

Article Estimation of Hourly Rainfall during Typhoons Using Radar Mosaic-Based Convolutional Neural Networks

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Abstract: Taiwan is located at the junction of the tropical and subtropical climate zones adjacent to the Eurasian continent and Pacific Ocean. The island frequently experiences typhoons that engender severe natural disasters and damage. Therefore, efficiently estimating typhoon rainfall in Taiwan is essential. This study examined the efficacy of typhoon rainfall estimation. Radar images released by the Central Weather Bureau were used to estimate instantaneous rainfall. Additionally, two proposed neural network-based architectures, namely a radar mosaic-based convolutional neural network (RMCNN) and a radar mosaic-based multilayer perceptron (RMMLP), were used to estimate typhoon rainfall, and the commonly applied Marshall–Palmer Z-R relationship (Z-R_MP) and a reformulated Z-R relationship at each site (Z-R_station) were adopted to construct benchmark models. Monitoring stations in Hualien, Sun Moon Lake, and Taichung were selected as the experimental stations in Eastern, Central, and Western Taiwan, respectively. This study compared the performance of the models in predicting rainfall at the three stations, and the results are outlined as follows: at the Hualien station, the estimations of the RMCNN, RMMLP, Z-R_MP, and Z-R_station models were mostly identical to the observed rainfall, and all models estimated an increase during peak rainfall on the hyetographs, but the peak values were underestimated. At the Sun Moon Lake and Taichung stations, however, the estimations of the four models were considerably inconsistent in terms of overall rainfall rates, peak rainfall, and peak rainfall arrival times on the hyetographs. The relative root mean squared error for overall rainfall rates of all stations was smallest when computed using RMCNN (0.713), followed by those computed using RMMLP (0.848), Z-R_MP (1.030), and Z-R_station (1.392). Moreover, RMCNN yielded the smallest relative error for peak rainfall (0.316), followed by RMMLP (0.379), Z-R_MP (0.402), and Z-R_station (0.688). RMCNN computed the smallest relative error for the peak rainfall arrival time (1.507 h), followed by RMMLP (2.673 h), Z-R_MP (2.917 h), and Z-R_station (3.250 h). The results revealed that the RMCNN model in combination with radar images could efficiently estimate typhoon rainfall.

Keywords: rainfall; modeling; radar image; typhoon; CNN; deep learning

1. Introduction

Taiwan is situated at the junction of the tropical and subtropical climate zones, bordering the Eurasian continent and the Pacific Ocean. Natural disasters frequently occur each year because of typhoons—the strong winds and rainfall of which often lead to severe disasters. In addition, the northwest Pacific Ocean is commonly affected by typhoons; approximately four typhoons strike Taiwan every year and cause serious severe damage [1,2]. For example, typhoon Megi, a typical moderate-strength typhoon, made landfall on the east coast of Taiwan in 2016. The strong winds and heavy rain caused severe damage; buildings were buried by a mudslide down a river, and 650,000 households experienced power outages, which resulted in US\$100 million in economic

losses [3]. Improving quantitative precipitation estimation (QPE) for tropical storms is crucial for disaster mitigation [4,5].

Taiwan's Central Mountain Range (CMR) runs from the north to the south of the island, dividing it into eastern and western parts. The CMR is situated in the east and is 340 km long and 80 km wide, with an average elevation of approximately 2500 m [6]. When a typhoon strikes Taiwan from the east, it exerts its most severe effects on the eastern regions, which sustain considerable damage. By contrast, the western regions sustain less damage because the typhoon structure is often disrupted and weakened by the CMR. Notably, the distribution of major rainfall during typhoons statistically resembles the contours of terrain height, often referred to as the "phase-locking" mechanism [7]. The phase-locking mechanism can provide a basic explanation of the topographic rainfall in the CMR associated with typhoons impinging from different directions [8]. Several researchers have discussed the effects of the aforementioned mechanism, such as [9–13]. These researchers have revealed that when typhoons approach Taiwan from the east before passing through the CMR, their routes are more easily estimated, and early warnings can be provided for precaution against the corresponding wind and rain. By contrast, after typhoons pass through the CMR, the routes, arrival times of wind and rain, and delays in rainfall become unpredictable [14,15]. Therefore, efficiently estimating typhoon rainfall is crucial for Taiwan.

A radar is commonly used for both weather surveillance and research to help meteorologists understand the dynamics and microphysical processes of atmospheric phenomena [16]. Radar reflectivity is a measure of the fraction of electromagnetic waves reflected by precipitation particles (e.g., rain, snow, or hail). Different colors are used to create radar images according to the intensity of the signal reflected by precipitation particles [3]. The intensity of reflection is associated with the size, shape, state of matter, and number of particles within a unit of precipitation. Stronger reflected signals generally indicate heavier precipitation. Therefore, radar images can be used to examine the intensity of precipitation and distribution of weather systems [17]. Currently, the Central Weather Bureau (CWB) of Taiwan has four S-band (10-cm wavelength) weather surveillance radar (WSR) systems; this new type of radar is also referred as WSR-88D (Weather Surveillance Radar—1988 Doppler). Of the four WSR systems, three are separately located in Hualien in Eastern Taiwan, Kenting in southern Taiwan, and Cigu in Western Taiwan (locations displayed in Figure 1); these three systems use a Doppler radar. The remaining system is located in Wufenshan in northern Taiwan and uses a dual-polarized radar. The scan range of the four systems covers Taiwan and its adjacent bodies of water (i.e., the Pacific Ocean, East China Sea, Taiwan Strait, and Luzon Strait) and forms a WSR network.



Figure 1. Geography of Taiwan and the locations of study sites and radar stations.

Numerous operational nowcasting systems use the relationship between static radar reflectivity (*Z*) and the rain rate (*R*), such as the commonly used Marshall–Palmer [18] formula of $Z = 200 R^{1.6}$, to convert radar echo into rainfall estimates. Radar- and gauge-based rainfall estimates are typically consistent, particularly when the rainfall intensity is high [19–25]. Researchers have studied the QPE of tropical cyclones. For example, Ku and Yoo [26] analyzed the rainfall engendered by typhoon Nakri by using radar and rain gauge data. Libertino et al. [27] developed a quasi-real-time procedure to optimize the radar estimation of rainfall rates. Moreover, Tang and Matyas [28] developed a nowcasting model for tropical cyclone precipitation based on rain retrieval for a Doppler radar. Chen et al. [29] reported the vertical structures of the raindrop size distribution and QPE parameters of two main synoptic systems: typhoons and Meiyu (or Baiu) fronts. According to these researchers, radar reflectivity factors constitute a vital variable that can be used as a QPE model input.

This study developed a model for estimating hourly rainfall during typhoons and analyzed the accuracy of typhoon rainfall estimation. As previously discussed, to address the problem of QPE, reflectivity measurements were employed. Radar imagery released by the CWB was used to estimate instantaneous rainfall, and a neural network-based model was employed to develop a precipitation estimation model. Specifically, multilayer perceptron (MLP) neural networks and convolutional neural networks (CNNs) were used to develop a typhoon precipitation estimation model.

Numerous studies have discussed typhoon rainfall estimation using machine learning models. Such models are typically composed of an MLP network, a radial basis function network, a support vector machine, and random forests and Bayesian networks [30–35]. Studies have combined such machine learning models with radar reflectivity and satellite remotely sensed data [36,37]. For example, Wei [38] developed a fuzzy inference-based neural network and estimated overland precipitation by using ground climatological data and radar reflectivity. Tao et al. [39] extracted useful features from bispectral satellite information, infrared images, and water vapor channels to detect rain by using deep neural networks.

Furthermore, studies have employed new deep learning models such as CNNs. CNNs are revolutionary in image analysis and are considered state-of-the-art for numerous tasks, including image classification, face recognition, and object detection [40-44]. CNNs are typically used in classification tasks in which the output of an image is a single-class label [45]. A standard CNN consists of alternating convolutional and pooling layers with fully connected layers above them [46]. A pretrained CNN such as VGG-16 [47] and its intermediate convolutional layer are used as an initial feature-map extractor. The convolutional layer is the core component of a CNN and outputs feature maps by computing the dot product between the local region in the input feature maps and a filter [48]. The pooling layer performs downsampling on feature maps by computing the maximum or average value of a subregion. Such newly developed models can be used to process radar images in atmospheric studies (e.g., rainfall inversion or typhoon intensity prediction). For example, Chen et al. [49] proposed a satellite imagery-based CNN for estimating the tropical cyclone intensity. Tran and Song [50] predicted multichannel radar image sequences by using deep neural network-based image processing techniques. Lee et al. [51] adopted CNNs using image patterns to estimate the tropical cyclone intensity by mimicking human cloud pattern recognition. Few studies have applied CNNs and remote sensing images to tropical cyclone rainfall estimation. Accordingly, the present study proposes a relevant methodology to fill this research gap.

This study proposes two structures for radar mosaic-based neural networks, namely a radar mosaic-based convolutional neural network (RMCNN) and a radar mosaic-based multilayer perceptron (RMMLP), to estimate typhoon rainfall. The neural network-based models were compared with empirical formulas by using the formula $Z = 200 R^{1.6}$ proposed by [18], which is referred to as the Marshall–Palmer model (Z-R_MP). In addition, the formula $Z = a R^b$ was reformulated at each station for the investigated events (Z-R_station). Regarding rainfall rate estimations of the studied stations, the smallest relative root mean squared error was computed by the proposed RMCNN (0.713), followed by RMMLP (0.848), Z-R_MP (1.030), and Z-R_station (1.392).

2. Materials

The geography of the research area is illustrated in Figure 1. Typhoons generally move from east to west through Taiwan. Accordingly, this study used three experimental stations, namely Hualien station in the east (121.6051°E, 23.9729°N), Sun Moon Lake station in central Taiwan (120.9081°E, 23.8813°N), and Taichung station in the west (120.6841°E, 24.1457°N), to analyze the accuracy of rainfall forecasts in typhoon precipitation.

This study considered 17 typhoons that affected the area between 2013 and 2017 (Figure 2). As the typhoons landed on Taiwan, the CWB released radar images every hour and collected observatory data. The resolution and color appearance of earlier radar images (released by CWB before 2012) differs from those of recent images (released by CWB after 2013). Therefore, we collected radar images starting from 2013. According to the CWB, the maximum wind speeds of mild, moderate, and severe typhoons are 17.2–32.6, 32.7–50.9, and >51 m/s, respectively. The statistics in Table 1 demonstrate that from 2013 to 2017, five severe (29.4%), seven moderate (41.2%), and five mild typhoons passed through the research area.

The radar reflectivity images collected in this study were radar mosaics produced by the CWB. The CWB typically creates a mosaic by using the reflectivity fields of the four WSR systems. Reflectivity is measured in decibels relative to *Z* (dB*Z*), and higher dB*Z* values suggest stronger echo signals. Radar mosaics are created as follows: The WSR systems scan for a period of approximately 7 min. Approximately 2.5 min later, the data collected by the four WSR systems are delivered to the host computer for data processing, and a composite mosaic is produced. After another 1–5 min, the mosaic and relevant data are sent to each servo host. Accordingly, a radar mosaic can be created approximately 15 min after the WSRs begin scanning.



Figure 2. Historical typhoon paths.

The radar mosaics collected during typhoons in the present study were composed of hourly radar images. The radar images of the typhoons that made landfall or approached Taiwan are depicted in Figure 3. Most of the radar mosaics were complete because they comprised radar images delivered from several radar systems. Few mosaics included partial sea areas that were not covered by the radar systems. This study filled in the missing areas in the images by using the most recent images captured before the time corresponding to missing data.



Figure 3. Reflectivity images of analyzed typhoons.

Trackson		Testan eiter	Total rain (mm)			
Typhoon	Period (UTC)	Intensity	Hualien	Sun Moon Lake	Taichung	
Cimaron	17–18 July 2013	Mild typhoon	29	1	13	
Usagi	21-22 September 2013	Severe typhoon	303	25	5	
Fitow	5–6 October 2013	Moderate typhoon	59	5	2	
Hagibis	15–16 June 2014	Mild typhoon	10	16	5	
Matmo	22–23 July 2014	Moderate typhoon	334	240	95	
Fung-Wong	19-22 September 2014	Mild typhoon	169	64	31	
Linfa	7–9 July 2015	Mild typhoon	9	2	12	
Soudelor	7–8 August 2015	Moderate typhoon	219	133	66	
Goni	22–23 August 2015	Severe typhoon	269	5	12	
Dujuan	28–29 September 2015	Severe typhoon	168	129	87	
Nepartak	7–9 July 2016	Severe typhoon	309	23	12	
Meranti	13–14 September 2016	Severe typhoon	323	52	19	
Megi	27–28 September 2016	Moderate typhoon	399	98	76	
Nesat	28–29 July 2017	Moderate typhoon	55	209	42	
Haitang	30–31 July 2017	Mild typhoon	90	79	153	
Hato	22–23 August 2017	Moderate typhoon	115	6	8	
Talim	13–13 September 2017	Moderate typhoon	33	0	0	

Table 1. Typhoons affecting the research area, 2013–2017 (17 incidents).

3. Methodology

This study designed a set of methods for estimating rainfall during typhoons by using the received instantaneous radar images. The procedures can be explained as follows:

Step 1: Collect relevant data from the research area and select typhoons for analysis. Typhoon weather information was scanned to confirm whether the typhoons affected the research area, and the event data of all historical typhoons were then examined;

Step 2: Refine the data collected from radar reflectivity images and gauge rainfall during the typhoons. After the relevant typhoon data were collected, data preprocessing was conducted. The preprocessed data were divided into radar images and observatory rainfall data. The observatory rainfall data obtained in this study were raw data. Parts of the observatory data were incomplete because of instrument malfunction or human error. Before data analysis, the missing values were supplied using interpolation. The method of radar image processing is explained in Section 2;

Step 3: Preprocess the data sets and categorize typhoon event data into training–validation and testing subsets. Of the analyzed typhoons, four approached the island from the east, made landfall on the east coast, passed through the CMR, and left the island from the west coast. The typhoon routes were near the three experimental stations in Hualien, Sun Moon Lake, and Taichung, and passed through the center of the island. This type of typhoon route results in the most severe damage. The four typhoons, namely Matmo in 2014 (Figure 2e), Soudelor in 2015 (Figure 2h), Dujuan in 2015 (Figure 2j), and Megi in 2016 (Figure 2m), constituted the testing set. The remaining 13 typhoons constituted the training–validation set. The training–validation. In total, 4701 hourly data were obtained. Of these, 4146 were used for the training–validation set and 555 were used for testing;

Step 4: Crop the reflectivity images. The latitudinal and longitudinal range of the original radar images was 117.32°–124.79°E, 21.70°–27.17°N. Because the original images had a wide geographical range, cropping was required to obtain the most suitable image size that included the rainfall data collected by ground-based observatories;

Step 5: Conduct neural network-based estimation and identify optimal reflectivity image sizes and model parameters. This study developed an RMCNN model in accordance with the different image sizes after cropping and initially applied default mode parameter values to identify the most suitable image size. After selection, relevant parameters for the RMCNN and RMMLP models were analyzed. The number of neurons and learning rate were calibrated in the RMCNN and RMMLP models. The model inputs were the reflectivity images cropped in Step 4, and the outputs were the rainfall rates at the stations. The RMCNN and RMMLP models were implemented using the open-source scikit-learn and Keras libraries in Python 3.7 (Python Software Foundation, Wilmington, DE, USA) [52,53];

Step 6: Evaluate the accuracy of the neural network-based models using the testing subset. Each selected typhoon was analyzed using the models to estimate typhoon rainfall and compare model errors and efficiency. This study used the root mean squared error (RMSE), mean absolute error (MAE), relative RMSE (rRMSE), relative MAE (rMAE), and efficiency coefficient (CE) as evaluation measures. Their equations can be defined as follows:

RMSE =
$$\sqrt{\frac{1}{n} \sum_{i=1}^{n} (R_i^{est} - R_i^{obs})^2}$$
, (1)

$$MAE = \frac{1}{n} \sum_{i=1}^{n} |R_i^{est} - R_i^{obs}|,$$
(2)

$$rRMSE = \frac{RMSE}{\overline{R}^{obs}},$$
(3)

$$rMAE = \frac{MAE}{\overline{R}^{obs}},$$
(4)

$$CE = 1 - \frac{\sum_{i=1}^{n} (R_i^{obs} - R_i^{est})^2}{\sum_{i=1}^{n} (R_i^{obs} - \overline{R}^{obs})^2},$$
(5)

where *n* represents the number of data; R_i^{est} and R_i^{obs} represent the *i*th estimated and observed values, respectively; and \overline{R}^{obs} represents the average observed value;

Step 7: Compare the optimal neural network-based models with empirical formulas by using the Z-R_MP and Z-R_station formulas. We computed the Z-R relationship at Hualien station (Z-R_Hualien) as $Z = 288 R^{1.195}$, that at Sun Moon Lake station as $Z = 378 R^{1.0957}$, and that at Taichung station (Z-R_Taichung) as $Z = 352 R^{0.8376}$.

Network Architecture

The developed RMMLP and RMCNN models were based on two types of neural networks, namely an MLP and a CNN. The framework of the proposed RMMLP (Figure 4) is a conventional type of ANN that includes input, hidden, and output layers. The additional fully connected layer directly receives the cropped images to be flattened (conversion from a two-dimensional to a one-dimensional array). Therefore, the RMMLP model can be used when images serve as the network model inputs.



Figure 4. Architecture of the proposed radar mosaic-based multilayer perceptron (RMMLP).

RMMLP model training involves learning and recall phases. In the learning phase, data training is conducted using known input and output values to obtain a set of connection weights in the hidden layer. The weights are used to calculate objective output results. In the recall phase, another input value (i.e., validation and test sets) is entered, and the estimated value is output using the weights obtained in the learning phase.

Unlike the RMMLP model, the RMCNN model has two additional layers: convolutional and pooling layers (Figure 5). The two additional layers enable the RMCNN to efficiently convert the collected information into applicable data for extracting features. Subsequently, the features are combined by the fully connected layer, and model training is conducted.



Figure 5. Architecture of radar mosaic-based convolutional neural network (RMCNN).

The convolutional layer of the RMCNN model contains several convolution kernels. Different weight combinations assigned to the convolution kernels can be used to sharpen images, detect edges, and extract features for recognition purposes. The neurons in the convolutional layer are feature detectors. The input end first corresponds to a convolution kernel and defines its size. In brief, the convolutional layer extracts features in an image. The convolution equation is expressed as follows:

$$\int_{-\infty}^{\infty} f(\tau)g(x-\tau)d\tau,$$
(6)

where f(x) is the original pixels; the original image is created after all pixels are superimposed. In addition, g(x) denotes the point of application.

Through the convolution equation, the modeling system can output a result superimposed by multiple inputs at a specific moment. In image analysis, a convolution kernel is the combination of all application points. The application points on the convolution kernel affect the original pixel sequentially; accordingly, the output of the linear superposition is the final output of the convolution kernel. The equation is as follows:

$$O(i,j) = (I * K)(i,j) = \sum_{m=0}^{1} \sum_{n=0}^{1} I(i+m,j+n)K(m,n),$$
(7)

where *O*, *I*, and *K* are outputs, inputs, and convolution kernels, respectively, and *m* and *n* are defined by the convolution kernel function.

In an RMCNN, the fully connected layer performs a regression on the extracted features flattened in the convolution and pooling layers. Data are processed using a dropout function that enables the models to shut down some of the neurons to prevent overfitting during training.

4. Modeling

This study employed the training–validation set to train model parameters and verify model applicability. Two types of neural network models (i.e., RMCNN and RMMLP models) were established to examine the most suitable size and hyperparameters (e.g., number of neurons and learning rate) concerning radar images. A trial-and-error approach was used for verification, and the RMCNN

architecture used in this study is displayed in Figure 5. The settings of each RMCNN model parameter are outlined as follows: filter weighting size = 3×3 ; padding method = same; max pooling size = 2×2 . The activation function of the convolutional layer was a rectified linear unit (ReLU) function, the activation function of the hidden layer was a sigmoid function, and the dropout rate was 0.2.

4.1. Image Resizing and Selection

The resolution of the original radar images was 1024×1024 pixels. This study first located and centered the experimental stations in the images and then cropped the sheet by sizes of 4×4 , 6×6 , ..., and 30×30 pixels. One pixel typically corresponds to an actual distance of 0.703 km. The cropped images and observatory rainfall data were then used as inputs into the RMCNN model for rainfall estimation. In this phase, the number of neurons and the learning rate in the hidden layer were set to 10 and 0.0001, respectively.

Tables 2–4 present the RMSE results for different image sizes for the Hualien, Sun Moon Lake, and Taichung stations, respectively. The lowest RMSE values for the estimations at both experimental stations (3.449, 3.061, and 2.478 mm/h) were observed when the image size of 12×12 pixels was used for Hualien and Taichung and the image size of 14×14 pixels was used for Sun Moon Lake. Therefore, these were selected as the most suitable image sizes. Here, 12 pixels correspond to an actual distance of 8.44 km.

Table 2. Results for various image sizes (pixel × pixel) at Hualien station.

Image size	4×4	6 × 6	8 × 8	10 × 10	12 × 12	14×14	16 × 16
RMSE (mm/h)	3.776	3.773	3.659	4.285	3.449	4.263	4.813
Image size	18 × 18	20×20	22 × 22	24 × 24	26 × 26	28×28	30 × 30
RMSE (mm/h)	3.886	3.639	4.344	4.014	3.854	4.461	4.114

Table 3. Results for various image sizes (pixel × pixel) at Sun Moon Lake station.

Image size	4 × 4	6 × 6	8 × 8	10 × 10	12 × 12	14×14	16 × 16
RMSE (mm/h)	3.473	3.787	3.273	3.447	3.343	3.061	3.330
Image size	18 × 18	20×20	22 × 22	24 × 24	26 × 26	28 × 28	30 × 30
RMSE (mm/h)	3.182	3.280	3.172	3.158	3.446	3.706	4.002

Table 4. Results for various image sizes (pixel × pixel) at Taichung station.

Image size	4×4	6 × 6	8 × 8	10 × 10	12 × 12	14×14	16 × 16
RMSE (mm/h)	2.797	2.997	3.061	2.662	2.478	2.640	2.534
Image size	18 × 18	20×20	22 × 22	24×24	26 × 26	28×28	30 × 30
RMSE (mm/h)	2.623	3.119	3.091	3.127	2.936	3.017	3.099

4.2. Parameter Calibration

After the most suitable image size was selected, the RMCNN model hyperparameters were examined. First, the number of neurons in the hidden layer was calibrated. The number of neurons was set between 5 and 35. Figure 6a,c,e present the RMSE values of the RMCNN and RMMLP models when applied at the Hualien, Sun Moon Lake, and Taichung stations, respectively. The lowest RMSE values (2.764 and 3.624 mm/h) were obtained when the RMCNN and RMMLP models applied at the Hualien station had 18 and 20 neurons, respectively; the lowest RMSE values (2.141 and 2.695 mm/h) for the estimations at the Sun Moon Lake station were obtained when the RMCNN and RMMLP models had 13 and 16 neurons, respectively; and the lowest RMSE values (1.542 and 1.756 mm/h) for

the estimations at the Taichung station were obtained when the RMCNN and RMMLP models had 20 and 22 neurons, respectively.



Figure 6. Parameter calibration of the number of neuron nodes and learning rate at Hualien (**a**,**b**), Sun Moon Lake (**c**,**d**), and Taichung (**e**,**f**).

This study used adaptive moment estimation (Adam) proposed by [54] to analyze the learning rate. The Adam algorithm was selected because it has an adaptive learning rate and can adjust the learning rate and update neural network weights on the basis of first- and second-order moment estimation, which increases the calculation efficiency. To apply the Adam algorithm, this study set the initial learning rate to between 0.0001 and 0.002. Figure 6b,d,f illustrate the RMSE values of the RMCNN and RMMLP models applied at the three stations. For the estimations at the Hualien station, the RMCNN and RMMLP models had minimum RMSE values (2.690 and 3.222 mm/h) when the learning rate was 0.0008 and 0.0009, respectively. For Sun Moon Lake station, the RMCNN and RMMLP models had minimum RMSE values (2.031 and 2.606 mm/h) when the learning rate was 0.0008, respectively. For Taichung station, the RMCNN and RMMLP models had minimum RMSE values (1.437 and 1.563 mm/h) when the learning rate was 0.0006 and 0.0007, respectively.

5. Results and Discussion

To examine the applicability of the three models and estimation errors for typhoons passing through the CMR from east to west, this study selected data on four typhoons for evaluation and compared the analysis results of the RMCNN, RMMLP, Z-R_MP, and Z-R_station models.

Four typhoons (Matmo, Soudelor, Dujuan, and Megi) were employed to identify the most suitable rainfall estimation model. Figure 7 presents hyetographs of observed rainfall and RMCNN, RMMLP, Z-R_MP, and Z-R_station model estimations at the Hualien, Sun Moon Lake, and Taichung stations.



Figure 7. Rainfall hyetographs and model estimations for (**a**) Hualien, (**b**) Sun Moon Lake, and (**c**) Taichung stations.

The rain duration of typhoon Matmo was 43 h (time series: t = 1-43 h; Figure 7). The Hualien, Sun Moon Lake, and Taichung stations had the maximum observed rainfall at t = 20 h (41 mm/h), t = 24 h (26 mm/h), and t = 24 h (20 mm/h), respectively. After the typhoon circulation structure was disturbed by the CMR, the observed rainfalls at the Taichung and Sun Moon Lake stations were less than that at the Hualien station. The results for the remaining three typhoons were similar. Typhoon Soudelor had a rain duration of 50 h (t = 44-93 h) and the Hualien station recorded the maximum rainfall at t = 66 h (54 mm/h), whereas the Sun Moon Lake station recorded the maximum rainfall with a 3-h delay (t = 69 h; 19 mm/h) and Taichung station recorded the maximum rainfall with a 7-h delay (t = 73 h; 9 mm/h). The rain duration of typhoon Dujuan was 28 h (t = 94-121). The maximum rainfall at the Hualien station was reached at t = 109 h (35 mm/h); that at the Sun Moon Lake station was reached at t = 114 h (34 mm/h), with a 5-h delay; and at the Taichung station, it was reached at t = 114 h (15 mm/h), with a 5-h delay. Typhoon Megi had a rain duration of 63 h (t = 122-184 h). The maximum rainfall at the Hualien, Sun Moon Lake, and Taichung stations was reached at t = 140 h (61 mm/h), t = 143 h (8 mm/h), and t = 151 h (8 mm/h; 11-h delay), respectively.

Regarding the estimated rain pattern, the estimations of all models at the Hualien station (Figure 7a) were mostly identical to the observed pattern. Concerning the peak rainfall on the hyetographs, all models reflected an increase in rainfall. However, these models had larger differences in estimated

types of rain, peak rainfall on the hyetograph, and the arrival time of peak rainfall for data recorded at the Sun Moon Lake and Taichung stations. This may be because the rapidly changing typhoon circulation structure and the radar images detected and received at the Sun Moon Lake and Taichung stations increase forecast uncertainty. By contrast, before a typhoon reaches the island, its structure and circulation observed at the Hualien station tend to be more stable, which facilitates the estimation of intense rainfall. This study compared these models according to their performance for several evaluation measures.

5.2. Evaluations

Figure 8 shows scatter plots comparing the observations obtained with the four model estimations. For both stations, the correlation coefficient (r) indicated that the RMCNN model was more accurate than the RMMLP, Z-R_MP, and Z-R_station models. The RMCNN model estimations at the Hualien station (r = 0.946) and Sun Moon Lake station (r = 0.961) were more satisfactory and consistent with the observed data than those at the Taichung station (r = 0.878).



Figure 8. Scatterplots of observations versus estimations using RMCNN, RMMLP, Marshall–Palmer Z-R relationship (Z-R_MP), and reformulated Z-R relationship at each site (Z-R_station) models for Hualien (**a**–**d**), Sun Moon Lake (**e**–**h**), and Taichung (**i**–**l**).

Regarding absolute errors, this study assessed the MAE and RMSE for the four examined typhoons. For the RMCNN model, the MAE and RMSE values for the four typhoons observed at the Hualien station were higher than those observed at the Sun Moon Lake and Taichung stations (Figure 9a,e). Similar results were observed for the RMMLP (Figure 9b,f), Z-R_MP (Figure 9c,g), and Z-R_station (Figure 9d,h) models. According to these results, the estimations at the Hualien station had a larger error because of the rainfall at this station.



Figure 9. Absolute errors for RMCNN, RMMLP, Z-R_MP, and Z-R_station: (a-d) MAE and (e-h) RMSE.

This study also used rMAE and rRMSE to evaluate the estimations for the four typhoons. For the RMCNN model, the rMAE and rRMSE values observed for the Taichung station were higher than those observed for the Hualien and Sun Moon Lake stations for typhoons Matmo, Soudelor, and Dujuan (Figure 10a,e). For the RMMLP and Z-R_MP models, the rMAE and rRMSE values observed for the Taichung station were also higher than those observed for the Hualien and Sun Moon Lake stations for typhoons Matmo and Soudelor (Figure 10b,c,f,g).



Figure 10. Relative errors for RMCNN, RMMLP, Z-R_MP, and Z-R_station: (**a**–**d**) rMAE and (**e**–**h**) rRMSE.

Table 5 presents the overall performance levels obtained for the models for the four examined typhoons at Hualien, Sun Moon Lake, and Taichung stations. The RMCNN model exhibited a superior performance for each measure compared with the RMMLP, Z-R_MP, and Z-R_station models. Moreover, the absolute errors observed for the estimations at the Hualien station were greater than those observed for the estimations at the Sun Moon Lake and Taichung stations, but the relative errors observed for the estimations at the Hualien station were lower than those observed for the estimations at the Hualien stations. Finally, the RMCNN model had the highest CE (0.867) for the estimations at the Hualien station, whereas the Z-R_station model had the lowest CE among all models at the three stations.

Station	Model	RMCNN	RMMLP	Z-R_MP	Z-R_station
	MAE (mm/h)	1.870	2.218	2.670	4.206
	RMSE (mm/h)	3.502	4.351	4.955	7.569
Hualian	rMAE	0.309	0.366	0.441	0.695
nualien	rRMSE	0.579	0.719	0.818	1.250
	r	0.946	0.930	0.868	0.854
	CE	0.867	0.794	0.733	0.378
	MAE (mm/h)	1.070	1.340	1.522	2.268
	RMSE (mm/h)	2.124	2.672	3.155	4.458
Sup Moon Lake	rMAE	0.314	0.393	0.446	0.665
Sun Moon Lake	rRMSE	0.623	0.783	0.925	1.307
	r	0.961	0.939	0.835	0.852
	CE	0.860	0.778	0.691	0.383
	MAE (mm/h)	0.771	0.905	1.141	1.474
	RMSE (mm/h)	1.641	1.828	2.361	2.836
Taichung	rMAE	0.440	0.517	0.651	0.842
Talcitung	rRMSE	0.937	1.043	1.348	1.619
	r	0.878	0.843	0.655	0.741
	CE	0.727	0.661	0.416	0.185

Table 5. Overall model performance levels for four typhoons.

5.3. Estimation Performance for Peak Rainfall

This study examined the estimation performance of the four models for peak rainfall. The relative error of peak rainfall and the absolute time error of peak rainfall were derived as measures for comparison. First, the relative error of peak rainfall (RE_{Peak}), defined as the average ratio of absolute errors, can be expressed as follows:

$$RE_{peak} = \frac{\sum_{k=1}^{m} |O_{k}^{p_{pre}} - O_{k}^{p_{obs}}|}{\sum_{k=1}^{m} O_{k}^{p_{obs}}},$$
(8)

where $O_k^{p_{pre}}$ is the estimated peak value in typhoon event *k*, $O_k^{p_{obs}}$ is the observed peak value in typhoon event *k*, and *m* is the total number of typhoon events.

Second, the absolute time error of peak rainfall (AT_{Peak}) , defined as the average of absolute time errors, can be expressed as follows:

$$AT_{peak} = \frac{1}{m} \sum_{k=1}^{m} |T_k^{p_{pre}} - T_k^{p_{obs}}|,$$
(9)

where $T_k^{p_{pre}}$ is the arrival time of estimated peak rainfall in typhoon event *k* and $T_k^{p_{obs}}$ is the arrival time of observed peak rainfall in typhoon event *k*.

Lower RE_{Peak} and AT_{Peak} values indicate higher performances. Figure 11 displays the RE_{Peak} and A_{TPeak} values for the four typhoons. As illustrated by Figure 11a, the following results were observed: (1) For the estimations at the Hualien and Sun Moon Lake stations, the RE_{Peak} value for the RMCNN model was superior to those for the RMMLP, Z-R_MP, and Z-R_station models, but for the estimations at the Taichung station, the RE_{Peak} value for the Z-R_MP model was superior to those for the RMCNN, RMMLP, and Z-R_station models; (2) with relative error of the estimated peak rainfall on RMCNN, Hualien station computed the smallest RE_{Peak} (0.262), followed by Sun Moon Lake station (0.303), and then Taichung station (0.385). The peak rainfall estimated at the Hualien station was less than that at the Sun Moon Lake and Taichung stations because the typhoon routes were disturbed by the CMR. Hence, peak rainfall was difficult to estimate at the Sun Moon Lake and Taichung stations.



Figure 11. Performance levels for RMCNN, RMMLP, Z-R_MP, and Z-R_station in terms of (**a**) the relative error of peak rainfall (RE_{peak}) and (**b**) the absolute time error of peak rainfall (AT_{peak}).

Additionally, as shown in Figure 11b, the following results were observed: (1) The AT_{Peak} values observed for the RMCNN and RMMLP models for the estimations at Hualien station were 0, indicating that the models accurately estimated the wind and rain arrival times. Although all models could not accurately estimate the rain arrival times for the estimations at the Sun Moon Lake and Taichung stations, the AT_{Peak} value obtained for the RMCNN model was smaller than those obtained for the RMMLP, Z-R_MP, and Z-R_station models; (2) the AT_{Peak} values obtained for all models for the estimations at Hualien station were smaller than those obtained for the estimations at the Sun Moon Lake and Taichung stations because the typhoon eye and structure were more stable before reaching landforms. Therefore, the peak rainfall arrival time was more easily estimated in Hualien.

6. Conclusions

This study examined the efficiency of typhoon precipitation estimation and evaluated the influence of the CMR on rainfall during typhoons. In general, when a typhoon approaches Taiwan from east to west, its route or the wind and rain it carries are more easily predicted before it passes through the CMR. By contrast, after the typhoon passes the CMR, its route and delay in rainfall become unpredictable.

This study considered 17 typhoons that affected the research area from 2013 to 2017 and collected hourly radar images released by the CWB during the typhoons, as well as observatory data. Hualien station in the east, Sun Moon Lake station in Central Taiwan, and Taichung station in the west were selected as the three experimental sites, and RMCNN, RMMLP, Z-R_MP, and Z-R_station models were employed. The RMCNN model was incorporated with the radar images to estimate typhoon rainfall. Using the overall rainfall rates of all stations, RMCNN computed the smallest relative root mean squared error (0.713), followed by RMMLP (0.848), Z-R_MP (1.030), and Z-R_station (1.392). Moreover, the smallest relative error of peak rainfall was yielded by RMCNN (0.316), followed by RMMLP (0.379), Z-R_MP (0.402), and Z-R_station (0.688). The smallest relative error of peak rainfall arrival time was computed by RMCNN (1.507 h), followed by RMMLP (2.673 h), Z-R_MP (2.917 h), and Z-R_station (3.250 h). On the basis of relevant evaluation measures, the RMCNN model outperformed the RMMLP, Z-R_MP, and Z-R_station models.

The estimations of the four models at Hualien station were mostly identical to the observed rainfall data. Although all models estimated an increase in rainfall at the peak rainfall time on the hyetographs, the peak value was underestimated. The estimations of the four models concerning the hyetograph and peak rainfall arrival time at the Sun Moon Lake and Taichung stations were considerably inconsistent with the observed data. This may be because the rapidly changing typhoon circulation structure and the radar images increase the uncertainty of rainfall forecasting. By contrast, peak rainfall and the peak rainfall arrival time were easier to detect at Hualien station because the typhoon structure and circulation are more stable before the typhoon reaches the island. In conclusion, this study employed

the RMCNN model integrated with radar imagers to estimate typhoon rainfall, and the results reveal that the model incorporating radar images can effectively estimate precipitation during typhoons.

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