

Article

The Performance of the High-Current Transformer during Operation in the Wide Frequencies Range

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Abstract: This paper presents the performance of the 26 kVA inductive high-current transformer (*HCT*) during operation in the frequencies range of transformed harmonics from 50 Hz to 5 kHz. Performed research concerns the determination of the possibility of obtaining an order of the higher harmonic of a given RMS value in its distorted output current for the required RMS value of the main component and the maximum safe instantaneous value of the input voltage equal to 400 V. The results are presented for serial, serial-parallel and parallel configurations of primary and secondary windings (9 cases). Therefore, the most favourable configuration of the primary and secondary windings sections may be chosen. The tests are performed for the transformation of the distorted current containing a fundamental component and one higher harmonic of order from the 5th changed by the 5 up to the 100th. The constant 10% higher harmonic level in relation to the main component of the distorted secondary current is set. The measurements are performed for different resistances and inductances of the secondary winding's load resulting from the length of the connected current track.

Keywords: high-current transformer; distorted current; higher harmonics; wideband supply; generation; output current; current transformer; testing at harmonic



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1. Introduction

The inductive high-current transformer (*HCT*) is used to step up current in the high-current test systems for the evaluation of the performance of current transformers, circuit breakers and power cables etc. It is composed of the toroidal magnetic core made from electrotechnical steel and primary and secondary windings divided into 4 sections. The configuration of the sections of the primary and secondary winding sets the input and output apparent power distribution between the current and voltage. The serial and parallel connection of sections in both windings will ensure the highest output voltage if increased impedance is connected to the secondary winding. The parallel connection of sections in the primary winding required the highest input current, but then only for the parallel connection of sections in the secondary winding was the rated apparent power of *HCT* available. The serial connection of its sections ensures 25% of the rated output apparent power and 25% of the rated output current is available. Distortion of the current in the power grid causes a need to perform the transformation accuracy test of measuring current transformers (*CTs*) in the wider frequencies range, not only for sinusoidal currents of 50 Hz (60 Hz) frequency [1–13]. This results from the fact that distorted active and reactive power is measured by the electricity meters and wideband metrological performance of instrument transformer is required to ensure their accurate measurements [14–21]. There are developed measuring systems for the evaluation of *CT* transformation accuracy for distorted current [4,5,7,8]. In the solutions presented in the papers [1,2,7,8,22], the tests are performed in the conditions of the rated ampere turns. In this case, the *HCT* is not required but this method is only applicable to window type *CTs*. This is because an additional primary winding has to be made. The required number of turns results from the rated current ratio of tested *CT* and its rated secondary current RMS value. The additional

primary winding is supplied from the wideband amplifier or calibrator, which may ensure about 100 A or 12.5 A output current, respectively [4,5,23–27]. If bar type *CT* needs to be tested, the *HCT* is required. In such a measuring system, the source of the reference signal is also needed. For this purpose, specially designed wideband inductive *CTs* or electronic transducers may be used [6,28–31]. The primary circuits of the reference device and tested bar type *CT* are connected in series and fed with the rated current from the *HCT*. To perform the wideband accuracy test of *CTs*, it must be supplied from the programmable power source that enables the generation of distorted current containing an adjustable level of harmonics. In ref. [23], a comparison of the wideband power sources able to be applied to the supplying of the high-current transformer is presented. The first solution is based on the pulse width modulation inverter, while the second one is composed of an audio power amplifier and a two-channel arbitrary generator.

In this paper, the performance of the 26 kVA inductive *HCT* during operation in the frequencies range of the transformed harmonics from 50 Hz to 5 kHz is presented. The research concerns the determination of the possibility of obtaining an order of the higher harmonic of a given RMS value in its distorted output current for the required RMS value of the main component and the maximum safe instantaneous value of the input voltage equal to 400 V. The tests are performed for the transformation of the distorted current containing a fundamental component and one higher harmonic of order from the 5th changed by the 5 up to the 100th. The results are presented for serial, serial-parallel and parallel configurations of primary and secondary windings (9 cases). Therefore, the most favourable configuration of the primary and secondary windings sections may be chosen. The constant 10% higher harmonic level in relation to the main component of the distorted secondary current is set. The measurements are performed for different resistances and inductances of the secondary winding's load resulting from the length of the connected current track equal to 6 m or 3 m. Tested *HCT* is supplied by the programmable power supply system. This limits the available input current to 20 A RMS. The leakage inductances of windings are the most important factors conditioning the performance of the *HCT* during operation in the wide frequencies range. Their values are determined for all available connections of sections. Therefore, the performance of the 26 kVA inductive *HCT* for the maximum input current of the primary winding for all available connections of its sections may be evaluated. Moreover, the improvements to the tested *HCT* construction to increase its distorted secondary current RMS value with 10% contribution of the higher harmonic in the frequencies range of operation up to 5 kHz are proposed.

The novelty of this paper is enumerated in the following bullet points:

- determination of the wideband performance of the tested *HCT* and identification of the most favourable connection of sections of secondary and primary windings,
- designation of the factors limiting the wideband operation of the inductive *HCT* with analysis of the influence of inductance and resistance of the load,
- proposition of the improvements to the construction of the tested inductive *HCT* to increase its distorted output current RMS value,
- presentation of the relationship between the RMS value of the distorted output current with a given harmonic order and required RMS value of the input primary voltage,
- designation of the negligibility of the influence of windings resistance and magnetic core excitation current on the wideband performance of the tested inductive *HCT*.

2. The Measuring Circuit and the Tested High-Current Transformer

The measuring circuit presented in Figure 1 is supplied by the programmable power supply system (*PPS*), enabling generation of the distorted currents [23,24]. To determine the wideband performance of the *HCT*, the digital power meter (*DPM*) with two measuring modules is used. Moreover, the *DPM* is able to perform the Fast Fourier Transform (*FFT*) of all the measured signals. The first *DPM*'s measuring module is connected to the primary side of the tested *HCT*, while the second one measures the secondary side voltage and current through the wideband current transformer (*WCT*). Utilisation of the *WCT* is required

to transform the high value of the secondary current flowing in the current track (CTr). The WCT can operate in the wide frequency range with high metrological performance, as presented in the papers [1,8,32].

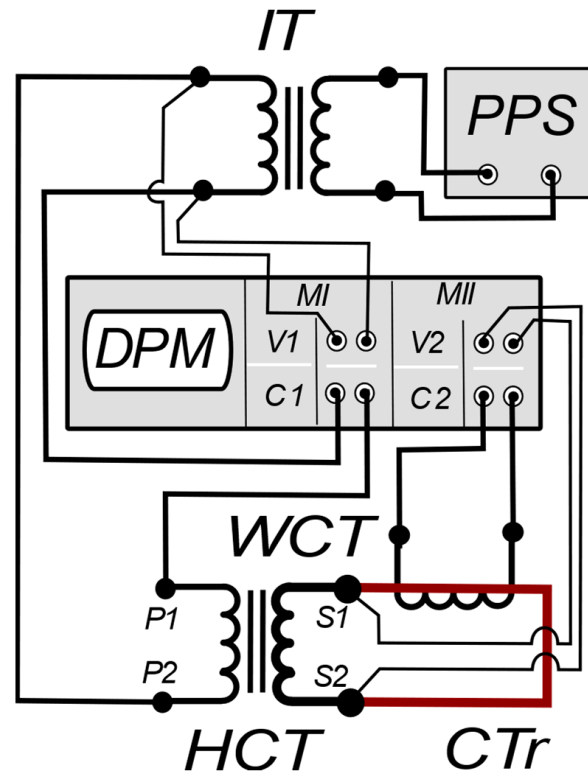


Figure 1. Measuring circuit used to determine the wideband performance of the HCT.

In Figure 1, the following abbreviations are used:

PPS—programmable power supply system,

DPM—digital power meter,

WCT—wideband current transformer,

HCT—high-current transformer,

CTr—current track,

MI/MII—I/II measuring module of the DPM,

V1/V2—1/2 voltage input,

C1/C2—1/2 current input,

P1/P2—terminals of the primary winding of the HCT,

S1/S2—terminals of the secondary winding of the HCT.

During the tests, the HCT is fed by the distorted input voltage with the maximum instantaneous value not exceeding 400 V. Therefore, the maximum instantaneous value of the generated higher harmonics is limited in accordance with the equation:

$$U_{max} = 400 \text{ V} = \max \left\{ 230\sqrt{2} \sin 2\pi 50t + U_{mhk} \sin(\omega_{hk}t + \varphi_{hk}) \right\}, \quad (1)$$

This limitation results from the maximum permitted electrical stress of the primary winding's insulation. The tests were performed in the condition where the secondary current was distorted by a single higher harmonic with the percentage level equal to 10% of the main component. To conduct research on the wideband performance of the HCT, the analysis of its equivalent circuit presented in Figure 2 was performed.

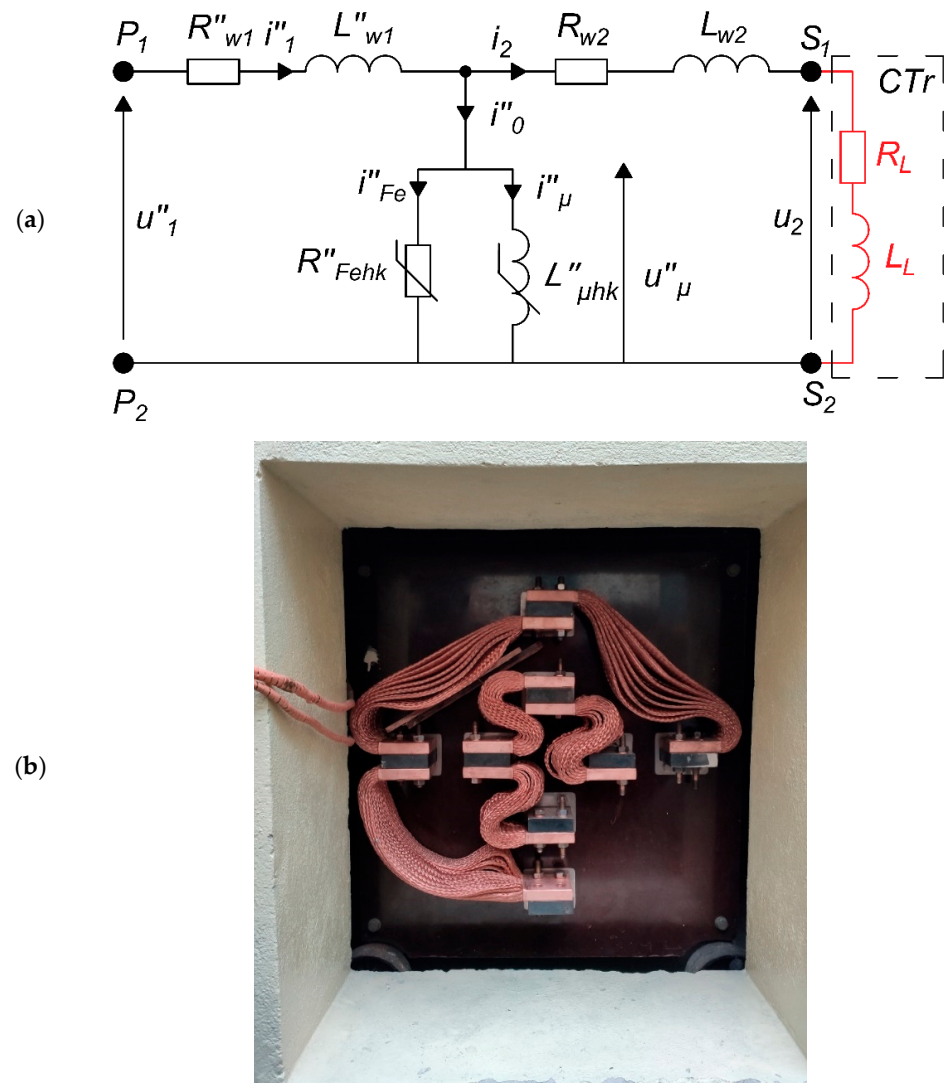


Figure 2. (a) Equivalent circuit of the HCT, (b) Photo of the HCT's secondary side.

In Figure 2, the following abbreviations are used:

The notation " means that the values are converted to the HCT's secondary side.

R''_{w1} —resistance of the primary winding,

L''_{w1} —leakage inductance of the primary winding,

R_{w2} —resistance of the secondary winding,

L_{w2} —leakage inductance of the secondary winding,

R_L —resistance of the load associated with the current track,

L_L —inductance of the load associated with the current track,

R''_{Fehk} —resistance associated with active power losses of the magnetic core,

$L''_{\mu hk}$ —mutual inductance of the HCT's windings,

i''_1 —instantaneous current of the HCT's primary winding,

i''_0 —instantaneous excitation current of the HCT's magnetic core,

i''_{μ} —instantaneous reactive component of the excitation current,

i''_{Fe} —instantaneous active component of the excitation current,

i_2 —instantaneous current of the HCT's secondary winding,

u''_1 —instantaneous voltage of the HCT's primary winding,

u''_{μ} —instantaneous voltage associated with mutual inductance of the HCT's windings,

u_2 —instantaneous voltage of the HCT's secondary winding.

The main factors which are dependent on frequency, taking into consideration the equivalent circuit (Figure 2a), are reactances of the windings and load. The influence of the magnetic core on the wideband operation of the HCT is negligible due to the low value of the excitation current in relation to the primary current [33]. In such a case, the primary voltage converted to the secondary side may be calculated from the following equation:

$$\begin{aligned}
 u''_1 = & \left[I_{2h1} \sqrt{2} \sin 2\pi 50t + I_{2hk} \sqrt{2} \sin(2\pi f_{hk}t + \varphi_{hk}) \right] R_L + \\
 & \left(I_{2h1} \sqrt{2} \sin 2\pi 50t \right) 2\pi 50 L_L + \left[I_{2hk} \sqrt{2} \sin(2\pi f_{hk}t + \varphi_{hk}) \right] 2\pi f_{hk} L_L + \\
 & \left[I_{2h1} \sqrt{2} \sin 2\pi 50t + I_{2hk} \sqrt{2} \sin(2\pi f_{hk}t + \varphi_{hk}) \right] R_{w2} + \\
 & \left(I_{2h1} \sqrt{2} \sin 2\pi 50t \right) 2\pi 50 L_{w2} + \left[I_{2hk} \sqrt{2} \sin(2\pi f_{hk}t + \varphi_{hk}) \right] 2\pi f_{hk} L_{w2} + \\
 & \left[I''_{1h1} \sqrt{2} \sin 2\pi 50t + I''_{1hk} \sqrt{2} \sin(2\pi f_{hk}t + \varphi_{hk}) \right] R''_{w1} + \\
 & \left(I''_{1h1} \sqrt{2} \sin 2\pi 50t \right) 2\pi 50 L''_{w1} + \left[I''_{1hk} \sqrt{2} \sin(2\pi f_{hk}t + \varphi_{hk}) \right] 2\pi f_{hk} L''_{w1},
 \end{aligned} \quad (2)$$

where:

hk —the order of higher harmonic component and

$h1$ —the main component.

The RMS values of each harmonic component of the instantaneous primary voltage are calculated using FFT.

Considering used large windings and current track cross-section diameters, their values of resistance are also not an influence on the wideband operation of the HCT. These values are significantly lower than the reactances of the windings and current track. Therefore, the voltage drops on the resistances are negligible, also including the effect of their increase with the temperature and skin effect.

The windings of the HCT are divided into sections, with a single section of the primary winding having 36 turns and the secondary winding having 1 turn. Each winding consists of 4 sections, allowing parallel, serial-parallel and serial connection of them. Examples of primary and secondary winding section connections are presented in Figure 3.

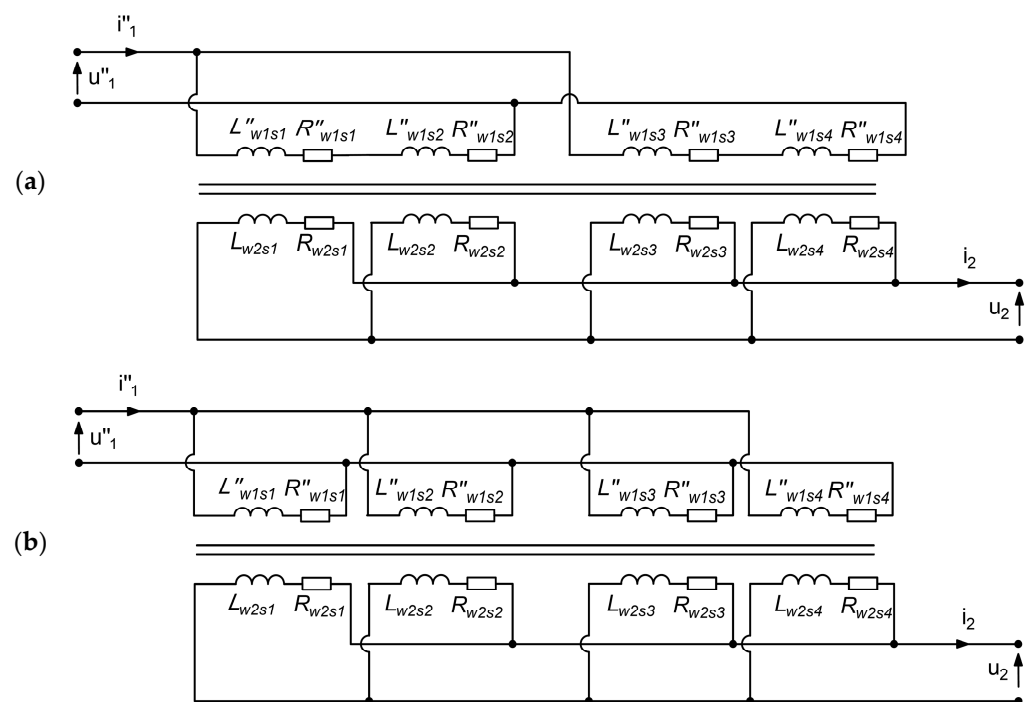


Figure 3. Cont.

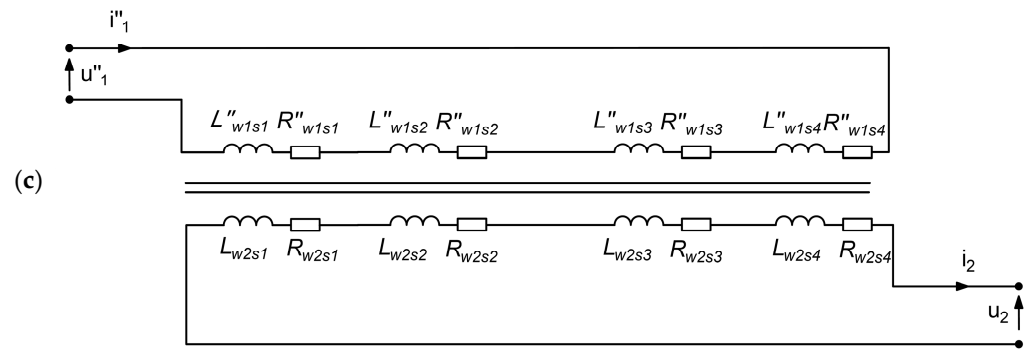


Figure 3. Examples of primary and secondary winding section connections: (a) serial-parallel, primary and parallel secondary winding sections, (b) parallel primary and parallel secondary winding sections, (c) serial primary and serial secondary winding sections.

In Figure 3, the following abbreviations are used:

The notation " means that the values are converted to the HCT's secondary side.

$R''_{w1s1}/R''_{w1s2}/R''_{w1s3}/R''_{w1s4}$ —resistance of each section of the primary winding,

$L''_{w1s1}/L''_{w1s2}/L''_{w1s3}/L''_{w1s4}$ —leakage inductance of each section of the primary winding,

$R_{w2s1}/R_{w2s2}/R_{w2s3}/R_{w2s4}$ —resistance of each section of the secondary winding,

$L_{w2s1}/L_{w2s2}/L_{w2s3}/L_{w2s4}$ —leakage inductance of each section of the primary winding.

The method of connecting the primary winding sections determines the power of the HCT by selecting the current supplied from the mains. The method in which the secondary winding sections are connected determines the permissible value of the current resulting from the multiple number of turns connected in parallel. The method in which the sections of the primary and the secondary windings are connected determines the current and voltage ratio of the HCT, defined based on the distribution of the output power between current and voltage.

3. Measurement of the HCT's Transformation Performance in the Wide Frequencies Range

The measurements were performed in the measuring circuit presented in Figure 1.

In all presented calculations of the values of the HCT's output current, the excitation current was ignored. Therefore, its value results from the current ratio and may be expressed as:

$$i''_1 = \frac{i_2}{n}, \quad (3)$$

where:

n —current ratio equal to turns ratio.

The condition that must be met is that the calculated input voltage from Equation (2) does not exceed the maximum permissible input voltage defined by Equation (1). At the same time, the condition that the RMS values of the maximum input current does not exceed 28.5 A, 57 A and 114 A for serial, serial-parallel and parallel configuration of the primary winding's section, respectively. In the overview of the results presented in Table 1, we compare maximum values, measured and calculated from Equation (3), of the obtained distorted secondary current where the whole frequency band of operation is ensured.

The cases where the required maximum instantaneous distorted primary voltage exceeds 400 V are shaded in the red colour. The cases where the measured distorted primary current exceeds 20 A RMS, which results from the maximum available output current of the programmable power supply system (PPS), are shaded in the green colour.

Table 1. Overview of the measured and calculated maximum values of the secondary current with the 100th order of higher harmonic equal to a 10% value of the main component.

Configuration of the Sections of the Primary Winding	Configuration of the Sections of the Secondary Winding	Current Ratio	R_L [m Ω]	L_L [μ H]	Measured Max Current with 10% of 100th Harm. [A]	Calculated Max Current with 10% of 100th Harm. [A]
serial	serial	36	0.3	3.0	350	380
			0.2	1.5	490	520
	serial-parallel	72	0.3	3.0	270	260
			0.2	1.5	455	430
	parallel	144	0.3	3.0	145	150
			0.2	1.5	255	270
serial-parallel	serial	18	0.3	3.0	360	360
			0.2	1.5	360	360
	serial-parallel	36	0.3	3.0	535	520
			0.2	1.5	720	720
	parallel	72	0.3	3.0	290	300
			0.2	1.5	510	540
parallel	serial	9	0.3	3.0	180	180
			0.2	1.5	180	180
	serial-parallel	18	0.3	3.0	360	360
			0.2	1.5	360	360
	parallel	36	0.3	3.0	570	590
			0.2	1.5	720	720

It results from the presented overview that the highest distorted output current with 10% of higher harmonics is obtained for configuration when the sections of the primary winding are connected in parallel and the secondary winding's sections are also connected in parallel. Calculated values of the secondary currents maximally differ from the measured values by about 30 A. Therefore, without considering the magnetic core excitation current, we obtain sufficient accuracy when determining the RMS value of the distorted secondary current (it is shown in Table 1 that the calculation accuracy is not worse than 8%). The limitation shaded in red results from the high required voltage of the higher harmonic due to the reactances of the windings and the load. Therefore, the secondary voltage comes from the limited input voltage and the turns ratio of the HCT. If the turns ratio is high, the secondary voltage is low and if the turns ratio is lower, the secondary voltage is higher. The change of the turns ratio also changes the input current. If the secondary current has to be retained, the input current has to be increased, while the turns ratio has to be lowered.

The cases when the highest and the lowest values of the secondary current with an 100th order higher harmonic equal to 10% of the main component were obtained are marked in bolded font (Table 1) and presented in detail in Figures 4 and 5.

In the above graph (in Figure 4a), for the case when the load of the secondary winding is equal to $R_L = 0.3 \text{ m}\Omega$; $L_L = 3 \text{ }\mu\text{H}$ and the applied maximum input current is equal to 9 A RMS, the output current is equal to 1300 A, but none of the higher harmonics may be obtained without exceeding the maximum RMS value of the input voltage. The operating bandwidth from 50 Hz to 5 kHz is obtained only for the highest 100 A RMS output current. This results from the required secondary voltage, which is increased with the order of the transformed higher harmonic. Considering the case presented in Figure 4b where the length of the current track is decreased, the RMS value of the output current for the analysed frequency range of operation of the tested HCT is increased to 250 A RMS. This is caused by the decrease of the inductance of the load, which thereby decreased the required RMS value of the output voltage.

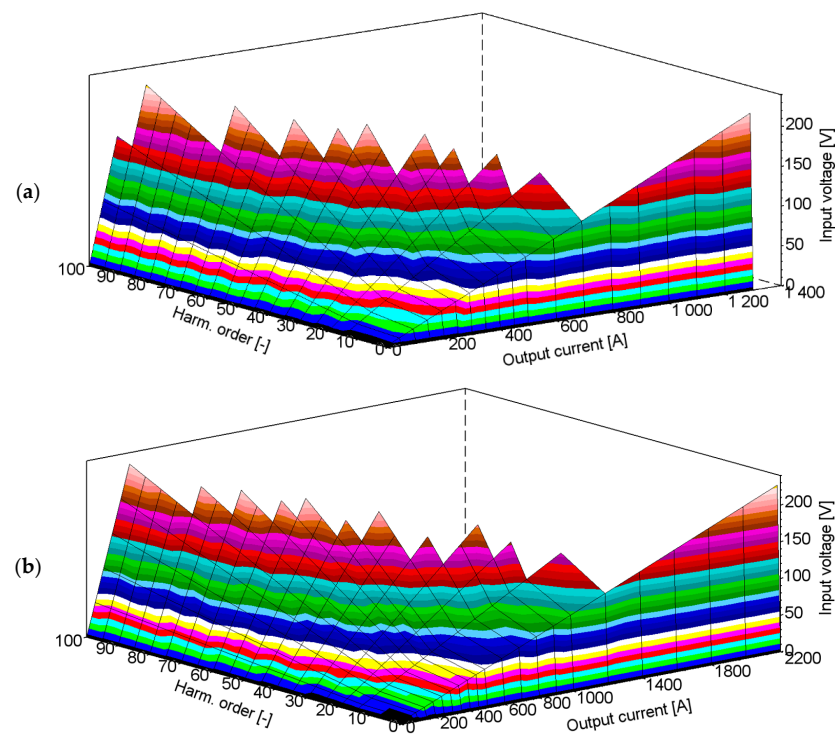


Figure 4. The measured distorted output current with a given harmonic order for supplied primary voltage obtained for serial connection of the primary winding's sections and parallel connection of the secondary winding's sections: (a) $R_L = 0.3 \text{ m}\Omega$; $L_L = 3 \text{ }\mu\text{H}$, (b) $R_L = 0.2 \text{ m}\Omega$; $L_L = 1.5 \text{ }\mu\text{H}$.

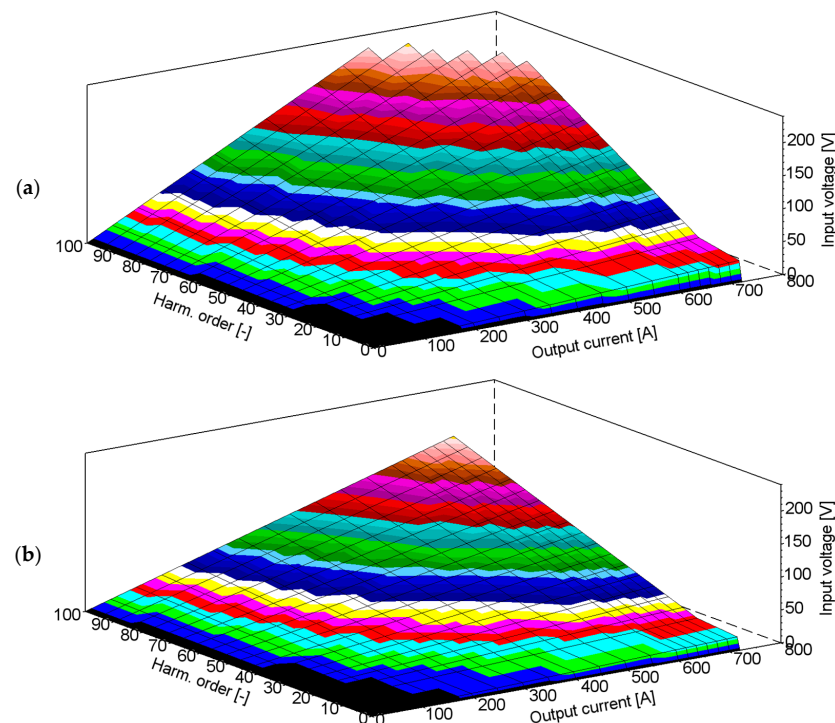


Figure 5. The measured distorted output current with a given harmonic order for the supplied primary voltage obtained for parallel connection of the primary winding's sections and parallel connection of the secondary winding's sections: (a) $R_L = 0.3 \text{ m}\Omega$; $L_L = 3 \text{ }\mu\text{H}$, (b) $R_L = 0.2 \text{ m}\Omega$; $L_L = 1.5 \text{ }\mu\text{H}$.

The measured distorted output current with a given harmonic order for the supplied primary voltage obtained for parallel connection of the primary winding's sections and parallel connection of the secondary winding's sections for two different loads is presented in Figure 5.

In the above graph (in Figure 5a), for the case when the load of the secondary winding is equal to $R_L = 0.3 \text{ m}\Omega$; $L_L = 3 \text{ }\mu\text{H}$ and the applied maximum input current is equal to 20 A RMS, the output current is equal to 720 A, but this may only be obtained up to the 60th order of higher harmonics. Higher order requires exceeding the maximum RMS value of the input voltage. The operating bandwidth from 50 Hz to 5 kHz is obtained only for the highest 570 A RMS output current. Considering the case presented in Figure 5b where the length of the current track is decreased, the RMS value of the output current for the analysed frequency range of operation of the tested *HCT* is increased to 720 A RMS. This is the most favourable configuration of the *HCT* (parallel connection of the primary and secondary winding's sections) when it is supplied by the programmable power supply system (*PPS*).

4. Calculation of the *HCT*'s Transformation Performance in the Wide Frequencies Range

In this paragraph, we present the results of the calculation of the *HCT* wideband performance in the cases when the primary current RMS value is limited only by the maximum input current resulting from the diameter of the wire used to make the primary winding. The values of the parameters of the equivalent circuit presented in Figure 2 required for calculations are determined in accordance with the method described in the paper [33]. The resistances of the windings are measured from the primary and secondary sides when the *HCT* is supplied by the direct current. The primary winding inductance is determined in the non-load state in the frequencies range from 50 Hz up to 5 kHz in accordance with the provided analysis of the vectorial diagrams. The secondary winding inductance is determined in the load state in the frequencies range from 50 Hz up to 5 kHz in accordance with the provided analysis of the vectorial diagrams. The results show a one percent deviation in the measured values. The overview of the calculated maximum values of the secondary current with an 100th order higher harmonic equal to 10% of the main component and obtained maximum higher harmonic order for the secondary current equal to 1000 A is presented in Table 2. The analysis is presented for four loads of the *HCT*'s secondary winding, where for the first three, only inductance of the current track is changed and in the last case, only the resistance is changed.

The cases where the required maximum instantaneous distorted primary voltage exceeds 400 V are shaded in the red colour. The cases where the required primary current exceeds 28.5 A RMS for the serial connection of the primary winding's sections, 57 A RMS for the serial-parallel connection of the primary winding's sections and 114 A RMS for the parallel connection of the primary winding's sections are shaded in the green colour.

When more current is available from the mains, the turns ratio has to be reduced; then, the secondary voltage will be higher, and the secondary current will increase in the considered frequency band of the *HCT*'s operation. If turns of the primary winding are equal to 18 and turns of the secondary winding are equal to 1 turn for the maximum available current, from the mains equal to 114 A RMS, the operation of the *HCT* in the order up to the 100th higher harmonic of the secondary current equal to 2000 A with a load $R_L = 0.3 \text{ m}\Omega$; $L_L = 1.5 \text{ }\mu\text{H}$ will be obtained. When the maximum instantaneous value of the primary voltage is increased to 600 V, it is possible to achieve a distorted current equal to 2600 A RMS with the maximum order of the 100th higher harmonic considering the limitation of the current input value equal to 114 A RMS with turns ratio equal to 23 (1 turn of the secondary winding). If the same limitation of the maximum values of the primary voltage is assumed and the limitation of the supplied current is increased to 175 A RMS with reduced turns ratio to 18, the distorted secondary current will be equal to 3150 A RMS with a set bandwidth of higher harmonics up to the 100th order.

Table 2. Overview of the calculated maximum values of the secondary current with 100th order higher harmonic equal to 10% of the main component and obtained maximum higher harmonic order for the secondary current equal to 1000 A.

Configuration of the Sections of the Primary Winding	Configuration of the Sections of the Secondary Winding	Current Ratio [–]	R_{w1} [mΩ]	L_{w1} [μH]	R_{w2} [mΩ]	L_{w2} [μH]	R_L [mΩ]	L_L [μH]	Max Harm. Order for 1000 A	Max Current with 10% of 100th Harmonic [A]
serial	serial	36	0.17	0.61	0.64	1.75	0.3	3.0	37th	380
								1.5	52th	520
								6.0	24th	240
	serial-parallel	72	0.04	0.15	0.24	0.70	0.3	3.0	37th	380
								3.0	26th	260
								1.5	43th	430
							3.0	6.0	14th	150
								3.0	26th	260
								3.0	15th	150
	parallel	144	0.01	0.04	0.14	0.32	0.3	1.5	27th	270
								6.0	8th	80
								3.0	14th	150
serial-parallel	serial	18	0.13	0.82	0.64	1.75	0.3	3.0	72th	720
								1.5	99th	990
								6.0	47th	470
	serial-parallel	36	0.03	0.20	0.24	0.70	0.3	3.0	72th	720
								3.0	52th	520
								1.5	84th	840
							3.0	6.0	29th	290
								3.0	52th	520
								3.0	30th	300
	parallel	72	0.01	0.05	0.14	0.32	0.3	1.5	54th	540
								6.0	16th	160
								3.0	30th	300
parallel	serial	9	0.07	1.41	0.64	1.75	0.3	3.0	132th	1030
								1.5	175th	1030
								6.0	88th	880
	serial-parallel	18	0.02	0.35	0.24	0.70	0.3	3.0	132th	1026
								3.0	100th	1000
								1.5	158th	1580
							3.0	6.0	57th	570
								3.0	100th	1000
								3.0	60th	600
	parallel	36	0.005	0.09	0.14	0.32	0.3	1.5	106th	1060
								6.0	32th	320
								3.0	60th	600

The cases when the highest and the lowest values of the secondary current with a 100th order higher harmonic equal to 10% of the main component were determined are marked in bolded font and presented in detail in Figures 6 and 7.

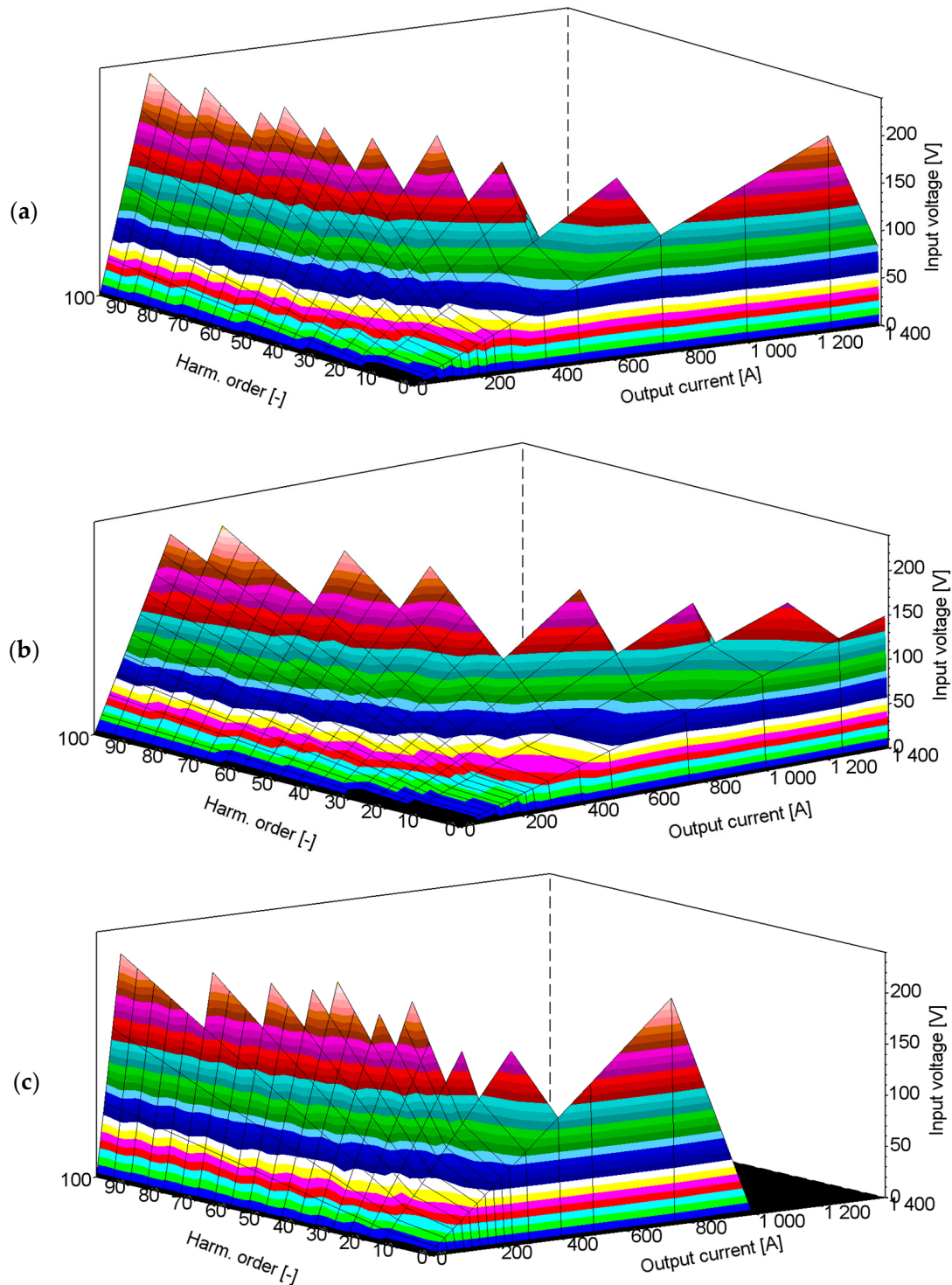


Figure 6. The calculated distorted output current with a given harmonic order for the supplied primary voltage obtained for serial connection of the primary winding's sections and parallel connection of the secondary winding's sections: (a) $R_L = 0.3 \text{ m}\Omega$; $L_L = 3 \text{ }\mu\text{H}$, (b) $R_L = 0.3 \text{ m}\Omega$; $L_L = 1.5 \text{ }\mu\text{H}$, (c) $R_L = 0.3 \text{ m}\Omega$; $L_L = 6 \text{ }\mu\text{H}$.

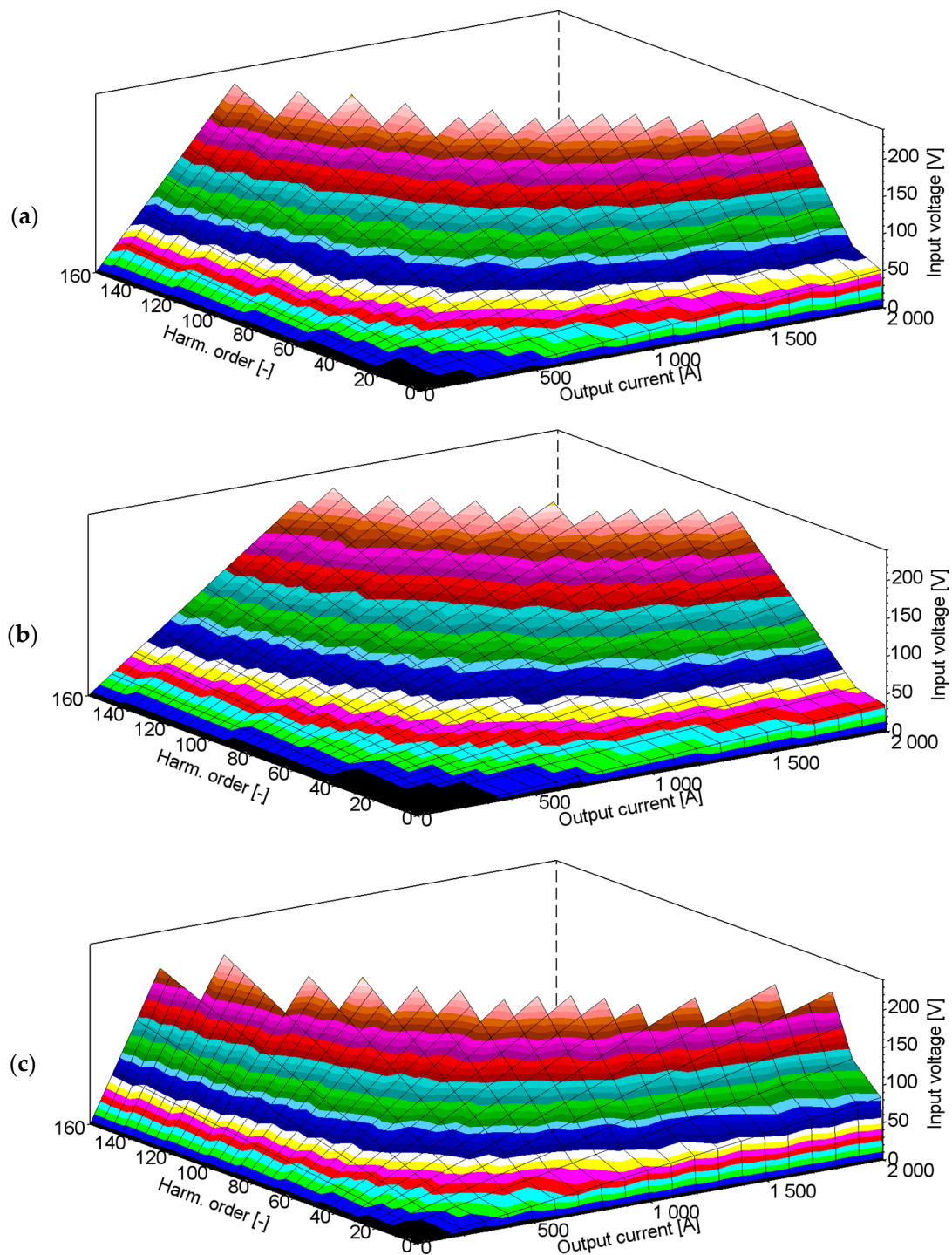


Figure 7. The calculated distorted output current with a given harmonic order for the supplied primary voltage obtained for the parallel connection of the primary winding's sections and the serial-parallel connection of the secondary winding's sections: (a) $R_L = 0.3 \text{ m}\Omega$; $L_L = 3 \text{ }\mu\text{H}$, (b) $R_L = 0.3 \text{ m}\Omega$; $L_L = 1.5 \text{ }\mu\text{H}$, (c) $R_L = 0.3 \text{ m}\Omega$; $L_L = 6 \text{ }\mu\text{H}$.

In the above graph (in Figure 6a), for the case when the load of the secondary winding is equal to $R_L = 0.3 \text{ m}\Omega$; $L_L = 3 \text{ }\mu\text{H}$ and the applied maximum input current is equal to 28.5 A RMS, the output current is equal to 1350 A, but none of the higher harmonics may be obtained without exceeding the maximum RMS value of the input voltage. This is the maximum permissible value of the secondary current when the sections of the primary winding are connected in serial. The operating bandwidth from 50 Hz to 5 kHz is obtained

only for the highest 150 A RMS output current. This results from the required secondary voltage which is increased with the order of the transformed higher harmonic. Considering the case presented in Figure 6b where the inductance of the load is decreased, the RMS value of the output current for the analysed frequency range of operation of the tested *HCT* is increased to 270 A RMS. In the case presented in Figure 6c for increased value of the inductance, the lower RMS values of the secondary current (80 A) is obtained. Presented diagrams are useful to determine the maximum RMS value of the distorted output current of the *HCT* for any assumed maximum order of the higher harmonic equal to 10% of the main component.

The calculated distorted output current with a given harmonic order for the supplied primary voltage obtained for the parallel connection of the primary winding's sections and serial-parallel connection of the secondary winding's sections for three configurations of load are presented in Figure 7.

In the above graph (in Figure 7a), for the case when the load of the secondary winding is equal to $R_L = 0.3 \text{ m}\Omega$; $L_L = 3 \text{ }\mu\text{H}$ and the applied maximum input current is equal to 114 A RMS, the output current is equal to 2050 A, but this may only be obtained up to the 40th order of the higher harmonic. Higher order requires exceeding the maximum RMS value of the input voltage. This is the maximum permissible value of the secondary current when the sections of the primary winding are connected in parallel. The operating bandwidth from 50 Hz to 8 kHz is obtained only for the highest 600 A RMS output current. This results from the required secondary voltage, which is increased with the order of the transformed higher harmonic. Considering the case presented in the Figure 6b where the inductance of the load is decreased, the RMS value of the output current for the analysed frequency range of operation of the tested *HCT* is increased to 800 A RMS. In the case presented in Figure 6c for increased values of the inductance, the lower RMS values of the secondary current (300 A) are obtained. In these cases, the maximum available RMS value of the input current from the mains is limited to 114 A. Therefore, the parallel configuration of both winding's sections provides 1060 A RMS with higher harmonics of order up to the 100th. This limitation results from the maximum permissible input voltage defined by Equation (1). Reduction of the turns ratio by decreasing the number of turns of the primary winding for an increased input current from the mains provides better distribution of the output power of the *HCT* between the current and voltage. Therefore, for the parallel configuration of the section of the primary and secondary windings, a higher distorted output current will be obtained.

5. Conclusions

This paper presents a simple method for the evaluation of the *HCT* wide frequency performance. Presented graphs enable determination of the maximum RMS value of the distorted output current with an assumed value of 10% of the higher harmonic component, defined in relation to the RMS value of the main component. This allows for identification of the most favourable connection of sections of secondary and primary windings. This paper presents the relationship between the RMS value of the distorted output current with a given harmonic order and the required RMS value of the input primary voltage. Moreover, the conducted analysis shows factors limiting the wideband operation of the inductive *HCT* with consideration of the influence of the inductance and resistance of the load. Comparison of the results of the measurements and calculations indicates a negligibility of the influence of windings resistance and magnetic core excitation current on the wideband performance of the tested inductive *HCT*. Provided discussion of the obtained results allows one to deduce the proposition of the improvements to the construction of the tested inductive *HCT* to increase its distorted output current RMS value. The most favourable conditions may be obtained for parallel configuration of sections of the primary and secondary windings with a decreased number of turns of the primary winding. However, this requires an increase in the value of the input current from the mains. The second option is to increase

the maximum instantaneous distorted primary voltage, which results from the maximum allowable electric stress of the primary winding's insulation.

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