


Article

Study on Frost-Suppression Characteristics of Superhydrophobic Aluminum Surface Heat Exchanger Applied in Air Source Heat Pump

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Abstract: In order to solve the frosting problem of air source heat pump (ASHP) outdoor heat exchange under low-temperature and low-humidity conditions, a superhydrophobic aluminum (Al) surface with a contact angle (CA) of 158.3° was prepared by chemical etching. The microscopic characteristics of droplet condensation and the freezing process of a superhydrophobic surface were revealed through visual experiments and theoretical analysis. On this basis, the frost-suppression effect of a superhydrophobic Al-based surface simulating the distribution of actual heat exchanger fins was preliminarily explored. The results demonstrated that, due to the large nucleation energy barrier and the coalescence-bounce behavior of droplets, the condensed droplets on the superhydrophobic surface appeared late and their quantity was low. The thermal conductivity of the droplets on a superhydrophobic surface was large, so their freezing rate was low. The frosting amount on the superhydrophobic Al-based surface was 69.79% of that of the bare Al-based surface. In turn, the time required for melting the frost layer on the superhydrophobic Al-based surface was 64% of that on the bare Al-based surface. The results of this study lay an experimental and theoretical foundation for the application of superhydrophobic technology on the scale of heat exchangers.

Keywords: air source heat pump; superhydrophobic; antifrosting; defrosting; frost-suppression mechanism



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1. Introduction

Electric ASHPs have found worldwide applications due to their advantages of energy saving and environmental protection [1–3]. However, when the heat pump operates under heating conditions in winter, at ambient air temperatures of −15 °C to 11.5 °C and relative humidity higher than 30%, coil pipes of heat pump outdoor units are prone to frosting [4]. As a result, frost deposition and accumulation on the coil surface will affect the heating capacity, and can even cause the unit to stop in severe cases [5,6].

In order to ensure the operation efficiency of ASHPs in winter, a variety of methods have been proposed to restrain and defrost the frost layer on the coil surface. Commonly used defrosting techniques include electric heating defrosting [7,8], reverse-cycle defrosting [9,10], thermal storage defrosting [9,10], and hot-gas bypass defrosting [10–13]. However, they often need either special equipment or complex process control [10,14]. Therefore, finding a stable, high-performance, safe and efficient defrosting technology has become an urgent task. In 1997, Barthlott and Neinhuis [15] established that the unique micro-nano structure of lotus leaves and the presence of a wax film on their surface are the reasons for their antiwetting and superhydrophobic properties. Inspired by the impressive superhydrophobic surfaces in nature, various superhydrophobic materials have been realized for a wide range of antifrost, anticorrosion, antifogging, oil-water separation, and self-cleaning applications [16–19]. Thereinto, the frost resistance of the superhydrophobic

surface has attracted the attention of many scholars, and numerous surface modification technologies have been proposed to construct superhydrophobic surface structures similar to lotus leaves [20,21]. The ASHP defrosting requires that a superhydrophobic surface be constructed on the metal substrate. At present, the commonly used methods for obtaining superhydrophobic surfaces on metal substrates consist of etching [22,23], templating [24,25], anodic oxidation [26], deposition [27,28], and hydrothermal reactions [29].

Superhydrophobic surfaces usually refer to the solid surfaces on which the CA of the droplets is greater than 150° and the roll-off angle is less than 10° [30]. The frost-suppression mechanism and the effect of superhydrophobic surface have been deeply investigated by predecessors. In the microscopic observation of frosting process, scholars have found that the frosting process includes droplet formation, droplet freezing, frost crystal formation, and frost layer growth [31]. Huang et al. [32] reported that the water droplet freezing time on the superhydrophobic copper foil surface was later than that on the plain copper foil surface due to the smaller contact area between the spherical water droplets and the superhydrophobic surface. Jung et al. [33] studied the nucleation mechanism theory and heat transfer physics of droplets on superhydrophobic surfaces and established that humidity and flowing gas in the surrounding environment can fundamentally change the crystallization mechanism of ice and greatly affect the ice hydrophobicity of the surface. According to Boreyko et al. [34], the bouncing phenomenon of droplets on the superhydrophobic surface can delay the growth of frost by preventing heterogeneous ice nucleation and limiting the formation of ice bridges between droplets. Luo et al. [35] observed the freezing of droplets on cold surfaces due to ice bridge propagation. In particular, ice bridges were formed between frozen and unfrozen droplets until all droplets on the surface became frozen. Meanwhile, the droplet distribution across the superhydrophobic surface was sparse, and the distances between the frozen and unfrozen droplets were long. In this respect, the droplet freezing speed on the superhydrophobic surface was slower than that on the bare surface. Wang et al. [36] conducted visual frosting experiments on the hydrophilic, hydrophobic and superhydrophobic surfaces, reporting that the superhydrophobic surface showed good frost-inhibition characteristics. Sommers et al. [37] compared the frosting processes on the hydrophilic, bare and hydrophobic surfaces, concluding that the frosting density of the hydrophilic surface was 20–26% higher than that of the bare surface, whereas the frosting density of the hydrophobic surface was 37–41% lower than that of the bare surface. Table 1 summarizes the results on superhydrophobic surface frost suppression published in 2010–2021.

In recent years, significant progress has been made in experimental research and theoretical analysis of metal-based superhydrophobic frost-suppression technology, but the study on superhydrophobic technology for ASHP frost suppression is still in the laboratory stage. There are three main reasons. First, a simple, efficient and environmentally friendly preparation technology to produce superhydrophobic metal surfaces on a large scale has not been found yet. Second, the frost-suppression mechanism of the superhydrophobic surface is still poorly understood. Third, the existing data on the superhydrophobic frost suppression are only on the single fin scale, and the application of superhydrophobic layer on the whole surface of the heat exchange requires a thorough investigation. Bearing these circumstances in mind, the preparation of superhydrophobic Al surfaces with long-term stability by means of chemical etching is reported here. Special attention is paid to the frost-suppression mechanism of the superhydrophobic surface in the early frosting stage. The superhydrophobic Al-based surface simulating the distribution of actual heat exchanger fins was prepared, and a visual frost-suppression experiment platform was set up to investigate the frost-suppression effect of superhydrophobic surfaces. The findings of this study open up new prospects for further promotion of superhydrophobic technology for inhibiting frosting of ASHPs.

Table 1. Studies on superhydrophobic surface frost suppression (2010–2021).

No.	Year	Authors	Results
1	2010	Huang [32]	Due to the smaller contact area between the spherical water droplet and the superhydrophobic surface, the water droplets' freezing time was later than that on the plain copper foil surface.
2	2011	Farhadi [38]	The superhydrophobic surface had good ice resistance, but the ice resistance of the surface deteriorated during the icing/deicing cycle.
3	2012	Jung [33]	Humidity and flowing gas in the surrounding environment could fundamentally change the crystallization mechanism of ice and greatly affect the ice hydrophobicity of the surface.
4	2013	Boreyko [34]	The bouncing phenomenon of superhydrophobic surface droplets could delay the growth of frost by preventing heterogeneous ice nucleation and limiting the formation of ice bridges between droplets.
5	2014	Liang [31]	The frosting process included droplet formation, droplet freezing, frost crystal formation, and frost layer growth.
6	2015	Kim [39]	When the refrigerant temperature was $-10\text{ }^{\circ}\text{C}$ or $-12\text{ }^{\circ}\text{C}$, the effect of frost retardation increased remarkably with an increase in superhydrophobic surface's contact angle. However, when the refrigerant temperature was $-8\text{ }^{\circ}\text{C}$, the effect of superhydrophobicity diminished at water contact angles greater than 150° .
7	2016	Wang [36]	Under the same experimental conditions, the frost amount of a superhydrophobic heat exchanger was reduced by 18.0% and 38.6%, respectively, compared with hydrophilic and ordinary heat exchangers; the defrosting time was reduced by 41.7% and 43.2%, respectively.
8	2016	Sommers [37]	The frosting density of the hydrophilic surface was 20–26% higher than that of the bare surface, and the frosting density of the hydrophobic surface was 37–41% lower than that of the bare surface.
9	2017	Ji [40]	The freezing of droplets on the superhydrophobic took from 17 min to 26 min, while those on the bare surface froze within 4 min.
10	2017	Chu [41]	Because of the self-propelled movements, the melting droplets on the superhydrophobic surface became quite dynamic, self-cleaning the surface and leaving very small surface coverage.
11	2018	Kim [42]	Neither the superhydrophilic surface nor the superhydrophobic one influenced the defrosting time when the density was less than 200 kg/m^3 . However, when the frost layer density was over 200 kg/m^3 , the superhydrophobic surface was effective in reducing defrosting time.
12	2019	Luo [35]	The droplet freezing speed on the superhydrophobic surface was slower than that on the bare surface due to the ice bridge propagation.
13	2020	Wang [43]	The sprayable superhydrophobic surface showed excellent antifrosting characteristics, and the frost layer thickness decreased by 33% after frosting for 60 min.
14	2020	Li [44]	When the surface inclination angle was more than 30° , the drainage rate of the superhydrophobic surface could reach more than 90%.
15	2020	Li [45]	Electrochemical measurements revealed that the superhydrophobic surface showed better corrosion resistance than the bare copper surface and the inhibition efficiency of the superhydrophobic surface was about 95.91%.
16	2021	Su [46]	The growth rate of the frost layer on the hydrophilic surface was twice that on the superhydrophobic surface and three times that on the superhydrophobic surface.
17	2021	Reichl [47]	The frost mass growth rate was reduced between 16% and 26% at the ambient temperature from $-2.0\text{ }^{\circ}\text{C}$ to $+5.5\text{ }^{\circ}\text{C}$ for the coated evaporator compared to the mass growth rate of the uncoated one.

2. Materials and Methods

2.1. Materials

Al-based alloy specimens (6.1 wt% Zn, 2.9 wt% Mg, 2.0 wt% Cu, 0.5 wt% Fe, 0.4 wt% Si, 0.3 wt% Mn, 0.28 wt% Cr, 0.2 wt% Ti, with balance being Al) with dimensions of $2.00\text{ cm} \times 1.00\text{ cm} \times 0.01\text{ cm}$, absolute alcohol (99.7%, AR), hydrochloric acid (37%, AR), sodium

hydroxide, hydrofluoric acid (40%, AR), fluorosilane ($\text{C}_{14}\text{H}_{19}\text{F}_{13}\text{O}_3\text{Si}$, 97%, AR), acetone (99.5%, AR), and deionized (D.I.) water.

2.2. Fabrication of the Superhydrophobic Surface

In this paper, superhydrophobic Al surfaces with micro-nano structure were prepared on bare Al fins by chemical etching. The method employed was as follows. First, the Al specimens were ultrasonically cleaned with acetone and ethanol baths to remove oil stains on the surfaces. Second, the samples were dipped in 5.0 wt% NaOH aqueous solution for 2 min to remove the oxide layer. Third, the specimens were exposed to etching by immersing them in a mixture of D.I. water, hydrochloric acid, and hydrofluoric acid for 18 min. Fourth, a 30 min surface modification with fluorosilane was performed. Finally, the specimens were put into an oven at 120 °C to solidify the fluoride on their surface. To obtain a stable superhydrophobic Al surface, the last step needed to be repeated three times.

The hydrophobicity of the surface was evaluated by measuring the contact angles (CA) using a contact-angle-measuring instrument (XG-CAM). In order to reduce the error caused by uneven surface etching, the front and back of the specimens were divided into four equal parts, and the average CA value at each centroid was taken as the measurement result of the specimen. In order to reduce the influence of droplet gravity on the measurement results, the droplet volume was limited to 5 mL.

2.3. Experimental Apparatus

Figure 1 illustrates the structure of the experimental setup, consisting of a wet air supply and conditioning system, a semiconductor refrigeration installation and a data acquisition device. The wet air supply and conditioning system enables one to adjust the relative humidity of the surrounding air from 43% to 92% and the air flow rate from 1.1 m/s to 1.3 m/s, and it is composed of a centrifugal fan and a humidifier. The semiconductor refrigeration system is made up of a circulating water pump, a water tank, a cold light source, a semiconductor refrigeration table and a thin-film temperature transducer, which can provide a variable low-temperature environment from 0 °C to −35 °C. The data acquisition system is composed of a charge coupled device camera (CCD), a temperature and humidity data logger and a PC. This system can collect the temperature and humidity data from the experimental platform and record the frosting process on the surface of the experimental specimens. Table 2 summarizes the measuring instruments and their errors.

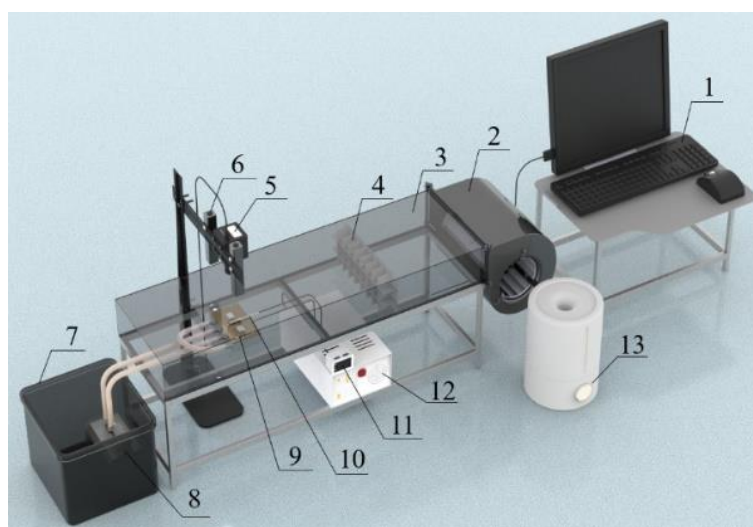


Figure 1. Schematic diagram of the experimental apparatus used in this work. 1. PC. 2. Centrifugal fan. 3. Transparent acrylic air duct. 4. Airflow straightener. 5. Camera. 6. Cold light source. 7. Water tank. 8. Circulating water pump. 9. Semiconductor refrigeration table. 10. Thin-film temperature transducer. 11. Temperature and humidity data logger. 12. Power supply. 13. Humidifier.

Table 2. Measuring accuracies of measurement instruments.







Equipment	Measure Target	Producer	Model	Margin of Error/Precision
Wind speed recorder	Wind speed	HOBO	WFWZY-1	5% \pm 0.05 m/s
Thin-film temperature transducer	Temperature of Al surface	TZW	T106	\pm 0.1 °C
Temperature and humidity data logger	Temperature and RH of the environment	HOBO	MX1101	0.21 °C \pm 2%

3. Results and Discussions

3.1. Characterization of Superhydrophobic Surface

In order to clarify the effect of chemical etching on the CA and hydrophobic properties of the surfaces, the bare Al specimen, the specimen after cleaning, the specimen after oxide layer removal, the specimen after etching and the specimens after surface modification with and without etching were numbered in order of 1–6 (see Table 3). The CA of each specimen was measured and the morphology of droplets on the sample surface was recorded. The data are available in Table 3. In this table, “—” means the step was not carried out; “√” means the step was carried out.

Table 3. The CA and the morphology of the droplets on each specimen.

No.	Cleaning	Removal of Oxide Layer	Etching	Modification	CA	Droplet Morphology
1	—	—	—	—	84.69°	
2	√	—	—	—	85.07°	
3	√	√	—	—	78.17°	
4	√	√	√	—	8.4°	
5	√	√	—	√	105.4°	
6	√	√	√	√	158.3°	

From the measured CA value and the droplet morphology of No. 6, it could be concluded that the chemical etching method used in this study allowed one to successfully prepare a superhydrophobic Al surface with a CA of 158.3°. In addition, after cleaning and removing the oxide layer, the CA of the surface changed little and was still hydrophilic. However, the CA dropped sharply to 8.4° and showed superhydrophilicity after etching. Compared with No. 5 and No. 6, it was found that the CA of the etched surface was rapidly increased to 158.3° after modification, while that of the modified surface without etching was 105.4°. This indicated that, even after surface modification, the construction of the micro-nano structure was essential in the preparation of a superhydrophobic surface.

In order to elucidate the reason for why the surface after etching was superhydrophilic, while etching and modification caused the superhydrophobic properties, specimens 4 and 6 were scanned with an electron microscope to observe any changes in their surface microstructure. Figure 2 shows the surface scanning electron microscope (SEM) images of these two specimens. From Figure 2a, a regular stepped structure with a micro-nano size was highlighted on the surface after etching. This stepped structure formed numerous interlaced micro-nano pores. As a result, the droplets in contact with the etched surface penetrated into the pores and spread over the surface of the specimen. This explained why the surface was superhydrophilic after etching. It is also evident from Figure 2b that a layer of a cotton-flocculent low-chemical energy substance uniformly adhered to the step structure of the modified specimen surface. That is because the superhydrophilicity of the specimen surface made the modified solution enter the micro-nano pores of the specimen

surface after etching. After thermal curing, fluorosilane was retained by the pores, leading to the superhydrophobic property of the surface.

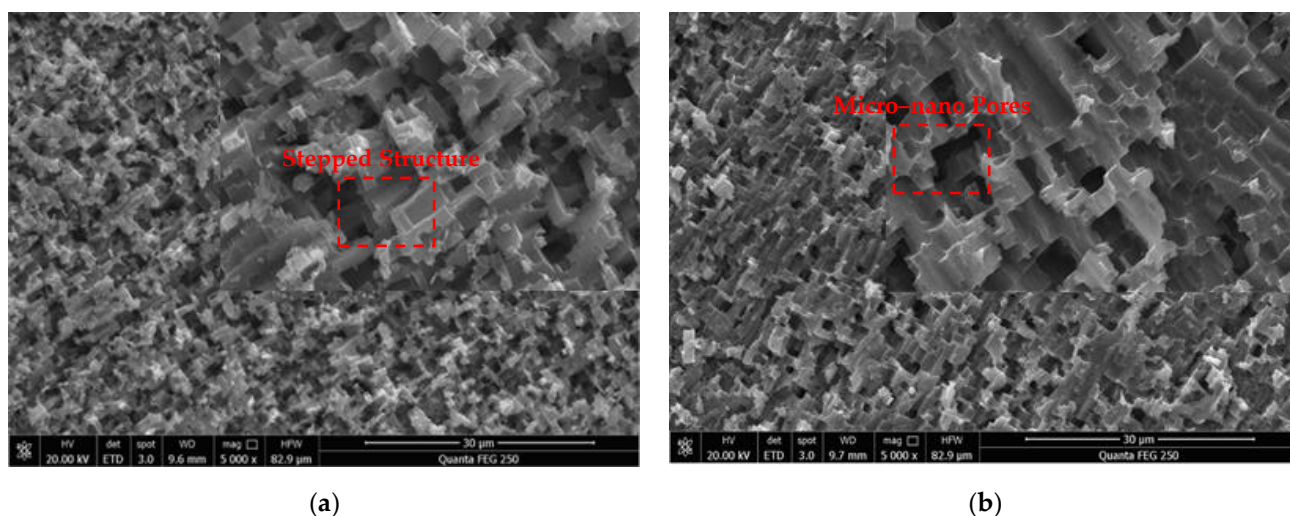


Figure 2. Surface SEM image of (a) etched and (b) modified specimens.

The EDS mapping of the prepared superhydrophobic specimen was also performed to determine the composition and content of each element in the superhydrophobic material. The results of the full-spectrum analysis are shown in Table 4. In addition, Figure 3 shows the surface composition diagram detected by EDS mapping.

Table 4. Element composition on the surface of a superhydrophobic specimen.

Element	Percentage by Weight	Percentage by Weight Sigma	Atomic Percent Ratio
C K	1.87	0.0017	4.07
O K	1.09	0.0029	1.79
F K	0.07	0.0003	0.10
Al K	96.88	0.9561	93.96
Si K	0.08	0.0003	0.08
Overall Amount	100.00	—	100.00

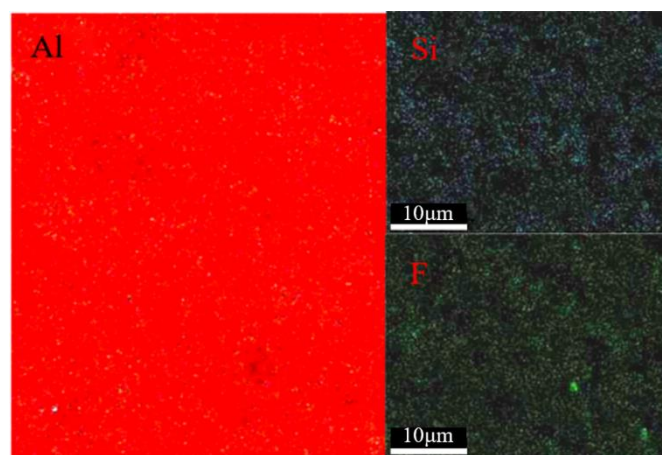


Figure 3. EDS mapping of elements on the superhydrophobic specimen.

Based on Table 3, the prepared superhydrophobic specimen contained only five elements: C, O, F, Al, and Si. Their atomic concentrations changed in descending order

as follows: $\text{Al} > \text{C} > \text{O} > \text{F} > \text{Si}$, where C, O, F, and Si elements were obtained in the modification solution. According to Figure 3, the homogeneous distribution of F and Si on the surface of the specimen indicated that the low-chemical-energy substances were uniformly attached to the surface of the specimen, endowing the Al surface after chemical etching with the superhydrophobic property.

3.2. Anticondensation Characteristic of the Superhydrophobic Surface

The condensation process of water vapor in moist air on the cold surface is the basic stage of condensation and frosting. Thus, exploring the condensation characteristic of a superhydrophobic surface would help us to gain insight into the frost-suppression mechanism of the superhydrophobic surface. The condensation experiments of the bare Al surface and the superhydrophobic Al surface were therefore carried out using the experimental platform mentioned in Section 2.3. The relative humidity of the experimental environment was 70% and the temperature was 11 °C. Figure 4 displays the condensation state of droplets on the two surfaces after 25 min of exposure to the temperature of −1 °C. It could be seen from the figure that the condensed droplets spread on the cold bare Al surface, and the size of a single droplet was large, while the contact area between the droplets on the superhydrophobic Al surface was small and the droplets had a spherical shape.

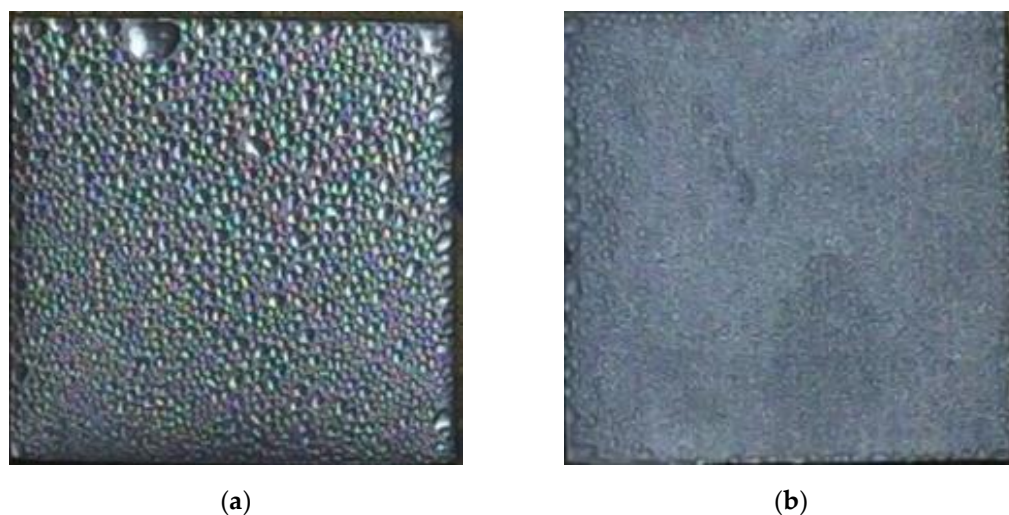


Figure 4. (a) Condensation of droplets on the bare Al surface at −1 °C; (b) Condensation of droplets on the superhydrophobic Al surface at −1 °C.

In order to make the cold surface undergo droplet condensation without the condensation of moist air, the temperature of the surface should not be too low. In this experiment, the cold surface temperature was adjusted to 0 °C, −1 °C, −2 °C and −3 °C, to investigate the condensation characteristic of the superhydrophobic surface. The amount of condensed water on the two surfaces was measured every 5 min to obtain the relationship between the amount of condensed water and time at different cold surface temperatures and the result are plotted in Figure 5.

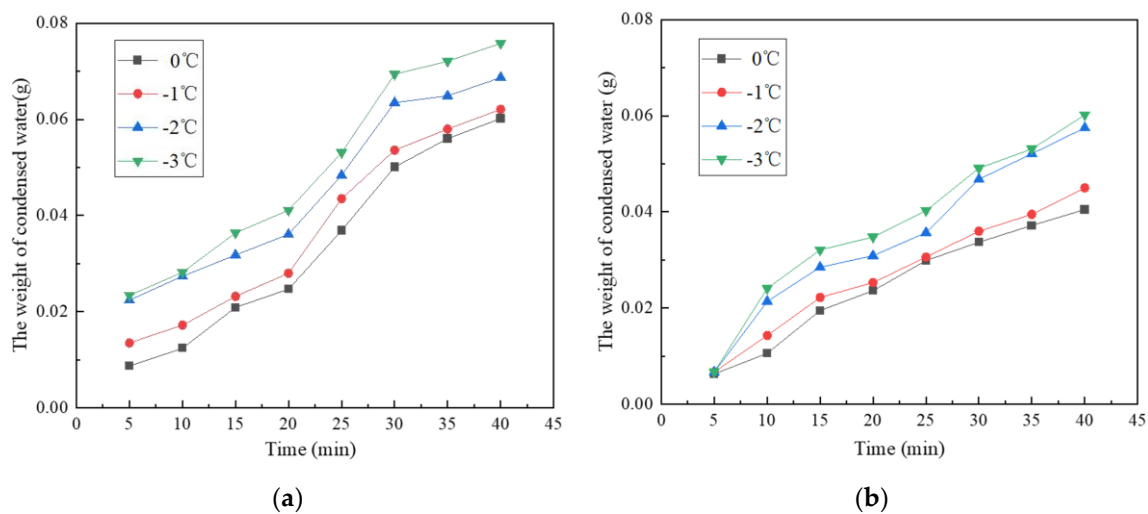


Figure 5. Weight of droplets at different temperatures (a) on the bare Al surface; (b) on the superhydrophobic Al surface.

The data revealed that the amount of condensed water on both surfaces increased with the decrease in temperature. At any time, the condensation water on the superhydrophobic Al surface was less than that on the bare Al surface at the same temperature. According to linear fitting, the average growth rate of droplet condensation on the bare Al surface was 0.00157 g/min, while that on the superhydrophobic surface was 0.00119 g/min. It could be concluded that the superhydrophobic Al surface exhibited better anticondensation properties than the bare Al surface. In addition, as shown in Figure 5, a slag emerged within 20–25 min of the frost growth on the superhydrophobic surface. This was because the anticondensation effect of the superhydrophobic surface in the early frosting stage made the frosting slow during this period.

The anticondensation properties of superhydrophobic surfaces can be explained by the unique condensation nucleation characteristics of droplets.

On the one hand, the droplet has a large nucleation energy barrier on a superhydrophobic surface. According to the theory of phase transformation kinetics, the water vapor in the wet air will agglomerate and droplets will nucleate on the cold surface under a certain degree of undercooling. The surface free energies of liquid-vapor, solid-liquid and solid-vapor are assumed to be σ_{LV} , σ_{SL} and σ_{SV} , respectively. The areas of liquid-vapor, solid-liquid and solid-vapor interfaces are referred to as A_{SV} , A_{SL} and A_{LV} . In turn, V is the volume and r is the radius of the liquid nucleus.

When liquid nuclei are formed, the Gibbs free energy changes ΔG are expressed as:

$$\Delta G = \Delta G_V V + \sigma_{LV} A_{LV} + (\sigma_{SL} - \sigma_{SV}) A_{SL} \quad (1)$$

The surface free energies of liquid-vapor, solid-liquid and solid-vapor interface have the following relationship with the CA (θ), which is the so-called Young's equation:

$$\sigma_{SV} - \sigma_{SL} = \sigma_{LV} \cos \theta \quad (2)$$

The change of free energy is the largest when the critical liquid core is formed. The critical radius r_c of the liquid core can be found as [35]:

$$r_c = -\frac{2\sigma_{LV}}{\Delta G_V} \quad (3)$$

The liquid nucleus formed on the plane is a spherical crown. The areas of liquid-vapor, solid-liquid, solid-vapor interfaces and the volume of the liquid nucleus are, respectively:

$$A_{LV} = 2\pi r^2(1 - \cos \theta) \quad (4)$$

$$A_{SV} = A_{SL} = \pi r^2 \sin^2 \theta \quad (5)$$

$$V = \frac{1}{3}\pi r^3(2 - 3\cos \theta + \cos^3 \theta) \quad (6)$$

Substituting Formulae (2)–(6) into Formula (1), the nuclear energy barrier ΔG on the plane is found to be:

$$\Delta G = \frac{16\pi\sigma_{LV}^3}{3\Delta G_V^2} \left(\frac{1}{2} - \frac{3}{4}\cos \theta + \frac{1}{4}\cos^3 \theta \right) \quad (7)$$

Hence, the condensed nuclear barrier reduction factor $f(\theta)$ can be defined as:

$$f(\theta) = \left(\frac{1}{2} - \frac{3}{4}\cos \theta + \frac{1}{4}\cos^3 \theta \right) \quad (8)$$

The reduction coefficient of condensed nuclear energy barrier $f(\theta)$ represents the induction effect of a solid surface on condensed nucleation. The smaller $f(\theta)$ is, the smaller the condensed nuclear energy barrier is. For a superhydrophobic surface, the value of CA is large and that of $f(\theta)$ is small, so that the condensation nucleation is difficult to form.

On the other hand, the unique coalescence-bounce behavior of droplets caused by the low adhesion of the superhydrophobic surface is also the reason for its anticondensation characteristics. Under the same driving force, condensation nucleation is more likely to occur at the concave surface structure when the size of the condensation liquid nucleus is smaller than or equal to the size of the superhydrophobic surface structure [35]. Moreover, the liquid nucleus formed at the concave surface may form Wenzel droplets after growing up. However, the Wenzel state droplets have high adhesion, which deteriorates the superhydrophobic performance. Therefore, the transformation of Wenzel state droplets into Cassie droplets is the key to maintaining the superhydrophobic performance of the superhydrophobic surface during the condensation process. The adjacent droplets continue to merge with their growth, and the total surface area decreases after the droplet coalescence, thereby leading to a release of some surface energy. The surface adhesion of the superhydrophobic surface is very low, and the energy released by droplet coalescence can overcome the surface adhesion work, which makes the droplet experience the transformation from the Wenzel state into the Cassie state. However, the surface adhesion of the bare Al surface is high, and the surface energy released by droplet coalescence is insufficient to reduce the surface adhesion work. Hence, the merged droplets remain in a Wenzel state. If there is still a residual energy after overcoming the surface adhesion work, it will be transformed into the kinetic energy of the merged droplet. At this time, the droplet can spontaneously bounce off the surface, thus effectively reducing the droplet coverage rate. Figure 6 depicts the coalescence-bounce behavior of droplets on the superhydrophobic surface.

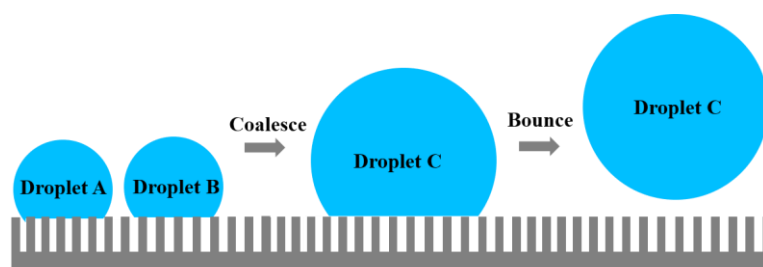


Figure 6. Coalescence–bounce behavior of droplets on the superhydrophobic surface.

3.3. Antifreezing Characteristic of the Superhydrophobic Surface

Frost crystals are always formed first on a frozen droplet, so the moment that the droplet freezes matches the onset of the growth of the frost layer. If the freezing of the droplets is delayed, the start of frost will also be retarded. Therefore, delaying the freezing of the droplets is important for frost suppression. In this work, an experimental study of the freezing process of droplets was performed on the bare and superhydrophobic Al surface. The relative humidity of the experimental environment was 81% and the temperature was 22 °C. The cold surface temperature was adjusted to −5, −8, −11, −14, −17, and −20 °C in turn. In order to make the cold surface undergo droplet condensation without the condensation of moist air, the temperature of the surface should not be too low. In this experiment, the cold surface temperature was adjusted to 0 °C, −1 °C, −2 °C and −3 °C, to investigate the condensation characteristic of the superhydrophobic surface. In particular, the freezing time of the first droplet on the cold surface was taken as the start freezing time and the freezing time of all droplets on the surface was considered the complete freezing time. Figure 7 depicts the times measured for the two surfaces at different temperatures, enabling one to establish the moments at which droplets started and finished freezing.

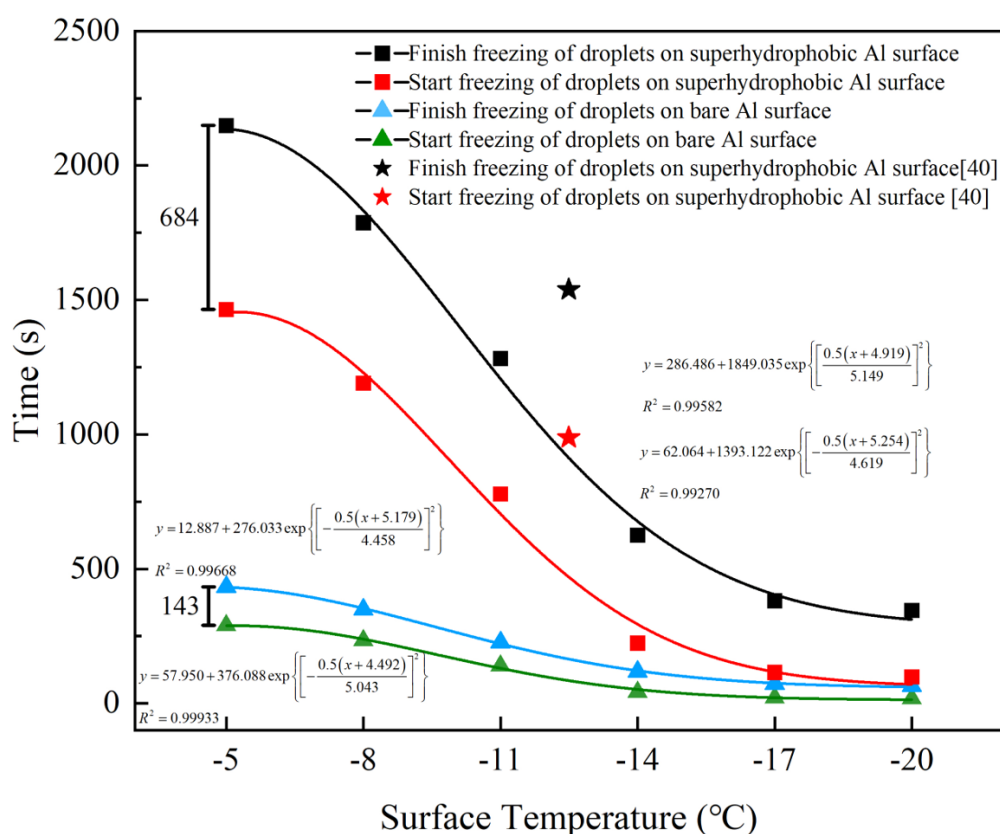


Figure 7. Initial and final freezing times of droplets on the two surfaces at different temperatures.

At −5 °C, the droplets on the bare Al surface started to freeze at 290 s and finished freezing at 433 s. However, the corresponding times on the superhydrophobic Al surface were 1464 s and 2148 s. Under this condition, the superhydrophobic Al surface took 5.05 times longer to start frosting than the bare Al surface and the freezing was 4.78 times slower than on the bare Al surface. As the cold surface temperature decreased, the freezing times for droplets on both surfaces decreased, as did the time required for the entire frosting process. At −20 °C, the superhydrophobic Al surface started to freeze in 98 s, which was also 80 s slower than the bare Al surface. In general, the average freezing time of droplets on the superhydrophobic Al surface was 5.19 times longer than on the bare Al surface at

various cold surface temperatures. From the results discussed above, one could conclude that superhydrophobic surfaces had good freezing resistance.

The reason for why the superhydrophobic surface exhibits this antifreezing characteristic is that the thermal resistance of droplets on this kind of surfaces is high. Therefore, the next step was to analyze the thermal conductivity during freezing of droplets on the superhydrophobic surface. It is known that the contact surface between the droplet and the superhydrophobic surface is a composite solid-liquid-gas interface and the droplet on the superhydrophobic surface is in Cassie-Baxter state [35]. Figure 8 illustrates the Cassie-Baxter model of a condensed droplet and the schematic diagram of the micro-nano structure of the superhydrophobic surface. The length, width and height of individual papillae of the micro-nano structure are assumed to be a , a and b , respectively, and the spacing between adjacent papillae is c . The thermal conductivity of air λ_a is $0.023 \text{ W}/(\text{m}\cdot\text{K})$; the thermal conductivity of Al λ_n is $273 \text{ W}/(\text{m}\cdot\text{K})$.

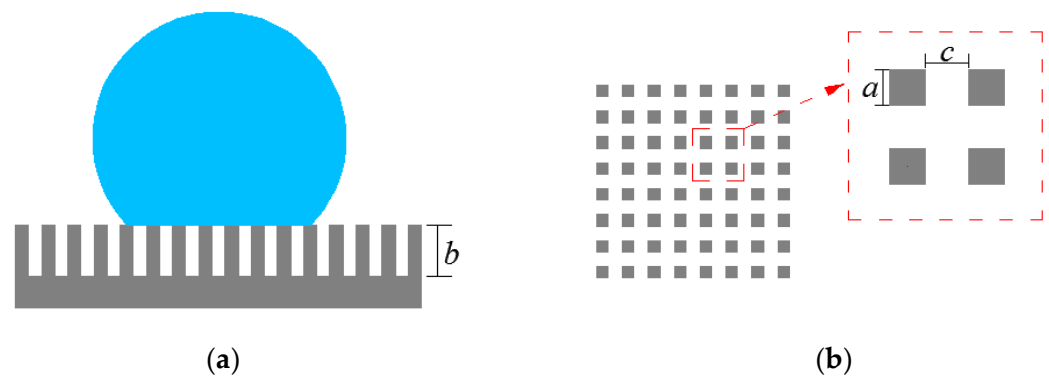


Figure 8. (a) The Cassie-Baxter model of a condensed droplet; (b) Schematic diagram of a surface micro-nano structure.

The thermal resistance of air conductivity R_a is:

$$R_a = \frac{b}{A_a \lambda_a} \quad (9)$$

In turn, the thermal resistance of a single papilla structure R_n is defined as:

$$R_n = \frac{b}{A_n \lambda_n} \quad (10)$$

The relationship between R_a and R_n gives a parallel thermal resistance, so the total thermal resistance R_c of the surface micro-nano structure is:

$$R_c = \frac{1}{\frac{1}{R_a} + \frac{1}{R_n}} \quad (11)$$

The ratio of the surface micro-nano structure to the area of the trapped air region is $a^2 : (c^2 + 2ac)$, so that A_a and A_n can be expressed as:

$$A_a = \frac{c^2 + 2ac}{a^2 + c^2 + 2ac} \pi r^2 \sin^2 \theta \quad (12)$$

$$A_n = \frac{a^2}{a^2 + c^2 + 2ac} \pi r^2 \sin^2 \theta \quad (13)$$

Substitute Equations (9), (10), (12) and (13) into Equation (11) to obtain the total thermal conductivity thermal resistance:

$$R_c = \frac{b}{\pi r^2 \sin^2 \theta} \cdot \frac{1}{\lambda_a + (\lambda_n - \lambda_a) \left(\frac{a}{a+c} \right)^2} \quad (14)$$

In this formula, $\frac{a}{a+c}$ approximately represents the ratio of a solid-liquid contact area to the total contact area of the micro-nano structure. It is assumed that the value of CA of the surface is 160° and the radius of the droplet on the surface is 0.1 mm. Figure 9 depicts the variation in R_c with $\frac{a}{a+c}$ at the heights of the micro-nano structure of 0.1 μm and 0.5 μm .

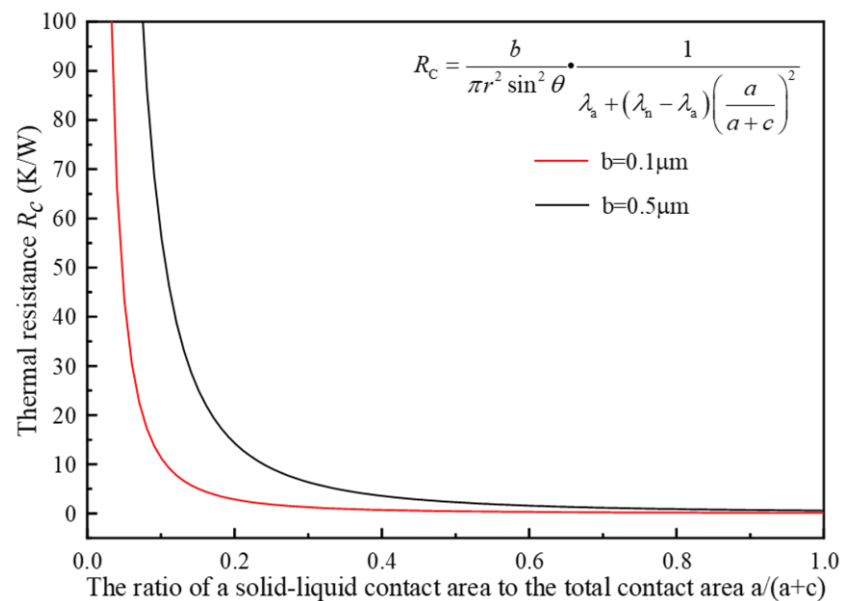


Figure 9. The relationship between the thermal resistance of micro-nano structures on the superhydrophobic surface and the percentage of a solid-liquid contact surface.

The R_c value at $b = 0.1 \mu\text{m}$ and $\frac{a}{a+c} = 0.1$ was found to be 11.57 K/W, decreasing to 0.17 K/W (about 68 times lower) at $b = 0.1 \mu\text{m}$ and $\frac{a}{a+c} = 0.9$. That was due to the fact that as $\frac{a}{a+c}$ decreased, the trapped air area increased, and the thermal resistance also increased. Therefore, droplet freezing could be effectively inhibited by increasing the area of intercepted air under the Cassie-Baxter wetting plot. On the other hand, the thermal resistance R_c increased by about 5.4 times (from 11.57 to 62.17 K/W) when b rose from 0.1 to 0.5. Thus, it could be concluded that increasing the height of the micro-nano structure at the same percentage of the trapped air area enabled one to also slow down the freezing rate of the droplets.

3.4. Antifreezing Test of the Superhydrophobic Surface

To advance the application of superhydrophobic surfaces at the heat exchanger scale, vertical fin bare and superhydrophobic Al bases (hereafter referred to as the bare Al base and the superhydrophobic Al base), both simulating the distribution of actual heat exchanger fins, were afterwards prepared in this work. The shapes of the Al bases are shown in Figure 10. Experimental studies were carried out to elucidate the frost-suppression and melting effects for these bases. During experiments, the ambient temperature was 7°C and the relative humidity was 37%. The temperature of the cold surface was adjusted to -18°C in order to create a uniform needlelike layer of frost on each fin, considering that the refrigeration table provided cooling to several fins. The frosting on both surfaces is illustrated in Figure 10, and the change in the weight of the frost layers within 60 min of frosting is shown in Figure 11.

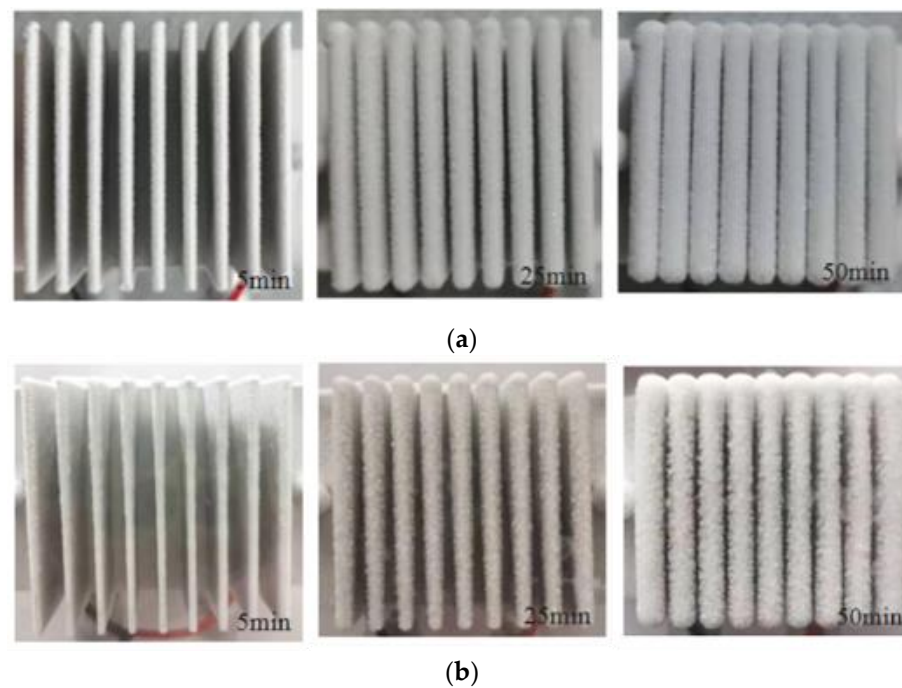


Figure 10. Frosting process on (a) bare and (b) superhydrophobic Al-based surfaces after 5 min, 25 min and 50 min.

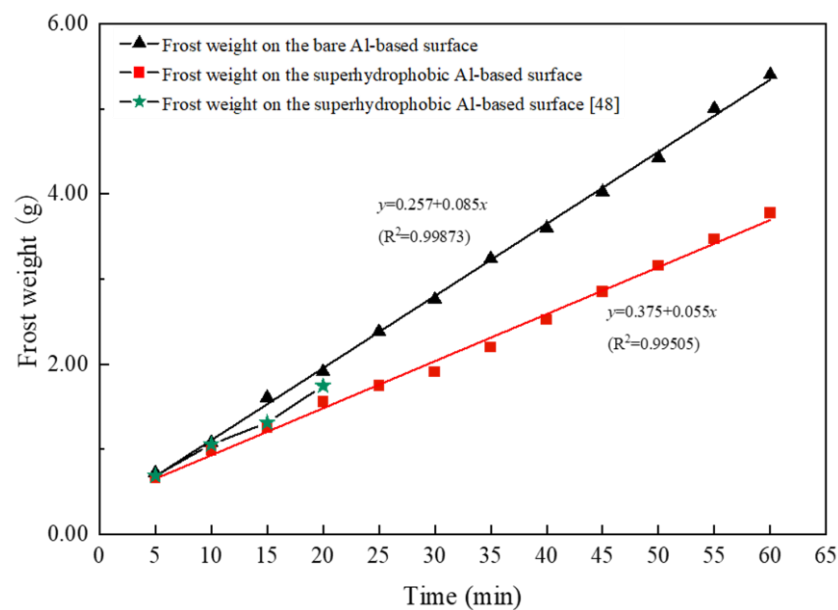


Figure 11. Variation of frost layer weight with time.

As can be seen from Figure 11, frost crystals have been formed on both Al-based surfaces by 5 min after the start of frosting. The amounts of frosting on the superhydrophobic and bare Al-based surfaces were 0.6588 g and 0.7218 g, respectively. After 25 min of frosting, the frost layers entered the full development period and widely appeared on both surfaces. Thus, the weights of frost on the superhydrophobic and bare Al-based surfaces were 1.746 g and 2.3824 g, respectively. The quantity of frost on the superhydrophobic Al-based surface was only 73.29% of that on the bare Al-based surface, which indicated that the superhydrophobic surface had an excellent frost-suppression property in the early stage of frosting. By 50 min of the frosting process, the frost weight on the superhydrophobic Al-based surface was still 71.36% of that of the bare Al-based surface. According to linear

fitting, the average growth rate of frost weight was 0.08481 g/min for the bare Al-based surface and 0.05529 g/min for the superhydrophobic Al-based surface. And the experimental data in this paper are roughly consistent with the experimental data of Jing [48]. One could thereby conclude that the superhydrophobic Al-based surface was endowed with a good frost-suppression effect during the whole frosting process.

After 1 h of frosting, the refrigeration system and the air supply system were switched off and the frost layers on both Al-based surfaces were allowed to melt in an outdoor environment (temperature of 7 °C, relative humidity of 37%, and wind speed of 1.0 m/s). The melting details of the frost layers on both Al-based surfaces are summarized in Figure 12, including the time taken for the frost layer to melt completely.

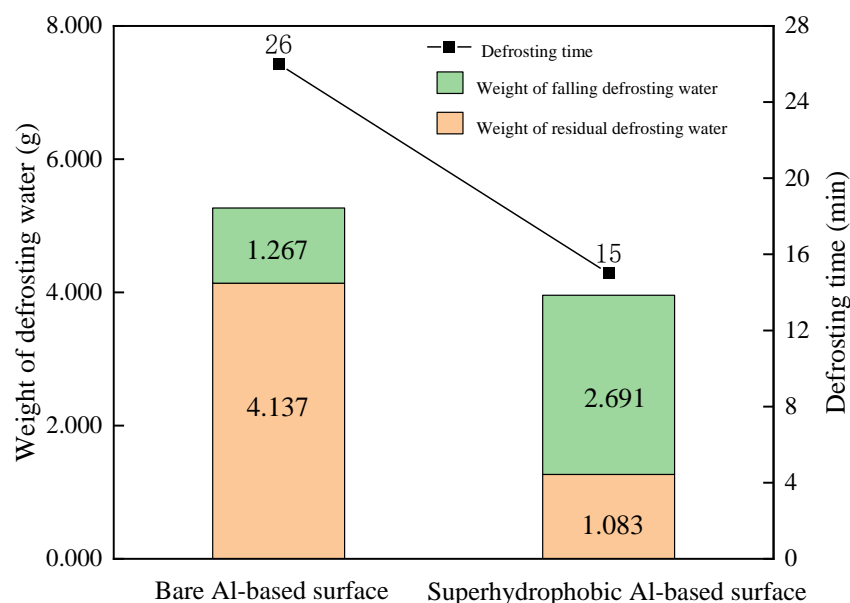


Figure 12. Weight of frost, residence position of defrosting water and defrosting time on two surfaces.

Moreover, liquid films with thicknesses of 1.5 to 4.2 mm were collected on the bottom of the bare Al-based surface and abundant droplets adhered to the vertical fins after defrosting. However, the superhydrophobic Al-based surface had the little droplet retention. As could be seen from Figure 12, 1.267 g of defrosted water was dropped from the bare Al-based surface and 4.137 g of water remained on the surface. In turn, the superhydrophobic Al-based surface lost 2.691 g of defrost water and retained 1.083 g of water. In other words, 76.56% of water remained on the bare Al-based surface after defrosting against 28.70% on the superhydrophobic Al-based surface. In addition, it took 25 min for the frost layer to melt completely on the Al-based surface, while the superhydrophobic Al-based surface took 16 min, which was only 64% of the bare Al-based surface. According to the experimental results, it could be inferred that the application of superhydrophobic technology is promising for reducing the frost melting time and inhibiting secondary frost formation.

4. Conclusions

From the technical route of superhydrophobic anti-frost technology, a superhydrophobic Al surface was prepared by chemical etching. A visual experimental platform was built to study the anticondensation and antifreezing properties of this surface, and the experimental results were analyzed by applying the theoretical means. Finally, a superhydrophobic Al-based surface simulating the distribution of actual heat exchanger fins was prepared, and its frost-suppression performance was experimentally studied. Based on the findings of this work, the following conclusions can be drawn: (1) The superhydrophobic Al surface with a CA value of 158.3° was prepared by chemical etching. In addition, the etching and modification processes were shown to be crucial for the prepa-

ration of such kinds of surfaces. (2) The anticondensation and antifreezing characteristics of superhydrophobic surfaces were found to be the key reasons for the frost-suppression characteristics of superhydrophobic surfaces. (3) The superhydrophobic Al-based surface was able to inhibit frosting and accelerate defrosting.

The ability to promote the application of superhydrophobic frost-suppression technology was demonstrated with the example of a superhydrophobic heat exchanger. Moreover, the antifrosting effect of superhydrophobic heat exchangers will be within the scope of the forthcoming study. Therefore, the proposed method for the preparation of metal-based superhydrophobic surfaces with a frost-suppression mechanism provides a theoretical and experimental basis for the practical use of superhydrophobic technology in the outdoor heat exchanger surfaces of ASHPs.

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Nomenclature

ASHP	Air source heat pump
Al	Aluminum
CA	Contact angle
SEM	Scanning electron microscope
ΔG	Gibbs free energy change
ΔG_V	Gibbs free energy of unit volume liquid nuclues
σ_{LV}	Surface free energy of liquid–vapor
σ_{SL}	Surface free energy of solid–liquid
σ_{SV}	Surface free energy of solid–vapor
A_{SV}	Area of liquid–vapor
A_{SL}	Area of solid–liquid
A_{LV}	Area of solid–vapor
r	Radius of the liquid nucleus
r_c	Critical radius
$f(\theta)$	Reduction coefficient of condensed nuclear energy barrier
a	Length/ Width of individual papillae of the micro–nano structure
b	Height of individual papillae of the micro–nano structure
c	Spacing between adjacent papillae
λ_a	Thermal conductivity of air
λ_n	Thermal conductivity of Al
R_a	Thermal resistance of air conductivity
R_n	Thermal resistance of a single papilla structure
R_c	Total thermal resistance of micro–nano structure
V	Volume of the liquid nucleus

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