



Article A Control Design Technology of Isolated Bidirectional LLC Resonant Converter for Energy Storage System in DC Microgrid Applications

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Abstract: This paper presents a new control method for a bidirectional DC–DC LLC resonant topology converter. The proposed converter can be applied to power the conversion between an energy storage system and a DC bus in a DC microgrid or bidirectional power flow conversion between vehicleto-grid (V2G) behavior and grid-to-vehicle (G2V) behavior. Furthermore, such a converter can be applied to energy storage systems for decentralized renewable energy generation systems, such as solar and wind power. In addition, this converter can be combined with a bidirectional inverter to allow energy storage in the system to improve the safety, stability, and power quality of the microgrid. In the proposed circuit structure, we use a bidirectional DC–DC LLC, which has the advantages of a higher voltage conversion ratio, lower part count, simpler control than similar converters such as DAB, CLLC, and L-LLC converters, and bidirectional power flow and electrical isolation. Specifically, to extend the battery life, it can be employed as a control strategy for discharging the energy stored in the battery (SOC) and reducing the temperature rise generated by the internal solid electrolyte interphase (SEI) when discharging the battery under the variation in distributed energy resource (DER) generation and load demand. To realize the bidirectional power conversion without using any auxiliary inductor and only changing the control strategy, the forward step-down power conversion was based on pulse frequency modulation (PFM) control, and the reverse step-up power conversion was based on pulse width modulation (PWM) control. In this paper, we introduce the bidirectional converter topology and its control strategy for the DC microgrid battery energy storage system. Finally, a 500 W prototype is built to verify the effectiveness of the proposed converter.

Keywords: bidirectional DC–DC converter; LLC topology; push–pull topology; resonant converter; zero voltage switching

1. Introduction

1.1. Overview

In addition to energy supply and demand, economic efficiency, environmental protection, and impact assessment are crucial to energy development. In the face of the multiple challenges of energy security and global warming, how to ensure the security of energy supply and sustainable development of the environment are key issues that policymakers must carefully consider. Therefore, developing low-carbon energy sources and improving the efficiency of various energy uses and conversions are becoming a priority. The development of distributed generation (DG) based on renewable energy [1] and the demand for clean electricity from photovoltaic, fuel cells, wind, geothermal, and ocean energy are increasingly favored because of the low energy density of renewable energy and the high cost of traditional power generation. Most renewable energy sources are intermittent and must be stored to ensure the stability of the power supply. For example, the battery energy storage system (BESS) [2] and the electric vehicles (EVs) [3] are power storage units for



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Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). different renewable energy sources and realize the vehicle-to-grid (V2G) behavior and the grid-to-vehicle behavior (G2V) [4]. Therefore, the BESS should have a bidirectional power flow capability to store energy when excess renewable energy is generated and release it when there is a shortage or during a peak in energy consumption. By incorporating storage elements into the renewable energy system, the concerns of variability and intermittency caused by integrating renewable energy with the grid can be mitigated to some extent. DC microgrids [5] can operate in one of two modes: stand-alone or grid-connected. In stand-alone mode, the local load is controlled by the renewable energy generated and the BESS. In the grid-connected mode, the power flow between DC and AC microgrids allows for more flexibility and can also provide ancillary services (A/S) [6], bringing additional benefits of decentralized grid flexibility to the generators and consumers. Figure 1 shows a typical DC microgrid structure. Since there are various renewable energy sources, such as photovoltaic panels that generate DC power, a DC–DC converter is used to connect the DC network for power conversion, and a DC–AC converter is used to transfer this renewable energy from the DC–DC converter to the AC grid, making the AC grid flexible and controllable. Accordingly, a DC-DC bidirectional converter transfers the BESS or EVs energy to the DC Bus.



Figure 1. Block diagram of a DC microgrid system.

Most recent research has focused on bidirectional power transfer because the bidirectional DC–DC converter is the key component in realizing the bidirectional power flow of BESS. Different topologies of bidirectional DC–DC converters have been proposed in the literature [7,8]. Bidirectional DC–DC converters can be classified into non-isolated and isolated topologies [9]. Non-isolated topologies transmit power without transformer or capacitor isolation and, therefore, lack the advantages of current isolation and high voltage gain ratio. However, they have advantages in size and weight due to their simple structure; thus, non-isolated bidirectional topologies are recommended for low-power and low-voltage gain applications. In contrast, isolated topology essentially converts the DC voltage on the primary side into a square voltage waveform and transmits it to the secondary side through a high-frequency transformer, which is then adjusted to DC output voltage. In practice, galvanic isolation is required in many specified systems for safety reasons. In addition, the voltage gain of the isolation topology can be increased by using the turn ratio of the transformer, so it is recommended for high-power and high-voltage-gain applications.

1.2. Detailed Analysis

In general, the BESS bidirectional DC–DC converter must have high power density, high efficiency, and high reliability. Various electrically isolated bidirectional DC–DC topologies have been proposed and studied in recent decades. Among these, the full-bridge phase-shift (FBPS) converter is an isolated DC–DC converter with good wide voltage regulation characteristics [10,11], but its lack of soft switching in the main circuit under light load reduces its efficiency. In addition, its topology is asymmetrical because the filter

inductors are placed on the secondary side. Therefore, even if the diodes are replaced by metal-oxide-semiconductor field-effect transistors (MOSFETs) on the secondary side, it cannot efficiently achieve bidirectional power flow. In the literature [12], a control method was proposed to operate the FBPS converter in a voltage-fed mode based on phase shift modulation in the direction of forward power flow and the current-fed mode in the direction of backward power flow based on pulse width modulation. However, there was no soft switching in the current-fed mode. In addition, when the secondary switches were turned on simultaneously to magnetize the inductor, the conduction loss was increased, and the available duty cycle was reduced, potentially leading to higher voltage stress in the PSFB converter. In another study [13], various voltage input dual active bridge (DAB) converter topologies, such as phase-shift dual active bridge (PSDAB) converters, were given two bridge switches on each side of the transformer. The phase shift between the gate drive signals for the primary-side and secondary-side switches was used to determine the power flow direction and the output power. The overall efficiency was reduced because of high backward energy and high switching loss during the cutoff period. In addition, the feature of zero-voltage switching (ZVS) was inevitably lost when the converter had a wide range of voltage variations, resulting in switching losses and increased circulating currents. At light loads, the soft switching range became narrower, and the circulating current inside the DAB converter increased significantly, resulting in a rapid decrease in efficiency. Therefore, it is challenging for this converter to maintain high efficiency over a wider voltage range. Although many improved modulation strategies have been proposed, such as single-phase-shift (SPS), dual-phase-shift (DPS) [14], and triple-phase-shift (TPS) [15], their control methods are complex and switching losses are still high. The circuit topologies of the bidirectional full-bridge CLLC converter proposed in [16,17] and the bidirectional full-bridge CLLLC resonant converter proposed in [18] are derived from the LLC series resonant converter. In the bidirectional control, the primary and secondary sides have symmetrical power conversion, a full-bridge symmetrical structure of the rectifier stage, and a bidirectional power flow with the symmetrical high-frequency transformer. Therefore, from a wide voltage range point of view, LLC is not a good choice because the large voltage gain implies a smaller ratio of magnetizing inductance to resonance inductance and a wide switching frequency range, leading to design complexity and increased power loss. The CLLC–C multiple resonance converter proposed in [19] rearranges CLLC or CLLC–C resonant networks to change the quality factor of the resonant network by controlling the auxiliary switch to achieve a wider voltage range.

The LLC resonant converter is suitable for soft switching but encounters problems when used in bidirectional operation. When the converter supplies energy in the backward direction, the magnetizing inductance of the transformer is embedded in the output voltage. This phenomenon causes the magnetizing inductor to be excluded from the circuit in the resonance process. In this case, the LLC resonance can be considered an LC series resonance with a maximum voltage gain of 1. Therefore, the LLC resonant converter is not suitable for backward voltage gains and wide voltage output. The converter proposed in [20] has a symmetrical resonant circuit on the primary and secondary sides to achieve bidirectional power flow. It achieves low or high voltage gain by selecting the operation of the halfbridge or full-bridge circuit structure. Therefore, this converter can realize the output voltage with a controlled voltage increase range to avoid the wide range of switching frequency variation in conventional bidirectional resonant converters. Another study [21] proposed a full-bridge topology-based bidirectional resonant converter. In the forward operation, switching between the half-bridge and full-bridge configurations extends the output voltage range by providing a step-down gain of 0.5 or 1. In the backward operation, a double voltage rectification (DVR)-control method is used to realize a double voltage gain on the rectifier side, which can effectively extend the operating voltage range. The conventional resonant converter control method is only used for unidirectional power conversion and works only in a buck or boost mode. In the study by [22], a bidirectional synchronous/nonsynchronous rectifier control method for bidirectional LLC chargers is

proposed, while a synchronous rectification was performed in the forward mode. In the backward mode, the asynchronous rectifier was performed to generate the gate drive signals with a delay angle between the secondary and primary sides, resulting in high voltage gain at low battery voltage, leading to increased power losses. In the high battery voltage range, the delay angle was adjusted to zero to achieve high efficiency. In [23], a PWM control strategy was proposed to realize the natural bidirectional power flow of LLC–DCX (DC–DC Transformer, DCX), which can operate even when the resonance parameter changes. However, since the optimal operation point is at the resonance point, deviation from the resonance point would result in circulating losses and reduced voltage gain. Several studies [24–29] proposed an L–LLC resonant structure by adding an auxiliary inductor to the conventional LLC topology so that the resonance characteristics of each resonant mode could be LLC in both directions of operation. The power loss increased by

adding an auxiliary inductor across the high voltage on the secondary side. Table 1 summarizes the above analysis and compares the existing converters. The PSFB [12] has relatively few parts and relatively poor efficiency, while DAB [15] has more parts and relatively low voltage gain with complex control. The CLLC [17] is similar to DAB [20], which has a higher number of switches and increased complexity of control in order to expand the output range and change from full-bridge to half-bridge and vice versa. The L–LLC [25] adds an auxiliary inductor across the high-voltage terminal on the secondary side to increase the power loss. It cannot achieve a wide voltage range because of its use of PFM control.

Ref. No. Parameter	[12]	[15]	[17]	[20]	[25]
Input voltage	12 V	70–110 V	280–403 V	400 V	30–50 V
Output voltage	400 V	60 V	400 V	200–450 V	350 V
Output power	300 W	300 W	1 kW	1 kW	3 kW
Max. efficiency	<90%	<96%	94.6%	93.5%	95.6%
Topology	PSFB	DAB	CLLC	CLLC	L-LLC
Control technique	Phase control	Phase control	PFM	PFM	PFM
No. of main switches	6	8	8	10	8
No. of inductors/ transformers/ capacitors	2/1/0	1/1/0	2/1/2	2/1/2	2/1/1

Table 1. Comparison of the existing converters.

1.3. Motivation

This paper presents a design method for a bidirectional LLC resonant converter used in energy storage systems. In addition, the asymmetric characteristics of the LLC resonant converter in the forward and backward modes are studied, and the effect of asymmetry on the resonant converter is investigated. In addition, a design method for a bidirectional LLC resonant converter is presented to reduce the need for an auxiliary inductor in the design of the backward resonant circuit shown in [24–29]. Specifically, a forward buck power flow adopts a conventional LLC resonant structure by relocating the LLC resonant tank, and a backward boost power flow employs a push–pull structure with an inductor and a capacitor in the secondary-side rectifier converter (LC-SRC) resonance by relocating the LC resonant tank. Therefore, the converter combines a conventional push–pull converter with PWM control to obtain a wide input voltage range and LC–SRC resonance characteristics. This LC-SRC converter not only has all the advantages of resonance characteristics but also the following benefits:

1. The low voltage side is defined as the primary side, whereas the high voltage side is defined as the secondary side;

- 2. All switches have ZVS turn-on, and the body diodes of the primary-side switches have ZCS turn-off, thus reducing switching losses and improving overall efficiency;
- 3. Compared with the half-bridge structure, the primary side is driven by the low-side gate drivers, so no floating gate drivers are needed, thus simplifying the design of the drive circuit and reducing costs;
- 4. The switching duty cycle is maintained at about 0.5 to obtain the maximum component utilization;
- 5. The series connection of a resonant capacitor can isolate the DC current to avoid the magnetic escape of the transformer.

In the following, Section 2 introduces the basic operating principles and related theoretical derivations of the proposed forward buck LLC resonant converter topology and the backward boost LC resonant push–pull converter topology. In Section 3, the parameters of the converter are designed, and in Section 4, the digital control method of battery charging and discharging is described. Section 5 presents the experimental results of a 500 W prototype, and Section 6 concludes the discussion.

2. Topology Description

2.1. Forward Buck-Type Energy Transfer

As shown in Figure 2, a typical LLC resonant converter consists of a high input voltage V_H , full-bridge switches S_1 to S_4 , an LLC resonant tank, a transformer, rectifiers S_5 and S_6 , an output filter C_L , and a load voltage V_L . The resonant tank consists of a series inductor L_r , a series capacitor C_r , and a magnetizing inductor L_m . The power flows from V_H through the transformer to V_L .



Figure 2. Proposed buck-type DC-DC Converter.

The series inductor L_r and the series capacitor C_r form a series resonant circuit with one resonant frequency f_{r1} defined in Equation (1), which has the minimum impedance to a sinusoidal current with the resonant frequency f_{r1} . The switching frequency f_s for the full-bridge switches S_1 to S_4 is far from the resonant frequency f_{r1} as the high input voltage V_H is increased on condition that the load voltage V_L is kept constant. As the load decreases, the magnetizing inductance L_m participates in the LLC resonant operation and generates the other resonant frequency f_{r2} , as described in Equation (2). Therefore, the switching frequency f_s determined by the load conditions moves between the range of f_{r1} and f_{r2} .

$$f_{r1} = \frac{1}{2\pi\sqrt{L_r C_r}}\tag{1}$$

$$f_{r2} = \frac{1}{2\pi\sqrt{(L_m + L_r)C_r}}$$
(2)

2.1.1. Voltage Gain under the Turns Ratio Equal to One

The principle of the first harmonic analysis (FHA) method is that the main component of the circulating current in the resonant circuit is a pure sinusoidal current. Therefore, by assuming that only the fundamental wave of the current transfers power to the load, ignoring all higher harmonics, the AC equivalent model of the LLC resonant converter can be obtained from the assumptions shown in Figure 3. In addition, the parasitic inductance of the output filter capacitor and the primary-side leakage inductance of the transformer are ignored, and the primary-side parameters are reflected to the secondary side.



Figure 3. AC equivalent circuit of the LLC resonant converter based on the FHA.

The equivalent circuit shown in Figure 4 can be obtained by applying Thévenin's theorem to the LLC equivalent circuit, as shown in Figure 3.



Figure 4. An equivalent circuit obtained from Thévenin's theorem based on a phasor diagram.

The voltage V_{Tp} is defined by Equation (3):

$$V_{Tp} = V_{ap} \frac{\omega_s^2 C_r L_m}{\omega_s^2 C_r (L_r + L_m) - 1}$$
(3)

The Thévenin's equivalent impedance of the AC equivalent circuit of the LLC resonant converter can be defined as Equation (4):

$$Z_T = \frac{j\omega_s L_m(\omega_s^2 C_r L_r - 1)}{\omega_s^2 C_r (L_r + L_m) - 1}$$
(4)

From (4), the Thévenin's equivalent inductive impedance can be written as Equation (5):

$$L_T = \frac{L_m(\omega_s^2 C_r L_r - 1)}{\omega_s^2 C_r (L_r + L_m) - 1}$$
(5)

To obtain the curves of the steady-state sinusoidal currents and voltages of the LLC converter, a phasor diagram is used to represent them, as shown in Figure 4.

The fundamental harmonic of the AC input voltage with the square wave, called V_H , is given by Equation (6):

$$V_{ap} = \frac{4V_H}{\pi} \tag{6}$$

The fundamental harmonic of the secondary-side AC output voltage with the square wave, called V_L , which is reflected from V_H , is given by Equation (7):

$$V_{bp} = \frac{4V_L}{\pi} \tag{7}$$

The load current I_o reflected to the secondary side, called I_{bp} , can be expressed by Equation (8):

$$I_{bp} = \frac{\pi}{2} I_o \tag{8}$$

Figure 5 shows the synthetic phase diagram. The angle ϕ represents the phase difference between the voltages V_{Tp} and V_{bp} . From the analysis of the vector diagram shown in Figure 5, Equation (9) can be written.

$$V_{Tp}^{2} = V_{bp}^{2} + (\omega_{s}L_{T}I_{bp})^{2}$$
⁽⁹⁾



Figure 5. Synthetic phasor diagram.

Substituting Equations (7) and (8) into (9) yields Equation (10):

$$V_{Tp}^{2} = \left(\frac{4V_{L}}{\pi}\right)^{2} + \left(\frac{\omega_{s}L_{T}\pi I_{o}}{2}\right)^{2}$$
(10)

Substituting Equations (3) and (5) into (10) yields Equation (11):

$$(V_L)^2 = (V_H)^2 \left[\frac{\omega_s^2 C_r L_m}{\omega_s^2 C_r (L_r + L_m) - 1}\right]^2 - \frac{\pi^4}{64} \left[\frac{\omega_s L_m (\omega_s^2 C_r L_r - 1) I_o}{\omega_s^2 C_r (L_r + L_m) - 1}\right]^2$$
(11)

where the following definitions are

$$M = \frac{V_L}{V_H} \tag{12}$$

$$\omega_s = 2\pi f_s \tag{13}$$

$$\omega_r = \frac{1}{\sqrt{C_r L_r}} \tag{14}$$

$$f_n = \frac{f_s}{f_{r1}} \tag{15}$$

$$\lambda = \frac{L_r}{L_m} \tag{16}$$

$$\overline{I_o} = \frac{\omega_s L_r}{V_H} I_o \tag{17}$$

By substituting Equation (12) to (17) into (11), the voltage gain *M* can be expressed as Equation (18):

$$M = \frac{\sqrt{f_n^4 - \frac{\pi^4}{64} [(f_n^2 - 1)\overline{I_o}]^2}}{f_n^2 (\lambda + 1) - \lambda}$$
(18)

From (18), the voltage gain is a function of the load current. The equivalent AC load resistance R_{ac} is defined as the load resistance R reflected to the secondary side of the transformer, as shown in Equation (19). Therefore,

$$R_{ac} = \frac{V_{bp}}{I_{bp}} \tag{19}$$

Based on (7) and (8), rearranging (19) yields

$$R_{ac} = \frac{4V_L}{\pi} \frac{2}{\pi I_o} \tag{20}$$

Equation (20) can be rewritten to

$$R_{ac} = R \frac{8}{\pi^2} \tag{21}$$

Additionally, the quality factor *Q* of the resonant circuit is defined as

$$Q = \frac{\sqrt{L_r/C_r}}{R_{ac}} \tag{22}$$

Therefore, by substituting Equation (22) into (18) and performing appropriate algebraic operations, Equation (23) can be obtained as

$$M = \frac{f_n^2}{\sqrt{\left[f_n^2(\lambda+1) - \lambda\right]^2 + \left[f_n Q(f_n^2 - 1)\right]^2}}$$
(23)

From (23), under a given value of λ , the curves of voltage gain M versus normalized switching frequency f_n under different quality factors of Q are plotted in Figure 6. Using Equation (23), under a given value of Q, curves of the voltage gain M as a function of the normalized switching frequency f_n from different quality factors of λ are plotted in Figure 7.



Figure 6. Curves of voltage gain *M* versus normalized switching frequency f_n under different quality factors of *Q*.



Figure 7. Curves of voltage gain *M* versus normalized switching frequency f_n under different values of λ .

The previous analysis considered a primary harmonic approximation equivalent circuit LLC converter where all voltages and currents are sinusoidal. In the following, the switching frequency of the LLC converter is investigated for modes where the switching frequency is lower, equal, or greater than the first resonance frequency. All the components are considered ideal, and all the primary-side parameters and loads are reflected to the secondary side. Only the waveforms within 0.5 T_s are considered, where T_s is the switching period.

Case 1: Switching Frequency Equal to Resonant Frequency ($f_s = f_{r1}$)

Figure 8 shows the corresponding illustrated waveforms, and Figure 9 shows the accompanying current flows in three operating modes.



Figure 8. Illustrated waveforms at $f_s = f_{r1}$.



Figure 9. Case 1 current flow: (a) Mode 1; (b) Mode 2; (c) Mode 3.

Mode 1: $[t_0 \le t \le t_1]$

As shown in Figures 8 and 9a, since the voltages v_a and v_{Lm} are positive, the resonant current i_{Lr} and the magnetizing current i_{Lm} are negative with sinusoidal and linear rise, respectively. At $t = t_1$, this mode ends at $i_{Lr} = 0$, proceeding to Mode 2.

Mode 2: $[t_1 \le t \le t_2]$

As shown in Figures 8 and 9b, the resonance current i_{Lr} is positive and increases sinusoidally, while the magnetization current i_{Lm} is negative and increases linearly. At $t = t_2$, this mode ends at $i_{Lm} = 0$, proceeding to Mode 3.

Mode 3: $[t_2 \le t \le t_0 + T_s/2]$

As shown in Figures 8 and 9c, the resonant current i_{Lr} and the magnetizing current i_{Lm} are both positive with sinusoidal and linear rise, respectively. At $t = t_3$, this mode ends at $i_0 = 0$, proceeding to Mode 1.

At the resonant frequency, the LLC resonant converter is able to turn on the secondaryside switch with ZVS. At the same time, the turn-off current is the maximum magnetizing inductance current. By selecting a suitable magnetizing inductance, a slight turn-off loss can be achieved. In addition, the primary-side diode is turned off with low voltage across it due to *di/dt*, which means less reverse recovery loss. Thus, the optimal performance of the LLC resonant converter is expected at the resonant frequency. At the resonant frequency, the series resonant circuit impedance is zero. Therefore, the input and output voltages are connected, and the voltage gain at the resonant frequency is equal to one.

Case 2: Switching Frequency Greater than Resonant Frequency ($f_s > f_{r1}$)

Figures 10 and 11 show the corresponding illustrated waveforms and the accompanying current flows, respectively. There are four operating modes.



Figure 10. Illustrated waveforms at $f_s > f_{r1}$.



Figure 11. Case 2 current flow: (a) Mode 1; (b) Mode 2; (c) Mode 3; (d) Mode 4.

Mode 1: $[t_0 \le t \le t_1]$

As shown in Figures 10 and 11a, the voltage v_a is larger than the voltage v_b . Since the voltages v_a and v_{Lm} are positive, the resonant current i_{Lr} and the magnetizing current i_{Lm} are negative with sinusoidal and linear rise, respectively. At $t = t_1$, this mode ends at $i_{Lr} = 0$, proceeding to Mode 2.

Mode 2: $[t_1 \le t \le t_2]$

As shown in Figures 10 and 11b, the resonance current i_{Lr} is positive and increases sinusoidally, while the magnetization current i_{Lm} is negative and increases linearly. At $t = t_2$, this mode ends at $i_{Lm} = 0$, proceeding to Mode 3.

Mode 3: $[t_2 \le t \le t_3]$

As shown in Figures 10 and 11c, the resonant current i_{Lr} and the magnetizing current i_{Lm} are both positive with sinusoidal and linear rise, respectively. At $t = t_3$, the input voltage v_a reverses and becomes negative, and this mode ends, proceeding to Mode 4.

Mode 4: $[t_3 \le t \le t_0 + T_s/2]$

As shown in Figures 10 and 11d, the resonance current i_{Lr} decreases until it equals the magnetization current i_{Lm} . At $t = t_0 + T_s/2$, $i_{Lr} = i_{Lm}$, this mode ends, proceeding to Mode 1.

When the circuit operates at $f_s > f_{r1}$, the voltage v_a reverses polarity before the current i_o naturally reaches zero, causing the rectifier diode to be turned off with relatively high voltage across it due to di/dt, which results in a relatively large reverse recovery current of the diode, thereby increasing switching losses and sacrificing efficiency. In addition, the high diode di/dt turn-off will generate additional voltage stress on the diode, thereby reducing the circuit reliability. For these reasons, the operation at $f_s > f_{r1}$ is undesirable compared with the operation Cases 1 and 2, which should be avoided.

Case 3: Switching Frequency Less than Resonant Frequency ($f_s < f_{r1}$)

Figures 12 and 13 show the corresponding illustrated waveforms and the accompanying current flows, respectively. There are four operating modes.



Figure 12. Illustrated waveforms at $f_s < f_{r_1}$.



Figure 13. Case 3 current flow: (a) Mode 1; (b) Mode 2; (c) Mode 3; (d) Mode 4.

Mode 1: $[t_0 \le t \le t_1]$

As shown in Figures 12 and 13a, the voltage v_b is larger than the voltage v_a . Since the voltages v_a and v_{Lm} are positive, the resonant current i_{Lr} and the magnetizing current i_{Lm} are negative with sinusoidal and linear rise, respectively. At $t = t_1$, this mode ends at $i_{Lr} = 0$, proceeding to Mode 2.

Mode 2: $[t_1 \le t \le t_2]$

As shown in Figures 12 and 13b, the resonance current i_{Lr} is positive and increases sinusoidally, while the magnetization current i_{Lm} is negative and increases linearly. At $t = t_2$, this mode ends at $i_{Lm} = 0$, proceeding to Mode 3.

Mode 3: $[t_2 \le t \le t_3]$

As shown in Figures 12 and 13c, the resonant current i_{Lr} and the magnetizing current i_{Lm} are both positive with sinusoidal and linear rise, respectively. At $t = t_3$, this mode ends at $i_{Lr} = i_{Lm}$, proceeding to Mode 4.

Mode 4: $[t_3 \le t \le t_0 + T_s/2]$

As shown in Figures 12 and 13d, during this state, $i_0 = 0$ and $i_{Lr} = i_{Lm}$ with linear rise. At $t_0 + T_s/2$, the input voltage v_a reverses and becomes negative, and this mode ends, proceeding to Mode 1.

The operation with $f_s < f_{r1}$ differs in one respect from the operation with $f_s = f_r$; the output rectifier current i_0 is discontinuous.

2.2. Backward Boost-Type Energy Transfer

Figure 14 illustrates the high-voltage gain zero-voltage switching (ZVS) push–pull resonant converter. The main circuit consists of a power switch, a high-frequency center-tap transformer, a resonant circuit, a full-bridge rectifier, and an output capacitor. The zero-voltage switching push–pull resonant converter consists of bidirectional switches S_5 and S_6 with a duty period of nearly 0.5. The resonant inductor L_r is built by the secondary-side leakage inductor and connected with the resonant capacitor C_r to form a resonant tank. However, the magnetizing inductance of a high-frequency transformer is considerable. Consequently, the magnetizing current is negligible. The series resonant circuit is fed from the square wave output voltage on the secondary side of this transformer. The L_r and C_r waveforms are converted into a sinusoidal current for soft-switching operation. The full-bridge rectifier makes the output voltage equal to the peak output voltage V_H can be regarded as constant. The regulation of the output current is controlled by the change in the duty cycle of the switching period.



Figure 14. Proposed step-up DC-DC Converter.

2.2.1. Series Load Resonant Converter Analysis

The proposed LC-SRC resonant converter is designed to reduce electromagnetic interference and harmonic distortion because the inductive reactance of the inductor is equal to the capacitive reactance in the resonant case, thereby generating the resonant frequency. In resonant frequency operation, the resonant tank impedance is minimized, and the resonant circuit is used to create a sinusoidal output current. In addition, the characteristic impedance of the resonant circuit is defined as Z_r in Equation (24), and its resonant angular frequency is defined as ω_r in Equation (25)

$$Z_r = \sqrt{\frac{L_r}{C_r}} \tag{24}$$

$$\omega_r = \frac{1}{\sqrt{L_r C_r}} \tag{25}$$

As shown in Figure 15, the load resistor R_L is connected in series with the resonant tank to form a series resonant circuit with an inductor L_r , a capacitor C_r , and a resistor R_L . If the frequency of the secondary-side output square wave voltage is f_s , the series resonant circuit has a filtering function, allowing only the fundamental current to pass. In addition, the turns ratio is n.



Figure 15. Equivalent circuit based on phasor diagram.

The equivalent impedance Z_{eq} of the resonant circuit, viewed from the input voltage to the right, is shown in Equation (26) as

$$Z_{eq} = R_L + j(\omega L_r - \frac{1}{\omega C_r})$$
(26)

The magnitude and phase of Z_{eq} are shown in Equations (27) and (28), respectively:

$$||Z_{eq}|| = \sqrt{R_L^2 + (\omega L_r - \frac{1}{\omega C_r})^2}$$
 (27)

$$\theta_{Zeq} = \theta_v - \theta_i = \tan^{-1}\left(\frac{\omega L_r - \frac{1}{\omega C_r}}{R_L}\right)$$
(28)

2.2.2. Voltage Gain

The ratio of the output voltage V_H to the input voltage nV_L in a series resonant circuit called voltage gain, is shown in Equation (28):

$$\frac{V_H}{nV_L} = \frac{R_L}{\sqrt{R_L^2 + (\omega_s L_r - \frac{1}{\omega_s C_r})^2}}$$
(29)

$$\omega_s = 2\pi f_s \tag{30}$$

The quality factor *Q* is defined by Equation (31):

$$Q = \frac{\omega_r L_r}{R_L} = \frac{1}{\omega_r R_L C_r} = \frac{\sqrt{\frac{L_r}{C_r}}}{R_L}$$
(31)

$$\omega_r = 2\pi f_r = \frac{1}{\sqrt{L_r C_r}} \tag{32}$$

In Equation (32), f_r is the resonant frequency of the series resonant circuit, so that the voltage gain can be expressed as Equation (33):

$$\frac{V_H}{nV_L} = \frac{1}{\sqrt{1 + Q^2 (\frac{\omega_r}{\omega_s} - \frac{\omega_s}{\omega_r})^2}}$$
(33)

As shown in Figure 16, the relationship between the output–input ratio and the normalized frequency of the series resonant circuit is plotted by different quality factors of Q. Under given values of V_L and ω_s , the higher the quality factor Q, the smaller the voltage across the load resistor, so reducing the inductance L_r and increasing the capacitance C_r can reduce the quality factor Q to increase the output voltage and keep it close to one.



Figure 16. Relationship between the voltage input–output ratio and normalized frequency of the series resonant circuit.

2.2.3. Operating Principles

The backward boost-type push–pull converter, shown in Figure 14, consists of a push–pull converter and a full-bridge rectifier. The switching frequency f_s of the resonant converter is operated at the series resonant frequency f_r so that the resonant circuit is reviewed as a high-frequency filterer, and after this filter, the full-bridge rectifier is used to generate the required DC output voltage. The switches S_5 and S_6 have duty cycles of nearly 0.5, and only the waveforms within 0.5 T_s are considered. Figures 17 and 18 show the corresponding illustrated waveforms and the accompanying current flows, respectively. There are six operating modes.

Mode 1: $[t_0 \le t \le t_1]$

As shown in Figures 17 and 18a, v_{TS} is positive, equal to nV_L . During this blanking time, the magnetizing current i_{Lm} charges the parasitic capacitance of the switch S_6 to double the input voltage V_L and discharges the parasitic capacitance of the switch S_5 to zero; the body diode of S_5 is conducted, and then S_5 can be turned on with ZVS. The current in the secondary-side magnetizing inductance L_m called i_{Lm} , increases linearly as in Equation (34):

$$i_{Lm}(t) = i_{Lm}(t_0) + (v_{TS}/L_m)t$$
(34)



Figure 17. Illustrated waveforms.



Figure 18. Current flow: (a) Mode 1; (b) Mode 2; (c) Mode 3; (d) Mode 4; (e) Mode 5: (f) Mode 6.

Mode 2: $[t_1 \le t \le t_2]$:

As shown in Figures 17 and 18b, v_{TS} is still positive. During this blanking time, the voltage across the switch S_6 is double the input voltage V_L . Since the switch S_5 is turned with ZVS at t_1 , the input voltage V_L is applied to the primary-side winding N_{p1} , and the corresponding duration is about one-half of the switching cycle. During this mode, i_{Lm} is negative and linearly rising, and the power is transferred through the transformer to the DC output on the secondary side. Thus, the voltage across the resonant capacitor C_r , called v_{Cr} , is expressed by Equation (35), the voltage across the resonant inductor L_r , called v_{Lr} , is expressed by Equation (36), the sinusoidal current i_o is expressed by Equation (37), and the secondary-side current i_s is expressed by Equation (38). At $t = t_2$, this mode ends $i_{Lm} = 0$, proceeding to Mode 3:

$$v_{Cr}(t) = v_{Cr}(t_1) \cos \omega_r(t - t_1)$$
(35)

$$v_{Lr}(t) = (v_{TS} - v_H) - v_{Cr}(t_1) \cos \omega_r(t - t_1)$$
(36)

$$i_o(t) = \frac{[v_{TS} - v_H - v_{Cr}(t_1)]}{Z_r} \sin \omega_r (t - t_1)$$
(37)

$$i_s(t) = i_o(t) + i_{Lm}(t)$$
 (38)

Mode 3: $[t_2 \le t \le t_3]$:

As shown in Figures 17 and 18c, the converter operation in this mode is the same as that in Mode 2 except that i_{Lm} is positive and linearly rising, and once the switch S_5 is turned off with relatively low current, proceeds to Mode 4. During Mode 3, i_{Lm} is linearly falling as in Equation (39):

$$i_{Lm}(t) = (v_{TS}/L_m)t \tag{39}$$

Mode 4: $[t_3 \le t \le t_4]$:

As shown in Figures 17 and 18d, v_{TS} is negative and equal to $-nV_L$, so i_{Lm} is linearly falling. During this blanking time, the magnetizing current i_{Lm} charges the parasitic capacitance of the switch S_5 to double the input voltage V_L and discharges the parasitic capacitance of the switch S_6 to zero. If the body diode of S_6 is conducted, then S_6 can be turned on with ZVS. Once the switch S_6 is turned on, this mode proceeds to Mode 5. During this mode, the calculation for i_{Lm} linearly falling is expressed by Equation (40) as

$$i_{Lm}(t) = i_{Lm}(t_3) - (v_{TS}/L_m)t$$
(40)

Mode 5: $[t_4 \le t_5]$:

As shown in Figures 17 and 18e, v_{TS} is still negative. During this blanking time, the voltage across the switch S_5 is double the input voltage V_L . Since the switch S_6 is turned with ZVS at t_4 , the input voltage V_L is applied to the primary-side winding N_{p2} , and the corresponding duration is about one-half of the switching cycle. During this mode, i_{Lm} is positive and linearly falling, and the power is transferred through the transformer to the DC output on the secondary side. Thus, the voltage across the resonant capacitor C_r called v_{Cr} is expressed by Equation (41), the voltage across the resonant inductor L_r is called v_{Lr} , is expressed by Equation (42), the sinusoidal current i_0 is expressed by Equation (43), and the secondary-side current i_s is expressed by Equation (44). At $t = t_2$, this mode ends $i_{Lm} = 0$, proceeding to Mode 3:

$$v_{Cr}(t) = v_{Cr}(t_4) \cos \omega_r(t - t_4)$$
 (41)

$$v_{Lr}(t) = (-v_{TS} - v_H) - v_{Cr}(t_4) \cos \omega_r(t - t_4)$$
(42)

$$i_{o}(t) = \frac{\left[-v_{TS} - v_{H} - v_{Cr}(t_{4})\right]}{Z_{r}}\sin\omega_{r}(t - t_{4})$$
(43)

$$i_s(t) = i_o(t) + i_{Lm}(t)$$
 (44)

Mode 6: $[t_5 \le t \le t_0 + T_s]$:

As shown in Figures 17 and 18f. The converter operation in this mode is the same as in Mode 5 except that i_{Lm} is negative and linearly falls once the switch S_6 is turned off with

a relatively low current, operating in Mode 1. During this mode, the calculation for i_{Lm} is linearly falling as expressed by Equation (45):

$$i_{Lm}(t) = (-v_{TS}/L_m)t$$
 (45)

3. Design Procedure for Bidirectional Converter

In the designing process for the forward buck-type forward energy-transferring mode, the high-voltage DC bus was defined as the input voltage, and for the boost-type backward energy-transferring mode, the low-voltage DC power supply created by the storage system was defined as the output voltage. Therefore, the first step was the design of the forward buck-type converter, followed by the design of the backward boost-type converter. Finally, the values of the commonly used components of these two modes were adjusted to meet the required specifications for the bidirectional operation.

3.1. Forward Converter Design

3.1.1. Transformer Turns Ratio Determination

The turns ratio of the transformer was calculated when the voltage gain M is 1 under the normal input condition. Therefore, the turns ratio should satisfy the following Equation (46):

$$n = M \times \frac{V_{H_nom}}{V_{L_nom}} \text{ at } M = 1$$
(46)

where V_{H_nom} is the nominal input voltage, and V_{L_nom} is the nominal output voltage.

3.1.2. Magnetizing Inductance L_m Design

Since the switch loss is related to the magnetizing inductance L_m , the larger the magnetizing inductance is, the smaller the on-state loss. In addition to the turn-on loss, the turn-off loss also depends on the turn-off current, which is equal to the magnetizing current i_{Lm} when the switching frequency is less than or equal to the resonance frequency, so a larger excitation inductance L_m can reduce the turn-off loss. In addition, the dead time needs to be increased to ensure ZVS. How to fully discharge the MOSFET's C_{oss} junction capacitance during the dead time to secure ZVS condition is shown in Equation (47), where the magnetizing current i_{Lm} at the end of the dead time is equal to the peak magnetizing current $i_{Lm,peak}$:

$$i_{Lm,peak} \times t_{dead} = 2 \times C_{eq} \times V_{H_nom}$$
(47)

Also, i_{Lm} can be expressed by Equation (48):

$$\dot{i}_{Lm} = \frac{V_{H_nom} \times T}{4 \times L_m} \tag{48}$$

where *T* is the switching period equal to the resonant period, t_{dead} is the time interval under the condition that two switches are both in the off state, C_{eq} is the output capacitance of the MOSFET, and V_{H_nom} is the DC input voltage of the LLC converter. From Equation (48), Equation (49) should be satisfied as

$$L_m < \frac{T \times t_{dead}}{8 \times C_{eq}} \tag{49}$$

3.1.3. Determining Resonant Circuit Equivalent Load Resistance R_{ac}

As the nominal output voltage and load are determined, the equivalent AC load resistance R_{ac} on the secondary side of the transformer is defined in Equation (50) as

$$R_{ac} = 8 \times \left(\frac{n}{\pi}\right)^2 \times \left(\frac{V_{L_nom}}{I_{L_nom}}\right)$$
(50)

3.1.4. Designing Resonant Inductance L_r and Capacitance C_r

To achieve load regulation over the entire operating range, the design must satisfy the values of Q and λ ($\lambda = L_r/L_m$) for the maximum voltage gain. Figure 6 shows that the lower the value of Q is, the higher the maximum voltage gain, whereas in Figure 7, it is evident that the higher the value of λ is, the higher the maximum voltage gain. For a given value of the resonant frequency f_r , increasing λ means decreasing the magnetizing inductance L_m , which increases the circulating current. Therefore, there is a compromise between the range of the available voltage gain and the conduction losses. Once the magnetizing inductance L_m is chosen, the relationship between the values of Q and λ , as defined by Equation (51), can be calculated as

$$\frac{Q}{\lambda} = \frac{2 \times \pi \times f_r}{R_{ac}} \times L_m \tag{51}$$

Therefore, the ratio of Q to λ was also determined for the designed magnetizing inductor L_m . A relatively large λ and a relatively small Q are usually preferred to obtain a relatively wide switching frequency operating range, and a value of λ between 0.25 and 0.1 is usually recommended.

$$L_r = \lambda \times L_m \tag{52}$$

The value of L_r can be obtained based on Equation (52), and substituting this value into Equation (53) obtains the value of C_r as

$$C_r = \frac{1}{\left(2 \times \pi \times f_r\right)^2 \times L_r} \tag{53}$$

The value of Q can be obtained by substituting Equations (50), (52) and (53) into Equation (54) as

$$Q = \frac{\sqrt{L_r/C_r}}{R_{ac}} \tag{54}$$

3.1.5. Transformer T Design

The primary-side and secondary-side turns, because of the output voltage being clamped, can be easily deduced from the primary-side turns N_p as in Equation (55)

$$N_p = \frac{V_{L_nom}}{4 \times f_r \times B_m \times A_e}$$
(55)

where V_{L_nom} is the nominal DC output voltage, B_m is the maximum flux density, and A_e is the magnetic core area.

Since the N_s is the turns ratio n times N_p , based on Equation (56), the turns of N_s can be obtained by

$$N_s = n \times N_p \tag{56}$$

3.2. Backward Converter Design

Because the topology proposed in this paper belongs to the bidirectional DC–DC converter, the circuit operations of the two converters use the same resonant circuit. Thus, the design of the two components should have the same parameters, but because of the different topologies, the design of the component parameters should comply with the established specifications to achieve a compromise in design. Since the detailed design of the forward buck-type LLC resonant converter is already explained, the values of its components have been designed to ensure a wide input voltage range. The following is the parameter design and calculation of a push–pull resonant converter. Since the backward boost-type push–pull resonant converter is mainly operated at the resonant point, the output voltage modulation was controlled by the PWM strategy. The maximum duty cycle,

called D_{max} , was chosen to be less than 0.5, so the turns ratio *n* of the transformer is given in Equation (57):

$$n = \frac{V_{H_nom}}{2 \times V_{L_nom} \times D_{max}}$$
(57)

The backward boost-type push–pull resonant converter is supplied with an appropriate AC resistance after the rectifier, called R_{ac} , at the nominal output voltage and load. This resistance can be defined in Equation (58) as

$$R_{ac} = \frac{8}{\pi^2} \frac{V_{H_nom}}{I_{H_nom}}$$
(58)

In the design procedure, choosing the switching frequency f_s equal to the resonant frequency f_r was adopted. As shown in Figure 16, choosing a smaller Q curve can achieve a smoother curve of the voltage-boosting gain.

Next, the values of the resonant components can be calculated, and hence, the values of L_r and C_r can be solved using Equations (59) and (60)

$$C_r = \frac{1}{2\pi f_r R_{ac} Q} \tag{59}$$

$$L_r = \frac{1}{\left(2\pi f_r\right)^2 C_r} \tag{60}$$

From Equation (58) to (60) mentioned above, the validation of the backward boost-type push–pull converter is similar to that of the forward buck-type LLC converter with respect to important components. Therefore, it can be shown that the same set of components of the resonant circuit can be used for different control methods on different structures of the bidirectional converter.

4. Battery Charge/Discharge Control Method

At present, battery charging methods, including constant-current (CC) mode, constantvoltage (CV) mode, constant-current constant-voltage (CC-CV) mode, and pulse mode, are commonly used. Among these methods, the CC–CV mode is the most preferable. The control framework of the proposed bidirectional LLC full-bridge resonant converter for charging and discharging modes is shown in Figure 19 and consists of two main parts. The first part comprises the power converter based on the full-bridge LLC resonant circuit, whereas the second part is built by the digital control circuit based on the dsPIC microcontroller. The first part was explained in detail earlier, so this section focuses on the design of the digital controller and the software-planning process. For the forward buck-type energy transfer, the voltage and current of the power converter were detected so that a pulse frequency modulation (PFM) signal to control the switching frequency of the switches S_1 to S_4 was created. At the same time, the switches S_5 and S_6 were turned off so that the low-voltage output was rectified by the body diodes of the switches S_5 and S_6 . For the backward boost-type energy transfer, a pulse width modulation (PWM) signal was generated so that the duty cycles of the switching frequency for S_5 and S_6 were controlled. At the same time, the switches S_1 to S_4 were turned off so that the high-voltage output was rectified by the body diodes of the switches S_1 to S_4 .

4.1. Software Planning Process

The MPLAB X IDE v6.00 software planning process is mainly divided into three parts. The first part is the main program shown in Figure 20 as a block diagram. In this part of the code, all the primary system operations and peripheral interfaces were initialized at the beginning. The switching operation of the forward buck charging behavior belongs to the PFM frequency control of the LLC full-bridge converter, which was designed to use one set of PWM1 channels containing two signals, PWM1H and PWM1L. The

PWM1H drives the high-voltage-side switch S_1 of the secondary-side forearm half-bridge leg and the low-voltage-side switch S_4 of the secondary-side rear-arm half-bridge leg. PWM1L drives the low-voltage-side switch S₂ of the secondary-side forearm half-bridge leg and the low-voltage-side switch S_3 of the secondary-side rear-arm half-bridge leg. The backward boost discharge behavior belongs to the PWM duty cycle control for the pushpull converter designed to use one set of PWM3 channels containing two signals, PWM3H and PWM3L, which drives the primary-side switches S_5 and S_6 , respectively. According to the literature [30], since the voltage source is embedded in the DC grid, the converter will be unstable when the converter is controlled under the constant voltage output. Therefore, the discharge mode proposed in this paper sets the battery to be discharged in a constant current mode according to the battery voltage to avoid the battery discharging under a high current at a low state of charge (SOC), resulting in reducing the battery temperature and increasing the battery life. When the converter was operated in the forward buck charging mode, the background loop was used to determine the status of the constant current mode/constant voltage mode and detect the fault status. When the converter was switched to the backward boost discharge mode, the background loop detected the battery voltage to set the reference value for the constant current output and the fault status.



Figure 19. System configuration for the bidirectional LLC full-bridge resonant converter charge/discharge.



Figure 20. Block diagram of the main program.

4.2. Forward Charge Mode

The second part of the code is the flowchart of the CC–CV mode control software for the forward buck LLC full-bridge resonant converter charging mode, as shown in Figure 21. The current sensor measured the battery charging current I_{ch} and subtracted the battery charging current I_{ch} from the reference current I_{ref} to obtain the error value. After this, a proportional integral controller was used to calculate the compensation value for this error, and a PFM signal was obtained from the compensation value to drive the switches S_1 to S_4 to realize constant current charging. When the converter operated in constant current charging mode, the DSP digital control circuit continued to detect the battery voltage. If the battery voltage reached the preset value of the constant voltage mode V_{CVM} , the converter switched to the CV charging mode. Therefore, the voltage sensor measured the battery voltage V_L and obtained an error value by subtracting the battery voltage V_L from the reference voltage V_{ref} . Afterward, a proportional integral controller was used to calculate the compensation value for this error, and a PFM signal was obtained from the compensation value to drive the switches S_1 to S_4 to realize output constant voltage charging. When the converter was switched to CV charging mode, the DSP digital control circuit continued to measure the battery charging current I_{ch} . When the battery charging current was less than or equal to the preset battery cutoff current $I_{cut off}$, the charging process was completed, and the DSP digital control circuit sent a termination signal to the switches S_1 to S_4 to turn off the converter.





4.3. Forward-Mode DSP Control ISR

Figure 22 shows the flowchart of forward-mode DSP control ISR, where "ISR" is an abbreviation of "interrupt service routine". The program entered the ADC interrupt subroutine to obtain information on voltage and current when the interrupt was triggered. Through try and error, the proportional gain k_p and integral gain k_i in the constant voltage mode (CVM) were set at 0.1 and 0.05, respectively, whereas the values of k_p and k_i in the constant current mode (CCM) were set at 0.1 and 0.06, respectively. At the same time, the corresponding periods in CCM and CVM were calculated out and compared together. After this, the period in CVM, called *V_Period*, was compared with the period in CCM, called *I_Period*, and the smaller one was chosen to control the switches S_1 to S_4 .



Figure 22. Flowchart of forward-mode DSP control ISR.

4.4. Backward Discharge Mode

The third part of the code is the flowchart of the CC control software for the backward boost push–pull converter discharging mode, as shown in Figure 23. First, the voltage sensor measured the battery voltage V_L , and the reference discharge current I_{dis_ref} was set according to the battery voltage V_L . At that time, the converter entered the CC mode, the current sensor measured the battery discharge current I_{dis} , and subtracted the reference current I_{dis_ref} from the battery discharge current I_{dis} to obtain the error value. A proportional integral controller was used to calculate the compensation value for this error value, and then the duty cycles of the switching frequency were obtained according to the compensation value to drive the switches S₅ and S₆ to realize constant current discharge. Simultaneously, the DSP digital control circuit detected the battery voltage V_L and then determined whether the battery voltage was less than the battery cutoff voltage V_{cut_off} . If the battery voltage V_L equaled the battery cutoff voltage V_{cut_off} , the discharge process was terminated. In this case, the DSP digital control circuit stopped sending signals to the switches S₅ and S₆, thus stopping the converter and preventing damage to the battery.



Figure 23. Flowchart of battery discharge.

4.5. Backward-Mode DSP Control ISR

Figure 24 shows the flowchart of backward-mode DSP control ISR. The program entered the ADC interrupt subroutine to obtain information on voltage and current when the interrupt was triggered. Via try and error, the proportional gain k_p and integral gain k_i in CCM were set at 0.15 and 0.01, respectively. After this, the duty in CCM, called *I_Duty*, was chosen to control the switches S_5 and S_6 .

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Figure 24. Flowchart of backward-mode DSP control ISR.

5. Experimental Results

First, the operating high-side voltage range of the bidirectional converter was determined to be between 360 V and 410 V for the forward buck mode fed from the high-voltage DC bus, and the low-side voltage range was between 43 V and 52 V for the backward boost mode fed from the low-voltage DC storage source. In this study, a sample 500 W bidirectional full-bridge resonant converter was presented, and its capability of bidirectional power transfer between the low-voltage system and the high-voltage DC bus was verified. The system and component specifications of the converter are listed as described in Table 2.

Parameter	Symbol	Specification
Low-side voltage	V _L	43~52 V
High-side voltage	V _H	360~410 V
Output power	Po	100~500 W
Resonant frequency	fr	125 kHz
PFM switching frequency	F _{llc_s}	96~160 kHz
PWM switching frequency	F _{pp_s}	125 kHz
Duty cycle	D	0.36~0.46
Transformer turns ratio	$N_{p1}:N_{p2}:N_s$	4:4:36
Magnetizing inductance	L _{ms}	586 μH
Leakage inductance	$L_{lk}(L_r)$	114 μH
Resonant capacitance	Cr	14.1 nF
Transformer core	T_1	PC40 (LP2930)
Primary-side switches	S_1, S_2, S_3, S_4	IPP60R120P7
Secondary-side switches	<i>S</i> ₅ , <i>S</i> ₆	IPP200N15N3G
DSP microcontroller	DSP	dsPIC33EP16GS502

Table 2. System specifications and component specifications.

5.1. Instrumentation Configuration

Figure 25 shows the instrumentation configuration for the experimental setup, where High Volt Source (Model: GWINSTEK PSW 800-4.32) supplied the voltage from 360 to 410 V, Low Volt Source (Model: GWINSTEK PSW 80-27) supplied the voltage 43~52 V, DC Electronic Load (Model: Chroma 63308A) provided the output load, and Digital Storage OSC (Model: KEYSIGHT DSOX4024) was used to measure the voltage and current waveforms. Test Board is the proposed prototype circuit. In addition, the measurement condition was that Electronic Load was set at the CV mode for the forward voltage-bucking and backward voltage-boosting operation.



Figure 25. Instrumentation configuration for the experimental setup.

Figure 26 shows the proposed main power stage on the top side and its peripheral circuits, where Aux. Power mainly supplies the operating voltages of the circuit board, such as 12 V for the secondary-side drive circuit, 12 V for the primary-side drive circuit and 5 V for the control board, dsPIC Controller is the control kernel of the circuit operation to measure the voltage and current signals as well as to output the gate driving signals to drive the switches, L_r/T_1 is the transformer which integrates the resonant inductor, S_1 to



 S_4 are the secondary-side switches, S_5 and S_6 are the primary-side switches, V_H is the high voltage output/input, and V_L is the low voltage output/input.

Figure 26. Proposed main power stage on the top side and its peripheral circuits.

Figure 27 shows the proposed main power stage on the bottom side and its peripheral circuits, where Gate Drivers_H and Gate Drivers_L are the individual drive circuits for the secondary-side high-voltage full-bridge switches and the primary-side push-pull switches, C_r is the resonant capacitor, the Volt Sensor is the isolated voltage detector on the secondary side, and the Current Sensor is the current detector on the primary side.



Figure 27. Proposed main power stage on the bottom side and its peripheral circuits.

5.2. Forward Charge Mode

The CC–CV charging mode of the forward buck converter takes a two-stage constant current charging. As shown in Figure 28, the blue color is the constant current charging curve. When the low-side voltage was lower than 46 V, the charging current was a constant current of 5 A. When the low-side voltage exceeded 46 V, the charging current was a constant current of 9.5 A. As shown in Figure 23, the black color is the low-side voltage curve, and the voltage increased with the increase in charging time. When the low-side voltage reached 52 V, it was charged with constant voltage, and the charging current started to decrease.

As shown in Figure 29, the waveforms are measured under a high-side input voltage DC bus of 390 V, the charging current is 5 A, the low-side voltage is 45 V, and the corresponding power was 225 W. The yellow curve is the gate drive signals v_{gs1} and v_{gs4} for the switches S_1 and S_4 , respectively; the green curve is the gate drive signals v_{gs2} and v_{gs3} for the switches S_2 and S_3 , respectively, and the blue curve is the voltage v_2 , which is the

voltage across the switch S_4 , called v_{ds4} . From these waveforms, it can be seen that the switch S_4 had a ZVS turn-on. In addition, the switching frequency f_s operated at 139.3 kHz, larger than the resonance frequency f_r (125 kHz). Accordingly, the resonant inductance current i_{Lr} of the red curve was larger than that of i_{Lm} at the turn-off of the switch S_1 .



Figure 28. Forward charging mode: charging voltage (black) and charging current (blue).



Figure 29. Forward charging mode under output voltage of 44 V and current of 5 A: v_{gs1} and v_{gs4} (yellow); v_{gs2} and v_{gs3} (green); i_{Lr} (red); v_2 (blue).

As shown in Figure 30, the waveforms are measured under a high-side input voltage DC bus of 390 V, the charging current was 9.5 A, the low-side voltage is 48 V, and the corresponding power was 450 W. The yellow curve is the gate drive signals v_{gs1} and v_{gs4} for the switches S_1 and S_4 , respectively; the green curve is the gate drive signals v_{gs2} and v_{gs3} for the switches S_2 and S_3 , respectively, and the blue curve is the voltage v_2 , which is the voltage across the switch S_4 , called v_{ds4} . From these waveforms, it can be seen that the switch S_4 had a ZVS turn-on. In addition, the switching frequency f_s operated at 110.3 kHz, which is lower than the resonance frequency f_r (125 kHz). Accordingly, the resonant inductance current i_{Lr} of the red curve was larger than that of i_{Lm} at the turn-off of the switch S_1 .



Figure 30. Forward power flow under output voltage of 48 V and current of 9.5 A: v_{gs1} and v_{gs4} (yellow); v_{gs2} and v_{gs3} (green); i_{Lr} (red); v_2 (blue).

As shown in Figure 31, the efficiency curve of the CC–CV charging mode obtained from the forward buck converter, the red curve shows that the efficiency of the CC charging mode was maintained above 95%, where the output power locates between 215 W and 235 W in the first stage of 5 A charging, and the output power locates between 460 W and 500 W in the second stage of 9.5 A charging. On the other hand, the blue curve shows that the efficiency of the CV charging mode was initially maintained above 95%, drops with the decrease of the output power, and finally drops to 88% when the output power was 100 W.



Figure 31. Efficiency for forward power flow: CC mode (red); CV mode (blue).

5.3. Backward Discharge Mode

The CC discharge mode of the backward boost converter takes constant current discharge when the low-side source is discharged. As shown in Figure 32, the blue color is the CC discharge curve. When the low-side voltage exceeded 47 V, the low-side source was discharged at a constant current of 9.6 A to the high-voltage DC bus. When the low-side source voltage was between 47 V and 46 V, the low-side source was discharged at a constant current of 6 A to the high-voltage DC bus. When the low-side source voltage was between 46 V and 44.5 V, the low-side source was discharged at a constant current of 4 A to the high-voltage DC bus. When the low-side source voltage DC bus. When the low-side source voltage DC bus. When the low-side source voltage at a constant current of 4 A to the high-voltage DC bus. When the low-side source voltage DC bus. As shown in Figure 27, the black color is the curve of the low-side source voltage, and this voltage decreases as the discharge time increases.



Figure 32. Backward power flow: discharging voltage (black); discharging current (blue).

As shown in Figure 33, the high-side output voltage DC bus was 408 V and 493 W, the input constant current of the converter was 9.65 A, and the low-side source voltage was 51 V. The yellow curve is the gate driving signal v_{gs5} for the switch S_5 , and the green curve is the voltage across the switch S_5 , called v_{ds5} . The blue curve is the voltage v_1 , the input voltage of the full-bridge rectifier on the high-voltage side. This figure shows that the switch S_5 had a ZVS turn-on, and the PWM switching frequency was 125 kHz with a duty cycle of 0.43.



Figure 33. Backward power flow: under low-side source voltage of 51 V and current of 9.5 A: v_{gs5} (yellow); v_{ds5} (green); i_{s5} and i_{s6} (red); v_1 (blue).

As shown in Figure 34, the high-side output voltage DC bus was 360 V, the power was 170 W, the input constant current of the converter was 4 A, and the low-side source voltage was 44.5 V. The yellow curve is the gate drive signal v_{gs5} for the switch S_5 , and the green curve is the voltage across the switch S_5 , called v_{ds5} . The blue curve is the voltage v_1 , which is the input voltage of the full-bridge rectifier on the high-voltage side. This figure shows that the switch S_5 had a ZVS turn-on, and the PWM switching frequency was 125 kHz with a duty cycle of 0.36.



Figure 34. Backward power flow under input voltage 44.5 V and current 4 A: v_{gs5} (yellow) and v_{ds5} (green); i_{s5} and i_{s6} (red); v_1 (blue).

Figure 35 shows the efficiency curve of the CC discharge for the backward boost converter, where the red curve for the efficiency under the CC discharge mode initially maintains more than 95%. The discharge current was determined by the low-side source voltage, and the corresponding output power was concentrated in 450~500 W, 180 W, and 80 W, as shown by blue color. However, the efficiency was reduced to 88% at the output power of 100 W.



Figure 35. Efficiency for backward power flow: CC mode (red).

5.4. Experimental Summarization

The experimental method adopts CC and CV mode control for forward buck-type energy transfer on the low-voltage side and the CC mode control for boost-type energy transfer on the low-voltage side. Stepwise segmented current charging and discharging techniques are adopted to avoid battery temperature rise caused by high power charging and discharging at low battery capacity, and this will reduce the battery life.

6. Conclusions

This paper proposed a bidirectional control strategy, which performs the bidirectional energy transfer function without changing the topology of the LLC resonant converter. The conventional PFM switching technique was used to control the full-bridge LLC switches for forward buck mode. The push–pull switches were controlled by the PWM switching technique with a variable duty cycle for backward boost mode. The proposed system utilized the resonant tank on the high-side voltage for bidirectional energy transfer, with ZVS on both the input switches and used the battery as the main target in the control strategy. When the battery was charged, there were three charging stages, and when the battery was discharged, the discharge control method was based on the stored energy of the battery (SOC). That is, the battery was discharged with low current at a low voltage to prolong the life of the battery, as well as to minimize temperature rise and internal solid electrolyte interphase (SEI). Furthermore, as compared with Table 1, the proposed converter had an input voltage range of 43–52 V, an output voltage range of 360–410 V, an output power of 500 W, and a maximum efficiency of 95.1%. We used LLC topology, adopted the PFM/PWM control technique, six main switches, and the number of inductors/transformers/capacitors was one each. Accordingly, the proposed control strategy can achieve wide input and output ranges with relatively few components.

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