

# Article



# Implementation of Connected and Autonomous Vehicles in Cities Could Have Neutral Effects on the Total Travel Time Costs: Modeling and Analysis for a Circular City

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Abstract: Autonomous vehicles promise to revolutionize the automobile market, although their implementation could take several decades in which both types of cars will coexist on the streets. We formulate a model for a circular city based on continuous approximations, considering demand surfaces over the city. Numerical results from our model predict direct and indirect effects of connected and autonomous vehicles. Direct effects will be positive for our cities: (a) less street supply is needed to accommodate the traffic; (b) congestion levels decrease: travel costs may decrease by 30%. Some indirect effects will counterbalance these positive effects: (c) a decrease of 20% in the value of travel time can reduce the total cost by a third; (d) induced demand could be as high as 50%, bringing equivalent total costs in the future scenario; (e) the vehicle-kilometers traveled could also affect the future scenario; and (f) increases in city size and urban sprawl. As a conclusion, the implementation of autonomous vehicles could be neutral for the cities regarding travel time costs. City planning agencies still have to promote complementary modes such as active mobility (walking and bicycle), transit (public transportation), and shared mobility (shared autonomous vehicles and mobility as a service).

Keywords: urban road network; connected and autonomous car; continuous approximation

## 1. Introduction

Traffic congestion is one of the most significant problems for cities as Colin Buchanan asserted in the 1960s [1]. Several strategies have been traditionally applied to smooth out congestion, most of them under the umbrella of transportation demand management. In recent years, experts have discussed the implementation of autonomous vehicles (AVs) and their benefits for decongesting cities. For this reason, in some countries, the planning agencies are designing long-term plans, and these agencies need modeling tools that anticipate the impact they may have on transportation networks [2]. AVs have different levels of automation, and there are multiple definitions for them; NHTSA proposes to use the SAE International's classification that defines five levels of automation [3], and the cars are entirely autonomous when they reach level five (L5).

Some experts believe that these cars will widely enter the automotive market during the next decade, others are not so optimistic. Inevitably, AVs will arrive in our cities, and both types of vehicles will share the streets: autonomous and connected vehicles (CAVs) and manual vehicles (MVs) [4,5].

Implementation of CAVs will need new technical requirements, which Martínez-Díaz et al. [6] explain them in detail, for example, a new on-board architecture, sensing system, new communications,

cloud requirements, infrastructure needs, and others. This will allow that these new cars could generate positives changes in transportation and urban mobility. For example, the reduction of the generalized transport cost and parking cost of private vehicles, reduction of disutility on travel time, reduction of polluting emissions, improvement in road safety, induced demand, and improvement in road capacity because the distance among vehicles can be less than nowadays [2,7].

Several previous researchers have determined the impact of AVs on isolated sections of a highway. The main objective of this research is to analyze the effects of the implementation of CAVs on an urban network. The paper assesses how CAVs will be deployed and will share the infrastructure with MVs by considering three aspects: the potential benefits for the optimal urban structure, the assessment of the direct and indirect impacts of AVs on the efficiency of a network, and the probable effects of the progressive implementation of CAVs. As its focus, this work presents a strategic and macroscopic analysis of CAVs, using a continuous, two-dimensional, total-cost function applied to a circular city. The analysis does not consider other topics such as safety or livability.

We used the continuous approximation method (CA). According to Daganzo [8], this method was initially proposed by Gordon Newell. Newell formulated a continuous model that obtains the optimal bus schedule of departures from a bus depot, in which the demand function is considered continuous [9]. If the information concerning the input parameters is not perfect, then the method will be appropriate for solving a problem. The CA method assumes the following conditions: the input data varies slowly over the domain; the total cost is the aggregation of small sub-region costs, and component costs and their constraints depend on the characteristics of these sub-regions [8]. The CA method has been applied in a wide range of transportation and logistics studies: Clarens and Hurdle [10], Daganzo [8], Daganzo and Pilachowski [11], Medina et al. [12], Pulido et al. [13], and others.

In the next section, we explore the impacts of CAVs on mobility. After that, we present the mathematical model and apply it to a case study in a circular city.

#### 2. Theoretical CAV Impacts on Urban Mobility

The classification of AV impacts depends on the type of connection between AVs and the transportation system. AVs should produce positive effects, but some of them will generate non-desirable impacts. These impacts have been explained in various publications [4,14,15], in which [14] is an extended article of [4].

#### 2.1. Direct Effects

Firstly, some consequences will directly impact the transportation system; they are positive in general terms, as the literature describes it [16]. We classify these direct effects in five groups [4,14]:

- Reduction of generalized travel costs: Efficient driving will create savings in fuel costs and increment the travel speed in all types of vehicles. Furthermore, in a Smart City with V2I communication (vehicle-to-infrastructure), the cars will find a vacant parking spot quickly (on-street or off-street), and the CAVs will directly travel to the parking spot without users at top speed.
- 2. Increment of efficiency and flexibility: Driverless vehicles will permit flexibility in operations for transit and taxis, but this could generate a social problem (unemployment). In private AVs, this reduction of cost is not relevant.
- 3. Road capacity increment: Previous papers show different results [7]. Chang and Lai [17] analyzed the mixed traffic flow in a freeway section; the results show that the increment of road capacity is close to 33%. VanderWerf et al. [18,19] studied the impact of autonomous adaptive cruise control (AACC) and cooperative adaptive cruise control (CACC) using traffic simulation. The results show that AACC vehicles will increase the capacity about 7% if the AACC rate is between 40% and 60%; meanwhile, CACC vehicles will increment the capacity to near 102% when all cars

are communicated [19]. Tientrakool et al. [20] estimated that the road capacity would increase by 43% with AVs and 273% with V2V vehicles. Lioris et al. [21] stressed that an intersection is the bottleneck of the road capacity. If vehicles with AACC crossed an intersection in a platoon, then the road capacity would be doubled or tripled. Even if cars have CACC technology, the headways will be shorter. In a smart city, CAVs will be more efficient at intersections for V2I technology. On the other hand, other authors disagree and think that AVs would not reduce the congestion because AVs will drive rather cautiously; moreover, it is likely to increase the vehicle-kilometers traveled [5].

- 4. Pollution reduction: Some authors estimate that pollution could decrease [5,15] due to these cars will be electric vehicles (optimization of energy consumption) [6]. On the contrary, other experts predict an increment of this negative externality [16,22].
- 5. Improvement in road safety: AVs correctly implemented will reduce human errors and negligence in comparison to manual driving [5,15], although some estimations have determined that the crash number at roundabouts increases when AVs increase as well [23].

# 2.2. Indirect Effects

Secondly, indirect effects will change the demand behavior [16]. Indirect effects of AVs will cause changes in the system equilibrium between transport supply and demand [4,14]. As a result, new requirements for infrastructure will be necessary for the long-term [24]:

- 1. Reduction in the subjective value of travel time savings (VTTS): Ortúzar and Willumsen (2011) define VTTS as "the willingness to pay to reduce travel time by one unit" [25]. It was first formulated by English economists: Becker (1965), Johnson (1966), Oort (1969), DeSerpa (1971), and Evans (1972) [25]. Users of AVs will do other tasks instead of driving, reducing the disutility of the travel time [26].
- 2. New users to the vehicle system: AVs will expand the range of users that will use these cars (e.g., minors, the elderly, and disabled people) [24].
- 3. Induced demand: The reduction of the value of time, congestion, and travel times will cause the increment of trip demand in AVs and CAVs. The changes in travel patterns will impact the reduction of transit users [15], and AV and CAVs could increase. Therefore, this phenomenon will encourage the vicious circle of public transportation [25].
- 4. The increment of vehicle-kilometers traveled (VKT): The increment of the VKT has at least three reasons [24]. First, splitting of joint trips [16] in which two or more members of a family that are currently traveling together could travel separately with AVs. Second, AVs will move without passengers ("ghost trips") [15,16]. Moreover, transportation costs will be lower due to a better amortization of a vehicle [5].
- 5. Changes in trip distribution: The improvements due to direct effects, such as the reduction of congestion, costs, and the value of travel time, will cause longer trips. Changes in the place of residence, work, or both will imply changes in the generation and attraction of trips.
- 6. Changes in the urban structure and urban activity system: Changes in trip distribution will imply an increment in the city size in the long-term. The urban model will change to a dispersal model (urban sprawl) because new urban areas will be built in places far away from the city center [24,27–29].
- 7. There are other impacts that are not less important than the previous ones. First, it could be generated a social opposition to this paradigm shift in mobility due to ethics, legal, environmental, and territorial issues [6].

## 3. Mathematical Modeling

Consider a circular city, which has a radius *R*, with circular and radial primary roads in which the demand is continuous. The modeling of a circular city allows obtaining independent results and

conclusions of a particular network, but its results apply to many cities that have a radio-centric structure (e.g., Paris, Milan, Moscow, Canberra, Chengdu, Santiago de Chile, and others). In addition, only relevant inputs of the problem are considered to obtain an analytical result that identifies relevant factors and obtains numerical results in reasonable computational times.

The two decision variables of the model are the distance between circulars and radials roads. We consider two types of primary roads ( $W = \{a : arterial; f : freeway\}$ ), and two types of vehicles that use these roads ( $V = \{mv : MV; av : AV\}$ ), but CAVs travel on dedicated lanes that allow the formation of platoons. Table A1 describes the continuous spatial variables of the model, and Table A3 presents the parameters used in the modeling of scenarios with MVs and AVs (Appendix A).

The formulated model is based on the CA method and has an objective function that represents the total system cost. Therefore, the model solves a system optimum (SO) with a static traffic assignment problem in a continuous space. The CA solves a function of costs, which each point  $(r, \theta)$  in polar coordinates (r is the radius and  $\theta$  is the angle in radians) depends on local cost attributes. Total cost function (TC in [\$]) results from the integration of the local average cost function of a differential area in polar coordinates ( $r dr d\theta$ ) over the circular city ( $0 \le r \le R$ ,  $0 \le \theta \le 2\pi$ ). The total cost function ( $TC = C_C^u + C_C^a$ ) has two elements: the total cost of users ( $C_C^u$  in [\$], Appendix A) and the agency cost ( $C_C^a$  in [\$], Appendix A).

## 3.1. Demand Modeling

The demand density function  $P(x_f, y_f, x_t, y_t)$  ([veh/km<sup>4</sup>·h]) represents the density of car users that begin their trip on the point  $(r_f, \theta_f)$  and finish it on  $(r_t, \theta_t)$  [30] from an infinitesimal area  $dr_f r_f d\theta_f$ to other  $dr_t r_t d\theta_t$  (Figure 1). This function allows calculating the generation of trips that access to a primary road, the trip attraction to the destination, and the distribution of trips.



**Figure 1.** Density of vehicle users from a point  $(r_f, \theta_f)$  to a point  $(r_t, \theta_t)$ .

Equation (1) shows the parameter  $\Delta$  that is the total number of trips in a circular city with a radius *R* km where the time of a modeled period is *T* hours ([h]).

$$\Delta = \int_0^{2\pi} \int_0^R \int_0^{2\pi} \int_0^R P(r_f, \theta_f, r_t, \theta_t) \cdot T \ r_t dr_t d\theta_t r_f dr_f d\theta_f \tag{1}$$

### 3.2. Trip Assignment

The model assumes that the assignment is a static traffic assignment problem in a continuous space. The incremental assignment is the implemented method, which it is considered a valid approximation for strategic planning. This method divides the distribution matrix at factors  $p_n$  ( $\sum_n p_n = 1$ , where *n* is the number of iterations). Thenceforth, the method iteratively assigns to the network each fractioned matrix. In a Smart City with only CAVs, the route assignment should be done by a central agency, which could assign a base matrix using the shortest distance path with the all-or-nothing method and remaining trips using the updated cost function as the incremental method.

Therefore, at Step 0 of this method, the all-or-nothing method is used. For this step, there are three cases [14]. The cars can take a radial road first and then take a circular road (i.e., a radial–circular

trip). In the opposite case, the users take a circular road and, after, a radial road (i.e., a circular–radial trip). Finally, the users take a radial road from the origin to the city center first and, subsequently, they take a radial road to the destination (i.e., a radial–radial trip). In the following steps, the assignment considers the travel time calculated from the accumulated flows. In order to finish the algorithm, the method must sequentially assign all fractions to the network. The results of the assignment are the density functions of demand Table A2 (Appendix A).

## 3.3. Assumptions

The following points summarize the model assumption.

- The private transport demand is known, deterministic, and the function varies concerning its position. Furthermore, the car users take the shortest route (minimum distance) to the destination, and they can use circular streets, radial streets, or both of them.
- The road capacity is proportional to the number of lanes.
- The drivers cannot stop and wait for a vacant parking space and cannot return upstream when they are looking for a parking spot [31]. The vehicles park on service streets; therefore, they do not cause a reduction of road capacity. The model does not consider the parking capacity.
- The model does not include urban freight distribution and public transportation costs.

## 3.4. Impacts of CAVs on Urban Mobility

In the modeling, the user cost of private trips has three components: accessibility cost to main roads (Equation (A2)), regular trip cost (Equation (A4)), and arriving cost to trip destinations (Equation (A6)). Furthermore, the agency cost contains the infrastructure costs (Equation (A7)). CAVs will impact in different ways at each stage [4]. Table 1 describes how CAVs will impact on each stage of a trip.

First Stage: Accessibility to Main Roads	Second Stage: Regular Trip	Third Stage: Arriving to Trip Destinations
1. The generalized cost functions $(\Psi_v^F \text{ and } \Psi_{w,v}^c)$ will decrease due to $v_v^F$ will increase, and the operation cost $(\varphi_v^t)$ will decrease; and 2. The value of travel time $(\mu_v)$ will decrease because the users could do other activities during the travel and it will decrease the stress level.	1. The value of travel time $(\mu_v)$ will drop for AV users, as explained previously; 2. The speed of AV and CAVs will increase because of AVs will be more efficient $(v_{w,v}^{ff})$ ; 3. The road capacity will increase due to connected CAVs will travel in platoons $(K_{d,w,v}^R(r,\theta))$ ; 4. The travel time, when CAVs cross an intersection, will decrease $(\tau_{w,v}^i)$ due to communication V2I (Smart City), platoon formation, less reaction time, traffic lights coordination; and 5. The unitary operational cost will decrease because of AVs will be more efficient $(\varphi_v^t)$ .	1. Drivers get out of the car at the final destination $(d_p = 0)$ ; 2. The generalized cost will decrease $(\Psi_v^F \text{ and } \Psi_v^p)$ due to AVs and CAVs will be more efficient. Moreover, the ratio $\mu_v / v_v^p$ will be null in the generalized cost $\Psi_v^p$ ; and 3. The users will not have to walk from the parking spot to the destination. Therefore, $((2 \cdot e^{-\lambda_p \cdot d_p})/\lambda_p + d_p - 1/\lambda_p)$ is null.

**Table 1.** List of estimated impacts in which CAVs will impact on each stage of a trip.

#### 3.5. Mathematical Solution

The mathematical problem is a nonlinear system with constraints from KKT conditions (Equations (A10)). In the CA method, the minimized function is  $tc(r, \theta)$ —that is the local cost at each  $(r, \theta)$  point; the problem has n decision variables  $(x_i(\cdot) = \{d_w^c(r), \Phi_w^r(\theta)\}, w \in W)$  and m constraints. The optimal analytical formulations are solved through the method of successive approximations.

#### 4. Application to a Case Study

This section has five parts: a description of the case study; parameters; finally, three points with the results of the model.

#### 4.1. Description of a Case Study

The analyzed case is a circular city with nine zones: a central business district (CBD), four internal zones, and four external zones (Figure 2a,b). If the city radius is 15 km (R) with a homogeneous trip density, then the CBD radius will be 5 km ( $R_1 = R_2/\sqrt{5}$ ), and the external radius will be about 11.2 km ( $R_2 = R \cdot \sqrt{5}/3$ ). The distribution matrix is symmetric and has 405,000 private trips per hour (Figure 2c).



Figure 2. Demand modelling: (a) generation, (b) attraction, and (c) trip distribution.

The distribution of trip demand (generation, attraction, and trip distribution) allows obtaining the demand density function using the incremental assignment method. Figure A1 (Appendix B) shows the density of vehicles that access to main roads, the density of vehicles that travel on main roads, and the density of vehicles that arrive at main roads. Moreover, Table A4 (Appendix B) shows the list of parameters for both types of vehicles used by the model.

#### 4.2. Optimal Urban Structure

Figure 3 represents the comparison between the results of the optimization with only MVs and CAVs (Level 5 of automation and connected vehicles). The graph (Figure 3) shows the inverse of the optimal decision variables: distance between circular ((a) and (b)) and radial roads ((c) and (d)). The average of the optimal distance between circular roads is 3.8 km in the base scenario and 7.5 km in the future scenario reducing by half the number of primary roads. In radial roads, the results are similar in both cases. The average optimal distance between radial roads is 2.1 km at a radius of 5 km, 4.1 at 10 km, and 6.2 at 15 km for the current scenario. In the scenario with CAVs, the distance for radial roads is 2.6 km at a radius of 5 km, 5.2 at 10 km, and 7.8 at 15 km. In the discretization, the gray lines represent the border between corridors and the area in this zone is approximately a unit, while the red points represent the location of optimal primary roads.

## Scenario with only MVs:





**Figure 3.** Comparison of modeling results between MVs and CAVs. The figure shows the cases: (**a**) MV density of circular roads, (**b**) MV density of circular roads, (**c**) MV density of radial roads, (**d**) MV density of radial roads, (**e**) optimal urban structure with only MVs and its congestion level, and (**f**) optimal urban structure with only CAVs and its congestion level.

Finally, the circular graphs (e) and (f) represent the congestion levels on all optimal primary roads of both scenarios. The graphs reveal that the saturation of the future scenario drops, even if there is less road infrastructure supply than in the base scenario.

## 4.3. Effects on the Urban Network

### 4.3.1. AV Direct Effects

This section explains some results of direct effects on the urban mobility [4,14].

- Reduction of road congestion. If the driving of AVs is more efficient than MVs, then the road capacity will rise, and the congestion will drop [32]. The reduction of the road saturation by CAVs can reach between a third and a half of MV saturation (Figure 4a).
- Reduction of costs. As a result of the previous improvement, the operation cost will also decrease. The cost functions will decrease by about 30%, as shown in Figure 4b.



**Figure 4.** Influence of direct effects based on Medina-Tapia and Robusté [4,14]: (**a**) MV and CAV saturation percentage, and (**b**) travel stage cost of MVs and CAVs.

## 4.3.2. AV Indirect Effects

On the other hand, the consequences of AV and CAV indirect effects will offset the savings by direct effects [4,14].

- Reduction of the value of travel time. Figure 5a shows blue lines that represent the reduction of the total cost if the value of travel time decreases and a red point that represents the total cost in the current scenario (only MVs). Kohli and Willumsen [26] asserted that the value of travel time could decrease by 20% in the scenario with only AVs. Therefore, if  $\mu = 8$  in our model (blue point), then the total cost will decrease by 35%. This is the gap of difference between the red point and the blue point.
- Induced demand. Figure 5b shows the economic model of this system: the price axis represents the travel cost, and the VKT indicator represents the quantity in the horizontal axis. Red lines represent the supply and demand curves for MVs in which the red point (e1) is the current equilibrium. With the operation of only CAVs, the transport supply should increase (blue line). Therefore, the system will have a new equilibrium point (point e2) that will have less congestion than the current scenario, but new users will enter the system. Blue demand lines represent this consequence. If the demand increases 50% (Demand 1.5x), the total cost in the new equilibrium (point e3) will be a little smaller than (or similar to) the current scenario (point e1). Figure 5a shows that if  $\mu = 8.2$ , the total costs of the current scenario and the scenario with 1.5x demand are equivalent.
- The increment of the VKT. This indicator could increase if AVs started to look for a parking spot only once the user gets out of the car at the destination. The results show an increment of over 5.10<sup>4</sup> km by CAVs compared to the current scenario [4,14], although this result is relative because CAVs will look for a vacant parking space using V2I technology in a Smart City.

• Changes in trip distribution and urban structure. If the trips are more extended than nowadays, the city size will increase, and the vicious cycle will be encouraged. Blue lines in Figure 5c represent the variation of the value of travel time between the city radius and the total cost with only AVs. The graph shows that the total cost will increase if the city grows; hence, this cost could be equivalent to the present scenario (MVs) around a radius of 35 km with  $\mu = 8$  [\$/h]. Therefore, the city size is as considerable as the induced demand. The green curve in Figure 5c shows that if the urban radius increases, the average user cost per kilometer will slightly decrease. Therefore, if the generalized cost, including the value of time, will be smaller than now, the trips will aim to be longer, and the users will modify the destination. This reduction of costs will cause dispersion along with long-term changes in the activity system and the urban structure. Fortunately, these cars are in the early implementation phases, but urban problems such as spatial segregation or urban sprawl are profound in some cities, and AVs and CAVs could deepen them even more [4,14].



(b) Figure 5. Cont.



**Figure 5.** Influence of indirect effects. (**a**) Variation of the value of travel time and demand on the cost function. (**b**) Effect of the induced demand by CAVs on the travel cost. (**c**) Effect of the urban radius on the cost of users.

#### 4.4. Progressive Implementation Analysis

We analyze the evolution of the CAV implementation through two factors: the total cost (Figure 6a) and congestion level (Figure 6b) by the penetration of CAVs from 0% to 100%. Both charts exhibit that the cost and congestion will decrease with this new technology if the demand is constant over time [32]. The curve fluctuates when it decreases because the model assigns the infrastructure (number of lanes) progressively according to the type of car, which will generate congestion. In Figure 6a, the user costs tend to decrease while the agency costs rise when the infrastructure dedicated to CAVs is implemented, reaching almost the convergence when all vehicles are driverless cars. Additionally, the total cost fluctuates, decreasing by the implementation of CAV-dedicated roads. Therefore, agencies have to invest in the mitigating of imbalances between supply and demand. Figure 6b shows that the gradual implementation could generate scenarios that are worse than the initial stage. In the early years of the implementation, the users' perception will be averse to incorporating this new automation.



**Figure 6.** Progressive implementation based on Medina-Tapia and Robusté [32]. (**a**) Cost variation by CAV penetration. (**b**) Saturation variation by CAV penetration.

## 5. Conclusions

Transportation policies should reduce the possible impacts and enhance the potential benefits of AVs. Agencies have to prepare and adapt cities for this change of paradigm in urban mobility. This research seeks to provide some initial ideas on the implementation of new technologies, in which planning agencies should consider them in long-term plans under sustainable development. Consequently, this paper analyzed three topics related to the implementation of CAVs.

First, the direct effects of CAVs will positively impact cities. According to our model, CAVs could influence the optimal structure of a city in two aspects. Firstly, the city will require less road supply. These savings are more significant with circular road supply than in radial roads. This reduction will allow agencies to manage this infrastructure better. Secondly, traffic congestion with CAVs decreases even with less road infrastructure. Despite this, not all of the expected effects are positive.

Second, indirect effects will mitigate the direct effects because the reduction of road capacity is not the only factor of importance. Several significant conclusions can be drawn from the results of this work. Firstly, the value of travel time is another crucial factor. On the one hand, it can reduce a third of the total cost; on the other hand, it might cause other significant externalities explained in the following points. Secondly, the induced demand is another element that might limit the benefits obtained through CAVs. Thirdly, the increment of vehicle-kilometers traveled is a difficult factor to measure, but the consequences can be substantial over the city. Finally, the dispersion of cities is a factor that has not received as much attention, and they have been less researched than others impacts of AVs. Thus, urban growth could be more significant than other factors, such as induced demand. All factors as a whole will tend to encourage the vicious cycle of public transportation and to promote unsustainable cities in the long-term.

Third, the analysis done on the progressive implementation of CAVs shows that the operation of these cars will be a complicated process, as reaching the optimal equilibrium requires additional resources for reducing possible scenarios as bad as the current scheme.

The three aspects previously analyzed expose the advantages and limitations of the implementation of CAVs from the point of view of travel costs. Therefore, a city with only CAVs will not be sustainable; urban sustainability will only be kept using complementary modes such as public and shared transportation. Moreover, these changes will boost the operation of new technologies such as shared autonomous vehicles (SAV), mobility as a service (MaaS), personal mobility devices (electric scooters, Segways, hoverboards, unicycles), and others.

In future works, the model will permit the proposal of different solutions in a city with heterogeneous demand spatially. Moreover, the influence of changes in user behavior will be analyzed in each stage of the trip, considering aspects such as modal choice, trip distribution, and assignment. Finally, in future analysis, we will also consider extending the study to the case of a real city.

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#### Appendix A

This section describes the mathematical formulation. The total cost function ( $TC = C_C^u + C_C^a$ ) has two elements: the total cost of users ( $C_C^u$  in [\$]) and the agency cost ( $C_C^a$  in [\$]). The model uses continuous spatial variables (Table A1); secondly, Table A2 describes the demand density functions obtained from the assignment method. Finally, Table A3 presents the list of parameters used in the modeling of a circular city.

Variables	
$d_w^c(r)$	distance function between circular roads of type $w \in W$ at the radius $r \text{ km [km/road]}$ ; and
$\Phi^r_w(\theta)$	angle function between radial roads of type $w \in W$ at a city point with angle $\theta$ [radian/road], which $d_r(r, \theta) = \Phi_r(\theta) \cdot r$ is the distance function between radial roads at a city point $(r, \theta)$ [km/road].

Table A1. Variables used in the modeling of a circular city.

**Table A2.** Demand density functions obtained from the assignment method.

Demand Functions		
$f^F_{k,v}(r,\theta)$	vehicles density of type $v \in V$ that access from the origin to a circular $(k = c)$ or radial $(k = r)$ primary road [veh/km <sup>2</sup> ·h];	
$f^R_{k,d,v}(r,\theta)$	vehicle flow density of type $v \in V$ that travel on a circular ( $k = c$ ) or radial ( $k = r$ ) primary road considering the direction $d$ [veh/km·h]; and	
$f^A_{k,v}(r,\theta)$	vehicles density of type $v \in V$ that arrive from a circular ( $k = c$ ) or radial ( $k = r$ ) primary road to the destination [veh/km <sup>2</sup> ·h].	

Table A3.         Nomenclature of parameter	s used in the modeling	of a circ	ular city.
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Other Par	ameters
Т	duration of period [h];
$\mu_v$	value of travel time of users in vehicle $v$ [\$/h];
$v_v^F$	car speed of type $v$ to access main roads of the city $[km/h]$ ;
$v_{w,v}^{ff}$	free-flow car speed of type $v$ on a primary road of type $w$ [km/h];
$v_v^p$	cruising speed of a car $v$ looking for a parking spot [km/h];
$v^a$	average walking speed for accessing to the destination point from parking site $[km/h]$ ;
$t_{w,v}^F$	average time for accessing the primary road $w$ of a car $v$ [h];
$t_{w,v}^{A}$	average time for accessing the local roads from a road $w$ of a car $v$ [h];
a and b	parameters of BPR volume-delay function [dimensionless];
$k_{w,v}$	capacity road per lane of type w [veh/lane·h];
$\eta_w$	number of lanes at a road $w$ [lane];
$\tau^i_{w,v}$	average time spent by a vehicle of type $v$ when crosses a crossroad on a road of type $w$ [h/veh];
$\lambda_P$	average density of vacant parking space [parking/km];
$d_p$	distance before arriving at the destination where the drivers begin to look for a parking spot [km];
$arphi_v^t$	car cost of type $v$ per distance unit [\$/km·veh];
$\varphi^p$	parking fee [\$/h·veh];
$\varphi^{h(f)}_{w,v}$	maintenance fixed cost by road infrastructure for a road $w$ and a car $v$ [\$/km]; and
$\varphi^{h(v)}_{w,v}$	maintenance variable cost by road infrastructure for a road $w$ and a car $v$ [\$/km·h].

## Appendix A.1 Users Costs

The total user cost function ( $C_C^u = C_F + C_R + C_A$  in [\$]) contains three elements: accessibility cost to a primary road ( $C_F$ ), cost spent in a regular car trip ( $C_R$ ), and arriving cost at the destination ( $C_A$ ).

## Appendix A.1.1 Accessibility Cost to Main Roads

The average access cost (Equation (A1) in [\$/veh]) for accessing to a circular  $(c_{c,w,v}^F(r))$  or a radial road  $(c_{r,w,v}^F(r,\theta))$  has two components. First, cars travel a quarter of the distance between the origin and the closest primary road. The average travel cost is the multiplication of this distance and the generalized cost  $\Psi_v^F (\Psi_v^F = \mu_v / v_v^F + \varphi_v^t$  in [\$/km·veh]). Second, the users incur a cost for accessing the primary road  $(t_{w,v}^F \cdot \Psi_{w,v}^c$  where  $\Psi_{w,v}^c = \mu_v + v_v^F \cdot \varphi_v^t$  in [\$/h·veh]).

$$c_{k,w,v}^{F}(\cdot) = \begin{cases} \frac{d_{w}^{c}(r)}{4} \cdot \Psi_{v}^{F} + t_{w,v}^{F} \cdot \Psi_{w,v}^{c} & k = c\\ \frac{r \cdot \Phi_{w}^{r}(\theta)}{4} \cdot \Psi_{v}^{F} + t_{w,v}^{F} \cdot \Psi_{w,v}^{c} & k = r \end{cases}$$
(A1)

The local accessibility cost function has two components: the demand density in rush hour  $(f_{k,v}^F(r,\theta)\cdot T)$  and the average access cost per vehicle  $(c_{k,w,v}^F(r))$ . This cost is the integration of a local cost over the city area for all types of roads w and vehicles v (Equation (A2)).

$$C_F = \int_0^{2\pi} \int_0^R \sum_{w \in W} \sum_{v \in V} f_{c,v}^F(r) \cdot T \cdot c_{c,w,v}^F(r) + f_{r,v}^F(r,\theta) \cdot T \cdot c_{r,w,v}^F(r,\theta) \ r \ dr \ d\theta$$
(A2)

Appendix A.1.2 Regular Trip Cost

In regular trips, the generalized travel cost function has three elements (Equation (A3) in  $[\$/km \cdot veh]$ ). The first component is a Bureau of Public Roads (BPR) function that represents the congestion effects. The free-flow travel cost per kilometer is the inverse of free-flow speed multiplied by the value of travel time  $(\mu_v / v_{w,v}^{ff})$ . The congestion level depends on the traffic flow  $(F_{c,w,d,v}^R(r,\theta) = f_{c,d,v}^R(r,\theta) \cdot d_w^c(r)$  and  $F_{r,w,d,v}^R(r,\theta) = f_{r,d,v}^R(r,\theta) \cdot r \cdot \Phi_w^r(\theta)$ ) and the capacity of the road type  $w(K_{d,w,v}^R(r,\theta))$  where the vehicles can travel in two directions:  $d \in \{d_1 = clockwise, d_2 = anticlockwise\}$  on circular roads, and  $d \in \{d_1 = inside, d_2 = outside\}$  on radial roads. Secondly, the unitary cost of a regulated crossroad by traffic lights is the ratio between the cost spent by crossing the road  $(\mu_v \cdot \tau_{w,v}^i)$  and the distance between roads  $(r \cdot \Phi_w^r(\theta) \circ r_{w}^c(r))$ . Finally, the last component is the operational cost  $(\varphi_v^t)$ .

$$C_{k,d,w,v}^{R}(r,\theta) = \begin{cases} \frac{\mu_{v}}{v_{w,v}^{ff}} \cdot \left(1 + a \cdot \left(\frac{F_{c,d,v}^{R}(r,\theta)}{K_{d,w,v}^{R}(r,\theta)}\right)^{b}\right) + \frac{\mu_{v} \cdot \tau_{w,v}^{i}}{r \cdot \Phi_{w}^{r}(\theta)} + \varphi_{v}^{t}k = c \\ \frac{\mu_{v}}{v_{w,v}^{ff}} \cdot \left(1 + a \cdot \left(\frac{F_{r,d,v}^{R}(r,\theta)}{K_{d,w,v}^{R}(r,\theta)}\right)^{b}\right) + \frac{\mu_{v} \cdot \tau_{w,v}^{i}}{d_{w}^{c}(r)} + \varphi_{v}^{t}k = r \end{cases}$$
(A3)

Similar to the previous case, the total trip  $\cot(C_R \text{ in } [\$])$  is the integration of the local cost function. The elements of the local cost function are the demand density in rush hour and the local generalized travel cost in each type of road *w* (Equation (A4)).

$$C_R = \int_0^{2\pi} \int_0^R \sum_{d \in D} \sum_{w \in W} \sum_{v \in V} f_{c,d,v}^R(r,\theta) \cdot T \cdot c_{c,d,w,v}^R(r) + f_{r,d,v}^R(r,\theta) \cdot T \cdot c_{r,d,w,v}^R(r,\theta) \ r \ dr \ d\theta$$
(A4)

Appendix A.1.3 Arriving Cost to Trip Destinations

After that a user has parked his car, he has to pay for the parking fee and has to walk to the final destination. The average destination cost has five elements. Firstly, the users incur a cost for accessing local roads  $(t_{w,v}^A, \Psi_{w,v}^c \text{ where } \Psi_{w,v}^c = \mu_v + v_v^F \cdot \varphi_v^t \text{ in } [\$/h \cdot \text{veh}])$ . Secondly, the driving cost on local streets before the users start to look for a vacant parking spot. This sub-cost is composed of the average distance (e.g.,  $(d_w^c(r) - d_p)/4)$  and the generalized cost  $(\Psi_v^F = \mu_v/v_v^F + \varphi_v^t)$ . Thirdly, the cost incurred by users, which are looking for a parking space, is the multiplication of the average distance between vacant spots  $(1/\lambda_P)$  and the generalized cost  $(\Psi_v^P = \mu_v/v_v^P + \varphi_v^t)$ . Fourthly, the user walking cost, which is the distance between the user parked and the destination, is the multiplication of the average [31], the expected walking distance after parking the vehicle has two cases. If a driver finds a vacant space before his destination (x < d) then this driver will walk d - x km. In another case, the driver will walk x - d km to the destination. Finally, the cost includes the car parking fee  $(\varphi^p)$ . Equation (A5) shows the average local destination cost ([\$/veh]) for each road type.

$$C^{A}_{k,w,v}(r) = \begin{cases} t^{A}_{w,v} \cdot \Psi^{c}_{w,v} + \left(\frac{d^{c}_{w}(r) - d_{p}}{4}\right) \cdot \Psi^{F}_{v} + \frac{1}{\lambda_{p}} \cdot \Psi^{P}_{v} + \left(\frac{2 \cdot e^{-\lambda_{p} \cdot d_{p}}}{\lambda_{p}} + d_{p} - \frac{1}{\lambda_{p}}\right) \cdot \Psi^{A}_{v} + \varphi^{p}k = c \\ t^{A}_{w,v} \cdot \Psi^{c}_{w,v} + \left(\frac{r \cdot \Phi^{r}_{w}(\theta) - d_{p}}{4}\right) \cdot \Psi^{F}_{v} + \frac{1}{\lambda_{p}} \cdot \Psi^{P}_{v} + \left(\frac{2 \cdot e^{-\lambda_{p} \cdot d_{p}}}{\lambda_{p}} + d_{p} - \frac{1}{\lambda_{p}}\right) \cdot \Psi^{A}_{v} + \varphi^{p}k = r \end{cases}$$
(A5)

Sustainability 2019, 11, 482

The total arriving cost ( $C_A$  in [\$], Equation (A6)) is the integration of the local cost composed of the demand function in rush period ( $f_{k,v}^A(r,\theta)\cdot T$ ), and the expected walking cost and parking fee ( $c_{k,v,v}^A(r,\theta)$ ).

$$C_A = \int_0^{2\pi} \int_0^R \sum_{w \in W} \sum_{v \in V} f^A_{c,v}(r) \cdot T \cdot c^A_{c,w,v}(r) + f^A_{r,v}(r,\theta) \cdot T \cdot c^A_{r,w,v}(r,\theta) \ r \ dr \ d\theta \tag{A6}$$

Appendix A.2 Agency Costs

In the agency cost ( $C_I$  in [\$], Equation (A7)), the local cost function ( $[\$/km^2]$ ) is the multiplication of the cost per linear kilometer and the road density  $(1/d_w^c(r) \text{ or } 1/r \cdot \Phi_w^r(\theta))$ . The unitary cost contains two parts: a fixed and a variable element.

$$C_{I} = \int_{0}^{2\pi} \int_{0}^{R} \sum_{w \in W} \sum_{v \in V} \frac{\varphi_{w,v}^{h(f)} + \varphi_{w,v}^{h(v)} \cdot T}{d_{w}^{c}(r)} + \frac{\varphi_{w,v}^{h(f)} + \varphi_{w,v}^{h(v)} \cdot T}{r \cdot \Phi_{w}^{r}(\theta)} r \, dr \, d\theta \tag{A7}$$

Appendix A.3 Constraints

The model also considers that the congestion should not overtake 90 percent of capacity for both roads (Equations (A8) and (A9)).

$$\max_{\theta} \left( \frac{f_{c,d,v}^{R}(r,\theta) \cdot d_{w}^{c}(r)}{K_{d,w,v}^{R}(r,\theta)} \right) \le 0.9 \qquad \forall r,d,w,v$$
(A8)

$$\max_{r} \left( \frac{f_{r,d,v}^{R}(r,\theta) \cdot \Phi_{w}^{r}(\theta) \cdot r}{K_{d,w,v}^{R}(r,\theta)} \right) \le 0.9 \quad \forall \theta, d, w, v$$
(A9)

#### Appendix A.4 Numerical Solution

The nonlinear system has *n* decision variables  $(x_i(\cdot) = \{d_w^c(r), \Phi_w^r(\theta)\}, w \in W)$  and *m* constraints. The set of Equation (A10) shows the KKT conditions, in which we obtain the first condition for each one of the decision variables (A10.1) when they are not negative (A10.5). The second condition contains the constraints  $c_j$  (A10.2). The third condition set is the complementary slackness (A10.3); if the inequality constraint is active, its slack is zero, and its multiplier  $(\lambda_j(\cdot))$  takes any non-negative value (A10.4). In Equation (A10), the expression contains an equation system with inequalities. This system of equations allows obtaining the optimal solution through the method of successive approximations.

$$\nabla tc(x_i(\cdot)) + \sum_{j}^{m} \lambda_j(\cdot) \cdot \nabla c_j(x_i(\cdot)) = 0 \quad \forall i = 1, \dots, n \ (1)$$

$$c_j(r, \theta) - b_j \le 0 \quad \forall j = 1, \dots, m \ (2)$$

$$\lambda_j(\cdot) \cdot (c_j(r, \theta) - b_j) = 0 \quad \forall j = 1, \dots, m \ (3)$$

$$\lambda_j(\cdot) \ge 0 \quad \forall j = 1, \dots, m \ (4)$$

$$x_i(\cdot) > 0 \quad \forall i = 1, \dots, n \ (5)$$
(A10)

Density of vehicles that access to circular roads





-7.5

-15

-15

Density of vehicles that access to radial roads







Density of vehicles that arrive at destination on circular roads

(c)

252° 0





324

15

288° 7.5

**Figure A1.** Traffic density assignment in rush period (K is a thousand trips): (**a**) Density of vehicles that access to circular roads. (**b**) Density of vehicles that access to radial roads. (**c**) Density of vehicles on circular roads. (**d**) Density of vehicles on radial roads. (**e**) Density of vehicles that arrive at the destination on circular roads. (**f**) Density of vehicles that arrive at the destination on radial roads.

## Appendix B

Stage 2

This section presents the inputs used in the modeling: demand and other parameters.

#### Appendix B.1 Demand

Figure A1 shows the homogeneous demand density with only MVs in each car trip stage using the incremental assignment method. In Stage 1, the density of generated and attracted trips in an

infinitesimal area ( $\lfloor veh/km^2 \cdot h \rfloor$ ) is concentrated on the central zone for trips that access circular primary roads (Figure A1a) and on the periphery for radial roads (Figure A1b). In Stage 2, the regular trip density at each city point ( $\lfloor veh/km \cdot h \rfloor$ ) is concentrated in an internal zone for circular roads (Figure A1c). On the other hand, radial trips are concentrated around the city center (Figure A1d). In Stage 3, the density represents attracted trips around a point ( $\lfloor veh/km^2 \cdot h \rfloor$ ) concerning trips that arrive from circular (Figure A1e) and radial roads (Figure A1f). Similar to Stage 1, the majority of attracted trips from circular roads are around the central area, whereas the most density of radial trips is in external zones [14].

#### Appendix B.2 Parameters

Table A4 shows the parameter list of both types of vehicles used by the model. Our model considers that the value of travel time will be equal for each type of car users [14]. The average value is based on Litman's report [33].

In arterial roads, the capacity of urban roads depends on the intersection capacity [21]. AACC allows the formation of platoons, although the headway could improve if the cars have CACC. In the current scheme with only MVs, the capacity of streets is 1,272 per lane  $(k_{w,v})$  [21]. In a future scenario with AVs, the road capacity will be 3,960  $(k_{w,v})$ ; it is three times bigger than the present scenario as stated in Lioris et al. [21]. For freeways, the investigations show that MVs can reach the capacity of 2,099 [veh/lane·h]. On the other hand, AACC vehicles will increase the road capacity about 7% if the ratio of AACC is between 40% and 60% [18,19], while the CACC vehicles increase the capacity about 102% when all vehicles are communicated (4,259 [veh/lane·h]). Therefore, in the modeling, the case of AVs includes the connected and automated vehicles (CAVs). In the modeling, arterial roads have six lanes and freeways have eight lanes. The lanes will distribute between MVs and AVs because of the number of lanes depends on the type of road and the penetration of AVs. In AV lanes, these cars will form platoons.

Р	arameters	Case of MVs	Case of CAVs
Т	(h)	1.5	1.5
$\mu_v$	(\$/h)	10	8
$v_v^F$	(km/h)	25	30
$v_{w,v}^{ff}$	(km/h)	<i>a</i> : 45; <i>f</i> : 95	<i>a</i> : 50; <i>f</i> : 100
$v_v^{\acute{p}}$	(km/h)	10	30
$v^a$	(km/h)	3	3
$t_{w,v}$	(h)	<i>a</i> : 45/3600; <i>f</i> : 5/60	a: 45/3600; f: 5/60
а		2	2
b		3	3
$k_{w,v}$	(veh/lane∙h)	<i>a</i> : 1,272; <i>f</i> : 2,099	<i>a</i> : 3,960; <i>f</i> : 4,259
$\eta_w$	(lane)	$a: [0 \dots 6]; f: [0 \dots 8]$	$a: [0 \dots 6]; f: [0 \dots 8]$
$\tau^i_{w,v}$	(h/veh)	<i>a</i> : 0.0125; <i>f</i> : 0	<i>a</i> : 0.0125·70%; <i>f</i> : 0
$\lambda_P$	(parking/km)	5	5
$d_p$	(km)	0.2	0.0
$\varphi_v^t$	(\$/km∙veh)	0.1	$0.1 \cdot 50\%$
$\varphi^p$	(\$/h·veh)	1	1
$\varphi^{h(f)}_{w,v}$	(\$/km)	<i>a</i> : $5.680 \cdot 10^6$ ; <i>f</i> : 10.85 \cdot 10^6	$arphi^{h(f)}_{w,MV}$ ·1.25
$\varphi^{h(v)}_{w,v}$	(\$/km·h)	$arphi^{h(f)}_{w,MV}{\cdot}1\%$	$arphi^{h(v)}_{w,MV}$ ·1.25

Table A4. Parameters used in each scenario.

We assume that the mileage in MVs is 10 km/L and the fuel price is 1 \$/L. Moreover, we assume AVs will save 50% in comparison to a conventional car [34]. Moreover, we assume that the parking fee is  $\varphi^p = 1$  [\$/veh·h]. Furthermore, the fixed unit cost value is based on the paved cost per linear meter built, and the lifetime of the road project divides it. The cost per kilometer is based on technical

reports of Arkansas's Department of Transportation [35]. The variable unitary cost can be considered as the 1% of fixed cost ( $\varphi^{h(v)} = 0.01 \cdot \varphi^{h(f)}$  [\$/km·h]). Finally, we assume that the infrastructure cost for AVs is 25% more expensive than the infrastructure for MVs.

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