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Framework for a Systematic Parametric Analysis to Maximize Energy Output of PV Modules Using an Experimental Design

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Abstract: Use of photovoltaic modules in buildings has been reported to be an effective tool in managing energy consumption. The novelty in the research herein is in a framework that integrates different performance parameters through the use of an experimental design to expect all variables via linear regression analysis. An emphasis is placed on making the method readily available to practitioners and experts in the area of renewable energy, using standard procedure and easily accessible software. This work empowers the decision-making process and sustainability through a parametric analysis of the installation of photovoltaic modules to increase their energy output towards nearly zero energy buildings. A case study of a group of photovoltaic modules is examined in four cities with different locations and climate data to validate the proposed framework. Results demonstrate that the installation of photovoltaic modules on the mounted roof is better than elevations, and the vertical installation of modules is the worst possible inclination to maximize the yielded energy. The impact of inclination is higher than orientation in influencing the energy productivity of photovoltaic modules. This work specifies integrating such modules mounted on roofs and elevations towards the equator line, by a proportion of inclination/latitude equal to 85 ± 3%, to maximize the energy output.

Keywords: photovoltaic modules; building integrated photovoltaic system; energy consumption; experimental design; nearly zero energy buildings

1. Introduction

The construction sector is renowned for its high consumption of energy and natural resources [1]. It is reported to be responsible for almost 30% of annual greenhouse gas (GHG) emissions and 34×10^6 Gigawatt-hours of total energy consumption worldwide, making it one of the top contributors to pollution [2], and causing several environmental impacts, such as global warming [3]. Soaring rates of urbanization will also exacerbate the issue even further, leading to an increase in energy consumption and GHG emissions [4]. Worldwide access to electricity has increased from around 73% in 1990 to 85% in 2014 [5]. The identification of sustainable energy solutions is a crucial need to enhance the effectiveness of energy consumption within the built environment [6], hence, it is highly important to understand the concept and the structure of future energy utilization [7].

The global desire for renewable energy systems witnessed an unprecedented upsurge in its uptake since 2014 [8], due to the augmentation of the global debate on energy costs and consumption rates [9]. Renewable energy systems provide a range of options for meeting the mounting demand for energy, particularly in a sustainable context that considers social and environmental aspects when planning the consumption of energy [10]. Specifically, solar energy is considered to be one of the most important renewable energy sources [11]; it can be converted into a useful form of energy using photovoltaic (PV) modules [12]. The focus of this study is hence on incorporating the installation of PV modules in a complete Building Integrated Photovoltaic (BIPV) system to increase energy efficiency in buildings and aid their transformation towards nearly zero energy buildings (nZEBs).

Although several aspects regarding the performance and design of PV modules have been examined in the literature, a systematic procedure for the assessment of critical performance and design parameters for installation of PV modules that can be easily accessed by practitioners is required, particularly, the orientation and inclination parameters [13]. In an attempt to address this, factorial design analysis, along with a visualization aid, for designing solar energy systems for buildings are adopted in order to assess and choose the best installation of PV modules at various inclinations and orientations on roofs and elevations of buildings. Enhancing the energy output (EO) of PV modules is conducted through a simulation and parametric analysis approach. Initially, an experimental design, which involves a systematic collection of data, is utilized to focus on the planning of the installation process itself rather than defining the coefficients of the design factors, based on a linear regression analysis. Such method helps to model all expected technical variables that maximize the performance of PV modules [14].

The novelty of this paper is to establish a framework that captures different performance parameters and design factors that determine the design energy efficiency of PV modules in a complete BIPV system. A reliance is on the use of standard procedure and software that make the work readily available to practitioners and experts in the area of renewable energy. PV*Sol software validates the extracted results and facilitates the selection process of the desired PV module by relying on the MeteoSyn climate database that contains thousands of global climate datasets and the use of an online component database that involves thousands of modules and inverters [15]. A case study of a group of PV modules is examined in different cities with varying irradiations, latitudes, and climate data to validate the developed methodological framework; the energy efficiency of PV modules in a complete BIPV system is examined, taking into consideration the energy produced, the installed capacity, and the potential of optimizing the EO of PV modules.

2. Background

In this section, a description of the components of a complete BIPV system is given. Moreover, a related literature review to the recent publications in the same field of the study is presented.
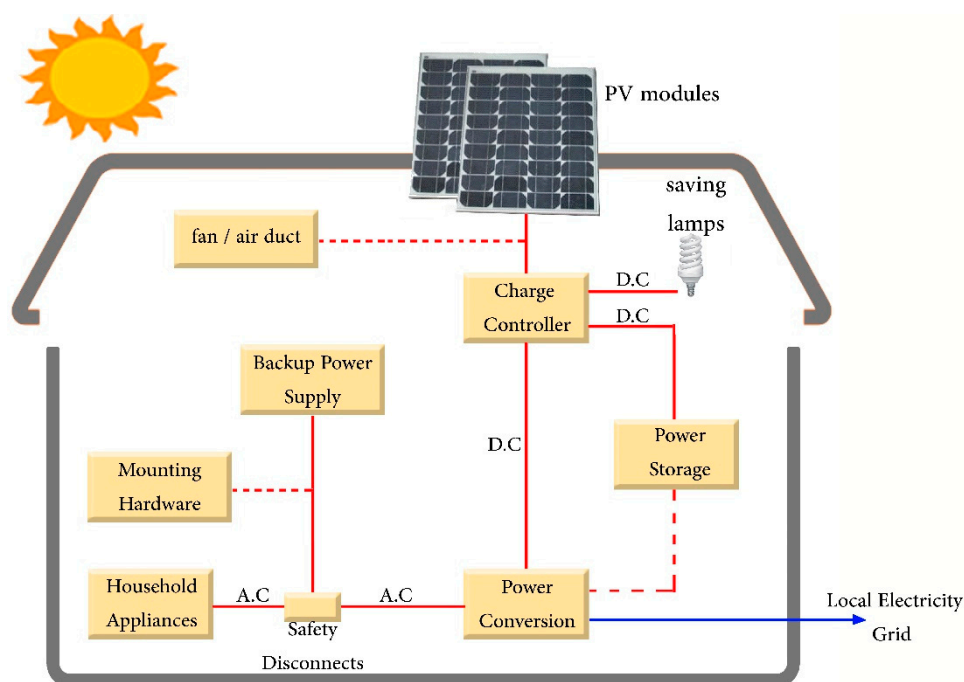
2.1. Components of a BIPV System

The built environment allows several forms of PV modules to be integrated into different parts of the structure of buildings, such as roofs, windows and semitransparent facades, facades, skylights, and shading systems [16]. The successful installation of BIPV systems necessitates the cooperation of both the functional and aesthetic issues within the financial constraints [17]. BIPV systems provide weather and sun protection, thermal insulation, noise protection, electromagnetic shielding, aesthetic quality, visual cover, and safety for construction projects. This comes back to the fact that the conventional building materials that are covering the final roof or façades of the building are being replaced by PV modules [18].

PV modules are classified into three generations based on the basic material used and the level of commercial maturity. The first-generation systems are the wafer-based crystalline silicon (c-Si), the most used material in the PV industry [19,20]. In 2013, c-Si wafers presented 91% of the total share in the global market of PV systems [21], and within the European Union, they accounted for around 85% of all

new PV systems installed [22]. C-Si modules are basically manufactured using two common materials: Poly-crystalline (p-Si) and mono-crystalline (mono-Si); mono-Si occupies less space and has the ability to produce higher energy output compared to p-Si; mono-Si is less affected by high temperatures compared to p-Si, which has a shorter lifespan. The choice between these two types depends mainly on the climate data of the installed region; the efficiency rate of mono-Si is higher than p-Si—20% and 15%, respectively—however, p-Si is cheaper than mono-Si. [23]. The second-generation systems use thin-film technology, such as cadmium telluride solar cell (CdTe) [24]. This generation is the most efficient among all other generations if they face the sun at a perfect angle [25]. The third-generation systems use other technologies such as thin-film solar cells (TFSC) [25]. The advantage of this generation is that the modules are less affected by high temperatures and allow opportunities for better alternative installation, however, they occupy more space and have a shorter lifespan compared to the first generation [24].

The basic components of a BIPV system are presented in Figure 1, including the PV modules, a charge controller, a power storage system, a power conversion equipment, a backup power supply, and appropriate supports, such as mounting hardware, wiring, and safety disconnects [19,20], in addition to a fan and air duct, which are optional components that help reduce the heating load in winter by drawing the heated air into the space [18]. The characteristic parameters of PV modules are measured under standard test conditions that require defining the solar irradiance, module temperature, and wind speed [26]. The PV modules can be first, second, or third generation [19], while a power storage system can refer to the utility grid itself or the number of batteries [27]. The charge controller can provide and reduce the pure flow of power energy to the utility grid [28]. The charge controller regulates the power into and out of the power storage. The power conversion equipment, such as an inverter, converts the output direct current (D.C) energy of PV modules to output alternating current (A.C) energy that is used for household appliances. The inverter is a piece of very important equipment that operates the power energy in the utility grid and delivers the maximum power to the electric power grid [29]. The backup power supply is optional equipment, such as a diesel generator, used for providing the necessary power when the input power source fails [20]. However, ensuring the safety of the instalment of PV modules and the reliability of the utility grid are two major technical requirements that need to be satisfied when installing a complete BIPV system [18].

Figure 1. The basic components of a complete Building Integrated Photovoltaic system.

The grid-interconnection of PV modules in a BIPV system can be designed in three main circumstances [28]: (i) Grid-connected without storage; (ii) grid-connected with storage; and (iii) off-grid with storage. The EO of PV modules in any of these circumstances can be influenced by several factors, such as the characteristics of the components of the PV modules, their geographical location, and the installation variables, as well as the local solar radiation [29]. The successful installation of such modules facilitates the achievement of ambitious energy targets [30], where the generated energy can be stored in the power storage as a D.C energy or can be converted by the power conversion to A.C energy. At this level, the A.C energy is ready to be consumed directly or fed into the local energy grid if it accepts such an interconnection agreement [31], as illustrated in the blue line in Figure 1, where the excess renewable energy generated can be transferred to the local electricity grid; it is rated by a policy mechanism called "feed-in tariffs" [32]. This mechanism is considered the most effective policy that stimulates the rapid development of renewable energy sources and has been implemented in several regions worldwide [33].

2.2. Related Literature

Renewable energy systems appear as sustainable and alternative energy forms; they are extensively utilized in nearly Zero Energy Buildings (nZEBs) to reduce the consumption of energy and, consequently, reduce the environmental impacts associated with climate change [34]. Several publications in the literature have been dedicated to evaluating the performance of PV modules from different aspects. This section reviews the recent academic papers of PV performance evaluation based on three axes of literature: (i) The application of PV modules towards sustainability; (ii) the factors that are influencing the performance of PV modules; and (iii) the recent trends to optimize the application of PV modules.

First, several publications observed the use of PV modules towards more sustainable built environment, such as D'Adamo [35], who analysed the profitability of residential PV systems as the main resource towards the clean global economy of the future. This work stimulated a new diffusion of PV plants, considering the output energy over 20 years. The author found that PV modules are important alternatives to improve environmental impacts and reduce the dependence on fossil fuels. Similarly, Ferreira et al. [36] conducted an economic overview of the application and production of PV modules in Brazil and observed that the energy generation of PV modules is a convenient alternative to the diversification of the energy matrix in the country. Khan and Arsalan [37] reviewed the technologies of solar PV modules towards sustainable electricity generation, taking into consideration their types, efficiency, cost factors, and mechanism. The authors indicated that the mature technology of PV modules is well-suited for all scale applications, and is more commercially developed in addition to the fact that PV modules are a major source of clean energy as they have the potential to supply the global increasing requirements of electricity. In addition to this, Stropnik and Stritih [38] studied methods for increasing the electrical efficiency and power output of PV panels using phase change materials (PCM). The authors focused on the experimental setup and simulation heat extraction from PV panels to evaluate the PV-PCM integration in a Canadian city and found that the annual energy efficiency could increase by more than 7% in the city. Traverso et al. [39] evaluated the sustainability assessment performance of the assembly production of p-Si PV modules in order to compare their life cycle sustainability assessment (LCSA). The authors indicated that LCSA methodology empowers the decision-making process of the different stakeholders towards the more sustainable performance of PV modules.

Second, some authors highlighted several factors that are influencing the application and, consequently, the EO of PV modules. For instance, the geographical location of the application site, where the longer sunshine hours of high-latitude regions result in better EO of PV modules than shorter sunshine hours of low-latitude regions [40]. You et al. [3] compared the environmental efficiency of four PV plants in China, including a mountain plant, desert plant, rooftop plant, and complementary plant. Taking into consideration several input variables (i.e., insolation, covering area, and annual sunshine duration) and output variables (i.e., annual electricity generation, the installed capacity, coal saving,

and CO_2 emission reduction), the authors found that there is a difference in the performance of PV plants. However, serious aerosol pollution and the high urbanization rate are the main agents of the inefficiencies of the output energy of these plants. Carstens and Cunha [41] identified the challenges and opportunities of PV use in Brazil, considering two main approaches: The multilevel perspective and the functions of the innovation system. The authors found that the vast territory and the high solar irradiance play a basic role in improving the EO of PV modules, while the lack of new technology development, the shortage of skilled professionals, and insufficient knowledge transfer are the main challenges of implementing PV modules.

Third, some authors proposed a new model for the optimum tilt angle of a soiled PV module. They found that the cell temperature of a PV panel and the tilt angle are key factors to evaluate the power output of PV modules [42]. Another study investigated the PV panels' optimum tilt angles for various cities in the Kingdom of Saudi Arabia. The authors used MATLAB software to optimize the tilt angle by maximizing solar radiation, considering the experimental work to validate the theoretical requirement for negative tilt angles during summer. The authors concluded that adjusting tilt angles six times per year harvests 99.5% of the solar radiation that could be achieved with daily PV panel adjustment [43]. Yu et al. [13] established a database to optimize the PV applications in Japan. The authors focused on the orientations and inclinations of installing PV modules as two major factors to achieve the aim of their study, while Han and Kim [44] developed an optimization-based framework to design renewable energy systems for the residential sector in Korea.

Furthermore, Gunerhan and Hepbasli [45], and Benghanem [46] in their studies indicated that the yearly optimum inclination of PV modules is nearly equal to the latitude of the installation site. Landau [47] examined the optimum inclination of PV modules in various cities around the world as shown in Table 1. The author suggested several formulae to find the best inclination at which the panel should be tilted. This work used a proportion of the best inclination compared to the latitude. At this level of the analysis, the results presented in Table 1 are collected from the proportion of dividing the optimum inclination of PV modules, suggested by Landau, for each city by the representative latitude, individually, ((inclination/latitude) × 100).

Table 1. The optimum inclination of photovoltaic modules in various cities [47], and the proportion of the best inclination compared to the latitude (adapted by the authors).

City	Optimum PV Module Inclination	Proportion of the Best Inclination Compared to the Latitude	City	Optimum PV Module Inclination	Proportion of the Best Inclination Compared to the Latitude
Winnipeg	41.1	82%	Houston	25.9	86%
Prague	41.1	82%	Cairo	25.9	86%
Minneapolis	37.3	83%	Dakar	13.1	87%
Milano	37.3	83%	Caracas	8.7	87%
Madrid	33.5	84%	Mérida	17.4	87%
Denver	33.5	84%	Bogotá	4.4	88%
Albuquerque	29.7	85%	Key West	22.1	88%
Tokyo	29.7	85%	Taipei	22.1	88%

Accordingly, it is apparent that an emphasis is placed in the literature on the optimization of certain design factors associated with the installation of PV modules, such as the orientation and inclination. Nevertheless, there is little focus on the development of a methodological framework that could integrate such installation in buildings using the experimental design on the one hand, and optimizing the EO of PV modules in a complete BIPV system by indicating the best geographic orientation and inclination, on the other hand. In the next section, the proposed framework to cover this apparent gap in the literature is presented.
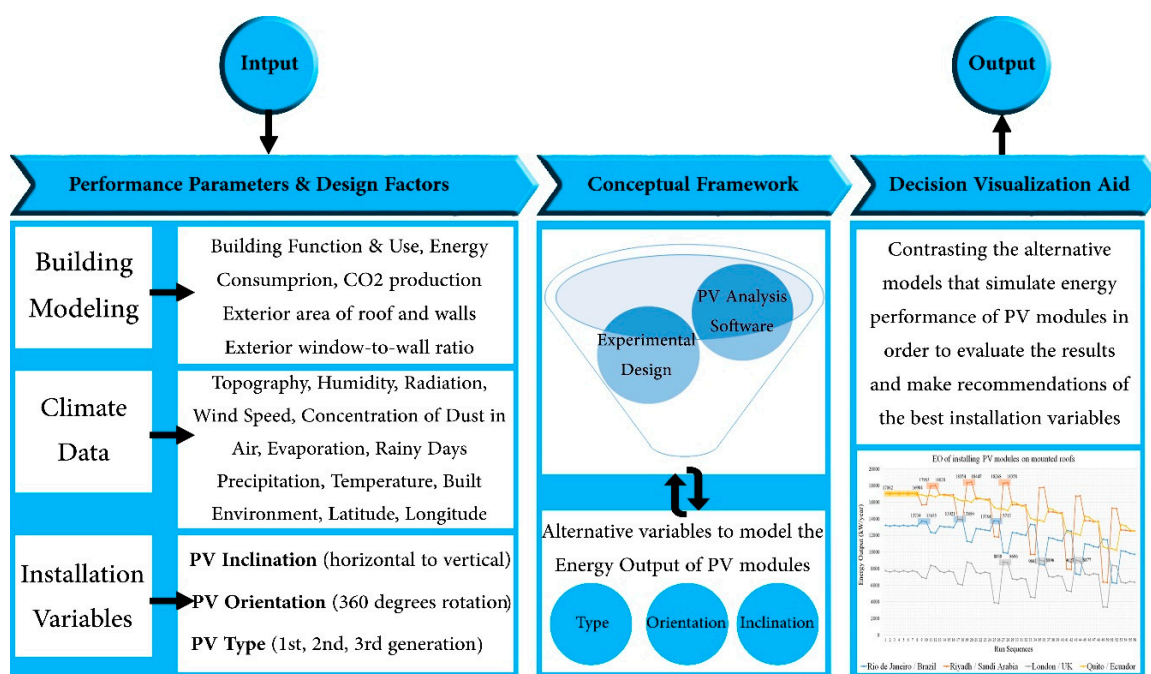
Furthermore, several studies in the literature have evaluated the energy performance of renewable energy systems based on the use of yearly data. Researchers that implemented this common practice include Bellos and Tzivanidis [48], Hasan et al. [49], Pillai et al. [50], Kim and Lim [51], and Han et al. [52].

Additionally, Autodesk reviewed the energy analysis and summarized the amount of electricity that a building site could produce using solar panels and wind turbines based on the use of yearly data [53,54]. Thus, the proposed framework in this work will be demonstrated on yearly data, but the same concept can still be extended for other temporal data as well.

3. Materials and Methods

A novel framework is proposed and highlighted in Figure 2, where the link between performance parameters and design factors is outlined. The installation of PV modules in a BIPV system requires the identification of various performance parameters and their associated design factors. Performance parameters refer to the characteristics that are defining and classifying a particular system in the model, while design factors are features and variables that define the performance parameters, and these are displayed in Figure 2, including building modelling, climate data, and PV module installation. Evaluating the parameters of PV module installation that are influencing their EO is the concern of this study. However, the next subsections highlight the main components of the proposed framework.

Figure 2. A methodological framework for installing PV modules in a BIPV system.

3.1. Performance Parameters and Design Factors

The initial step in the proposed approach is the integration of a number of performance parameters that impact the operation phase EO of PV modules. In these terms, the building modelling parameter means recognizing the type of building design (the design of the final roof and elevations) [32]. The design factors relevant to this parameter include: (i) The identification of the function and use of the building; (ii) type of energy use and consumption; (iii) CO_2 production; (iv) exterior area of roof and walls; and (v) the exterior window-to-wall ratio associated with the building [55–57]. Examples of the associated design features of the climate data parameter include the topography, humidity level, solar radiation, wind speed, the concentration of dust in the air, evaporation, rainy days, precipitation, temperature, built environment, latitude, and longitude of the exact location where the PV modules are to be installed [58–60]. The third performance parameter of the proposed framework of this study is PV module installation, which means defining the model of the installed panels, quantity, and installation variables (i.e., PV type, PV inclination, and PV orientation) [29].

The geographic orientation and inclination are two vital installation variables playing a fundamental role in the installation of PV modules in a successful BIPV system [61]. Determining the PV orientation involves analysing the wind, rain, and site conditions in order to define the best geographic orientation for the PV modules [62,63]. The PV inclination refers to the analysis of the sun movement and latitude in order to identify the preferable inclination of the PV modules [64,65]. It is reported that the performance of PV modules is affected by the orientation and inclination, which are the main factors influencing the amount of solar energy incident upon the surface of the PV module [66]. Thus, this work will focus on these two installation variables. In addition, the PV type is another parameter to be considered to validate the impact on the energy yielded from the installed module [20]. The proposed methodological framework of this analysis can accommodate a large number of PV inclinations (i.e., from horizontal to vertical inclination) and PV orientations (i.e., 360 degrees rotation) as well as the available PV types on the local market. However, some specific PV types, PV inclination, and PV orientation are chosen in the case study, shown in Section 5, to validate the proposed framework.

3.2. Evaluation Method

This step starts by evaluating the collected database of energy consumption and output emissions using indicators of sustainability, which can lead to better decisions and more actions that are effective. This is achieved by simplifying, clarifying, and making aggregated information available to policy makers. Hence, sustainability indicators are used to calibrate the progress toward sustainable development goals by communicating the thoughts and values of the collected results [67]. The methodology of this study makes use of an experimental design procedure to indicate the best geographic orientation and inclination of PV modules in buildings. The experimental design work, which was applied via linear regression, is based on a parametric analysis that examines different values for several design factors related to the PV type, PV orientation, and PV inclination. Such a process provides maximum information at minimum experimental cost [68]. This work examines the performance of PV modules at various types, inclinations, and orientations to support policy makers in planning the features required to be targeted when installing such energy sources. Hence, the expected variables generated via the experimental design were accommodated individually and evaluated using PV*Sol software to integrate the installation process of PV modules and estimate the EO of PV modules installed in a complete BIPV system [15]. This software allows the simulation of PV systems and facilitates the process of design and analysis of grid connected PV systems [69]. In the literature, PV*Sol software has been applied as a PV analysis software to validate such results and design and model the performance of PV systems and low-energy solar buildings [70,71].

3.3. Decision Visualization Aid

The last step of the methodological framework of this study is to evaluate the collected results by contrasting the alternative models that simulate the energy performance of PV modules to define the best installation variables that could improve their energy efficiency. This process starts by clarifying and classifying sources of data, comparing results, and suggesting recommendations and new design options. Changes to the variables in experimental design were evaluated using software, such as Minitab. This software was used for determining all the expected variables of the experimental design work and to define the coefficients of the design factors through a linear regression analysis [72].

4. Linking Framework Components

In terms of the required analysis, the first step is to identify the size of the case study, which means identifying the amount, weight, and quality of the specific product investigated (i.e., building), as shown in Figure 3.
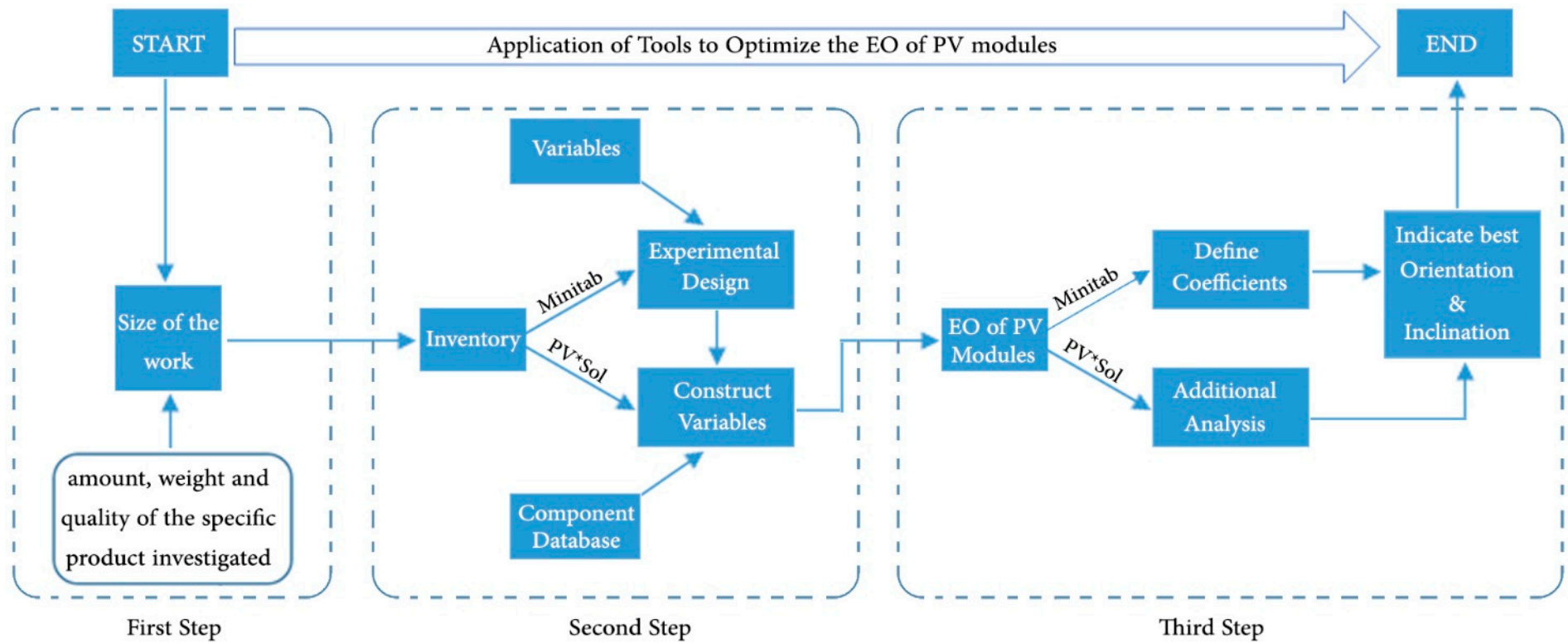
Figure 3. Linking framework components.

The second step is to build the inventory of database. The proposed framework applies an experimental design to estimate all the expected variables using a parametric analysis based on linear regression. At this level of the analysis, the interaction effects are found by the use of statistical factorial design technique [73]. This involves running a full complement of all possible factor combinations and estimating all the interaction effects, through knowing the number of factors (κ) and the number of levels for each factor. A factorial design model is presented in Equation (1) that allows the estimation of all coefficients ($\beta_0, \dots, \beta_\kappa$) [14,74]:

$$\Upsilon = \beta_0 + \beta_1.\chi_1 + \beta_2.\chi_2 + \dots + \beta_\kappa.\chi_\kappa + \epsilon. \tag{1}$$

Though Equation (1) calculates all the actual responses and interactions of the expected variables [74], in the experimental design, errors are inevitable [75]. Minitab is used to estimate all the expected variables and reduce regression errors and uncertainty [72]. The variables of the experiment are then examined using PV analysis software. This work utilized PV*Sol software to construct the determined variables, individually, and estimate the EO of PV modules [76]. PV*Sol software relies on the MeteoSyn climate database, which contains thousands of global climate datasets. In addition, an online component database that contains thousands of modules and inverters used [15] in order to sort out files and, accordingly, facilitate the selection process of the desired module or inverter type [77]. Collecting a reliable dataset requires assessing the following parameters:

i.　System, climate data, and grid: For system, this involves recognizing the type of building design (basically the design of the final roof and elevations); for climate, this is related to obtaining the climate data associated with each region analysed, and identifying the exact location where the PV modules are to be installed, in order to determine the latitude, longitude, annual sum of global irradiation, and annual average temperature; and for grid, this involves determining the usage voltages and phase system of electricity.

ii.　PV modules: This refers to defining the model of the examined PV module, the number of PV modules, installation type, inclination, orientation, shading, and degradation of the module.

iii.　Inverters: This refers to selecting the configurations, determining the values of the configuration module, and the number of inverters.

iv.　Cables: This is associated with calculating the loss of energy in cables, based on their length and thickness, through consideration of the distances between the various components of the BIPV system.

The third step is to evaluate the collected database in order to calculate the EO of PV modules. At this level of the analysis, the collected results of the PV analysis software are evaluated in two phases. First, the results are transferred to the experimental design software to define the coefficients of the assigned design factors through linear regression analysis [72]. Second, analysis of additional PV modules mounted on the roof is conducted to define the specific inclinations that would maximize the EO of the PV modules. This stage requires running another analysis in the *PV*Sol* software to specify the best inclinations. Conducting such an analysis demands a parametric analysis involving gradual increments of inclinations.

5. Case Example: Installation of PV Modules in a Complete BIPV System

The applied case study aims to validate the proposed framework used to model the decisions involved in installing PV modules in a complete BIPV system. In order to showcase the versatility of the proposed framework, the proposed analysis of the installation of PV modules was conducted in four different cities with differing climate data, latitude, longitude, annual average temperatures, and global annual irradiation. The chosen cities include Rio de Janeiro in Brazil, Riyadh in Saudi Arabia, London in the United Kingdom, and Quito in Ecuador. The choice of these cities was made to ensure comprehensive consideration of various climatic conditions. Rio de Janeiro is located down the

equator to the west side of the Greenwich, at a latitude of 22° and longitude of 43°. Riyadh is located up the equator to the east side of the Greenwich, at a latitude of 24° and longitude of 46°. London is located on the north side of the equator on the Greenwich, while Quito is located to the west side of the Greenwich directly on the equator.

It is important to note that Rio de Janeiro and Riyadh are almost located on a symmetric location with respect to the Greenwich and equator. Rio de Janeiro has a tropical climate, while the climate of Riyadh is characterized as dry [78,79]. London and Quito have moist subtropical climates [78–80]. In particular, the choice of including Riyadh and London in the study is to analyse the impact of differing climate conditions between the cities, where other performance parameters are near identical, on the total sum of EO of PV modules.

5.1. Size of the Case Study

The case study of this work examines the installation of 100 PV modules, considering two types of 100 W PV modules of the first generation systems, namely poly-crystalline (p-Si) and mono-crystalline (mono-Si), that are commonly adopted worldwide. The parametric analysis considers a range of different inclinations of PV modules mounted on roofs and elevations, which is subsequently incremented by 10° (0, 10, 20, 30, 40, 50, and 60°) based on the four cardinal directions (i.e., North, South, East, and West). An option of integrating PV modules on the exterior walls of elevations at a vertical inclination (90°) was also examined.

5.2. Inventory of Database

The inventory of the database focuses on the operation phase of the case study and was constructed through three main steps based on the guidelines provided in Section 4.

First, the assigned design factors that were determined in the case study, Table 2, were integrated into a linear statistical regression using Minitab software to cover all the expected variables of the experimental design, using three factors within different levels. This is known as a mixed-level design or general full factorial design [14]. The first factor is the PV type (PV_T), consisting of two levels which consider the most known types of PV modules of the first generation system (p-Si and mono-Si). The second factor is the PV orientation (PV_O), which consists of four levels, associated with the four cardinal directions. The third factor is the PV inclination (PV_I), which is considered via two scenarios, namely scenario A and scenario B. Scenario A is associated with seven levels while scenario B is comprised of eight levels; both scenarios consider the various inclinations between the horizontal and vertical positioning of the installation of PV modules within an increment of 10°, as displayed in Table 2. However, this step considers the same distances between the PV modules, disregarding the shading impacts.

The model for such an experiment analysis is presented in Equation (2). The number of sequences for each experiment based on a single iteration will be the result of multiplying the number of levels associated with each factorial design considered within a single analysis together [81]. As an example, the number of sequences that are required to cover all the expected variables on roof mounting installations is 56 ($2 \times 4 \times 7$) whereas at elevation, it is 64 ($2 \times 4 \times 8$). Applying Equation (2) in the case study example of this work results in the following:

$$EO = \beta_0 + \beta_1.PV_T + \beta_2.PV_O + \beta_3.PV_I + \beta_{12}.PV_T \times PV_O + \beta_{13}.PV_T \times PV_I + \beta_{23}.PV_O \times PV_I + \beta_{123}.PV_T \times PV_O \times PV_I + \epsilon. \quad (2)$$

An interaction between the assigned factors that are defining the functional unit is achieved to simulate all expected variables. The effects of such interaction are found only by the use of a statistical factorial design technique, as described in the work of Fegade et al. [73]. The EO response based on the main effects of PV_T, PV_O, and PV_I is captured, in terms of ($PV_T \times PV_O$), ($PV_T \times PV_I$), ($PV_O \times PV_I$), and ($PV_T \times PV_O \times PV_I$); these terms were included to consider all possible interactions between the main variables. The constant, β_0, is the response of EO when all main effects are equal to 0, while β_1, β_2,

β_3, β_{12}, β_{13}, β_{23}, and β_{123} denote the unknown parameters to be estimated. The variable, ϵ, refers to the experimental error.

Second, PV*Sol software was applied to estimate the EO of PV modules based on the running sequences that were previously built in the regression model. At this step, the database for each sequence was constructed individually. This means that a total of 120 (56 (for roof − mounted installements) + 64 (for elevation installment)) separate analyses were performed in this software.

Third, the collected results in the PV*Sol software were integrated into Minitab software in order to evaluate the collected data and estimate the coefficients of the various effects of design factors, based on the EO of PV modules in the chosen cities. Furthermore, an additional and more specific examination of the EO of PV modules mounted on roofs was conducted based on the best geographic orientation of PV modules and the range of optimum inclinations in the chosen cities. This additional examination applied the same PV types as mentioned in Table 2, while it only considered the PV orientations that would optimize the EO of PV modules for each city, individually, taking into consideration a 1° increment to the inclination angle in order to quantify the best choice for positioning the PV modules.

Table 2. The assigned factors defining the functional unit.

PV_T	PV_O	PV_{IA}	PV_{IB}
p-Si 100 W (1)	North (1)	0° (1)	0° (1)
mono-Si 100 W (2)	South (2)	10° (2)	10° (2)
	East (3)	20° (3)	20° (3)
	West (4)	30° (4)	30° (4)
		40° (5)	40° (5)
		50° (6)	50° (6)
		60° (7)	60° (7)
			90° (8)

5.3. Assessment of Design Factors

The experimental design was applied at this level of the analysis to clarify the various effects of the assigned design factors. Tables 3 and 4 present the estimated values of the EO of PV modules in a complete BIPV system mounted on roofs and elevations, respectively.

The results of the regression equation, regression errors, and coefficients are fully presented in the supplementary file. Moreover, the supplementary file illustrates the main effects plot of installing PV modules on mounted roofs (Figures S1–S4) and elevations (Figures S5–S8). The presented information in this file shows that there is no error (error = 0) in building up the analysis of variance in the four examined cities. The estimated coefficients of the assigned factorial designs, which are shown in Figure 4, were analysed in Minitab software based on the collected EO results in the four cities. Figure 4 indicates the factors that have the most influence on the energy efficiency of the PV modules, where PV_{IA} and PV_{IB} refer to the factorial impact of the PV inclination based on scenarios A and B, respectively; PV_O refers to the factorial impact of the PV orientation; PV_T refers to the factorial impact of the PV type; PV_O:PV_{IA} and PV_O:PV_{IB} refer to the factorial impact of the interaction between the PV orientation and PV inclination based on scenarios A and B, respectively; PV_T:PV_{IA} and PV_T:PV_{IB} refer to the factorial impact of the interaction between the PV type and PV inclination based on scenarios A and B, respectively; PV_T:PV_O refers to the factorial impact of the interaction between the PV type and PV orientation; and PV_T:PV_T:PV_{IA} and PV_T:PV_T:PV_{IB} refer to the factorial impact of the interaction between the PV type, PV orientation, and PV inclination based on scenarios A and B, respectively. As can be noticed from Figure 4, PV_{IA} and PV_{IB} have the highest influence regarding the generation of EO for roof mounted instalment and elevations, respectively, while PV_O is the second factor that could affect the EO in such models. The third factor that could affect the EO of PV modules is the interaction between the orientation and inclination, while the lowest one is the interaction between the type and the inclination. Yet, the type of PV modules comes as the fourth factor that could influence the EO of PV modules.
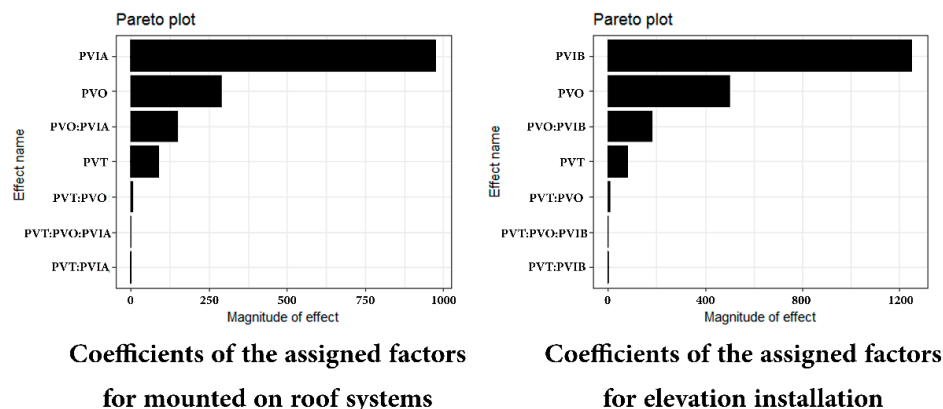
Table 3. Energy output of PV modules mounted on roofs based on the assigned design factors.

Run Sequence	Factorial Designs			EO (kWh/Year)			
	PV_T	PV_O	PV_{IA}	Rio de Janeiro/Brazil	Riyadh/Saudi Arabia	London/United Kingdom	Quito/Ecuador
1	1	1	1	13,221	17,060	7758	17,062
2	2	1	1	13,129	17,102	7601	16,904
3	1	2	1	13,221	17,060	7758	17,062
4	2	2	1	13,129	17,102	7601	16,904
5	1	3	1	13,221	17,060	7758	17,062
6	2	3	1	13,129	17,102	7601	16,904
7	1	4	1	13,221	17,060	7758	17,062
8	2	4	1	13,129	17,102	7601	16,904
9	1	1	2	13,734	15,699	6973	16,891
10	2	1	2	13,655	15,702	6825	16,733
11	1	2	2	12,386	17,953	8381	16,817
12	2	2	2	12,280	18,028	8223	16,640
13	1	3	2	13,126	16,881	7690	16,963
14	2	3	2	13,036	16,919	7535	16,802
15	1	4	2	13,034	16,847	7716	16,806
16	2	4	2	12,944	16,894	7564	16,651
17	1	1	3	13,921	13,931	6163	16,324
18	2	1	3	13,850	13,901	6027	16,151
19	1	2	3	11,282	18,354	8801	16,180
20	2	2	3	11,164	18,447	8647	15,983
21	1	3	3	12,824	16,400	7551	16,585
22	2	3	3	12,737	16,435	7403	16,424
23	1	4	3	12,644	16,329	7594	16,299
24	2	4	3	12,556	16,381	7449	16,147
25	1	1	4	13,784	11,841	3896	15,371
26	2	1	4	13,712	11,794	3822	15,188
27	1	2	4	9949	18,268	8838	15,180
28	2	2	4	9830	18,358	8696	14,979
29	1	3	4	12,357	15,696	6781	16,030
30	2	3	4	12,273	15,724	6658	15,862
31	1	4	4	12,091	15,605	6846	15,562
32	2	4	4	12,005	15,656	6730	15,421
33	1	1	5	13,339	9731	4592	14,067
34	2	1	5	13,256	9681	4492	13,867
35	1	2	5	8544	17,730	9041	13,846
36	2	2	5	8433	17,795	8896	13,646
37	1	3	5	11,734	14,821	7107	15,252
38	2	3	5	11,650	14,835	6974	15,098
39	1	4	5	11,411	14,691	7165	14,715
40	2	4	5	11,327	14,734	7040	14,581
41	1	1	6	12,587	7952	5351	12,454
42	2	1	6	12,489	7895	5231	12,242
43	1	2	6	7365	16,731	9027	12,215
44	2	2	6	7260	16,754	8877	12,014
45	1	3	6	10,997	13,783	7359	14,318
46	2	3	6	10,910	13,778	7219	14,177
47	1	4	6	10,653	13,652	7411	13,740
48	2	4	6	10,567	13,680	7276	13,612
49	1	1	7	11,554	6378	3398	10,659
50	2	1	7	11,440	6324	3345	10,445
51	1	2	7	6310	15,283	8432	10,414
52	2	2	7	6213	15,258	8291	10,215
53	1	3	7	10,160	12,656	6389	13,292
54	2	3	7	10,068	12,627	6273	13,162
55	1	4	7	9799	12,535	6453	12,646
56	2	4	7	9711	12,543	6346	12,525

Table 4. Energy output of PV modules on elevations based on the assigned design factors.

Run Sequence	Factorial Designs			EO (kWh/Year)			
	PV_T	PV_O	PV_{IB}	Rio de Janeiro/Brazil	Riyadh/Saudi Arabia	London/United Kingdom	Quito/Ecuador
1	1	1	1	13,186	16,684	7744	16,709
2	2	1	1	13,099	16,717	7590	16,563
3	1	2	1	13,186	16,684	7744	16,709
4	2	2	1	13,099	16,717	7590	16,563
5	1	3	1	13,186	16,684	7744	16,709
6	2	3	1	13,099	16,717	7590	16,563
7	1	4	1	13,186	16,684	7744	16,709
8	2	4	1	13,099	16,717	7590	16,563
9	1	1	2	13,696	15,352	6961	16,538
10	2	1	2	13,623	15,348	6816	16,390
11	1	2	2	12,355	17,558	8364	16,468
12	2	2	2	12,254	17,621	8209	16,309
13	1	3	2	13,091	16,509	7675	16,616
14	2	3	2	13,006	16,538	7524	16,473
15	1	4	2	13,000	16,475	7702	16,455
16	2	4	2	12,915	16,513	7552	16,313
17	1	1	3	13,882	13,622	6154	15,979
18	2	1	3	13,817	13,589	6019	15,820
19	1	2	3	11,256	17,951	8782	15,845
20	2	2	3	11,142	18,031	8632	15,668
21	1	3	3	12,790	16,038	7537	16,250
22	2	3	3	12,709	16,064	7392	16,106
23	1	4	3	12,611	15,968	7580	15,957
24	2	4	3	12,528	16,011	7438	15,817
25	1	1	4	13,746	11,810	3893	15,329
26	2	1	4	13,679	11,768	3820	15,154
27	1	2	4	9928	18,205	8818	15,140
28	2	2	4	9813	18,303	8680	14,948
29	1	3	4	12,325	15,646	6769	15,988
30	2	3	4	12,246	15,680	6648	15,830
31	1	4	4	12,060	15,555	6833	15,518
32	2	4	4	11,979	15,612	6719	15,386
33	1	1	5	13,303	9513	4587	13,761
34	2	1	5	13,226	9463	4489	13,563
35	1	2	5	8527	17,340	9020	13,549
36	2	2	5	8419	17,394	8879	13,355
37	1	3	5	11,704	14,493	7093	14,946
38	2	3	5	11,625	14,500	6964	14,800
39	1	4	5	11,383	14,365	7152	14,400
40	2	4	5	11,302	14,401	7029	14,273
41	1	1	6	12,554	7772	5344	12,180
42	2	1	6	12,461	7717	5225	11,970
43	1	2	6	7353	16,362	9007	11,946
44	2	2	6	7250	16,377	8861	11,749
45	1	3	6	10,970	13,477	7345	14,025
46	2	3	6	10,887	13,467	7207	13,891
47	1	4	6	10,627	13,348	7397	13,445
48	2	4	6	10,545	13,372	7265	13,323
49	1	1	7	11,527	6369	3395	10,637
50	2	1	7	11,417	6316	3343	10,427
51	1	2	7	6301	15,238	8414	10,392
52	2	2	7	6206	15,219	8277	10,197
53	1	3	7	10,137	12,620	6377	13,257
54	2	3	7	10,048	12,597	6264	13,134
55	1	4	7	9777	12,499	6441	12,612
56	2	4	7	9693	12,512	6337	12,497
57	1	1	8	7411	3515	2572	6134
58	2	1	8	7297	3509	2556	5975
59	1	2	8	3972	9269	6178	5994
60	2	2	8	3933	9160	6052	5844
61	1	3	8	7241	8880	4812	9544
62	2	3	8	7145	8792	4725	9398
63	1	4	8	7030	8843	4881	9182
64	2	4	8	6944	8789	4804	9045

Figure 4. Coefficients of the assigned factorial designs.

5.4. Evaluation of Results

After classifying and evaluating the results collected in the previous section, the aim is to highlight the best geographic orientation and inclination of PV modules that would increase the EO of the functional unit. Tables 3 and 4 display the results of the EO of PV modules that were installed in a complete BIPV system in the four examined cities. However, Figures 5 and 6 illustrate the same results in a way to facilitate the comparison of EO of PV modules between these cities. The two figures show that the installation of PV modules mounted on the roof would generate more EO than the installation of modules on elevations. Besides, they illustrate that the sequence number (9, 10, 17, 18, 25, and 26) maximizes the EO of PV modules in Rio de Janeiro. The sequence number (11, 12, 19, 20, 27, and 28) maximizes the EO of PV modules in Riyadh. The sequence number (27, 28, 35, 36, 43, and 44) maximizes the EO of PV modules in London. The sequence number (1, 2, 3, 4, 5, 6, 7, and 8) maximizes the EO of PV modules in Quito.

The analysis of the collected results presented in Figures 5 and 6 and the main effects plot for each city presented in the supplementary file (Figures S1–S8) are shown in Table 5, which identifies the basic conclusions yielded from the collected results in the case study. Several performance parameters are required to be considered in order to install PV modules in a complete BIPV system such as latitude, climate data, and building modelling. For example, the EO of PV modules increases in higher global annual irradiation sites and vice versa [82,83]. Table 5 illustrates that the vertical installation of PV modules on elevations is the worst inclination to maximize the EO. Moreover, it shows the best and worst geographic orientation for PV modules on roof mounting systems, and the preferable elevation of the building to install these modules in each city as follows:

In Rio de Janeiro, positioning PV modules towards the North orientation within a range of inclinations between 10° and 30° for mounted roof systems and elevations would maximize the EO of PV modules, while the South geographic orientation is the worst for the same installation. The Northern façade is the best orientation for installing PV modules, while the Eastern and Western façades are the second and third preferable orientations, respectively.

In Riyadh, positioning the PV modules at the Southern orientation within a range of inclinations between 10° and 30° for mounted roof systems and elevations would maximize the EO of PV modules, while the North geographic orientation is the worst for the same installation. The Southern façade is the best orientation to install PV modules, while the Eastern and Western façades are the second and third preferable ones, respectively.

In London, positioning the PV modules at the Southern orientation within a range of inclinations between 30° and 50° for mounted roof systems and elevations would maximize the EO of PV modules, while the North geographic orientation is the worst for the same installation. The Southern façade is the best orientation for installing PV modules, while the Western and Eastern façades are the second and third preferable elevations, respectively. It is estimated that the EO of PV modules installed on any of these facades is equal.
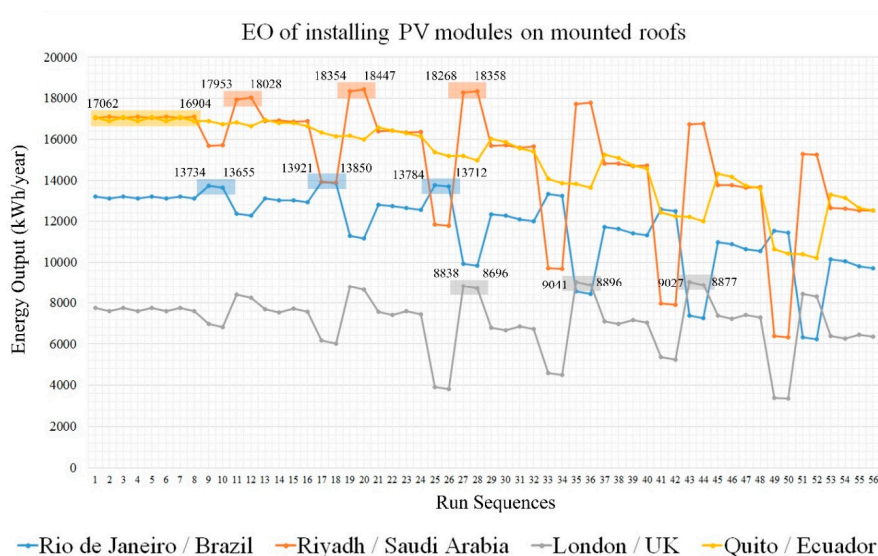
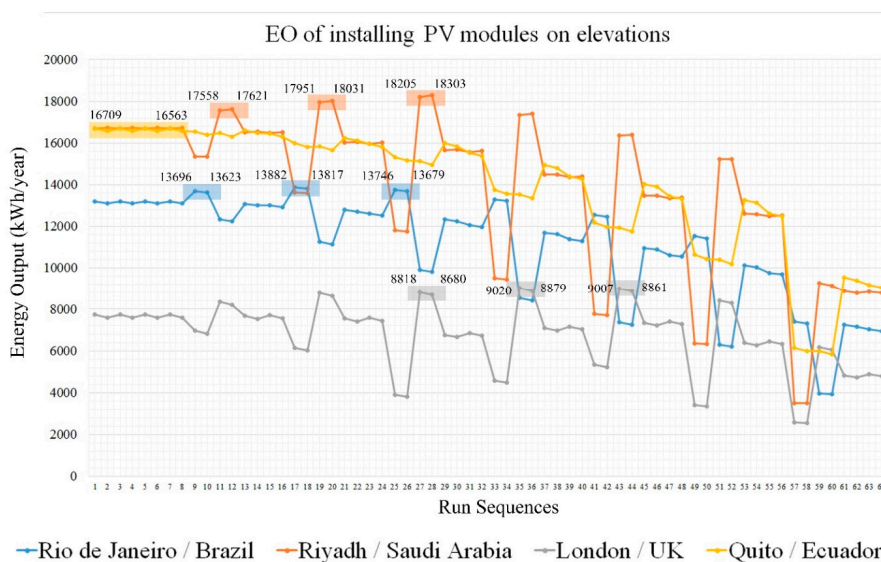**Figure 5.** EO of installing PV modules mounted on roofs.

Figure 6. EO of installing PV modules on elevations.

In Quito, positioning PV modules to the East and West geographic orientation for roofs and elevations would maximize the EO of PV modules, while the North and South geographic orientation are the worst orientations at which to install PV modules. However, the horizontal positioning of PV modules installed on roofs and elevations would maximize the EO of these modules. East and West façades are preferable for the installation of PV modules rather than other elevations. It must be noted that the EO of PV modules based on various geographic orientations is significantly smaller than in the other cities analysed in the case study.

On the other hand, Figure 4 illustrates the results of the regression analysis, which evaluated the coefficients of the assigned design factors of the functional unit of this work. It shows that the impact of PV inclination is the main factor that highly affects energy generation in a BIPV system, whether it be mounted on roofs or elevations. This means that the choice of a proper inclination will increase the energy efficiency in PV modules. The impact of the PV orientation is the second main factor that affects the energy generation in a BIPV system, while the third important factor is the interaction between both the inclination and geographic orientation of PV modules. The impact of the PV type is the fourth important factor that influences energy generation in PV modules. However, the impacts

of other interactions between PV types, PV orientation, and PV inclination are the lowest coefficient factors that would stimulate the EO of PV modules and can be neglected. This point was confirmed by analysing the figures presented in the supplementary file (Figures S1–S8). It must be noted that p-Si and mono-Si have a slight impact on influencing energy generation compared to the PV orientation. Yet, PV inclination is the main factor that could significantly influence energy generation.

Table 5. Summary of results of the case study.

Basic Notifications	Rio de Janeiro/Brazil	Riyadh/Saudi Arabia	London/United Kingdom	Quito/Ecuador
The best geographic orientation of PV modules mounted on roof	North	South	South	East and West
The worst geographic orientation of PV modules mounted on roof	South	North	North	North and South
Range of preferable inclination of PV module	10°–30°	10°–30°	30°–50°	0°
The worst inclination of PV modules on elevations	90°	90°	90°	90°
Best elevation to install PV modules	North	South	South	East and West
Second/Third preferable elevation to install PV modules	East/West	East/West	West/East	North/South
Worst elevation to install PV modules	South	North	North	N/A

5.5. Additional Roof Mounted Analysis

An additional specific examination of the EO of PV modules mounted on roofs was conducted based on the best geographic orientation of PV modules and the range of preferable inclinations in the examined cities. The need for this analysis is due to the aim of defining the specific inclinations that would maximize the EO of PV modules. The city of Quito was excluded from this analysis as Table 5 shows that the horizontal installation of PV modules is the best geographic orientation associated with the city.

The examination was conducted for the other three cities using a subsequent increment of 1° in order to quantify the best angle for positioning PV modules, as shown in Figure 7. The analysis of Rio de Janeiro (a) and Riyadh (b) included 21 frequent inclinations between 10° and 30° within the Northern and Southern geographic orientations, respectively, while the analysis of the city of London (c) included 21 frequent inclinations between 30° and 50° within a Southern geographic orientation. According to this additional analysis, Figure 7 illustrates the best inclination that would optimize the annual EO of PV modules and the proportion of (inclination/latitude), which is evaluated as previously outlined in Section 2.2, as follows:

(a) In Rio de Janeiro, the best inclination is 19°. The EO equals 13,929 kWh/year and 13,858 kWh/year for poly-crystalline and mono-crystalline, respectively, with a proportion of around 86%. The installation of PV modules within 10° or 30° will cause an annual energy waste of 195 and 145 kWh, respectively, using poly-crystalline modules, and 203 and 146 kWh, respectively, using mono-crystalline modules.

(b) In Riyadh, the best inclination is 21°. The EO equals 18,395 kWh/year and 18,488 kWh/year for poly-crystalline and mono-crystalline, respectively, with a proportion of 87%. The installation of PV modules within 10° or 30° will cause an annual energy waste of 442 and 127 kWh, respectively, using poly-crystalline modules, and 460 and 130 kWh, respectively, using mono-crystalline modules.

(c) In London, the best inclination is 43°. The EO equals 9066 kWh/year and 8920 kWh/year for poly-crystalline and mono-crystalline, respectively, with a proportion of 84%. The installation of PV modules within 30° or 50° will cause an annual energy waste of 228 and 634 kWh, respectively, using poly-crystalline modules, and 224 and 629 kWh, respectively, using mono-crystalline modules.
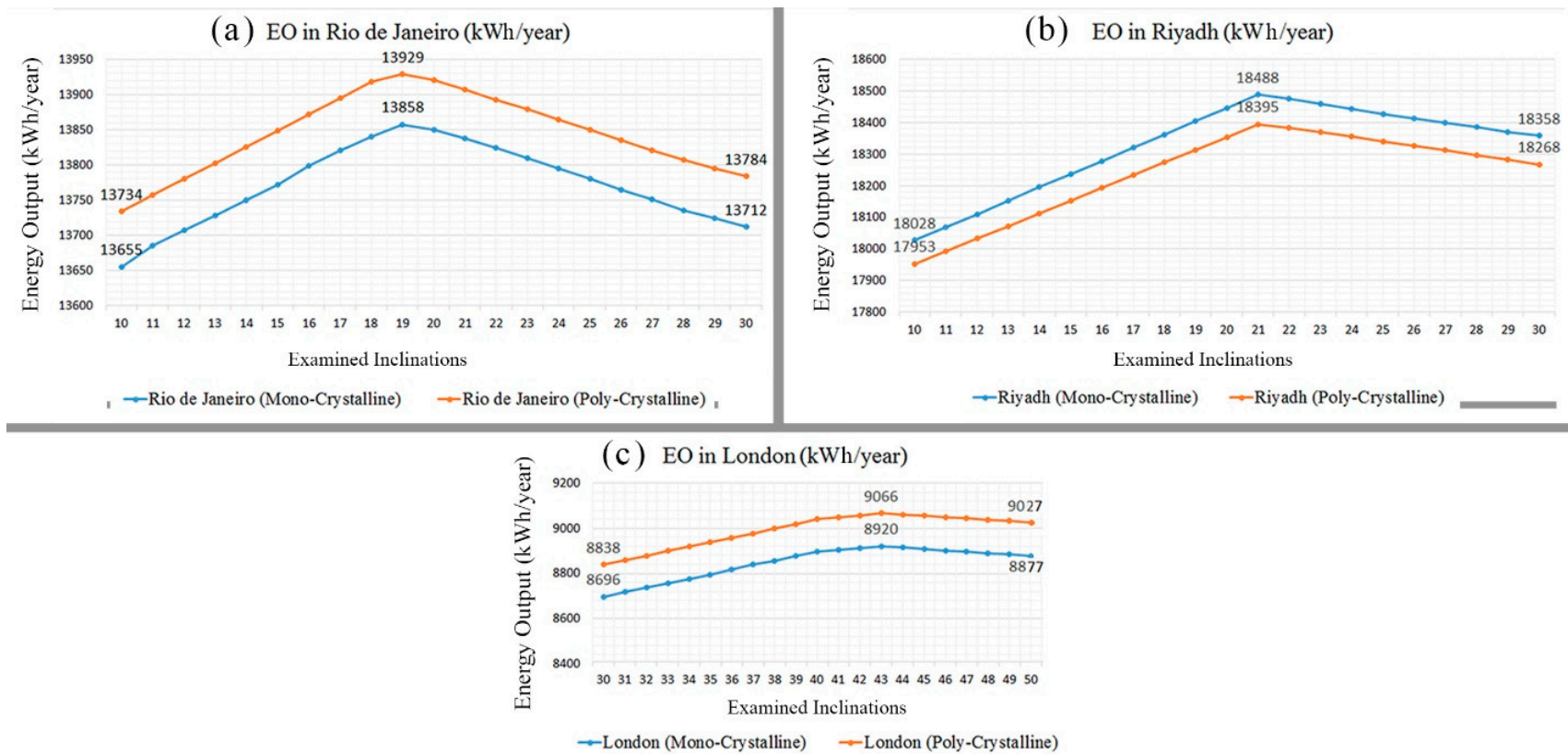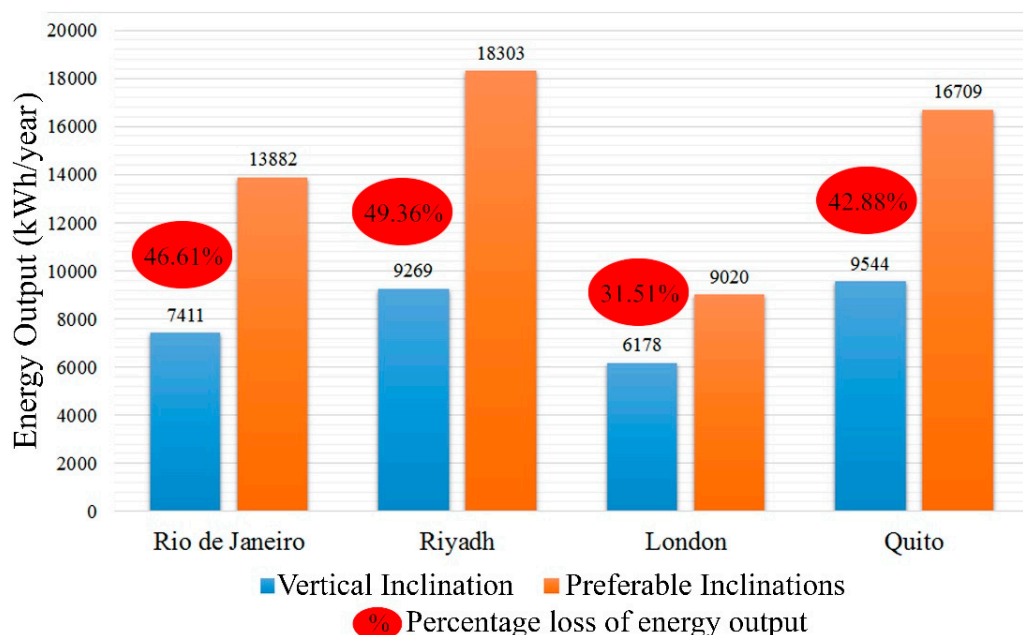
Figure 7. EO of installing PV modules mounted on roofs within a frequency of (1°).

6. Discussion

Analysis of the results of this work illustrate that the performance parameters (building modelling, climate data, and the installation variables) and their related design factors in the proposed framework using the experimental design can significantly evaluate the EO of PV modules. Additionally, this work clarifies that the impact of the PV type is the lowest coefficient factor that could influence energy generation. However, the impact of the PV inclination is the main coefficient factor that influences the process of producing energy in PV modules, while the impact of the PV orientation is considered the second main coefficient factor that simulates energy generation; Figures S1–S8 in the supplementary file have proven this point.

This work indicates that the geographic orientation of PV modules towards the Southern orientation is ideal for cities located North of the Equator while positioning PV modules at a Northern orientation is ideal for cities located South of the Equator. As expected, this means that PV modules should be oriented towards the equator line, however, the installation of PV modules on the East and West elevations of buildings would maximize the EO of PV modules in lower latitude regions close to the equator. In terms of PV inclination, the integration of PV modules on the exterior walls of buildings within a vertical inclination would produce the minimum EO in the four cities. The case study example confirms this point, as shown in Figure 8. It is clear that there would be a loss of one-third to almost one-half of the EO when PV modules are integrated on the exterior walls of buildings within a vertical inclination compared to the preferable inclinations of PV modules for each city: 46.61% in Rio de Janeiro, 49.36% in Riyadh, 31.51% in London, and 42.88% in Quito. This proves that the vertical installation of PV modules on elevations is the worst inclination compared to the preferable inclination for each region, in terms of maximizing the EO of these modules.

Figure 8. EO loss between the vertical inclination and preferable inclination of PV modules on elevations.

It must be noted that the installation of PV modules mounted on the roof is better than the elevation to maximize the EO of these modules. The results associated with the installation of PV modules in buildings located in Rio de Janeiro and Riyadh, which are situated at almost symmetric latitudes, show that the best inclination that increases the EO of PV modules is between 10° and 30°. This inclination increases to be between 30° and 50° in the city of London, while the horizontal inclination is suggested as the best position of PV modules for the city of Quito, which is located directly on the equator. Specifically, the installation of PV modules at inclinations of 0, 19, 21, and 43° would

maximise the EO of PV modules in Quito, Rio de Janeiro, Riyadh, and London, respectively. As a result, this work considers that the closer we get towards the equator, the lower the preferred inclination angles for the installation of PV modules. Consequently, comparing the collected results at this level of the analysis with the work of Gunerhan and Hepbasli [45], Benghanem [46], and Landau [47], presented in the literature review, reveals that PV modules should be oriented towards the equator line at inclinations almost equal to the latitude of the site, in the range of {(0.85 × Latitde_of_the_site) ∓ 3%}.

7. Conclusions

It is important to consider the energy performance of PV modules in order to enhance the sustainability of the built environment towards nZEBs. In an attempt to design better energy performing PV modules, the work in this study presented a methodological framework that could help to integrate the experimental design within the installation variable of PV modules in order to examine all possible design variables that influence the energy levels of these modules. The novelty of this work is in the establishment of a framework that captures performance parameters and design factors that determine the design energy efficiency of PV modules in a complete BIPV system. An emphasis was placed on the use of a standard procedure and software, making the work readily available to practitioners and experts in the area of renewable energy. An integrated methodological framework, which considers various performance parameters and related design factors, based on the experimental design was presented in order to empower the decision-making process of PV module installation. This work considers that improvements of the EO efficiency of PV modules as a major source of renewable energy in buildings has the potential to satisfy the increasing requirements of electricity and, consequently, reduce the dependence on fossil fuels, thus achieving sustainability and protection of the built environment.

A case study of 100 PV modules was examined in four cities, each with a different climate, through the use of an experimental design. The cities analysed included Rio de Janeiro, Riyadh, London, and Quito. First generation PV modules were studied, namely mono-crystalline and poly-crystalline modules. These modules were integrated into a complete BIPV system at different inclinations and geographic orientations. PV*Sol software was adopted as an analysis and planning tool in order to estimate the output energy of PV modules. Minitab software was utilized to build up the experimental design, estimate all the expected variables, and to conduct a linear regression analysis to define the coefficients of the assigned design factors.

It is envisaged that the proposed method will empower the decision-making process and sustainability of the installation of PV modules in a complete BIPV system. The results indicate that the performance parameters suggested in the framework significantly impact the maximization of the EO of PV modules. These parameters include the type of building design (i.e., the design of the final roof and elevations), the climate data, in addition to installation variables, such as the PV type, PV orientation, and PV inclination. Among the applied installation variables of this work, it must be noted that the impact of PV inclination was the major coefficient factor influencing energy generation; the impact of PV orientation was the second coefficient factor influencing energy generation; while the impact of PV type was the lowest coefficient factor influencing the energy generation of PV modules. Yet, it was found that the installation of PV modules on roofs would generate more EO compared to the elevation installation, however, the integration of PV modules on the exterior walls of buildings at a vertical inclination produces the minimum EO compared to other configurations in all cities; between 30% and 50% of the EO of PV modules would not be efficient if PV modules were integrated on the exterior walls compared to the mounted roofs of buildings. The results also display that the global positioning of PV modules in buildings should be towards the equator line. The installation of PV modules on the East and West elevations of buildings are preferable in locations close to the equator. However, it is preferable that PV modules are installed at lower inclinations, in cities close to the equator line. Maximizing the EO of PV modules requires positioning PV modules at inclinations almost equal to the latitude of the site, in the range of {(0.85 × Latitde_of_the_site) ∓ 3%}.

This work has three major limitations. First, the case example examined the first generation of PV modules, mounted on roofs and elevations of buildings, thus neglecting the important role of building modelling, in particular, the design of the elevations and roof, in determining the amount of the installed PV modules. Second, it disregarded the possible shadows on the functional unit; shadows have a negative impact on solar systems. Hence, multi-criteria decision analysis (MCDA) can be a viable direction for future works as a way to assess the other generations of PV modules and explicitly evaluate the conflicting criteria of the elevations and roof design. The third limitation is that building up the sequences of the experimental design in the PV*Sol software required that the same data and variables were entered for every sequence, which means plenty of time was consumed building up the case study. Hence, a future recommendation is the use of different software that facilitates entering the input data and saves time.

Supplementary Materials: The following are available online at http://www.mdpi.com/2071-1050/11/10/2992/s1, Figure S1. Main effects plot of installing PV modules on mounted roofs for Rio de Janeiro, Figure S2. Main effects plot of installing PV modules on mounted roofs for Riyadh, Figure S3. Main effects plot of installing PV modules on mounted roofs for London, Figure S4. Main effects plot of installing PV modules on mounted roofs for Quito, Figure S5. Main effects plot of installing PV modules on elevations for Rio de Janeiro, Figure S6. Main effects plot of installing PV modules on elevations for Riyadh, Figure S7. Main effects plot of installing PV modules on elevations for London, Figure S8. Main effects plot of installing PV modules on elevations for Quito

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