

Structural, Electronic and Vibrational Properties of $\text{YAl}_3(\text{BO}_3)_4$

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Table S1. Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ($\text{\AA}^2$) of $\text{YAl}_3(\text{BO}_3)_4$ single crystal.

Atom	x	y	z	$U_{\text{iso}}^*/U_{\text{eq}}$
Y	1.0000	1.0000	1.0000	0.0053 (3)
Al	0.44422 (18)	1.0000	1.0000	0.0060 (4)
B1	1.0000	1.0000	0.5000	0.0060 (13)*
B2	0.5570 (6)	1.0000	0.5000	0.0068 (10)*
O1	0.1494 (4)	1.0000	0.5000	0.0069 (7)
O2	0.4083 (4)	1.0000	0.5000	0.0086 (8)
O3	0.5506 (3)	0.8503 (3)	0.4794 (4)	0.0084 (5)

Table S2. The main bond lengths ($\text{\AA}$) of $\text{YAl}_3(\text{BO}_3)_4$ single crystal.

Y—O3 ⁱ	2.318 (2)	B1—O1 ^{xiv}	1.387 (3)
Y—O3 ⁱⁱ	2.318 (2)	B1—O1 ^{xv}	1.387 (3)
Y—O3 ⁱⁱⁱ	2.318 (2)	B1—O1 ^{xvi}	1.387 (3)
Y—O3 ^{iv}	2.318 (2)	B2—O3	1.369 (4)
Y—O3 ^v	2.318 (2)	B2—O3 ^{xvii}	1.369 (4)
Y—O3 ^{vi}	2.318 (2)	B2—O2	1.381 (7)
Al—O3 ^x	1.861 (3)	Al—O1 ^{xii}	1.916 (2)
Al—O3 ^{vii}	1.861 (3)	Al—O2 ^{xi}	1.927 (3)
Al—O1 ^{xi}	1.916 (2)	Al—O2 ^{xii}	1.927 (3)

Symmetry codes: (i) $y+1/3, x+2/3, -z+5/3$; (ii) $-x+y+2/3, -x+4/3, z+1/3$; (iii) $-y+5/3, x-y+4/3, z+1/3$; (iv) $x+2/3, y+1/3, z+1/3$; (v) $-x+4/3, -x+y+2/3, -z+5/3$; (vi) $x-y+4/3, -y+5/3, -z+5/3$; (vii) $-x+y+1/3, -x+5/3, z+2/3$; (viii) $-y+7/3, x-y+5/3, z+2/3$; (ix) $x+1/3, y-1/3, z+2/3$; (x) $y-1/3, x+1/3, -z+4/3$; (xi) $-y+4/3, x-y+5/3, z+2/3$; (xii) $-x+y-1/3, -x+4/3, z+1/3$; (xiii) $-y+4/3, x-y+5/3, z-1/3$; (xiv) $-x+y, -x+1, z$; (xv) $x+1, y, z$; (xvi) $-y+2, x-y+2, z$; (xvii) $x-y+1, -y+2, -z+1$

Table S3. Fractional atomic coordinates and isotropic displacement parameters ($\text{\AA}^2$) of $\text{YAl}_3(\text{BO}_4)_3$ powder.

Atom	<i>x</i>	<i>y</i>	<i>z</i>	<i>B</i> _{iso}
Y	0	0	0	0.65 (7)
Al	0.5571 (2)	0	0	0.91 (9)
B1	0	0	0.5	1.7 (2)
B2	0.4432 (8)	0	0.5	0.86 (18)
O1	0.8497 (4)	0	0.5	1.07 (13)
O2	0.5928 (6)	0	0.5	1.10 (13)
O3	0.4490 (4)	0.1509 (4)	0.5196 (4)	0.74 (11)

Table S4. Main bond lengths ($\text{\AA}$) of $\text{YAl}_3(\text{BO}_4)_3$ powder.

Y—O3 ⁱ	2.312 (3)	B1—O1 ^{iv}	1.396 (4)
Al—O1 ⁱⁱ	1.910 (3)	B2—O2	1.389 (9)
Al—O2 ⁱⁱ	1.912 (4)	B2—O3	1.382 (5)
Al—O3 ⁱⁱⁱ	1.862 (3)		

Symmetry codes: (i) $y-1/3, x-2/3, -z+1/3$; (ii) $-y+2/3, x-y-2/3, z-2/3$; (iii) $-x+y+2/3, -x+1/3, z-2/3$

Table S5. Calculated optimized lattice parameters and atomic positions of $\text{YAl}_3(\text{BO}_3)_4$ in comparison with the experimental data.

	DFT				Exp.	
<i>a</i> , ($\text{\AA}$)		9.0830			9.28485	
<i>c</i> , ($\text{\AA}$)		6.9881			7.23005	
<i>V</i> , ($\text{\AA}^3$)		499.28			539.79	
Y (3 <i>a</i>)	0	0	0	0	0	0
Al (9 <i>d</i>)	0.55782	0	0	0.5571	0	0
B1 (3 <i>b</i>)	0	0	0.5	0	0	0.5
B2 (9 <i>e</i>)	0.44134	0	0.5	0.4432	0	0.5
O1 (9 <i>e</i>)	0.84888	0	0.5	0.8497	0	0.5
O2 (9 <i>e</i>)	0.59178	0	0.5	0.5928	0	0.5
O3 (18 <i>f</i>)	0.44639	0.14994	0.52520	0.4490	0.1509	0.5196

Table S6. Calculated and experimental phonon frequencies (cm^{-1}) of $\text{YAl}_3(\text{BO}_3)_4$ together with proposed assignments. Notations: ss – symmetric stretching, as – antisymmetric stretching, π – out-of-plane bending, δ – in-plane bending, libr. – librations, tr – translations.

Calculated				Experimental		Assignment
A_1	A_2	E (TO)	E (LO)	Raman	Infrared	
1327.10	1368.07	1381.59	1490.32	1453	1383	BO_3 as
		1315.84	1344.37	1335	1348	
		1268.23	1292.78	1314	1281	
				1298	1254	
1039.74 959.24		1006.22	1008.16	1287		BO_3 ss
				1023		
				1015	984	
				982		
697.94	755.87	769.20	781.90	773	810	$\text{BO}_3 \pi$ and $\text{BO}_3 \delta$
				764	788	
					765	
				714	724	
	692.47 640.88	701.75 668.32	702.40 668.38	705	705	
				690	675	
				673	662	
				646		
585.47		613.95	642.29	620		$\text{BO}_3 \delta$ + Al tr.
				609		
				600	611	
				555	577	
397.86		497.28	535.53	527	535	BO_3 t. + Al tr.
				423	510	
				407	496	
				401	464	
	481.96 440.88 416.99 381.76	478.66 446.90 438.07 389.13	497.09 447.08 439.13 399.08	388	420	
				344		
				338		
				307		
273.98	307.83 281.30 220.40	270.74 230.85	271.19 230.87	303		BO_3 libr. + Al tr.
				262		
				228		
				137		
		118.52	135.86	120		Y tr.
						Y tr.
	63.83					

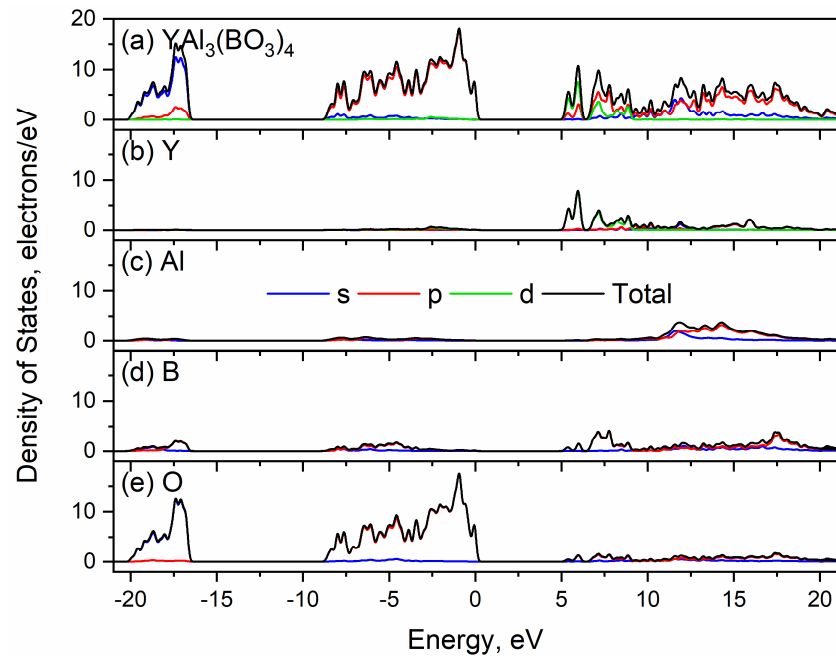


Figure S1. Total (a) and partial density of states (b), (c), (d), (e) of $\text{YAl}_3(\text{BO}_3)_4$.

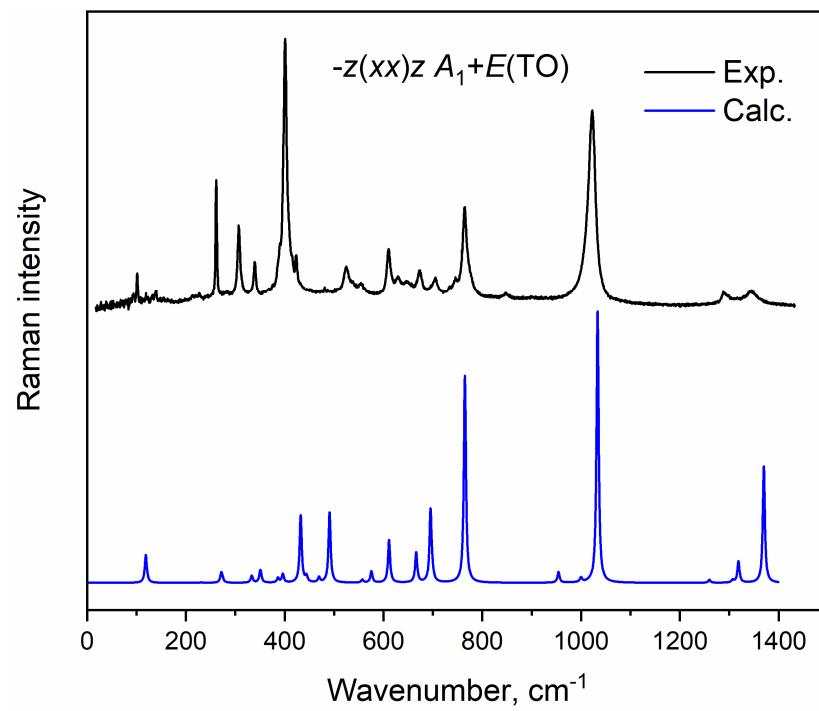


Figure 2. Polarized Raman spectrum of YAB single crystal obtained from the $-z(xx)z$ orientation.

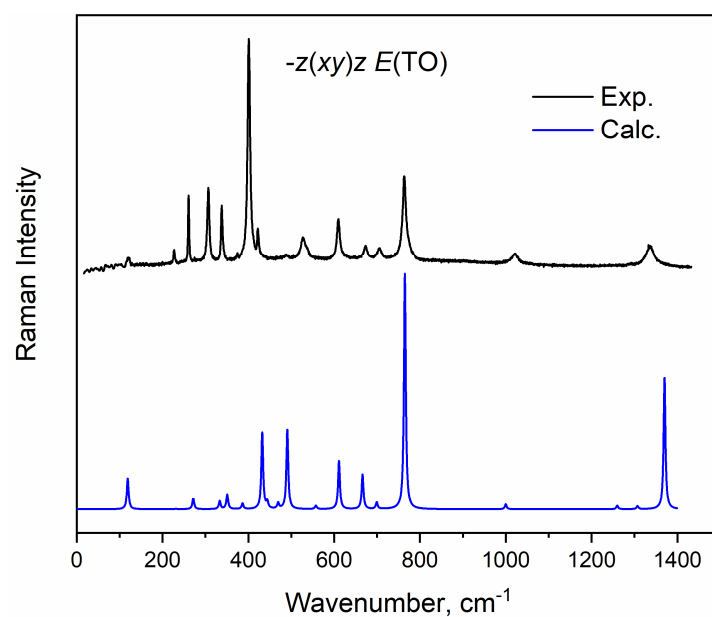


Figure S3. Polarized Raman spectrum of YAB single crystal obtained from the $-z(xy)z$ orientation.

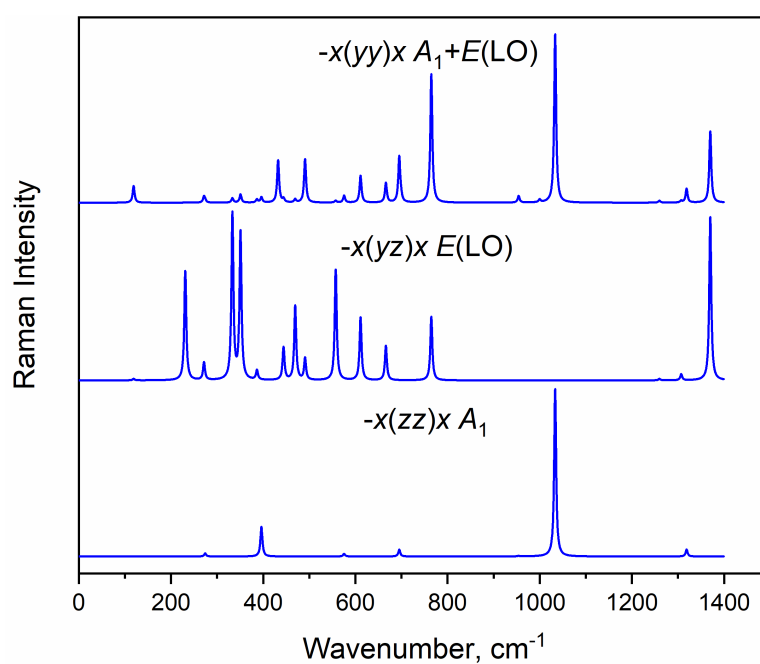


Figure S4. Calculated Raman spectra of YAB in the $-x(zz)x$, $-x(yz)x$ and $-x(yy)x$ polarizations.

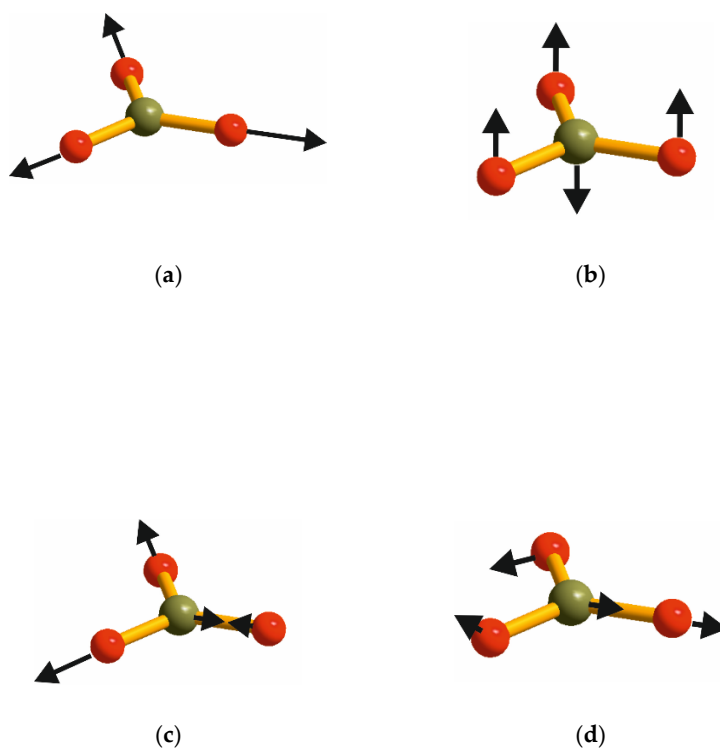


Figure 5. Normal modes of vibration of $[\text{BO}_3]^{3-}$ ions: (a) ν_1 symmetric stretching, (b) ν_2 out-of-plane bending, (c) ν_3 antisymmetric stretching, (d) ν_4 in-plane bending.



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