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An Optimization Model for Water Management under the Dual Constraints of Water Pollution and Water Scarcity in the Fenhe River Basin, North China

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Abstract: Sustainable watershed development suffers from severe challenges, such as water pollution and water scarcity. Based on an analysis of water quality and water utilization in the Fenhe River Basin, an inexact two-stage stochastic programming model with downside-risk aversion was built for optimal water resource allocations for the four primary water use sectors (industry, domestic use, agriculture, and the environment) in the Fenhe River Basin. The model aims to maximize the comprehensive watershed benefits, including water benefits, water costs, water treatment costs, and downside risks. The constraints are water quality, available water resources, and sectoral demands in different hydrological scenarios. The results show that pollutant emissions decrease as risk-aversion levels increase and show the opposite trend in the midstream and downstream areas. The increase in water resource allocation for agriculture and reduction in ecological water indicate that agriculture suffered the greatest water shortage and risk. Improving water recycling and coordinating the transferred water resources increases the comprehensive benefits and reduces sectoral risks. The model effectively manages rational water allocations under dual constraints and provides support for coordinating socio-economic development and environmental protection in the river basin.

Keywords: water resource allocation; pollutant emission; two-stage stochastic programming; downside risk; coordinated development



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1. Introduction

Water resources play a central role in human survival, ecosystem security, and socio-economic development [1–3]. However, with the rapid population expansion and economic development, water shortages and water pollution have become severe problems worldwide [4–6]. Excessive water resource exploitation, inefficient utilization, and increased pollutant emissions have exacerbated the deterioration of water quality and water scarcity [7,8]. Water pollution is the most pressing issue in China, and water scarcity has become a critical constraint for regional socio-economic development [9,10]. High-quality and sustainable development based on improving water quality and rational water resource utilization is a developmental priority in China. Therefore, optimal regional and sectoral water resource allocation for coordinated development between the social economy and the environment are important.

Previous studies reveal that optimal allocation of water resources is one of the most effective resolutions for addressing water pollution, water shortages, and rising water demand [11–16]. Moreover, appropriate policy interventions, such as adjusting the industrial structure and technological progress, are necessary to achieve harmonious economic and societal development [17]. Additionally, there are many uncertainties in the water environment system, including stochasticity of available water resources caused by climate change [18–21], uncertainties regarding plans and policies, and the complexity of

interconnected processes between the social economy and the environment (e.g., water utilization, wastewater treatment, recycling, and water quality). These uncertainties generate enormous challenges for water resources and water quality management.

Several optimization approaches have been developed for water resource allocation and water quality management with uncertainties [22–26]. The inexact two-stage stochastic programming (ITSP) model, which integrates interval-parameter programming (IPP) and two-stage stochastic programming (TSP), has been widely applied to address different forms of multiple uncertainties in water resource allocation and water quality management [27–32]. However, the ITSP model does not consider the variability of the second-stage cost or benefit, which may lead to an unbalanced allocation pattern [33,34]. Previous studies have found that the downside-risk method is an advantageous measure that balances benefits and resource allocation by minimizing the risks for all parties under certain conditions [35]. The downside risk method can be integrated with the programming model with a scenario-based description of problem data and generate a series of solutions that help decision-makers quantitatively evaluate trade-offs between the system's economy and stability [36–38]. Moreover, most studies do not sufficiently consider watersheds with severe water pollution and water scarcity problems, such as the Fenhe River basin in the Shanxi province, northern China. The Fenhe River increasingly suffers from environmental problems, such as severe water pollution and ecological damage, which exacerbates watershed water shortages and cross-sectoral water competition [39]. Thus, an effective approach for dealing with severe environmental problems and water shortages in river basins must be explored.

Therefore, this study aims to develop an ITSP model and introduce downside-risk aversion (ITSDP) to address rational water resource allocation under the dual constraints of water pollution and water shortage in the Fenhe River Basin. The model combines comprehensive water benefits with environmental protection, as the water resource conflict between the environment and production sectors must be resolved, and water resource allocation strategies for different watershed divisions and sectors should be optimized to ensure coordinated development. Figure 1 presents the general framework of the ITSDP model for optimal water management in the Fenhe River Basin with uncertainties for integrating water quality management and water resource allocation. The application of the model could help optimize regional water resource allocation strategies and pollutant emissions under the constraints of water quality and water quantities. Furthermore, the results could help watershed decision-makers establish and improve water-based industrial structures and layouts.

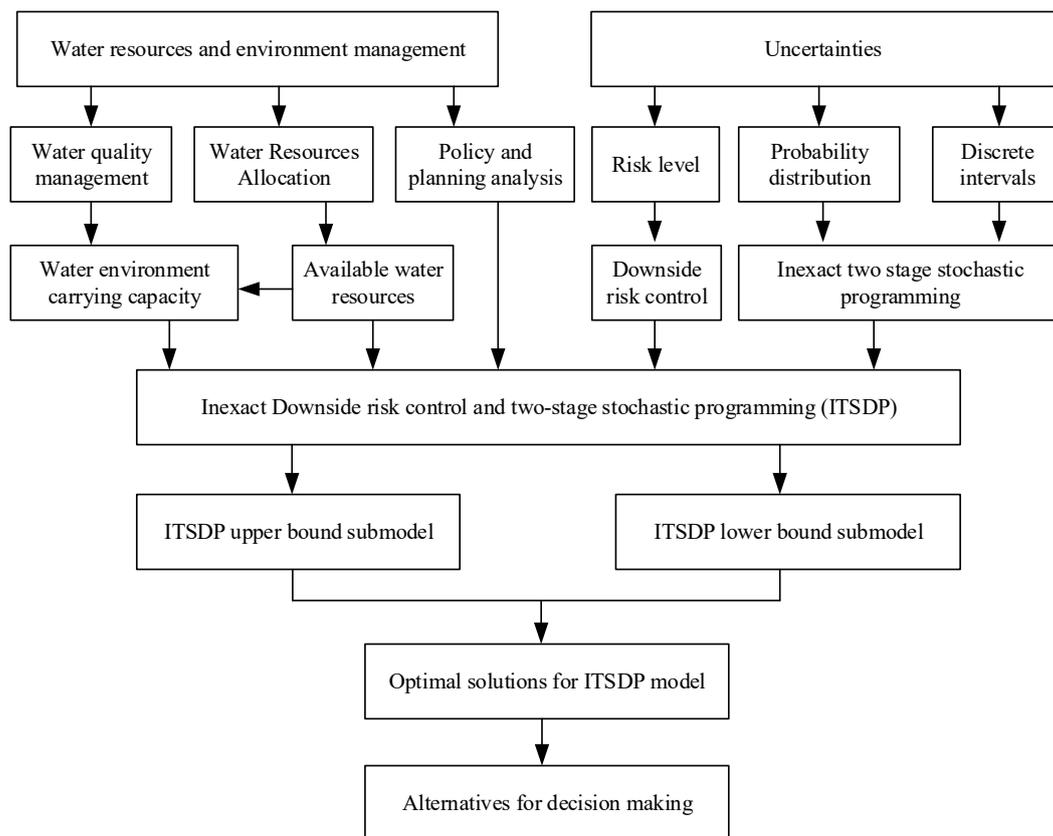


Figure 1. Framework for the inexact downside risk aversion and two-stage programming model.

2. Materials and Methods

2.1. Study Area

The Fenhe River (110°30' E–113°32' E, 35°20' N–39°00' N) is the second largest branch of the Yellow River and the largest river in Shanxi, with a total length of 694 km and a watershed area of approximately 39,471 km² [40]. The Fenhe River Basin has a semi-humid climate, the multi-year (1956–2010) average rainfall of the entire basin is 504.8 mm (with a ten-year decreasing trend), and the water surface evaporation is 900–1200 mm. The total available water resources (from 1956–2010) of the Fenhe River Basin are 2.656 billion m³ [41].

The Fenhe River Basin is highly urbanized and agriculturally developed. The utilization of surface water development is over 70%, and the average utilization of groundwater development reaches 85% [42]. However, the Fenhe River Basin is a relatively severely water-deprived region with a water resource per capita of 378 m³—18% of the national average [40]. The utilization rate of water resources has long exceeded 70%, leading to severe water conflicts between the social economy and the environment [42]. Moreover, due to over-exploitation, uneven allocation, and low utilization efficiency of water resources, excessive pollutant discharge has caused severe environmental problems in the Fenhe River.

In this study, the scope of the Fenhe River Basin was determined by analysis of data from a Digital Elevation Model in the Shanxi province, using the hydrological analysis module of ARCGIS. The river basin is divided into the upstream, midstream, and downstream areas and a total of 16 water environment control units with the corresponding water quality sections (Figure 2).

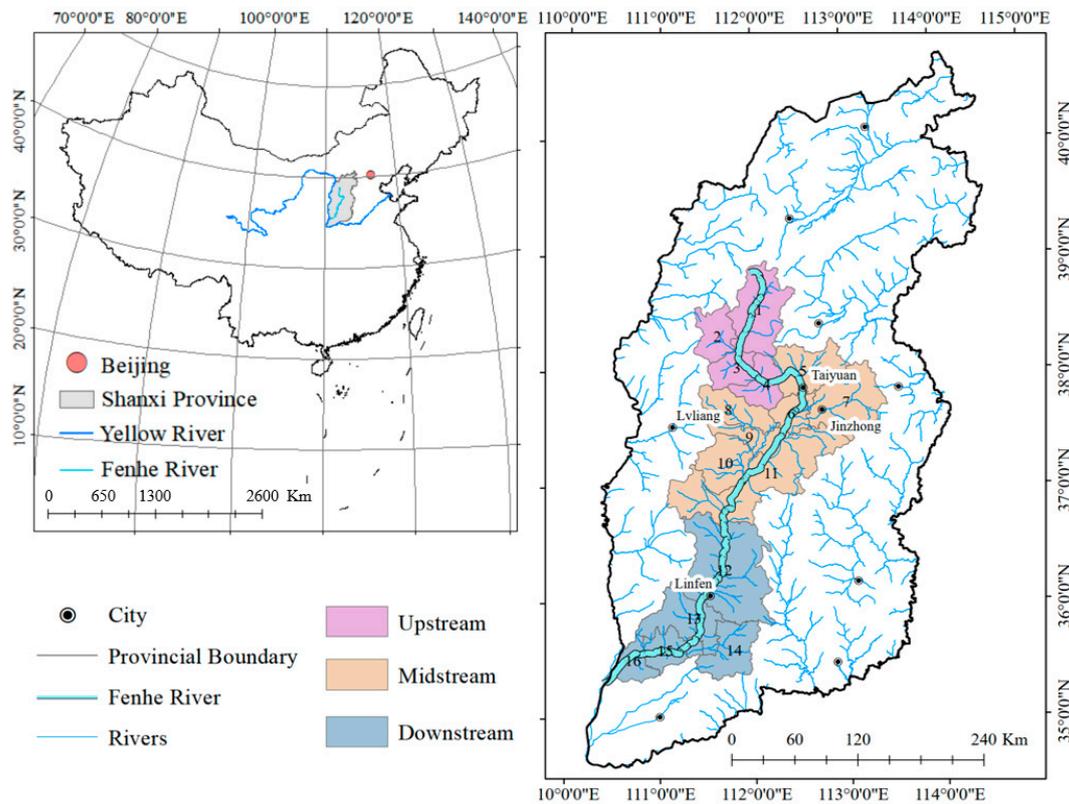


Figure 2. Geographical position and study area of the Fenhe River Basin.

2.2. Model Development

This study considers long-run programming of 15 years and three periods (i.e., 2021–2025, 2026–2030, and 2031–2035). Three hydrological scenarios (low, medium, and high) reflect different water environment carrying capacities and water resources. The ITSDP model for integrating water benefits and downside-risk control under dual constraints of water shortage and pollution in the Fenhe River Basin was formulated as follows:

$$max f^{\pm} = f_1^{\pm} - f_2^{\pm} - f_3^{\pm} - f_4^{\pm} - f_5^{\pm} - f_6^{\pm} \tag{1}$$

where f^{\pm} is the comprehensive benefit of the basin (10^6 million CNY) over the programming periods.

1. Water utilization benefits:

$$f_1^{\pm} = \sum_{i=1}^{16} \sum_{k=1}^4 \sum_{t=1}^3 L_t \cdot UNB_{ikt}^{\pm} \cdot \left(IAW_{ikt}^{\pm} + \sum_{h=1}^3 p_h \cdot RW_{ikth}^{\pm} \right) \tag{2}$$

where i denotes the control unit; k denotes the water sectors ($k = 1$ for industry, $k = 2$ for domestic, $k = 3$ for agriculture, and $k = 4$ for the environment); t denotes different periods; L_t denotes the length of period t , and the values are fixed at 5 years; UNB_{ikt}^{\pm} represents the sectoral water-use benefit (10^4 CNY/ 10^4 m³); represents the pre-allocation of water resources for each sector (10^4 m³/year); and RW_{jkt}^{\pm} represents reused water resources for each sector (10^4 m³/year).

2. Water shortage penalty:

$$f_2^{\pm} = \sum_{i=1}^{16} \sum_{k=1}^4 \sum_{t=1}^3 \sum_{h=1}^3 L_t \cdot p_h \cdot PNB_{ikt}^{\pm} \cdot DW_{ikth}^{\pm} \tag{3}$$

where h denotes hydrological scenarios, p_h denotes the occurrence probability of scenario h , PNB_{jkt}^\pm represents the reduction of net benefit per unit of water resource not delivered (10^4 RMB/ 10^4 m³), and DW_{ikth}^\pm represents the allocation deficit of water resources for each sector (10^4 m³/year).

3. Cost of water supply:

$$f_3^\pm = \sum_{i=1}^{16} \sum_{k=1}^4 \sum_{t=1}^3 L_t \cdot \left(IAW_{ikt}^\pm - \sum_{h=1}^3 p_h \cdot DW_{ikth}^\pm \right) \cdot CW_{ikt}^\pm + \sum_{i=1}^{16} \sum_{k=1}^4 \sum_{t=1}^3 \sum_{h=1}^3 p_h \cdot L_t \cdot RW_{ikth}^\pm \cdot CRW_{ikt}^\pm \quad (4)$$

where CW_{jkt}^\pm represents the cost of the water supplies (10^4 CNY/ 10^4 m³) and CRW_{jkt}^\pm is the cost of reused water (10^4 CNY/ 10^4 m³).

4. Cost of wastewater treatment:

$$f_4^\pm = \sum_{i=1}^{16} \sum_{k=1}^4 \sum_{t=1}^3 L_t \cdot \left(IAW_{ikt}^\pm - \sum_{h=1}^3 p_h \cdot DW_{ikth}^\pm \right) \cdot \alpha_{ikt}^\pm \cdot (CWW_{ikt}^\pm + \zeta_{ikt}^\pm \cdot CRWT_{ikt}^\pm) \quad (5)$$

where CWW_{jkt}^\pm represents the costs of wastewater treatment (10^4 CNY/ 10^4 m³) and $CRWT_{jkt}^\pm$ denotes the costs of wastewater reclamation (10^4 CNY/ 10^4 m³).

5. Cost of ecological water:

$$f_5^\pm = \sum_{i=1}^{16} \sum_{t=1}^3 \sum_{h=1}^3 L_t \cdot p_h \cdot GW_{ith}^\pm \cdot CEW_{it}^\pm \quad (6)$$

where GW_{ith}^\pm is the ecological water (i.e., ecological water is to purify excessive pollutant emission) and CEW_{it}^\pm is the cost of ecological water.

6. Downside risk constraints:

$$f_6^\pm = \omega \cdot \sum_{i=1}^{16} \sum_{k=1}^4 \sum_{t=1}^3 DRisk_{ikt}^\pm \quad (7)$$

where ω represents the risk control level and $DRisk_{ikt}^\pm$ is the sectoral downside risk.

Constraints:

1. Water resource constraints:

$$\sum_{k=1}^4 (IAW_{ijkt}^\pm - DW_{ijkth}^\pm) \leq AWQ_{it}^\pm; \forall i, t, h \quad (8)$$

$$\sum_{i=1}^{16} \sum_{k=1}^4 (IAW_{ikt}^\pm - DW_{ikth}^\pm) + GW_{ith}^\pm \leq TAWQ_t^\pm; \forall t, h \quad (9)$$

$$DIAW_{ikth}^\pm \leq IAW_{ikt}^\pm; \forall i, k, t, h \quad (10)$$

where AWQ_{it}^\pm denotes the available regional water resources (10^4 m³/year).

2. Water sector demand constraints:

$$(IAW_{ikt}^\pm - DW_{ikth}^\pm) + RW_{ikth}^\pm \geq WD_{minikt}^\pm; \forall i, k, t, h \quad (11)$$

$$(IAW_{ikt}^\pm - DW_{ikth}^\pm) + RW_{ikth}^\pm \leq WD_{maxikt}^\pm; \forall i, k, t, h \quad (12)$$

where $WD_{\min ikt}^{\pm}$ represents the minimum water resources requirement and $WD_{\max ikt}^{\pm}$ represents the maximum water resources requirement ($10^4 \text{ m}^3/\text{year}$).

3. Regional wastewater treatment capacity constraints:

$$\sum_{j=1}^3 \left(IAW_{ijkt}^{\pm} - DW_{ijkth}^{\pm} \right) \cdot \alpha_{ikt}^{\pm} \leq ATW_{ikt}^{\pm}, \forall i, t, h, k = 1, 2 \quad (13)$$

where α_{ikt} is the wastewater emission coefficient and ATW_{ikt}^{\pm} represents the wastewater treatment capacity (10^4 tons).

4. Regional wastewater reuse capacity constraints:

$$\left(IAW_{ikt}^{\pm} - DW_{iktth}^{\pm} \right) \cdot \alpha_{ikt}^{\pm} \cdot \zeta_{ikt}^{\pm} \geq \sum_{k=1}^4 RW_{iktth}^{\pm}, \forall i, t, h \quad (14)$$

where ζ_{ikt} is the wastewater reuse rate.

5. Water environment carrying capacity constraints:

$$\sum_{k=1}^3 \sum_{j=1}^3 \left(IAW_{ijkt}^{\pm} - DIAW_{ijkth}^{\pm} \right) \cdot \alpha_{ikt}^{\pm} \cdot \left(1 - \zeta_{ikt}^{\pm} \right) \cdot EC_{krt}^{\pm} \cdot IDR_{krt} \\ - \left(CS_{irt}^{\pm} - C0_{irt}^{\pm} \right) \cdot GW_{ith}^{\pm} \leq ALD_{irtth}^{\pm}, \forall i, r, t, h \quad (15)$$

where r is the controlled water pollutant ($r = 1$ for chemical oxygen demand (COD), $r = 2$ for ammonia nitrogen ($\text{NH}_4\text{-N}$), $r = 3$ for total phosphorus (TP)), EC_{krt}^{\pm} represents the concentration of pollutants after wastewater treatment (mg/L), IDR_{krt} represents the river load ratio of different pollutants, and ALD_{irtth}^{\pm} is the environmental capacity (tons) of different pollutants.

6. Downside risk

$$PRW_{iktth}^{\pm} = L_t \cdot \left\{ \begin{array}{l} UNB_{ikt}^{\pm} \cdot \left(IAW_{ikt}^{\pm} + RW_{iktth}^{\pm} \right) - PNB_{ikt}^{\pm} \cdot DW_{iktth}^{\pm} \\ - \left[\left(IAW_{ikt}^{\pm} - DW_{iktth}^{\pm} \right) \cdot CW_{ikt}^{\pm} + RW_{iktth}^{\pm} \cdot CRW_{ikt}^{\pm} \right] \\ - \left(IAW_{ikt}^{\pm} - DW_{iktth}^{\pm} \right) \cdot \left(\alpha_{ikt}^{\pm} \cdot CWW_{ikt}^{\pm} + \alpha_{ikt}^{\pm} \cdot \zeta_{ikt}^{\pm} \cdot CRWT_{ikt}^{\pm} \right) \end{array} \right\}, \forall i, k, t, h \quad (16)$$

$$Delta_{iktth}^{\pm} = \left\{ \begin{array}{ll} \Omega_{it}^{\pm} - PRW_{iktth}^{\pm}, & PRW_{iktth}^{\pm} < \Omega_{it}^{\pm} \\ 0, & PRW_{iktth}^{\pm} > \Omega_{it}^{\pm} \end{array} \right\}, \forall i, k, t, h \quad (17)$$

$$DRisk_{ikt}^{\pm} = \sum_{h=1}^3 p_h \cdot Delta_{iktth}^{\pm}, \forall i, k, t \quad (18)$$

where PRW_{iktth}^{\pm} represents the actual benefit, Ω_{it}^{\pm} represents the expected regional benefit, $Delta_{iktth}^{\pm}$ represents the positive deviation from the expected benefit, and $DRisk_{ikt}^{\pm}$ represents the downside risk.

The objective is to maximize the comprehensive benefits of the river basin, including the benefits of water resource sectors, water shortage penalties, and the cost of water supply, wastewater treatment, and wastewater reclamation. The constraints are for the relationships between decision values and water quality requirements, including available water resources, environmental water carrying capacity, and downside risks.

Using an interactive algorithm, the ITSDP model can be transformed into two deterministic sub-models that correspond to the lower and upper bounds of the desired objective function value. The DW_{iktth}^{-} , RW_{iktth}^{+} , GW_{ith}^{-} , $DRisk_{ikt}^{-}$ and DW_{iktth}^{+} , RW_{iktth}^{-} , GW_{ith}^{+} , $DRisk_{ikt}^{+}$ sub-models are solved to form the final ITSDP model solution: $[DIAW_{iktth}^{-}, DIAW_{iktth}^{+}]$, $[RW_{iktth}^{-}, RW_{iktth}^{+}]$, $[GW_{ith}^{-}, GW_{ith}^{+}]$, and $[DRisk_{ikt}^{-}, DRisk_{ikt}^{+}]$.

2.3. Datasets

Table 1 lists the available water resources in the upper, middle, and lower reaches of the Fenhe River, including surface water, groundwater, and transferred water from the Yellow River. These were calculated based on regional water resource planning and management policies.

Table 1. Available water resources in the Fenhe River Basin ($10^4 \text{ m}^3/\text{year}$).

Water Resources	Periods	Regions		
		Upstream	Midstream	Downstream
Surface water	t = 1	[22,640, 28,300]	[59,200, 74,000]	[27,840, 34,800]
	t = 2	[22,880, 28,600]	[61,520, 76,900]	[27,840, 34,800]
	t = 3	[23,120, 28,900]	[63,840, 79,800]	[27,840, 34,800]
Groundwater	t = 1	[2560, 3200]	[49,600, 62,000]	[24,600, 30,750]
	t = 2	[2560, 3200]	[47,120, 58,900]	[22,880, 28,600]
	t = 3	[2560, 3200]	[44,640, 55,800]	[21,160, 26,450]
Transferred water	t = 1	[1800, 2250]	[76,800, 96,000]	[54,840, 68,550]
	t = 2	[2400, 3000]	[86,400, 108,000]	[59,920, 74,900]
	t = 3	[3000, 3750]	[96,000, 120,000]	[65,000, 81,250]

Table 2 lists the water environment carrying capacities in the Fenhe River Basin, which were calculated based on hydrological parameters under different scenarios.

Table 2. Water environment carrying capacities in the Fenhe River Basin (tons).

Periods	Pollutants	Regions	Hydrological Scenarios		
			h = 1	h = 2	h = 3
t = 1	r = 1	upstream	1297.46	1996.10	3629.27
		midstream	13,888.68	21,367.20	38,849.45
		downstream	6375.08	9807.82	17,832.40
	r = 2	upstream	90.62	139.42	253.49
		midstream	345.84	532.06	967.38
		downstream	65.81	101.24	184.08
	r = 3	upstream	32.55	50.07	91.04
		midstream	210.06	323.18	587.59
		downstream	57.26	88.09	160.16
t = 2	r = 1	upstream	1297.46	1996.10	3629.27
		midstream	13,390.74	20,601.13	37,456.61
		downstream	4781.31	7355.87	13,374.30
	r = 2	upstream	90.62	139.42	253.49
		midstream	343.55	528.53	960.97
		downstream	49.36	75.93	138.06
	r = 3	upstream	32.55	50.07	91.04
		midstream	207.15	318.70	579.45
		downstream	42.94	66.07	120.12
t = 3	r = 1	upstream	1297.46	1996.10	3629.27
		midstream	10,805.19	16,623.37	29,110.03
		downstream	4781.31	7355.87	9807.82
	r = 2	upstream	90.62	139.42	253.49
		midstream	303.03	466.19	842.50
		downstream	49.36	75.93	101.24
	r = 3	upstream	32.55	50.07	91.04
		midstream	176.33	271.28	486.72
		downstream	42.94	66.07	88.09

3. Results and Discussions

3.1. System Benefits and Risks

In this study, the optimal results were obtained without the downside-risk control constraints for a ω value fixed at 0. Further, values of 5, 15, 30, and 50 were selected to reflect increasing risk control levels and obtain the corresponding optimal results of water resource allocation and pollutant emissions. In this section, we compare and analyze the differences in the system benefits and risks of the Fenhe River Basin under different risk levels.

Figure 3 shows the system benefits of water resource utilization and corresponding risks for different ω values. The figure shows a similar change in benefits and risks. The total benefits are CNY [25.39, 32.76], [25.29, 32.68], [25.18, 32.47], [25.04, 32.15], and [24.92, 31.81] $\times 10^6$ million, and the risks are [0.58, 2.01], [0.51, 1.92], [0.49, 1.90], [0.48, 1.90], and [0.47, 1.90] $\times 10^6$ million for ω of 0, 5, 15, 30, and 50, respectively. Both benefits and risks decrease slightly as the ω values increase, indicating that certain water resources transfer to lower-benefit sectors to meet the stronger risk-control requirement. As the risk control level increases, the model will optimize the water resource allocations for units and sectors based on factors such as water efficiencies, pollutant emission intensities, and water environment carrying capacities.

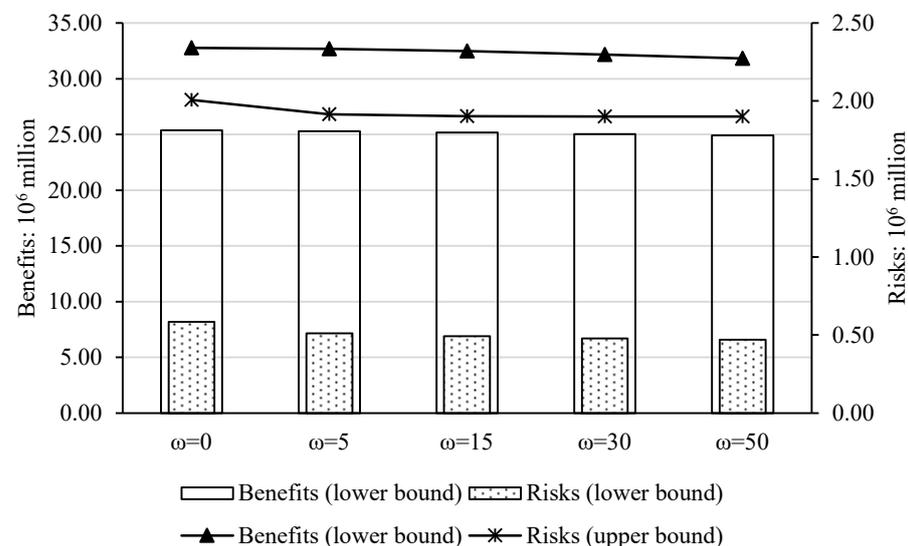


Figure 3. Benefits and risks in the Fenhe River Basin at different risk levels.

Figure 4 shows different changes in sectoral risks. Industry and agriculture risks show a downward trend as risk control levels increase, and the risks are CNY [0.253, 0.725], [0.202, 0.684], [0.202, 0.614], [0.200, 0.596], and [0.199, 0.598] $\times 10^6$ million and CNY [0.139, 0.335], [0.130, 0.332], [0.120, 0.326], [0.113, 0.323], and [0.105, 0.321] $\times 10^6$ million, for values of 0, 5, 15, 30, and 50, respectively. However, domestic risks are CNY [0.192, 0.947], [0.178, 0.900], [0.171, 0.964], [0.165, 1.029], and [0.164, 1.035] $\times 10^6$ million, respectively. The upper bound of the risks gradually increases for values of 5, 15, 30, and 50. These risks correspond to the lower bound of water resources and environmental carrying capacity, and more water resources are allocated to sectors with high benefits and low pollutant emission intensities.

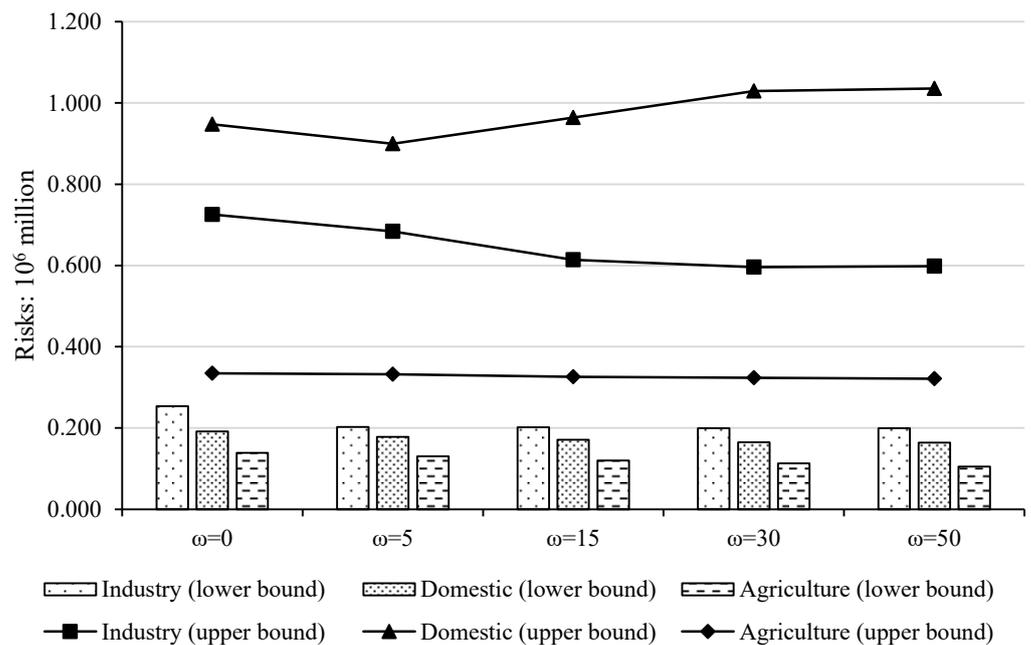


Figure 4. Sectoral risks in the Fenhe River Basin at different risk levels.

Table 3 lists the sectoral risks in different periods and regions. The results show trends consistent with the analysis on total risks in the river basin. For example, in period 3, industry and agriculture risks in the downstream area are CNY [0.253, 0.543], [0.202, 0.543], [0.202, 0.474], [0.200, 0.456], and [0.199, 0.456] × 10⁶ million and CNY [0.041, 0.074], [0.040, 0.074], [0.038, 0.073], [0.036, 0.072], and [0.035, 0.072] × 10⁶ million, showing a downward trend as the ω values increase. Domestic risks show an upward trend for ω values of 5, 15, 30, and 50, and the risks are CNY [0.125, 0.461], [0.119, 0.535], [0.115, 0.580], and [0.115, 0.582]. In period 1, the agriculture risks in the upstream area are CNY [0.001, 0.003], [0.001, 0.002], [0.001, 0.002], [0.001, 0.002], and [0.001, 0.002] × 10⁶ million, and the risks remain unchanged for values of 5, 15, 30, and 50. The industry and domestic risks are zero, indicating that the system’s benefits and risks are balanced. Compared to the other areas, the upstream area has relatively sufficient water resources and environmental carrying capacity. The developed ITSDP model can optimize water resource allocation strategies to meet the highest system benefit under different risk control requirements. Furthermore, the supply of ecological water resources to purify water quality reduces the amount of water available for production and increases risks. The strong water quality constraint plays a decisive role in the optimal allocation of water resources in this study.

Table 3. Sectoral risks in the Fenhe River Basin (CNY 10⁶ million).

Periods	Sectors	Regions	Risk Control Levels				
			ω = 0	ω = 5	ω = 15	ω = 30	ω = 50
t = 1	Industry	upstream	0	0	0	0	0
		midstream	0	0	0	0	0
		downstream	[0, 0.007]	0	0	0	0
	Domestic	upstream	0	0	0	0	0
		midstream	[0.032, 0.045]	[0.031, 0.045]	[0.031, 0.044]	[0.031, 0.045]	[0.031, 0.045]
		downstream	0	0	0	0	0
	Agriculture	upstream	[0.001, 0.003]	[0.001, 0.002]	[0.001, 0.002]	[0.001, 0.002]	[0.001, 0.002]
		midstream	[0.005, 0.027]	[0.005, 0.027]	[0.005, 0.025]	[0.005, 0.025]	[0.005, 0.024]
		downstream	[0.019, 0.046]	[0.018, 0.045]	[0.018, 0.045]	[0.017, 0.045]	[0.015, 0.044]

Table 3. Cont.

Periods	Sectors	Regions	Risk Control Levels				
			$\omega = 0$	$\omega = 5$	$\omega = 15$	$\omega = 30$	$\omega = 50$
t = 2	Industry	upstream	0	0	0	0	0
		midstream	0	0	0	0	0
		downstream	[0, 0.157]	[0, 0.124]	[0, 0.124]	[0, 0.124]	[0, 0.124]
	Domestic	upstream	0	0	0	0	0
		midstream	[0.019, 0.049]	[0.016, 0.048]	[0.016, 0.048]	[0.015, 0.052]	[0.015, 0.052]
		downstream	0	0	0	0	0
	Agriculture	upstream	[0.001, 0.004]	[0.001, 0.004]	[0.001, 0.004]	[0.001, 0.004]	[0.001, 0.004]
		midstream	[0.006, 0.037]	[0.006, 0.038]	[0.006, 0.034]	[0.006, 0.034]	[0.006, 0.033]
		downstream	[0.03, 0.059]	[0.029, 0.059]	[0.029, 0.059]	[0.028, 0.058]	[0.026, 0.058]
t = 3	Industry	upstream	[0, 0.006]	[0,0.005]	[0,0.004]	[0,0.004]	[0,0.006]
		midstream	[0, 0.012]	[0,0.012]	[0,0.012]	[0,0.012]	[0,0.012]
		downstream	[0.253, 0.543]	[0.202, 0.543]	[0.202, 0.474]	[0.200, 0.456]	[0.199, 0.456]
	Domestic	upstream	0	0	0	0	0
		midstream	[0.013, 0.371]	[0.006, 0.345]	[0.006, 0.337]	[0.004, 0.352]	[0.004, 0.356]
		downstream	[0.128, 0.482]	[0.125, 0.461]	[0.119, 0.535]	[0.115, 0.580]	[0.115, 0.582]
	Agriculture	upstream	[0.002, 0.005]	[0.002, 0.005]	[0.002, 0.005]	[0.001, 0.005]	[0.001, 0.005]
		midstream	[0.034, 0.079]	[0.027, 0.078]	[0.02, 0.078]	[0.018, 0.078]	[0.016, 0.078]
		downstream	[0.041, 0.074]	[0.040, 0.074]	[0.038, 0.073]	[0.036, 0.072]	[0.035, 0.072]

3.2. Water Resource Allocation and Pollutant Emissions

In this section, we comprehensively analyzed the pollutant emissions and water resource allocation strategies of the Fenhe River Basin under different risk control levels, to study the key constraints of the sustainable development of the basin. Figures 5–7 show the emissions of the main pollutants (COD, $\text{NH}_4\text{-H}$, and TP) during the study periods. These figures indicate that emissions of the three pollutants gradually increase for scenarios 1, 2, and 3, which are influenced by the increasing water resources and environmental carrying capacities. For example, in period 1, for ω values of 15, the amounts of TP emission Figure 7 are [1303.04, 1879.12], [1779.22, 2084.21], and [2112.36, 2188.52] tons for scenarios 1, 2, and 3, respectively. In periods 2 and 3, the amounts are [1178.63, 1748.45], [1556.89, 1893.39], and [1952.14, 2076.31] tons and [984.26, 1306.73], [1035.78, 1557.28], and [1717.21, 1850.83] tons. These show a downward trend of pollutant emissions over time due to the requirement of water quality improvement. As ω values increase, the stronger risk control constraint leads to the optimization of water resource allocation strategies, and the pollutant emissions show different tendencies. For period 3 and scenario 2, the amounts of COD emissions Figure 5 are [80,355.82, 114,004.60], [80,400.54, 116,705.51], [80,383.72, 121,337.26], [80,177.29, 128,239.97], and [80,097.39, 128,220.25] tons, showing an obvious upward trend for ω values increasing from 0 to 30, and the same as $\text{NH}_4\text{-H}$ and TP. For period 2 and the same scenario, emissions of the three pollutants show slight and different fluctuations. The amounts of COD emissions fluctuate with [118,727.20, 150,165.3], [118,685.06, 150,216.61], and [121,704.1, 149,513.43] tons for ω values of 0, 5, and 15, and gradually increase to [120,761.79, 149,996.61] and [121,912.25, 150,347.08] tons for ω values of 30 and 50. For $\text{NH}_4\text{-H}$, the amounts are [1558.24, 1778.04], [1560.31, 1778.67], [1572.82, 1771.39], [1563.26, 1769.81], and [1559.74, 1763.8] tons, showing a downward trend for ω values of 5, 15, 30, and 50. Unlike the COD and $\text{NH}_4\text{-H}$, the amounts of TP emissions are [1519.19, 1903.4], [1518.64, 1902.73], [1556.89, 1893.39], [1545.2, 1900.39], and [1558.55, 1903.6] tons, showing an upward trend for ω values of 5, 15, 30, and 50. These differences are closely related to regional industrial structures, water resource allocation strategies for sectors, and various pollutant emission intensities. Additionally, Figures 5–7 show more significant changes in period 3, and datasets such as the available water resources for scenario 2 are closer to regional policies and plans; thus, the following analysis would be carried out for period 3, scenario 2.

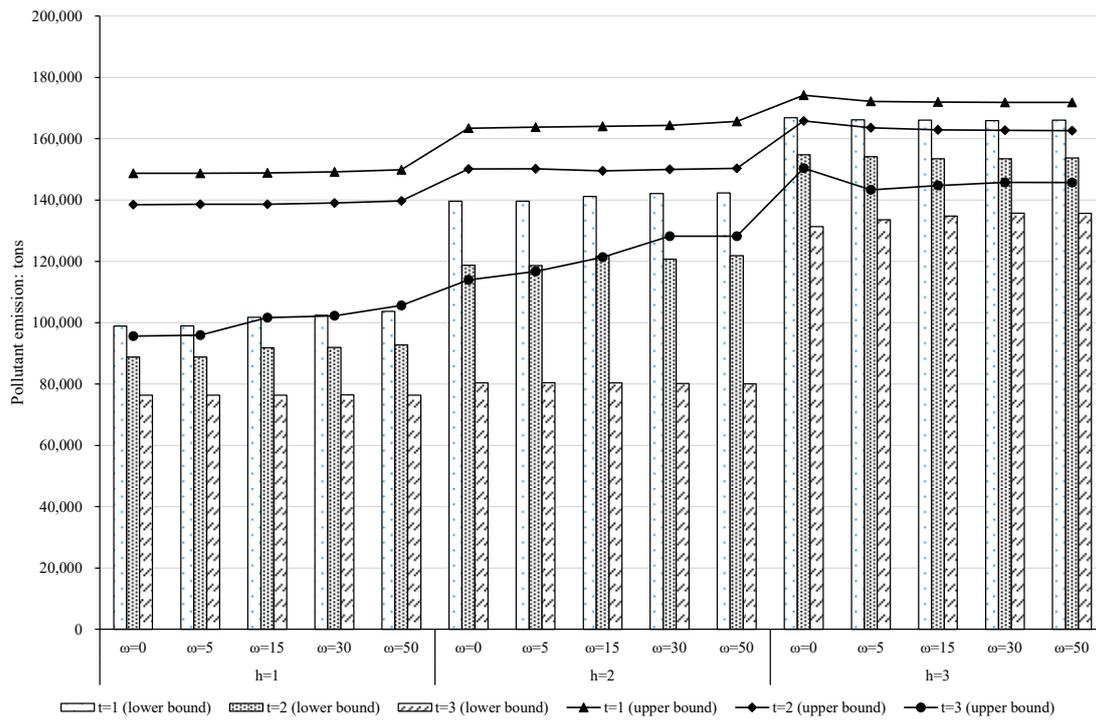


Figure 5. COD emissions in the Fenhe River Basin at different risk levels.

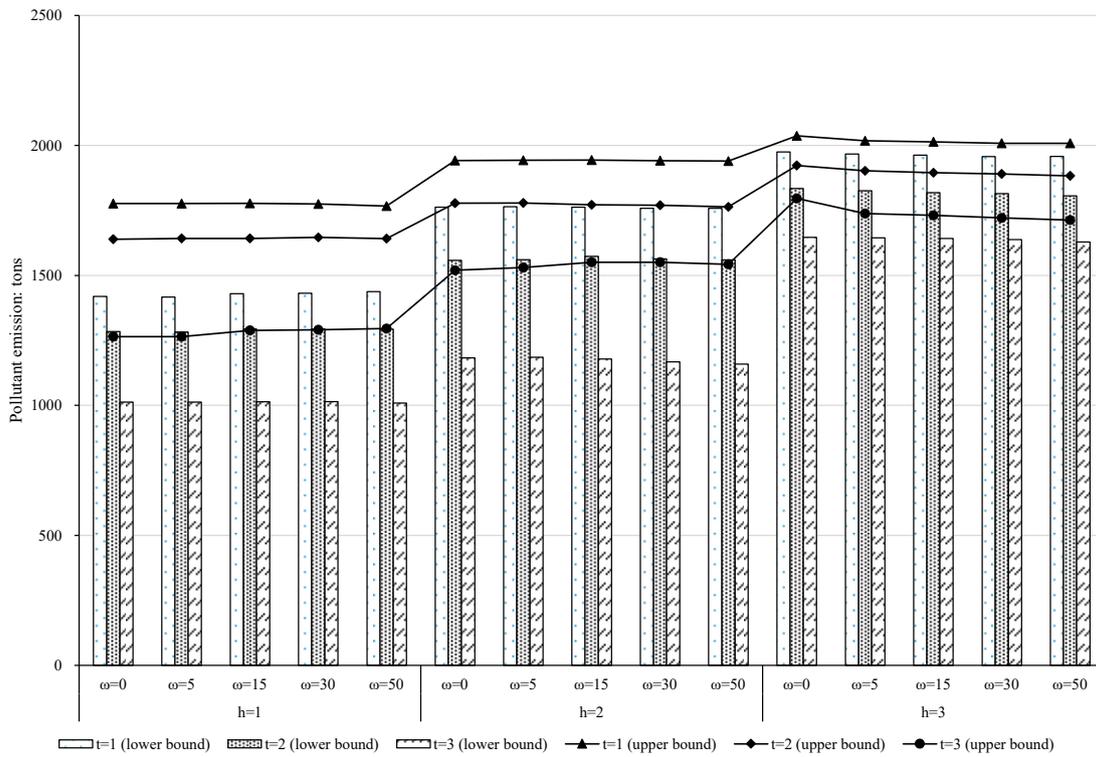


Figure 6. NH₄-H emissions in the Fenhe River Basin at different risk levels.

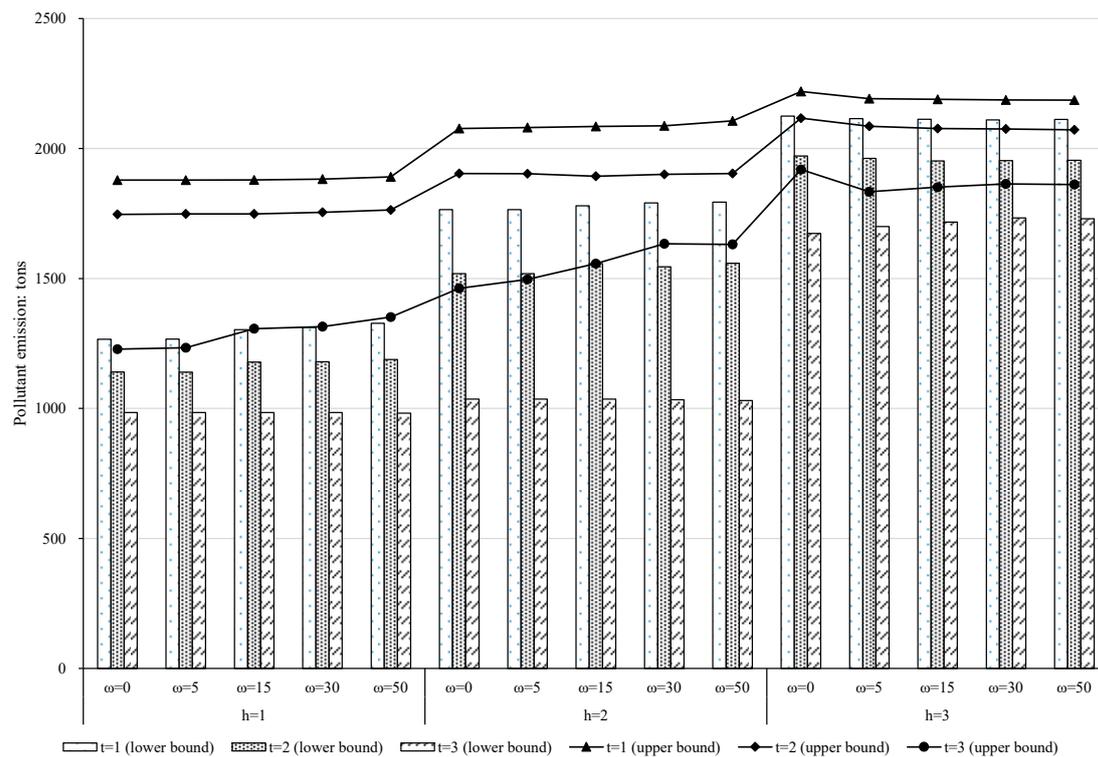


Figure 7. TP emissions in the Fenhe River Basin at different risk levels.

Figure 8 shows regional differences of pollutant emissions. The upstream area has the smallest pollutant emissions and shows a gradual downward trend as ω values increase. For example, the amounts of COD emissions are [3937.51, 4802.34], [3937.51, 4802.34], [3974.81, 4426.28], [4030.00, 4426.28], and [3961.33, 4320.60] tons for ω values of 0, 5, 15, 30, and 50, respectively, the same as for $\text{NH}_4\text{-H}$ and TP, which indicates that in the upstream area, sectors with lower benefits also have relatively low pollutant emission intensities. In the other areas, pollutant emissions show different tendencies. In the downstream area, COD, $\text{NH}_4\text{-H}$, and TP emissions generally increase as ω values increase, with a slight decrease in ω values of 5. For example, the amounts of $\text{NH}_4\text{-H}$ are [355.05, 440.1], [356.01, 431.55], [348.29, 444.86], [342.95, 448.68], [342.74, 448.99] tons for values of 0, 5, 15, 30 and 50, respectively. However, in the midstream, unlike COD and TP emissions that show an upward trend as ω values increase, the amounts of $\text{NH}_4\text{-H}$ emissions are [735.3, 977.58], [736.81, 996.49], [737.97, 1007.52], [731.11, 1004.21], and [730.86, 1003.87] tons, which fluctuate and show a downward trend for ω values of 15, 30, and 50. The changes in pollutant emissions reflect the optimization of water resource allocation strategies and the differences in factors such as the industrial structure, water benefit, and environmental carrying capacity in different areas of the basin.

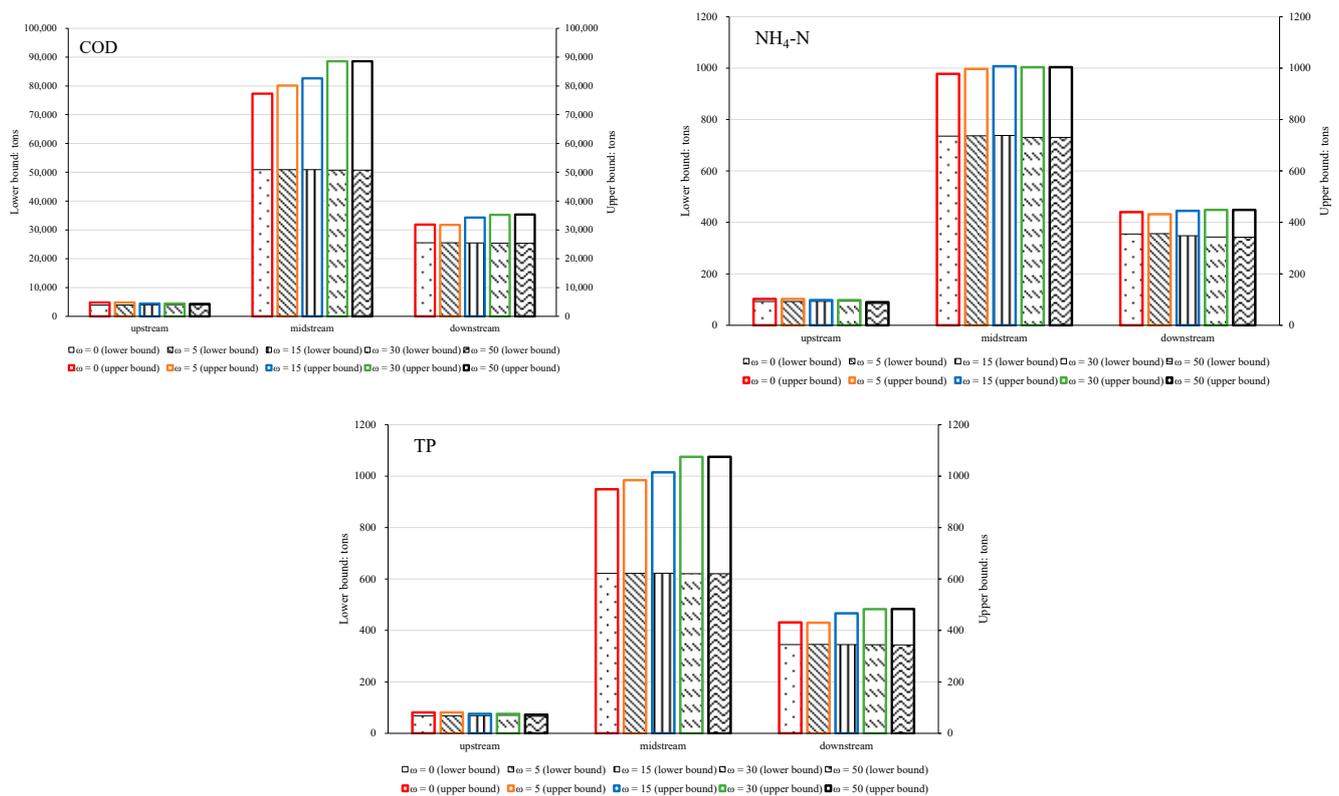


Figure 8. Pollutant emissions in the Fenhe River Basin in period 3, scenario 2.

Figure 9 shows the water resource allocation for different sectors. In the upstream area, the total industry and domestic water consumption remains unchanged as ω values increase, while the amounts of allocated fresh water and reused water for the two sectors have changed for ω values of 50. The water consumption of agriculture shows a downward trend, and the amounts are $[17,643.79, 23,006.55]$, $[17,643.79, 23,006.55]$, $[17,643.79, 20,985.81]$, $[17,870.91, 20,985.81]$, and $[17,893.23, 20,839.33] \times 10^4 \text{ m}^3$. Considering the downward trend of sectoral risks and pollutant emissions, the decrease in total water consumption demonstrates that benefits and costs are the main factors affecting resource allocation strategies for agriculture in the upstream area. In the midstream area, water resource allocations show differences across the four sectors. Water consumption of the industry remains unchanged as ω values increase due to relatively high sectoral benefits. Water consumption of the domestic and agriculture sectors shows opposite tendencies. Fresh water and reuse water for the domestic sector are $[46,283.31, 50,081.57]$, $[46,578.61, 50,081.57]$, $[46,784.56, 49,036.18]$, $[45,442.33, 45,956.5]$, and $[45,534.13, 46,025.65] \times 10^4 \text{ m}^3$ and $[11,221.41, 12,351.39]$, $[11,226.32, 12,351.39]$, $[11,296.26, 12,040.38]$, $[10,971.21, 11,503.76]$, and $[10,769.79, 11,360.53] \times 10^4 \text{ m}^3$ for ω values of 0, 5, 15, 30, and 50, and these show a gradual downward trend. Oppositely, as ω values increase, more water resources are allocated to agriculture in order to balance sectoral benefits. The same tendency appears in the downstream area for the two sectors. However, water resource allocation strategies for the industry show obvious fluctuation; the amounts of fresh water are $[11,962.2, 17,436.72]$, $[11,682.12, 19,914.18]$, $[14,637.63, 21,864.76]$, $[15,646.56, 18,878.45]$, and $[15,688.91, 18,691.18] \times 10^4 \text{ m}^3$ for ω values of 0, 5, 15, 30, and 50. Considering the downward trend of industrial risks in this area, it indicates that the developed ITSDP model optimizes water resource allocations based on different regional industrial structures and benefits.

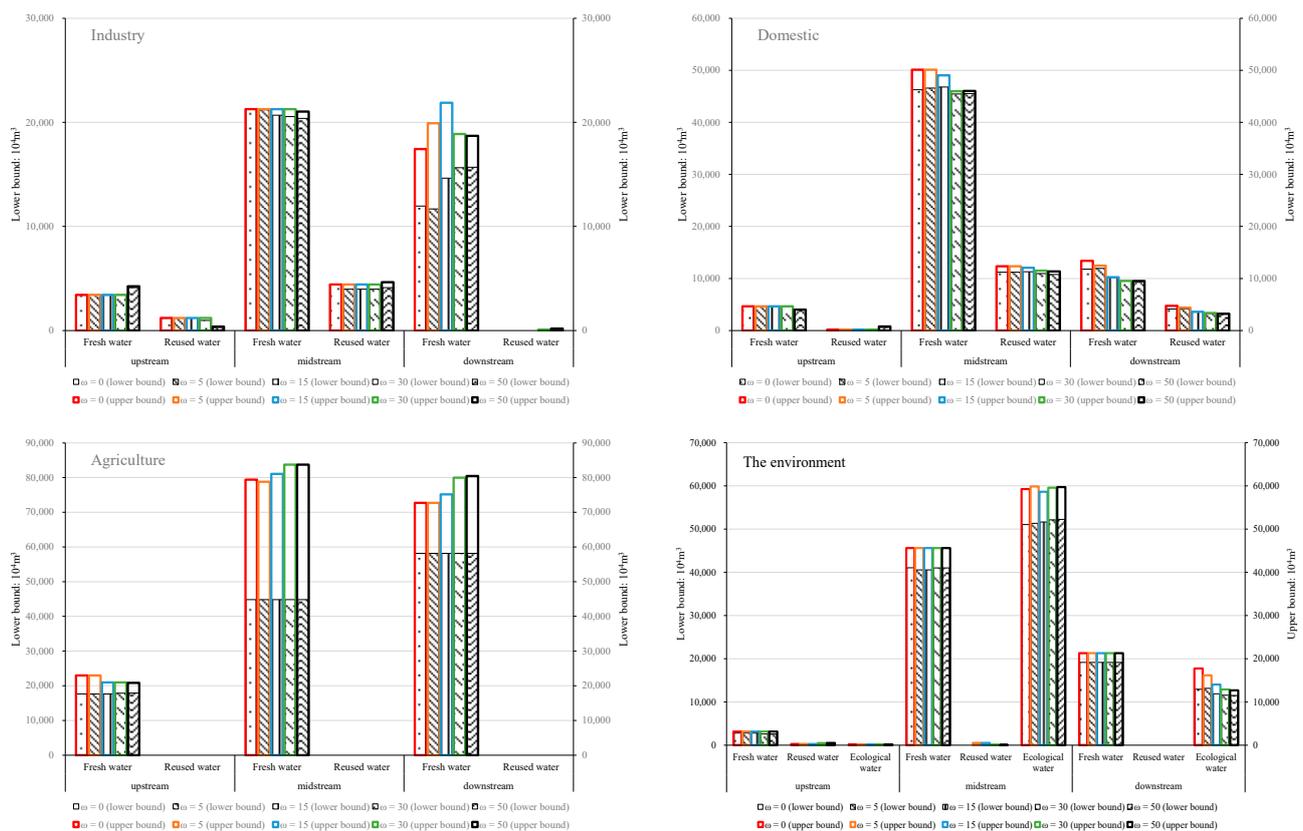


Figure 9. Water resource allocation strategies for sectors in the Fenhe River Basin.

Additionally, ecological water consumption in this study reflects the gaps between pollutant emissions and environmental carrying capacity for different values, showing various changes due to regional and sectoral differences in pollutant emission intensities. In the midstream area, it shows fluctuation, and the amounts of ecological water are [51,044.31, 59,268.6], [51,313.11, 59,856.65], [51,626.08, 58,622.38], [52,122.75, 59,570.23], and [52,225.92, 59,707.16] $\times 10^4 \text{ m}^3$. In the upstream and downstream areas, the amounts of ecological water show a downward trend as values increase; the developed model optimizes water resource allocation and reduces pollutant quantities entering the river in these areas.

3.3. Policy Scenarios Analysis

Risks and ecological water consumption indicate that water resources are insufficient for coordinating watershed socio-economic development and ensuring environmental quality in the Fenhe River basin. In this section, we set up two policy intervention scenarios to study the potential effect of appropriate policy interventions for further optimization of water resource allocation. To reflect the severe water shortage conditions, we consider a low water resource level ($h = 1$) and a ω value of 15 as the baseline scenario (S1), and another two policy scenarios are set: (1) S2: The water reuse rate gradually increases 10% over time; (2) S3: Coordinating the transferred water resources in the whole river basin for optimal regulation.

The risks in the three scenarios (Table 4) are CNY [0.09, 0.18], [0.08, 0.16], and [0.08, 0.13] $\times 10^6$ million in period 1, CNY [0.08, 0.39], [0.05, 0.37], and [0.06, 0.16] $\times 10^6$ million, and CNY [10.22, 14.67], [10.36, 14.77], and [11.97, 15.39] $\times 10^6$ million in periods 2 and 3. The results indicate that improving the water reuse rate (S2) and coordinating the water resources of the whole river basin (S3) could increase the benefits and control regional risks, and S3 shows a more significant effect. The results can support decision makers to formulate water management requirements and coordinate the optimal allocation of water resources in the entire river basin.

Table 4. Benefits of water resource utilization and risks in the Fenhe River Basin (CNY 10^6 million).

	Periods	Policy Scenarios		
		S1	S2	S3
Benefits	t = 1	[5.89, 6.68]	[5.91, 6.69]	[5.94, 6.69]
	t = 2	[8.23, 10.46]	[8.25, 10.51]	[8.61, 10.46]
	t = 3	[10.22, 14.67]	[10.36, 14.77]	[11.97, 15.39]
Risks	t = 1	[0.09, 0.18]	[0.08, 0.16]	[0.08, 0.13]
	t = 2	[0.08, 0.39]	[0.05, 0.37]	[0.06, 0.16]
	t = 3	[0.54, 2.07]	[0.51, 1.94]	[0.11, 0.33]

Figure 10 shows the deficits in water resource pre-allocations in different scenarios. The results show a regional difference. For example, in period 1, the water deficits of agriculture in S2 decrease from $[3753.41, 8668.13] \times 10^4 \text{ m}^3$ (S1) to $[3539.54, 8535.12] \times 10^4 \text{ m}^3$, and in S3, they increase to $[7255.75, 9467.58] \times 10^4 \text{ m}^3$. In the midstream and downstream areas, the results show different changes. The agricultural scale in the upstream area is relatively below, and S3 regulates the transferred water resources in the whole river basin, which leads to more water resources being allocated to other areas of higher benefits.

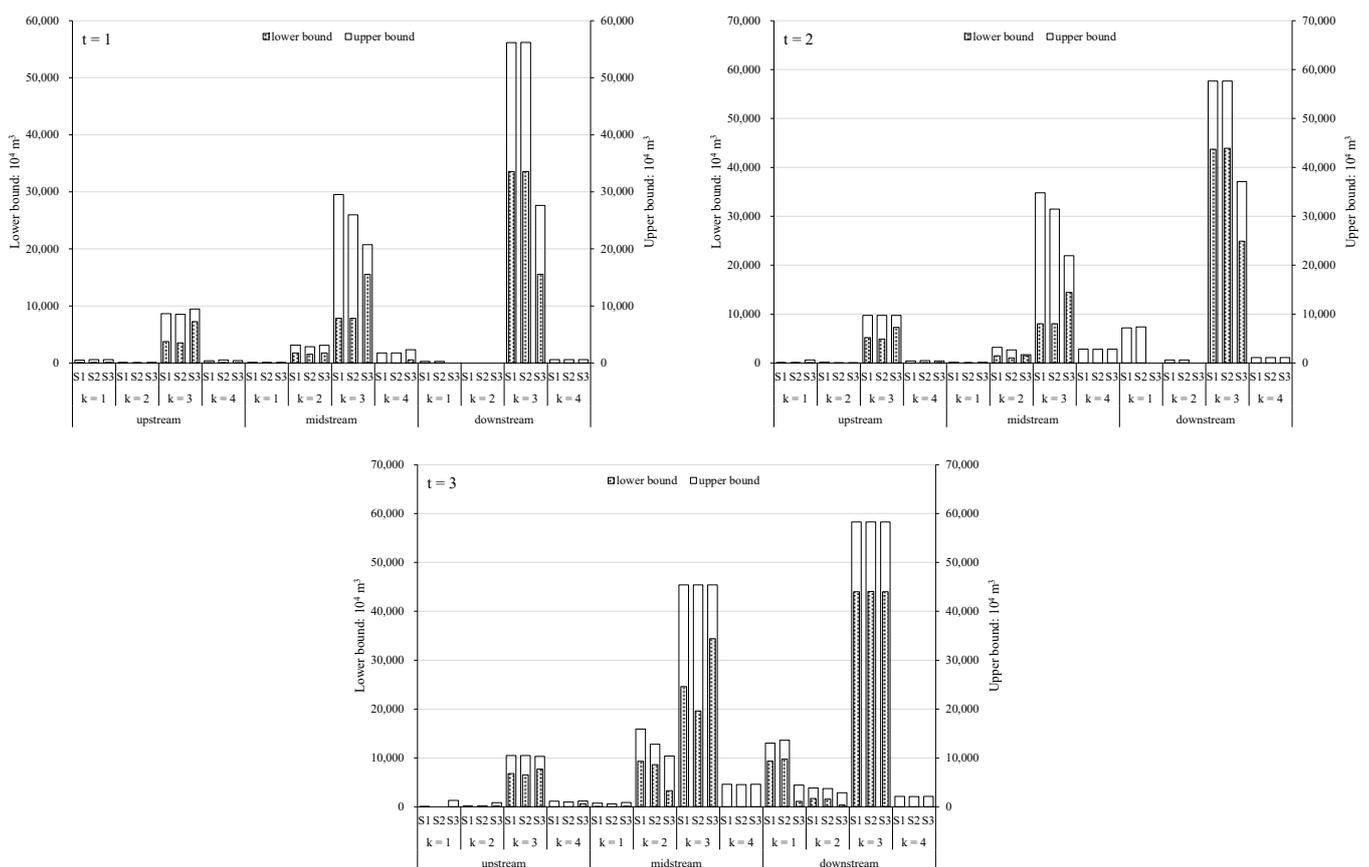
**Figure 10.** Water resource deficits in the Fenhe River Basin.

Figure 11 shows ecological water supplies in different scenarios. Compared to the other scenarios, S2 has fewer ecological water supplies; for example, the amounts are $[34,046.38, 46,012.89] \times 10^4 \text{ m}^3$ (S1), $[31,367.80, 42,790.44] \times 10^4 \text{ m}^3$, and $[38,340.87, 40,257.44] \times 10^4 \text{ m}^3$ (S3). A higher water reuse rate means fewer pollutant emissions. Additionally, the amounts of ecological water under S3 are the largest in the midstream area in period 2, compared to the downstream area. For example, the amounts of ecological

water are $[41,982.57, 55,669.92] \times 10^4 \text{ m}^3$ (S1), $[40,475.93, 50,915.65] \times 10^4 \text{ m}^3$ (S2), and $[49,665.20, 63,614.76] \times 10^4 \text{ m}^3$ (S3), respectively. It indicates that more water resources are allocated to the production sectors with higher benefits over the river basin. Water shortages mainly appear in the downstream areas, according to requirements of water resources and environment protection. The results show that water recycling is a critical factor for addressing water shortage and reducing pollutant emissions, and appropriate policy interventions would further optimize water resource allocation and effectively alleviate water shortage and water pollution in the Fenhe River Basin.

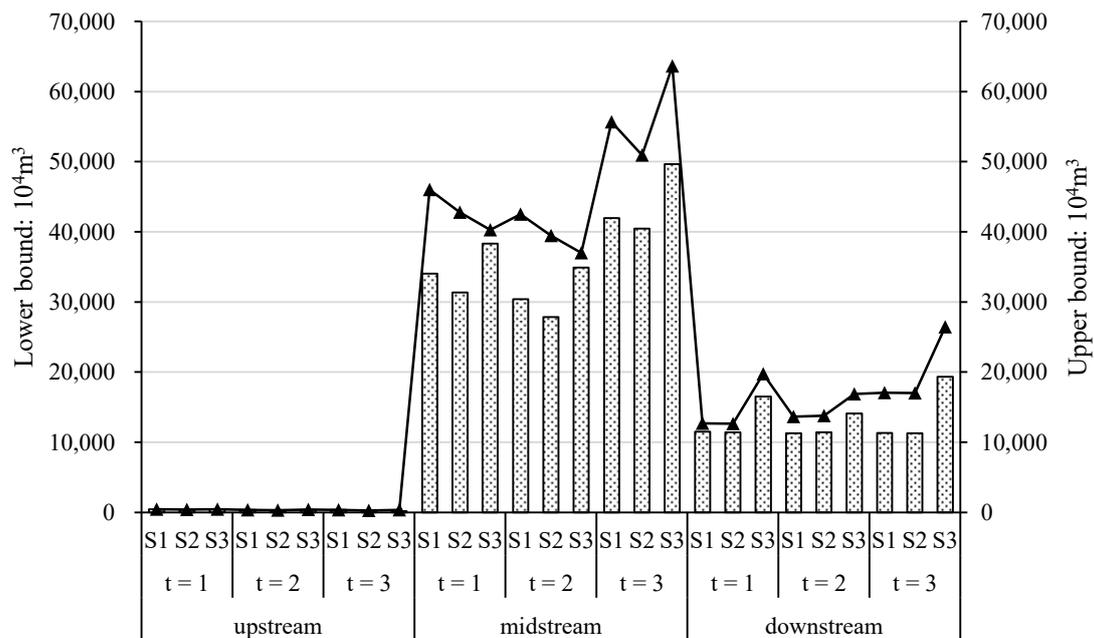


Figure 11. Ecological water supplies in the Fenhe River Basin in different scenarios.

4. Conclusions

In this study, an improved ITSDP model was built for optimal water resource allocation and pollutant emissions under dual constraints and uncertainties in the Fenhe River Basin, a highly urbanized, densely populated, typically water-deprived area with high degrees of contamination. The proposed model simultaneously addresses the uncertainties presented as interval values and probability distributions by integrating the IPP and TSP methods. The introduction of the downside risk aversion method effectively avoids possible risks caused by uneven water resource allocations. By solving the ITSDP model, optimal water resource allocation and pollutant emissions for the primary water use sectors were calculated for the programming periods under different scenarios. Additionally, we obtained the amounts of ecological water supplies required for purifying excessive pollutant emissions to identify areas with significant environmental water problems. These results, such as pollutant emissions and ecological water supplies, subject to strong water quality constraints, could provide a basis for regional emission permit systems. Furthermore, the optimal results under different risk levels and policy scenarios, namely S2 and S3, could reflect the subjective will of decision-makers for regional socio-economic development, environment protection, and possible changes of regional planning and policies.

The aim of this study was to use the ITSDP model to develop an effective approach to determine and optimize water resource allocations. The coordination of water quality protection and socio-economic development could support the establishment of water-based industrial structures and layouts. The results suggest that this approach is applicable and effective for the optimization of water resource allocation and water quality management in the Fenhe River Basin and could also be applied in other contexts or water-stressed areas. However, this model does not consider the gross ecosystem production from wa-

ter resources utilizations, which has been a significant indicator of regional sustainable development. Further studies are needed to address these limitations.

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