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Multi-Objective Structural Optimization Design of Horizontal-Axis Wind Turbine Blades Using the Non-Dominated Sorting Genetic Algorithm II and Finite Element Method

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Abstract: A multi-objective optimization method for the structural design of horizontal-axis wind turbine (HAWT) blades is presented. The main goal is to minimize the weight and cost of the blade which uses glass fiber reinforced plastic (GFRP) coupled with carbon fiber reinforced plastic (CFRP) materials. The number and the location of layers in the spar cap, the width of the spar cap and the position of the shear webs are employed as the design variables, while the strain limit, blade/tower clearance limit and vibration limit are taken into account as the constraint conditions. The optimization of the design of a commercial 1.5 MW HAWT blade is carried out by combining FEM analysis and a multi-objective evolutionary algorithm under ultimate (extreme) flap-wise load and edge-wise load conditions. The best solutions are described and the comparison of the obtained results with the original design is performed to prove the efficiency and applicability of the method.

Keywords: structural optimization design; horizontal-axis wind turbine (HAWT) blades; non-dominated sorting genetic algorithm (NSGA) II; finite element method (FEM); blade weight

1. Introduction

The blade is one of the most important components of wind turbines. A successful structural design of Horizontal-Axis Wind Turbine (HAWT) blades must satisfy a wide range of objectives, such as minimization of weight and cost, resistance to extreme and fatigue loads, restricted tip deflections, and avoiding resonances, but some of these objectives are in conflict [1]. Thus, optimization is a complex procedure characterized by several trade-off decisions aimed at finding the optimum overall combination of performance and economy. The decision-making process is very difficult and the design trends are not uniquely established. A number of different commercial wind turbine blades have been optimized by experimental tests and simplified analytical methods, but there is no clear evidence on which of these has to be regarded as optimal.

In general, the weight and cost of the turbine are the keys to making wind energy competitive with other sources of power [2]. Most modern wind turbine blades are made of glass fiber reinforced polymer (GFRP) due to its light weight, high strength and stiffness, superior fatigue and corrosion properties. However, as the size of the blades becomes larger, the blade weight grows rapidly (approximately as a cubic power of length) and GFRP cannot satisfy the structural requirements, which leads to the use of lighter and stronger materials such as carbon fiber reinforced polymer (CFRP) [3]. The usage of CFRP can efficiently decrease the blade weight, which has a multiplier effect throughout the system including the foundation, but since CFRP is almost 10 times more expensive than GFRP, the obvious disadvantage is increased material costs. The combination of GFRP and CFRP in an appropriate way to achieve optimal utilization (reducing both the weight and the material cost) is an important issue worthy of research. Thus, the weight and the material cost of the blade are set to be a multi-objective function in this study.

A number of papers have recently described how to deal with the structural design problems of blades using numerical models and optimization techniques. Liao [4] developed a multi-criteria constrained optimum design model to minimize the blade mass. The thickness and the location of layers on spar caps were selected as the design variables and an improved particle swarm optimization algorithm was used to search for the optimum solution. Similarly, the authors in [5,6] used the First-Order optimization method and a particle swarm optimization (PSO) algorithm combined with the finite element method (FEM) to minimize the mass of a 1.5 MW wind turbine blade, respectively. Hu [7] presented an automated optimization process, wherein the layer thickness, material type and orientation angle of GFRP/CFRP layers are optimized to reduce the total cost and mass of a HAWT composite blade based on ultimate limit state analysis. Jureczko [8] selected the shell thickness, the web thickness, the number and the arrangement of stiffening ribs as design variables. The design process of the blades is formulated as a multi-objective optimization task to minimize the blade vibrations, minimize the material cost and maximize the output generated, *etc.* However, only the mass of the blade is given in the final results. The results of other objectives and the parameters of the blade structure are not discussed in detail.

In these papers, optimization methods are described where a single objective function is taken into account at each time with the presence of constraints. The problem involving multiple objectives is addressed using a single objective function where the multiple objectives are combined by means of appropriate weights. Thus, these methods do not have the capability to obtain the real set of trade-off

solutions among multiple objectives. In many circumstances, however, the designer is interested in knowing the complete set of optimal blade configurations which correspond to the desired objectives.

This paper considers a two-objective optimization strategy of minimizing the weight as well as the material cost of a 1.5 MW HAWT blade. The main characteristics of the blade structure, namely, the number and the location of layers in the spar cap, the position of the shear webs and the width of the spar cap are employed as design variables. The optimization design for the blade is carried out under the action of ultimate flap-wise load, edge-wise load and their combination conditions using a non-dominated sorting genetic algorithm (NSGA) II and a FEM model of the blade for structural analysis.

2. Properties of the Blade

The original blade, with a length of 37 m and a weight of 6580.4 kg, is composed of three parts: root, skin and shear webs. Figure 1 shows the geometry and a typical structural cross section of the blade. The materials consist of a surface gel coat, reinforcing materials and unidirectional glass fiber for the skin and the spar cap. Balsa and PVC core materials are also used in the leading edge, the trailing edge, and the shear webs. Material properties of GFRP and CFRP are listed in Table 1.



Figure 1. The geometry and a typical structural cross section of the blade.

Table 1. Material properties of the glass fiber and carbon fiber.

Material	E_1 (GPa)	E_2 (GPa)	G ₁₂ (GPa)	<i>v</i> ₁₂	ρ (kg/m ³)	Cost (m ³)
GFRP	42.19	12.53	3.52	0.24	1910	1
CFRP	130.00	10.30	7.17	0.28	1540	10

The finite element method (FEM) has traditionally been used in the development of wind turbine blades mainly to investigate the structural performance in terms of global stress/strain levels, tip deflections and frequencies [9–12]. The FEM model of the proposed blade is created by using the well-known commercial software package ANSYS. Since its establishment and validation have been introduced in details in our previous work [6], only a brief overview will be provided here.

The FEM model of the blade is a parametric model, which means that the main structural parameters of the blade can be modified to create various blade models. The SHELL91 and the SHELL99 types are used for modeling the thick sandwich structures and the other parts of the blade, respectively. In order to simplify the model, the shear webs and the spar cap are connected directly without considering the effect of the adhesives. A regular quadrilateral mesh generation method is used

to generate elements with low aspect ratios to prevent producing erroneous results. In this work, a few changes in the spar cap of the model are made for a better parameterization, and the blade weight of the modified FEM model is 6555.2 kg. The FEM model of the blade is shown in Figure 2.





The loading on a wind turbine blade is stochastic and has components from the following sources: aerodynamic, gravitational, inertial (centrifugal and gyroscopic) and operational (gridfailure, braking, *etc.*). Design loads for a blade include the ultimate flap-wise load, edge-wise load and their combination in the form of a moment distribution along the blade length [13,14]. All the three load cases are considered to investigate the structural performance of the blade. The ultimate flap-wise load and edge-wise load distributions of the FEM model are shown in Figure 3.





3. Formulation of the Optimization Problem

3.1. Design Variables

The spar cap of the blade consists of laminates made by primarily unidirectional fibers to carry the flap-wise and edge-wise bending loads. Its thickness is typically large in comparison to those of the shear webs and the outer shells [15]. Consequently, the spar cap makes a major contribution to the overall weight and cost of a HAWT blade. The shear webs are designed to resist shear force within the cross-section of the foil when the blade is under the bending loads, their positions will have an influence on the structural performance (the strength and stiffness) of the blade. The overall weight and the cost of the blade can further decrease if the shear webs are repositioned appropriately. Hence, the spar cap parameters (the number and the location of layers in the spar cap, the width of the spar cap) and the shear webs parameters (the positions of the shear webs) are used as the design variables.

Figure 4 shows the original material layup of the spar cap. The region from 0.1 to 0.66 (shown in green) along the span-wise location of the blade will be optimized because it has a much greater number of layers than the other regions.

Figure 4. Original material layup of the spar cap.



Span-wise location of the blade Eight discrete control points are used to define the layup of the selected region, and the number of layers changes linearly between the control points, as shown in Figure 5. Point 3 to point 6 each have three parameters that are the location of layers, the number of GFRP and CFRP layers, while the other points each have two parameter that is the number of GFRP and CFRP layers. In addition, point 4 and point 5 have the same number of layers. Two more parameters L_1 , L_2 are used to define the positions of

Twenty variables in total are defined in this paper, which can be expressed in the following form:

the shear webs and the width of the spar cap, as shown in Figure 1.

$$X = [x_1 \ x_2 \ \dots \ x_n]^1, \quad n = 20$$
(1)

where x_1 to x_7 are the number of GFRP layers in the spar cap, x_8 to x_{14} are the number of GFRP layers in the spar cap, x_{15} to x_{18} are the location of layers in the spar cap, x_{19} is the position of the shear webs, and x_{20} is the width of the spar cap.



Figure 5. Parametric of the material layup of the spar cap.

3.2. Design Objectives

The purpose of the present work is to improve the structural characteristics of the blade, reducing both its overall weight and its cost. Therefore, a weight function and a function that combines the main materials cost of the blade represent the objective functions of the problem. The first objective function f_w is computed by normalizing the current weight w to the value of the original blade w_0 , in formula:

$$f_w = \min(w/w_0) \tag{2}$$

$$w = \sum_{i} \rho_i \times V_i \tag{3}$$

where ρ_i is the material density, V_i is the volume of the material.

The second objective function f_c is the ratio between the cost c of the current blade and the cost c_0 of the original blade, in formula:

$$f_c = \min(c \,/\, c_0) \tag{4}$$

$$c = \sum_{j=1}^{2} \sum_{i=1}^{7} (LN_{i}^{j} + LN_{i+1}^{j})(LL_{i+1}^{j} - LL_{i}^{j}) \times SW \times C^{j} + C_{c}$$
(5)

where LN_i is the number of layers of the control point; LL_i is the position of layers of the control point; *SW* is the width the spar cap; *C* is the material cost per cubic meter; C_c is the cost of the rest parts of the blade and is set to be a constant value; j = 1 represents the usage of GFRP while j = 2 represents the usage of CFRP.

3.3. Constraint Conditions

The structural design of the blade is a multi-criteria constrained optimization problem [4,8]. The strength, stiffness, dynamic behavior, stability and durability design requirements, such as blade/tower clearance limit, strain limit along the fiber direction, surface stress limit, avoiding resonance, buckling resistance and fatigue lifetime over 20 years should be well satisfied [10]. In this paper, the following constraint conditions are taken into account: the strain constraint, the tip deflection, the vibration

constraint, the buckling constraint and the fatigue lifetime constraint. These constraints represent the strength, stiffness, dynamic behavior, stability and durability design requirements, respectively:

(1) The strain constraint: the strain generated by the loads cannot exceed associated permissible strain [16]. As the permissible strain of GFRP is smaller than that of CFRP, the strain constraints of the parts use only GFRP and the parts use both GFRP and CFRP are defined different. This is expressed as follows:

$$\begin{cases} \varepsilon_{\max} \leq \varepsilon_{CFRP} / \gamma_{S1} = 0.35\% / (C_{4a} \times C_{4b}) \\ \varepsilon_{\max}' \leq \varepsilon_{GFRP} / \gamma_{S1} = 0.55\% / (C_{4a} \times C_{4b}) \end{cases}$$
(6)

where ε_{max} is the maximum strain of the parts use both GFRP and CFRP, while ε_{max} is the maximum strain of the parts use only GFRP, ε_{CFRP} and ε_{GFRP} are the permissible strains of CFRP and GFRP, γ_{S1} is the strain safety factor, C_{4a} and C_{4b} are factors decided by the manufacturing process and the material properties, respectively. For a prepreg process or a semi-automatic manufacturing process, $C_{4a} = 1.1$. For unidirectional fiber-reinforced composite materials, $C_{4b} = 1.0$.

(2) The tip deflection constraint: in order to avoid the risk of blade/tower collisions, the maximum tip deflection should be less than the set value. The Germanischer Lloyd (GL) regulations specify that the quasi-static tip deflection under the extreme unfactored operational loading is not to exceed 50 percent of the clearance without blade deflection. The International Electrotechnical Commission (IEC) 61400-1 specifications, on the other hand, require no blade/tower contact when the extreme loads are multiplied by the combined partial safety factors for loads and the blade material [1]. This can be expressed as follows:

$$d_{\max} \le d_a / \gamma_{S2} \tag{7}$$

where d_{max} is the maximum tip deflection; d_a is the allowable tip deflection; γ_{S2} is the tip deflection safety factor.

(3) The vibration constraint: a good design philosophy for reducing vibration is to separate the natural frequencies of the blade from the harmonic vibration associated with rotor rotation, which would avoid resonance where large amplitudes of vibration could severely damage the blade. This is expressed in the inequality form:

$$\left|F_{\text{blade}} - F_{\text{rotor}}\right| \ge \Delta \tag{8}$$

where F_{blade} is the first natural frequency of the blade, F_{rotor} is the frequency of the rotor rotation and Δ is the associated allowable tolerance.

(4) The buckling constraint: since the blade is a thin-walled structure, and it is subjected to large flap-wise bending moments, the surface panels near the blade root are particularly vulnerable to elastic instability, so the buckling problem must be addressed [17]. Generally, ultimate loads are deemed the most likely cause of blade buckling. In order to avoid buckling failure, the buckling load should be greater than ultimate loads. This can be expressed as follows:

$$\lambda_1 \ge 1.0 \times \gamma_{S3} \tag{9}$$

where λ_1 is a ratio of the buckling load to the maximum ultimate load, called lowest buckling load factor; γ_{S3} is the buckling safety factor. λ_1 is calculated using a nonlinear buckling analysis in ANSYS under the above ultimate load conditions.

(5) The lifetime fatigue constraint: the durability requirement for the turbine blades is typically defined as a minimum 20-year fatigue life (which corresponds roughly to 10⁸ cycles) when subjected to stochastic wind-loading conditions and cyclic gravity-induced edge-wise bending loads in the presence of thermally fluctuating and environmentally challenging conditions [18,19]. In most cases, the lifetime of the blade is controlled by its fatigue strength, which can be defined as follows [7]:

$$N = 10^{(1 - \frac{\sigma_{\max}}{\sigma_Y})/\beta} \ge \gamma_4 N_0 \tag{10}$$

where N is the number of cycles corresponding to peak working stress; σ_{max} is the maximum stress of the blade; σ_{γ} is the allowable material stress; β is a fatigue coefficient that varies for different materials. For the blade composite materials, the value of β is 0.10632 [20]. γ_{S4} is the lifetime safety factor; N_0 is the number of allowable cycles.

In addition, considering the manufacturing maneuverability and the continuity of the material layup, the design variables should be satisfied with the following inequality form:

$$\begin{cases} x_i^L \le x_i \le x_i^U & i = 1, 2, \cdots, 20 \\ x_j - x_{j+1} \le 0 & j = 1, 2, 3, 8, 9, 10 \\ x_{k+1} - x_k \le 0 & k = 4, 5, 6, 11, 12, 13 \end{cases}$$
(11)

where x^{L} is the lower bound of the variables; x^{U} is the upper bound of the variables.

The lower and upper bounds of the variables and the constraint conditions are shown in Table 2.

Parameter	Lower bound	Upper bound	Units
x_1	0	38	-
x_2	0	48	-
x_3	0	58	-
x_4	0	65	-
x_5	0	55	-
x_6	0	45	-
x_7	0	40	-
x_8	0	30	-
x_9	0	35	-
x_{10}	0	40	-
x_{11}	0	45	-
x_{12}	0	40	-

Table 2. Lower and upper bounds of the variables and the constraint conditions.

Parameter	Lower bound	Upper bound	Units
x_{13}	0	35	-
x_{14}	0	30	-
x_{15}	0.17	0.23	-
x_{16}	0.25	0.33	-
x_{17}	0.41	0.49	-
x_{18}	0.53	0.59	-
x_{19}	0.13	0.25	m
x_{20}	0.50	0.70	m
$\varepsilon_{\rm max}$	-	5,000	μ
E' _{max}	-	3,180	μ
d_{\max}	-	5.5	m
$F_{\rm blade}$	≤0.94 o	or ≥0.96	Hz
λ_1	1.30	-	-
N	$1.20 imes 10^8$	-	-

Table 2. Cont.

4. NSGA II

The NSGA II [21–23], which is an improved version of NSGA, is used in this paper. It is one of the most efficient and famous multi-objective evolutionary algorithms and has been widely applied to solve complicated optimization problems.

The method randomly generates an initial parent population P_0 of size N. The population is sorted based on non-domination and each solution is assigned a fitness equal to its non-domination level (1 is the best level, 2 is the next best level, and so on). An offspring population Q_0 with the same size as the parent population is created through recombination based on binary tournament selection and by inducing variations using mutation operators. From the first generation onward, the procedure is different. First, a combined population $R_t = P_t \cup Q_t$ of size 2N is formed, which is sorted according to a fast non-domination procedure. The new parent population P_{t+1} is formed by adding solutions from the first front till the size becomes N. Thereafter, the solutions of the last accepted front are sorted according to a crowded comparison operator and the first N points are picked. The new offspring population Q_{t+1} of size N is regenerated and the procedure is repeated in the subsequent generation. Detail description of the non-dominated sorting approach and the crowded comparison operator can be found in [21]. The flow chart for the algorithm is presented in Figure 6.

The NSGA II parameters used in this paper are listed in Table 3.

Parameters	Value
Number of individuals	20
Number of iterations	50
Probability of crossover	0.8
Probability of mutation	0.01

 Table 3. Implemented NSGA II parameters.



Figure 6. Flowchart of the NSGA II.

5. Results and Analysis

Figure 7 shows the Pareto front obtained by taking the minimum weight and the minimum cost of the blade as the optimization objectives. The curve of the Pareto front illustrates a monotone decreasing trend and divides the optimal region into two parts, *i.e.*, parts I and II. Part I is an ideal solution region that cannot be reached under the design conditions, while part II is a feasible solution region. The Pareto front solutions are the best trade-offs that can be reached in practice. The points on the right hand of the front identify design solutions having low weight yet high cost, whereas the points on the left hand of the front present design solutions having low cost but high weight. It cannot be said which point on the Pareto front is much better than others in theory. The choice of the solution in the practical design should be made according to the designer's preference for less weight or less cost.



To better explain the formation of the Pareto front, three optimized solutions extracted at different positions on the Pareto front are analyzed, as marked in Figure 7. The values of the design variables of blades A, B, C and the original design are listed in Table 4. Because CFRP is much lighter and stronger than GFRP, but more expensive, thus the costs of the three blades increase with the number of CFRP layers, while the total number of layers and the blade weights decrease.

Peremeter	Original design	Blade A	Blade B	Blade C	Unit
x_1	33	30	20	5	-
x_2	43	39	27	6	-
x_3	53	45	29	9	-
x_4	62	53	31	10	-
x_5	53	43	27	8	-
x_6	43	37	25	6	-
x_7	33	29	20	3	-
x_8	0	2	4	12	-
x_9	0	2	11	21	-
x_{10}	0	3	13	27	-
x_{11}	0	3	15	30	-
x_{12}	0	2	8	25	-
x_{13}	0	1	5	20	-
x_{14}	0	1	3	14	-
x_{15}	0.19	0.19	0.20	0.20	-
x_{16}	0.28	0.30	0.30	0.28	-
x_{17}	0.46	0.45	0.44	0.45	-
x_{18}	0.55	0.55	0.56	0.55	-
x_{19}	0.188	0.146	0.143	0.142	m
x_{20}	0.62	0.58	0.55	0.54	m

Table 4. Values of the design variables.

Figure 8 shows the total material layup and GFRP layup of the spar cap. It can be seen that the total number of layers and the number of GFRP layers both decrease obviously, especially from 0.19 to 0.56 along the span-wise locations of the blade after optimization, and the thickest region becomes smaller. It indicates that the two regions from 0.1 to 0.19 and 0.56 to 0.66 have a less impact on the objectives than the middle part. As the region from 0.1 to 0.19 withstands a larger bending moment, the number of layers in this region is a bit more than it in the region from 0.56 to 0.66 after optimization.





The position of the shear webs and the width of the spar cap both decrease after optimization. In order to find the effect of the position of the shear webs on the structural performance of the blade, a sensitivity analysis has been carried out. The result shows that the moving the shear webs to the centerline of the spar cap can reduce the maximum equivalent strain, *i.e.*, improve the strength of the blade. A smaller width of the spar cap can reduce the amount of materials, which is beneficial for reducing the cost as well as the weight of the blade.

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The structural performance of the blade is presented in Table 5. Compared with the original blade, the weights of the blades A, B, C decrease by 6.4%, 16.9% and 24.8%, respectively, while the values of cost change by 4.2%, -29.4% and -76.8%, respectively. The decrease of the maximum tip deflections, the increase of the first natural frequencies and the lowest buckling load factors from blade A to blade C are a result of increasing the number of CFRP layers, which is good for improving the blade stiffness and reducing the response of the blade being excited.

Scheme	Blade weight	Cost	Maxi equiv strai	imum valent n (μ)	Maximum tip deflection	The first natural frequency	The lowest buckling	The lifetime
			GFRP	CFRP	(m)	(Hz)	loadfactor	cycles
Original design	1.000	1.000	4074	4286	4.59	1.027	2.02	$2.28 imes 10^8$
Blade A	0.936	0.958	4859	3143	5.13	1.016	1.45	$1.73 imes 10^8$
Blade B	0.831	1.294	4253	3056	3.77	1.210	1.87	1.61×10^8
Blade C	0.752	1.768	4685	3131	3.01	1.328	2.33	1.32×10^{8}

Table 5. Structural	performance	of the blades
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The decrease in total number of layers leads to a degradation in the fatigue strength of the blade, thus the fatigue lifetime gradually approaches the critical value after optimization. Since the blade A has both lower cost and less weight than the original blade, it seems to be a more desirable result than the other blades by the consideration of the present two optimization objectives.

6. Conclusions

This paper illustrates a two-objective optimization method that uses NSGA II and a FEM model for the structural design of HAWT blades. The method is used to obtain the best trade-off solutions between the blade weight and the cost. The NSGA II handles the design parameters chosen for optimization and searches for the group of optimal solutions following the basic principles of Genetic Programming and Pareto concepts. The FEM model utilizes ANSYS to determine the structural performance of a HAWT blade, while it measures the fitness functions of the optimization as well.

The method has been applied successfully to a 1.5 MW commercial HAWT blade, and a set of trade-off solutions are obtained. The results indicate that the minimization of mass requires more CFRP, while the minimization of cost requires a good arrangement of GFRP combined with CFRP. Satisfactory results to reduce the weight as well as the cost of the blade are achieved and significant improvements in the structural performance of the blade are obtained by rearranging the original material layup in the spar cap, the width of the spar cap and the positions of the shear webs, which can be advantageous from the production and manufacturing requirements point of views.

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Conflicts of Interest

The authors declare no conflict of interest.

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