

## Supplementary Information

**Table S1** Correction of equations used in the FW-DW system, compared to the one used in Dijkgraaf et al. (2019)

Parameter	Equation in Dijkgraaf et al. (2019)	Correction
Energy conversion from MJ to kWh	Energy in kWh = Energy in MJ * $\frac{10^6}{3600 * 24}$	Energy in kWh = Energy in MJ * $\frac{10^3}{3600}$
Methane yield in anaerobic digestion unit	$y_m = m_{COD}^{HPS} * y_{m\ practical}$  $y_m$ is methane yield (m <sup>3</sup> ), $m_{COD}^{HPS}$ is total COD mass in the HPS(kg), $m_{COD}^{HPS\ to\ AD}$ is total COD mass that goes into ADU (kg), $y_{m\ practical}$ is the practical methane yield per kg COD (m <sup>3</sup> /kg)	$y_m = m_{COD}^{HPS\ to\ AD} * y_{m\ practical}$
Water dilution requirement in HPS	$V_{dil}^{HPS} = \frac{m_x^{HPS}(t) - V^{HPS} * c_{x\ max}^{HPS}}{c_x^{HPS}}$ If $c_x^{HPS}(t) > c_{x\ max}^{HPS}$	$V_{dil}^{NS} = \frac{m_x^{HPS}(t) - V^{HPS} * c_{x\ max}^{HPS}}{c_{x\ max}^{HPS} - c_{x\ GW}^x}$ If $c_x^{HPS}(t) > c_{x\ max}^{HPS}$ and $c_{x\ max}^{HPS} > c_{x\ GW}^{HPS}$
Mass of N or P in HPS after dilution	$m_{x\ flushed} = m_{x0} - \max(V_{N\ dil}, V_{P\ dil}) * c_{x0}$  $m_{x\ flushed}$ is mass of $x$ in the HPS after dilution performed and then flushed (mg), $m_{x0}$ is mass of $x$ before dilution (mg), $V_{N\ dil}$ is Volume of dilution due to N (L), $V_{P\ dil}$ is Volume of dilution due to P (L), $c_{x0}$ is concentration of $x$ before dilution (mg/L), $V_{dil}$ is volme of dilution (L), $V^{HPS}$ is volume of HPS (L), $x$ indicates nitrogen (N) or phosphorus (P)	$m_{x\ flushed} = \frac{m_{x0} + V_{dil} * c_{x\ GW}}{V^{HPS} + V_{dil}} * V^{HPS}$