Article

Large Eddy Simulation of Flow Characteristics around Cylinders with Crosswise and Streamwise Arrangements in Ocean Energy

Weiming Zhai [1], Ming Liu [2]🆔, Changjiu Huang [3], Daoxi Cheng [1] and Lei Tan [2,*]🆔

[1] Reactor Thermal-Hydraulic Laboratory, Reactor Engineering Technology Research Institute, China Institute of Atomic Energy, Beijing 102413, China; zhaiming19842002@163.com (W.Z.); 15101124213@163.com (D.C.)

[2] State Key Laboratory of Hydroscience and Engineering, Department of Energy and Power Engineering, Tsinghua University, Beijing 100084, China; lium16@tsinghua.org.cn

[3] State Grid Sichuan Electric Power Company, Chengdu 610041, China; huangcjcmht@sina.com

* Correspondence: tanlei@mail.tsinghua.edu.cn; Tel.: +86-10-6278-0605

Abstract: The flow around cylinders is one of the most fundamental phenomena in extracting wave energy from ocean waves. Compared with flows around a single cylinder, the investigation of flows around multiple cylinders is still limited and requires further studies to reveal flow characteristics. To this end, large eddy simulations are conducted to investigate the flow around double cylinders with crosswise and streamwise arrangements. Systematic studies on the influence of the number of mesh cells, the first near-wall mesh size, and the transient time step are carried out to achieve accurate and efficient simulations. The drag coefficient, flow separation, and flow pattern for different arrangements under various cylinder spacings are analyzed according to simulation results. For the crosswise arrangement, the flow pattern switches from the single-body regime to the synchronized vortex-shedding regime as the spacing increases. For the streamwise arrangement, the flow pattern develops from the reattachment regime to the vortex-shedding regime as the spacing increases.

Keywords: large eddy simulation; flow around cylinder; crosswise arrangements; streamwise arrangements; ocean energy

1. Introduction

The exploitation of ocean energy has raised a great deal of concern in recent years due to the burdens of fossil energy exhaustion and environmental pollution [1,2]. The extraction of ocean wave energy is widely recognized as a promising technology because it is adaptive to short-term energy storage. For wave energy conversion technologies, the periodic waves can result in the resonant motions of the body, especially with the existence of vortex-induced vibrations [3,4]. Then, the hydrokinetic energy of ocean waves can be converted into electricity through the vibrating bodies [5]. From this point of view, it is of great significance to investigate the vortex and vibration of flows around blunt bodies [6–8]. Among these studies, flow around cylinders [9,10] is one of the most common phenomena because of the extensive underlying mechanisms. It has attracted much attention [11], which provides effective guidance for the shape design to enhance lift and reduce drag [12].

The investigation starts from the flow around a single cylinder respective of different Reynolds numbers. In recent decades, owing to the rapid development of computation power, the technology of computational fluid dynamics (CFDs) has increasingly become a reliable tool for simulating flows around cylinders. Increasing computational power has also made it possible to conduct large eddy simulations (LESs) for turbulent flows [13,14]. Even for such simple geometries as a square cylinder or circular cylinder, complex flow phenomena will appear [15]. In order to improve the simulation accuracy of flows around cylinders, the influence of discretization scheme has been investigated by Breuer [16],

and the central difference scheme shows better agreement with experimental results. The sub-grid scale (SGS) stress model is a significant aspect when conducting LESs. Studies by Lysenko et al. [17] indicate that the influence of the SGS model is almost negligible when near-wall regions are refined properly. Breuer [16], Kravchenko and Moin [18], and Ma et al. [19] investigated the influence of spanwise length on simulation results and found that they are almost independent of spanwise length when it is larger than π times the cylinder diameter. The existing studies have already established a framework to accurately simulate flows around a single cylinder by means of LESs [20–22].

Based on various studies on the flow around a single cylinder, researchers also have begun to pay attention to flows around multiple cylinders [23–26], which is closer to realistic conditions. When multiple cylinders are applied, the flow characteristics are influenced by different spacing and different arrangements, i.e., crosswise arrangement, streamwise arrangement, and staggered arrangement. Many experimental and numerical studies were conducted with various spacing [27–29]. Results show that there exists a critical value of non-dimensional spacing where the vortex-shedding regime will switch. For the crosswise arrangement, the vortex-shedding regime can be classified into three typical regimes: the single-body regime, biased-flow regime, and synchronized vortex-shedding regime [30–32]. The appearance of different regimes mainly depends on cylinder spacing. It is found that the vortex streets may influence each other to form a gap flow deflection under intermediate cylinder spacing, while becoming two symmetrical wake streets as cylinder spacing continues to increase [33]. Also, the interaction can become more significant when crosswise cylinders with different diameters are installed [34]. By comparison, the vortex-shedding regime for the streamwise arrangement is influenced by not only the cylinder spacing but also the Reynolds number. It can be classified into four regimes: the no-vortex-shedding regime, single-body regime, reattachment regime, and vortex-shedding regime [29]. Numerical simulations of flows around streamwise cylinders under moderate [35] and high [36] Reynolds numbers have been performed by means of LES. The drag and lift performance of the upstream and downstream cylinders are quite different under different Reynolds numbers [37].

Above all, it has been shown in the existing studies that the flow phenomena are even more complex in flows around multiple cylinders compared with a single cylinder. The flow characteristics of multiple cylinders are quite sensitive to both cylinder arrangements as well as the Reynolds number. However, according to the best of the authors' knowledge, the numerical simulations on crosswise and streamwise arranged cylinders is relatively rare compared with such studies on a single cylinder. To this end, it is of great importance to investigate in detail the flow phenomena, i.e., drag performance, velocity profiles, and vorticity structures, in flows around multiple cylinders.

Therefore, large eddy simulations are conducted for flows around multiple cylinders with crosswise and streamwise arrangements in the present study. The influence of arrangement settings and cylinder spacing on flow characteristics is analyzed. The structure of the present paper is organized as follows. In Section 1, previous studies on flows around cylinders are reviewed. In Section 2, the present physical model and numerical methods are described, with detailed validation of the numerical settings. Then, the validated numerical methods are applied to double cylinders with crosswise and streamwise arrangements, and the simulation results are analyzed and discussed in Section 3. Finally, in Section 4, the main conclusion of the present study is summarized.

2. Numerical Methods

2.1. Physical Model and Computational Domain

As shown in Figure 1, the turbulent flow around the cylinder with a fixed inlet and zero gradient outlet is considered in the present study. Here, the fluid is regarded as incompressible with constant properties, i.e., density and viscosity.
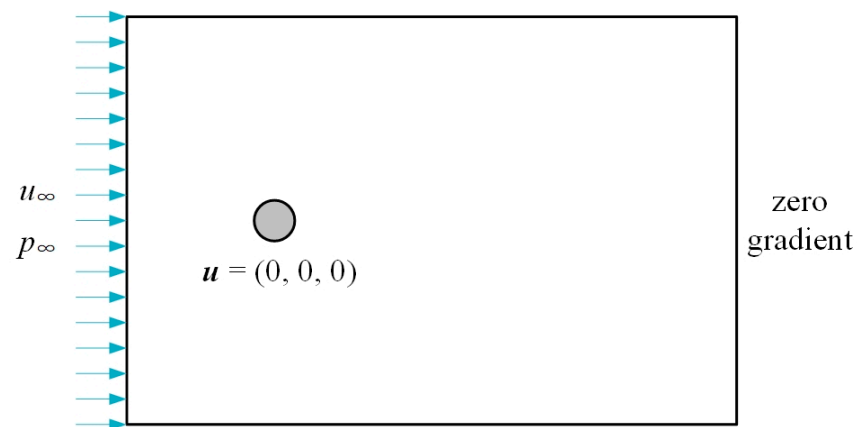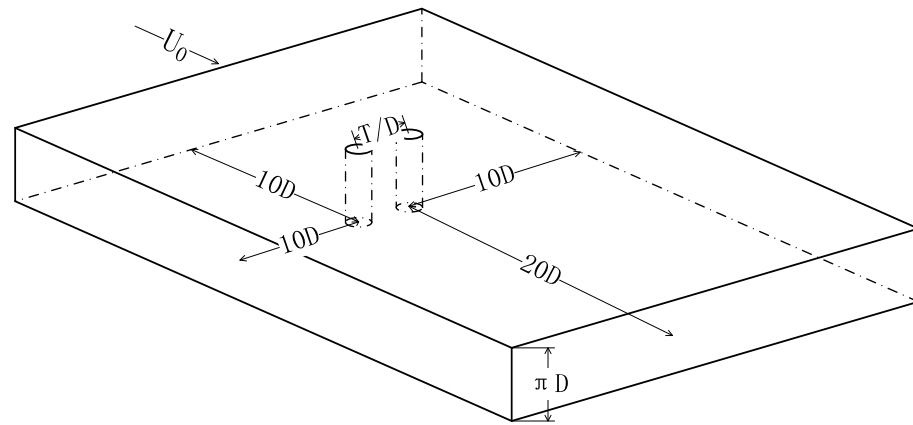
Figure 1. Schematic of flows around cylinder.

As shown in Figure 2, flows around (a) a single circular cylinder, (b) crosswise cylinders, and (c) streamwise cylinders are investigated in the present study. The definition of the coordinate system is illustrated in Figure 2a, which also applies to the crosswise and streamwise cylinders. The inlet is set $10D$ upstream of the cylinder, and the outlet is set $20D$ downstream of the cylinder, where D denotes the diameter of the cylinder. The upper and lower boundaries are set $10D$ away from the cylinder, and the spanwise length is set as πD to eliminate its effect, according to previous studies [16]. The Reynolds number, Re = $U_0 D / v$, is defined by the inflow velocity U_0 and the cylinder diameter D, and kinematic viscosity v is equal to 3900 in the present simulations [38]. For the crosswise arrangement, the distance between the cylinder centers perpendicular to the inflow direction T is regarded as the cylinder spacing, and it is normalized according to the cylinder diameter as T/D. For the streamwise arrangement, the distance between cylinder centers along the inflow direction L is regarded as the cylinder spacing, and it is also normalized according to the cylinder diameter as L/D.
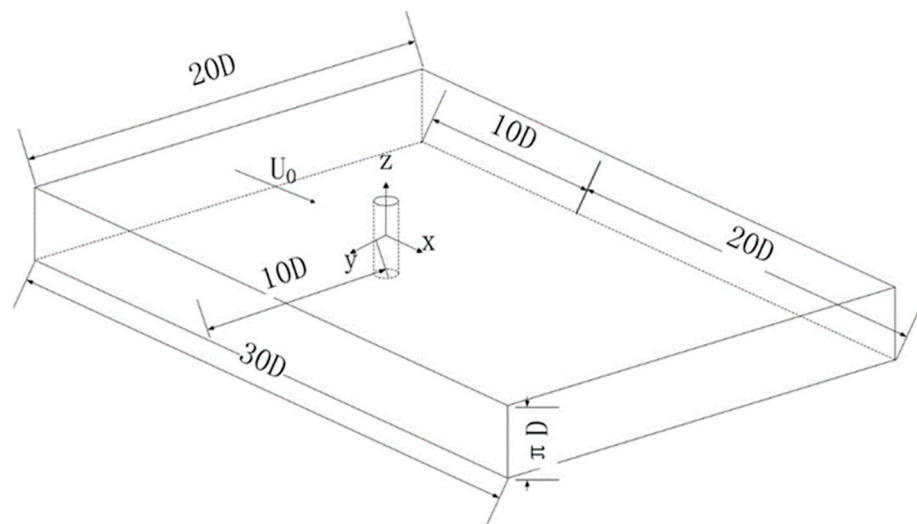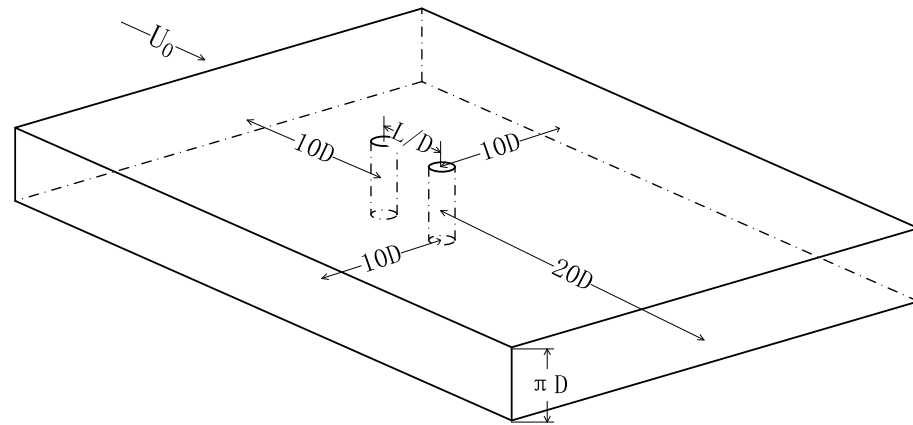

(**a**) Single cylinder

Figure 2. *Cont.*

(**b**) Crosswise cylinder

(**c**) Streamwise cylinder

Figure 2. Schematic of the computational domain for (**a**) Single cylinder, (**b**) Crosswise cylinder, and (**c**) Streamwise cylinder.

2.2. Numerical Methods

Large eddy simulations of flows around cylinders are conducted by means of commercial CFD software ANSYS Fluent [39,40], and the Smagorinsky–Lilly SGS model is applied. The governing equations for large eddy simulations with the Smagorinsky–Lilly SGS model are listed as follows:

$$\frac{\partial \overline{u}_j}{\partial x_j} = 0, \tag{1}$$

$$\frac{\partial \overline{u}_i}{\partial t} + \frac{\partial (\overline{u}_i \overline{u}_j)}{\partial x_j} = -\frac{1}{\rho}\frac{\partial \overline{p}}{\partial x_i} + \frac{\partial}{\partial x_j}\left(\nu \frac{\partial \overline{u}_j}{\partial x_j}\right) - \frac{1}{\rho}\frac{\partial \tau_{ij}}{\partial x_j}, \tag{2}$$

where u_i denotes velocity and the over-bar denotes filtered quantity; ρ, p, and ν stand for density, pressure, and kinetic viscosity, respectively; and τ_{ij} is SGS turbulent stresses, which is calculated by:

$$\tau_{ij} = -2\mu_t \overline{S}_{ij} + \frac{1}{3}\delta_{ij}\tau_{kk}, \tag{3}$$

$$\overline{S}_{ij} = \frac{1}{2}\left(\frac{\partial \overline{u}_i}{\partial x_j} + \frac{\partial \overline{u}_j}{\partial x_i}\right), \tag{4}$$

$$\mu_t = \rho L_s^2 \sqrt{2\overline{S}_{ij}\overline{S}_{ij}}, \tag{5}$$

$$L_s = \min(\kappa d, C_s \Delta), \tag{6}$$

where κ is the von Karman constant, d is the distance to the closest wall, C_s is the Smagorinsky constant, and Δ is the local grid size. The details for the numerical methods can be found in Ref. [41].

The pressure implicit with splitting of operators (PISOs) algorithm is used to couple velocity and pressure. Both skewness correction and neighbor correction are set as 1 in the present simulations. The bounded second order implicit time integration scheme is employed for temporal discretization. The fixed value of inflow velocity without turbulent fluctuations is given at the inlet, and the outflow boundary condition with zero gradient is set at the outlet. The no-slip boundary condition is set on the cylinder surface as well as the side boundaries in the y-direction. The periodic boundary conditions are employed for side boundaries in the z-direction. In the present simulations, turbulent perturbation is not introduced to the inflow velocity. The entrance length is set as 10 times the cylinder diameter, and it takes about 10 typical vortex-shedding cycles to become fully developed. The structured mesh is generated using commercial software ANSYS ICEM, and the mesh distributions around the single and double cylinders are displayed in Figure 3. The maximum value of $y+$ is kept as 1.5 for the grids so that wall function is not used in the present simulations.
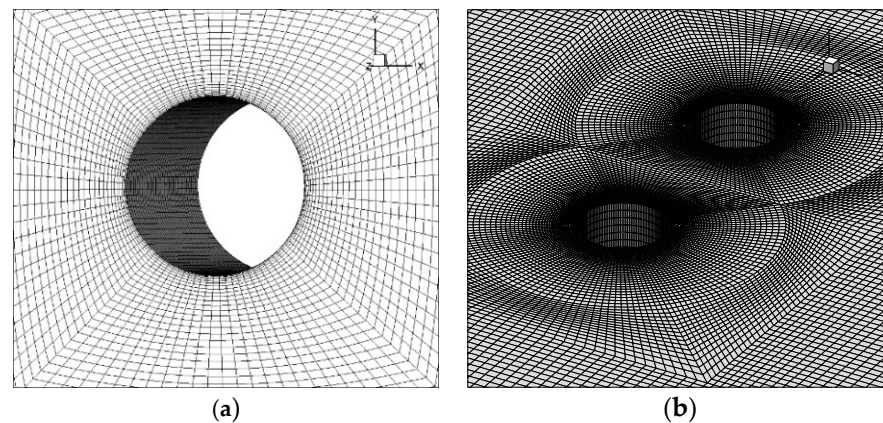

(a)   (b)

Figure 3. Computational mesh for (**a**) Single cylinder and (**b**) Double cylinders.

2.3. Grid Independence Tests

As indicated by previous numerical studies, the number of mesh cells, the cell size of the first near-wall layer, and the transient time steps will affect numerical results. Therefore, the influence of these factors is investigated in this section. For flows around a single cylinder, the drag coefficient and lift coefficient are defined to estimate its hydraulic performance as follows:

$$c_D = \frac{F_d}{0.5\rho U_\infty^2 A}, \tag{7}$$

$$c_L = \frac{F_l}{0.5\rho U_\infty^2 A}, \tag{8}$$

where F_d and F_l are the total drag and lift on the cylinder, respectively; ρ and U_∞ are the freestream density and velocity, respectively; and A is the projection area. Here, the experimental results of the time-averaged drag coefficient c_D and Strouhal number St $= fD/U_\infty$ by Ong and Wallace [11] are employed in the present study to validate the accuracy of the simulation results, where $c_D = 0.99 \pm 0.05$ and St $= 0.215 \pm 0.005$ under Re = 3900. The Strouhal number is a dimensionless number that is widely used to describe oscillating flow mechanisms. In the present study, the vortex shedding frequency f is determined according to the fast Fourier transformation of the time evolution of the

instantaneous lift coefficient within 40 typical vortex-shedding cycles. Figure 4 shows typical time evolution of drag coefficient and lift coefficient.
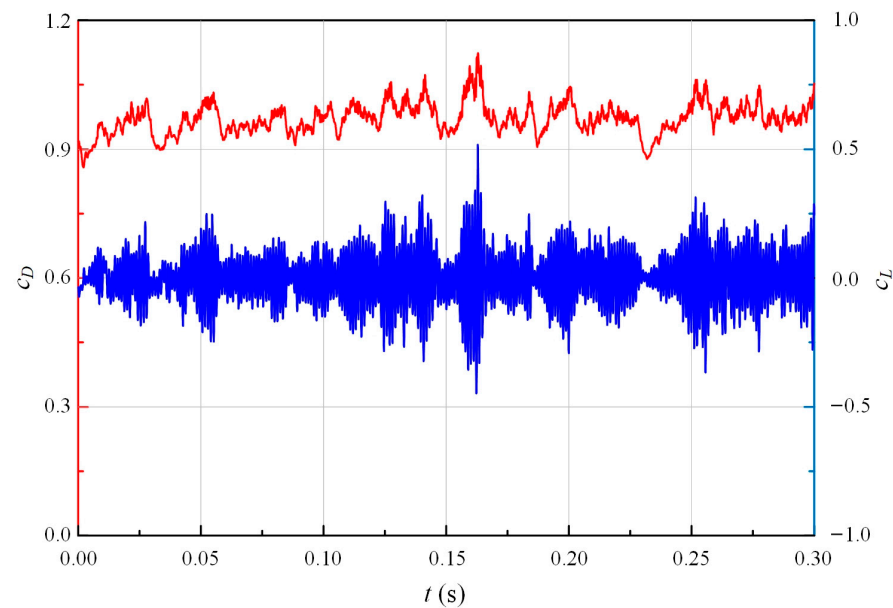

Figure 4. Time evolution of drag coefficient (red color) and lift coefficient (blue color).

In the present study, a total of three sets of mesh are employed to validate the independence of the number of mesh cells. Here, the number of nodes on the radial direction (r), circumferential direction (θ), and spanwise direction (z) is gradually increased, and hence the corresponding total number of mesh cells rises from 0.78 million to 2.80 million. Table 1 lists mesh parameters and corresponding simulation results. It can be found that the simulation results hardly change when the number of mesh cells exceeds 1.82 million. Therefore, Mesh 2, with the medium number of mesh cells, is employed in the following simulations.

Table 1. Independence test of number of mesh cells.

Mesh	Mesh Distribution ($r \times \theta \times z$)	Number of Mesh Cells	c_D	Relative Error of c_D	St	Relative Error of St
Mesh 1	$50 \times 120 \times 35$	0.78×10^6	0.977	1.31%	0.189	12.06%
Mesh 2	$70 \times 120 \times 48$	1.82×10^6	0.981	0.81%	0.201	6.77%
Mesh 3	$90 \times 200 \times 58$	2.80×10^6	0.978	1.17%	0.209	2.99%

Then, keeping the total number of mesh cells constant, the cell size of the first near-wall layer is gradually reduced from 0.01 to 0.0001, and the corresponding value of $y+$ decreases from 8 to 0.5. The influence of the cell size of the first near-wall layer is summarized in Table 2. The simulation results of time-averaged drag coefficient are almost independent of its value, and hence Mesh 2-3, with y+ = 1.5, is employed in the following simulations. Here, the results are averaged with the time interval equal to the transient step within 40 typical vortex-shedding cycles.

Table 2. Independence test of cell size of the first near-wall layer.

Mesh	Number of Mesh Cells	Cell Size of the First Layer	$y+$	c_D	Relative Error of c_D	St	Relative Error of St
Mesh 2-1	1.82×10^6	0.01	8	0.982	0.81%	0.200	6.77%
Mesh 2-2	1.82×10^6	0.005	5.6	0.965	2.56%	0.204	5.26%
Mesh 2-3	1.82×10^6	0.001	1.5	0.971	1.88%	0.215	0.14%
Mesh 2-4	1.82×10^6	0.0005	0.8	0.985	0.47%	0.225	4.68%
Mesh 2-5	1.82×10^6	0.0001	0.5	1.017	2.73%	0.231	7.44%

Then, the value of the transient time step Δt is also a significant parameter for unsteady simulations. A total of three values of transient time step Δt are considered in the present simulations, and the simulation results are listed in Table 3. Both the time-averaged drag coefficient and Strouhal number are nearly unchanged as the transient time step reduces. Therefore, the value of $\Delta t = 1 \times 10^{-4}$ s is selected in the following studies to seek a balance between simulation accuracy and computation consumption.

Table 3. Independence test of transient time step.

Δt (s)	c_D	Relative Error of c_D	St	Relative Error of St
1×10^{-4}	0.971	1.88%	0.2153	0.14%
5×10^{-5}	1.017	2.72%	0.2289	6.47%
1×10^{-5}	0.913	7.78%	0.2209	2.76%

So far, the mesh parameters and transient numerical settings for accurate and efficient simulations have been determined. According to the present numerical settings, the relative errors of time-averaged drag coefficient and Strouhal number compared with the existing experimental data are 1.88% and 0.14%, respectively, which validates the accuracy of the present numerical method. In the following analysis, these numerical settings will be applied to crosswise and streamwise cylinders.

3. Results and Discussion

3.1. Single Cylinder

Before the discussion of double cylinders, the simulation results of the single-cylinder case are analyzed. In this section, the Reynolds number is systematically increased from 1000 to 10,000 by increasing the inflow velocities, while the other numerical settings are kept the same. Table 4 summarizes the drag coefficient and Strouhal number at different Reynolds numbers. It can be found that, with the increase in the Reynolds number, the drag coefficient gradually reduces, while the Strouhal number increases and then decreases. Such variation trend shows good agreement with results reported in the existing literature [11].

Table 4. Hydrodynamic parameters of flow around a single cylinder.

Case	Re	c_D	St
1	1000	1.210	0.210
2	2000	0.976	0.211
3	3000	0.983	0.214
4	3900	0.971	0.215
5	5000	0.974	0.196
6	6000	0.943	0.186
7	7000	0.916	0.175
8	8000	0.892	0.165
9	10,000	0.855	0.153

The circumferential distribution of the mean pressure coefficient under different values of the Reynolds number are displayed in Figure 5 together with the schematic to illustrate the definition of the circumferential angle θ. The circumferential locations of the flow separation points are also listed in Table 5. As shown in Figure 5, the pressure coefficients at the windward side are almost the same under different Reynolds numbers. However, as the Reynold number increases, the flow separation point moves upstream, with a higher value of both the minimum pressure coefficient and the pressure recovery level at the leeward side. As a result, the drag coefficient also reduces with the increase in the Reynolds number.
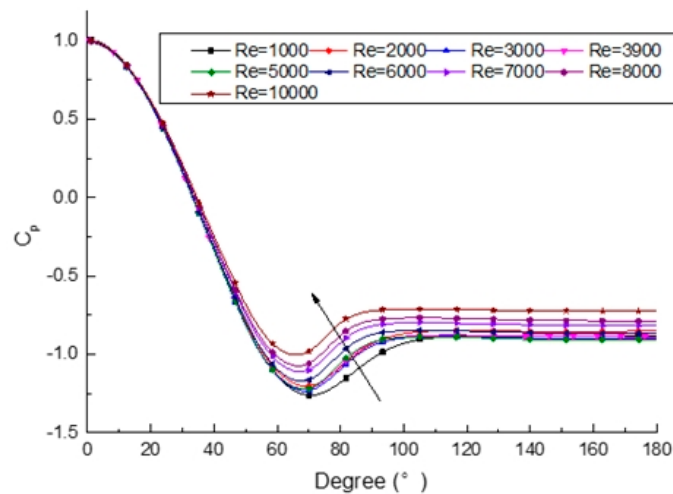
(**a**) Mean pressure coefficient
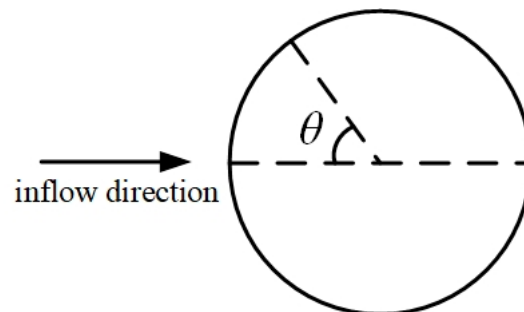
(**b**) Circumferential angle

Figure 5. (**a**) Mean pressure coefficient around single cylinder and (**b**) definition of circumferential angle θ.

Table 5. Flow separation parameter of a single cylinder.

Case	Re	θ_{sep}
1	1000	92.25
2	2000	88.18
3	3000	86.40
4	3900	85.66
5	5000	84.74
6	6000	83.50
7	7000	82.46
8	8000	81.65
9	10,000	80.64

Figure 6 displays the distribution of streamwise velocity along the *y*-direction at different downstream locations. Within the near wake regions (x/D = 1.06, 1.54, and 2.02), the distribution of streamwise velocity develops from a U-shape toward a V-shape. The minimum velocity at the centerline gradually reduces as the flow develops downstream. By comparison, in the downstream region further away from the cylinder (x/D = 6, 7, and 10), the streamwise velocity maintains a V-shaped distribution. However, the minimum velocity at the centerline gradually increases instead as the flow develops downstream. Comparing the velocity distribution at different Reynolds numbers, it can be found that the minimum velocity at the centerline increases and then decreases with the increase in the Reynolds number.
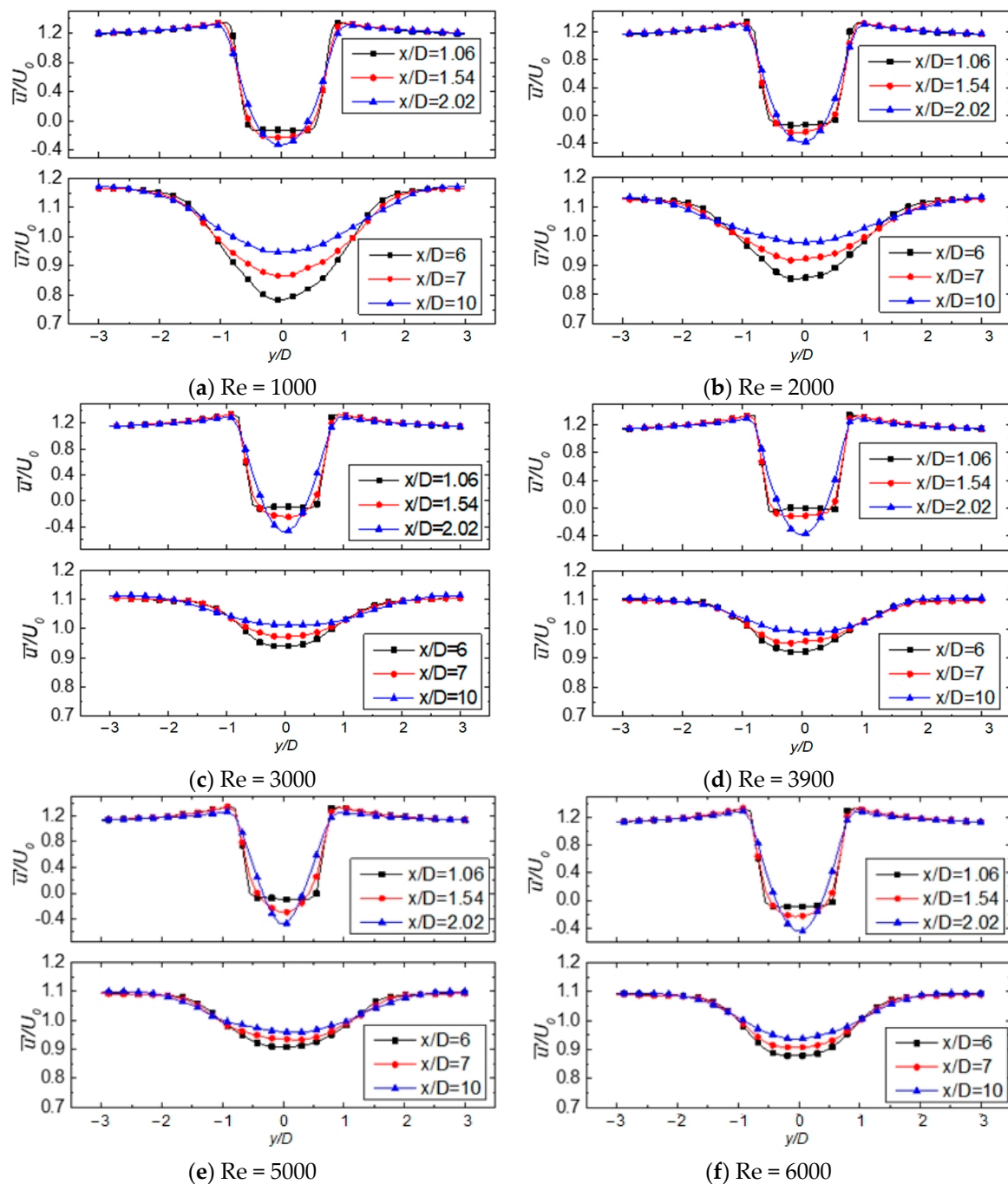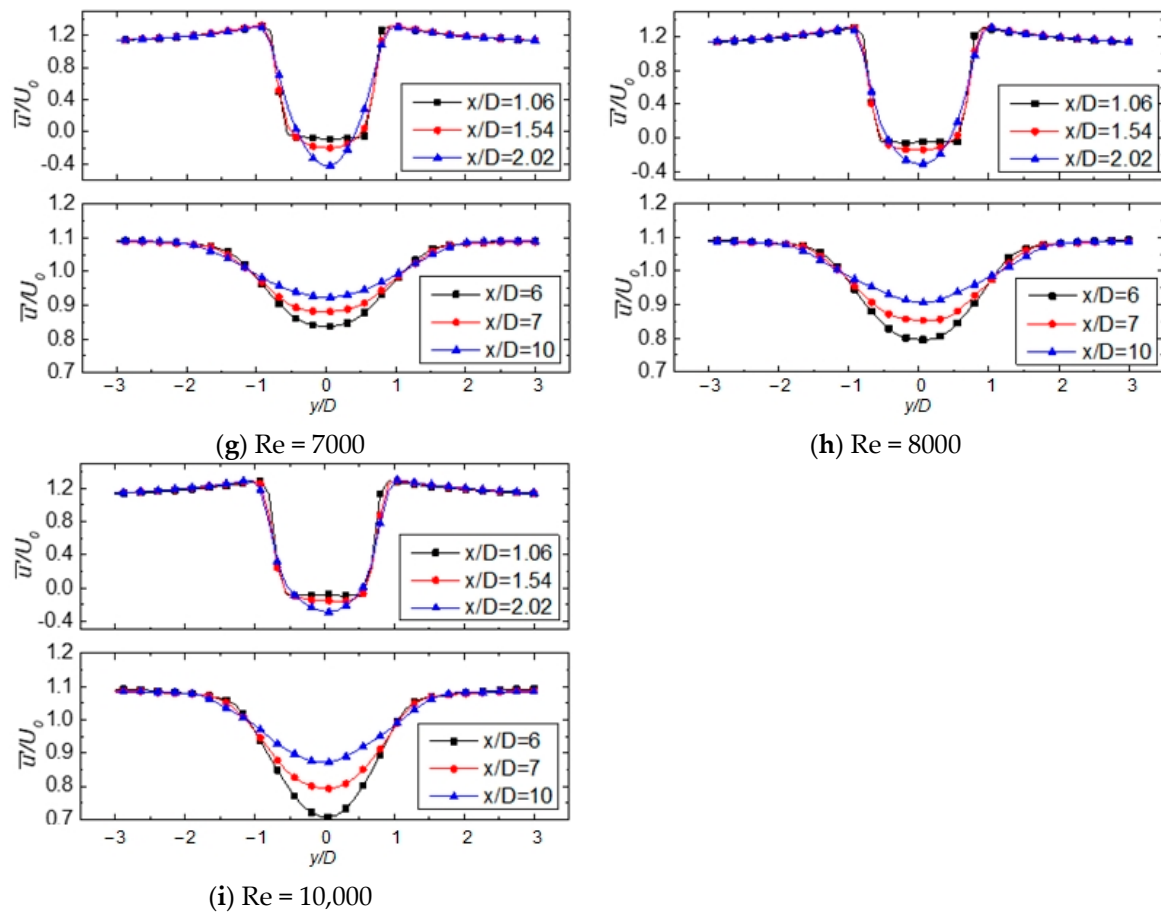

Figure 6. *Cont.*

(**g**) Re = 7000　　　　　　　　　　　　　　　　　　(**h**) Re = 8000

(**i**) Re = 10,000

Figure 6. Mean streamwise velocity at downstream locations for a single cylinder for (**a**) Re = 1000, (**b**) Re = 2000, (**c**) Re = 3000, (**d**) Re = 3900, (**e**) Re = 5000, (**f**) Re = 6000, (**g**) Re = 7000, (**h**) Re = 8000, and (**i**) Re = 10,000.

3.2. Crosswise Cylinders

For two cylinders with a crosswise arrangement, the following equivalent drag coefficient is defined as follows:

$$\frac{c_{D,s}}{c_{D,0}} = \frac{(c_{D,s1} + c_{D,s2})}{2c_{D,0}}, \tag{9}$$

where $c_{D,s}$, $c_{D,0}$, $c_{D,s1}$, and $c_{D,s2}$ denote the drag coefficient for the crosswise two cylinders, the single cylinder, the first cylinder in the crosswise arrangement, and the second cylinder in the crosswise arrangement, respectively. The equivalent drag coefficient for two cylinders is defined so that the drag performance of a two-cylinder system can be compared with the single cylinder directly. A total of three cases with different cylinder spacing are considered in the present study, i.e., $T/D = 1.2$, 1.6, and 2.5. Table 6 lists the hydrodynamic performances of the crosswise cylinders with different cylinder spacing. As shown in Table 6, the drag coefficient of crosswise cylinders is always higher than that of the single cylinder. Among the crosswise cylinders with different cylinder spacings, as the cylinder spacing increases, the drag coefficient decreases and then increases, while the Strouhal number gradually increases.

Table 6. Hydrodynamic performance of crosswise cylinders.

Case	T/D	$c_{D,s}$	St
Case Single	0, single cylinder	1.00	0.215
Case T1.2	1.2	1.41	0.098
Case T1.6	1.6	1.10	0.215
Case T2.5	2.5	1.37	0.264

Figure 7 displays the circumferential distribution of pressure coefficient $c_p = (p - p_\infty)/(0.5\rho U_\infty{}^2)$ in each cylinder for the crosswise arrangement. For the single-cylinder case, due to the absence of the influence of other cylinders, the near-wall shear wall in both sides can develop fully and freely and finally separates on the leeward side. As a result, an almost symmetrical distribution appears along the streamwise direction. By comparison, an asymmetrical distribution of pressure coefficients can be observed in each cylinder in the crosswise arrangement due to the wake interactions with each other. The location with maximum pressure coefficient, which corresponds to the stagnation point, is located on the cylinder directly in front of the incoming flow for the single-cylinder case. However, the stagnation point is then biased toward the side with the spacing for both cylinders in the crosswise arrangement.

(**a**) Cylinder 1   (**b**) Cylinder 2
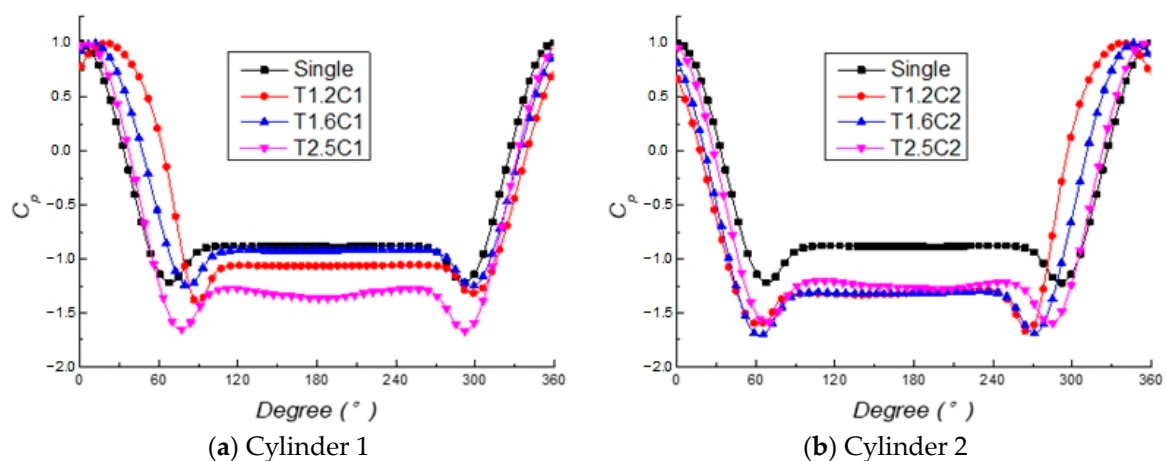
Figure 7. Mean pressure coefficient around cylinders with crosswise arrangement for (**a**) Cylinder 1 and (**b**) Cylinder 2.

In order to quantitatively compare the flow separation of different cases, the stagnation point θ_{sta}, the separation point on the spacing side θ_{ses}, and the separation point on the other side θ_{seo} on each cylinder are calculated and summarized in Table 7. As the cylinder spacing increases, the deviation of the stagnation point gradually decreases, which indicates less interaction between the cylinders. As for the flow separation point, with the increase in cylinder spacing, for cylinder 1, the one at the spacing side moves downstream while the one at the outer side moves upstream. By comparison, for the other cylinder, the flow separation point at the spacing side moves upstream while the one at the outer side moves downstream. The difference between flow separation points on the spacing and outer sides $|\theta_{ses} - \theta_{seo}|$ represents the wake width. It can be seen that the wake width of cylinder 1 is always higher than that of cylinder 2. This phenomenon indicates that in the crosswise arrangement of two cylinders, one plays a more significant role than the other.

Table 7. Flow separation parameter of side-by-side cylinders.

Case	T/D	Cylinder 1				Cylinder 2			
		θ_{sta}	θ_{ses}	θ_{seo}	$|\theta_{ses} - \theta_{seo}|$	θ_{sta}	θ_{ses}	θ_{seo}	$|\theta_{ses} - \theta_{seo}|$
Single	0	0	272	88					
T1.2	1.2	19.31	284.98	100.84	184.14	338.21	74.89	250.47	175.58
T1.6	1.6	9.81	278.3	98.02	180.28	347.24	81.56	255.27	173.71
T2.5	2.5	4.64	273.79	95.77	178.02	355.14	86.46	264.11	177.65

Figure 8 illustrates the distribution of the mean streamwise velocity at two downstream locations (x/D = 1.06, 6.00) for the single cylinder and crosswise cylinders. At the downstream location very close to the wake region, the velocity downstream of the crosswise cylinders shows a W-shaped distribution, while the single cylinder has a V-shaped distribution. When it comes to the wake region slightly away from the cylinder, the velocity for crosswise cylinders with small spacing (T/D = 1.2) tends to show a V-shaped distribution, which is similar to that for the single cylinder. However, the W-shaped distribution of velocity still appears in the larger spacing (T/D = 1.6 and 2.5). It is indicated that the flow patterns for the crosswise cylinders with small spacing of T/D = 1.2 belong to the single-body regime [30].
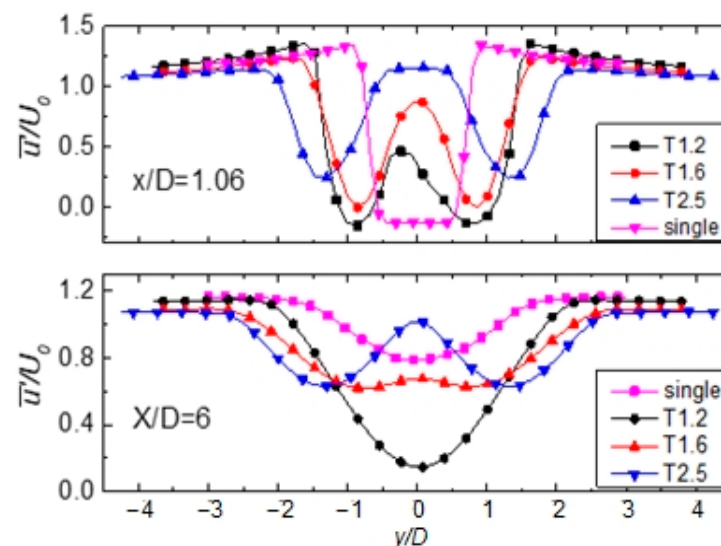

Figure 8. Mean streamwise velocity at downstream locations for crosswise cylinders.

Figure 9 shows the contour distribution of vorticity around crosswise cylinders at different cylinder spacings at (left) $t = t_0$ and (right) $t = t_0 + 5/6T$, where T stands for the vortex shedding period. The vortex induced from the upper cylinder is denoted with capital letters (A and B), while the vortex induced from the lower cylinder is denoted with lowercase letters (a and b). At the smallest cylinder spacing of T/D = 1.2, because of the interaction of shear layers in the quite small spacing, the vortex at the spacing side induced from each cylinder is influenced by the other and quickly suppressed. Therefore, only the vortex at the outer side of each cylinder can shed from the cylinder and then form the so-called "single-body regime", which is quite similar to the pattern of flow around a single cylinder. At the moderate cylinder spacing of T/D = 1.6, because of the weaker interaction of the shear layers, the vortex induced at the spacing side can also shed from the cylinder. Therefore, in the middle of the vortex band formed by the shedding of the outer sides of the two cylinders, a new vortex band is created, where the shedding vortex is generated alternately by the spacing side of the two cylinders. As the cylinder spacing further increases to T/D = 2.5, at this point the interaction of shear layers in the
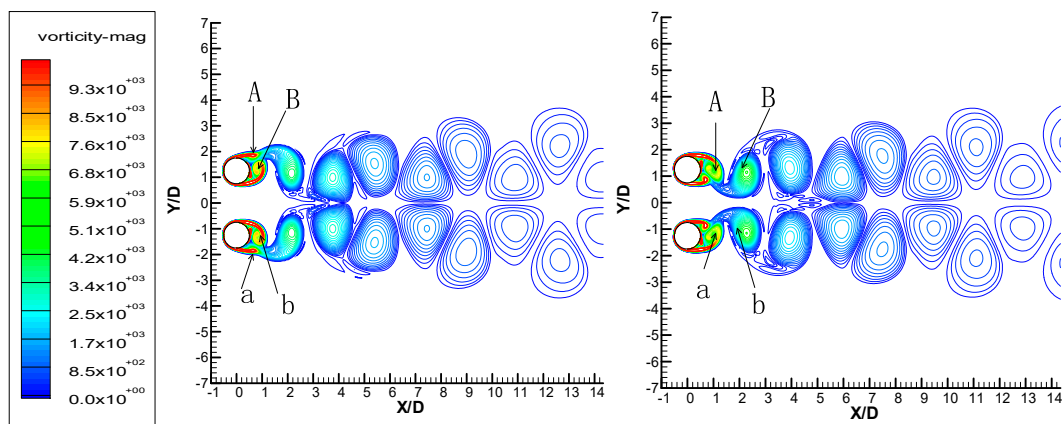
spacing is already very weak, so that the vortex shedding structures of the two cylinders are almost completely independent of each other. According to the above discussion, it can be concluded that the interaction of two crosswise cylinders will suppress vortex formation at the spacing side when the cylinder spacing is small.
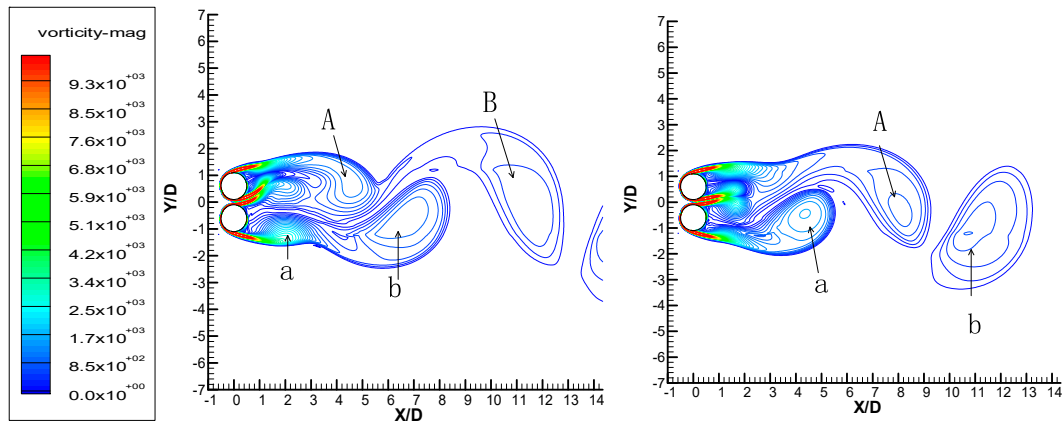
(**a**) $T/D = 1.2$
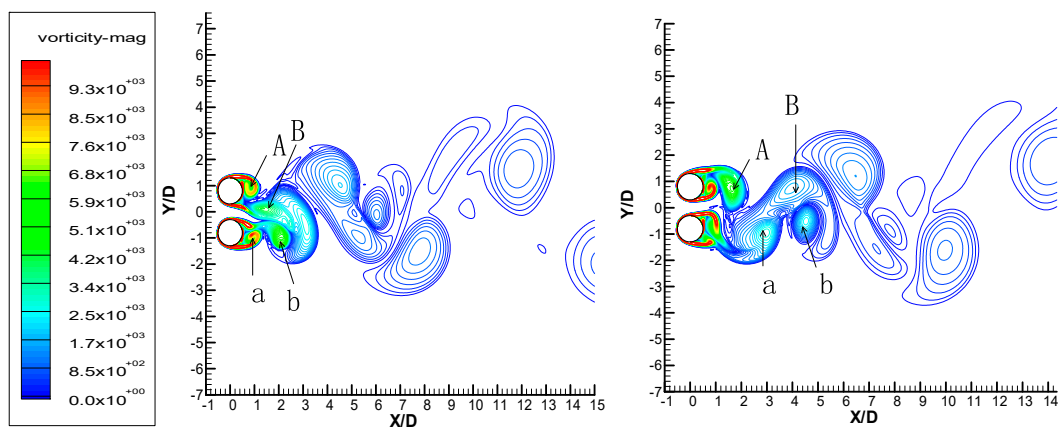
(**b**) $T/D = 1.6$

(**c**) $T/D = 2.5$

Figure 9. Vorticity distribution around crosswise cylinders at (**left**) $t = t_0$ and (**right**) $t = t_0 + 5/6T$ for (**a**) $T/D = 1.2$, (**b**) $T/D = 1.6$, and (**c**) $T/D = 2.5$.

3.3. Streamwise Cylinders

As for the two cylinders with the streamwise arrangement, also three cases of cylinder spacing are considered in the present study, and the simulated hydrodynamic performances are summarized in Table 8. The subscripts C1 and C2 in Table 8 denote the upstream cylinder and the downstream cylinder, respectively. As shown in Table 8, for the streamwise arrangement, the drag coefficient of the upstream cylinder almost keeps constant at the level lower than that of a single cylinder when the cylinder spacing is relatively small ($L/D < 3.0$). However, when the cylinder spacing further increases, the drag coefficient of the upstream cylinder will rise to a value higher than that of a single cylinder. By comparison, with the increase in the cylinder spacing, the drag coefficient of the downstream cylinder gradually increases, while the value is always significantly lower than that of the upstream cylinder. As for the Strouhal number, it decreases and then increases with the increase in cylinder spacing.

Table 8. Flow separation parameter of streamwise cylinders.

Case	*L/D*	$c_{D,C1}$	$c_{D,C2}$	**St**
Case Single	0, single cylinder	1.210		0.215
Case L2.5	2.5	0.917	−0.080	0.136
Case L3.0	3.0	0.915	0.168	0.126
Case L3.5	3.5	1.370	0.307	0.2

The circumferential distribution of the pressure coefficient on upstream cylinder 1 and downstream cylinder 2 are plotted in Figure 10. Because of the symmetric characteristics along the streamwise direction, only the circumferential distributions from 0° to 180° are displayed here. For upstream cylinder 1, the distribution of pressure coefficient of the streamwise cylinders is quite similar to that of a single cylinder. At the windward side, the pressure coefficients of the streamwise cylinders are almost the same as that of a single cylinder. However, the difference in pressure coefficients between a single cylinder and streamwise cylinders starts to appear when it comes to the leeward side, which indicates that the downstream cylinder mainly influences the leeward side of the upstream cylinder. Also, such difference gradually reduces with the increase in the cylinder spacing. As for downstream cylinder 2, the circumferential distribution of pressure coefficient shows a quite different characteristic. For small spacing of $L/D = 2.5$ or 3.0, the pressure coefficient at the windward side is even lower than at the leeward side. As cylinder spacing further increases to $L/D = 3.5$, the pressure coefficient at the windward side becomes higher than that at the leeward side again, which is closer to the distribution of a single cylinder.
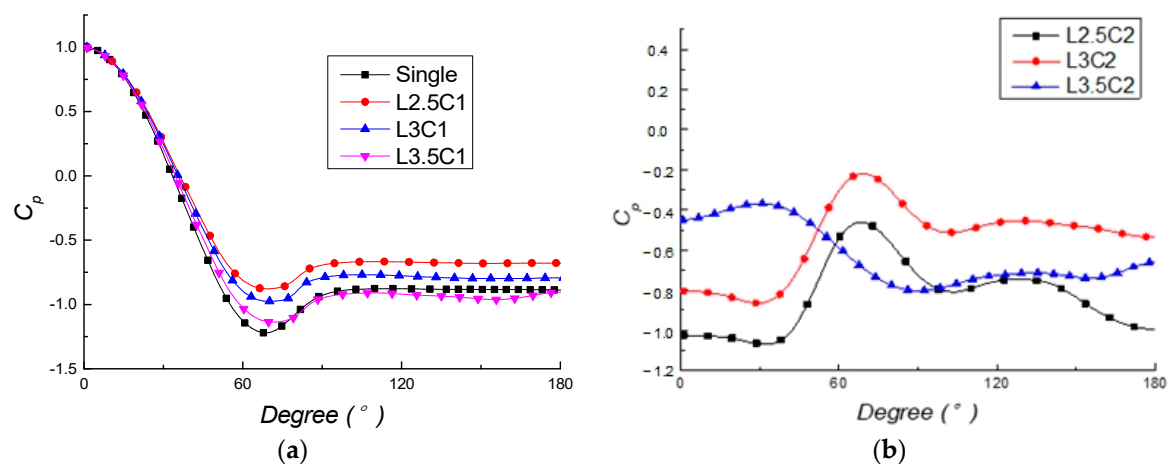

Figure 10. Mean pressure coefficients around cylinders with streamwise arrangement for (**a**) Cylinder 1 and (**b**) Cylinder 2.

The flow separation points are also calculated for the upstream and downstream cylinders, and the results are listed in Table 9. It can be found that the flow separation point moves upstream in the upstream cylinder, while it moves downstream in the downstream cylinder. Also, the flow separation for both upstream and downstream cylinders is always later than that of a single cylinder.

Table 9. Flow separation parameter of streamwise cylinders.

Case	L/D	Upstream Cylinder 1 θ_{sep}	Downstream Cylinder 2 θ_{sep}
Single	0	88	
L2.5	2.5	93.04	119.74
L3.0	3.0	92.57	120.78
L3.5	3.5	90.18	125.48

Figure 11 depicts the distribution of streamwise velocity along the *y*-direction at different downstream locations for a single cylinder and streamwise cylinders. From top to bottom they are the single cylinder, the upstream cylinder, and the downstream cylinder, respectively. The development of velocity distribution from U-shaped to V-shaped in the single-cylinder case does not exist in the streamwise cylinders. The velocity distribution downstream of the upstream cylinder is more complex than that of the downstream cylinder, especially in the case of small cylinder spacing, which mainly results from the blockage effect of the downstream cylinder.
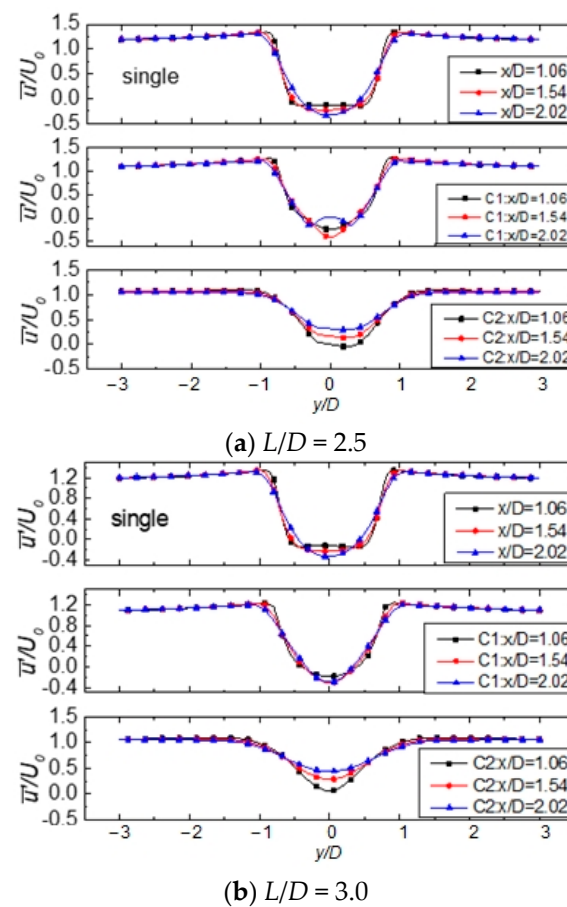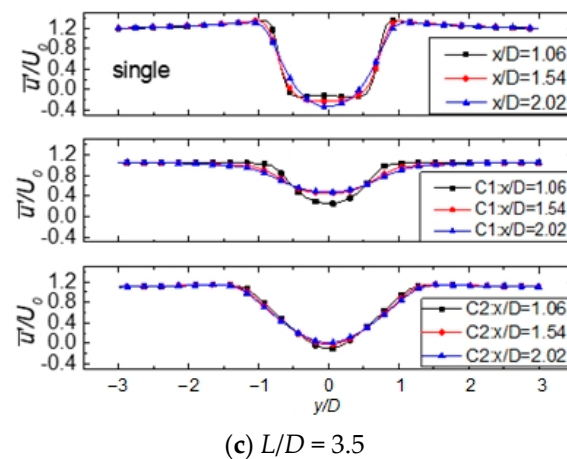

(**a**) *L/D* = 2.5

(**b**) *L/D* = 3.0

Figure 11. *Cont*.

(**c**) L/D = 3.5

Figure 11. Mean streamwise velocity at downstream locations for streamwise cylinders for (**a**) L/D = 2.5, (**b**) L/D = 3.0, and (**c**) L/D = 3.5.

Figure 12 illustrates the contour distribution of vorticity around streamwise cylinders at different cylinder spacings at (left) $t = t_0$ and (right) $t = t_0 + 5/6T$, where the symbols A and B denote the flow patterns induced by the upstream and downstream cylinders, respectively. At the small cylinder spacing of L/D = 2.5 and 3.0, before the shear layer has time to develop into a vortex, it is already blocked by the downstream cylinder and attaches again to the surface of the downstream cylinder. The shear layer from the upstream cylinder attached to the downstream cylinder merges with the downstream cylinder's own shear layer, and then sheds with the vortex of the downstream cylinder. Such reattachment contributes to the increase in the pressure coefficient in the downstream cylinder, as shown in Figure 10b. By comparison, when it comes to the large cylinder spacing of L/D = 3.5, the cylinder spacing is sufficiently large for the full development of shear layers. Therefore, the double-cylinder flow pattern is switched from the reattachment regime to the vortex-shedding regime. As shown in Figure 12c, the vortex structure A3 sheds from the upstream cylinder and then merges with the attached shear layer on the downstream cylinder. This development promotes the vortex shedding from the downstream cylinder. Therefore, the Strouhal number at the large cylinder spacing is higher than that at small cylinder spacings because the vortex-shedding process is accelerated by the merging of the shedding vortex from the upstream cylinder and the shear layer on the downstream cylinder. According to the above discussion, it can be summarized that the interaction of two streamwise cylinders will suppress the vortex formation of the upstream cylinder when cylinder spacing is small.
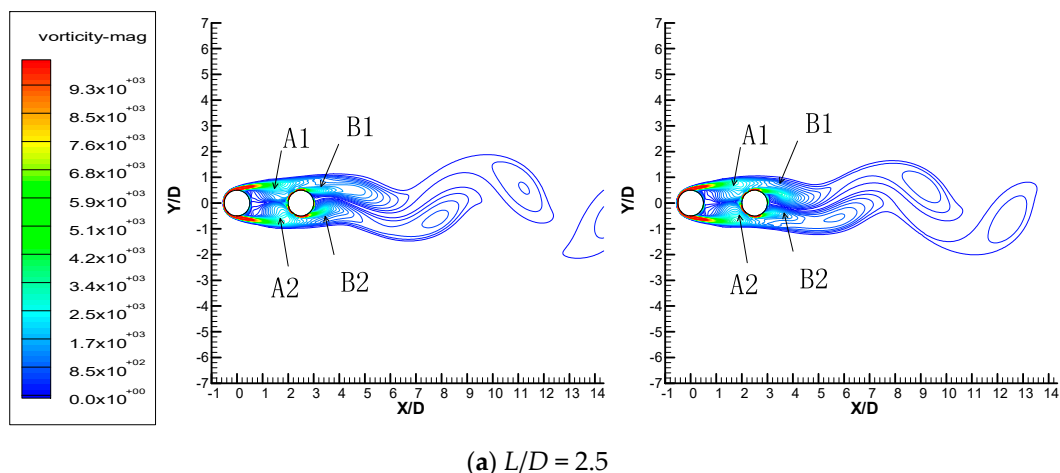

(**a**) L/D = 2.5
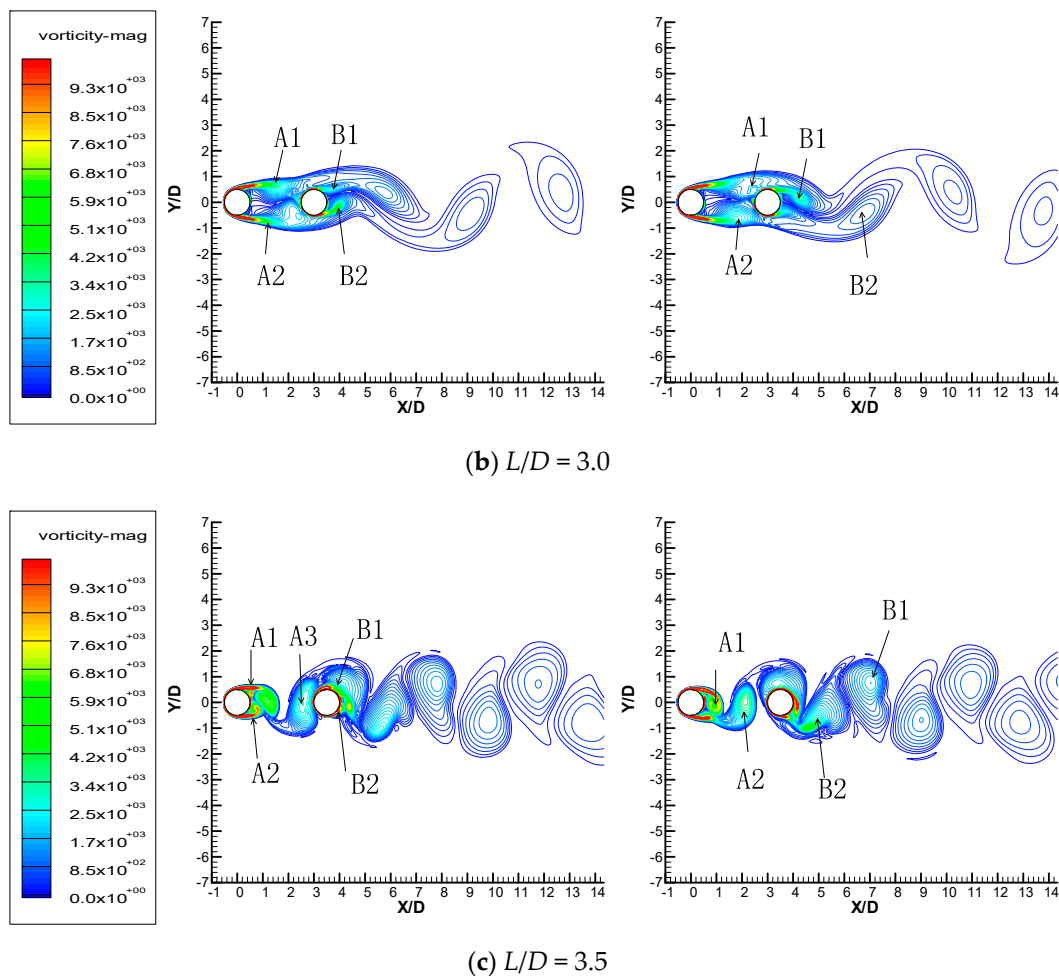
Figure 12. *Cont.*

(**b**) *L/D* = 3.0

(**c**) *L/D* = 3.5

Figure 12. Vorticity distribution around streamwise cylinders at (**left**) $t = t_0$ and (**right**) $t = t_0 + 5/6T$ for (**a**) *L/D* = 2.5, (**b**) *L/D* = 3.0, and (**c**) *L/D* = 3.5.

Moreover, as indicated in Du X, et al. [42]'s and de Moraes and Pereira [43]'s studies, the surface roughness of the cylinder can also significantly influence the flow characteristics. When rough cylinder surfaces are applied, both drag and Strouhal numbers reduce compared with a smooth cylinder surface, as do instabilities. Also, it is pointed out that the surface roughness of the downstream cylinder has a larger influence in the streamwise arrangement.

4. Conclusions

Large eddy simulations are carried out in the present study to investigate the flow characteristics around double cylinders with crosswise and streamwise arrangements. According to the numerical results, the following conclusions can be drawn.

The influences of the number of mesh cells, the first near-wall mesh size, and the transient time step on the simulation results are studied systematically to determine the proper parameters for accurate and efficient simulations. After determining all these numerical settings, the relative errors of time-averaged drag coefficient and Strouhal number compared with the existing experimental data are 1.88% and 0.14%, respectively, which validates the accuracy of the present numerical method.

For crosswise arrangements, the drag coefficient is always higher than that of the single cylinder. The stagnation points for both cylinders deviate toward the spacing side due to their interactions with each other. With an increase in the cylinder spacing, the flow pattern switches from a single-body regime to a synchronized vortex-shedding regime because of weaker interaction.

For streamwise arrangements, as cylinder spacing increases, the drag coefficient of the upstream cylinder gradually increases from a lower value to a higher one compared with the single cylinder, while the drag coefficient of the downstream cylinder is always smaller. Also, the flow separation point moves upstream in the upstream cylinder, while it moves downstream in the downstream cylinder. The flow pattern develops from the reattachment regime to the vortex-shedding regime.

As this study is aimed at ocean wave energy utilization, it is straightforward to perform further simulations of fluid–solid interaction that consider the vibration of multiple cylinders. By means of such analysis, the vortex-induced vibrations of multiple cylinders can be investigated in detail. This remains to be future researched.

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