





## Article

# A Three-Phase Phase-Modular Single-Ended Primary-Inductance Converter Rectifier Operating in Discontinuous Conduction Mode for Small-Scale Wind Turbine Applications

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**Abstract:** Small-scale wind turbines play an important role in distributed generation since customers can use their houses, farms, and business to produce electric energy. The development of the power electronics system that processes the electric energy from small-scale wind turbines is a concern due to cost, simplicity, efficiency, and performance trade-offs. This paper presents the results of applying a three-phase phase-modular single-ended primary-inductance converter rectifier to processing the energy of a small-scale wind turbine system. The rectifier was designed according to the specifications of a commercial small-scale wind turbine system and tested in an emulator workbench, providing experimental data on the operation of the rectifier in this application. The rectifier can process the energy of a non-sinusoidal three-phase system since the permanent magnet synchronous generator has trapezoidal waveforms. The results show that the rectifier has the advantages of (i) using the inductance of the generator as the input filter inductor of the rectifier, (ii) providing input currents with the same shape as the voltages and in phase without the use of a current control system, (iii) simplicity of control of the DC output voltage and PWM modulation, and (iv) phase-modular characteristics that allow operating with phase fault without any additional control techniques. Due to the operation in discontinuous conduction mode, low efficiency in high power and/or low input voltage specifications are disadvantages.

**Keywords:** wind energy; wind turbine; power factor correction rectifiers; single-ended primary-inductance converter; discontinuous conduction mode



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## 1. Introduction

Renewable energy sources are a sustainable solution for increasing electric energy generation worldwide. The field of 100% renewable energy (RE) systems research proposes that this can be achieved entirely using renewable sources, not only for the electricity sector but for all energy and non-energy industries [1].

Wind energy has become an essential part of human life worldwide and has undergone substantial development in different areas in recent decades [2]. Onshore wind power in particular plays a pivotal role in modern power systems due to its low costs [3]. In small-scale generation, customers can use their houses, farms, and business to produce electric energy, reducing tariffs and contributing to integrated grids and the environment [4–6].

Most studies and commercially available small wind turbines (SWTs) are based on permanent magnet synchronous generators (PMSG) [7–9]. Small-scale wind turbines operate with variable speed, and the grid connection is made through static power converters with system control to maximize the power generated and decrease harmonics on the grid while using simple, low-cost, and robust solutions [10–22].

The energy electronic processing from wind turbines is generally carried out using a two-stage approach: the first stage is realized by an AC–DC converter (rectifier) and the second stage is performed by a DC–AC converter (inverter) [23].

Regarding the rectifier stage, two types are widely employed: diode bridge rectifiers and pulse width modulated (PWM) rectifiers. Diode bridge rectifiers are low-cost, simple, and robust solutions. However, they present a low power factor because they drain currents with high harmonic content [24]. Specifically, in the application of rectifiers for processing the energy of small-scale wind turbines, the harmonic components of the current will produce parasitic torques in the generator. Therefore, the losses and the temperature in the generator will increase, decreasing the overall efficiency.

PWM rectifiers allow sinusoidal currents in wind turbines and maximum power tracking for different wind speeds. A classic solution in this conversion system is with boost rectifier topologies that need an output voltage higher than the input voltage for proper operation [24,25]. However, generator voltage depends on wind speed, which can be a limiter [26]. Moreover, a current control system must be implemented in each rectifier phase to achieve a high power factor, increasing the cost and complexity through voltage and current sensors.

The utilization of topologies based on single-ended primary-inductance converter (SEPIC) rectifiers allows operation as a step down/up rectifier. Moreover, when operating in discontinuous conduction mode (DCM), SEPIC rectifiers can naturally provide a high power factor without a current control system [27]. This characteristic can maximize the power extracted by the SWT, mainly in low-wind speed operation [28].

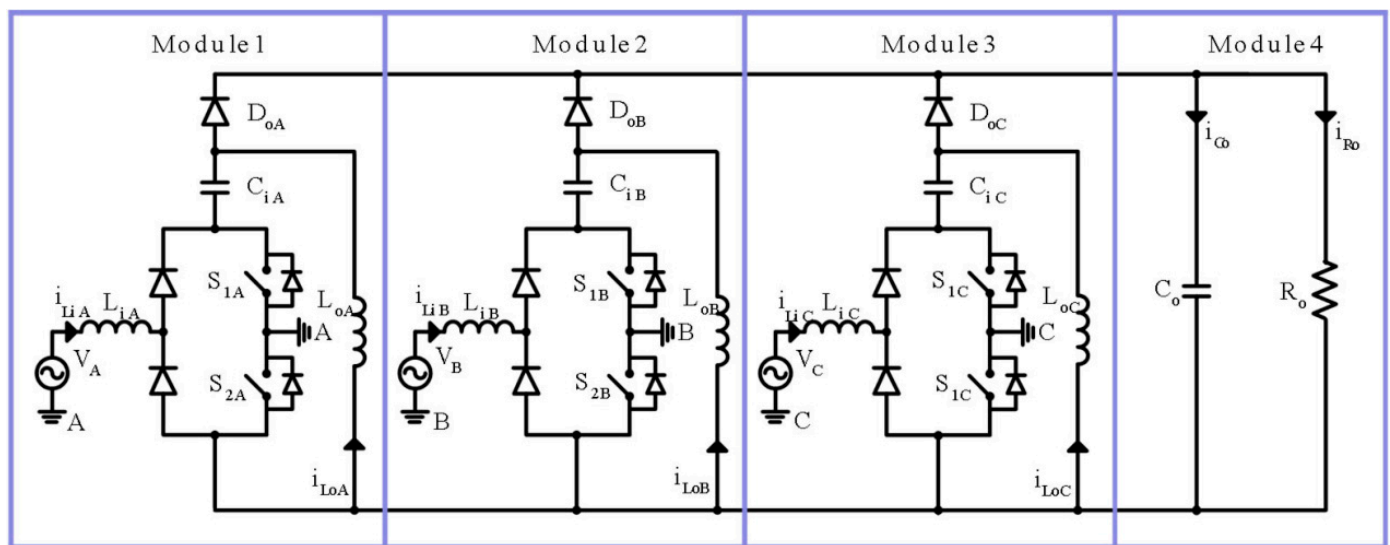
This paper proposes a three-phase phase-modular SEPIC rectifier operating in DCM for processing energy in small-scale wind turbine applications. This rectifier was first presented in ref. [28], in which the rectifier was tested with an AC power source at input, and the high power factor corrector capability was verified. The contributions of this paper with regard to previous studies are as follows:

- Theoretical analysis to obtain the dynamic model for output voltage control;
- Experimental analysis of the rectifier processing the energy from a small-scale wind turbine emulator workbench;
- Efficiency analysis.

First, the rectifier topology and theoretical analysis are presented in Section 2, with the discussion of two modulation strategies. Section 3 presents the main design equations for the power stage and losses calculation. Section 4 presents the control and dynamic model for controlling the DC output voltage. The prototype assembly and the experimental results are presented in Section 5. Finally, the conclusions are stated in Section 6.

## 2. Theoretical Analysis

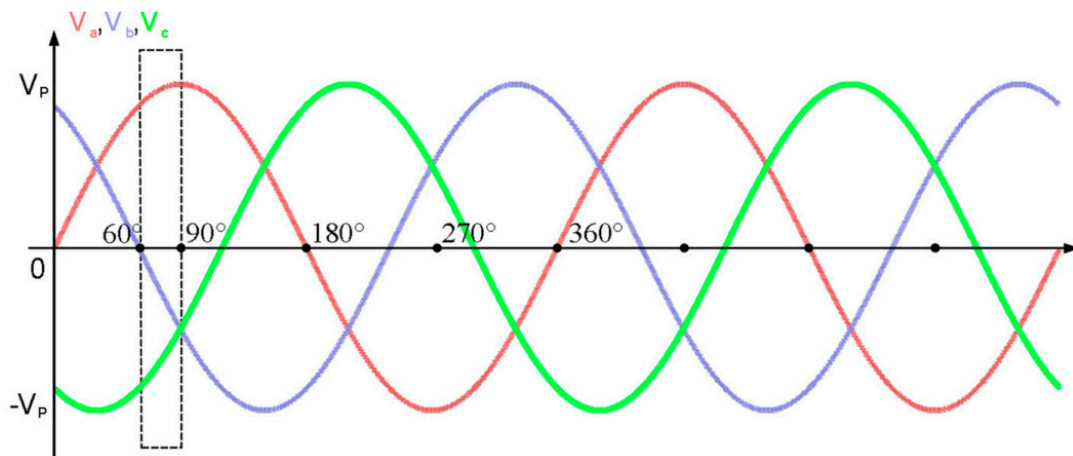
The phase-modular SEPIC rectifier with two switches per module is presented in Figure 1. The rectifier is connected to a six-wire three-phase grid obtained through a PMSG with open-end stator windings. In this application, the SEPIC rectifier input inductances ( $L_{iA}$ ,  $L_{iB}$  and  $L_{iC}$ ) can be eliminated, and stator inductances can be used as rectifier input inductances.



**Figure 1.** Three-phase phase-modular single-ended primary-inductance converter (SEPIC) rectifier.

When operating in DCM, this rectifier has input currents naturally in phase with the input voltages in a way that does not require the use of a current control system [29,30] to achieve a high power factor. As a result of modular characteristics, the three-phase rectifier can be analyzed and designed as three independent modules (single-phase), each responsible for a third of the output power. To perform theoretical analysis, we considered the input voltage interval of  $60^\circ < \omega t < 90^\circ$ , as depicted in Figure 2. Consequently, the input voltages satisfy the inequality shown in Equation (1):

$$|V_A| > |V_B| > |V_C| \quad (1)$$



**Figure 2.** Section used for theoretical analysis.

### 2.1. PWM Techniques for the Three-Phase SEPIC Rectifier

Since the rectifier structure for each phase is realized with a bridgeless implementation, the modulation scheme can be performed in two different approaches. The three-phase rectifier modulated with conventional modulation presents the same command signal for both transistors, as represented in Figure 3.

The alternative modulation proposed in [31] aims to reduce the losses by not conducting diodes in anti-parallel transistors. Figure 4 represents the command signals profile, where in the positive semi-cycle, the superior transistor is switched following the modulator comparison while the inferior transistor is turned on; the opposite occurs for the negative semi-cycle. Figure 5 shows a circuit for the implementation of alternative modulation. It

is important to highlight that the alternative modulation must be synchronized with the input voltage of each phase. Therefore, it requires extra voltage sensors and the use of a phase-locked loop (PLL) circuit for synchronization.

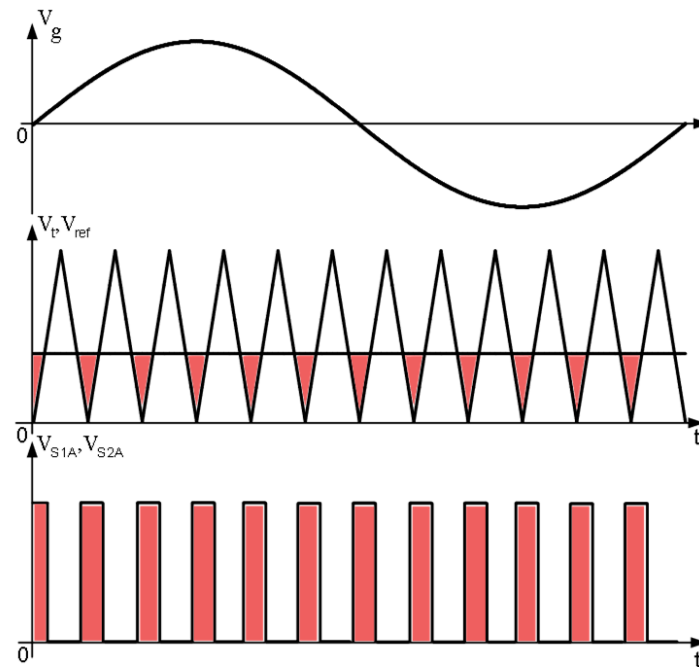


Figure 3. Conventional modulation waveforms.

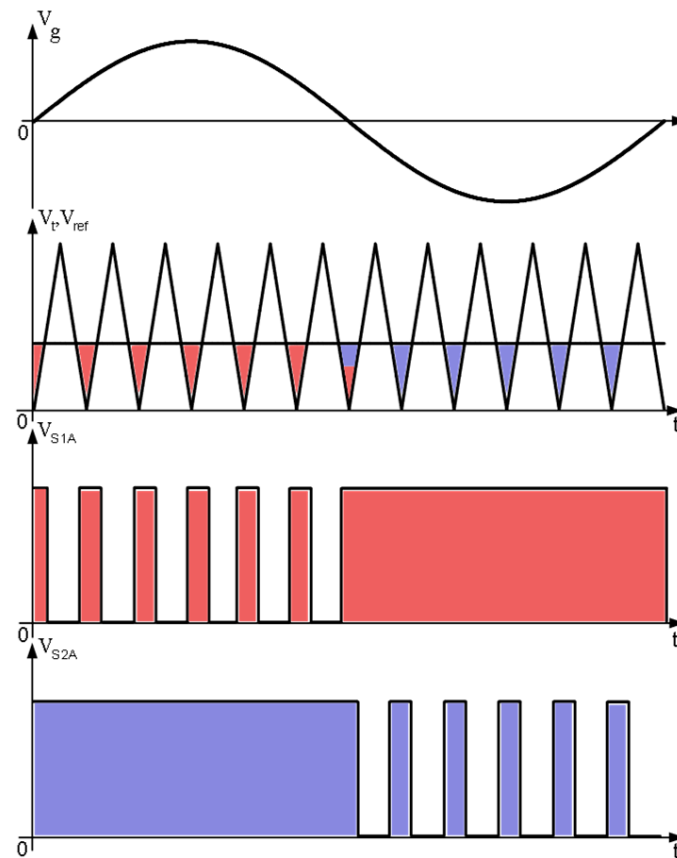
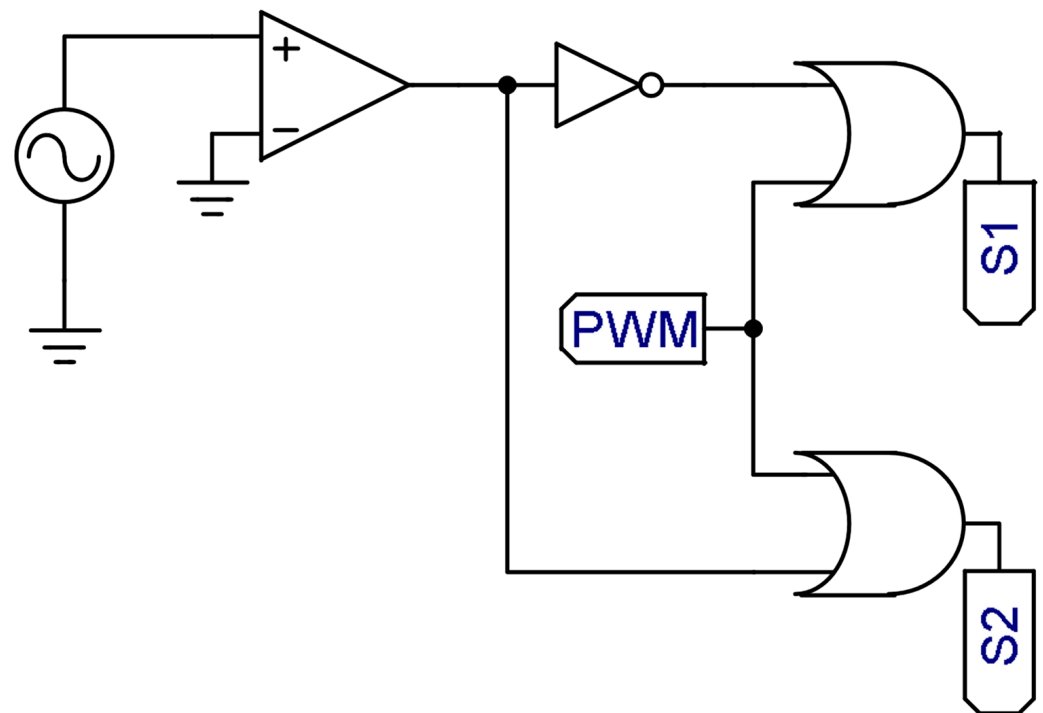


Figure 4. Alternative modulation waveforms.



**Figure 5.** Circuit implementation for alternative modulation.

## 2.2. Stages of Operation

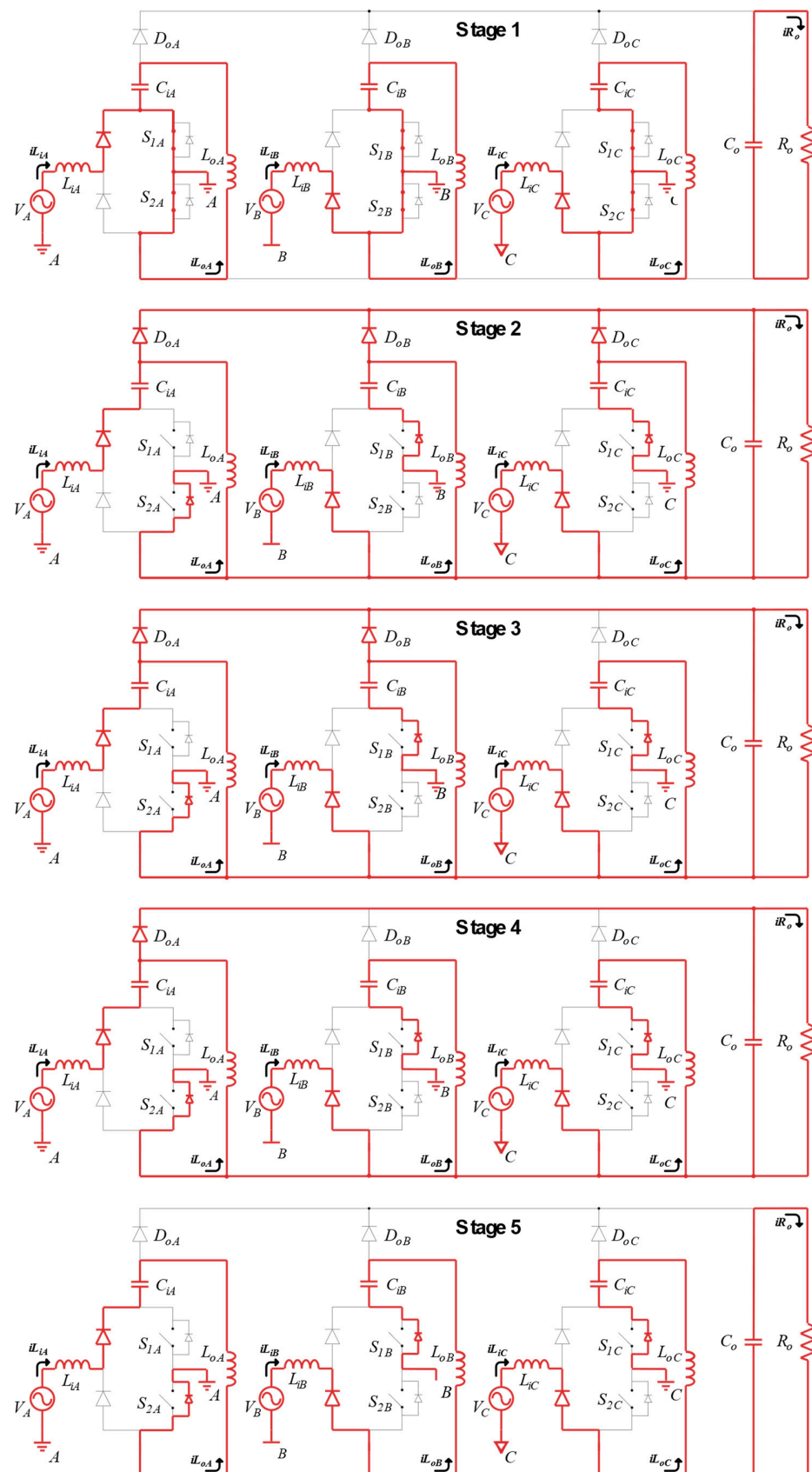
When operating with conventional PWM modulation, the SEPIC rectifier simultaneously presents the same command signal for all transistors. In DCM, the converter has five stages of operation, as seen in Figure 6.

During the first stage of operation, all transistors are turned on, and output diodes are blocked. The inductor currents increase according to the following relations:  $V_A/L_{iA}$ ,  $V_B/L_{iB}$ ,  $V_C/L_{iC}$ ,  $V_A/L_{oA}$ ,  $V_B/L_{oB}$ ,  $V_C/L_{oC}$ . Meanwhile, the load is fed by capacitor  $C_o$ .

The second stage of operation starts when all transistors are turned off. At this moment, the output diodes come into conduction, transferring the inductors' storage energy to the load  $R_o$ . At the input, current circulates through the anti-parallel diode according to the semi-cycle of input voltage at each moment. The inductor currents decrease according to the following relations:  $-V_o/L_{iA}$ ,  $-V_o/L_{iB}$ ,  $-V_o/L_{iC}$ ,  $-V_o/L_{oA}$ ,  $-V_o/L_{oB}$ ,  $-V_o/L_{oC}$ .

When considering the input voltage interval  $60^\circ < \omega t < 90^\circ$ , the amplitude of each AC input voltage differs, and the storage energy on the passive elements of each module is also different. Therefore, the end of the energy transfer process of each module occurs at different times. Since the amplitude of AC voltage  $V_C$  is smaller, the output diode of the third phase will be the first to stop conducting, as represented in the third stage of operation.

The fourth stage of operation starts when diode  $D_{oB}$  blocks, and then the second module stops energy transfer to load  $R_o$  and to capacitor  $C_o$ . The fifth and last stage starts when diode  $D_{oA}$  blocks, and the third module stops energy transfer to output. The capacitor  $C_o$  feeds the load  $R_o$ . The fifth stage indicates DCM since all semiconductors are blocked.



**Figure 6.** Operation Stages for SEPIC rectifier (the electronic components have the following abbreviations: V: voltage sources, L: inductors, C: capacitors, D: diodes, S: transistors, and R: resistors).

### 2.3. Ideal Waveforms

The ideal waveforms based on the operation stages section are illustrated in Figure 7, which shows the current and voltage waveforms on the transistors ( $S_{1A}$ ,  $S_{1B}$ ,  $S_{1C}$ ,  $S_{2A}$ ,  $S_{2B}$ ,  $S_{2C}$ ), currents and voltages on the output diodes ( $D_{oA}$ ,  $D_{oB}$ ,  $D_{oC}$ ), and the command signal for the transistors.

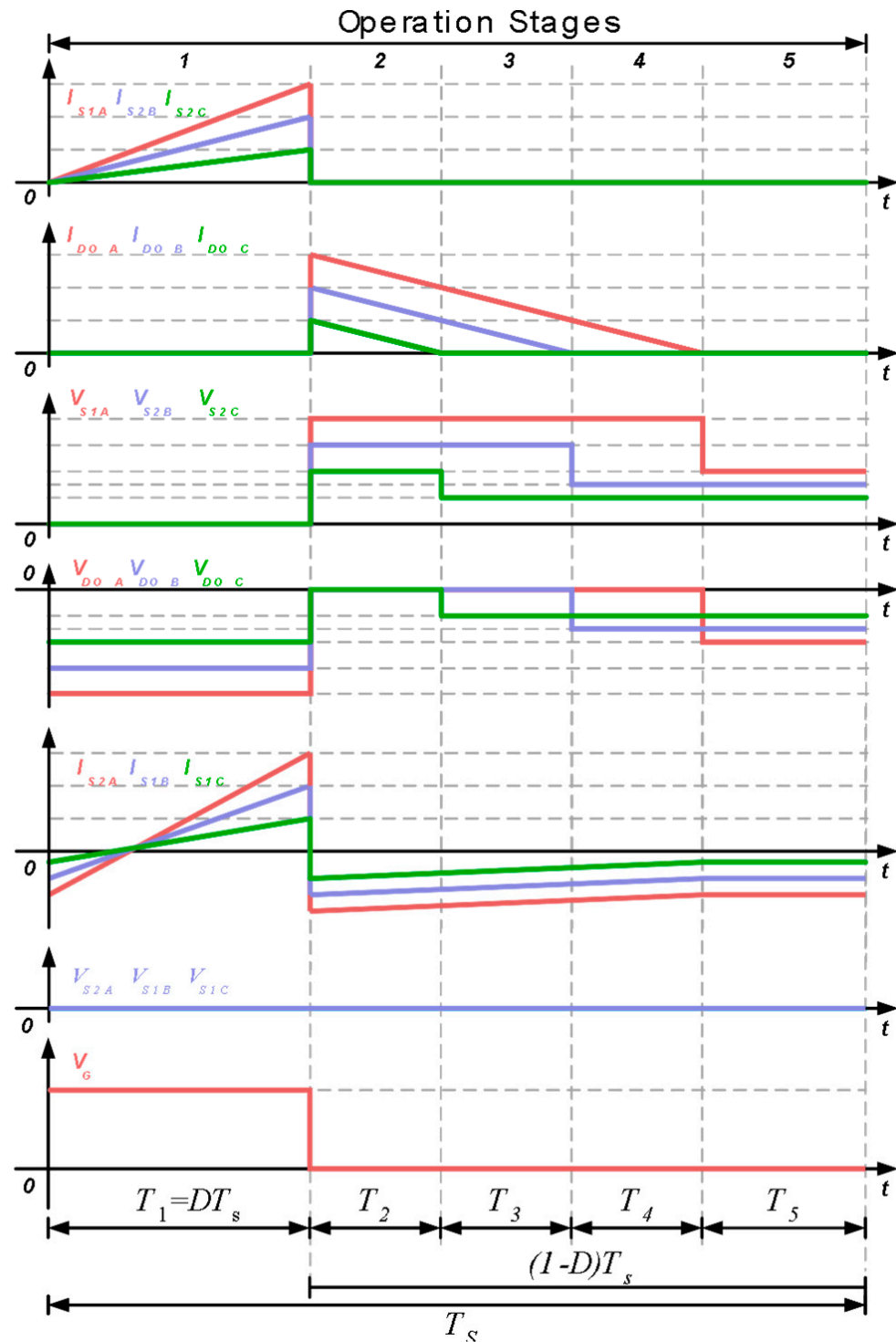


Figure 7. Ideal waveforms based on operation stages section.



### 3. Design Equations and Losses Calculation

The main equations for the power circuit design are shown below [28]. Moreover, the losses calculation in each component is presented.

#### 3.1. Inductor Design

Equations (2) and (3), respectively, are inductance values for the input and output inductors in each module. Output inductors are designed from values of input inductors, which, in turn, are calculated from a current ripple specification, ensuring the DCM operation.

$$L_i = \frac{V_p D}{\Delta I_{Li} f_s} \quad (2)$$

$$L_o = \frac{L_i R_o V_p^2 D^2}{4 L_i V_o^2 f_s - R_o V_p^2 D^2} \quad (3)$$

The root mean square (rms) input current value and the average and rms output current values on inductors are shown in Equations (4)–(6), respectively.

$$I_{Li_{rms}} = \frac{\sqrt{6}}{24} \sqrt{\frac{D^3 V_p^2 [12 V_o^2 L_i D (L_i + 2 L_o) + L_o^2 (16 V_o^2 - 9 V_p^2 D^2)]}{V_o^2 L_i^2 L_o^2 f_s^2}} \quad (4)$$

$$I_{Lo_{avg}} = \frac{D^2 V_p^2 (L_i + L_o)}{4 V_o L_i L_o f_s} \quad (5)$$

$$I_{Lo_{rms}} = \frac{1}{24} \sqrt{\frac{2 D^3 V_p [V_p V_o L_i^2 (128 - 192 D) + V_p^2 L_o D \pi (54 L_i - 27 L_o) + V_o^2 L_i^2 \pi (48 - 36 D)]}{\pi V_o^2 L_i^2 L_o^2 f_s^2}} \quad (6)$$

#### 3.2. Capacitor Design

Equations (7) and (8) show input and output capacitance values, respectively. Input capacitors are designed from a voltage ripple specification, while the capacitor  $C_o$  is designed from a specification of hold-up time ( $t_{hold}$ ).

$$C_i = \frac{D^2 V_p [D (V_p L_o - V_o L_i) + 2 V_o L_i]^2}{8 V_o^2 L_i^2 L_o \Delta V_{Ci} f_s^2} \quad (7)$$

$$C_o = \frac{2 P_o t_{hold}}{V_o^2 - (0.9 V_o)^2} \quad (8)$$

#### 3.3. Semiconductor Design

The maximum voltage, maximum current, average current, and rms current values on transistors are given by Equations (9)–(12), respectively:

$$V_{S_{max}} = V_p + V_o \quad (9)$$

$$I_{S_{max}} = \frac{D V_p (L_i + L_o)}{L_i L_o f_s} \quad (10)$$

$$I_{S_{avg}} = \frac{D^2 V_p [4 V_o L_i (4 - D) + L_o (V_p D \pi + 8 V_o)]}{16 \pi V_o L_i L_o f_s} \quad (11)$$



$$I_{S_{rms}} = V_p \sqrt{\frac{V_o D^3}{\pi} \frac{3\pi V_o [L_o^2(16 - 9D) + 4L_i^2(8 - 3D) + 32L_i L_o] + 2V_p(64L_o^2 + 96L_i L_o)}{24V_o L_i L_o f_s}}, \quad (12)$$

while the maximum voltage across output diodes is given by Equation (13):

$$V_{Do_{max}} = V_p + V_o \quad (13)$$

The maximum, average, and rms current values on output diodes are shown in Equations (14)–(16), respectively.

$$I_{Do_{max}} = \frac{DV_p(L_i + L_o)}{L_i L_o f_s} \quad (14)$$

$$I_{Do_{avg}} = \frac{D^2 V_p^2 (L_i + L_o)}{4V_o L_i L_o f_s} \quad (15)$$

$$I_{Do_{rms}} = \frac{2DV_p(L_i + L_o)}{3L_i L_o f_s} \sqrt{\frac{DV_p}{\pi V_o}} \quad (16)$$

The maximum voltage and average current values for the rectifier diodes are shown in Equations (17) and (18), respectively.

$$V_{Dr_{max}} = V_p + V_o \quad (17)$$

$$I_{Dr_{avg}} = \frac{D^2 V_p (L_i + L_o)}{2\pi L_i L_o f_s} \quad (18)$$

### 3.4. Losses Calculation

The losses calculation approach in this paper considers the losses in transistors, diodes, and inductors. The transistor losses can be calculated using Equation (19), where  $R_{DSon}$  is the conduction resistance,  $t_f$  is the fall time, and  $t_r$  is the rise time.

$$P_{S_{losses}} = R_{DSon} \cdot I_{S_{rms}}^2 + \frac{f_s}{2} \cdot (t_f + t_r) \cdot I_{S_{max}} \cdot V_{S_{max}} \quad (19)$$

The diode losses can be calculated using Equation (20), where  $V_F$  is the forward diode voltage for the output and rectifier diodes.

$$P_{Do, r_{losses}} = V_F \cdot I_{Do, r_{avg}} \quad (20)$$

The losses in inductors are estimated from copper losses and magnetic core losses as presented in Equation (21), where  $l_w$  is the wire length,  $\rho_c$  is the copper resistivity,  $S_w$  is the wire cross-sectional area,  $B_{max}$  is the maximum flux density,  $V_n$  is the core volume, and  $a$ ,  $b$ , and  $c$  are constants of magnetic material.

$$P_{Li, o_{losses}} = \frac{\rho_c \cdot l_w}{S_w} \cdot I_{Li, o_{rms}}^2 + B_{max}^a \cdot V_n \cdot (b \cdot f_s + c \cdot f_s^2) \quad (21)$$

The total losses in the rectifier can be estimated using Equation (22):

$$P_{losses} = 6 \cdot P_{S_{losses}} + 3 \cdot P_{Do_{losses}} + 6 \cdot P_{Dr_{losses}} + 3 \cdot P_{Li_{losses}} + 3 \cdot P_{Lo_{losses}} \quad (22)$$

Finally, the efficiency is estimated using Equation (23):

$$\eta = \frac{P_o}{P_o + P_{losses}} \quad (23)$$

#### 4. Control and Dynamic Model

The control and modulation strategy are shown in Figure 8 through a block diagram. As the rectifier operates in DCM, it emulates a resistance for the input (e.g., for the PMSG). Consequently, the input currents have the exact shape of the respective input voltages without the necessity of a current control system. The control system is thus composed of a single voltage control system for controlling the DC output voltage.

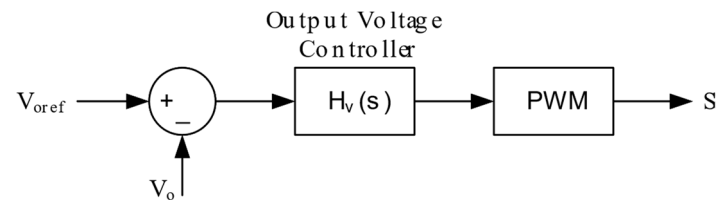


Figure 8. Block diagram of control system.

The PWM modulator is implemented with a saw-tooth signal, performing a trailing edge modulation. Each transistor is commanded with the same command signal, implementing a simple command circuit.

##### 4.1. Determination of Dynamic Model

To obtain the small-signal model for the control of the rectifier's output voltage, the equivalent circuit shown in Figure 9 is considered [32]. The current  $i_o(t)$  is composed of the sum of the output currents of each module, as shown in Equation (24):

$$\langle i_o(t) \rangle_{T_s} = \langle i_{DoA}(t) \rangle_{T_s} + \langle i_{DoB}(t) \rangle_{T_s} + \langle i_{DoC}(t) \rangle_{T_s} \quad (24)$$

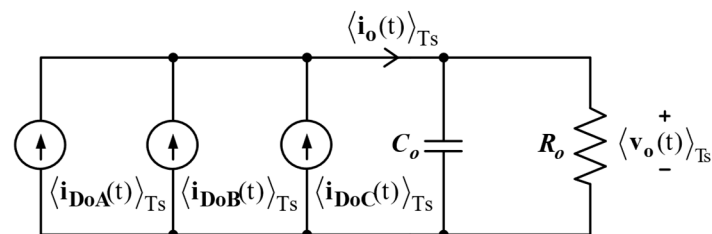


Figure 9. Equivalent circuit for three-phase SEPIC rectifier.

The following differential equation, which describes the dynamic output voltage behavior, is obtained through the circuit analysis from the equivalent circuit depicted in Figure 9:

$$\langle i_o(t) \rangle_{T_s} = C_o \frac{d\langle v_o(t) \rangle_{T_s}}{dt} + \frac{\langle v_o(t) \rangle_{T_s}}{R_o} \quad (25)$$

For the linearization process, each variable in Equations (24) and (25) is rewritten as the sum of a constant value and a small-signal variable. The constant value represents the operation point (steady-state value), and the small-signal variable represents a perturbation around the operation point and is denoted by a  $\hat{\phantom{x}}$  mark on the variable. Therefore, it yields the following:

$$\begin{aligned} \langle i_o(t) \rangle_{T_s} &= I_o + \hat{i}_o(t) \\ \langle v_o(t) \rangle_{T_s} &= V_o + \hat{v}_o(t) \end{aligned} \quad (26)$$

For the operation point, it yields Equation (27):

$$I_o = C_o \frac{dV_o}{dt} + \frac{V_o}{R_o} \rightarrow I_o = \frac{V_o^2}{R_o} \quad (27)$$

Replacing Equations (26) and (27) with Equation (25), we obtain Equation (28):

$$\hat{i}_o(t) = C_o \frac{d\hat{v}_o(t)}{dt} + \frac{\hat{v}_o(t)}{R_o} \quad (28)$$

The average value of the output current can also be written in the form of Equation (29):

$$\langle i_o(t) \rangle_{T_s} = \frac{3d(t)^2 V_p^2 (L_i + L_o)}{4 \langle v_o(t) \rangle_{T_s} L_i L_o f_s} \quad (29)$$

It is observed in this expression that the current value  $i_o(t)$  suffers variation when the duty cycle is changed. Therefore, any variation in the duty cycle also causes output voltage variation, causing a change in the current value. Consequently, applying a perturbation on duty cycle  $d(t)$  leads to a direct and indirect variation in the current  $i_o(t)$ . The direct variation is generated by duty cycle alteration, while the indirect one is generated by output voltage variation. Thus, the current alteration for a specific duty cycle perturbation can be expressed as partial functions as shown in Equation (30):

$$\hat{i}_o(t) = \frac{\partial \langle i_o(t) \rangle_{T_s}}{\partial d(t)} \hat{d}(t) + \frac{\partial \langle i_o(t) \rangle_{T_s}}{\partial \langle v_o(t) \rangle_{T_s}} \hat{v}_o(t) \quad (30)$$

Solving Equation (30), Equation (31) is obtained:

$$\hat{i}_o(t) = \frac{3DV_p^2(L_i + L_o)}{2V_o L_i L_o f_s} \hat{d}(t) - \frac{3D^2 V_p^2 (L_i + L_o)}{4V_o^2 L_i L_o f_s} \hat{v}_o(t) \quad (31)$$

Equating Equations (28) and (31) and applying the Laplace transform to the result of equality, the dynamic model represented by the transfer function for the small signal is obtained, as can be seen in Equation (32):

$$G(s) = \frac{\hat{v}_o(s)}{\hat{d}(s)} = \frac{\frac{3R_o D V_p^2 (L_i + L_o)}{2V_o L_i L_o f_s}}{R_o C_o s + \frac{3R_o D^2 V_p^2 (L_i + L_o)}{4V_o^2 L_i L_o f_s} + 1} \quad (32)$$

#### 4.2. Transfer Function Validation

To validate the transfer function shown in Equation (32), a numeric simulation was performed using the values of the design specifications listed in Table 1 and the values of passive components listed in Table 2. The result obtained by applying negative and positive steps on the duty cycle of 2% of its nominal value is shown in Figure 10, where it is compared with the circuit simulation result for the output voltage. Such a comparison highlights the similarity between the simulated rectifier dynamic response and the small-signal dynamic model response. Therefore, it is possible to use this model to represent the dynamic behavior of the output voltage of the rectifier.

**Table 1.** Design specifications.

Specification	Value
Output power ( $P_o$ )	1500 W
Input voltage ( $V_{inRMS}$ )	90 V
Output voltage ( $V_o$ )	250 V
Maximum duty cycle ( $D$ )	0.55
Switching frequency ( $f_s$ )	25 kHz
Ripple voltage in capacitors ( $\Delta V_{Ci}$ )	28.5%
Ripple current in input inductors ( $\Delta i_{Li}$ )	12%
Hold-up time ( $t_{hold}$ )	8 ms

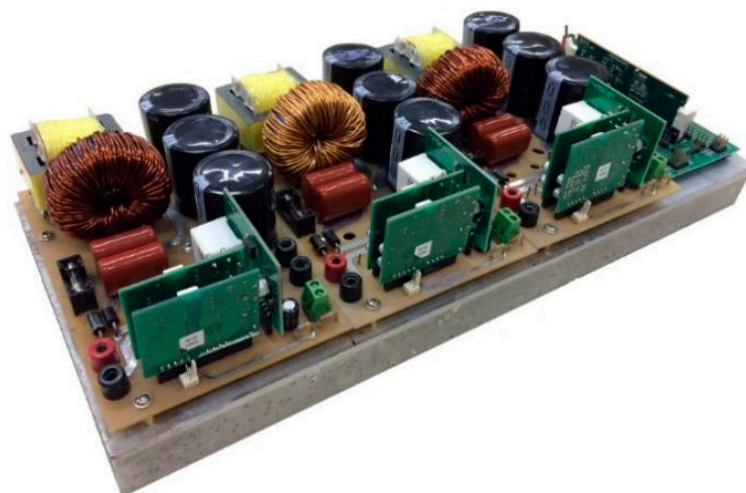
**Table 2.** List of components.

Specification	Value
Transistors	SPW47N60C3 (650 V/47 A)
Rectifier diodes	1N5408 (1000 V/3 A)
Output diodes	MUR860 (600 V/15 A)
Input inductors	Inductance: 2.916 mH
	Number of turns: 144
	Wire conductor: 16 AWG
	Toroidal core: APH46P60
Output inductors	Inductance: 101.412 $\mu$ H
	Number of turns: 29
	Wire conductor: 64 $\times$ 32 AWG
	EE core: EE42/21/15 3C90
Input capacitors	2 $\times$ 2.2 $\mu$ F/250 V
Output capacitor	3 $\times$ 470 $\mu$ F/400 V

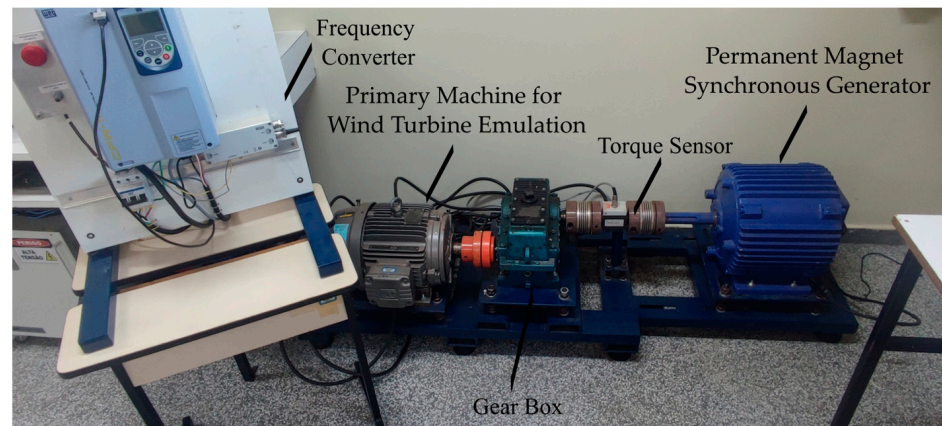
**Figure 10.** Dynamic responses of rectifier output voltage (red) and small-signal model (blue) for a step of 2% in duty cycle.

## 5. Prototype and Experimental Results

In order to demonstrate the experimental operation of the SEPIC rectifier, a proof-of-concept prototype was built with 1500 W of rated power. The other design specifications are shown in Table 1. A photograph of the prototype is presented in Figure 11, and the bill of components is presented in Table 2.

**Figure 11.** Prototype of SEPIC rectifier with the phase-modular concept.

The experimental results were obtained from a small-scale wind turbine emulator workbench built with a frequency converter, a permanent magnet synchronous motor as a primary machine, a gear box, a torque sensor, and a permanent magnet synchronous generator. A picture of the workbench can be seen in Figure 12.

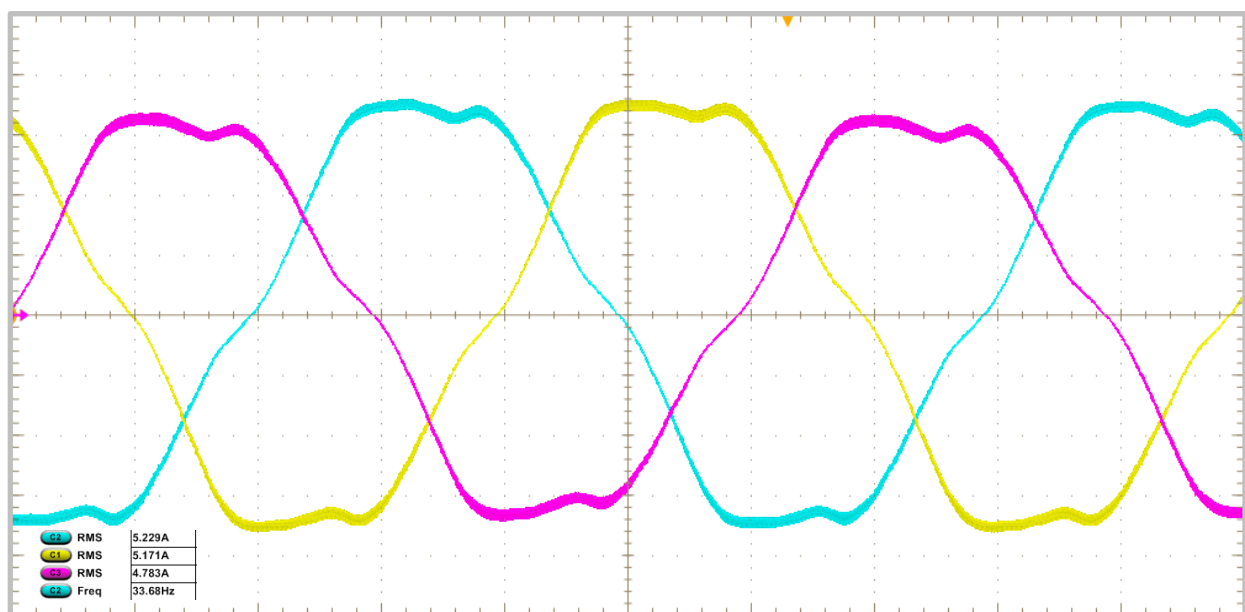


**Figure 12.** Small-scale wind turbine emulator workbench.

The workbench can operate with maximum values of 3 kW of rated power, 12 m/s of rated wind speed, and 350 rpm of rated angular speed. The permanent magnet synchronous generator has 3 kW of rated power, 90 V of rated voltage, 30 Hz of rated frequency, ten poles, and a trapezoidal-shaped back-EMF (electromotive force).

The experimental verification on the small-scale wind turbine workbench emulates the operating conditions of the rectifier in a wind turbine, which is crucial to verify its performance and validate the theoretical studies.

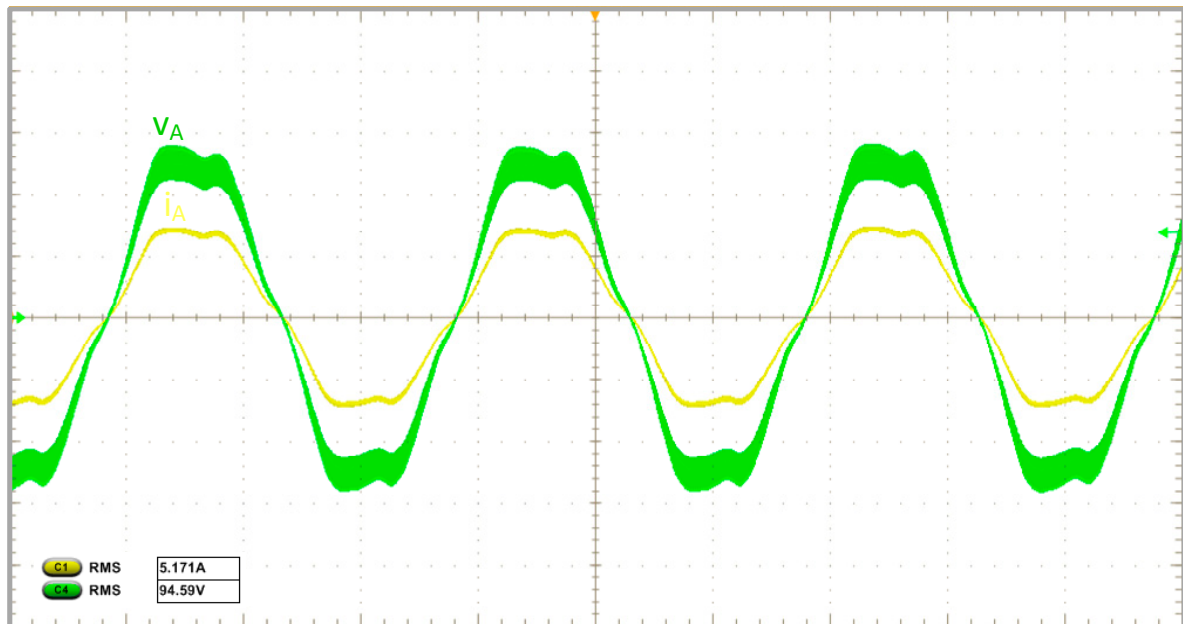
The current waveforms drained from the PMSG are shown in Figure 13. It is possible to observe waveforms with a trapezoidal shape, and the currents present rms values of 5.23, 5.17, and 4.78 A.



**Figure 13.** Waveforms of currents obtained from the PMSG (3 A/per division (/div)). Time (5 ms/div).

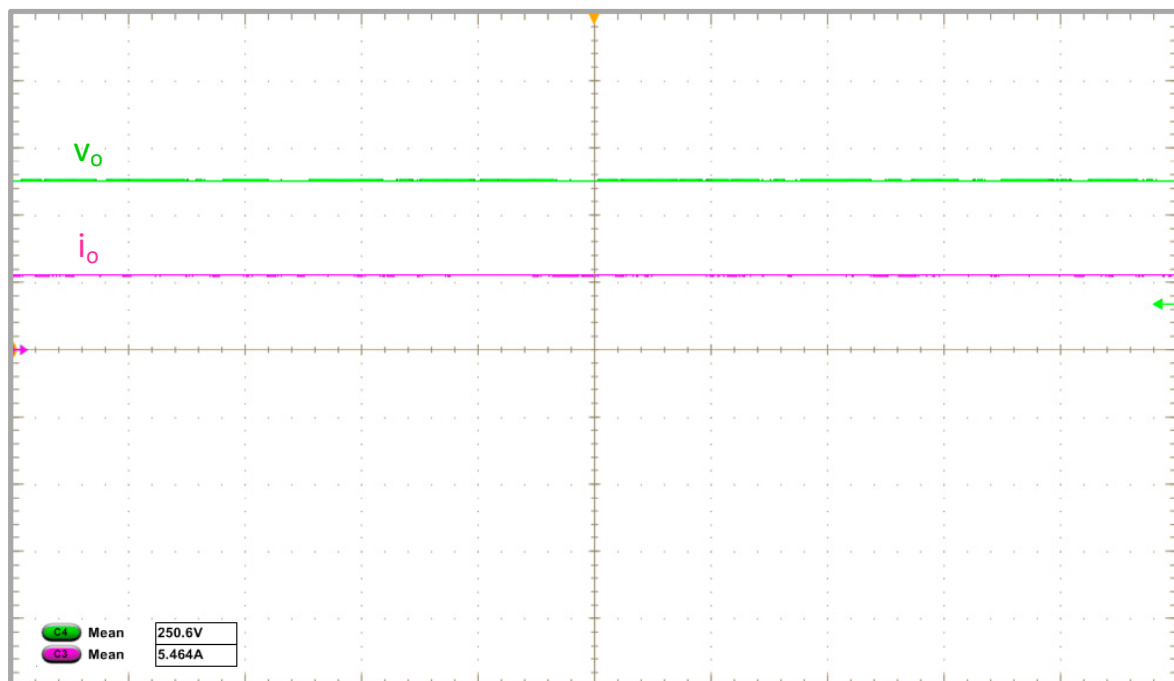
The voltage (green) and current (yellow) waveforms in phase A are shown in Figure 14, with the rms voltage value in phase A approximately 90 V and frequency 30 Hz. From the trends outlined in this figure, it is possible to conclude that the rectifier provides a

high power factor since the voltage and the current have the same shape, and there is no phase shift between voltage and current. Additionally, the rectifier can operate with non-sinusoidal waveforms.



**Figure 14.** Waveforms of voltage (green) (50 V/div) and current (yellow) (5 A/div). Time (10 ms/div).

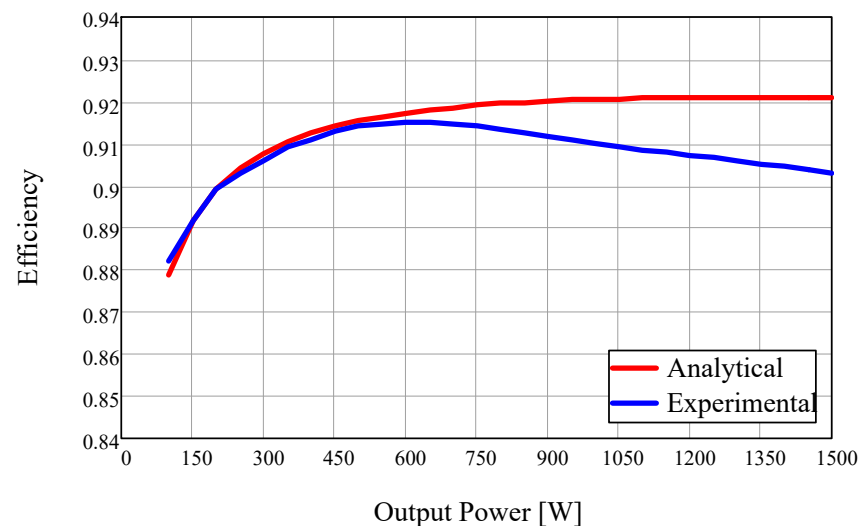
On the other hand, the output voltage and current waveforms are shown in Figure 15. The average output voltage is approximately 250 V, while the average output current is 5.5 A. Therefore, the output power is about 1.375 kW.



**Figure 15.** Waveforms of output voltage (100 V/div) and output current (5 A/div). Time (10 ms/div).

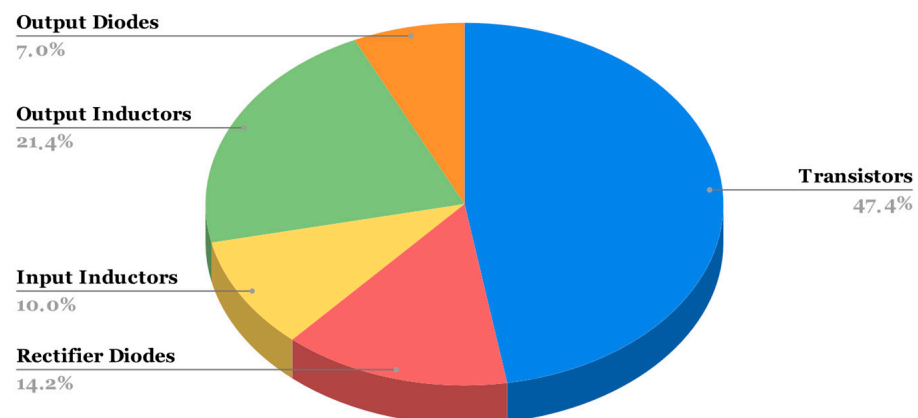
From Figure 15, it is possible to observe that the output voltage is kept at approximately 250 V by the action of the voltage controller.

The experimental and theoretical efficiency curves as a function of the output power are depicted in Figure 16. The rectifier presents an efficiency greater than 90% for a wide power variation. The maximum efficiency is about 91.5% when the rectifier processes about half of the rated power.



**Figure 16.** Experimental and analytical curves of efficiency as a function of the output power.

Figure 17 exhibits the theoretical losses distribution at rated power per component. It should be highlighted that the largest proportion of losses is in the transistors (47.4%) and the output inductors (21.4%).



**Figure 17.** Theoretical losses distribution at rated power per component.

The experimental results show the proposal's feasibility when processing the energy of a small-scale wind turbine system. The three-phase phase-modular SEPIC rectifier provides high energy quality, maximizing the active power extracted from the wind turbine.

## 6. Conclusions

This paper proposes a three-phase phase-modular SEPIC rectifier to process the energy of a small-scale wind turbine. From the theoretical analysis, the design equations were stated, and a proof-of-concept prototype was built. The experimental results obtained from the emulator workbench show the ability of the rectifier to process the energy of a non-sinusoidal three-phase system since the permanent magnet synchronous generator has trapezoidal waveforms.



In conclusion, the proposal shows the following advantages of using this rectifier concept:

- The inductances of the PMSG can be used as the input inductances of the rectifier, which decreases the component count of the rectifier, thus reducing the cost;
- The high power factor is achieved naturally, as a characteristic of the rectifier operating in DCM, avoiding the use of a current control system. Therefore, this reduces the cost without using current and voltage sensors;
- The output quantities (for example, the DC output voltage) can be controlled using simple control techniques and PWM modulation as the same control scheme as a DC–DC converter;
- The phase-modular concept allows operation with phase fault without any additional control technique;
- If necessary, the rectifier can provide high-frequency galvanic isolation between the generator and the output by replacing output inductors with coupled inductors.

In future works, maximum power point tracking (MPPT) strategies will be studied and implemented, and they will allow the system to operate at the point of maximum power for a range of wind speed variations.

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## Abbreviations

The following abbreviations have been used in this manuscript:

SEPIC	Single-Ended Primary-Inductor Converter
DCM	Discontinuous Conduction Mode
DC	Direct Current
PWM	Pulse Width Modulation
SWT	Small Wind Turbines
PMSG	Permanent Magnet Synchronous Generator
PLL	Phase-Locked Loop
AC	Alternating Current
RMS	Root Mean Square
EMF	Electromotive Force
MPPT	Maximum Power Point Tracking

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