



Article

# Development and Urban Sustainability: An Analysis of Efficiency Using Data Envelopment Analysis

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Abstract: In recent decades, the majority of cities in developing countries have grown rapidly and have experienced increasing environmental problems. These changes have generated a broad discussion on urban sustainability and development. In this discussion, it is fundamental to establish methods for measuring urban sustainability using a quantitative approach. This research seeks to estimate and evaluate the environmental, social, and economic efficiency of cities in a developing country, Colombia, using data envelopment analysis to determine the changes that occurred between 2005 and 2013. In this study, indicators related to economic, environmental, and social performance are used with the objective of analyzing efficiency from urban sustainability. The results indicate differences among cities, where the efficient cities show adequate resource use, lower environmental impacts, improved social conditions, and guaranteed economic growth and development. Moreover, as the city scale increases, urban sustainability declines. All these findings are important in the formulation and design of adequate urban policies to improve and strengthen sustainability and social welfare over the long term, particularly in cities in developing countries.

Keywords: urban sustainability; data envelopment analysis; Colombian cities

#### 1. Introduction

Urban growth tends to occur in the major urban regions of developed and developing countries. In the latter, countries are consolidated as massive agglomerations of more than 20 million people, particularly in Asia, Latin America, and Africa [1]. The global urban population has grown precipitously from 746 million in 1950 to 3.9 billion in 2014, a figure that is projected to increase to 2.5 billion people by 2050. Approximately 50% of the world's urban dwellers live in smaller settlements of less than 500,000 inhabitants, whereas approximately 80% reside in one of 28 megacities containing over 10 million people [2].

Cities are recognized as important generators of development, growth, innovation, and poverty reduction mainly because of the concentration of national economic activity, commerce, public service provision, and transportation. Key links between cities and rural areas also improve the infrastructure of countries [1–3]. Moreover, cities are related to higher levels of learning and education, better health, easier access to social services, and enhanced opportunities for cultural and political participation. However, cities have negative aspects, such as vehicular congestion, higher levels of pollution, and higher demand for resources, that drive unsustainable production and consumption patterns [4–6]. These patterns suggest an unsustainable model of cities, which implies the need to rethink the means of urban planning and growth to improve overall performance and urban efficiency to produce more

competitive, equitable, and sustainable urban areas. Figure 1 shows the urbanization cycle and its environmental impacts [7].

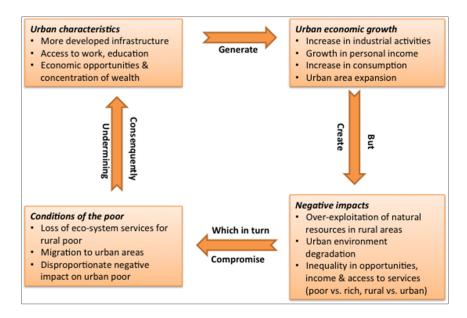


Figure 1. The urbanization cycle and environmental impacts.

The concept of urban efficiency derives from different theories and concepts developed in the 20th century, such as the notion of sustainable cities. A sustainable city is defined by the combination of economic development, social development, and environmental protection that includes all human rights and fundamental freedoms, including the right to development and the right to work, so that all its citizens are able to meet their needs without compromising the wellbeing of the natural world or the living conditions of other people, currently or in the future [8,9]. Green architecture seeks to reduce the negative environmental impact of buildings, urban designs and settlements through efficiency and moderation in the use of materials, energy, and development space; this concept includes systemic reforms in architectural and urban design, land use planning, transportation, agriculture, and energy production [10]. A compact city's objective is a high-density, mixed-use, and intensified urban form that emphasizes that activities should be located closer together to ensure better access to services and facilities via public transport, walking and cycling and that utility and infrastructure provision should be more efficient [11]. In addition, an eco-city is a human settlement modelled on the self-sustaining, resilient structure and function of natural ecosystems that minimizes waste and pollution, maximizes energy efficiency in buildings and transportation, utilizes renewable energy and resources as much as possible, provides high-quality public spaces for citizens, and conserves valued features of the local ecology and landscape [12,13]. These concepts and theories demonstrate the importance of measuring urban efficiency to ensure progress and improve sustainability.

In cities, efficiency has been studied for in following areas. (i) Specific sectors: [14] studied various tools to stimulate and improve the urban efficiency of small and medium enterprises (SMEs) in Venezuela using qualitative methods, such as stakeholder analysis and policy Delphi, finding that the main barriers to efficiency in SMEs are a lack of buyers and end user sensitivity. In addition, these methods indicated that the best mix of public administration tools include command and control, responsible consumption, ecoefficient products, and environmental responsibility education/training. In European SMEs, the main barriers to efficiency are a lack of infrastructure and technology, and the main stimuli are legislation and customer requirements [15]; (ii) Urban metabolism: Sustainable operation suggests mutualism and symbiosis between socioeconomic development and ecological environment protection. Studies have shown that urban features such as form and compactness ratios

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are key to urban efficiency and resource efficiency, whereas high population density increases pollution costs and decreases environmental efficiency [16,17]; (iii) Data envelopment analysis (DEA): [18] examined the environmental protection mechanisms and economic development of 211 cities in China from an environmental efficiency perspective and found that local governments should develop appropriate policies to maximize the use of technology and develop management practices that enhance both growth and protection. In addition, [19] evaluated the urban environmental sustainability of Chinese cities, determining that environmental sustainability requires resource, environmental, and economic balance. These studies demonstrate the importance of analyzing efficiency in cities as a strategy for formulating adequate policies that promote sustainable development.

Moreover, methods of measuring efficiency can be divided into three types: (i) The single-ratio model of economic output/environmental impact. This model has been accepted and aggregates different environmental impacts into one score using life cycle analysis. The single-ratio model is easy to understand and communicate and is mainly used to analyze the efficiency of products and technologies [20,21]; (ii) Substitution of the numerator with other composite indicators, such as energy indicators [22], ecological footprint indicators [23], and material flow analysis indicators [24]. This method can be used to evaluate the environmental performance of the system; (iii) Models for assessing efficiency, such as the Range Adjusted Measure (RAM) model. These models explain desirable and undesirable outputs in the production process [25] and positive matrix factorization [26]. In recent years, various studies have used DEA to calculate efficiency using different models with multiple inputs and outputs [27–29].

Against this background, this research seeks to estimate and evaluate the urban efficiency of a developing country, Colombia, using DEA to determine the change over the 2005–2013 period and to evaluate the relationship between inputs and outputs across different models. The main contributions of this study are in identifying the main factors that increase urban sustainability in Colombian cities and in considering the different inputs and desirable and undesirable outputs from a quantitative perspective, which allows us to identify both sources and levels of inefficiency and to determine how cities can improve sustainability and development. Thus, this study provides more accurate measurements of sustainable efficiency in various Colombian cities and contributes to the literature on efficiency and development measurement, as the integration of efficiency and development performance is very new. This study also contributes to the limited empirical evidence on the relation between sustainable development and efficiency.

It is expected that the findings of this study will aid researchers and policymakers. For researchers, this study provides interesting insights into the current literature on the joint assessment of environmental and development elements to measure efficiency in urban contexts. This study also provides policymakers with useful information with which to design more effective environmental protection policies in cities such that development is balanced with sustainable performance.

This paper is organized into four sections. Section 2 explains the conceptual model. The results and discussion are delineated in Section 3. The final section discusses the conclusions and provides avenues for future work based on this research.

## 2. Methods

#### 2.1. Data Envelopment Analysis (DEA) Models and Application Considerations

This study uses DEA to determine urban efficiency. DEA is a mathematical linear programming method that applies the frontier approach to measure the performance of entities called decision-making units (DMUs). It develops a best practices frontier because a DMU converts or transforms multiple inputs and outputs. This technique measures the relative efficiency or performance of a DMU based on its proximity to the best practices frontier [30–32]. Moreover, DEA allows the assessment of relative efficiency in a group of DMUs that use resources (inputs) to generate products (outputs) by defining and quantifying inefficient DMUs based on several inputs and outputs.

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In DEA, efficiency comprises three components: technical efficiency (TE), the capacity of a DMU to achieve maximal output from a given set of inputs; allocative efficiency, the capacity of a DMU to use inputs in optimal quantities given their respective prices; and scale efficiency (SE), from the features of performance scale, produces the maximum output that could be provided by a DMU with particular operational features. These three measures are then combined to provide a measure of total economic efficiency [31,33].

In this study, DEA is applied due to its flexibility and ability to model and adapt to several situations, such as the measurement of urban efficiency. The model implies that a city generates a single output y from a vector of n inputs x = (x1, x2, ..., xn). Let yi indicate output and vector xi indicate the input package of the ith DMU. Assume that input-output data are observed for m DMUs. Then, the technology set can be defined by the production possibility set  $S = \{(x, y): y \text{ can be produced from } x\}$  based on a few regularity assumptions to ensure the feasibility of all observed input-output combinations, free disposability with respect to inputs and outputs and convexity. This research considers two DEA models: the Charnes-Cooper-Rhodes (CCR) input model (see Equation (1)) [30] and the Banker-Charnes-Cooper (BCC) input model (see Equation (2)) [32].

The calculated value of  $\theta c$  is the efficiency of DMU 0 in the CCR model.  $\theta c \leq 1$ , and  $\theta c$  reaches 1 only if both slack vectors are equivalent to zero and none of the input variables of DMU 0 are larger than any linear grouping of the other DMUs [34]. The input-oriented linear programming equations for the CCR and BCC models in the dual form are expressed as follows (see Equations (1) and (2), respectively).

CCR model:

$$\theta^* = \min \theta_C$$

subject to

$$\theta_{c}X_{ik} \geqslant \sum_{j=1}^{n} \lambda_{j}x_{ij}, \qquad i = 1, \dots, m$$

$$y_{rk} \leqslant \sum_{j=1}^{n} \lambda_{j}y_{rj}, \qquad r = 1, \dots, s$$

$$\lambda_{j} \geqslant 0, \quad \forall i, j, r$$

$$(1)$$

BCC model:

$$\theta^* = \min \theta_B$$

subject to

$$\theta_B X_{ik} \geqslant \sum_{j=1}^n \lambda_j x_{ij}, \qquad i = 1, \dots, m$$

$$y_{rk} \leqslant \sum_{j=1}^n \lambda_j y_{rj}, \qquad r = 1, \dots, s$$

$$\lambda_j \geqslant 0, \quad \forall i, j, r$$
(2)

where the subscript k indicates the DMU to be evaluated (in this study, the selected cities), subscripts j, I, and r represent the serial number of DMU in the set j = 1,..., n, the serial number of the input in the set i = 1,..., n, and the serial number of the output in the set i = 1,..., n, respectively.  $\theta_k$  is the efficiency measure for DMU "k";  $x_{ij}$  is the amount of input "i" for DMU "j";  $x_{ik}$  is the amount of input "i" for DMU "k";  $y_{rj}$  is the amount of output "r" for DMU "j";  $y_{rk}$  is the amount of output "r" for DMU "k"; and  $\lambda_j$  is the weight assigned to all inputs and outputs of DMU "j".

The difference between the CCR and BCC models is illustrated by Equations (1) and (2). The first model (CCR) considers constant returns to scale (CRS), whereas the second model (BCC) considers variable returns to scale (VRS). The result of the CCR model is an integrated efficiency value called TE, whereas the result of the BCC model is called pure technical efficiency (PTE). TE can never be larger than PTE, and SE is calculated as the TE/PTE ratio. In this study, the PTE of a particular city establishes the current level of environmental, economic, or social sustainability [34], while SE indicates the environmental, economic, or social sustainability trends as the city size increases.

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Finally, TE determines the possible level of environmental, economic, or social sustainability at current and future city scales [34].

To apply DEA, it is important to consider the following requirements: (i) the input and output variables selected must be positive, as in this study; (ii) the DMUs selected should be homogenous identities (in this case, cities) in which the same inputs produce the same outputs; and (iii) the degrees of freedom in the DEA increase with the number of DMUs and decrease with the number of inputs and outputs. Therefore, the number of cities should be several times larger than the sum of the number of input-side indicators and output-side indicators, where the minimum number of DMUs (cities) is either the product of the number of inputs and the number of outputs or three times the sum of the number of inputs and outputs.

In this study, each proposed model (see Figure 2) has two inputs and two outputs or three inputs and one output, implying that at least twelve DMUs are required to provide the needed degrees of freedom. The cities were divided into two groups to guarantee that the DMUs were comparable, applying the k-means clustering method proposed by [35]. The cities were grouped into large, high-production cities and those of medium size and production levels. Both groups include a minimum of five Colombian cities, that is, at least 12 DMUs. These are solved using a window analysis, using 20 large, high-production cities and 24 cities of medium size and production levels. The same city in a different period is considered another DMU, that is, each city is compared to both other cities and itself over time.

DEA window analysis is conducted with the objective of obtaining the efficiency scores of Colombian cities in accordance with [36,37], where the same city in different time periods (in this case, years) is considered a different DMU. Hence, the performance of a city is not only evaluated with that of other cities at the same time but also with itself at different times. This analysis uses four-year windows from 2005 to 2013 for 11 Colombian cities to achieve the degrees of freedom required for DEA. The cities are divided into larger, high-production cities and cities of medium size and mid-level production, and every window analysis includes 20 or 24 DMUs (see Table 1). Window analysis allows us to increase the number of DMUs and input and output variables and to evaluate the stability of each city's performance over time. Moreover, this technique should allow significant inferences regarding changes in the performance of the analyzed DMUs by studying their efficiency in a dynamic setting.

Number of Window		Period								
Window 1	2005	2006	2007	2008						
Window 2		2006	2007	2008	2009					
Window 3			2007	2008	2009	2010				
Window 4				2008	2009	2010	2011			
Window 5					2009	2010	2011	2012		
Window 6						2010	2011	2012	2013	

Table 1. Window Breakdown selected to analysis Colombian cities.

Note: Each window represents the selected period or width of the window, which in this study includes six four-year windows from 2005 to 2013.

#### 2.2. Sample

Eleven major cities were selected to ensure that the analyzed samples comprehensively and objectively reflected the characteristics of Colombian cities and that the data were available. The selected cities are departmental capitals that include key industrial, commercial, or cultural centres of Colombian regions.

The 11 selected cities are scattered across Colombian departments, and their gross domestic product (GDP) per capita (2013) ranged from US\$380 to US\$1300. Although most of these 11 cities have populations exceeding 300,000 inhabitants, these can still be divided into medium and large cities,

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with the exception of Bogotá, which is considered a megacity. The economic, social, and environmental data for these cities are complete, and they are listed in Table 2.

#### 2.3. Variables and Outline

In the sustainability approach, the city is a broad concept that integrates various subsystems: social development, economic development, environmental management, and urban governance. This approach incorporates the management and investment decisions of municipal authorities in coordination with national authorities and institutions [38]. To measure sustainability in cities, several indicators and sub-indicators of environmental quality, economic efficiency, and social equality have been formulated and presented in studies [39,40].

To apply the proposed DEA models, the city indicators were distributed into input and output groups with the objective of adequately distinguishing between efficient and inefficient Colombian cities. The 11 Colombian cities were analyzed using nine indicators in three different models (see Figure 2).

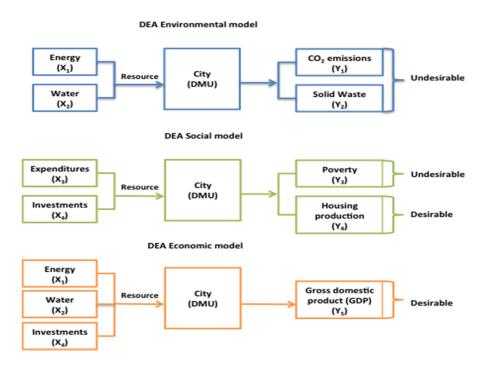


Figure 2. Input-output indicators for the proposed DEA models.

The inputs were annual secondary energy consumption (x1), which is measured as electricity and natural gas in terajoules; annual water consumption (x2), which is measured in cubic metres; and annual expenditures (x3) and investments (x4) by the local government, which are measured in monetary units in current prices. Desirable outputs include GDP (y5) measured in monetary units in current prices, which indicates the economic contribution of a city, and housing production (y4) measured as housing production or new homes built per 1,000 inhabitants per year. Undesirable outputs include carbon dioxide emissions (y1), which are measured in tonnes, and solid waste generation, which is also measured in tonnes (y2) and indicates environmental problems in cities. Poverty (y3) measures the percentage of persons living in poverty based on a per capita household income below the poverty line relative to the total population, as reported by the Colombian statistics office. To represent the treatment of undesirable outputs, reciprocals (y1 = 1/y1, y2 = 1/y2, and y3 = 1/y3) were used as output indicators in the DEA models [41,42]. Using the reciprocals of undesirable outputs allows less undesirable to be preferred in the efficiency analysis of a city, e.g., in model 1, cities with higher efficiency generate less CO<sub>2</sub> emissions and solid waste given their energy

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and water consumption. This could be because relatively lower amounts of energy and water were consumed, because efficiency increased for energy and water use or because of technological changes. Hence, relatively lower amounts of CO<sub>2</sub> emissions or waste were generated by a city over the sample period.

The data in this analysis were primarily drawn from the DANE (Colombian Department of Statistics), DNP (National Planning Department), Colombian Finance and Public Credit Ministry, and local government reports for the selected cities. Energy, water, and waste data are published by the SSPD (Public Utility Superintendence) through the SUI system (Single Information System for public services), and data on households are reported by the CENAC (Centre for Construction and Urban and Regional Development Research).

#### 3. Results and Discussion

In this section, we present the results of the DEA analysis for the selected cities in Colombia. The analysis framework is based on the above-mentioned models and formulas. First, the cities are divided into cities of larger size and higher production and cities of medium size and production levels. The proposed DEA models are then used to determine the trends in and differences among the selected cities. Finally, the models' results are compared to determine the cause-effect relations.

#### 3.1. Division of Cities

To ensure homogeneity among the Colombian cities selected for this study, the cities are grouped by size and production level using cluster analysis to reflect the city's overall characteristics. In this study, the eleven sample cities were divided into two groups whose major characteristics are listed in Table 2.

Groups	Composition and characteristics	Cities
Large, high-production cities	These are major cities in Colombia. These cities are characterized by a strong economic base and urban services, and they have relatively advanced technologies and convenient transportation. Their economic activity is strong.	Five cities: Barranquilla, Bogotá, Bucaramanga, Cali, Medellín
Medium-sized, mid-level production cities	These are intermediate cities in Colombia.  These cities are small or medium sized, with improvements in economic and technical conditions.  Their competitiveness needs to be improved overall, and their transportation and urban infrastructure is insufficient.	Six cities: Cartagena, Ibague, Manizales, Pasto, Pereira, Villavicencio

Table 2. Division of cities.

#### 3.2. DEA Environmental Model

Tables 3 and 4 show the results of the DEA environmental model for Colombian cities. Among the large, high-production cities, Bucaramanga, Medellin, and Cali are characterized by higher efficiency, whereas among the medium-sized cities, Pasto, Villavicencio, and Pereira exhibit higher efficiency under the CRS assumption (TE). These cities are more efficient in terms of the relation between resource use (energy and water) and lower pollution (CO<sub>2</sub> emissions and solid waste) and are therefore more environmentally sustainable. Policies, management, and other conditions in these cities allow efficient resource use, better resource consumption and reduce environmental impacts. According to the [43], in recent years, less material input has been required to produce one unit of real GDP, indicating that economic output is maintained while reducing negative environmental effects.

For VRS (PTE), the same cities are considered efficient in both groups, but when city scale increases, urban environmental sustainability decreases, as in the case of Bogotá, which is recognized

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as a megacity. In terms of SE, the inefficient cities (Barranquilla, Bogotá, Cartagena, and Ibague) present decreasing returns to scale, suggesting that urban environmental sustainability declines as the scale of these cities increases. This result occurs particularly through uncontrolled increases in population, resource use and production caused mainly by uncontrolled immigration resulting from violence or from people seeking better opportunities. This behavior generates an uncontrolled urbanization process. [44] have demonstrated that rapid urban expansion and population growth require more resources that in turn generate more consumption and production. Hence, increasing production and consumption in cities produce different environmental problems, such as air, water, and land pollution, as well as ecosystem degradation, which is consistent with the results related to city scale because a larger city creates greater environmental problems. Moreover, the results for cities should demonstrate that the intensity effect can be studied as a resource efficiency effect of the production chain in which resource efficiency is the inverse of pressure intensity [45].

Table 3. Results of the DEA environmental model for large, high-production cities.

Cities	Technical Efficiency											
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean		
Barranquilla	0.604	0.661	0.714	0.774	0.792	0.820	0.871	0.833	1	0.785		
Bogotá	0.616	0.649	0.659	0.681	0.703	0.716	0.746	0.751	0.748	0.697		
Bucaramanga	0.958	1	0.958	1	0.968	0.995	1	1	1	0.987		
Cali	0.704	0.714	0.757	1	0.797	0.813	0.840	0.862	0.831	0.813		
Medellin	0.769	0.821	0.806	0.892	0.861	0.838	0.874	0.881	0.852	0.844		
Cities		Pure Technical Efficiency										
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean		
Barranquilla	0.623	0.688	0.742	0.811	0.809	0.878	0.881	0.858	1	0.810		
Bogotá	0.649	0.671	0.673	0.760	0.743	0.766	0.775	0.782	0.790	0.734		
Bucaramanga	1	1	0.973	1	0.977	1	1	1	1	0.994		
Cali	0.724	0.728	0.765	1	0.821	0.823	0.853	0.884	0.848	0.827		
Medellin	1	0.842	0.824	0.913	0.876	0.883	0.891	0.896	0.872	0.889		
Cities					Scale E	ficiency						
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean		
Barranquilla	0.970	0.961	0.962	0.954	0.979	0.934	0.989	0.971	1	0.969		
Bogotá	0.949	0.967	0.979	0.896	0.946	0.935	0.963	0.960	0.947	0.949		
Bucaramanga	0.958	1	0.985	1	0.991	0.995	1	1	1	0.992		
Cali	0.972	0.981	0.990	1	0.971	0.988	0.985	0.975	0.980	0.982		
Medellin	0.769	0.975	0.978	0.977	0.983	0.949	0.981	0.983	0.977	0.952		

Table 4. Results of the DEA environmental model for cities of medium size and production levels.

Cities		Technical Efficiency											
	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean			
Cartagena	0.610	0.618	0.621	0.622	0.624	0.826	0.689	0.713	0.677	0.667			
Ibague	0.652	0.653	0.691	0.747	0.751	0.836	0.695	0.849	0.919	0.765			
Manizales	0.807	0.807	0.763	0.768	0.631	0.716	0.838	0.758	0.722	0.757			
Pasto	1	0.955	1	0.979	1	0.985	0.903	1	1	0.980			
Pereira	0.816	0.842	0.814	0.709	1	0.671	0.756	0.674	0.611	0.766			
Villavicencio	0.849	0.743	0.829	0.871	0.635	0.652	1	0.578	0.783	0.771			

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Cities	Pure Technical Efficiency												
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean			
Cartagena	0.650	0.681	0.682	0.692	0.682	0.872	0.743	0.759	0.709	0.719			
Ibague	0.659	0.669	0.748	0.763	0.766	0.854	0.765	0.957	0.932	0.779			
Manizales	0.893	0.842	0.823	0.818	0.665	0.762	0.870	0.794	0.746	0.801			
Pasto	1	0.961	1	0.988	1	0.994	0.956	1	1	0.989			
Pereira	1	0.860	0.822	0.756	1	0.691	0.917	0.707	0.681	0.826			
Villavicencio	0.887	0.769	0.853	0.894	0.643	0.708	1	0.678	0.889	0.813			
Cities	Scale Efficiency												
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean			
Cartagena	0.938	0.907	0.911	0.899	0.915	0.947	0.927	0.939	0.955	0.927			
Ibague	0.989	0.976	0.924	0.979	0.980	0.979	0.908	0.991	0.986	0.981			
Manizales	0.904	0.958	0.927	0.939	0.949	0.940	0.963	0.955	0.968	0.945			
Pasto	1	0.994	1	0.991	1	0.991	0.945	1	1	0.991			
Pereira	0.816	0.979	0.990	0.938	1	0.971	0.824	0.953	0.897	0.930			
Villavicencio	0.957	0.966	0.972	0.974	0.988	0.921	1	0.853	0.881	0.946			

### 3.3. DEA Social Model

The results of the DEA social model are presented in Tables 5 and 6. In both groups, Bucaramanga, Cali, Villavicencio, and Manizales exhibit higher TE based on the CRS assumption; this pattern indicates that these cities are more efficient at utilizing their expenditures and investments to decrease poverty and to increase housing production, particularly for lower socioeconomic segments.

These results suggest that, in these cities, investment and expenditure strategies have focused on the population segments with the highest need, which could contribute to decreasing social inequality and positively affect a city's productivity. In these cities, investments and expenditures should be intended to create measurable social benefits in addition to financial returns. Opportunities exist to make better use of scarce resources to support important social benefits and to identify potential interventions that balance the needs of public asset owners (particularly for scale, comparability and comfort) while ensuring the delivery of social benefits [46].

**Table 5.** Results of the DEA social model for larger, high-production cities.

Barranquilla   0.849   0.851   0.839   0.776   0.775   0.732   0.746   0.832   0.800   0.8												
Barranquilla   0.849   0.851   0.839   0.776   0.775   0.732   0.746   0.832   0.800   0.838	Cities				Te	echnical	Efficien	cy				
Bogota   0.639   0.634   0.635   0.652   0.657   0.638   0.643   0.646   0.647   0.088     Bucaramanga   0.956   0.966   1   1   0.982   0.985   0.993   1   1   0.988     Cali   0.844   0.818   0.802   0.818   0.907   0.763   0.719   0.768   0.873   0.388     Medellin   0.746   0.727   0.721   0.697   0.772   0.744   0.685   0.684   0.681   0.388     Cities   Pure Technical Efficiency	Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean	
Bucaramanga         0.956         0.966         1         1         0.982         0.985         0.993         1         1         0.982           Cali         0.844         0.818         0.802         0.818         0.907         0.763         0.719         0.768         0.873         0.8           Medellin         0.746         0.727         0.721         0.697         0.772         0.744         0.685         0.684         0.681         0.2           Cities         Pure Technical Efficiency           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.870         0.876         0.897         0.794         0.897         0.904         0.857         0.881         0.886         0.3           Bogotá         0.648         0.639         0.639         0.653         0.661         0.646         0.652         0.651         0.651         0.6           Bucaramanga         1         0.999         1         1         1         0.998         0.997         1         1         0.3           Cali         0.912         0.87	Barranquilla	0.849	0.851	0.839	0.776	0.775	0.732	0.746	0.832	0.800	0.800	
Cali         0.844         0.818         0.802         0.818         0.907         0.763         0.719         0.768         0.873         0.8           Medellin         0.746         0.727         0.721         0.697         0.772         0.744         0.685         0.684         0.681         0.3           Cities         Pure Technical Efficiency           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.870         0.876         0.897         0.794         0.897         0.904         0.857         0.881         0.886         0.8           Bogotá         0.648         0.639         0.639         0.653         0.661         0.646         0.652         0.651         0.651         0.6           Bucaramanga         1         0.999         1         1         1         0.998         0.997         1         1         0.3           Cali         0.912         0.871         0.843         0.856         0.947         0.866         0.760         1         1         0.3           Medellin         0.774         0.743	Bogotá	0.639	0.634	0.635	0.652	0.657	0.638	0.643	0.646	0.647	0.643	
Medellin         0.746         0.727         0.721         0.697         0.772         0.744         0.685         0.684         0.681         0.721           Cities           Pure Technical Efficiency           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.870         0.876         0.897         0.794         0.897         0.904         0.857         0.881         0.886         0.3           Bogotá         0.648         0.639         0.639         0.653         0.661         0.646         0.652         0.651         0.651         0.6           Bucaramanga         1         0.999         1         1         1         0.998         0.997         1         1         0.9           Cali         0.912         0.871         0.843         0.856         0.947         0.866         0.760         1         1         0.3           Medellin         0.774         0.743         0.735         0.808         0.818         0.884         0.815         0.722         0.726         0.3           Cities	Bucaramanga	0.956	0.966	1	1	0.982	0.985	0.993	1	1	0.987	
Pure Technical Efficiency           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.870         0.876         0.897         0.794         0.897         0.904         0.857         0.881         0.886         0.3           Bogotá         0.648         0.639         0.639         0.653         0.661         0.646         0.652         0.651         0.651         0.6           Bucaramanga         1         0.999         1         1         1         0.998         0.997         1         1         0.9           Cali         0.912         0.871         0.843         0.856         0.947         0.866         0.760         1         1         0.3           Medellin         0.774         0.743         0.735         0.808         0.818         0.884         0.815         0.722         0.726         0.3           Cities           Scale Efficiency           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquill	Cali	0.844	0.818	0.802	0.818	0.907	0.763	0.719	0.768	0.873	0.812	
Cities         2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.870         0.876         0.897         0.794         0.897         0.904         0.857         0.881         0.886         0.8           Bogotá         0.648         0.639         0.639         0.653         0.661         0.646         0.652         0.651         0.651         0.6           Bucaramanga         1         0.999         1         1         1         0.998         0.997         1         1         0.9           Cali         0.912         0.871         0.843         0.856         0.947         0.866         0.760         1         1         0.8           Medellin         0.774         0.743         0.735         0.808         0.818         0.884         0.815         0.722         0.726         0.3           Cities           Scale Efficiency           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.976         0.971 <td>Medellin</td> <td>0.746</td> <td>0.727</td> <td>0.721</td> <td>0.697</td> <td>0.772</td> <td>0.744</td> <td>0.685</td> <td>0.684</td> <td>0.681</td> <td>0.717</td>	Medellin	0.746	0.727	0.721	0.697	0.772	0.744	0.685	0.684	0.681	0.717	
2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.870         0.876         0.897         0.794         0.897         0.904         0.857         0.881         0.886         0.3           Bogotá         0.648         0.639         0.639         0.653         0.661         0.646         0.652         0.651         0.651         0.6           Bucaramanga         1         0.999         1         1         1         0.998         0.997         1         1         0.9           Cali         0.912         0.871         0.843         0.856         0.947         0.866         0.760         1         1         0.3           Medellin         0.774         0.743         0.735         0.808         0.818         0.884         0.815         0.722         0.726         0.3           Cities           Scale Efficiency           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.976         0.971         <	Cities		Pure Technical Efficiency									
Bogotá         0.648         0.639         0.639         0.653         0.661         0.646         0.652         0.651         0.651         0.6           Bucaramanga         1         0.999         1         1         1         0.998         0.997         1         1         0.9           Cali         0.912         0.871         0.843         0.856         0.947         0.866         0.760         1         1         0.8           Medellin         0.774         0.743         0.735         0.808         0.818         0.884         0.815         0.722         0.726         0.3           Scale Efficiency           Scale Efficiency           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.976         0.971         0.935         0.977         0.864         0.810         0.870         0.944         0.903         0.9	Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean	
Bucaramanga         1         0.999         1         1         1         0.998         0.997         1         1         0.98           Cali         0.912         0.871         0.843         0.856         0.947         0.866         0.760         1         1         0.8           Medellin         0.774         0.743         0.735         0.808         0.818         0.884         0.815         0.722         0.726         0.3           Scale Efficiency           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.976         0.971         0.935         0.977         0.864         0.810         0.870         0.944         0.903         0.9	Barranquilla	0.870	0.876	0.897	0.794	0.897	0.904	0.857	0.881	0.886	0.874	
Cali         0.912         0.871         0.843         0.856         0.947         0.866         0.760         1         1         0.8           Medellin         0.774         0.743         0.735         0.808         0.818         0.884         0.815         0.722         0.726         0.3           Cities           Scale Efficiency           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.976         0.971         0.935         0.977         0.864         0.810         0.870         0.944         0.903         0.9	Bogotá	0.648	0.639	0.639	0.653	0.661	0.646	0.652	0.651	0.651	0.649	
Medellin         0.774         0.743         0.735         0.808         0.818         0.884         0.815         0.722         0.726         0.726           Cities           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.976         0.971         0.935         0.977         0.864         0.810         0.870         0.944         0.903         0.944	Bucaramanga	1	0.999	1	1	1	0.998	0.997	1	1	0.999	
Scale Efficiency           2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.976         0.971         0.935         0.977         0.864         0.810         0.870         0.944         0.903         0.94	Cali	0.912	0.871	0.843	0.856	0.947	0.866	0.760	1	1	0.895	
Cities         2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.976         0.971         0.935         0.977         0.864         0.810         0.870         0.944         0.903         0.9	Medellin	0.774	0.743	0.735	0.808	0.818	0.884	0.815	0.722	0.726	0.781	
2005         2006         2007         2008         2009         2010         2011         2012         2013         M           Barranquilla         0.976         0.971         0.935         0.977         0.864         0.810         0.870         0.944         0.903         0.93	Cities					Scale E	ficiency					
	Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean	
Bogotá 0.986 0.992 0.994 0.998 0.994 0.988 0.986 0.992 0.994 0.9	Barranquilla	0.976	0.971	0.935	0.977	0.864	0.810	0.870	0.944	0.903	0.917	
	Bogotá	0.986	0.992	0.994	0.998	0.994	0.988	0.986	0.992	0.994	0.992	
Bucaramanga 0.956 0.967 1 1 0.982 0.987 0.996 1 1 0.98	Bucaramanga	0.956	0.967	1	1	0.982	0.987	0.996	1	1	0.988	
Cali 0.925 0.939 0.951 0.956 0.958 0.881 0.946 0.76 0.873 0.9	Cali	0.925	0.939	0.951	0.956	0.958	0.881	0.946	0.76	0.873	0.911	
Medellin 0.964 0.978 0.981 0.863 0.944 0.842 0.840 0.947 0.938 0.94	Medellin	0.964	0.978	0.981	0.863	0.944	0.842	0.840	0.947	0.938	0.922	

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**Table 6.** Results of the DEA social model for cities of medium size and production levels.

Cities				Te	echnical	Efficien	сy				
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean	
Cartagena	0.762	0.717	0.718	0.701	0.771	0.758	0.788	0.813	0.694	0.747	
Ibague	1	0.975	0.839	0.735	0.808	0.757	0.981	0.902	0.917	0.879	
Manizales	0.948	0.775	0.751	0.831	0.929	0.872	0.918	1	1	0.892	
Pasto	0.905	0.666	0.641	0.754	1	0.714	1	0.902	0.725	0.812	
Pereira	0.888	0.969	0.810	0.846	0.853	0.945	0.878	0.769	1	0.884	
Villavicencio	0.827	0.911	0.877	1	0.997	0.953	0.881	0.986	0.824	0.917	
Cities		Pure Technical Efficiency									
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean	
Cartagena	0.809	0.755	0.729	0.720	0.798	0.813	0.791	0.827	0.712	0.773	
Ibague	1	0.999	0.874	0.763	0.818	0.831	1	0.936	0.938	0.907	
Manizales	0.984	0.859	0.753	0.846	1	0.974	0.980	1	1	0.933	
Pasto	0.908	0.667	0.647	0.763	1	0.892	1	0.908	0.781	0.841	
Pereira	0.895	1	0.814	0.847	0.859	1	0.885	0.812	1	0.901	
Villavicencio	0.831	0.945	0.903	1	0.998	0.973	0.914	1	0.846	0.934	
Cities					Scale E	fficiency					
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean	
Cartagena	0.942	0.950	0.985	0.974	0.966	0.932	0.996	0.983	0.975	0.967	
Ibague	1	0.976	0.960	0.963	0.988	0.911	0.981	0.964	0.978	0.969	
Manizales	0.963	0.902	0.997	0.982	0.929	0.895	0.937	1	1	0.956	
Pasto	0.997	0.999	0.991	0.988	1	0.800	1	0.993	0.928	0.966	
Pereira	0.992	0.969	0.995	0.999	0.993	0.945	0.992	0.947	1	0.981	
Villavicencio	0.995	0.964	0.971	1	0.999	0.979	0.964	0.986	0.974	0.981	

For the VRS assumption, the results for PTE indicate that the same cities in both groups are considered efficient as for the CRS assumption. When city scale increases, urban social sustainability decreases because of the increase in the complexity and the demands of social needs, which in certain cases, the city is unable to solve due to scarce resources or lack of capacity to respond. These results concur with the [47,48], which states that as cities grow in size and population, it is important to seek harmony among spatial, social, and environmental aspects based on two key pillars: equity and sustainability. Moreover, cities that experience high levels of inequality and poverty increase their risk of political tension and social conditions that undermine security and economic development, which in turn reduce incentives for investment and increase the amount of public resources needed to maintain national security. Hence, resources that can strengthen productivity, development, social services, and infrastructures must be used for security; however, this choice leads to deterioration of the cities' social conditions [49].

#### 3.4. DEA Economic Model

This model analyses the relation between resources and GDP. Tables 7 and 8 show the results of this model. In both models (CRS and VRS), Bucaramanga, Medellin, Cali, Cartagena, and Pasto show higher efficiency. Therefore, in the first case CRS assumption, these cities are more efficient in the use of resources (energy, water, and investments) to generate a higher GDP; they have better economic sustainability, indicating that management drives the lower use of resources to generate more economic production.

For VRS (PTE), the results indicate that the same cities are considered efficient in both categories, and when city scale increases, urban economic sustainability declines. The SE results show that inefficient cities experience a reduction in returns to scale, indicating that urban economic sustainability decreases as these cities increase in size.

**Table 7.** Results of the DEA economic model for larger, high-production cities.

Cities	Technical Efficiency											
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean		
Barranquilla	0.723	0.664	0.810	0.651	0.589	0.647	0.715	0.678	1	0.720		
Bogotá	0.847	0.845	0.843	0.876	0.756	0.805	0.848	0.806	0.911	0.838		
Bucaramanga	0.891	1	0.958	1	0.924	0.890	1	0.906	1	0.952		
Cali	0.885	0.854	0.857	1	1	1	0.961	0.772	1	0.925		
Medellin	1	0.992	0.988	0.964	0.799	0.966	0.931	1	1	0.960		
Cities		Pure Technical Efficiency										
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean		
Barranquilla	0.742	0.669	0.868	0.660	0.730	0.826	0.895	0.687	1	0.786		
Bogotá	0.848	0.850	0.847	0.878	0.822	0.816	0.859	0.883	0.913	0.857		
Bucaramanga	0.898	1	0.995	1	1	0.917	1	0.907	1	0.946		
Cali	0.914	0.879	0.859	1	1	1	1	0.815	1	0.941		
Medellin	1	1	1	1	0.809	0.968	0.933	1	1	0.968		
Cities					Scale E	ficiency						
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean		
Barranquilla	0.974	0.993	0.933	0.986	0.807	0.783	0.799	0.987	1	0.918		
Bogotá	0.999	0.994	0.995	0.998	0.920	0.987	0.987	0.913	0.998	0.977		
Bucaramanga	0.992	1	0.963	1	0.924	0.971	1	0.999	1	0.983		
Cali	0.968	0.972	0.998	1	1	1	0.961	0.947	1	0.983		
Medellin	1	0.992	0.988	0.964	0.988	0.998	0.998	1	1	0.992		

 Table 8. Results of the DEA economic model for cities of medium size and production levels.

Cities				To	echnical	Efficien	сy			_		
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean		
Cartagena	0.732	0.942	0.945	1	0.567	1	0.989	1	0.948	0.903		
Ibague	0.673	0.955	0.646	0.880	0.619	0.661	0.579	0.858	0.728	0.733		
Manizales	0.897	0.805	0.684	0.772	0.542	0.658	0.704	0.815	0.514	0.710		
Pasto	0.820	0.655	1	1	1	0.946	0.604	1	0.621	0.850		
Pereira	0.767	0.822	0.776	0.669	0.836	0.682	0.721	0.772	0.537	0.731		
Villavicencio	0.502	0.618	0.647	0.697	0.629	0.538	1	0.829	0.953	0.713		
Cities		Pure Technical Efficiency										
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean		
Cartagena	0.751	0.945	0.947	1	0.592	1	1	1	1	0.915		
Ibague	0.746	1	0.708	0.901	0.843	0.926	0.634	1	0.833	0.843		
Manizales	1	0.859	0.734	0.815	0.585	0.999	0.970	1	0.589	0.839		
Pasto	1	0.675	1	1	1	0.958	0.708	1	0.654	0.888		
Pereira	0.827	0.857	0.828	0.697	1	0.774	0.863	0.859	0.602	0.812		
Villavicencio	0.768	0.683	0.953	0.911	0.888	0.545	1	0.867	1	0.846		
Cities					Scale Ef	ficiency						
Cities	2005	2006	2007	2008	2009	2010	2011	2012	2013	Mean		
Cartagena	0.975	0.997	0.998	1	0.958	1	0.989	1	0.948	0.985		
Ibague	0.902	0.955	0.912	0.977	0.734	0.714	0.913	0.858	0.874	0.871		
Manizales	0.897	0.937	0.932	0.947	0.926	0.659	0.726	0.815	0.873	0.857		
Pasto	0.820	0.970	1	1	1	0.987	0.853	1	0.950	0.953		
Pereira	0.927	0.959	0.937	0.960	0.836	0.881	0.835	0.899	0.892	0.903		
Villavicencio	0.654	0.905	0.679	0.765	0.708	0.987	1	0.956	0.953	0.845		

The results indicate that medium-sized cities more closely balance population and productivity activities to become efficient. In contrast, large cities show disproportionate population growth increases demands for housing resources, decreasing the productivity relation.

These results show that it is important to generate new processes and innovations to promote greener economic development. These processes and innovations include cost savings through the effective and efficient use of resources, less reliance on unsustainable energy sources, new jobs, and economic investment created through sustainable consumption and production, generating urban sustainability by improving resource efficiency, reducing carbon emissions, minimizing environmental risks, and enhancing ecosystems [50]. In Colombia, medium-sized cities have achieved improvements in urban sustainability through better urban planning and management, promoting economic development, reducing environmental impacts, and improving social welfare.

Economic growth and sustainability require solutions in which both are balanced and coexist. This balance implies the development of innovation strategies and solutions that allow growth spirals of the economy and the population, prevent resource depletion, reduce environmental impacts, and improve social conditions. However, environmental problems reflect the tension between short-term growth and long-term survival [51], which requires the development of adequate sustainability policies, particularly in cities that tend to have larger populations and generate more social and pollution problems.

The DEA models proposed in this study have different advantages: (i) these models can handle multiple inputs and output to evaluate sustainability from different approaches; (ii) they do not require the assumption of a functional form relating inputs to outputs; (iii) cities are directly compared against a peer or a combination of peers; (iv) inputs and outputs can have very different units; and (v) this technique allows efficiency evaluation of sustainability over time in the selected cities. However, the DEA models suggested have some limitations: (i) these models are not adequate for calculating absolute efficiencies (they are adequate for comparing peers but not comparing performance to a theoretical maximum); (ii) DEA is a nonparametric technique, and statistical hypothesis testing is complex; (iii) it is not meaningful to compare the scores between two different studies; (iv) all efficient cities are assigned the same score (1.00); thus, a further ranking is not possible; (v) this is a quantitative analysis that should be complemented with qualitative analyses that should include urban governance and policy processes to strengthen the analysis and design of urban instruments and programs to achieve sustainable and balanced economic and social development in cities.

The results of the three models reveal differences in the two categories of cities selected for this study. Colombian cities achieve higher efficiency in three sustainability areas (environmental, social, and economic factors). These results suggest that policies are integral to achieving sustainable development, which includes higher economic growth and development, improved social performance and quality of life, and lower environmental impacts.

The models proposed in this study can be applied in other Latin American cities to analyze sustainable efficiency and to compare performance along different dimensions of sustainability, which will allow the adequate design of urban policies to promote better environmental resource use, greater social inclusion, and economic growth.

This study suggests that achieving sustainability requires quantitative and qualitative analysis and evaluation, where the urban governance strategy is key to balancing conditions related to social equity without risking the harmony, productivity, and employment of urban systems. It is important to promote cleaner production, innovation, social inclusion, adequate public management, and new livelihood opportunities to effectively enable sustainable urban development.

## 4. Conclusions

This study uses various DEA models to evaluate the relative sustainable development of typical Colombian cities and to determine the different relations and factors that influence these results. The following conclusions can be drawn:

(1) In this study, DEA is applied to assess the relative sustainable development of 11 Colombian cities. The majority of these cities (*i.e.*, Bucaramanga, Medellin, Cali, Pasto, Villavicencio, and Pereira) exhibit relatively sustainable development.

- (2) The results for Colombian cities suggest that inefficiency is present when decreasing returns to scale exist and that when city scale increases, urban sustainability tends to decline.
- (3) Efficiency is decreased by several factors, such as changes in scale (increased size tends to generate a higher concentration of population with higher demands for services, which decreases the efficiency of resource and energy use). Moreover, in megacities or large cities, investments are atomized in social areas, such as housing, which should increase social inequality and reduce productivity.
- (4) A city's scale also affects the environment because of coupling (*i.e.*, the relation between exponential growth in demand for goods and consumption). Hence, megacities and large cities experience increased material and energy flows, generating more environmental processes and higher air pollution and waste, while productivity is maintained or decreased. In contrast, medium-sized cities are characterized by a better relation between material and energy use, resulting in increased efficiency.
- (5) Sustainable development requires resource, environmental, economic, and social balance. For megacities and large cities, it is necessary to promote decoupling, which implies decreasing the exponential growth of goods and services demands in relation to lineal population growth. This change would increase efficiency and decrease environmental and social impacts. Moreover, it is important to balance social investment to decrease inequality. In Colombian cities of both categories, more efficient cities use resources adequately, decrease environmental impacts, improve social conditions, and guarantee economic growth and development.

The findings of this study are important for developing adequate urban policies based on the size and features of cities, promoting sustainable development based on balancing economic, social, and environmental conditions and considering each city's situation and features to improve urban planning and development, particularly in developing countries. Moreover, it is important to continue analyzing sustainable performance using other approaches and to determine the main factors that contribute more sustainable development.

Future studies should consider additional cities in Latin America, other inputs and outputs, and time series, depending on data availability. One possible extension is to measure dynamic urban sustainability using other techniques, such as meta-frontier analysis and the Malmquist index. Research could also be extended to parametric analysis, qualitative analysis, and cause-effect relationships applying panel data techniques.

#### References

- 1. UN-Habitat (United Nations Human Settlements Programme). The State of the World's Cities rEport 2006/2007. Available online: https://sustainabledevelopment.un.org/content/documents/11292101\_alt.pdf (accessed on 29 September 2015).
- UN (United Nations). World Urbanization Prospects (Highlights). Available online: http://esa.un.org/ unpd/wup/Highlights/WUP2014-Highlights.pdf (accessed on 2 October 2016).
- 3. Pardo Martínez, C.; Alfonso, W. The suburbanisation process in Bogotá D.C. and municipalities of the Savanna of Bogotá, 1998–2010. In *Suburbanization versus Peripheral Sustainability of Rural-Urban Areas Fringes*; Nova: New York, NY, USA, 2014; pp. 103–122.
- Brezies, E.; Krugman, P. Technology and the Life Cycle of Cities. J. Econ. Growth 1997, 2, 369–383.
- Saxenian, A. Regional Advantage: Culture and Competition in Silicon Valley and Route 128; Harvard University Press: Cambridge, MA, USA, 1994.
- 6. Alfonso, W.; Pardo Martínez, C. Urban material flow analysis: An approach for Bogotá, Colombia. *Ecol. Indic.* **2014**, *42*, 32–42.
- 7. ICLEI. Eco-Efficient Cities—Quality of Life for All at Least Cost for the Globe, 2006. Available online: http://www.iclei.org/sa (accessed on 29 August 2016).

8. Expert Group on the Urban Environment. *The Sustainable Cities Report. European Commission, Directorate General XI, Environment, Nuclear Safety and Civil Protection*; Expert Group on the Urban Environment: Brussels, Belgium, 1996.

- 9. Girardet, H. Creating Sustainable Cities; Green Books for the Schumacher Society: Cambridge, UK, 1999.
- 10. Tabb, P.; Deviren, S. *The Greening of Architecture: A Critical History and Survey of Contemporary Sustainable Architecture and Urban Design*; Ashgate Publishing Ltd.: Burlington, VT, USA, 2014.
- 11. Lee, J.; Kurisu, K.; Hanaki, K. Development of the compact city index and its application to Japanese cities. *Urban Stud.* **2015**, *52*, 1054–1070.
- 12. Miao, B.; Lang, G. A Tale of Two Eco-Cities: Experimentation under Hierarchy in Shanghai and Tianjin. *Urban Policy Res.* **2014**. [CrossRef]
- 13. Ecocity Builders. International Ecocity Framework and Standards. Available online: http://ecocitybuilders.org (accessed on 2 May 2015).
- 14. Fernández-Viñé, M.; Gómez, T.; Capuz, S. Assessment of the public administration tools for the improvement of the eco-efficiency of Small and Medium Sized Enterprises. *J. Clean. Prod.* **2013**, 47, 265–273.
- 15. UEAPME (European Association of Craft, Small and Medium-sized Enterprises). Overview of the Problems Faced by Micro and Small Businesses when Applying the Concept of Eco-efficiency, Including Energy Efficiency; UEAPME: Brussels, Belgium, 2007.
- 16. Zhang, Y.; Zhao, Y.; Yang, Z.; Chen, B.; Chen, G. Measurement and evaluation of the metabolic capacity of an urban ecosystem. *Commun. Nonlinear Sci. Numer Simulat.* **2009**, *14*, 1758–1765.
- 17. Liu, Y.; Song, Y.; Arp, H. Examination of the relationship between urban form and urban eco-efficiency in china. *Habitat Int.* **2012**, *36*, 171–177.
- 18. Wang, Q.; Zhao, Z.; Shen, N.; Liu, T. Have Chinese cities achieved the win–win between environmental protection and economic development? From the perspective of environmental efficiency. *Ecol. Indic.* **2015**, 51, 151–158. [CrossRef]
- 19. Yu, Y.; Wen, Z. Evaluating China's urban environmental sustainability with Data Envelopment Analysis. *Ecol. Indic.* **2010**, *69*, 1748–1755.
- 20. Koskela, M.; Vehmas, J. Defining eco-efficiency: A case study on the Finnish forest industry. *Bus. Strateg. Environ.* **2012**, *21*, 546–566. [CrossRef]
- 21. Mattila, T. Any sustainable decoupling in the Finnish economy? A comparison of the pathways and sensitivities of GDP and ecological footprint 2002–2005. *Ecol. Indic.* **2012**, *16*, 128–134.
- 22. Agostinho, F.; Pereira, L. Support area as an indicator of environmental load: Comparison between Embodied Energy, Ecological Footprint, and Emergy Accounting methods. *Ecol. Indic.* **2013**, 24, 494–503.
- 23. Jorgenson, A.; Clark, B. Societies consuming nature: A panel study of the ecological footprints of nations, 1960–2003. *Soc. Sci. Res.* **2011**, *40*, 226–244. [CrossRef]
- 24. Rattanapan, C.; Suksaroj, T.; Ounsaneha, W. Development of Eco-efficiency Indicators for Rubber Glove Product by Material Flow Analysis. *Procedia Soc. Behav. Sci.* **2012**, 40, 99–106. [CrossRef]
- 25. Ramli, N.; Munisamy, S. Eco-efficiency in greenhouse emissions among manufacturing industries: A range adjusted measure. *Econ. Model.* **2015**, *47*, 219–227.
- 26. Wu, J.; Wu, Z.; Holländer, R. The application of Positive Matrix Factorization (PMF) to eco-efficiency analysis. *J. Environ. Manag.* **2012**, *98*, 11–14.
- 27. Sarkis, J.; Cordeiro, J. Ecological modernization in the electrical utility industry: An application of a bads–goods DEA model of ecological and technical efficiency. *Eur. J. Oper. Res.* **2012**, 219, 386–395.
- 28. Song, M.; An, Q.; Zhang, W.; Wang, Z.; Wu, J. Environmental efficiency evaluation based on data envelopment analysis: A review. *Renew. Sustain. Energy Rev.* **2012**, *16*, 4465–4469.
- 29. Pardo Martínez, C. Estimating and Analyzing Energy Efficiency in German and Colombian Manufacturing Industries Using DEA and Data Panel Analysis. Part I: Energy-intensive Sectors. *Energy Sour. Part B Econ. Plan. Policy* **2015**, *10*, 322–331.
- 30. Charnes, A.; Cooper, W.; Rhodes, E. Measuring efficiency of decision making units. *Eur. J. Oper. Res.* **1978**, 2, 429–444. [CrossRef]
- 31. Charnes, A.; Cooper, W.; Lewin, A. *Data Envelopment Analysis: Theory, Methodology and Applications*; Kluwer: Boston, MA, USA, 1994.
- 32. Banker, R.; Charnes, A.; Cooper, W. Some models for estimating technical and scale efficiencies in data envelopment analysis. *Manag. Sci.* **1984**, *30*, 1078–1092.

33. Coelli, T.; Prasada, D.; O'Donnell, C.; Battese, G. *An Introduction to Efficiency and Productivity Analysis*, 2nd ed.; Springer: New York, NY, USA, 2005.

- 34. Cooper, W.W.; Seiford, L.M.; Kaoru, T. Data Envelopment Analysis, A ComprehensiveText with Models, Applications, Reference and DEA-Solver Software; KluwerAcademic Publisher: Morwell, Australia, 2000.
- 35. Mac Queen, J. Some methods for classification and analysis of multivariate observations. In Proceedings of 5th Berkeley Symposium on Mathematical Statistics and Probability, Berkeley, CA, USA, 21 June–18 July 1965; University of California Press: Berkeley, CA, USA, 1967; Volume 1, pp. 281–297.
- 36. Charnes, A.; Clark, T.; Cooper, W.; Golany, B. A developmental study of data envelopment analysis in measuring the efficiency of maintenance units in U. S. Air Forces. *Ann. Oper. Res.* **1985**, 2, 95–112.
- 37. Bowlin, W. Evaluating the efficiency of US Air Force real-property maintenance activities. *J. Oper. Res. Soc.* **1987**, *38*, 127–135.
- 38. World Economic and Social Survey (WESS). Sustainable Development Challenges. Chapter III: Towards Sustainable Cities, 2013. Available online: http://www.un.org/en/development/desa/policy/wess/wess\_current/wess2013/Chapter3.pdf (accessed on 2 November 2015).
- 39. Canadian International Development Agency (CIDA). Indicators for Sustainability. How cities are monitoring and evaluating their success, 2012. Available online: www.sustainablecities.net (accessed on 29 January 2016).
- 40. Shen, L.; Ochoa, J.; Shah, M.; Zhang, X. The application of urban sustainability indicators—A comparison between various practices. *Habitat Int.* **2011**, *35*, 17–29.
- 41. Fare, R.; Grosskopf, S.; Lovell, C.; Pasurka, C. Multilateral productivity comparison when some outputs are undesirable: A nonparametric approach. *Rev. Econ. Stat.* **1989**, *71*, 90–98.
- 42. Pardo Martínez, C.; Alfonso, W. Regional analysis across Colombian departments: A non-parametric study of energy use. *J. Clean. Prod.* **2016**, *115*, 130–138.
- 43. UNEP. Decoupling natural resource use and environmental impacts from economic growth, 2003. Available online: http://www.unep.org (accessed on 19 October 2015).
- 44. Puppim, J.; Doll, C.; Suwa, K. Urban Development with Climate Co-Benefits: Aligning Climate, Environmental and Other Development Goals in Cities. Available online: http://collections.unu.edu/view/UNU:1498 (accessed on 19 October 2015).
- 45. European Environment Agency (EEA). Progress on Resource Efficiency and Decoupling in the EU-27. Available online: http://www.eea.europa.eu/publications/progress-on-resource-efficiency-and (accessed on 9 November 2015).
- 46. Wood, D.; Thornley, B.; Grace, K. Impact at Scale the Second Report Published by the Global Impact Investing Policy Project, 2012. Available online: https://www.rockefellerfoundation.org/app/uploads/ Impact-at-Scale\_Full-Report.pdf (accessed on 15 November 2015).
- 47. UN-Habitat (United Nations Human Settlements Programme). State of the World's Cities 2008/2009 Harmonious Cities, 2008. Available online: https://sustainabledevelopment.un.org/content/documents/11192562\_alt-1.pdf (accessed on 29 January 2016).
- 48. Pardo Martínez, C.; Alfonso, W. Effects of Urbanisation and Suburbanisation on Health in the Bogotá Region. In *Health, Violence, Environment and Human Development in Developing Countries*; Nova: New York, NY, USA, 2013; pp. 147–164.
- 49. Garcia, A.; Gruat, J. Social Protection: A Life Cycle Continuum Investment for Social Justice, Poverty Reduction and Development, International Labour Office, 2003. Available online: http://www.ilo.org/public/english/protection/download/life cycl/ lifecycle.pdf (accessed on 19 October 2015).
- 50. UNEP. Global Initiative for Resource Efficient Cities, 2012. Available online: http://www.unep.org/pdf/GI-REC\_4pager.pdf (accessed on 7 November 2015).
- 51. Higgins, K. Economic Growth and Sustainability—Are They Mutually Exclusive? Striking a Balance between Unbounded Economic Growth and Sustainability Requires a New Mind Set. Available online: http://www.elsevier.com/connect/economic-growth-and-sustainability-are-they-mutually-exclusive# (accessed on 17 November 2015).



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