR data are verified by the change in the snow depth.

During the experiment period, when the GNSS signal is transmitted to the surface receiver, the signal will pass through the atmosphere, and a signal refraction effect will occur when passing through the troposphere. Williams et al. considered that tropospheric delay will cause height error in the obtained vertical reflection distance [31]. Aiming at this problem, this article gives the tropospheric delay information during the experiment, as shown in Figure 4.



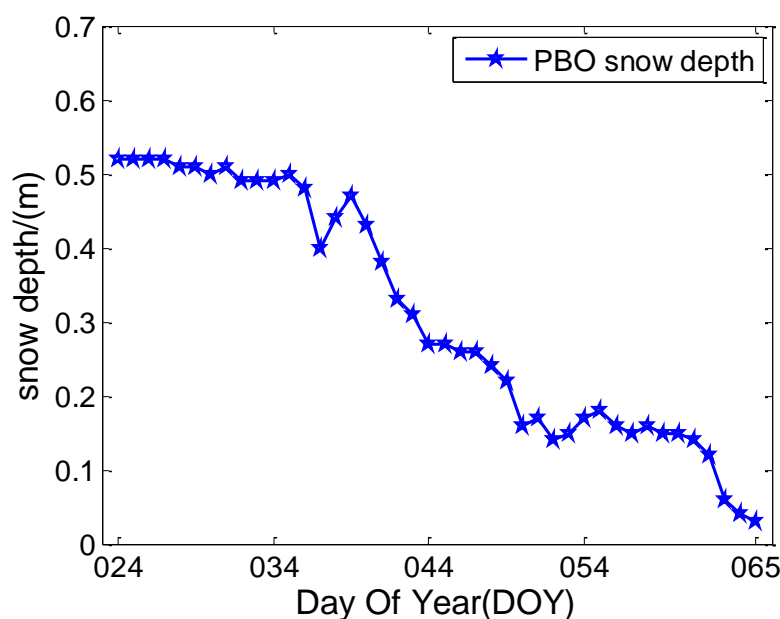


Figure 3. Snow depth of P387 in the experimental period.

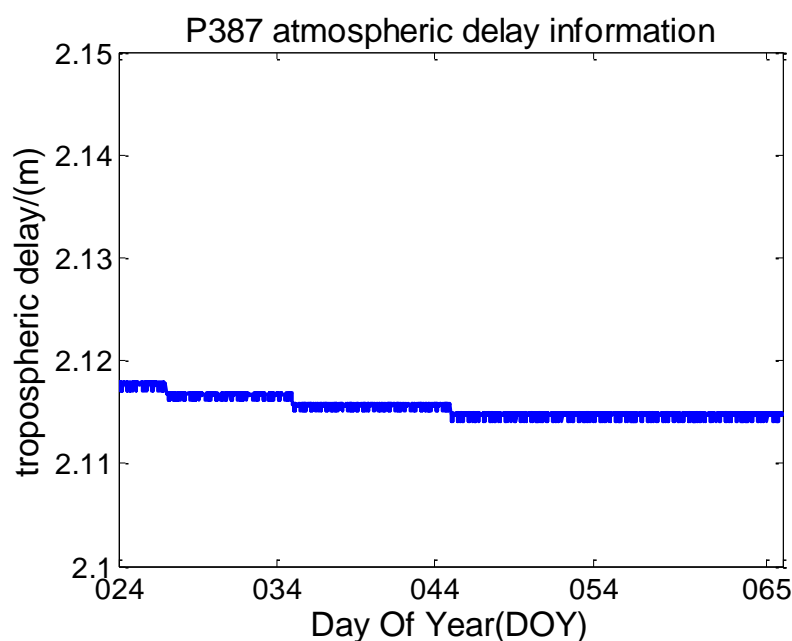


Figure 4. Atmospheric delay information of P387 station during the experiment.

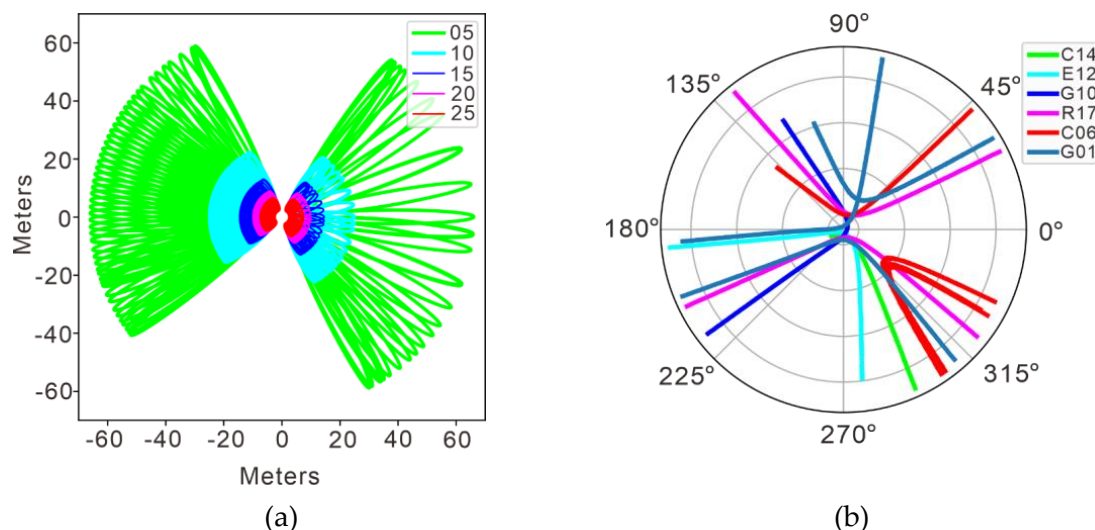
As can be seen from Figure 4, the troposphere delay slowly changes during the 42 days of experiment, and is basically the same. He et al. corrected the tropospheric delay error in the process of retrieving coastal typhoon storm surge by using GNSS-IR signal, and the final accuracy was only improved by approximately 0.5 cm, which can ignore its influence [32]. Therefore, the error caused by tropospheric delay is not especially corrected in the process of snow depth retrieval.

### 2.2.3. Reflection Region Analysis

The effective reflection region of GNSS signal to the surface can be described by the first Fresnel reflection region, which is a group of ellipses related to the receiver antenna height, satellite azimuth, and satellite elevation angle.

Figure 5a shows the Fresnel reflection region of GPS G10 satellite with DOY of 024 in 2017 at P387 station. Assuming that receiver antenna height is 2 m, different color lines

represent the reflection regions with different satellite elevation angles. With the increase in the elevation angle, the Fresnel reflection region will be smaller. The figure shows the Fresnel reflection region map of the satellite elevation angle of 5–25 degrees.



**Figure 5.** Reflection region and reflection point track: (a) Fresnel reflection region around P387 station; (b) ground motion trajectory of reflection points around P387 station.

It can be seen that the effective reflection region is related to the satellite elevation angle. When the satellite elevation angle gradually increases, the effective reflection region will decrease in size, and will gradually approach the receiver antenna. Large interference will occur when the satellite is at a low elevation angle. The larger the satellite elevation angle, the less affected the satellite is by the multipath of surrounding signals. Therefore, the signal data with low satellite elevation angle should be selected in the process of snow depth retrieval.

Figure 5b shows that the trajectory of reflection points changes with the change in the relative position between GNSS satellite and receiver, showing both different directions and distributions at different arcs and the ground reflection point trajectory formed by some satellites of the four GNSS systems. The combined signal sensing range of the four GNSS systems is significantly expanded, which can provide more data sources and wider sensing region, which is conducive to improving the time resolution of snow depth retrieval.

#### 2.2.4. SNR Types

PBO provides multi-GNSS and multi-frequency SNR data in the observation data of receiver independent exchange format (RINEX) version 3.03. The SNR types of P387 station mainly include S1C, S1W, S2L, S2W, and S5Q for GPS; S1C and S2C for GLONASS; S1C, S5Q, S6C, S7Q, and S8Q for Galileo; S2I, S6I, and S7I for BDS; S1C, S2L, and S5Q for quasi-zenith satellite system (QZSS); and S1C and S5I for satellite-based augmentation system (SBAS). The data sampling interval is 15 s, and the specific information is shown in Table 1.

Table 1 shows that the P387 station provides SNR data of different signal types of six satellite systems. After reading the data, it is found that the QZSS and SBAS have fewer satellites and no available arc segments. Therefore, this article does not consider using QZSS and SBAS data for snow depth retrieval; instead, the SNR data of GPS, GLONASS, Galileo, and BDS are used. In the article, multi-GNSS and multi-frequency SNR data are used to retrieve the snow depth. In addition to GPS, the observation satellites will be extended to other systems, which is of great help in improving the retrieval accuracy of snow depth and expanding the observation range and time resolution.

**Table 1.** Multi-GNSS and multi-frequency SNR types and description information provided by the P387 station.

Satellite System	Frequency Band/Frequency (MHz)	Channel or Code	Carrier Phase	SNR Types	Yes/No Use
GPS	L1/1575.42	C/A	L1C	S1C	YES
		Z-tracking and similar (AS on)	L1W	S1W	
	L2/1227.60	L2C(L)	L2L	S2L	
		Z-tracking and similar (AS on)	L2W	S2W	
GLONASS	L5/1176.45	Q	L5Q	S5Q	YES
	G1/(1602 + k*9/16)	C/A	L1C	S1C	
	K = −7 ... + 12	C/A	L2C	S2C	
	G2/(1246 + k*7/16)				
Galileo	E1/1575.42	C	L1C	S1C	YES
	E5a/1176.45	Q	L5Q	S5Q	
	E6/1278.75	C	L6C	S6C	
	E5b/1207.14	Q	L7Q	S7Q	
	E5(E5a + E5b)/1191.795	Q	L8Q	S8Q	
BDS	B1/1561.098	I	L1I	S2I	YES
	B3/1268.52	I	L6I	S6I	
	B2/1207.140	I	L7I	S7I	
QZSS	L1/1575.42	C/A	L1C	S1C	NO
	L2/1227.60	L2C(L)	L2L	S2L	
	L5/1176.45	Q	L5Q	S5Q	
SBAS	L1/1575.42	C/A	L1C	S1C	NO
	L5/1176.45	I	L5I	S5I	

Note: When reading RINEX 3.03, BDS 1I/Q/X and 2I/Q/X can be regarded as the same as 2I/Q/X in the current RINEX standard, and the AS in Table 1 is anti-spoofing.

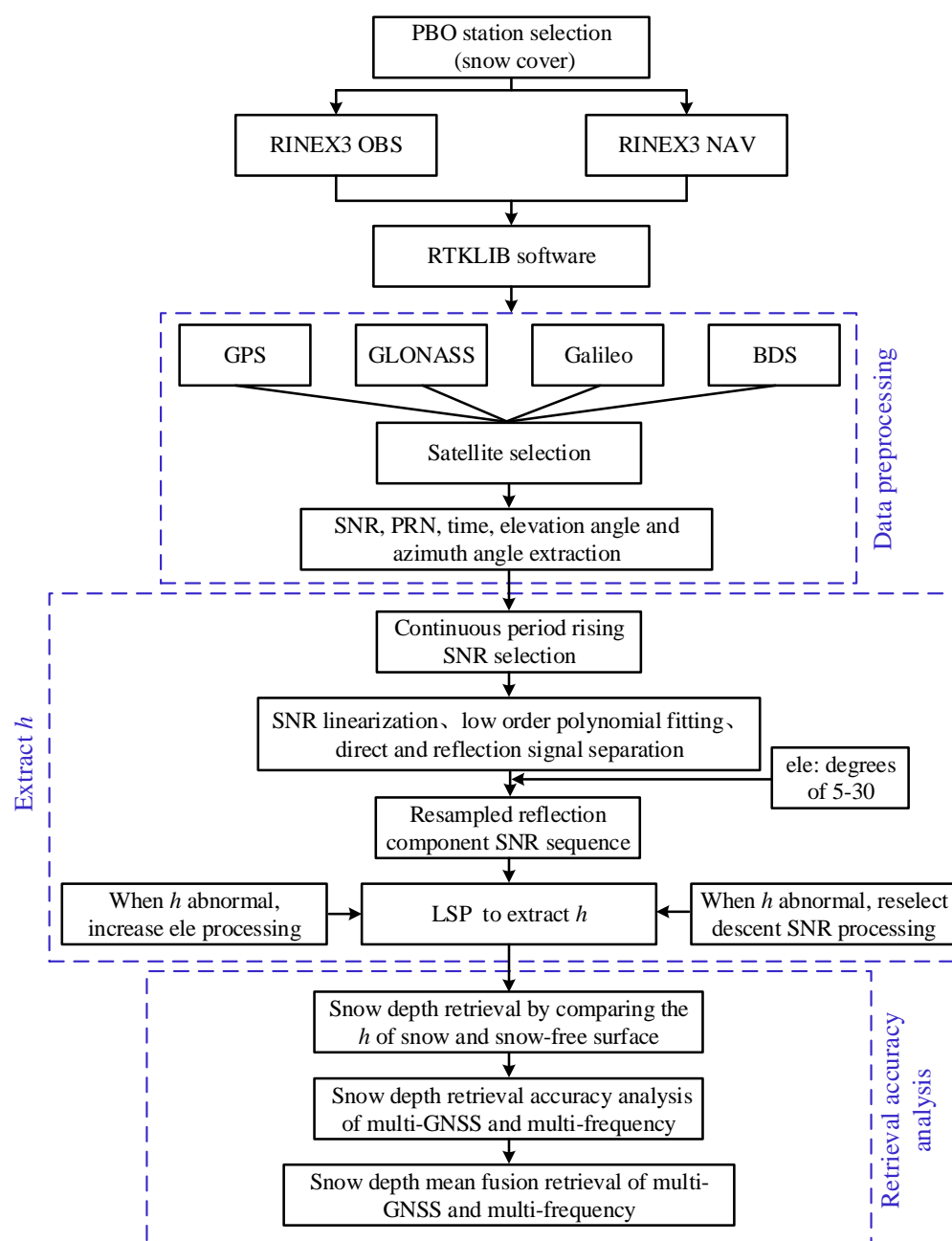
### 3. Experiment and Results

#### 3.1. Experimental Technical Scheme

Figure 6 shows the experimental technical scheme of multi-GNSS and multi-frequency GNSS-IR snow depth retrieval. It can be seen that the technical route of the article can be divided into three parts: (1) GNSS-IR data preprocessing is carried out, where the SNR, pseudo-random noise (PRN), satellite elevation angle, azimuth angle, and other data parameters are extracted from the observation (OBS) file and navigation (NAV) file collected by GNSS receivers; (2) the LSP method is used to analyze both the reflector height of snow-free and snow surfaces and the difference between them in order to retrieve the snow depth; (3) the multi-GNSS and multi-frequency GNSS-IR snow depth retrieval results and PBO snow depth data are compared, and then the mean fusion analysis of the multi-GNSS and multi-frequency GNSS-IR snow depth retrieval results is carried out.

Figure 6 shows that RTKLIB software is used for data processing in the article. By reading the OBS file and NAV file in RINEX 3.03 format, the corresponding elevation angle, azimuth angle, SNR, and other data can be extracted. In order to select the satellites in the four GNSS systems that have available observation arc data in 42 days of the experimental stage, this article finally sets the G10 satellite of GPS, R17 satellite of GLONASS, E12 satellite of Galileo, and C14 satellite of BDS as the experimental data source satellites. In the article, the SNR data in the rising stage are mainly selected for processing. When the retrieval results show abnormal values, the SNR data in the falling stage can be selected as a supplement for retrieval. At the same time, the minimum elevation angle threshold of 5 degrees can also be increased accordingly in order to achieve a more practical retrieval value.



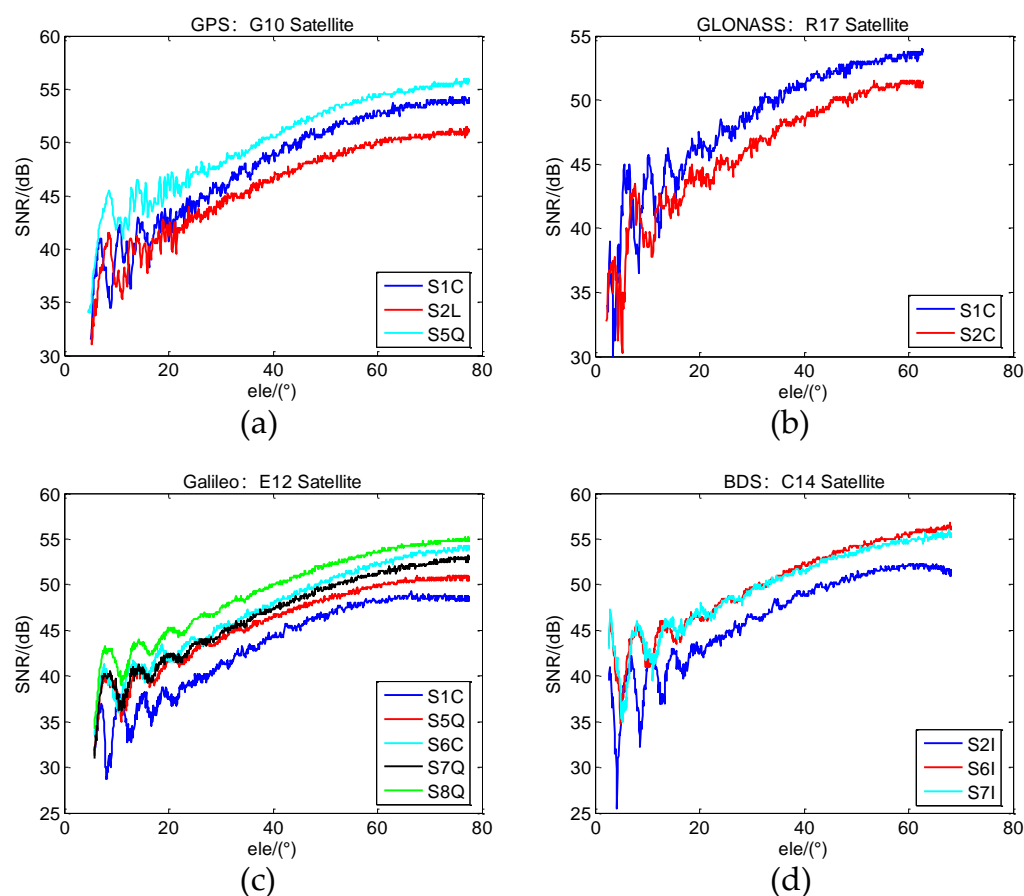


**Figure 6.** The technical process of multi-GNSS and multi-frequency GNSS-IR snow depth retrieval. Among the ele is the satellite elevation angle.

### 3.2. Extraction $h$

#### 3.2.1. Multi-GNSS and Multi-Frequency SNR Sequence Extraction

In the article, multi-GNSS and multi-frequency SNR sequences are extracted by RTKLIB software. Figure 7 shows the rising SNR sequences of G10 (S1C, S2L, and S5Q), R17 (S1C and S2C), E12 (S1C, S5Q, S6C, S7Q, and S8Q), and C14 (S2I, S6I, and S7I) satellites in the four GNSS systems on DOY 024 in 2017. Through data preprocessing, it is found that the SNR values of G10 (S1W and S2W) are the same, and that the SNR difference with other signal frequencies is significant. Therefore, these two types of SNR data are not used for the experimental in the article. Figure 7 shows the SNR sequence change in the elevation angle from low to high.



**Figure 7.** Multi-GNSS and multi-frequency SNR sequences: (a) DOY 024: GPS SNR sequence; (b) DOY 024: GLONASS SNR sequence; (c) DOY 024: Galileo SNR sequence; (d) DOY 024: BDS SNR sequence.

Figure 7 shows that the SNR sequence has strong oscillation at a low elevation angle. It is greatly affected by multipath at a low elevation angle, and the interference caused by the direct signal and the reflected signal is obvious. When increasing the elevation angle, the interference degree gradually decreases. Therefore, after removing the direct signal from the SNR sequence, this article mainly selects the SNR sequence of the reflected signal in the range of elevation angles of 5–30 degrees for snow depth retrieval. At the same time, it can be seen that the SNR sequences of the four GNSS systems at different frequencies have specific differences.

### 3.2.2. SNR Sequence Data Processing

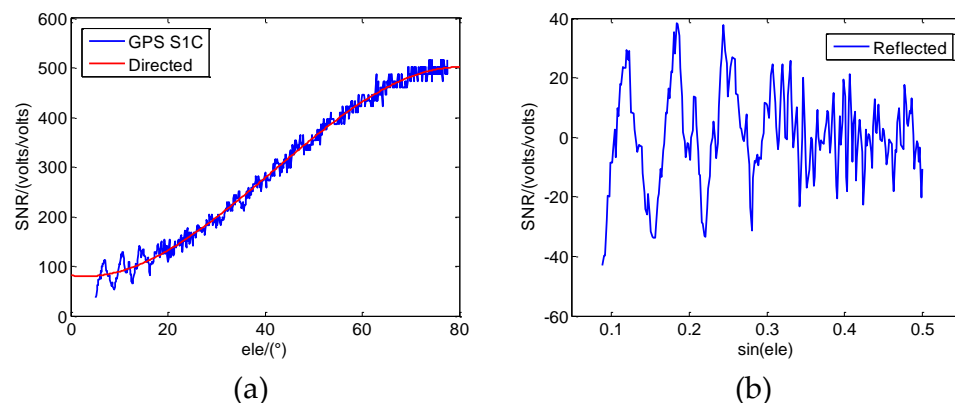
In the article, the composite SNR sequence is linearized first, and then the linearized SNR sequence is fitted by a cubic low-order polynomial to obtain the direct signal part. The SNR sequence of the reflected signal is obtained by subtracting the composite SNR sequence from the direct signal part. Figure 8 shows the processing of GPS S1C SNR data.

### 3.2.3. LSP Analysis Results of the Snow Surface

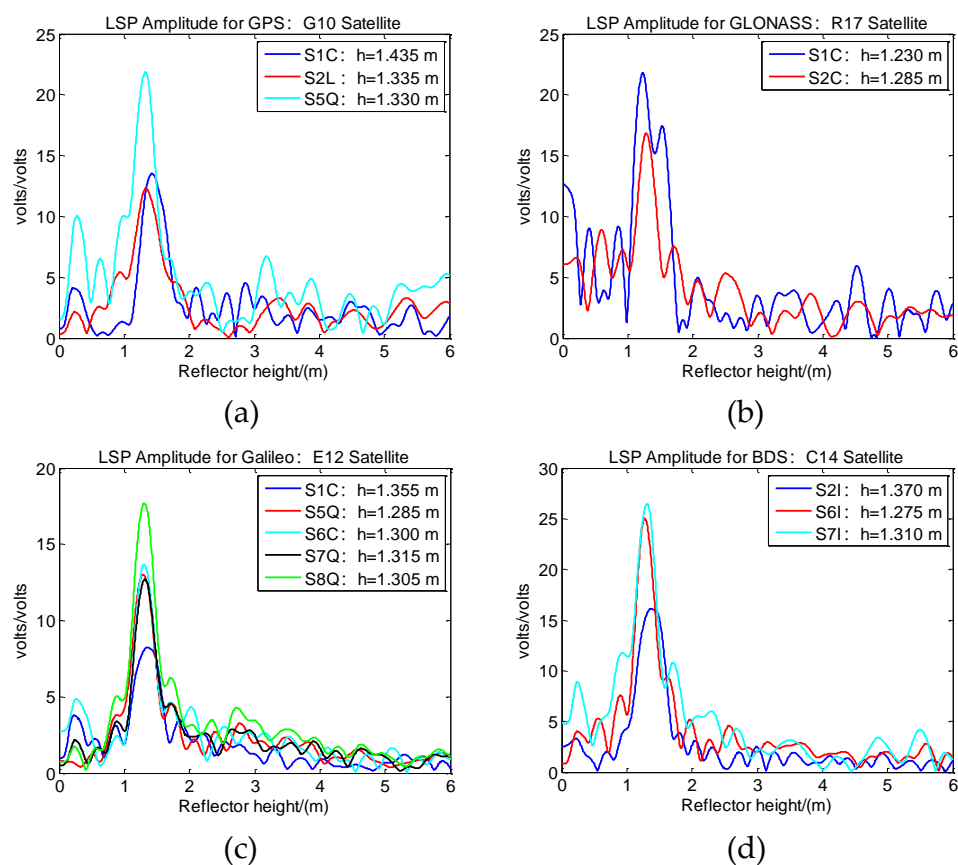
Based on the LSP method analysis of the SNR sequence of the multi-GNSS and multi-frequency reflection signal of DOY 024 in 2017, the results are shown in Figure 9.

Figure 9 shows that there are some differences in the results of the multi-GNSS and multi-frequency LSP analysis. Specifically, the S2L and S5Q results in GPS are 1.335 m and 1.330 m, which are consistent and close to 0.1 m compared with the S1C results. The results of S1C and S2C in GLONASS are 1.230 m and 1.285 m, and the difference is 0.055 m. The results of S1C, S5Q, S6C, S7Q, and S8Q in Galileo are 1.355 m, 1.285 m, 1.300 m, 1.315 m, and 1.305 m. The difference between the maximum and the minimum is 0.070 m, and the

deviation of S5Q, S6C, S7Q, and S8Q is slight. The results of S6I and S7I in BDS are 1.275 m and 1.310 m, respectively, and the difference is slight. The difference between the results of S6I and S2I is 0.095 m. From the above data, it can be seen that the LSP analysis results of different GNSS systems are different, and that the results of different frequencies in each GNSS system are also different, but the overall consistency is good. In the article, through the LSP method analysis, the reflector height in the multi-GNSS and multi-frequency can be obtained, and the LSP of the snow surface can be obtained.



**Figure 8.** SNR sequence data processing: (a) GPS S1C SNR and direct signal fitting; (b) reflected signal extraction.



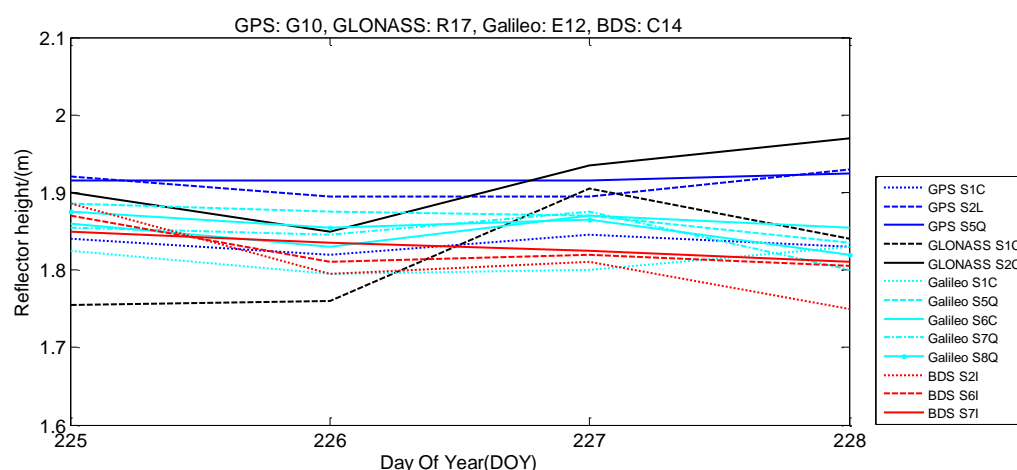
**Figure 9.** Multi-GNSS and multi-frequency LSP analysis results: (a) GPS LSP results; (b) GLONASS LSP results; (c) Galileo LSP results; (d) BDS LSP results.

### 3.2.4. LSP Analysis Results of the Snow-Free Surface

In order to weaken the difference between the multi-GNSS and multi-frequency LSP results, this article proposes that the snow-free surface reflector height is analyzed by

the multi-GNSS and multi-frequency LSP results. Using the above method, the four-day accumulated data (satellites G10, R17, E12, and C14) of DOY 225–228 in 2017 were selected for processing; this period is about October and belongs to the defined bare soil period. This article selects the data of this period to process, which can reduce the influence of surface vegetation on signal propagation. The multi-GNSS and multi-frequency reference values were obtained by averaging the four-day LSP results.

Figure 10 shows that there are some differences in the results of multi-GNSS and multi-frequency LSP. There are some differences between the results of GPS S1C, S2L, and S5Q, but the results of a single frequency at 4 days are basically the same, with slight deviation. The Galileo S5Q, S6C, S7Q, and S8Q results are basically the same, and S1C has a specific difference, but the results of a single frequency at 4 days are basically the same. The deviation of the BDS S6I and S7I results is slight, and the deviation of the S2I results is significant at 225 and 228 on the annual accumulation day. The results of the GLONASS S1C analysis showed a significant variation at 227 accumulated days, and the rest showed good consistency. In the article, the snow depth is obtained through the comparison of the reflector height of different GNSS systems at different frequencies under snow and snow-free surfaces, which can better adapt to the use of multi-GNSS and multi-frequency GNSS-IR technology. The reference value of the reflector height in different GNSS systems at different frequencies is calculated, as shown in Table 2.



**Figure 10.** The snow-free surface reflector height reference value of multi-GNSS and multi-frequency LSP analysis results.

**Table 2.** Multi-GNSS and multi-frequency LSP mean values of the snow-free reflector height.

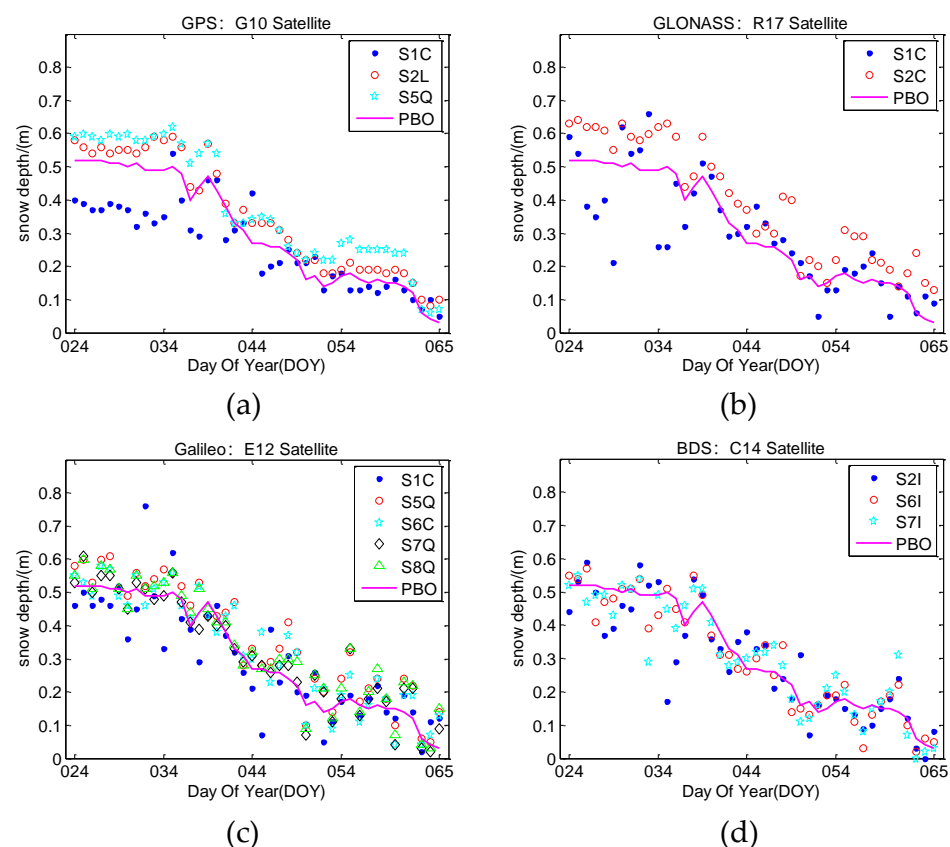
Satellite System	SNR Types	Mean LSP of 4 Days/m
GPS	S1C	1.834
	S2L	1.910
	S5Q	1.918
GLONASS	S1C	1.815
	S2C	1.914
Galileo	S1C	1.813
	S5Q	1.866
	S6C	1.854
	S7Q	1.844
	S8Q	1.854
BDS	S2I	1.810
	S6I	1.826
	S7I	1.830

Table 2 shows that the results of LSP at different frequencies of the four GNSS systems are more than 1800 m, which is more in line with the actual situation and can be used as the initial reference value of the reflector height of the snow-free surface.

### 3.3. GNSS-IR Snow Depth Retrieval Results

#### 3.3.1. Multi-GNSS and Multi-Frequency GNSS-IR Snow Depth Retrieval Results

The snow depth is obtained by comparing and analyzing the difference in reflector height under snow-free and snow surfaces. The results of the different frequency retrievals of GPS, GLONASS, Galileo, and BDS are compared with the PBO snow depth data, and the results are shown in Figure 11.



**Figure 11.** Comparison between multi-GNSS and multi-frequency GNSS-IR snow depth retrieval results and PBO snow depth: (a) GPS snow depth retrieval results; (b) GLONASS snow depth retrieval results; (c) Galileo snow depth retrieval results; (d) BDS snow depth retrieval results.

Figure 11 shows that the snow depth retrieval from the multi-GNSS and multi-frequency SNR data has a trend that is similar to that of the PBO snow depth data. Among them, the results of S1C in GPS are more biased than those of S2L and S5Q. The trend of the S1C results in GLONASS is worse than that of S2C. The results of S1C in Galileo are worse than those of S5Q, S6C, S7Q, and S8Q. The trend of the BDS S2I results is worse than that of the S6I and S7I results.

#### 3.3.2. Mean Fusion of Multi-Frequency Retrieval Results in the Four GNSS Systems

The results of the mean fusion of different frequencies in the four GNSS systems are shown in Figure 12.

Figure 12 shows the consistency between the retrieval results of the four GNSS systems and the PBO snow depth, where the trend is more consistent than the previous single frequency retrieval results.



### 3.3.3. Mean Fusion Retrieval Results of Multi-GNSS System

After the mean fusion of multi-frequency in the four GNSS systems, the retrieval results of highly similar trends are obtained. To further improve the accuracy, the mean fusion of the snow depth retrieval results of the multi-GNSS system is carried out, and the final GNSS system retrieval results are obtained, as shown in Figure 13.

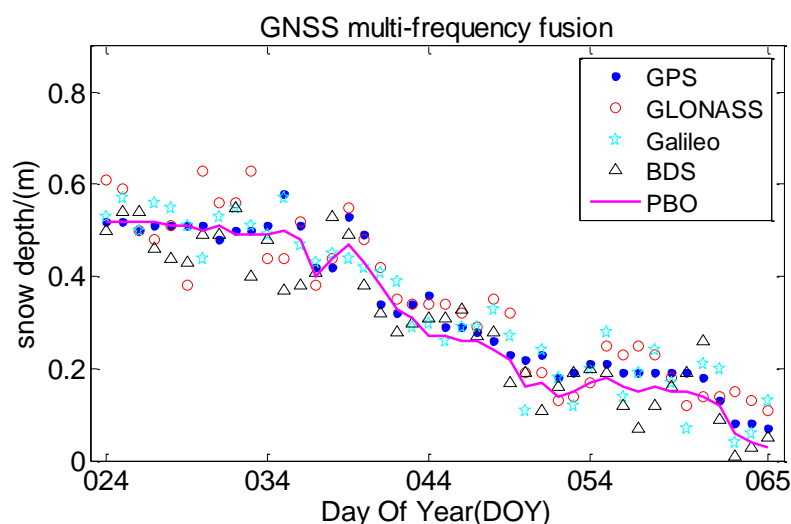


Figure 12. Mean fusion of multi-frequency retrieval results in the four GNSS systems.

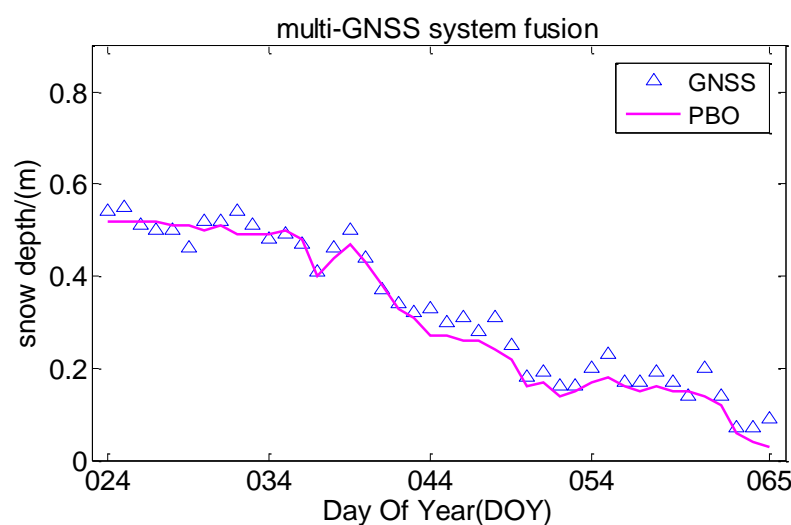


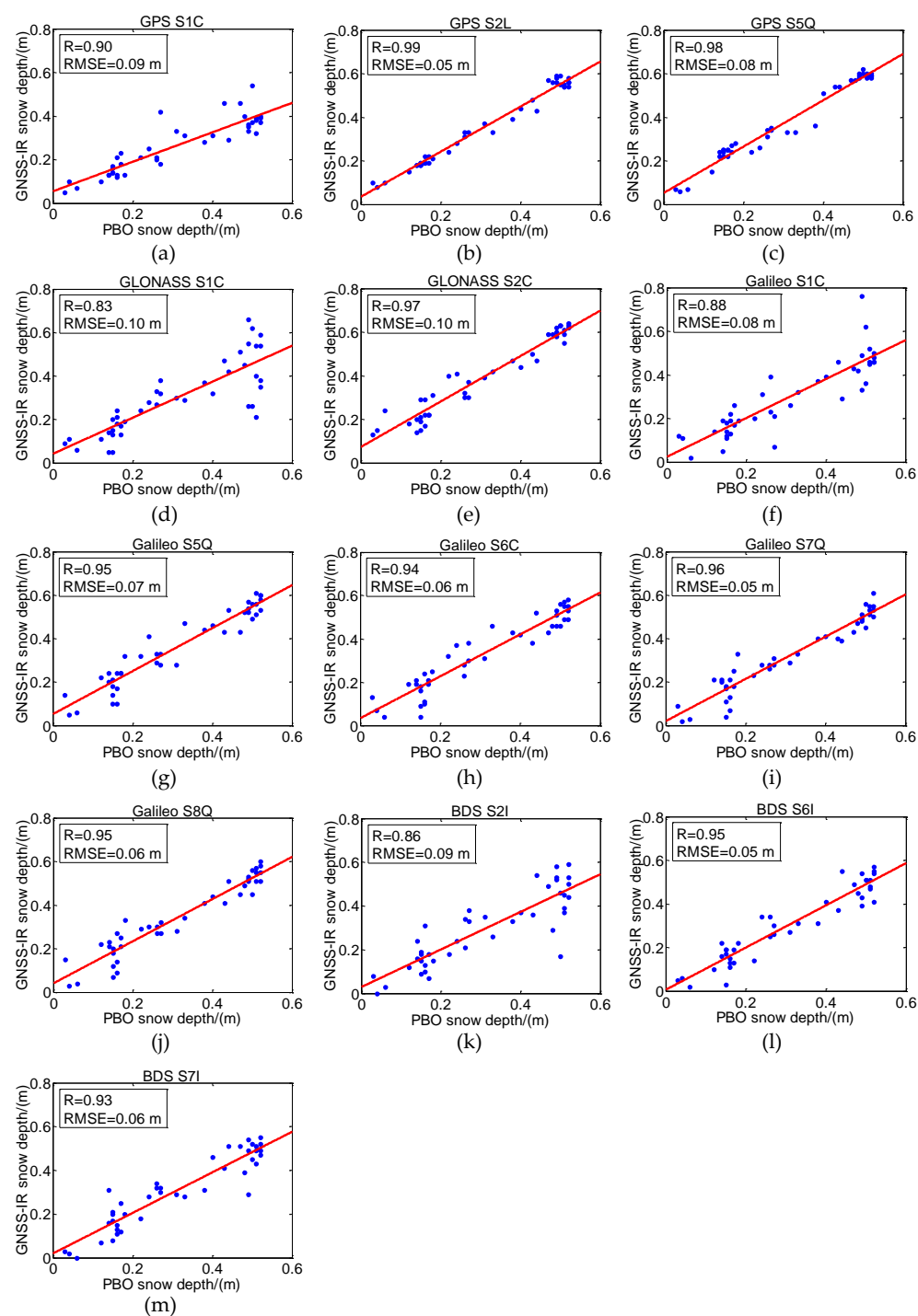
Figure 13. Mean fusion retrieval results of multi-GNSS system.

Figure 13 shows that the mean fusion results between the multi-GNSS system are in good agreement with the PBO snow depth results, and that the trend is basically the same.

## 4. Discussion

### 4.1. Accuracy Analysis between Multi-GNSS and Multi-Frequency GNSS-IR Snow Depth Retrieval Results and PBO Snow Depth

The above retrieval results are further analyzed, and the retrieval results of different frequency signals in multi-GNSS system are compared; the correlation coefficient ( $R$ ) and root mean square error (RMSE) are shown in Figure 14.



**Figure 14.** Correlation and RMSE between multi-GNSS and multi-frequency GNSS-IR snow depth retrieval results and PBO snow depth: (a) GPS S1C; (b) GPS S2L; (c) GPS S5Q; (d) GLONASS S1C; (e) GLONASS S2C; (f) Galileo S1C; (g) Galileo S5Q; (h) Galileo S6C; (i) Galileo S7Q; (j) Galileo S8Q; (k) BDS S2I; (l) BDS S6I; (m) BDS S7I.

Figure 14 shows the correlation of multi-GNSS and multi-frequency GNSS-IR snow depth retrieval results compared with the PBO snow depth. Table 3 shows the specific R and RMSE.

**Table 3.** R and RMSE between multi-GNSS and multi-frequency GNSS-IR snow depth retrieval results and PBO snow depth.

Satellite System	SNR Types	R	RMSE/m
GPS	S1C	0.90	0.09
	S2L	0.99	0.05
	S5Q	0.98	0.08
GLONASS	S1C	0.83	0.10
	S2C	0.97	0.10
Galileo	S1C	0.88	0.08
	S5Q	0.95	0.07
	S6C	0.94	0.06
	S7Q	0.96	0.05
	S8Q	0.95	0.06
BDS	S2I	0.86	0.09
	S6I	0.95	0.05
	S7I	0.93	0.06

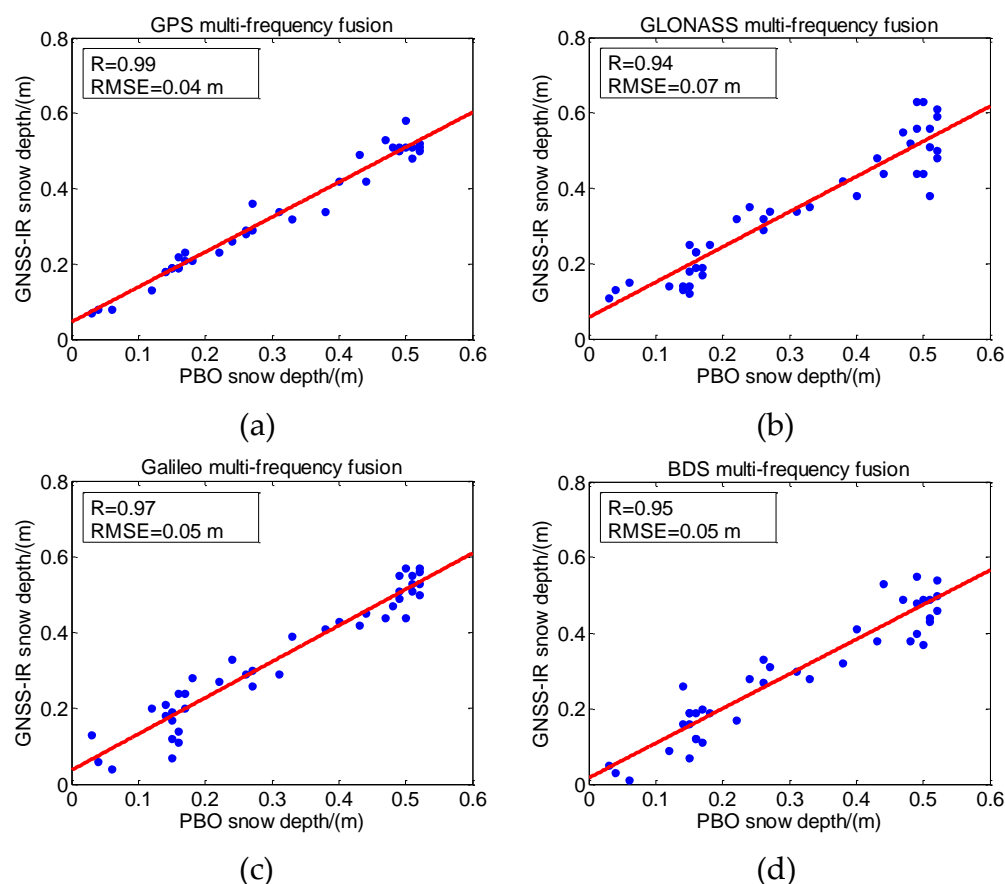
Figure 14 and Table 3 show that the snow depth results of the GNSS-IR retrieval at different frequencies of the four GNSS systems have a strong correlation with the PBO snow depth. The R of the GPS S2L and S5Q results were 0.99 and 0.98, respectively, which are highly correlated, whereas the R of the S1C was 0.90, which is relatively low. The R of GLONASS S1C and S2C were 0.83 and 0.97, respectively. The correlation of S2C was strong and that of S1C was weak. The R of Galileo S5Q, S6C, S7Q, and S8Q results was approximately 0.95, and that of S1C was 0.88, which is rather weak. The R of BDS S6I and S7I results was 0.95 and 0.93, showing a strong correlation, and that of S2I was 0.86, which was rather weak. At the same time, the RMSE of the results of different frequencies of the four GNSS systems and PBO data were basically in the range of 5 cm to 10 cm, and the error was small. The above data show that the feasibility of retrieving the snow depth using multi-GNSS and multi-frequency GNSS-IR is high. At the same time, for GPS S1C, GLONASS S1C, Galileo S1C, and BDS S2I, the results in the four GNSS systems are rather weak. From the above results, in addition to GPS and GLONASS signals, the Galileo and BDS signals also have a good ability in snow depth retrieval.

#### 4.2. Accuracy Analysis of Multi-Frequency Mean Fusion Results in the GNSS Systems

Mean fusion retrieval is carried out for multi-frequency retrieval results under the four GNSS systems; the accuracy between the retrieval results and PBO snow depth are further analyzed, as shown in Figure 15.

Figure 15 shows that the retrieval results of the four GNSS systems are obtained by averaging the snow depth results of the GNSS-IR retrieval at multi-frequency. The R between the GPS, GLONASS, Galileo, BDS, and PBO results was 0.99, 0.94, 0.97, and 0.95, respectively, showing strong correlations. At the same time, the RMSE of the four GNSS systems have been reduced to a certain extent, to basically in the range of 4 cm to 7 cm, indicating that the mean fusion of different frequency retrieval results in the four GNSS systems has a good effect on the improvement of retrieval accuracy, which can eliminate the weak correlation of GPS S1C, GLONASS S1C, Galileo S1C, and BDS S2I.

Compared with the snow depth of the different frequency signal in the multi-GNSS system retrieval results, the GNSS multi-frequency mean fusion method can effectively improve the retrieval accuracy. The specific improvement accuracy is shown in Table 4.



**Figure 15.** Mean fusion accuracy analysis of multi-frequency retrieval results in the four GNSS systems: (a) GPS multi-frequency fusion; (b) GLONASS multi-frequency fusion; (c) Galileo multi-frequency fusion; (d) BDS multi-frequency fusion.

**Table 4.** Comparison of different frequency signal in the multi-GNSS system retrieval results; multi-frequency mean fusion accuracy increases in R and decreases in the RMSE.

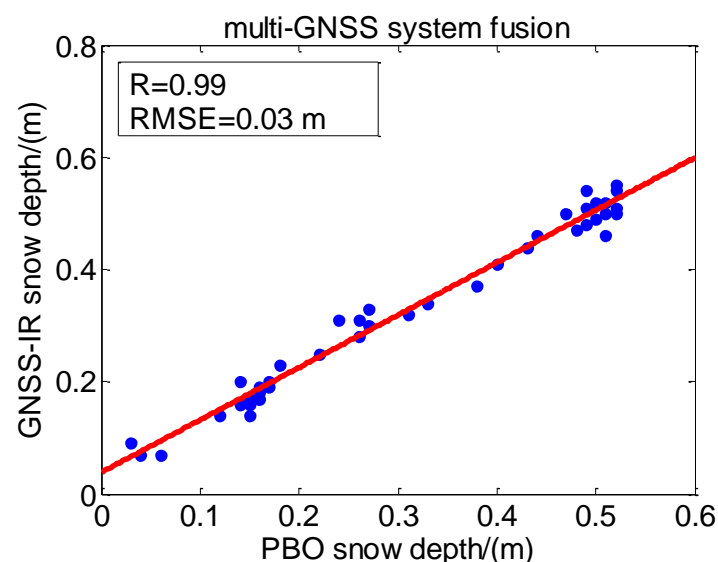
Satellite System	SNR Types	Increases in R	Decreases in the RMSE
GPS	S1C	9.1%	55.6%
	S2L	0.0%	20.0%
	S5Q	1.0%	50.0%
GLONASS	S1C	11.7%	30.0%
	S2C	−3.2%	30.0%
Galileo	S1C	9.3%	37.5%
	S5Q	2.1%	28.5%
	S6C	3.1%	16.7%
	S7Q	1.0%	0.0%
	S8Q	2.1%	16.7%
BDS	S2I	9.5%	44.4%
	S6I	0.0%	0.0%
	S7I	2.1%	16.7%

As can be seen from Table 4, the R of the GNSS multi-frequency mean fusion increases by 11.7%, which is higher than a single frequency in multi-GNSS system retrieval results, and the GLONASS S2C results decrease by 3.2%, but most of the results' correlations are improved. At the same time, the RMSE decreases by 55.6%, and though the retrieval accuracy of Galileo S7Q and BDS S6I is not improved, the other accuracy has been greatly

improved. This shows that the mean fusion of the GNSS multi-frequency retrieval results can effectively improve the accuracy of the snow depth retrieval.

#### 4.3. Accuracy Analysis of Mean Fusion Retrieval between Multi-GNSS System

The accuracy of multi-frequency fusion retrieval results has been improved to a certain extent. Furthermore, the fusion accuracy of the retrieval results of the four GNSS systems is analyzed, as shown in Figure 16.



**Figure 16.** Comparison of the mean fusion results of multi-GNSS system with PBO snow depth.

Figure 16 shows that the R between the mean fusion results of the multi-GNSS system and PBO snow depth was 0.99, showing a strong correlation. At the same time, the RMSE was 3 cm, and the error was also significantly reduced, indicating the effectiveness of this method.

In order to further improve the combined retrieval accuracy of the GNSS system, the GNSS multi-frequency fusion results are further mean fused. The fusion results are compared with the four GNSS systems, and the results are shown in Table 5.

**Table 5.** Comparison of multi-frequency mean fusion; multi-GNSS system fusion accuracy increases in R and decreases in the RMSE.

Satellite System	Increases in R	Decreases in the RMSE
GPS	0.0%	25.0%
GLONASS	5.1%	57.1%
Galileo	2.0%	40%
BDS	4.0%	40%

It can be seen from Table 5 that the accuracy of the results after multi-GNSS system fusion is further improved. Compared with the results of GNSS multi-frequency fusion, the R of the four GNSS systems are improved, except for GPS. GLONASS has the highest increase of 5.1%. In terms of RMSE, GLONASS increased by 57.1%. The GPS is not improved on R, but it is improved by 25% on RMSE. It can be seen from the above results that the further fusion of the multi-frequency retrieval results of the four GNSS systems can effectively improve the retrieval accuracy. Therefore, the multi-GNSS system combined snow depth retrieval method has strong reliability.



## 5. Conclusions

Snow is an important indicator to measure the global hydrological cycle and climate. The accurate long-term monitoring of snow depth is helpful for water resource management and climate disaster warning, and has important application prospects. Based on the current GNSS-IR snow depth retrieval method, the temporal resolution is affected by the number of sky satellite arcs, so multi-GNSS and multi-frequency GNSS-IR are introduced as a supplement. The snow depth retrieval is carried out by using the multi-GNSS and multi-frequency SNR data. The snow depth parameters are obtained by comparing the LSP results of snow-free and snow surfaces. At the same time, the results are compared and analyzed in terms of the PBO snow depth, and the correlation and error analysis of the multi-GNSS and multi-frequency GNSS-IR mean fusion results are carried out. The following conclusions are drawn through experimental analysis:

- (1) QZSS and SBAS systems in multi-GNSS and multi-frequency SNR data provided by PBO are not suitable for use due to the lack of observation arcs. The GPS S1W and S2W data values are the same, and the other frequency SNR data difference is too large and should not be used;
- (2) The LSP results of the snow-free surface can be effectively used as the initial reflector height reference value. The snow depth results of multi-GNSS and multi-frequency GNSS-IR retrieval have a strong correlation with PBO snow depth data, and the RMSE of different frequency retrieval results in the multi-GNSS system is between 5 cm and 10 cm. The correlation between the retrieval results of the GPS L1, GLONASS G1, Galileo E1, and BDS B1 bands in the snow depth retrieval results is rather weak;
- (3) The mean fusion of multi-frequency retrieval results in GPS, GLONASS, Galileo, and BDS can effectively improve the accuracy and solve the relatively weak results in some bands. The four GNSS systems retrieval results show a strong correlation, and the RMSE is between 4 cm and 7 cm. Comparing the different frequency signals in the multi-GNSS system retrieval results, the multi-frequency mean fusion increase by 11.7% in R and the RMSE decreases by 55.6%, which is the highest;
- (4) The mean fusion accuracy of the retrieval results of the GPS, GLONASS, Galileo, and BDS is significantly improved. The R between the retrieval results and the PBO results is 0.99, and the retrieval accuracy is better than 3 cm, which significantly enhances the accuracy. In the comparison of the multi-frequency mean fusion, the multi-GNSS system fusion increases by 5.1% in R and the RMSE decreases by 57.1%, which is the highest.

Compared with a single GNSS-IR signal, multi-GNSS and multi-frequency GNSS-IR improves the accuracy, continuity, and time resolution of snow depth retrieval. A mean fusion of multi-GNSS and multi-frequency GNSS-IR retrieval results can further enhance the accuracy. With the development of global navigation systems, more types of signals and perfect constellation structures will be provided. Multi-GNSS and multi-frequency GNSS-IR will play a more critical role in the field of snow depth detection.

**Author Contributions:** Conceptualization, H.W., R.Z. and L.Y.; methodology, J.T.; formal analysis, J.L. and X.L.; data curation, S.N., P.L., Y.W. and N.L.; writing—original draft preparation, J.T.; writing—review and editing, H.W. and R.Z.; supervision, H.W. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research was funded by the Jiangsu Agriculture Science and Technology Innovation Fund, grant number: CX (21) 3068 and the Anhui Educational Commission Key Project, grant number: KJ2020A00706.

**Institutional Review Board Statement:** Not applicable.

**Informed Consent Statement:** Not applicable.

**Data Availability Statement:** The GNSS site data were provided under the PBO Observation Program of the United States, and the measured snow depth data were obtained from <https://data.unavco.org/archive/gnss/products> (accessed on 21 October 2021).

**Acknowledgments:** We thank the PBO Observation Program of the United States for providing the GNSS data, and the University of Colorado for providing data for snow depth comparison analysis. We thank RTKLIB software for providing early SNR extraction. We also thank Roesler, C. and Larson, K.M. for providing open access MATLAB code to generate reflector heights from GNSS SNR data (the paper that accompanies this code: Software tools for GNSS interferometric reflectometry (GNSS-IR)).

**Conflicts of Interest:** The authors declare no conflict of interest.

## References

- Walsh, J.E. Snow cover and atmospheric variability: Changes in the snow covering the earth's surface affect both daily weather and long-term climate. *Am. Sci.* **1984**, *72*, 50–57.
- Rott, H.; Yueh, S.H.; Cline, D.W.; Duguay, C.; Essery, R.; Haas, C.; Heliere, F.; Kern, M.; Macelloni, G.; Malnes, E.; et al. Cold Regions Hydrology High-Resolution Observatory for Snow and Cold Land Processes. *IEEE Proc.* **2010**, *98*, 752–765. [\[CrossRef\]](#)
- Larson, K.M.; Gutmann, E.D.; Zavorotny, V.U.; Braun, J.J.; Williams, M.W.; Nievinski, F.G. Can we measure snow depth with GPS receivers? *Geophys. Res. Lett.* **2009**, *36*, 876–880. [\[CrossRef\]](#)
- Georgiadou, Y.; Kleusberg, A. On Carrier Signal Multipath Effects in Relative GPS Positioning. *Manuscr. Geod.* **1988**, *13*, 172–179.
- Ge, L.; Han, S.; Rizos, C. Multipath Mitigation of Continuous GPS Measurements Using an Adaptive Filter. *GPS Solut.* **2000**, *4*, 19–30. [\[CrossRef\]](#)
- Ray, J.K.; Cannon, M.E. Synergy between Global Positioning System Code, Carrier, and Signal-to-Noise Ratio Multipath Errors. *J. Guid. Control Dyn.* **2001**, *24*, 54–63. [\[CrossRef\]](#)
- Larson, K.M.; Small, E.E.; Gutmann, E.D.; Bilich, A.L.; Braun, J.J.; Zavorotny, V.U. Use of GPS receivers as a soil moisture network for water cycle studies. *Geophys. Res. Lett.* **2008**, *35*, 1–5. [\[CrossRef\]](#)
- Nievinski, F.G.; Larson, K.M. Inverse Modeling of GPS Multipath for Snow Depth Estimation—Part I: Formulation and Simulations. *IEEE Trans. Geosci. Remote Sens.* **2014**, *52*, 6555–6563. [\[CrossRef\]](#)
- Nievinski, F.G.; Larson, K.M. Inverse Modeling of GPS Multipath for Snow Depth Estimation—Part II: Application and Validation. *IEEE Trans. Geosci. Remote Sens.* **2014**, *52*, 6564–6573. [\[CrossRef\]](#)
- Wan, W.; Larson, K.M.; Small, E.E.; Chew, C.C.; Braun, J.J. Using geodetic GPS receivers to measure vegetation water content. *GPS Solut.* **2015**, *19*, 237–248. [\[CrossRef\]](#)
- Larson, K.M.; Small, E.E. GPS ground networks for water cycle sensing. *IEEE Geosci. Remote Sens. Symp.* **2014**, 3822–3825.
- Larson, K.M. GPS interferometric reflectometry: Applications to surface soil moisture, snow depth, and vegetation water content in the western United States. *Wiley Interdiscip. Rev. Water* **2016**, *3*, 775–787. [\[CrossRef\]](#)
- Larson, K.M.; Nievinski, F.G. GPS snow sensing: Results from the EarthScope Plate Boundary Observatory. *GPS Solut.* **2013**, *17*, 41–52. [\[CrossRef\]](#)
- Larson, K.M.; Small, E.E. Estimation of Snow Depth Using L1 GPS Signal-to-Noise Ratio Data. *IEEE J. Sel. Top. Appl. Earth Observ. Remote Sens.* **2017**, *9*, 4802–4808. [\[CrossRef\]](#)
- Tabibi, S.; Nievinski, F.G.; Dam, T.V.; Monico, J.F.G. Assessment of modernized GPS L5 SNR for ground-based multipath reflectometry applications. *Adv. Space Res.* **2015**, *55*, 1104–1116. [\[CrossRef\]](#)
- Tabibi, S.; Nievinski, F.G.; Dam, T.V. Multi-GNSS and multi-frequency SNR multipath reflectometry of snow depth, Trans EOS, G44A-07. In Proceedings of the AGU Fall Meeting Abstract, San Francisco, CA, USA, 17 December 2015.
- Tabibi, S.; Nievinski, F.G.; Dam, T.V. Statistical Comparison and Combination of GPS, GLONASS, and Multi-GNSS Multipath Reflectometry Applied to Snow Depth Retrieval. *IEEE Trans. Geosci. Remote Sens.* **2017**, *55*, 3773–3785. [\[CrossRef\]](#)
- Jin, S.; Qian, X.; Kutoglu, H. Snow Depth Variations Estimated from GPS-Reflectometry: A Case Study in Alaska from L2P SNR Data. *Remote Sens.* **2016**, *8*, 63. [\[CrossRef\]](#)
- Zhou, W.; Liu, L.; Huang, L.; Li, J.; Chen, J.; Chen, F.D.; Xing, Y.; Liu, L. Monitoring snow depth based on the SNR signal of GLONASS satellites. *J. Remote Sens.* **2018**, *22*, 889–899. [\[CrossRef\]](#)
- Zhou, W.; Liu, L.; Huang, L.; Yao, Y.; Chen, J.; Li, S. A new GPS SNR-Based Combination Approach for Land Surface Snow Depth Monitoring. *Sci. Rep.* **2019**, *9*, 3814. [\[CrossRef\]](#)
- Wang, Z.; Liu, Z.; An, J.; Lin, G. Snow depth detection and error analysis derived from SNR of GPS and BDS. *Acta Geod. Cartogr. Sin.* **2018**, *47*, 8–16. [\[CrossRef\]](#)
- Wang, X.; Zhang, S.; Wang, L.; He, X.; Zhang, Q. Analysis and combination of multi-GNSS snow depth retrievals in multipath reflectometry. *GPS Solut.* **2020**, *24*, 1–13. [\[CrossRef\]](#)
- Bilich, A.; Larson, K.M.; Axelrad, P. Observations of signal-to-noise ratios (SNR) at geodetic GPS site CASA: Implications for phase multipath. *Proc. Cent. Eur. Geodyn. Seismol.* **2004**, *23*, 77–83.
- Bilich, A.; Larson, K.M. Mapping the GPS multipath environment using the signal-to-noise ratio (SNR). *Radio Sci.* **2007**, *42*, RS6003. [\[CrossRef\]](#)
- Zhang, S.; Peng, J.; Zhang, C.; Zhang, J.; Liu, Q. GiRsnow: An open-source software for snow depth retrievals using GNSS interferometric reflectometry. *GPS Solut.* **2021**, *25*, 1–8. [\[CrossRef\]](#)
- Roussel, N.; Ramillien, G.; Frappart, F.; Darrozes, J.; Gay, A.; Biancale, R.; Striebig, N.; Hanquiez, V.; Bertin, X.; Allain, D. Sea level monitoring and sea state estimate using a single geodetic receiver. *Remote Sens. Environ.* **2015**, *171*, 261–277. [\[CrossRef\]](#)
- Roesler, C.; Larson, K.M. Software tools for GNSS interferometric reflectometry (GNSS-IR). *GPS Solut.* **2018**, *22*, 1–10. [\[CrossRef\]](#)

- 
28. Axelrad, P.; Larson, K.; Jones, B. Use of the correct satellite repeat period to characterize and reduce site-specific multipath errors. In Proceedings of the ION GNSS 2005, Long Beach, CA, USA, 13–16 September 2005; pp. 2638–2648.
  29. Lomb, N.R. Least-squares frequency analysis of unequally spaced data. *Astrophys. Space Sci.* **1976**, *39*, 447–462. [[CrossRef](#)]
  30. Scargle, J.D. Studies in astronomical time series analysis. II—Statistical aspects of spectral analysis of unevenly spaced data. *Astrophys. J.* **1982**, *263*, 835–853. [[CrossRef](#)]
  31. Williams, S.D.P.; Nievinski, F.G. Tropospheric delays in ground-based GNSS multipath reflectometry—Experimental evidence from coastal sites. *J. Geophys. Res. Solid Earth.* **2017**, *122*, 2310–2327. [[CrossRef](#)]
  32. He, X.; Wang, J.; Wang, X.; Song, M. Retrieval of coastal typhoon storm surge using multi-GNSS-IR. *Acta Geod. Cartogr. Sin.* **2020**, *49*, 1168–1178. [[CrossRef](#)]