



Article Characteristic Value of the Modulus of Elasticity (MOE) for Natural and Planted Larch in Northeast China

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Abstract: The density and modulus of elasticity (MOE) distribution can provide information on the effectiveness of parametric and non-parametric methods in calculating the characteristic value of MOE. In this study, we aim to determine the optimal distribution model of the actual measured data of the lumber. We also estimate the lumber's MOE characteristic value and compare the difference in density and MOE between natural and planted larch. Approximately 1200 pieces of dimension lumber of 4 m × 140 mm × 40 mm in size, made from larch and planted larch, were obtained, tested, and the corresponding standard MOE value was calculated. Results revealed the 3-parameter Weibull distribution to be optimal in fitting the natural and planted larch distributions. The parametric method proved effective in calculating the characteristic value of both larch groups, with characteristic MOE values of 9.73 kN/mm² and 8.84 kN/mm², and characteristic density values of 530 kg/m³ and 460 kg/m³ for natural and planted larch, respectively. Moreover, the MOE and density values followed grades C40 and C35. Thus, the conclusion is that the parametric method should be used to determine these characteristic values for natural and planted larch.

Keywords: MOE; planted larch; characteristic value; dimension lumber; probability distribution; non-destructive testing

1. Introduction

Wood is an environmentally friendly building material that is widely used in civil buildings and public constructions across Europe, North American, Japan, and other regions, due to its carbon storage capabilities, low density, high strength, good seismic performance, aesthetically pleasant appearance, and positive effects on indoor environments, such as air humidity control, bactericidal action, and good smell [1]. The rapid development of wood buildings in China relies largely on both natural forest and imported wood. However, there is a lack of full-sized mechanical test data of fast-growing plantation wood, which limits the use of plantation wood in the field of wood structure materials and wood buildings. Planted larch can overcome the problem of slow-growing natural larch by improving the utilization of planted forests, particularly in China, decreasing the dependence on natural wood and thus protecting natural forests.

As a structural timber resource, larch is well-suited for wood construction in China and Russia due to its high strength [2] and wide distribution in the Far East of Russia and Northeast and Northern China. Furthermore, natural and plantation larch forests are one of the most important wood species in China, supplying the largest amount of structural lumber in the country. Extensive research has been performed on the classification and full-scale mechanical property determination of larch, collecting valuable experimental data and providing theoretical support for the safe use of larch in wood structures and buildings [3–5]. Full-size experimental tests on natural larch lumber have been reported by



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Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). Zhong [6,7], Jiang [3], Lou [8], and Wang [9] et al., promoting the utilization of natural larch in China. However, studies on the full-size mechanical properties of planted larch lumber are limited, leading to a lack of test data for timber design applications. Thus, in order to use planted larch to build frame structures and grade the lumber by stress, experimental tests (particularly those based on full-size lumber) with extensive samples are urgently required to provide basic data support for the necessary calculations in timber design.

Dimension lumber is the lumber processed to a specified size according to a standard or code [10]. The modulus of elasticity (MOE) of the dimension lumber is key for the grading of lumber, the design of wood structures [11], and, in particular, to determine the level of deflection that meets the serviceability limit states under bending [12]. The MOE of dimension lumber is commonly investigated using static test methods (denoted as MOE_{static}). However, such test procedures are time-consuming, labor-intensive, and can damage the lumber. Therefore, non-destructive tests (NDTs) have been developed to replace static test methods and to determine the $MOE_{Dynamic}$ of lumber [9]. NDTs are convenient, save time, and most importantly they do not damage the lumber. Commonly used NDT techniques include the transverse vibration method, the longitudinal fundamental frequency vibration (FFV) test method, and the stress wave method [13–15]. The FFV method is commercially employed for stress grading and developments and can be combined with laser scanning. Previous work has reported the accurate and robust *MOE*_{Dynamic} measurements via the FFV method [16–18]. Experimental tests reveal the correlation coefficients (R^2) between the dynamic elastic modulus ($MOE_{Dynamic}$) and static elastic modulus (MOE_{static}) determined by the FFV and static test method to exceed 0.8 [14,19,20]. Therefore, the MOE_{static} can potentially be replaced by *MOE*_{Dynamic} to grade the lumber and estimate the deflection.

In the current study, we focused on obtaining more data and knowledge on natural and planted larch for designing and grading the wood and lumber. In particular, the $MOE_{Dynamic}$ and density differences between natural and planted larch lumbers were analyzed and compared, and we also extensively measured the MOE_{static} numbers of natural and planted larch lumber via the FFV test method. Moreover, the density and $MOE_{Dynamic}$ distributions were evaluated by fitting them with normal, lognormal, and Weibull distribution functions. The density and $MOE_{Dynamic}$ differences were compared between natural and planted larch, and the characteristic values of the density and $MOE_{Dynamic}$ of natural and planted larch dimension lumber were evaluated based on the density and $MOE_{Dynamic}$ distributions. In the end, parameter and non-parameter methods were used to calculate the characteristic values, to compare which method was more suitable, and to determine the characteristic values for natural and planted larch.

2. Materials and Methods

2.1. Materials and Equipment

Natural and planted larch from Northeast China were used to process the dimension lumber. Natural larch (*Larix gemlinii*) logs with diameters of 25 cm to 35 cm, a length of 4 m, and a ring number between 20 and 30 were taken from Mohe Forest Farm in Heilongjiang, China. Planted larch (*Larix keampferi Carr*) logs of similar size were collected from Qingyuan Forest Farm in Liaoning, China. All the logs underwent sawing, kiln drying, and planing to obtain dimension lumber of 4 m × 140 mm × 40 mm in size (longitudinal × tangential × radial). A total of 600 lumber samples were prepared for both the natural and planted larch. The moisture content of the samples ranged within $12.21 \pm 2.57\%$.

A frequency collector sensor and Fast Fourier Vibration analyzer (FAKOPP Enterprise BT) were used for the FFV tests. Furthermore, we used a band tape (SATA Tools Company, Shanghai, China) and digital slide calipers (MITUTOYO) with accuracies of 1 mm and 0.01 mm to measure the lumber length and thickness/width, respectively. An electronic weight scale (METTLER TOLEDO) was used to determine the lumber weight to an accuracy of 0.05 kg, while a portable moisture meter (Sanliang) with an accuracy of 0.1% was employed to test the moisture content of the lumber. A universal mechanical test machine

(Jinanshijin Company, Jinan, China) with a 30 t load was used to test the static MOE and the collection load and deflection was performed via a TDS-530 data collector (Tokyo Measuring Instrument Company in Tokyo, Japan).

2.2. Lumber Density and Dynamic MOE Testing

Following processing, the dimension lumber samples were marked with a number and stored in an air-drying shed for more than 3 months to maintain an equilibrium moisture content of approximately 12%. The weight (m), length (L), width (b), thickness (h), and moisture content (MC) of each piece of lumber were measured and the global density (ρ) was calculated as $\rho = m/(L \cdot b \cdot h)$. The FFV test method was then employed to calculate the lumber's dynamic MOE (MOE_{Dynamic}) by assuming a linear relationship between the natural frequency of the lumber and its density. More specifically, the dynamic response to the external excitation of the lumber was collected and the natural frequency was obtained through the Fast Fourier Vibration analyzer of FAKKOP, thus determining the lumber's MOE_{Dynamic} [21]. During the FFV tests, a hammer was used to strike one end of the lumber (Figure 1), as per the manual of FAKKOP, while the resonance frequency (f_m) was obtained from a voice frequency collector microphone, of the M9 type, from the Salar company (Figure 2). In order to avoid random error, frequency tests were repeated at least 3 times for each piece of lumber until a constant frequency was reached. The lumber frequency (f_m) was recorded as the mean of the three repetitions. The lumber density and frequency (f_m) were combined to calculate $MOE_{Dynamic}$:

$$MOE_{Dynamic} = \rho (2Lf_m)^2 \tag{1}$$

where $MOE_{Dynamic}$ is the lumber dynamic MOE determined from the FFT method (Pa); *L* is the sample length (m); f_m is the initial longitudinal resonance frequency (Hz) of the sample; and ρ is the average density of the sample (kg/m³).



Figure 1. Principle for the determination of the elasticity modulus via FFV (*E_{FFV}*).



Figure 2. Test set-up (**a**) and screenshot of the software to determine the resonance frequency (f_m) (**b**).

The mean and standard deviation (SD) of the density and $MOE_{Dynamic}$ values for natural and planted larch lumber were determined in R language (Version 3.6.3, R Core Team). Based on the *Three Sigma Rule* [22], if the absolute difference between the test value

and mean value of all data was greater than 3 times the standard deviation ($|x_i - \overline{x}| > 3\sigma$), the test value was rejected to minimize errors.

2.3. Testing the Lumber Static Bending MOE

In order to verify the accuracy of the $MOE_{Dynamic}$ determined via the FFV test method, 80 pieces of dimension lumber were randomly selected from the natural larch dimension lumber and their static bending elastic modulus (MOE_{static}) was tested using the universal test machine. Linear regression analysis with the dynamic MOE data ($MOE_{Dynamic}$) was then performed using the MOE_{static} values.

The static bending MOE (MOE_{static}) of the dimension lumber was tested based on the ASTM D198-15 Standard Test Method of Static Tests of Lumber in Structure Sizes [23] and the Chinese standard GB/T 28993-2012 Standard test methods for mechanical properties of structural lumber [24]. More specifically, we employed the third point flatwise bending test method (Figure 3) with a span-to-thickness ratio of 21 and loading distance at the center of 280 mm for the MOE_{static} tests. The load and deflection were determined by a load cell and electronic indicator, respectively, and measurement values were collected with a data logger at a 1 Hz sampling rate. In order to ensure accuracy, each lumber was tested three times on load data ranging between 1.8 kN and 3.3 kN, as these values were below 40% of the estimated failure load. The average MOE value of the last two measurements was used as the static MOE for the lumber sample due to the slight difference in values between the first and last two tests.



Figure 3. Schematic of the static MOE tests.

2.4. Estimate the Distribution Parameter of Density and MOE

Normal, lognormal, and Weibull distributions are typically adopted to fit the physical and mechanical properties of lumber [25]. The selected distribution model can influence the predicted and evaluated values of the larch, and also has an influence on the characteristic values. In particular, the characteristic value determined via the parameter method is observed to be more accurate if the corresponding density and MOE are known in advance. In the current study the density and MOE of the two larch types were fitted using the three distributions, and the goodness of the fits were compared using the K-S test method [26].

2.4.1. Parameter Estimations of the Normal, Lognormal, and Weibull Distributions

The maximum likelihood method was employed to estimate the normal distribution parameters, namely, the sample mean, μ , and variance, σ^2 . The lognormal distribution parameters were similarly determined by calculating the logarithm of the individual measured data.

The 2- and 3-parameter Weibull distributions were also determined, and the goodness of fit was evaluated. Table 1 reports the basic expressions for the 3-parameter Weibull distribution.

Probability Density Function (PDF)	Cumulative Distribution Function (CDF)	Mean	Variance
$f(x) = \frac{k}{\lambda} \left(\frac{x - x_u}{\lambda}\right)^{k - 1} e^{-\left[\frac{x - x_u}{\lambda}\right]^k}$	$F(x) = 1 - e^{-\left[\frac{x - x_u}{\lambda}\right]^k}$	$\lambda\Gamma\left(1+rac{1}{k} ight)$	$\lambda^2 \bigg[\Gamma \Big(1 + \tfrac{2}{k} \Big) - \Big(\Gamma \Big(1 + \tfrac{1}{k} \Big) \Big)^2 \bigg]$

Table 1. Weibull distribution functions and parameters.

Note: $x_u = 0$ represents the 2-parameter distribution.

We calculated the 2-parameter Weibull distribution parameters (e.g., shape parameter k and scale parameter λ). The data were sorted in ascending order and plotted as a cumulative density function (CDF). The CDF of the 2-parameter Weibull distribution was calculated via Equations (2) and (3).

$$\frac{i}{(n+1)} = 1 - e^{-\left(\frac{\rho_i}{\lambda}\right)^k} \tag{2}$$

where *i* is the data point number in ascending order; and *n* is the number of samples. The logarithm of both the sides of Equation (3) was then taken:

$$lg(lg\frac{n+1}{n+1-i}) = klg\rho_i + lg(\frac{lge}{\lambda^k})$$
(3)

Equation (4) can be interpreted as a linear equation with slope k and intercept $lg(lge/\lambda k)$. Taking the larch density data as an example, parameter k and scale parameter λ were calculated as 9.03615 and 0.69555, respectively.

In order to estimate the 3-parameter Weibull distribution parameters, location parameter x_u was subtracted from each data point. The other parameters were determined as with the 2-parameter Weibull distribution.

2.4.2. K-S Test

The K-S test was adopted to compare the goodness of fit between the different distribution models. The Kolmogorov–Smirnov (K-S) test is one of the most common methods used to investigate the distribution of random variables and employs all the sample information. In brief, this method initially evaluates the parameters of the possible distribution model and subsequently calculates the maximum difference value (D_n) between the assumed distribution function and the order statistics. According to the significance level (α) and sample number (n), the corresponding critical value is taken from a K-S critical value table to determine whether the assumed distribution is reasonable [27]. If $D_n < D_{n,\alpha}$, the sample data are fitted with the assumed distribution function.

3. Results and Discussion

3.1. Relationship between Dynamic and Static MOE

The relationship between the dynamic and static MOE is shown in Figure 4 and Equation (4); it depicts the derived linear relationships and fitting results, and Equation (4) describes how the MOE_{Static} can be predicted based on the $MOE_{Dynamic}$.

$$MOE_{Static} = 0.791 \times MOE_{Dynamic} + 2.749 \ (R^2 = 0.758)$$
 (4)



Figure 4. Relationship between the dynamic MOE values and static MOE values.

From Figure 4, it was also found that the mean $MOE_{Dynamic}$ was very close to that of MOE_{Static} , with values of 15.81 GPa and 15.25 GPa, respectively, and a 3.7% difference between them. There was a strong linear correlation between the $MOE_{Dynamic}$ and MOE_{Static} values ($R^2 = 0.758$), indicating the ability of the FFV-determined $MOE_{Dynamic}$ values to evaluate the lumber mechanical properties, potentially replacing the static method. As the FFV test was easy and fast, while the full-size static MOE test method was time consuming and based on a complex mechanical test machine, the FFV method would reduce operation complexity and costs compared with the static MOE test processing, and is thus more suitable for large-scale factory production.

3.2. Differences in the Density and MOE_{Dynamic} between Natural and Planted Larch

3.2.1. Statistical Results of the Density and MOE_{Dynamic} Tests

By using the *Three Sigma Rule*, one natural larch sample and four planted larch specimens were rejected; the results are shown in Table 2 and Figure 5. The violin plots in Figure 5 contain the distribution information on the density and $MOE_{Dynamic}$. The box plots inside the violin plot present the 5th, 25th, 50th, 75th, and 95th percentile of the data from the bottom to top. The density and $MOE_{Dynamic}$ means are also represented as the mean confidence diamond plot inside the box plot.

Group	N	l	Density	M	OE_{Dynamic}		MOE _{static}			
Gloup	1	Mean (g/cm ³)	SD (g/cm ³)	CV	Mean (GPa)	SD (GPa)	CV	Mean (GPa)	SD (GPa)	CV
Natural larch	599	0.66	0.08	12.00%	15.52	2.97	19.12%	15.02	2.35	15.62%
Planted larch	596	0.57	0.06	11.12%	13.10	2.78	21.20%	13.11	2.20	16.75%

Table 2. Density	v and MOE statistics o	the two-dimensional	larch lumber types.
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Note: N is the number of samples, SD denotes the standard deviation, and CV is the coefficient of variation.



Figure 5. Density and MOE test results of the natural and planted larch dimension lumber. Note: The horizontal line in the boxplots are the 5th, 25th, 50th, 75th, and 95th percentile; inside the boxplot is the confidence diamond plot of the mean value, and outside the boxplot is the violin plot.

The natural larch dimension lumber density and MOE_{Dynamic} values exceeded those of the planted larch by approximately 15.8% and 14.8%, respectively. The average planted larch lumber density is in strict agreement with that measured from small clear wood samples by Zhou [28], who determined an average density of small clear wood samples from 30-year-old larch logs of 0.566 \pm 0.071 g/cm³. However, the average MOE reported by Zhou was 16.775 \pm 3.699 GPa, exceeding the $MOE_{Dynamic}$ and MOE_{static} of the full-size planted larch lumber. This indicates that the larch density determined from small clear wood specimens can reflect the global density of full-size dimension lumber, yet this was not true for negative MOE values. This may be attributed to the fiber grain deviation, knots, inside cracking, and other defects that reduce the lumber MOE yet have no significant impact on density. The planted larch test data reported in Zhou and the current study can act as a mutual verification. The lumber MOE was then tested using the full-size test method to evaluate the lumber mechanical properties. Results demonstrate the strong potential of the FFV method in determining the MOE_{Dunamic} of full-size lumber to predict MOE_{static} . The mean density and $MOE_{Dynamic}$ of 0.57 g/cm³ and 13.10 GPa, respectively $(MOE_{static} \text{ calculated as } 0.791 \times 13.10 + 2.749 = 13.11 \text{ GPa}, \text{ according to Equation (4)}), \text{ can}$ represent the mechanical properties of full-size planted larch lumber from Northeast China.

3.2.2. Significance Tests between Natural and Planted Larch

In order to determine any significant difference in density and $MOE_{Dynamic}$ between planted larch and natural lumber, we performed parametric (*t*-test) and non-parametric (Wilcoxon test) tests to compare the mean value differences of the two variables. The *t*-test was generally used on sample data that passed the normality (Shapiro–Wilk) and homogeneity (F-test) tests, implying significant differences in the density and/or MOE between the planted and natural larch dimension lumber. Non-parametric testing was applied to data that did not pass these tests. Table 3 reports the test results.

Experimental Conditions		Shapiro–Wilk Test		F	F-Test		Test	Wilcoxon Test	
		W	Prob < W	F Ratio	<i>p</i> -Value	t Ratio	Prob > t	Z	Prob > Z
Density Natural larch Planted larch	0.9976	0.5481		.0.0001 **		-0.0001 **	10.0405	.0.0001 **	
	Planted larch	0.9853	< 0.0001 **	1.5745	<0.0001	22.2776	<0.0001	19.0425	<0.0001
MOE _{Dynamic} –	Natural larch	0.9977	0.5863	1.1.100	0 1051	14 5501	<0.0001 **	13.5729	<0.0001 **
	Planted larch	0.9824	< 0.0001 **	1.1420	0.1051	14.3381			

Table 3. *t*-Test and Wilcoxon test results of the density and MOE.

Note: ** denotes significant differences at the 0.01 level.

The results reveal that the data failed the Shapiro–Wilk and F-tests, and thus the *t*-test prerequisites for density and $MOE_{Dynamic}$ were not met. Therefore, the subsequent analysis was based just on the Wilcoxon test. Significant differences were observed in the density and $MOE_{Dynamic}$ between planted and natural larch dimension lumber. In particular, the natural larch's $MOE_{Dynamic}$ values exceeded those of planted larch after combining with the mean value of Figure 5. The faster the growth of the planted larch under favorable silviculture measures, the lower the density, the greater the ratio value of the spring wood, and the wider the width of the growth ring, resulting in lower $MOE_{Dynamic}$ values for planted larch. Although the $MOE_{Dynamic}$ of the planted larch lumber was smaller than that of natural larch, once converted to MOE_{static} , it was still obviously greater than the MOE of SPF (Spruce–Pine–Fir from Canada), which is commonly used in light-frame buildings. For example, the average MOE of SPF with a No. 1 grade was approximately 10 ± 1.82 GPa [25]; thus, the average MOE_{static} of the planted larch lumber was 30% greater than that of SPF. Therefore, planted larch can effectively replace natural larch and is more resistant under bending compared to SPF.

3.3. Distribution Parameter of Density and MOE, and Their K-S Test

The K-S test was adopted to compare the goodness of fit between the different distribution models (Figure 6 and Tables 4 and 5). Here, for the normal and lognormal distributions, the critical values were calculated as $D_{599,0.05} = 0.886 / \sqrt{599} = 0.03620$ and $D_{596,0.05} = 0.886 / \sqrt{596} = 0.03629$, while the corresponding Weibull distribution values were determined as $D_{599,0.05} = 0.888 / \sqrt{599} = 0.03628$ and $D_{596,0.05} = 0.886 / \sqrt{596} = 0.03637$. Only the D_n is smaller than $D_{n,0.05}$, so the Weibull distribution with three parameters is accepted after the K-S test. Figure 6 and Tables 4 and 5 depict the K-S test results and distribution parameters.



Figure 6. Cont.



Figure 6. D_n values of the Weibull distribution compared with the K-S critical value. Note: D_n is the maximum difference value between the assumed distribution function and the order statistics, and $D_{n,0.05}$ is the critical value for the K-S test. Only the D_n is smaller than $D_{n,0.05}$, so the Weibull distribution with three parameters was accepted after the K-S test.

Table 4. K-S tests of the normal and lognormal distributions based	on the estimated	parameters.
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Samplas	Possible	Distribution Pa	arameters	Value of D	Critical Value (D. s.s.)	Reject or Accept	
Samples	Type Mean Variance Variate of D_n		Critical value $(D_{n,0.05})$	Reject of Accept			
ρ of natural larch $n = 599$	Normal Lognormal	$0.660\ 48 \\ -0.422\ 15$	0.006 28 0.014 99	0.031 16 0.054 24	0.036 20	Accept Reject	
<i>E</i> of natural larch $n = 599$	Normal Lognormal	15.023 27 2.696 95	5.507 48 0.026 02	0.016 94 0.036 55	0.036 20	Accept Reject	
ρ of planted larch $n = 596$	Normal Lognormal	0.568 21 -0.571 06	0.003 99 0.012 13	0.039 20 0.021 63	0.036 29	Reject Accept	
<i>E</i> of planted larch $n = 596$	Normal Lognormal	13.109 23 2.559 43	4.822 48 0.027 81	0.064 63 0.044 54	0.036 29	Reject Reject	

Notation: ρ is density, *E* is the dynamic MOE determined via FFV, D_n is the maximum difference value between the assumed distribution function and the order statistics, and $D_{n,0.05}$ is the critical value for the K-S test.

	Possi	ible Weibull	Distributio			Delector		
Samples	Location x _u	Shape k	Scale λ	Scale Mean Variance λ		Value of D_n	$(D_{n,0.05})$	Accept
a of natural larch $n = 599$	0	9.036 15	0.695 55	0.66	0.007 60	0.048 70	0.026.28	Reject
p of flatural fater $h = 577$	0.39	3.796 89	0.299 16	0.66	0.006 32	0.024 44	0.036 28	Accept
E of potential leads $u = 500$	0	6.948 94	16.024 67	14.98	6.425 59	0.042 22	0.026.28	Reject
E of natural farch $n = 399$	7.10	3.724 02	8.766 39	15.01	5.608 99	0.022 60	0.030 28	Accept
a of planted larch $n = 596$	0	9.042 21	0.597 05	0.57	0.005 60	0.075 71	0.026.27	Reject
p of planted laten $n = 390$	0.41	2.707 17	0.179 90	0.57	0.004 06	0.031 80	0.036 37	Accept
a of planted larch $u = 506$	0	6.252 06	14.052 77	13.07	5.942 08	0.067 66	0.026.27	Reject
p of planted laten $n = 390$	8.34	2.310 85	5.384 09	13.11	4.796 82	0.035 16	0.036 37	Accept

Table 5. K-S tests of the Weibull distribution with two and three parameters.

Notation: ρ is density, and *E* is the dynamic MOE determined via FFV. Only the Weibull distribution with two parameters, with a location of 0, and the Weibull distribution with three parameters with the smallest D_n value is shown in Table 5.

The figures and table results revealed that the natural larch lumber density exhibited a good fit with the normal and 3-parameter Weibull distributions, with the highest goodness of fit observed for the three-parameter Weibull distribution with location parameter $x_u = 0.39$. The $MOE_{Dynamic}$ of natural larch lumber fitted well with the normal and 3-parameter Weibull distributions, with the former exhibiting the best goodness of fit (Figure 6A). The planted larch lumber density exhibited a good fit with the lognormal and 3-parameter

Weibull distributions, with the former presenting the highest goodness of fit. The MOE of planted larch lumber was observed to fit well with the 3-parameter Weibull distribution at a location parameter equal to 97.6–98.9% of the minimum $MOE_{Dynamic}$, with the goodness of fit optimized at the location parameter 8.34 GPa ($x_u = 8.34$) (Figure 7D). In order to simplify the distribution model, the 3-parameter Weibull distribution was suggested to fit the density and $MOE_{Dynamic}$ of natural and planted larch as it passed the K-S test for the four test data types. Besides, Figure 6 also revealed that the distribution of the measured data of planted larch was left-biased, meaning that there were more samples with a low and medium density and elastic modulus. Thus, the Weibull distribution with three parameters was a better fit of the density and MOE distribution of planted larch full-size lumber.



Figure 7. Distribution histograms and fitting curves of larch lumber MOE.

3.4. Determine the Characteristic Based on Distribution of Density and MOE

The characteristic value is the 5th-percentile value at 75% confidence level, also known as the standard value in China according to GB 5005 [2], forms the basis of the design values and is crucial for the safety and reliability of wood constructions. According to ASTM D2915-10 [29] and Zhong Yong [30], both parametric and non-parametric methods can be used to calculate the characteristic value of the lumber density and MOE. The parametric method was used to calculate the characteristic value according to the formula $E_{k,e} = \overline{x} - k s$, where the *k* value is decided by the number of samples and the confidence level. If the average value \overline{x} and standard variation *s* were known, the characteristic value $E_{k,e}$ could be calculated. In turn, the non-parametric method was based on the order number of the test value to estimate the characteristic value, and the order was based on the sample number and confidence level. Generally, the parametric method is considered as more effective when the data distribution model is known in advance, while the non-parametric method is associated with smaller errors. Table 6 reports the determined characteristic values.

Sample	Statistical Value 5% Quantile under the Best Distribution			Characteristic Value			
	Mean	SD	Normal	Lognormal	Weibull	Parametric Method	Non-Parametric Method
ρ of natural larch (g/cm ³)	0.66	0.079	0.53	-	-	0.53	0.52
E of natural larch (GPa)	15.02	2.347	11.16	-	-	11.05	11.06
ρ of planted larch (g/cm ³)	0.57	0.063	-	0.47	-	0.46	0.47
<i>E</i> of planted larch (GPa)	13.11	2.196	-	-	9.83	9.39	9.67

Table 6. Characteristic values of density and MOE for the larch dimension lumber.

Notation: ρ is density, *E* is the dynamic MOE determined via FFV, SD denotes the standard deviation, and CV is the coefficient of variation.

The characteristic values of the density and MOE_{Dynamic} for natural and planted larch lumber via the parametric and non-parametric methods where highly similar, with differences of 1.92%, 0.01%, 2.13%, and 2.90%, respectively. The differences between the characteristic values calculated by the parametric method and the 5% quantile under the best distribution were 0, -0.99%, -2.13%, and -4.48%, respectively. The corresponding non-parametric method differences were -1.92%, -0.90%, 0, and -1.63%. This indicates that the characteristics of the density and $MOE_{Dynamic}$ for natural and planted larch calculated by the parametric and non-parametric methods were almost equal. The planted larch $MOE_{Dynamic}$ calculated by the parametric method was slightly smaller than that of the non-parametric method and the 5% quantile under the best distribution. This may be attributed to the MOE_{Dynamic} distribution model (Figure 6D), with the median mean value exceeding the mean value of the data. More specifically, with the exception of the natural larch lumber density, the characteristic values calculated by the parametric method were slightly lower than the non-parametric values. Thus, the parametric method can more effectively estimate the characteristic value for larch and should be the preferred approach to determine the characteristic values of density and MOE for natural and planted larch. The characteristic density values of natural and planted larch were determined as 0.53 g/cm³ and 0.46 g/cm³; the characteristic MOE_{Dynamic} values were 11.05 GPa and 9.39 GPa; and the characteristic MOE_{static} values in flatwise samples were $11.05 \times 0.791 + 2.749 = 11.49$ GPa and $9.39 \times 0.791 + 2.749 = 10.17$ GPa, respectively. By taking into account the horizontal adjustment factor, the characteristic MOE_{static} in edgewise values for natural and planted larch were 11.19/1.15 = 9.73 GPa (9730 MPa) and 10.17/1.15 = 8.84 GPa (8840 MPa); and the characteristic values of density were 0.53 g/cm³ (530 kg/m^3) and 0.46 g/cm^3 (460 kg/m^3), respectively.

By comparing the value with the requirement of EN 338:2016, *Structural timber*. *Strength classes* [31], the standard MOE value of natural and planted larch was able to meet the requirements of the standard modulus with grades C40 and C35. The standard MOE of both larch groups exceeded the standard modulus of elasticity for visual grade larch with an I_c grade in GB 5005, where the standard MOE should greater than 8.6 GPa [2]. Thus, the number of *MOE* tests for visual natural and planted larch lumber can potentially be reduced during factory processing. The grading of natural and planted larch should be performed using the FFV method as it is able to increase the characteristic values for high density and MOE lumber via increasing the mean value or decreasing the variation in larch.

4. Conclusions

The results presented in the current paper can serve as a point of reference to promote the application of natural and planted larch for wooden-based buildings. Based on the experimental tests and analysis, we determined the following key conclusions as follows:

1. A relatively strong linear relationship was observed between the dynamic and static MOE of the larch lumber, proving the FFV method as reliable for the testing of the dynamic and static MOE estimations of larch dimension lumber based on the equation $MOE_{static} = 0.791 \times MOE_{Dynamic} + 2.749$ ($R^2 = 0.758$).

- 2. According to statistical analysis and non-parametric testing, the density and MOE_{static} of the planted larch lumber were significantly lower (p = 0.01) than those of natural larch lumber, and the average density and MOE_{static} of planted larch were 13.6% and 12.7% lower those that of natural larch, respectively.
- 3. The density determined from clear samples could at times be used to evaluate the average density of lumber; however, this was not the case for the *MOE*_{static}. This was because the average density obtained from full size testing was very close to the average density of the small clear samples, yet the average *MOE*_{static} obtained from the full-size tests was significantly lower than that of the small clear specimens.
- 4. The 3-parameter Weibull distribution model optimally fits the density and MOE of natural and planted larch, as it was the only distribution to pass the K-S test. In particular, the distribution for the measured data was left-biased, and thus there were more samples with a low and medium density and elastic modulus.
- 5. The parametric method was demonstrated to be more effective in calculating the characteristic values of natural and planted larch compared to the non-parametric method. The standard value of MOE_{static} for natural and planted larch were 9.73 GPa and 8.84 GPa, and hence the MOE_{static} met lumber grades C35 and C30.

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