

Article

Aspen Plus[®] Process Simulation Model of the Biomass Ash-Based Treatment of Anaerobic Digestate for Production of Fertilizer and Upgradation of Biogas

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Abstract: The use of the commercial simulator Aspen Plus[®] could bring an amelioration in the accuracy of the predictions of the chemical species composition in the output streams of the anaerobic digestion process. Compared to the traditionally employed lumped models, which are elaborated from scratch, the models implemented in Aspen Plus[®] have access to a broad library of thermodynamic and phenomena transport properties. In the present investigation, a process simulation model for anaerobic digestion has been prepared by including a stoichiometric-equilibria reactor to calculate the extent of the ionization of the molecules present in the anaerobic digestate. The model characterizes the technical feasibility of anaerobic digestate stabilization, by means of biomass ash-based treatment, for the production of an organic fertilizer and potential biogas upgradation with the synthesis of ammonium carbonate. First of all, the titration of the manure digestate with the hydrochloric acid showed that a dose of 3.18 mEq/g would be required to attain the targeted pH of zero-point charge, upon addition of the sewage sludge ash in a ratio to the manure digestate of $0.6 \pm 0.2\%$. Secondly, the profiles of ammonia, carbon dioxide, and methane found in the biogas agree with the pH of the treated digestate and enable the upgrading of the biogas with the production of NH_4HCO_3 . The model needs to be further developed to ensure the standards are attained in all output streams of stabilized anaerobic digestate, biomethane, and isolated added-value chemical fertilizers.

Keywords: waste valorization; stabilization; nutrient recovery; closed-loop; modeling; circular economy; ammonium carbonate; organic fertilizer; bioenergy; biogas upgrading



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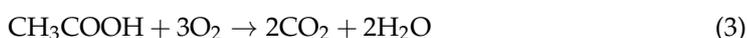
1. Introduction

Anaerobic digestate is the byproduct of biogas production through anaerobic digestion (AD) of the organic matter. Broadly speaking, AD is a waste valorization technology that has the simultaneous purposes of recovering energy while treating the waste before disposal or land application as soil amendment [1]. The easiest way of modeling anaerobic digestion is with the use of an unstructured unsegregated model. A model is considered unstructured if it does not involve the metabolism of the microorganism, and it is regarded as unsegregated if there is no differentiation between the species that are degrading the biomass [2]. First-order kinetics have been traditionally the most widely used for the modeling of substrate consumption and biogas release during AD [2–4]. This lumping approach has limitations, as, recently, a new approach (i.e., combining the first-order kinetic model and the Gamma distribution function) has been applied to elucidate that the so-called kinetic constants are not constant during the whole AD [5]. Acetic acid is synthesized in the penultimate stage of AD (known as acetogenesis) and is the simplest fermentable substrate for the production of biogas, as described in Equation (1). In the area of wastewater treatment, where AD has wide application for the treatment of sewage sludge, the concentration of substrates

is expressed as Chemical Oxygen Demand (COD) because this generalization allows the use of the same concentration units for different organic pollutants. Thereby, the reaction of biogas production can be further generalized as illustrated in Equation (2), taking into account that the COD of 1 g of CH₃COOH is 1.6 g of O₂, (following the stoichiometry of Equation (3)). It is important to mention that the biogas composition still depends on the type of substrate and, in the case of acetic acid, it corresponds to equal moles of CH₄ and CO₂ being produced (Equation (1)). The general relation between the consumption of substrate and the production of biogas corresponds to Equations (4) and (5). In order to model the production of biogas, it is necessary to introduce the theoretical yield or conversion coefficient of COD to biogas (α). Once again, α depends on the initial substrate and the biogas composition.



$$\text{Substrate (S; mg COD/L)} \rightarrow \text{Biogas (B; mL)} \quad (2)$$



$$\frac{dS}{dt} = -k(d^{-1}) \cdot S \xrightarrow{\text{solving}} S = S_0 \cdot e^{-k \cdot t} \quad (4)$$

$$B = \alpha \cdot (\text{mL/g COD}) \cdot V_{\text{reactor}} \cdot (L) \cdot (S_0 - S), \quad (5)$$

being

$$\alpha = 700 \frac{\text{mL} [50 \text{ vol.}\% \text{ CH}_4 + 50 \text{ vol.}\% \text{ CO}_2]}{\text{g COD}} \quad (@ 0^\circ \text{C} \ \& \ 1 \text{ atm})$$

It has been suggested that the basis of COD be replaced by volatile solids (VS), particularly at the time of conducting the biochemical methane potential (BMP) test with other residues different from wastewater, such as solid organic wastes and energy crops, because the determination of COD in solid heterogeneous substrates is difficult and open to uncertainty [6]. Since expressing the biogas production as mL/g VS is even a more general approach than the use of the COD basis, it is not possible to calculate analytically the theoretical yield of biogas in these units because the stoichiometric relation of these parameters needs to be determined empirically with a BMP test. According to the British regulation BSI PAS 110:2014 [7], the threshold value of stability of the anaerobic digestate is 450 mL/g VS. This means that the biogas released in the Residual Biogas Potential (RBP) test (i.e., following a particular protocol to conduct the BMP test) should not be greater than that upper limit by the end of the 28-day anaerobic assay, in order to allow the organic manure to be applied to land: *The concentration of volatile fatty acids (VFA) in a sample may be determined ahead of an RBP test, by means of gas chromatography. If a digestate sample's VFA result exceeds 0.774 g COD/g VS, this might indicate that the sample will fail a subsequent RBP test* [7]. It should be noted that initially tighter upper limits were proposed, both for the pre-screening of the anaerobic digestate samples (0.43 g COD/g VS) and for the RBP value (250 mL biogas/g VS) [8]. In a revision of the protocol, Banks et al. [9] suggested that reducing the incubation from 28 days to 10 days might be possible considering a threshold value of 200 mL biogas/g VS [9]. The early parameter estimation (of the kinetic constant and the biogas yield) is much appreciated by companies and plant operators whose decision-making processes cannot be held for the whole BMP test, which could run over 100 days [10]. In fact, the reason for all these adaptations of BMP/RBP protocols is to enable their widest application by the stakeholders of the agroindustry, in the simplest manner possible. This standardization pretends a better management of the organic waste: preventing the putrefaction of the organic sludge after land application and reducing the emissions of greenhouse gases. However, this explanation of AD in layman's terms should

not hinder the scientific community from using rigorous computational methods for further understanding the underlying biochemistry of the anaerobic fermentation, improving the design of the bioreactors, and assessing the technical feasibility of other operations around the AD plant. Similarly, taking advantage of the meticulous property and thermodynamic calculations supported by commercial packages for process engineering, such as Aspen Plus® [11], could also offer a better understanding of the AD process and enhance the monitoring of the upstream, mainstream, and downstream operations [12,13]. Particularly, this would allow the performance at the industrial-scale plant level to be analyzed, by following closely the interactions of the atomic elements and molecules of the feedstocks, during all processing steps.

The appraisal of novel processing conditions, such as the biomass ash-based treatment of the anaerobic digestate [14], is much more justified by the use of the Aspen Plus® simulation package, which allows a wide range of parameters to be specified. The biomass ash-based treatment of the anaerobic digestate aims to improve the properties of the organic material as a slow-release fertilizer, due to the sorption processes taking place. Advances in this technology should continue until reaching a high efficiency in the solid–liquid separation, given the high moisture content of the anaerobic digestate (95 wt.%) [15], the large quantities produced of this material (30,000 tonnes per year and per AD plant), and the cost of storage, transportation, and land application (GBP 10/tonne for a 10-mile delivery) [16]. The present article informs about the development of the process simulation model (PSM) of Rajendran et al. [11] in Aspen Plus® to monitor the biogas production and the valorization of anaerobic digestate by means of biomass ash-based treatment [14]. An assessment of the synergistic approaches that could reduce the cost of processing and handling the anaerobic digestate, aims to increase the viability of the treatment of anaerobic digestate and promote an overall enhancement of the circular economy [1]. The Aspen Plus® model that has been developed for simulating the conditions of the stabilization of the anaerobic digestate via ash-based treatment and the concentration profiles of the WS fraction of the digestate and the upgraded biogas were compared to the experimental findings and data from the literature. Therefore, the results of implementing upstream and downstream operations in the commercial package are presented, with emphasis on stabilizing the anaerobic digestate, upgrading the biogas, and producing a stream of CO₂ and NH₃ suitable for the manufacturing of ammonium bicarbonate (NH₄HCO₃).

2. Materials and Methods

The model that Rajendran et al. [11] made available was used as the base to build the PSM (Figure 1). It is regarded as a library model because 46 reactions were implemented in Aspen Plus® v10, some of them with the use of FORTRAN programming language [11]. The AD was represented by a two-stage process comprising a stoichiometric-equilibria reactor (B2) for the hydrolysis of the molecules of the substrate and a kinetic reactor (B3) involving the stages of acidogenesis, acetogenesis, and methanogenesis. The utilization of the model of Rajendran et al. [11] already represents an improvement with respect to the use of Anaerobic Digestion Model No 1 [17] because the latter is a lumping model while the former is a structure-based model (i.e., molecule-by-molecule), which gives greater insight that cannot be seen with the lumping approach. The model of Rajendran et al. [11] offers accurate predictions of biogas production under the testing conditions in which it has been designed. However, the chemistry of the anaerobic digestate has been neglected and it is necessary to include an ionization reactor for simple characterization purposes (e.g., determination of the pH of the anaerobic digestate) and to be able to build the subsequent downstream steps. For the modeling of the biomass ash-based treatment, the streams of HCl, sewage sludge ash (SSA), and manure digestate (MD) were mixed in an ionization reactor (B4) in which the rate of mass transfer and the dissociation of the compounds present in the gas, liquid, and solid phases were implemented (Figure 1). The calculation block B4 can be further justified by the need of stripping the CO₂ and NH₃ off the anaerobic digestate for the NH₄HCO₃ manufacturing process described by Wang

et al. [18]. A theoretical analysis of this downstream synthesis operation is included in the discussion section; although, this needs to be confirmed experimentally. Several challenges are expected, such as the fact that using biogas as stripping agent is less efficient than the use of biomethane (>98 vol.% CH₄) for that purpose [19]. On the other hand, the minimization of the requirements of energy and resources for the manufacturing of the NH₄HCO₃ is in line with the outcomes of the techno-economic assessments of Drapanauskaite et al. [20] and Centorcelli et al. [21], who simulated the preparation of the inorganic fertilizer as part of distillation processes.

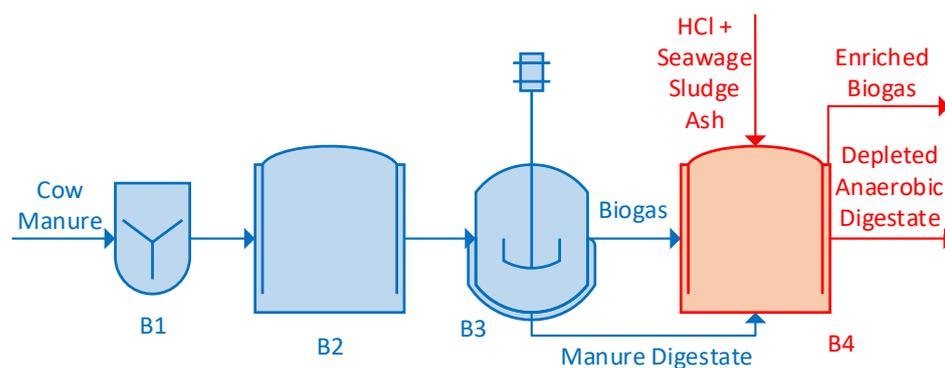


Figure 1. Process flow diagram including the calculation blocks: B1, mixer; B2, stoichiometric-equilibria reactor; B3, kinetic reactor; and B4, ionization reactor, where the dissociation equilibria and mass transfer constants of the chemical species contained in the biogas and the MD are implemented to monitor the stabilization with the ash-based treatment.

The stoichiometric-equilibria reactor (B4) was ruled by the instantaneous equilibrium of gas, liquid, and solid phases. For this purpose, it was necessary to assume a Damköhler number (i.e., reaction rate/mass flow rate) greater than 100 [22] and chemical reactions involving compounds in the same phase (either liquid, gas, or both), which would not be limited by the rates of chemical kinetics and mass transfer between the phases. The Electrolytes Wizard function of Aspen Plus[®] was applied to correlate some of the ionic species in the liquid phase with the temperature (Equation (6)). The parameters A, B, C, and D of Equation (6), where the equilibrium constants (K_{eq}) are the subject, were derived from either Aspen Plus[®] Components Databank (Table A1) or the literature (Table A2). Particularly, the Electrolytes Wizard does not include the acidic dissociation of amino acids and other organic compounds present in the anaerobic digestate as per the original PSM of Rajendran et al. [11] and some of these compounds would need to be added manually. The original PSM only considers the conversion of amino acids to acetic acid and the dissociation of the remaining amino acid molecules that were not converted to biogas was not taken into account. In order to successfully implement the ionization reactor in the Aspen Plus[®] model, it was necessary to estimate the properties of the system characterizing the blending of the MD and the SSA, such as the critical temperature and the heat of vaporization. The property method model used in this simulation was the Non-Random Two-Liquid model. The Aspen Plus[®] Components Databanks provided most of the properties for the components of the system, and when this information was not available, the parameters were determined with the method developed by Joback and Reid [23] and the R-PCER method. The ideal gas heat capacity for the components present in the system was calculated with the Aspen Ideal Gas Heat Capacity Polynomial Equation, while the Heat of vaporization was calculated with Watson's correlation [24].

$$\ln(K_{eq}) = A + \frac{B}{T} + C \times \ln(T) + D \times T \quad (6)$$

The mixer (i.e., B1 in Figure 1) was employed to merge the composition of multiple feedstock streams and to consider the impact of the SSA on the AD of cow manure (Table 1).

In fact, Rajendran et al. [11] initially included this calculation block to appraise the co-digestion of several substrates. The present investigation considered the SSA (Table 2) with the greatest phosphorus content reported by Franz [25], which was obtained over the co-combustion of 85 wt.% sewage sludge and 15 wt.% phosphate-rich bone meal as fuel. It is important to mention that the consideration of the SSA as one of the input streams of the blender (i.e., calculation block B1 in Figure 1) did not affect the AD process because the subsequent calculation blocks B2 and B3 (Figure 1), which were originally developed by Rajendran et al. [11], did not include the effect of the inorganic elements of Table 1. In the present work, the ash-based treatment of the anaerobic digestate was completed by combining the acidification with a second dose of ash in the downstream ionization reactor (B4). The purpose was to balance the stability granted by the isoelectric point of the anaerobic digestate [26,27] and the pH of zero-point charge (pH_{zpc}) of the wood ash [28].

Table 1. Composition of the liquid cow manure considered as feedstock for the PSM of Rajendran et al. [11] and based on the data reported by Budiyono et al. [29].

Component	Mass Fraction
H ₂ O (Water)	0.9400
C ₆ H ₁₂ O ₆ (Dextrose)	0.0100
NH ₃ (Ammonia)	0.0010
Cellulose	0.0220
C ₅ H ₈ O ₄ (Hemicellulose, Glutaric Acid, etc.)	0.0100
C ₅₇ H ₁₀₄ O ₆ (Triolein)	0.0004
C ₅₁ H ₉₈ O ₆ (Tripalmitin)	0.0004
C ₃₇ H ₆₈ O ₅ (1-palmitoyl-2-linoleoyl-sn-glycerol)	0.0004
C ₁₃ H ₂₅ O ₇ N ₃ S (Protein)	0.0030
C _{4.39} H ₈ NO _{2.1} (Keratin)	0.0018
Pseudo-component (Inert) ¹	0.0110
Total	1.0000

¹ Originally defined in case 1 using cow manure as the feedstock employed in AD of the work of Rajendran et al. [11].

Table 2. SSA composition reported by Franz [25] from the incinerator of Winterthur (Switzerland).

Compound	Mass Fraction
CaO	0.1120
SiO ₂	0.0987
Al ₂ O ₃	0.0321
Fe ₂ O ₃	0.0987
P ₂ O ₅	0.1037
MgO	0.0153
K ₂ O	0.0030
Na ₂ O	0.0237
TiO	0.0025
MnO	0.0005
SO ₃	0.0099
Cl	0.0000
H ₂ O (Moisture) ¹	0.0500
C (Black Carbon, Carbonate, etc.) ¹	0.4500
Total	1.0000

¹ Values estimated (50 wt.% of the SSA are black carbon and moisture) based on the description provided by Anderson [30] and Forbes et al. [31].

The results reported in this article correspond to 7 different process strategies: Case 1 is the foundation case (labeled as untreated MD) that served as a benchmark and it implied the production of MD using the original PSM of Rajendran et al. [11]. In Case 2, a stream of pure hydrochloric acid was incorporated at 0.1000 times the flowrate of the MD toward the ionization reactor (1HCl:10MD). In Case 3, a stream of hydrochloric acid was incorporated at 0.1176 times the flowrate of the MD towards the stoichiometric-equilibria reactor (1HCl:8.5MD). In Case 4, a stream of hydrochloric acid was incorporated

at 0.1212 times the flowrate of the MD toward the ionization reactor (1HCl:8.25MD). The remaining 3 cases are built on Case 3 (i.e., considering the previous acidification of the MD with the dose of 3.18 mEq HCl/g). In this way, in Case 5, the stream of SSA (Table 1) was incorporated at 0.0040 times the flowrate of the MD towards the stoichiometric-equilibria reactor (1SSA:1.76HCl:15MD). In Case 6, the stream of ash (Table 1) was incorporated at 0.0060 times the flowrate of the MD towards the ionization reactor (1SSA:1.18HCl:10MD). In Case 7, the stream of ash was incorporated at 0.0080 times the flowrate of the DM to the stoichiometric-equilibria reactor (1SSA:0.88HCl:7.5MD). According to the study of Zheng et al. [32], the amount of ash that should be added to the digestate to attain the most efficient dewatering is the same as the total solid content of the latter material, which, for the samples of SSA and MD, would correspond to a ratio of 0.06 (Table 2). The doses of SSA to MD employed in Case 5, Case 6, and Case 7 (0.0060 ± 0.0020) were an order of magnitude lower than the specification provided by Zheng et al. [11], due to the intended preparation of a solid granular fertilizer with the targeted nutrient profile N/P/K 3/1/1 [14]; although, attaining this ratio depends on the number of nutrients that remain in the water-soluble (WS) fraction after the solid-liquid separation. The results of the Aspen Plus[®] simulation were compared against those previously obtained experimentally and with the software visual MINTEQ [28]. The ANOVA test ($p < 0.05$) was performed with Microsoft Excel[®] to identify significant differences between the trends observed.

3. Results

3.1. pH of the Treated Digestate: Simulation and Experimental Results

Figure 2 shows the pH results of MD acidified with HCl (Cases 2–4) using doses in the range of 2.70–3.28 mEq/g, which were previously employed in the preparation of blended fertilizers with wood fly ash (WFA), wood bottom ash (WBA), food waste digestate (FWD), and agrowaste (PVWD) [28]. The simulation with Aspen Plus[®] does not provide standard deviation for single runs, but the number of iterations was set up to 500 in order to achieve convergence with a tolerance error of 0.0001, 0.00075, 0.00075, and 0.0005 in the calculation blocks B1, B2, B3, and B4 (Figure 1), respectively. Figure 3 illustrates the deviation of the buffer capacity of the digestate: experimental and simulation inflection points of the M-alkalinity of anaerobic digestate. The model predicts a higher buffer capacity than what was found experimentally (0.5–1 mEq HCl/g digestate) and with visual MINTEQ titrations (2–2.5 mEq HCl/g digestate). The trends were similar in the sense that both software packages predicted a higher buffer capacity for the anaerobic digestates than what was found experimentally (Figure 3). This might be related to the fact that the nature of the digestates tested was different: MD, FWD, and PVWD. The FWD presented a greater buffer capacity due to the higher content of ammoniacal nitrogen ($\text{NH}_4^+\text{-N}$) than the PVWD. It is important to highlight that the buffer effects of the VFA were not accounted for in the visual MINTEQ simulation, which could explain the greater buffer capacity of MD found in the Aspen Plus[®] simulation (i.e., Cases 1–4; Figures 2–4). On the other hand, as elucidated in the previous work [33], the impact of the acid added to the anaerobic digestate on the pH is related to both the concentration of free H^+ _(aq) and the sorption processes involving the anionic species of the acid, particularly in the case of H_2SO_4 and $\text{CH}_3\text{CH}(\text{OH})\text{COOH}$. Therefore, the dose of acid is better reported as mEq acid/g digestate rather than as mmol H^+ -acid/g digestate [28]. The severe acidification of the anaerobic digestate ($\text{pH} < 4$) can be justified by working at the isoelectric point of this material [26,27] and the pH_{zpc} upon addition of the ash, to maximize the sorption phenomena underlying the stabilization of the blended fertilizer. Following this balanced approach, case 3 with a pH of 4.10, which involved a dose of 3.18 mEq HCl/g MD, was used as the base for conducting the addition of the SSA in cases 5 to 7.

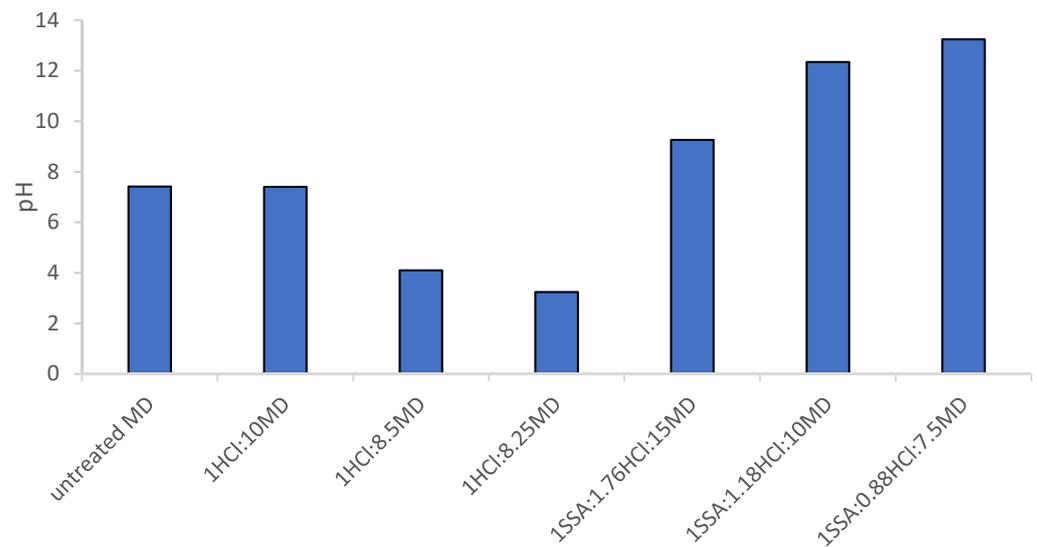


Figure 2. Effect on the pH of altering the parameters in the process represented in Figure 1 following HCl doses of 2.70 mEq/g MD (1HCl:10MD), 3.18 mEq/g MD (1HCl:8.5MD), and 3.27 mEq/g MD (1HCl:8.25MD) and via addition of SSA to the MD according to the ratios with regard to the dry matter of the digestate of 1/15 (1SSA:1.76HCl:15MD), 1/10 (1SSA:1.18HCl:10MD), and 1/7.5 (1SSA:0.88HCl:7.5MD).

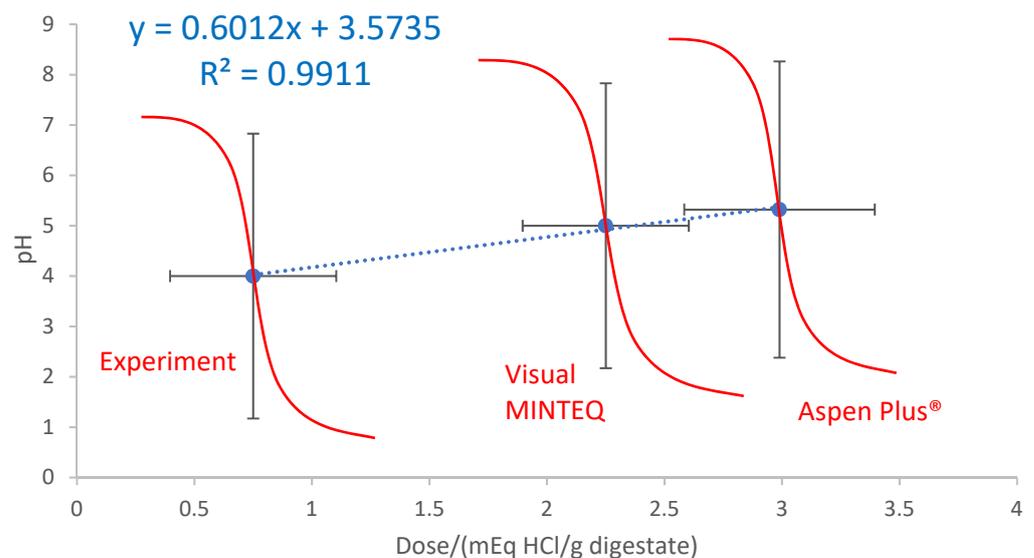


Figure 3. Deviation of the buffer capacity of the digestates: Inflexion points (in blue color) of the M-alkalinity of anaerobic digester digestate (schematic titration curves represented in red color) found with 3 titration methods: Experiments and modeling with Visual MINTEQ and Aspen Plus® (considering the cases 1HCl:10MD, 1HCl:8.5MD, and 1HCl:8.25MD in Figure 2).

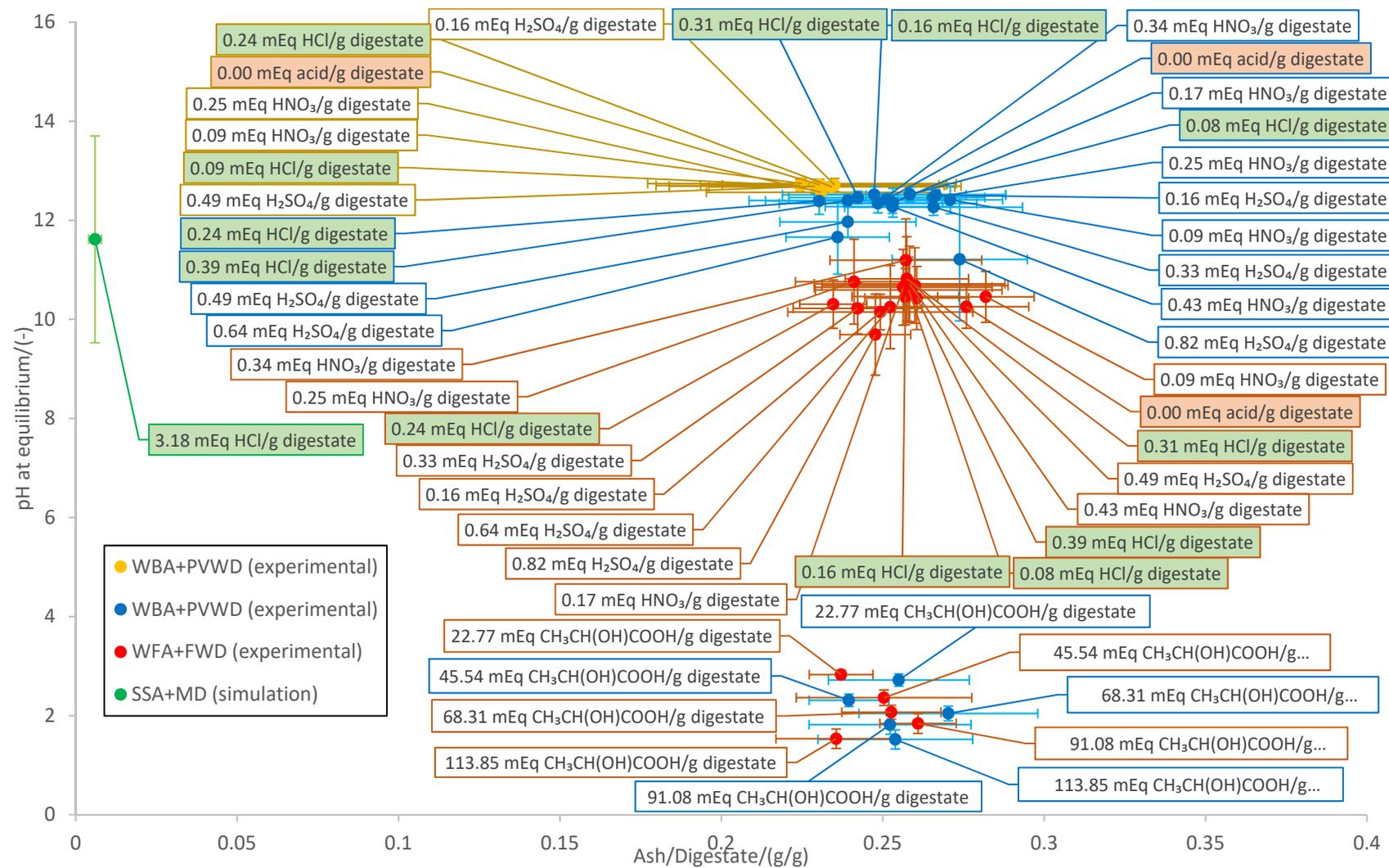


Figure 4. Dependence of pH on the blending ratio determined in the Aspen Plus[®] simulation (SSA+MD; including cases 5, 6, and 7) and the experimental work previously reported [28,33].

Figure 3 also establishes the correlation of the experimental pH, which is directly measured with a pH probe in the lab, and the pH calculated in the simulations (visual MINTEQ and cases 2 to 4 of Aspen Plus[®]) with the concentration of free-H⁺ (mol/L), which could be found at a particular acid dose (mEq/g digestate). There is a significant difference in the buffer capacity of the soil organic amendment determined through the three methods, particularly in terms of the dose of HCl ($p < 0.05$). The deviation can be explained by the fact that the simulations (visual MINTEQ and Aspen Plus[®]) overestimate the inflection point of the M-alkalinity of the anaerobic digestate compared to the experimental pH [28], leading to a significantly greater consumption of acid reagent, which increases the cost of processing the anaerobic digestate. The large error bars in Figure 3 are due to the calculation of the average value of pH in the inflection point of the titrations (both experimental and simulation), considering the highest and lowest pH values of the schematic titration curve represented in red color (Figure 3).

Figure 4 compares the pH range obtained with the Aspen Plus[®] simulation (11.61 ± 2.09), using a dose of 3.18 mEq HCl/g MD and blending ratio (SSA/MD) of 0.0060 ± 0.0020 , to the experimental data reported by Moure Abelenda et al. [28] and to the first set of experiments conducted by Moure Abelenda et al. [33]. Despite the HCl dose employed for the Aspen Plus[®] simulation being ~10 times greater than that of the other acids (H₂SO₄, HCl, and HNO₃), although ~10 times lower the dose of lactic acid, the trend was not followed for the pH of the blend SSA+MD (Figure 4). The pH of the SSA+MD should be greater than 2.71 ± 0.12 but lower than 11.21 ± 1.24 (Figure 4). It is important to highlight that the Aspen Plus[®] simulations were conducted with the composition of the SSA of the Winterthur incinerator (Winterthur, Switzerland) originally reported by Franz [25]. Franz [25] did not include the characterization of the loss of ignition for the determination of other elements that might be present in the SSA (e.g., moisture and carbon), but it was reported that the SSA was poorly crystallized, based on the mineral analysis via X-ray diffraction. In fact, Anderson [30] informed that about 70% of SSA consists of glassy-phase material. Therefore, assuming the content of carbon and moisture as reported in Table 1 (i.e., 50 wt.% of the SSA are black carbon and moisture) leads to a more reliable Aspen Plus[®] model because a lower pH of the blend SSA+MD will be obtained, due to the lower content of alkaline elements in the SSA. The Aspen Plus[®] model also needs to be improved by oxides of elements such as aluminum, with an amphoteric behavior, which act as a base under low pH and as an acid under high pH. On top of that, the alkaline elements were inputted in the model as hydroxides, formed upon reaction of the oxides with water; although, the SSA stream would be less basic if the metals of the SSA were in the form of carbonates. Several conditions could explain the chemical speciation of the metals in the ash derived from an incineration process at mild temperature conditions (<1000 °C), as described by Franz [25], including the lengthy storage and the reaction of the SSA with the CO₂ of the atmosphere [34]. It is necessary to use a factorial design of experiments to ensure that several parameters (i.e., type of digestate, type of ash, and acidification dose of the anaerobic digestate prior to adding the ash) are not changing at the same time when conducting the simulation. The most important conclusion that can be inferred based on Figure 4 is that under the conditions studied, the pH_{ZPC} (11.21 ± 1.24 – 12.74 ± 0.11) was always attained for the blend of acidified digestate and ash, unless the lactic acid was employed as acidification agent.

The previous investigation described the need to combine the FWD with a low share of fine ash, such as the WFA, to minimize the increase in pH and maximize the sorption of ammoniacal nitrogen [28]. Although the high NH₄⁺-N content of the FWD has a buffer effect (associated with the P-alkalinity of the anaerobic digestate) that avoids drastic changes in pH, the PVWD is more suitable as it might not lead to an excess of NH₃ volatilization (beyond the optimum ratio of NH₃ to CO₂ for the production of NH₄HCO₃; Equation (9)). This is due to the greater content of undigested vegetable fiber of the PVWD compared to the FWD, which makes the former digestate more suitable to tolerate the greater basicity of the WBA. In fact, the dose of ash added to the anaerobic digestate was found to be less

relevant than the properties (e.g., particle size) and composition (e.g., concentration of basic elements) of the ash to determine the final pH of the blend. For this reason, the difference in pH due to the dose of ash is not significant ($p < 0.05$), except when lactic acid was used as an acidification agent. The simulation with Aspen Plus[®], testing the addition of the SSA to the MD (cases 5–7; Figure 2) appears to have more sensitivity than working in experimental conditions. Therefore, a limitation of the simulation with Aspen Plus[®] is that the model offers more control over the pH of the blend than the experimental conditions, and this might be misleading in the design of the valorization process of the anaerobic digestate via ash treatment. For example, in the simulation the pH_{zpc} can be attained with a milder dose of ash, saving the acid reagent that would be necessary for the prior acidification of the anaerobic digestate to operate at the best conditions for the chemical stabilization [35].

3.2. Nutrient Profile of the Blend of Ash and Digestate in the Stabilization Process

The profile of the WS nutrients in the seven cases evaluated in the present study is shown in Figure 5. The WS fraction of the organic soil amendment is more reactive than the water-insoluble (WI) fraction. This is important because the WS nutrients are absorbed in the rhizosphere by the plant roots, but, also, this fraction of nutrients is more prone to be lost via leaching and volatilization. According to the data represented in Figure 5, the greatest change in availability was found in the WS K, which increased progressively until reaching a maximum in Case 5 (1SSA:1.76HCl:15MD). The outlier value of WS K in Case 2 (1HCl:10MD) that does not fit with the observed trend for the other six cases could be related to the fragility of the model. Thereby, the profile of WS K can be explained by the fact that more severe acidification leads to more solubilization of metals [36]. In addition, the SSA is also a source of K that increases the WS K concentration, but as the pH of the blend becomes closer to the pH_{zpc} , the concentration of the WS nutrients is reduced, due to the sorption processes responsible for the chemical stabilization that enhance the properties of the manure as controlled release fertilizer. As can be seen in Figure 5, the ratio of WS N to WS P is kept below a value of one in all cases, with the exception of case 7 (1SSA:0.88HCl:7.5MD). The increase in the concentration of WS N could be related to the ammonification phenomenon resulting from the mineralization of WI organic nitrogen [37]. In fact, Figure 6 shows the increase in inorganic nitrogen (mainly NH_4^+ -N) in the WS fraction in case 6 (1SSA:1.18HCl:10MD) and case 7 (1SSA:0.88HCl:7.5MD) due to the high pH. In the manufacturing of a slow-release fertilizer, it is important to pay special attention to the rate of nutrient release and the concentration of nutrients in the WI fraction. The mass balances of nitrogen, carbon, potassium, phosphorus, magnesium, calcium, and sulfur, considering the different phases implemented in the stoichiometric-equilibria reactor (calculation block B4 of Figure 1), can be established with the research data collected from the simulation of each of the seven cases, which are offered as Excel files in the Supplementary Materials: the most relevant data have been summarized in an MS Word file (Tables S1–S3).

The balanced use of the HCl and ash allows the pH_{zpc} in the blend with the digestate to be reached and takes advantage of the amphoteric behavior of some of the components of the ash, because this inorganic material comes in contact with the isoelectric point of the anaerobic digestate. The equilibrium constant of the amino acids that remain in the manure digestate, because they were not converted to VFA and biogas, can be more than a single value because of the presence of several functional groups. Depending on the pH of the medium and the isoelectric point of each amino acid, priority will be given to the release of a proton from a particular functional group. For example, tyrosine has three different dissociation constants corresponding to the carboxyl group, the protonated amine group, and the phenol group (Table A2). In this way, the priority of proton release from tyrosine depends on the pH as follows: below a pH of 2.20, there is no proton release; below a pH of 9.11, the carboxylic acid releases its proton; below 10.07, the protonated amino group releases its proton; and above the pH of 10.07, finally, the phenol group releases its proton. This means that the isoelectric point of the tyrosine, at which the zwitterion is stable and

this amino acid has a net charge of zero, ranges from a pH of 2.20 up to 9.11. As this amphoteric behavior stabilizes the manure digestate because it minimizes the repulsion between molecules, the addition of the SSA as a nutrient supplement needs to be planned accordingly since the components detailed in Table 1, such as the Al_2O_3 , can also act as an acid or as a base depending on the pH. In this way, the addition of the SSA can further reduce the repulsion between molecules, promote the solid–liquid separation, and allow the dewatering when the blend reaches the pH_{zpc} .

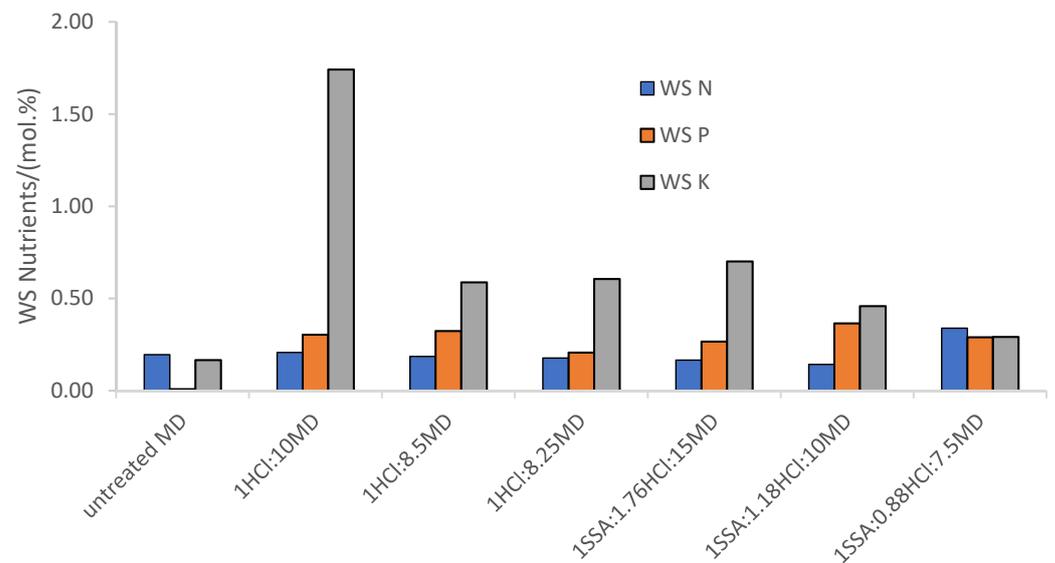


Figure 5. Profile of WS N, WS P, and WS K in the treated MD with HCl and SSA.

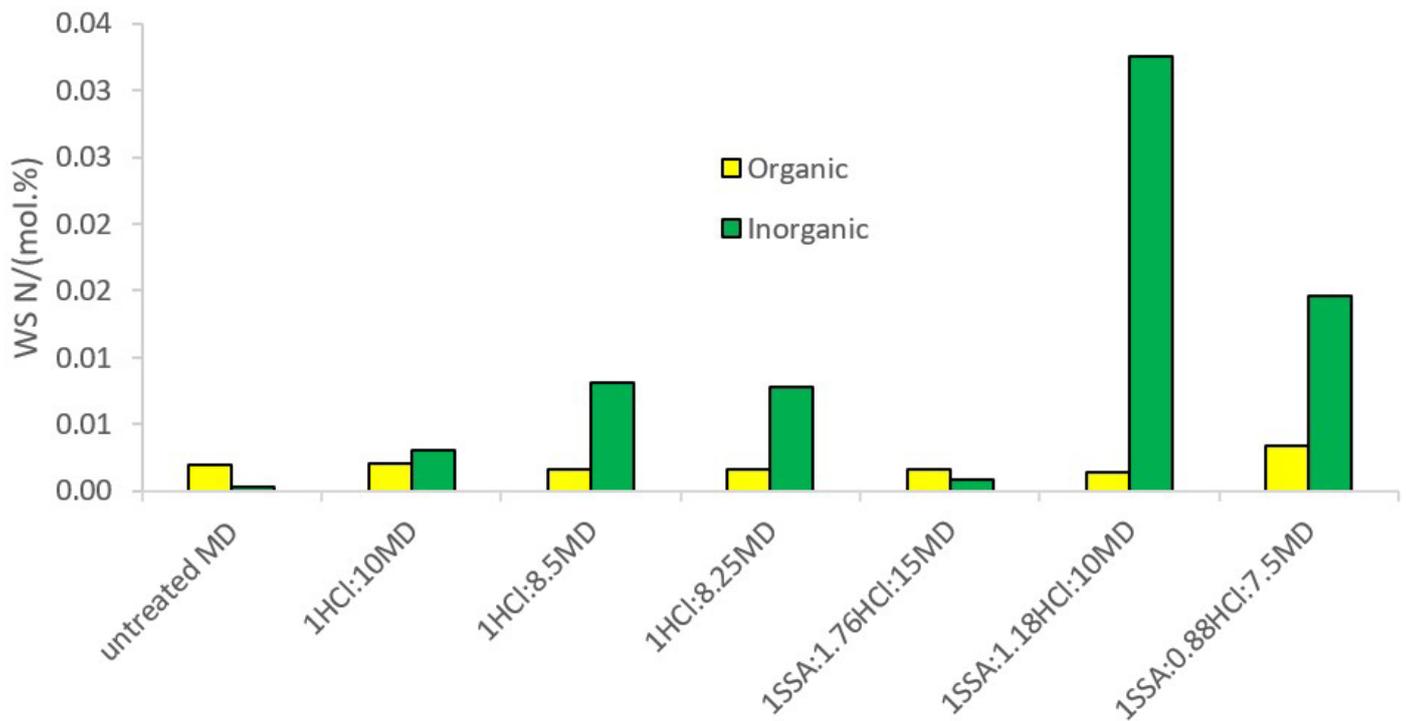


Figure 6. Share of WS organic and inorganic nitrogen in the treated MD with HCl and SSA.

Figure 7 represents a process for the preparation of the blended fertilizer of ash and digestate and the synergistic upgradation of the biogas and production of NH_4HCO_3 in a closed-loop process, which is techno-economically better regarded than the production

of $(\text{NH}_4)_2\text{SO}_4$ [20]. The ash-based treatment of the digestate at the pH_{zpc} generates a gaseous stream containing CO_2 and NH_3 that could be used for the synthesis of NH_4HCO_3 . (Equation (9)). The Aspen Plus[®] simulations of the present article are suitable for the design of the block that is depicted in Figure 7 in red color. In line with the simulation based on the calculation block B4 (Figure 1), and as in the process designed by Wang et al. [18] for the manufacturing of NH_4HCO_3 , in Figure 7, the stream of biogas coming out of the anaerobic digestion plant enters the stabilization tank as a stripping agent. The stripping process can be enhanced by using biomethane (>98 vol.%) rather than biogas, as Burke [19] described in the ammonium bicarbonate patented process. In any case, conditions of the pH_{zpc} employed allow the release of NH_3 and CO_2 . Depending on the carbonate content of the ash, the amount of CO_2 released could increase significantly upon addition of the inorganic material to the digestate at the isoelectric point, shortly before the pH of the blend rises to reach the pH_{zpc} . In the case where not enough CO_2 was available in the stripped gas (Equation (17)), the cooling and scrubbing shower of Figure 7 could operate with a diluted solution of H_2SO_4 to produce primarily $(\text{NH}_4)_2\text{SO}_4$ and, to a lower extent, NH_4HSO_4 and NH_4HCO_3 , as described by Ukwuani and Tao [38]. Under an excess of H_2SO_4 in the scrubbing solution, the formation of NH_4HSO_4 will prevail [38] and the condensed water may contain some traces of H_2SO_4 , but this compound will not affect negatively the stabilization treatment of the digestate with ash, upon recirculation of the condensed aqueous scrubbing solution.

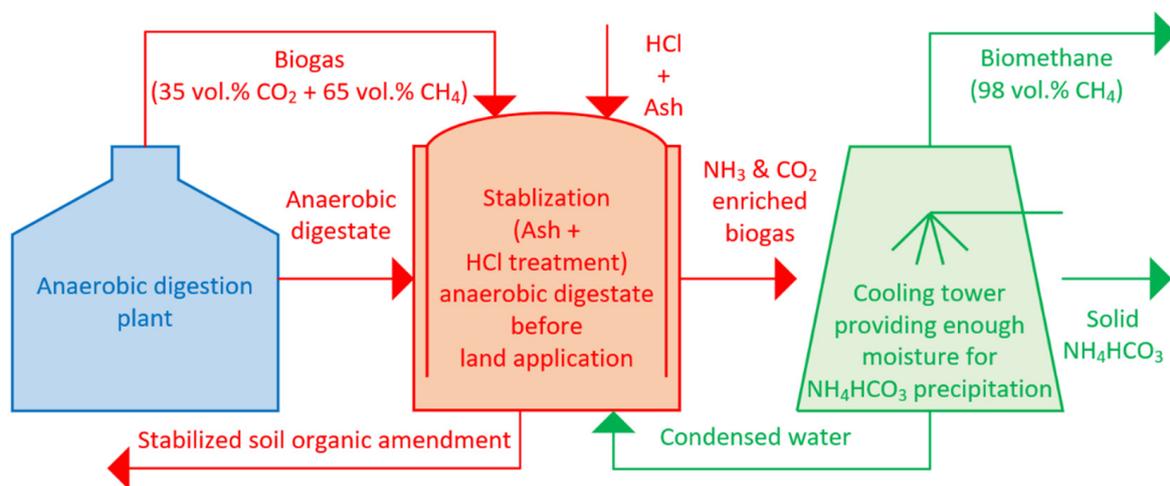


Figure 7. Ash-based treatment of the anaerobic digestate (present investigation in red color) for the production of NH_4HCO_3 and upgrading of biogas (future research in green color).

3.3. Composition of the Biogas Released from the Stabilization Process of the MD with the SSA

Figure 8 shows that the volatilization of NH_3 is only significant at high pH and this trend is contrary to the volatilization of CO_2 . In this way, the highest CO_2 released is attained with the HCl acidification of MF, prior to the addition of SSA (Figure 9). Case 5 represents an exception to the expected trend and can be explained by the fragility of the Newton method-based solver of the model, which has been found sensitive to the initial solutions of the large number of nonlinear equations associated with the chemical and physical equilibria. Finally, the profile of CH_4 in the biogas can be explained by the fact that the release of the CO_2 could be representative of the content of the former gas; thus, when the release of CO_2 was promoted, the share of CH_4 in the biogas was lower and vice versa (Figure 10).

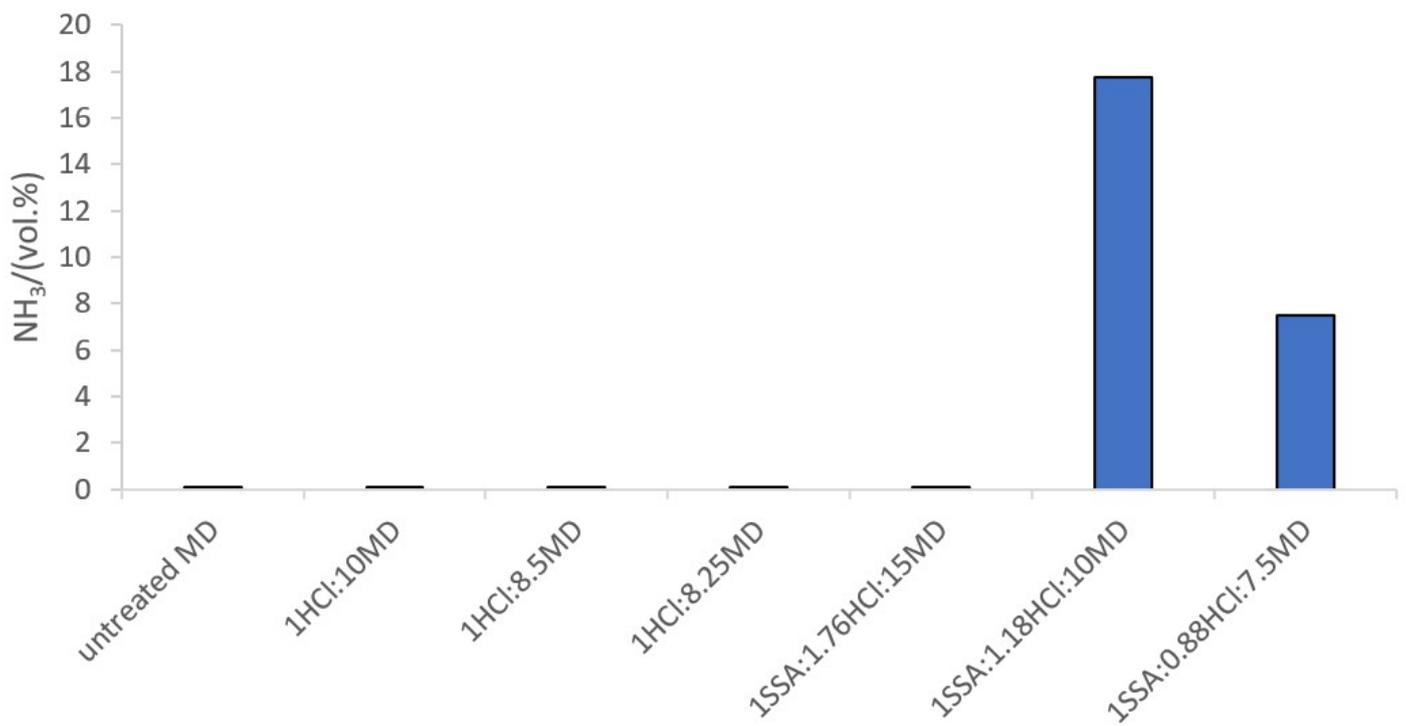


Figure 8. Ammonia content in the biogas for the 7 cases evaluated.

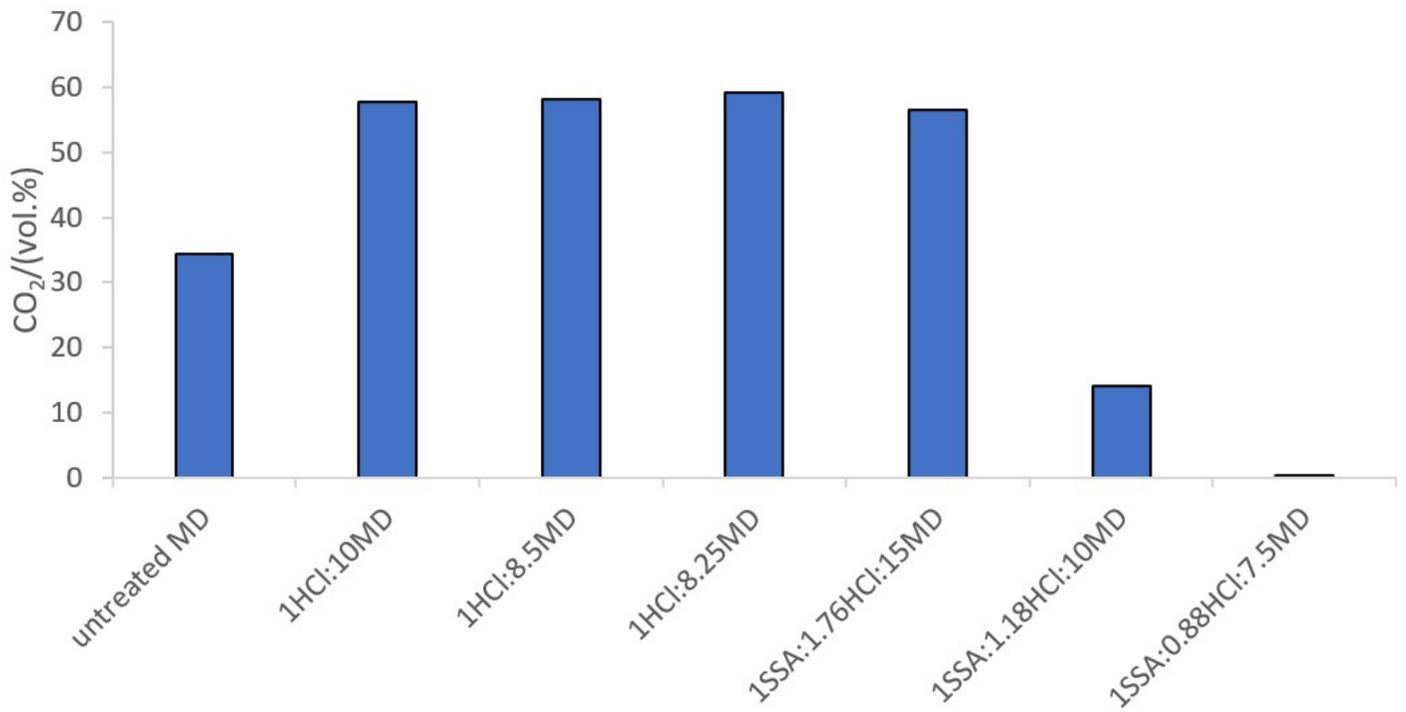


Figure 9. Carbon dioxide content in the biogas for the 7 cases evaluated.

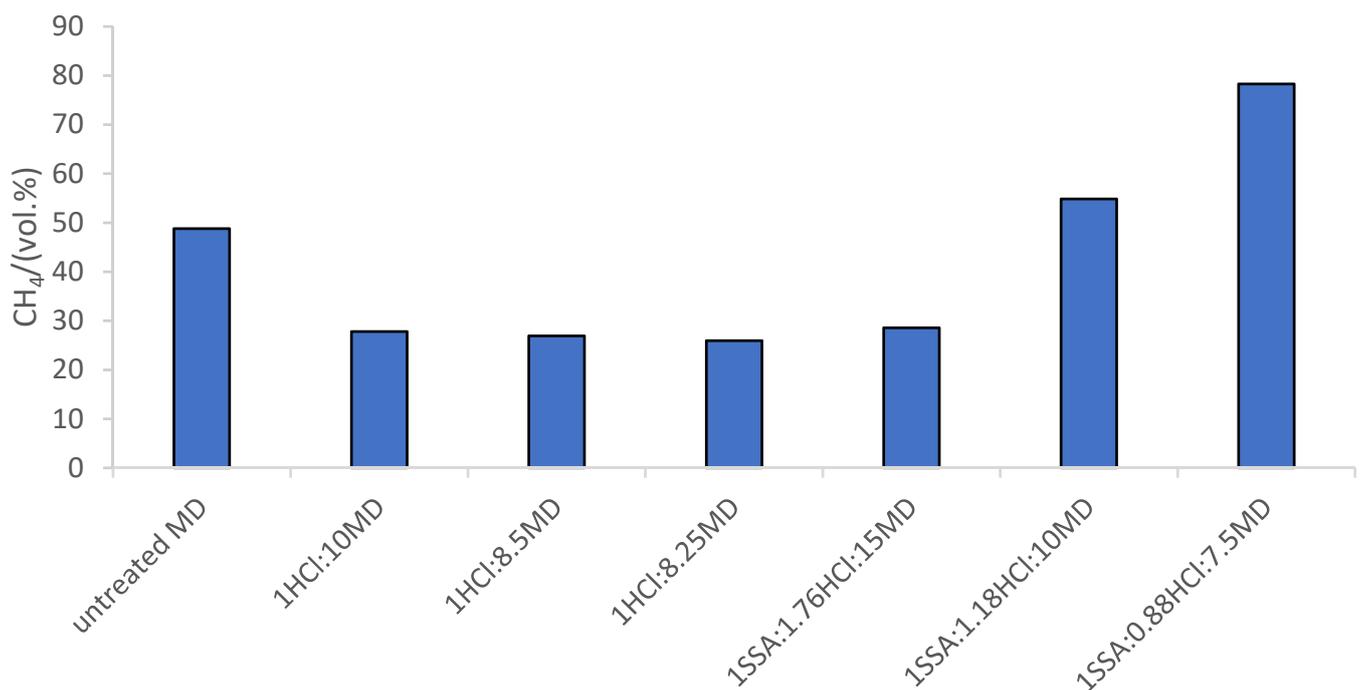


Figure 10. Methane content in the biogas for the 7 cases evaluated.

4. Discussion

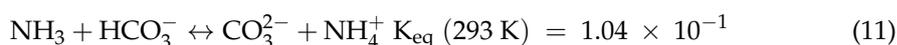
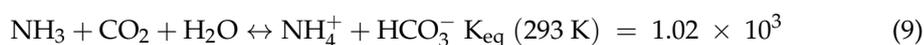
A third of all gaseous emissions (including CH₄, CO₂, and NH₃) associated with the management of organic residues via AD technology are derived from the last stage of storage [39,40]. Although the rate of biogas production reaches its peak during the controlled mesophilic or thermophilic fermentation that occurs in the anaerobic digester, the time of the psychrophilic storage can be 10 times longer [35,41,42]. For this reason, there are storage systems with facilities for the recovery of the biogas [43]. However, open lagoons are also used to hold the anaerobic digestate before land application, where these gases are simply emitted into the atmosphere [40,44]. The values reported in the literature (Table 3) are below the upper limit of 450 mL biogas/g VS established in the British regulation PAS 110 [7]; hence, these digestates would be suitable to be used as organic amendments. Table 3 offers a summary of the residual biogas and methane potentials of different types of digestate (i.e., produced from different substrates and employing different types of solid–liquid separation equipment). Except for the results reported by Gioelli et al. [40], a direct relationship could be established between the solid content of the fractions of the anaerobic digestate and the biogas production. This could be explained by the greater concentration of fermentable organic matter (solid fraction > whole digestate > liquid fraction) and the greater surface area of a material that is not submerged in liquid [14]. The results of Sambusiti et al. [45] agree with the higher concentration of biodegradable material in the solids, with a theoretical methane yield of 415 mL CH₄/g cellulose, 424 mL CH₄/g xylan, and 420 mL CH₄/g proteins. They further proposed that the liquor might have a greater concentration of less degradable humic substances in addition to ammonia that inhibits the fermentation in concentrations higher than 2.5 g/L.

Table 3. Summary of the residual biogas and methane potentials of anaerobic digestate produced from different substrates and with a variety of solid–liquid separation equipment (e.g., screw press, compression roller, etc.).

Fraction	mL Biogas/g VS	mL CH ₄ /g VS	References
Whole	61	34	[40]
Liquid	67	39	
Whole	135 ¹	70	[45]
Solid	173	90	
Whole	21–82	3–38	[44]
Solid (Fresh)	152–312	71–157	
Solid (Stored 15–30 d)	153–210	76–109	[46]

¹ Calculated assuming a 52 vol.% of methane in the biogas, based on the data of the anaerobic digestion plant described by the authors.

The role of CH₄, CO₂, and NH₃ in the upstream (i.e., conditioning and pretreatment of the feedstock), mainstream (i.e., operating conditions of the main AD bioreactors), and downstream (i.e., storage, nutrient recovery, and solid–liquid separation) should be recognized for the overall monitoring of the valorization technology [12,13,47]. Particularly, the CO₂ injection is employed as manure pretreatment to increase the production of CH₄ by promoting the bioconversion of the inorganic source of carbon directly through hydrogenotrophic methanogenesis, indirectly through homoacetogenic acetate formation followed by acetolactic methanogenesis or via electron transfer [47]. Therefore, the stabilization reactor was fed with the streams of biogas and anaerobic digestate as described in Figures 1 and 7. In order to enhance the chemistry of the multiple reactions between the NH_{3(aq)} and the CO_{2(g)} data obtained from the investigations related to the absorption of CO_{2(g)} in aqua-ammonia solutions were considered. According to Mani et al. [48], the reactions between the CO_{2(g)} and the NH_{3(aq)} are exothermic and occur at room temperature (293 K) and atmospheric pressure to produce NH₄HCO₃, ammonium carbonate ((NH₄)₂CO₃), and ammonium carbamate (NH₂COONH₄). The multiple reactions between the weak acid (Equation (7)) and the weak base (Equation (8)) correspond to a complex system, which is difficult to represent unless neglecting some equilibria, due to the short availability of thermodynamic data. Based on Equations (7)–(11), the composition of the system CO₂-NH₃-H₂O depends on the concentrations of CO_{2(g)} and the NH_{3(aq)}, which together with the dissociation of VFA, determine the pH of the system [49].



Source: [48].

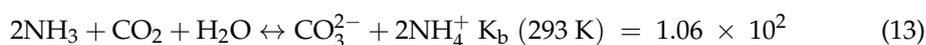
In terms of the rate of the reactions, the hydration of the CO_{2(g)} represents the bottleneck of the series (Equations (7)–(11)), as displayed in Table 4.

Table 4. Reaction orders and kinetic constants of the main reactions occurring in the CO₂-NH₃-H₂O system.

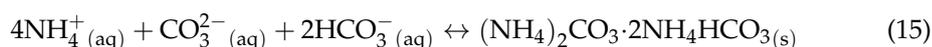
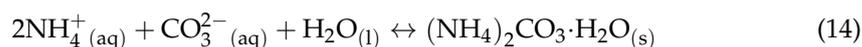
Reaction	Order	Kinetic Constants (@ 20 °C)	References
Equation (7)	1 2	$k_{\text{CO}_2} = 3.25 \times 10^{-2} \text{ s}^{-1}$ $k_{\text{HCO}_3^-} = 15 \text{ M}^{-1} \cdot \text{s}^{-1}$	[50–52]
Equation (8)	1	$k_{\text{NH}_3} = \text{Instantaneous}$	[53]
Equation (9)	2	$k_{\text{CO}_2} = k_{\text{NH}_3} = 3.37 \text{ M}^{-1} \cdot \text{s}^{-1}$ $> 3.25 \times 10^{-2} \text{ s}^{-1}$	[53,54]
Equation (10)	2	$k_{\text{HCO}_3^-} = k_{\text{NH}_3} = 3.37$ $\text{M}^{-1} \cdot \text{s}^{-1}$	[53,54]
Equation (11)	2		[54]

According to Mani et al. [48], if the concentration of CO₂ (aq) is equal to or greater than that of NH₃ (aq), the formation of ammonium bicarbonate prevails (Equation (9)). However, under an excess concentration of NH₃, the formation of carbamate (Equation (10)), and to a lesser extent, the formation of ammonium carbonate (Equation (11)), takes place. According to Budzianowski [53], the solid formation (in a scrubber) can be neglected if the concentration of NH₃ does not exceed 5–10 wt.%, which corresponds to 50–100 mg NH₃/L H₂O. The concentration of ammonia used in the study of Mani et al. [48] to avoid the formation of solid precipitates (2.5 mol NH₃ (aq)/L, 4.3 wt.%, or 42.5 mg NH₃ (aq)/L) is in agreement with the threshold value given by Budzianowski [53].

If the NH₃ (aq) is not completely consumed by the neutralization reaction with the CO₂ (aq), it is more correct to express the equilibria between the NH₃ (aq) and the CO₂ (g) as Equations (12) and (13). With regard to Equations (11) and (13), it is important to highlight that the UNIQUAC model in Aspen Plus[®] predicts the subsequent formation of (NH₄)₂CO₃, according to Equations (14) and (15) [55]. Looking at the thermodynamic data available for both reactions at ambient pressure, the formation of ammonium carbamate is more abundant than the ammonium carbonate [48,56]. From the point of view of the kinetics, the formation of carbamate is quicker ($k_{\text{CO}_2} = k_{\text{NH}_3} = 3.37 \text{ M}^{-1} \cdot \text{s}^{-1}$; Table 4) because it avoids the hydration of the CO₂ (g) ($3.25 \times 10^{-2} \text{ s}^{-1}$; Table 4). Therefore, the formation of ammonium carbamate is more likely with dry ice (i.e., solid carbon dioxide) [57], and it is converted to ammonium carbonate once is freely in an aqueous solution [56]. The combination of ammonia and carbon dioxide under high pressure (110 atm) and temperature (200 °C) leads to the production of urea [56,58].



Source: [48]



Source: [55]

Considering the solubility of the ammonium salts (Table 5), heterogeneous equilibria could be considered for the system NH₃-CO₂-H₂O and homogeneous equilibria could be avoided by pumping CO₂ (g) into the system, according to Equations (16) and (17) [48], given the lower solubility of the ammonium bicarbonate (Table 5). In fact, the manufacture

of NH_4HCO_3 as fertilizer has been proposed following a similar procedure by means of distillation of the liquid fraction of the anaerobic digestate [20].

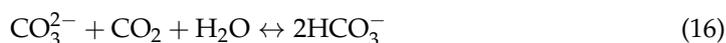


Table 5. Solubility of the ammonium salts in the heterogeneous system $\text{NH}_3\text{-CO}_2\text{-H}_2\text{O}$.

Ammonium Salt	Solubility in Water/(g/L)	References
NH_4HCO_3	220	[48]
	200	[53]
$(\text{NH}_4)_2\text{CO}_3$	320	[48]
	300	[53]
$\text{NH}_2\text{COONH}_4$	790	[48]
	600	[53]

Source: [48]

It is important to highlight that carbamate, ammonium carbamate, and ammonium bicarbonate appear in the original code of the PSM (Tables S4–S6) and only the ammonium carbonate is missed [49]. In the study of Mani et al. [48], the relative abundances of carbamate, bicarbonate, and carbonate were 43.3%, 22.5%, and 34.2%, respectively, at the end of the first hour of CO_2 (g) absorption in the NH_3 (aq) solution and a reasonable relative proportion of all these chemical species were found after 8 h of continuous operation (Table 6). However, there was a consistent decrease in carbamate and carbonate in favor of the formation of bicarbonate. An increase in the relative amount of bicarbonate would be expected if the absorption study continued for longer than 8 h. As described in Table 6, the profile of these chemical species in the liquid fraction of anaerobic digestate, which can be understood as an aqueous solution with all the species in equilibrium, can be found in the work of Drapanauskaite et al. [20].

Table 6. Share (relative amounts expressed as a percentage in molar scale) of carbamate, bicarbonate, and carbonate in aqueous solutions with the coexistence of NH_3 (g) and CO_2 (g) [20,48].

Nature of the Solution	Liquid Fraction of Anaerobic Digestate [20]	240 mL Solution of 2.5 mol NH_3 (aq)/L Bubbled for 8 h at a Rate of 15 L/h of 10 vol.% CO_2 and 90% N_2 [48] ¹
% NH_2COO^- ²	1.05	14.7
% HCO_3^-	97.24	75.7
% CO_3^{2-}	1.70	9.6

¹ The loss of ammonia was less than 1.3% (molar basis) during the 8 h absorption test. ² Relative amounts expressed as a percentage in molar scale.

When evaluating the synthesis of NH_3HCO_3 it is necessary to propose an experimental design that minimizes the uncertainty in the collection of the empirical data, for example, using the response surface methodology [59]. This experimental design can be coupled with contemporary machine learning methods, such as the Gaussian process regression, to construct a robust model [60].

5. Conclusions

First of all, the titration of the MD with the HCl showed that a dose of 3.18 mEq/g would be required to attain the pH_{zpc} upon addition of the SSA to the MD following a ratio of $0.6 \pm 0.2\%$. These doses of HCl and SSA that were applied to the MD to reach the pH_{zpc} in the simulation were significantly different from those found in the experiments

employing several acidification agents, ashes, and digestates of different natures. Only the use of a very high dose of lactic acid (68.31 ± 36.00 mEq/g digestate) prevented the blend of acidified digestate and wood ash to reach the pH_{zpc} .

Secondly, with regard to the concentration of nutrients in the WS fraction of the MD, only an outlier value was found in the profile of potassium that showed the relative fragility of the Aspen Plus[®] model and the need to revise it and make it more robust to be able to operate over a wider range of conditions.

Thirdly, the profiles of NH_3 , CO_2 , and CH_4 found in the biogas agree with the processes described for the simultaneous upgrading and production of NH_4HCO_3 . In this way, the acidification to attain the isoelectric point of the anaerobic digestate ($\text{pH} < 4$) promoted the release of CO_2 and minimized the volatilization of NH_3 . Once the SSA was added to stabilize the MD at the pH_{zpc} (11.61 ± 2.09), the opposite trend occurred; thus, the volatilization of NH_3 increased and the sequestration of CO_2 in the blend took place. As the concentration of CO_2 in the blend is much greater than that of NH_3 , the increase in the volatilization of the later compound and the mitigation of the former one led to an upgrading of the biogas to ~ 80 vol.% CH_4 .

For future work, further development of the model of the biomass ash-based treatment of the anaerobic digestate is proposed by optimizing the downstream manufacturing of NH_4HCO_3 and upgrading the biogas. It is required to confirm experimentally the exhaustive review of the underlying chemistry of the liquid–gas system with NH_3 , CO_2 , H_2O , and CH_4 . This will be followed by the implementation of refined kinetics and equilibria, both physical and chemical, in the Aspen Plus[®] PSM.

Supplementary Materials: The following supporting information can be downloaded at: <https://www.mdpi.com/article/10.3390/en16073039/s1>. Spreadsheets for the 7 scenarios investigated. A Word file summarizing the most relevant data: Table S1. Mass balance of the nutrients monitored in the Aspen Plus[®] simulations. (1/3); Table S2. Mass balance of the nutrients monitored in the Aspen Plus[®] simulations. (2/3); Table S3. Mass balance of the nutrients monitored in the Aspen Plus[®] simulations. (3/3); Table S4. List of the components in the PSM of Rajendran et al. [11]. (1/3); Table S5. List of the components in the PSM of Rajendran et al. [11]. (2/3); Table S6. List of the components in the PSM of Rajendran et al. [11]. (3/3).

Author Contributions: Conceptualization, A.M.A. and F.A.; methodology, A.M.A., A.A. and F.A.; software, A.M.A., A.A. and F.A.; validation, A.M.A. and F.A.; formal analysis, A.M.A., A.A. and F.A.; investigation, A.M.A., A.A., K.T.S. and F.A.; resources, K.T.S. and F.A.; data curation, A.M.A.; writing—original draft preparation, A.M.A. and A.A.; writing—review and editing, A.M.A. and F.A.; visualization, A.M.A.; supervision, K.T.S. and F.A.; project administration, K.T.S. and F.A.; funding acquisition, A.M.A., K.T.S. and F.A. All authors have read and agreed to the published version of the manuscript.

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Data Availability Statement: Research data are publicly available as spreadsheet files in the Supplementary Materials of this article. Restrictions apply to the availability of data regarding the production facilities where the bioenergy residues (i.e., anaerobic digestate and wood ash) were sampled. Data of the stakeholders of this project are available upon request to the authors with the permission of third parties.

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Abbreviations

AD, anaerobic digestion; BMP, biochemical methane potential; COD, chemical oxygen demand; FWD, food waste digestate; K_{eq} , equilibrium constant; MD, manure digestate; mol.%, molar percentage; NH_4^+-N , ammoniacal nitrogen; pH_{zpc} , pH of zero-point charge; PSM, process simulation model; PVWD, post-harvest vegetable waste digestate; RBP, residual biogas potential; SSA, sewage sludge ash; VFA, volatile fatty acids; vol.%, volume percentage; VS, volatiles solids; WI, water-insoluble; WS, water-soluble; WBA, wood bottom ash; WFA, wood fly ash; α , conversion coefficient of COD to volume of biogas; wt.%, weight percentage.

Appendix A

Table A1. Parameters from the Aspen Plus[®] Components Databanks for determination of unitless equilibrium constants of selected chemical species in the aqueous fraction.

Compound	Formula	Reaction	Parameters for Equation (6)
Ammonia	NH_3	Hydrolysis	$A = -1.25656; B = -3335.7; C = 1.4971; D = -0.037057$
Bicarbonate	HCO_3^-	Dissociation	$A = 216.05; B = -1243.17; C = -35.4819$
Carbon dioxide	CO_2	Hydrolysis	$A = 231.465; B = 12,092.1; C = -36.7816$
Hydrogen sulfide	H_2S	Dissociation (1st proton)	$A = -41.05; B = 6640.05; C = 15.106$
Carbonic acid	CO_2	Dissociation (1st proton)	$A = -8.3$
Water	H_2O	Hydrolysis	$A = 132.899; B = -13,445.9; C = -22.4773$

Table A2. Parameters from literature for determination of unitless equilibrium constants of selected amino acids in the aqueous fraction.

Compound	Formula	Reaction	Equation (6)	References
Arginine	$C_6H_{11}N_4O_2$	Dissociation	$A = -30.36$ (Guanidinium), -20.91 (Amine), -5.01 (Carboxyl)	[61]
Aspartic acid	$C_4H_7NO_4$	Dissociation	$A = -22.70$ (Amine), -8.98 (Carboxyl), -4.42 (Carboxyl)	[62]
Glutamic acid	$C_5H_9NO_4$	Dissociation	$A = -22.40$ (Amine), -9.37 (Carboxyl), -4.84 (Carboxyl)	[63]
Isoleucine	$C_6H_{13}NO_2$	Dissociation	$A = -22.29$ (Amine)	[63]
Lysine	$C_6H_{14}N_2O$	Dissociation	$A = -24.22, -5.01$	[61]
Methionine	$C_5H_{11}NO_2S$	Dissociation	$A = -21.18, -5.24$	[64]
Phenylalanine	$C_9H_{11}NO_2$	Dissociation	$A = -21.00, -4.21$	[61]
Proline	$C_5H_9NO_2$	Dissociation	$A = -22.41$	[61]
Serine	$C_3H_7NO_3$	Dissociation	$A = -5.68$	[63]
Threonine	$C_4H_9NO_3$	Dissociation	$A = -23.99, -6.05$	[61]
Tryptophan	$C_{11}H_{11}N_2O_2$	Dissociation	$A = -21.60, -5.47$	[61]
Tyrosine	$C_9H_{11}NO_3$	Dissociation	$A = -23.16, -20.95, -5.06$	[23,65]
Valine	$C_5H_{11}NO_2$	Dissociation	$A = -5.29$	[63]

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