



Article Analysis Method of Design Strengths of P. edulis Bamboo

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Abstract: In order to determine the design strengths of *P. edulis* bamboo material, this research carried out a series of material tests on the full-culm P. edulis bamboo specimens, including compression tests parallel to the grain, bending tests, tension tests parallel to the grain, shear tests parallel to the grain and compression tests perpendicular to the grain. The standard values of different strengths for bamboo material were obtained by the Bootstrap method. The influence of the load combination and load effect ratio on the relationship between reliability index β and resistance factor γ_R was analyzed. A method for calculating the target reliability index of bending strength was proposed. The design strengths of the P. edulis bamboo material were determined and the adjustment method considering different design situations was also put forward. The research results show that the target reliability of the bending strength of bamboo material is suggested to be 3.57. With the same β value, γ_R is the maximum under the combination of constant load + snow load, and γ_R is the minimum under the combination of constant load + live load on the office building floor. Under the same load combination and load ratio, the shear strength along the grain has the maximum γ_R and the compression strength along the grain has the minimum $\gamma_{\rm R}$. The design strengths of the *P. edulis* bamboo material were determined by the larger γ_R of two cases (one is that the load ratio of constant load over live load on the residential building floor is 1.0 and another is that the constant load over live load on the office building floor is 1.0). The design strengths can provide reference for the design and application of bamboo structure.

Keywords: P. edulis bamboo; design strength; the Bootstrap method; reliability; resistance factor

1. Introduction

Building construction is an industry with high energy consumption and high pollution, which has caused serious impacts on the environment and ecology [1-3]. Exploring new building materials has become an urgent problem to be solved in the civil engineering industry. In recent years, various countries have issued a series of policies to promote the application of green buildings, and the development of the green buildings is an inevitable trend of economic and social development. Bamboo has the advantages of fast growth, wide distribution, high strength, high strength-to-weight ratio, and high rigidity-to-weight ratio [4-10]. It has been successfully applied in several projects [11-13]and is a new kind of green building material with great development potential. China is one of the main distribution centers of bamboo resources in the world and Phyllostachys edulis (moso) bamboo is the most widely distributed bamboo species with the highest economic value. However, due to the lack of design specifications, the application of bamboo structure is quite limited at present. Before the bamboo structure can be safely designed and popularized, it is essential to put forward the design strengths of bamboo material. However, currently, there is little relevant research on the design strengths of P. edulis bamboo material.

The development of an engineering structure design method has experienced the evolution process from the Allowable Stress Design (ASD) method to the probabilistic Limit State Design (LSD) method based on reliability theory. Currently, the LSD method



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based on the reliability theory is widely accepted and adopted in the design specification of various countries, including the wood structure specifications of Chinese and European code. The LSD method has also been adopted for emerging new materials that no design specifications are available. For example, Xiao et al. [14] obtained the design values of the recombined bamboo strengths through the LSD method. Zhong et al. [15] analyzed the reliability of the compressive strength of bamboo fiber-reinforced composite (BFRC) and proposed the recommended design strengths. Gong et al. [16] carried out the compression test parallel to the grain of Chinese fir specification wood and obtained the design strengths by using the LSD method. Zhu et al. [17] analyzed the reliability of wood structure and proposed the strength determination method of wood material. Liu et al. [18] analyzed the influence of probability distribution model and fitting data points on reliability. Therefore, the probabilistic LSD method based on reliability was used to study the design value of strength (design strength) for the *P. edulis* bamboo material in this research. Reliability analysis methods include the central point method, JC method, and so on. Each method has its advantages. In order to simplify the calculation, a reliability calculation formula based on the central point method is adopted in this paper.

Reasonable determination of the standard value of strength for bamboo material is the basis of bamboo structure design. It was found that there are great differences in the standard values of the strength obtained by different sample quantities; however, there is no uniform regulation on the sample quantity at present. The resistance factor is the key index to determine the design strengths of materials, and the target reliability is the key parameter to determine the resistance factor. At present, the target reliability is determined according to the ductile or brittle failure characteristics of the materials, while the bending resistance of bamboo presents semi-brittle failure characteristics, and there is still lack of a method to evaluate the target reliability of semi-brittle materials.

The strength design values are very important for the design and application of bamboo structures. In order to study the design strengths of the *P. edulis* bamboo material, the following work was carried out in this research for Chinese *P. edulis* bamboo material: (1) Systematic tests on different strengths of *P. edulis* bamboo material were carried out, including compression strength parallel to the grain, bending strength, tension strength parallel to the grain, shear strength parallel to the grain, and compression strength perpendicular to the grain; (2) The influence of sample quantity on the standard values of strengths was analyzed, and then the standard values of bamboo strengths were obtained based on Bootstrap method; (3) A method for determining the target reliability of bending strength of bamboo was explored; (4) The LSD method based on the reliability theory was used to analyze the relationship between the reliability and the resistance factor considering different load combinations; (5) The design strengths of the *P. edulis* bamboo material were determined, and the adjustment method for the design strengths under different load combinations and load effect ratios was proposed.

2. Materials and Methods

2.1. Materials

The strength tests of the *P. edulis* bamboo material were carried out according to ISO 22157-2019 [19] and JG/T199-2007 [20] standards. The bamboo material used in the experiment is *P. edulis* bamboo, which was collected from Hunan Province of China and was about 4 years old. Bamboo poles with a diameter of breast height (DBH) of about 100 mm were cut down randomly in the bamboo forest (Figure 1a). The length of the cut bamboo stalks were 6 m. The length of the components was cut to be 3 m from the bottom of bamboo poles. The material tests were carried out on the smaller specimens among all the three-meter long bamboo components. The material specimens for compression tests parallel to the grain and shear tests parallel to the grain were prepared with a height–diameter ratio of 1. The specimens for bending tests were prepared with a size of 220 mm \times 15 mm \times t mm. The dimensions of specimens are 330 mm \times 15 mm \times t mm for tension



tests parallel to the grain, and 15 mm \times 15 mm \times t mm for compression tests perpendicular to the grain.

Figure 1. Bamboo specimens and material tests for different strengths (*UCS* refers to compression strength parallel to the grain, *MOR* refers to bending strength, *UTS* refers to tensile strength parallel to the grain, *USS* refers to shear strength parallel to the grain, *CCS* refers to compression strength perpendicular to the grain): (**a**) selection of bamboo; (**b**) test.

2.2. Mechanical Properties

According to the standards [19,20], a series of tests of the specimens, including compression strength parallel to the grain (*UCS*), bending strength (*MOR*), tensile strength parallel to the grain (*UTS*), shear strength parallel to the grain (*USS*), and compression strength perpendicular to the grain (*CCS*), were conducted using an universal testing machine, as shown in Figure 1b. In the formal loading stages, *UCS*, *UTS*, and *USS* tests were loaded at the rate of 0.01 mm/s, *MOR* tests were loaded at the rate of 1 N/s, and *CCS* tests were loaded at the rate of 20 N/mm² per minute. The calculation formulas for the design strengths of *P. edulis* bamboo are as follows [19,20]:

$$f_{\rm m} = \frac{P_{\rm max}}{A} \tag{1}$$

$$MOR = \frac{150P_{\max}}{th^2} \tag{2}$$

where $f_{\rm m}$ could be the compression strength parallel to the grain, tensile strength parallel to the grain, shear strength parallel to the grain, and the compression strength perpendicular to the grain (MPa), MOR is the bending strength, $P_{\rm max}$ is the maximum load (N), A is the corresponding stressed area (mm²), *t* is the thickness (mm) of the bending specimen, and *h* is the height of the bending specimens (mm).

2.3. Moisture Content Adjustment

After completing the mechanical property tests, the moisture contents of the bamboo material were tested according to the standard JG/T199-2007 [20], where the samples used

to determine the moisture contents were immediately taken from the vicinity of the failure location. The moisture content calculation formula of *P. edulis* bamboo is given below [20]:

$$W = \frac{m - m_0}{m_0} \tag{3}$$

where *W* is the moisture content (%), *m* is the air-dry mass of the specimens (g), and m_0 is the absolutely dry mass of the specimens (g).

In order to calculate the design strengths of bamboo material from the obtained test results, the corresponding moisture content reference point should be determined initially (12% according to JG/T199-2007 [20]); due to that, the moisture content has a significant effect on the test results of bamboo material [21]. The modified formula of the mechanical property value is given below [20]:

$$f_{12} = K_{\rm W} f_{\rm W} \tag{4}$$

$$K_{\rm W} = \frac{1}{a + be^{cw}} \tag{5}$$

where f_{12} (MPa) is the strength of the pecimens under the standard moisture content (12%), f_W (MPa) is the strength when the moisture content is W, and K_W is the moisture content correction factor, which is related to the specific strength index and moisture content [20]. The strength of the bamboo material in this research is based on the standard moisture content (12%).

2.4. Outlier Detection

Considering that it is difficult to avoid outliers in the test data, the *IQR* criterion was adopted in this research to process the data and to eliminate the outliers. The *IQR* criterion assumes that the data conform to normal distribution, and the detection interval is calculated by taking the quantile value Q1 at 1/4 and Q2 at 3/4 of the data array from small to large. The distance between two quantiles (*IQR*) is calculated by the Formula (6), and the outlier detection interval is calculated by the Formula (7) [22]:

$$IQR = Q2 - Q1 \tag{6}$$

$$[Q1 - 1.5IQR, Q2 + 1.5IQR] \tag{7}$$

2.5. Bootstrap Resampling Method

Given an original data sample with size k, of which the overall distribution type and statistical parameters are unknown, the Bootstrap sample can be obtained by randomly sampling k times from the original data sample (which can be put back). The mean value and the variance of the Bootstrap sample were statistically analyzed to infer the characteristics of the overall distribution type and statistical parameters. The original sample of a given variable is $X = \{x_1, x_2, ..., x_k\}$, after which random sampling was conducted on it, and each value represented by xi in the original sample has an equal probability of being selected and can be selected repeatedly. After sampling k times, Bootstrap samples were obtained as $Y_j = \{y_{1j}, y_{2j}, ..., y_{kj}\}$. The mean a (Y_j) and variance $S^2(Y_j)$ of Bootstrap samples were calculated by the Formulas (8) and (9) [23]:

$$a(Y_{j}) = \frac{\sum_{i=1}^{k} y_{i_{j}}}{k}$$

$$\tag{8}$$

$$S^{2}(Y_{j}) = \frac{\sum_{i=1}^{k} [y_{i_{j}} - a(Y_{j})]^{2}}{k - 1}$$
(9)

The above operation were repeated p times to obtain the sample set $B = \{Y_1, Y_2, ..., Y_p\}$, containing p Bootstrap samples. The mean and the variance of p Bootstrap samples can be used to evaluate the overall sample characteristics of the variables.

2.6. Probability Distribution Model and Calculation of Standard Values of Material Strength

Normal distribution and Lognormal distribution are often used to fit the data in the statistics of material strength. The distribution functions f(x) of the two models are given below [24]:

Normal distribution:

$$f(x) = \frac{1}{\sqrt{2\pi}S} \exp\left\{-\frac{(x-a)^2}{2S^2}\right\}$$
(10)

Lognormal distribution:

$$f(x) = \frac{1}{xd\sqrt{2\pi}} \exp\left\{-\frac{(\ln x - b)^2}{2c^2}\right\}$$
(11)

where *x* is a random variable, representing the measured *UCS*, *MOR*, *UTS*, *USS*, and CCS in this study, *a* and *S* are the mean value and standard deviation, respectively, *b* is the average value of ln*x*, and *c* is the standard deviation of ln*x*.

The calculation formula for the standard value of strength conforming to normal distribution is shown in Formula (12), and the calculation formula for the standard value of strength conforming to Lognormal distribution is shown in Formula (13) [25]:

$$f_{\mathbf{k}} = a - \eta S \tag{12}$$

$$f_{\mathbf{k}} = e^{a(1 - \eta COV)} \tag{13}$$

where f_k is the standard value of strength (MPa), *a*, *S*, and *COV* are the mean value (MPa), standard deviation (MPa), and coefficient of variation, respectively, and η is the characteristic coefficient (1.645) [25].

2.7. Reliability Analysis Method

The calculation formula of reliability β is as follows [26]:

$$\beta = \frac{K_{\rm R}\gamma_{\rm R}(\gamma_{\rm G} + \gamma_{\rm B}\rho) - (K_{\rm G} + K_{\rm B}\rho)}{\sqrt{\left[K_{\rm R}\gamma_{\rm R}(\gamma_{\rm G} + \gamma_{\rm B}\rho)\delta_{\rm R}\right]^2 + \left(K_{\rm G}\gamma_{\rm G}\right)^2 + \left(K_{\rm B}\rho\gamma_{\rm B}\right)^2}}$$
(14)

where $K_{\rm R}$ is the uncertainty of resistance and $\delta_{\rm R}$ is the coefficient of resistance variation, $\gamma_{\rm R}$ is the partial coefficient of resistance, $\gamma_{\rm G}$ and $\gamma_{\rm Q}$ are permanent load component coefficients and variable load component coefficients, respectively, $K_{\rm G}$ and $\delta_{\rm G}$ are the permanent load uncertainty coefficient and variation coefficient, respectively, $K_{\rm B}$ and $\delta_{\rm B}$ are the variable load uncertainty coefficient and variation coefficients, respectively, and ρ is the ratio of the variable load to the standard value of the permanent load effect.

The design strengths of the bamboo material are calculated by Formula (15) [27]:

$$f_d = \frac{f_k K_P K_A K_Q}{\gamma_R} \tag{15}$$

where f_d is the design value of bamboo material (MPa), f_k is the standard strength value of bamboo material (MPa), K_P is the uncertainty coefficient of the calculation model, K_A is the indefinite coefficient of geometric parameters, K_Q is the reduction coefficient of the

strength of the material converted into the strength of the component, and the calculation formula is shown in Formula (16) [27]:

$$K_Q = K_{Q1} K_{Q2} K_{Q3} K_{Q4} \tag{16}$$

where K_{Q1} is the coefficient considering the influence of natural defects, K_{Q2} is the coefficient considering the influence of drying defects, K_{Q3} is the influence coefficient considering long-term load, and K_{Q4} is the coefficient considering the size effect.

3. Results

3.1. Standard Values of Material Strengths

The strength values of the bamboo material were taken as the average strengths of the small clear specimens at both ends of the bamboo components. Statistical parameters such as mean value (*a*), standard deviation (*S*), and coefficient of variation (*COV*) were analyzed, and the results are shown in Table 1, where n represents the number of components. It can be seen from Table 1 that bamboo material has excellent tensile strength, compression strength parallel to the grain, and bending strength properties, and different strength values are ranked as UTS > MOR > UCS > CCS > USS.

Table 1. Eigenvalue statistics.

Strength Index	UCS	MOR	UTS	USS	CCS	
	п	154	116	128	145	109
Original data	a/MPa	54.04	130.02	139.36	15.57	33.38
Original data	S/MPa	6.83	19.49	34.88	2.26	9.07
	COV	0.13	0.15	0.25	0.15	0.27
	п	154	115	127	143	107
After processing <i>IQR</i>	a/MPa	54.04	129.71	138.58	15.56	32.84
criteria	S/MPa	6.83	19.28	33.89	2.11	8.21
	COV	0.13	0.15	0.25	0.14	0.25
	п	54.04	129.69	138.63	15.56	32.84
After processing the	a/MPa	0.55	1.79	2.98	0.18	0.69
boolstrap method	S/MPa	0.01	0.01	0.02	0.01	0.02
Standard values f_{1} /MPa		53.14	126.75	133.72	15.27	31.71

Note: *n* refers to the number of components, *a* refers to mean value, *S* refers to standard deviation, and COV refers to coefficient of variation.

To analyze the influence of sample size on the statistical results of bamboo material strengths, taking the bending strength as an example, 10, 30, 50, 70, and 100 datapoints were randomly selected from 115 original samples after eliminating outliers according to the *IQR* criterion. Each sample was repeated 100 times, and the error value was obtained by comparing the mean value of the 5th percentile value of the 100 samples with the 5th percentile value of the original sample. The statistical results of the error value are shown in Table 2. As can be seen from Table 2, the mean error between the 5th percentile value of bending strength obtained by conventional sampling and the 5th percentile value of the original sample quantities is 24.46%. The Bootstrap method was used to re-sample the data of different sample numbers randomly selected above, and the frequency of re-sampling was 10,000 times. It is shown that the mean value of the bending strength error is 5.26% using the Bootstrap method.

 Table 2. Deviation of bending strength 5% subdivision value under different sample size.

Sample Size	10	30	50	70	100	Mean Values
Regular sampling	28.94%	26.53%	23.44%	23.49%	19.90%	24.46%
The Bootstrap sampling method	5.20%	5.36%	5.22%	5.22%	5.30%	5.26%

The above sampling process shows that the number of samples has significant influence on the standard value of material strength. The Bootstrap resampling method is used to calculate the standard value of material strength with small errors and can significantly reduce the influence of sample size. Moreover, the same influence of number of samples were found on other material strength indexes.

The Bootstrap method was used to process the data after removing the outliers through the *IQR* criterion, and the number of resampling was 10,000 times. The characteristic values of the bamboo material strengths calculated by the Bootstrap method are shown in Table 1, where 10,000 bamboo material strength values obtained by the Bootstrap analysis were statistically analyzed to obtain the distribution histogram, as shown in Figure 2. It can be seen from Figure 2 that the distribution curves obtained by using the Normal function and Lognormal function to fit the bamboo material strength values are almost identical. Therefore, the standard values of the bamboo material strengths calculated by using the fitting results of Normal function and Lognormal function tended to be equal. In this research, Formula (10) is used to calculate the standard values of the bamboo material strengths, and the results are shown in Table 1. The obtained standard values of *UCS*, *MOR*, *UTS*, *USS*, and *CCS* are 53.14 MPa, 126.75 MPa, 133.72 MPa, 15.27 MPa, and 31.71 MPa, respectively.









Figure 2. Histogram of a probability distribution of bamboo material strengths processed by the Bootstrap method: (**a**) *UCS*; (**b**) *MOR*; (**c**) *UTS*; (**d**) *USS*; (**e**) *CCS*.

3.2. Statistical Parameters of Load and Resistance

This research considered the influence of five different kinds of loads (dead load, live load of residential floor, live load of office floor, wind load with 30-year recurrence period, and snow load with 50-year recurrence period) and the statistical parameters of all kinds of loads shown in Standard for design of timber structures (GB 50005-2017) [27]. Moreover, the composition of bamboo material is similar to that of wood material; the statistical parameters of resistance can be referred to the specification GB 50005-2017 [27].

3.3. Reliability Indexes

According to the standards GBJ 68-1984 [25] and GB 50153-2008 [28], the reliability indexes under the ultimate bearing capacity of structural members within the design service life (50 years) should be determined according to the structural safety level and the failure type of structural members. This research considered the structural safety level as the second level. Figure 3 shows the typical load-displacement curves of the material properties tests. According to the test results shown in Figure 3 together with the results of existing literature [29–32], the compression strength parallel to the grain and compression strength perpendicular to the grain of bamboo material display obvious ductility failure characteristics. Therefore, the target reliability β_0 of the compression strength parallel to the grain and compression strength perpendicular to the grain of bamboo material is set to 3.2. The tensile strength parallel to the grain and shear strength parallel to the grain show obvious brittle failure characteristics; therefore, the target reliability β_0 is 3.7.

The load-displacement curves obtained from the bending performance tests of bamboo material are similar [33,34]. At the initial stage of loading, specimens went through a long elastic stage, and at the later stage of loading, some specimens appeared a plastic stage, even though the plastic stage was relatively short. Therefore, this research considered it unsafe if the bending resistance of bamboo material is classified as a ductile failure ($\beta_0 = 3.2$), and moderate if it is classified as a brittle failure ($\beta_0 = 3.7$).

The ductility factor is a parameter to measure ductility, and the higher the ductility factor, the better the ductility is. It can be calculated according to Formula (17) [35]:

1

$$u = \Delta_{\rm u} / \Delta_{\rm y} \tag{17}$$

where μ is the ductility factor, Δy is the yield displacement, and Δu is the displacement corresponding to the ultimate load F_u (0.85 times the maximum load F_{max}). The PARK method is used to locate Δy (Figure 4). Specifically, through the two points F_{max} and 0.75 F_{max} on the curve, we can draw a perpendicular line to the vertical axis and intersect the curve at point A and Point C, respectively. Then, we can connect OA, intersect the horizontal line between point C and the vertical axis at point B, and make a vertical line



crossing the horizontal axis through point B, and the displacement of point intersecting horizontal axis is the yield displacement Δy .

Figure 3. The typical load-displacement curves: (a) UCS; (b) MOR; (c) UTS; (d) USS; (e) CCS.



Figure 4. Schematic diagram of ductility factor calculation.

First, the combined statistical analysis of ductility factors of the compression strength tests parallel to the grain and compression strength tests perpendicular to the grain were carried out, and then the combined statistical analysis of ductility factors of the tensile strength tests parallel to the grain and shear strength tests parallel to the grain were carried out. Finally, the box diagram as shown in Figure 5 was obtained. The average ductility factors of the two groups of data were calculated as μ_1 and μ_2 , respectively. Similarly, the average ductility factor of the bending tests μ_3 was obtained, and the bending target reliability of bamboo material $\beta_3 = 3.57$ was obtained by the linear interpolation method (Table 3).



Figure 5. Ductility coefficient statistics.

Table 3. Ductility coefficient and target reliability.

Parameters	μ_1	μ_2	μ_3	β_1	β_2	β_3
Values	4.35	1.27	2.05	3.2	3.7	3.57

Four different load combinations (dead load + residential floor live load (D + R), dead load + office floor live load (D + O), dead load + wind load (D + W), and dead load + snow load (D + S)) were considered in this study. Seven different load effect ratios (0, 0.25, 0.5, 1.0, 2.0, 3.0, and 4.0) were calculated by the ratio of the variable load effect to the permanent load. The JC method was used for reliability analysis to obtain the relationship curves between the reliability indexes and the resistance factors. In this study, the results of compression strength parallel to the grain, bending strength, and tensile strength parallel to the grain tests are displayed in Figures 6–8. As can be seen from Figures 6–8, with the increase of the resistance factors, the reliability indexes show a trend of gradual increase. The load ratios have a significant influence on the reliability indexes, and for the same resistance factors, the reliability indexes show an increasing trend with the increase of the load ratios. With the increase of load ratios, the magnitude of the increase of reliability indexes with the increase of load ratios is greater than that of D + W and D + S load combinations.



Figure 6. Compression strength parallel to the grain reliability curve (β refers to reliability index, γ_R refers to resistance factor): (a) D + R; (b) D + O; (c) D + W; (d) D + S.





Figure 7. Cont.



Figure 7. Bending strength reliability curve (β refers to reliability index, γ_R refers to resistance factor): (a) D + R; (b) D + O; (c) D + W; (d) D + S.



Figure 8. Tensile strength parallel to the grain reliability curve (β refers to reliability index, γ_R refers to resistance factor): (a) D + R; (b) D + O; (c) D + W; (d) D + S.

3.4. Resistance Factors

The resistance factors of various mechanical properties of bamboo material under the target reliability are shown in Table 4. It can be seen from the table that, with the same

strength indexes, the resistance factor for D + S load combination is the largest, and the resistance factor for D + O load combination is the smallest when the load effect ratio $\rho > 0$. Under the same load combination and load effect ratio, the resistance factors of the shear strength parallel to the grain test are the largest, and the resistance factors of the compression strength parallel to the grain test are the smallest.

Strength Indexes	Load Combination -	ρ						
		0	0.25	0.5	1	2	3	4
	D + R	1.63	1.37	1.22	1.05	0.93	0.88	0.84
1100	D + O	1.63	1.35	1.19	1.01	0.86	0.81	0.78
ucs	D+W	1.63	1.44	1.33	1.23	1.16	1.15	1.14
	D+S	1.63	1.45	1.35	1.27	1.23	1.23	1.24
	D + R	1.71	1.44	1.28	1.10	0.97	0.92	0.90
MOD	D+O	1.71	1.42	1.24	1.05	0.91	0.85	0.83
MOK	D+W	1.71	1.50	1.39	1.28	1.21	1.20	1.19
	D+S	1.71	1.51	1.41	1.32	1.29	1.28	1.29
	D + R	1.73	1.45	1.29	1.11	0.97	0.93	0.91
	D+O	1.73	1.43	1.26	1.06	0.91	0.86	0.82
uis	D+W	1.73	1.52	1.40	1.29	1.22	1.21	1.20
	D+S	1.73	1.53	1.42	1.33	1.30	1.29	1.30
USS	D + R	1.93	1.64	1.46	1.26	1.11	1.05	1.03
	D+O	1.93	1.61	1.42	1.20	1.03	0.97	0.94
	D+W	1.93	1.71	1.58	1.46	1.39	1.37	1.36
	D+S	1.93	1.72	1.61	1.51	1.47	1.47	1.46
CCS	D + R	1.67	1.41	1.26	1.09	0.96	0.91	0.89
	D+O	1.67	1.39	1.22	1.04	0.89	0.84	0.81
	D+W	1.67	1.48	1.37	1.27	1.21	1.19	1.18
	D+S	1.67	1.49	1.39	1.31	1.28	1.27	1.28

Table 4. Resistance factors under target reliability.

To fulfill the design strengths requirement of the target reliability, adopting the maximum of the resistance factors γ_R under different load combinations as the final resistance factor is safe but uneconomical. According to the functional use of the structure, the load combinations are divided into two groups: the first group is D + R and D + O, which is a more commonly used load combination, and the second group is D + W and D + S, which may be dominant in a few areas. When the load ratio under the first group of load combinations is equal to 1.0, relatively larger resistance factors were adopted to calculate the design strength [15].

In the first group of load combinations, when $\rho > 1.0$, the resistance factors can ensure the safety of the structure, so adjustment is not necessary in this case. When $\rho < 1.0$, the design strengths shall be adjusted according to the resistance factors. The ratio of the reciprocal of the resistance factor when $\rho = 0$ to the reciprocal of the resistance factor when $\rho = 1.0$ was used as a reference value of the adjustment coefficient. The design strengths of various mechanical properties were adjusted by the formula in Table 5, where λ is the adjustment coefficient. Under the second group of load combinations, the design strengths were adjusted by the ratio of the larger resistance factors when $\rho = 1.0$ and the corresponding resistance factors of the first group. With this adjustment, the design strengths of *UCS*, *MOR*, *UTS*, *USS*, and *CCS* under the second group of load combinations need be multiplied by the reduction coefficient of 0.83 based on the first group.

Strength Indexes	Adjustment Formulas
UCS, MOR, UTS, CCS	$\lambda = 0.64 + 0.36\rho$
USS	$\lambda = 0.65 + 0.45\rho$

Table 5. Adjustment formula of design strength.

3.5. Determination of Design Strengths

To sum up, the analysis method of design value of bending strength of bamboo is as follows. Firstly, the target reliability of bending resistance is determined based on the ductility coefficient. Then, according to the reliability calculation formula, reliability analysis is carried out and the partial coefficient of resistance under the target reliability is obtained. Finally, the design strength value of bamboo is calculated according to the calculation formula of the design strength value. The design strengths of the bamboo material obtained based on the study in this research are shown in Table 6. The curves of the design strengths considering adjustment method proposed in this study are shown in Figure 9, with a two-fold line shape.

Table 6. Design strengths of P. edulis bamboo material.



Figure 9. Curves of design strengths considering the adjustment: (a) D + R and D + O; (b) D + W and D + S.

4. Conclusions

(1) The *P. edulis* bamboo materials were tested for compression strength parallel to the grain, bending strength, tensile strength parallel to the grain, shear strength parallel to the grain, and compression strength perpendicular to the grain and the strength data were analyzed statistically. The bamboo material has an excellent compression strength parallel to the grain, bending strength, tensile strength parallel to the grain, and different material strengths are ranked as UTS > MOR > UCS > CCS > USS.

(2) The Bootstrap method was used to analyze the material strengths after removing all the outliers by *IQR* criteria and obtain the standard values of the *P. edulis* bamboo material strengths. The standard values of *UCS*, *MOR*, *UTS*, *USS*, and *CCS* are 53.14 MPa, 126.75 MPa, 133.72 MPa, 15.27 MPa, and 31.71 MPa, respectively. This method can significantly reduce the influence of sample size on the test results.

(3) The effects of load combinations, load effect ratio on the relationship between reliability index β , and resistance factor γ_R were analyzed, and β increases with the increase

of $\gamma_{\rm R}$. Under the same condition of β , the resistance factors under the combination of dead load + snow load (D + S) are the highest, while the resistance factors under the combination of dead load + live office floor load (D + O) are the lowest. Under the same load combinations and load effect ratios, the resistance factors of the shear strength parallel to the grain test are the largest, and the resistance factors of the compression strength parallel to the grain test are the smallest.

(4) Considering safety and economic factors, the design strengths of *P. edulis* bamboo material were determined by the larger resistance factors of load effect ratio = 1.0 under dead load + live load on the residential floor (D + R) and dead load + live load on office floor (D + O). The obtained design strengths of *UCS*, *MOR*, *UTS*, *USS*, and *CCS* are 15.26 MPa, 44.24 MPa, 49.34 MPa, 3.87 MPa, and 9.18 MPa, respectively, for the *P. edulis* bamboo material investigated in this study.

(5) The design strengths under the load ratio of dead load + live load on the residential floor (D + R) and dead load + live load on the office floor (D + O) were adjusted when the load ratios were less than 1.0. The adjustment coefficients increase linearly with the increase of the load ratios, and the adjustment curves under the total load ratio show a two-fold line shape. The design strengths under dead load + wind load (D + W) and dead load + snow load (D + S) are multiplied by a reduction factor of 0.83 based on the design strengths under dead load + live office floor load (D + O).

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