



Article Research on the Impact of Output Adjustment Strategy and Carbon Tax Policy on the Stability of the Steel Market

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Abstract: China's steel industry has not yet implemented a carbon tax policy, and its benefits and impacts are still in the theoretical research stage. In addition, enterprises have an insufficient ability to respond to changes in production and sales, which seriously affects the market's stability. The government should simultaneously start from multiple perspectives, such as energy conservation, emission reduction, dynamic adjustments, and business decisions. Therefore, this research constructs a repeated dynamic game model including carbon tax policy and other mixed reduction policies, and studies the stability and related indicators of the market. The results are as follows: (1) the output adjustment policies that enterprises can implement will show an increasing trend under the single carbon tax policy. (2) The output adjustment policies that enterprises need to be more cautious in formulating their production plans, and their output adjustment policies will be restricted and affected by more factors. In summary, enterprises should comprehensively consider emission reduction policies, output adjustment policies and other enterprises 'output changes, to ensure that the steel market will not fall into an imbalanced state.

Keywords: China's steel industry; repeated dynamic game; carbon tax policy; bounded rationality; output adjustment; market stability

1. Introduction

The steel industry is one of the most important core industrial sectors in China. While providing the country with a guarantee of raw materials, it also causes serious pollution problems for the environment. In addition, the steel industry is in a transitional period from the pursuit of product output to the pursuit of high-quality development. Blindly pursuing high output will affect the enterprise's development and even affect the overall stability of the industry. Therefore, in this context, how enterprises can achieve high-quality development by taking into account economic benefits, product output, environmental impact, and other aspects, related research work will become a research focus, and the difficulty that the steel industry faces and needs to be solved urgently.

At present, there are many studies on theoretical models of emission reduction policies. However, it is clear that with the introduction of high-quality development policies, the increasingly stringent emission reduction targets, and the more complicated market competition, the steel industry market needs to consider energy conservation, emission reduction, dynamic adjustment, enterprise decision-making, and other multi-dimensional factors; only in this way can the research be closer to the real future development trend. In this regard, relevant research is relatively weak.



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). This research will focus on the study of the steel market change characteristics under different emission reduction policies, different targets, and different output adjustment policies, and will analyze the stability and dynamic output adjustment situation of enterprises.

2. Literature Review

The achievements of China's steel industry are internationally recognized; however, there are also many problems that need to be solved. Frequent environmental problems such as haze and acid rain have occurred and the potential of the steel industry in terms of energy conservation and emission reduction is gradually being compressed. In view of the current industrial development status, the emission reduction policies based on economic incentives represented by a carbon tax are more widely recognized. Mann [1] recommends a carbon tax because it is easier to implement. Wu et al. [2], Wang et al. [3], Yahoo and Othman [4], and Li and Su [5] used the CGE model (computable general equilibrium) to analyze the overall social impact of carbon tax policies on government and enterprises, such as Qiao et al. [6], Xu et al. [7], and Cao et al. [8]. There is not much research on carbon tax policy applied to the steel industry. This paper sorts out the relevant content, as shown in the Table 1.

Table 1. The literature and summary information on carbon tax applied to the steel industry.

Researcher	Main Theory and Model
Mathiesen and Maestad [9]	partial equilibrium model
Liang et al. [10]	CGE model
Nie et al. [11]	C-D production function
Kuo et al. [12]	evolutionary game
Wakiyama and Zusman [13]	time-series autoregressive moving average (ARMA) model
Duan et al. [14,15]	dynamic game
Ntombela et al. [16]	CGE model
Li et al. [17]	environmental-economic simulation model
Zhu et al. [18]	CGE model
Wu and Xie [19]	CGE model and the optimization model
Deng and Adams [20]	life cycle assessment
Liu et al. [21]	life cycle assessment
Zhao et al. [22]	supply chain analysis

In this study, the output adjustment strategy mainly refers to the bounded rationality output adjustment strategy. As bounded rationality is closer to the real level, it gradually attracted the attention and application of more scholars, and established different bounded rationality models, as a comparison with all situations under complete rationality, which greatly expanded the research ideas. The literature about bounded rationality in industry application are shown in Table 2.

From the review of the above literature, it can be found that carbon tax theory has been widely used in the study of economic and environmental impacts. The CGE model, game model and other energy–economic–environment models constructed on this basis are also relatively mature. However, due to the carbon tax mechanism not being widely promoted, there are few studies on the application of the literature to the steel industry. The bounded rationality expectation strategy has also been widely used. The applications of repeated game theory, stability theory, chaos theory, and chaos control theory are also relatively mature. The literature mainly focuses on theoretical research, and the actual production problems of steel industry are still rare. The literature combining carbon tax and bounded rationality is even rarer. With the introduction of the concept of high-quality development, competition in many aspects such as output, economic benefits, and environmental impacts will inevitably unfold between steel enterprises. However, in terms of how the market changes after the introduction of carbon tax mechanism, bounded rationality expectation,

Researcher	Industrial Sector
Ji [23]	electricity industry and electricity market
Sun and Ma [24]	steel industry and steel market
Tu [25]	power and renewable resources industry
Dang and Hong [26]	glass substrates industry
Tan and Liang [27]	coal industry and coal market
Li et al. [28]	tourism industry
Di et al. [29,30]	transportation planning
Liu [31]	carbon trade market
Yu [32]	transportation industry
Ding et al. [33]	electricity system
Zhang [34]	carbon trade market
Sang, Xie and Wang [35]	ship-building industry
Zhang et al. [36]	remanufacturing industry
Wu [37]	electricity market
Duan et al. [38]	steel industry
Rezvani and Hudson [39]	oil and gas industry
Fan et al. [40]	coal Industry
Gao et al. [41]	creative industry
Ma et al. [42]	vehicle industry
Hammond et al. [43]	construction industry

and different emission reduction targets, as well as market stability and its system dynamics characteristics, the literature is essentially nonexistent.

 Table 2. The literature about bounded rationality in industry application.

In summary, based on the previous research, this paper will introduce multiple emission reduction mechanisms represented by carbon tax and bounded rationality strategies into a repeated dynamic game model, analyze the scenario and stability of the steel market under different emission reduction targets, strategies and different production adjustment strategies, and study the steel market imbalance conditions, stability regions, bifurcation diagrams, Lyapunov exponent and reasonable policy recommendations of the steel industry.

Therefore, the remainder of this paper is organized as follows: in Section 3, this research establishes a dynamic game model based on bounded rationality and carbon tax mechanism, sets single and mixed carbon tax policy scenarios, and introduces data sources. In Section 4, the research presents and discusses the results in detail. In Section 5, conclusions and policy recommendations for the steel industry and the enterprise are provided.

3. Method

Specifically, due to market changes in trade and emission reduction requirements, information acquisition between enterprises and the government and between enterprises is no longer timely and effective. Decision-makers of various enterprises have a certain lag and concern in obtaining information, making it difficult for them to obtain information. The decision-makers of enterprises are no longer "complete, autonomous and rational" decision-makers, and there is a certain range of decision-making (bounded rationality).

The existence of bounded rationality changes the production strategy of enterprises. Although each firm realizes that the equilibrium output achieved in a completely rational state is the most reasonable production plan (Sections 3.1 and 3.2), in the production process from the current production state to the equilibrium output, the decision makers of each enterprise will not adopt this production plan immediately due to the error in information acquisition or the consideration of their own interests, but will wait and see or follow the steps and gradually take production decisions according to the market situation. The production decision model constructed in this paper will reflect the relationship between bounded rationality and enterprise production decisions in this process (Section 3.3). The existence of bounded rationality may make "abnormal" decisions in the production process,

resulting in an unbalanced state of the market. That is to say, if a certain enterprise (or enterprises) has deviations in the decision-making process, the so-called most reasonable production plan will no longer exist.

Different from the previous research that only obtained the final output, after the introduction of bounded rationality, this paper will consider the two basic processes of final decision-making and production decision-making at the same time. Only if these two basic processes are satisfied at the same time is the resulting production scheme feasible. Therefore, this section will elaborate on the methodology based on the above steps.

3.1. The Establishment and Game Analysis of the Static Output Selection Model

According to the researcher's previous research [14,15], in this paper, the main research focus includes the government and six regions. In this paper, subscript 1 substitutes North China, subscript 2 substitutes Northeast China, subscript 3 represents East China, subscript 4 represents South Central China, subscript 5 represents Southwest China, and subscript 6 represents Northwest China. Combined with previous research [14,38,44,45], we reintegrated the parameters required in this paper, which are shown in Table 3.

Table 3. Notations and explanations used in this paper.

Notations	Explanations
Q	Steel production
Р	The price of steel
α	The constant of the market inverse demand curve
β	The primary coefficient of the market inverse demand curve
q_i	Steel production of region <i>i</i>
$e_{2015,i}$	The region $i CO_2$ emission intensity of per ton steel in 2015
e_i	The region $i CO_2$ emission intensity of per ton steel at some stage
r_i	The decline range of CO_2 emission intensity of per ton steel in region <i>i</i> at some stage
Ŕ	The decline target of national CO_2 emission intensity of per ton steel at some stage
MAC	Marginal abatement cost curve in steel industry
a_i	The quadratic coefficient of steel industry's MAC in region <i>i</i>
b_i	The primary coefficient of steel industry's MAC in region <i>i</i>
C_i	The cost function of steel industry in region <i>i</i>
$C_{0,i}$	The production cost of steel industry in region <i>i</i>
c_i	The cost of base period emission reduction in region <i>i</i>
Т	The total carbon tax
t	The unit value of carbon tax
W	Social welfare function
CS	Consumer surplus
PS	Producer surplus
D(E)	Total macro external environment loss of CO_2 emission
heta	The external loss parameter of CO ₂
π_i	The profit function of steel industry in region <i>i</i>
Ε	The total CO_2 emissions in steel industry
ξ_i	The adjustment coefficient, rate of output adjustment
η	The production subsidies
т	The CO_2 emission reduced by the CCS demonstration project
Α	The primary coefficient of CCS demonstration project cost curve
В	The constant of the CCS demonstration project cost curve
S	The total subsidy
М	The total cost of the CCS demonstration project

In a certain emission reduction policy scenario, regional oligopolies in the market compete for CO_2 emission reduction and production simultaneously. At this time, enterprise *i*'s profit function basic form in case *K* is:

$$\pi_{caseK,i} = P(Q)q_i - C_iq_i = (\alpha - \beta Q)q_i - q_iC_{0,i} - q_i\lambda(c_i + \int_0^{r_i} MAC_i(r)dr) = (\alpha - \beta Q)q_i - q_iC_{0,caseK,i} - q_i\lambda(c_i + \int_0^{r_i} MAC_i(r)dr)$$
(1)

If the enterprise pays a carbon tax in the process of production and CO₂ emission reduction, its profit function can be expressed as:

$$\pi_{caseK,tax,i} = P(Q)q_i - C_iq_i = (\alpha - \beta Q)q_i - q_iC_{0,i} - q_i\lambda(c_i + \int_0^{r_i} MAC_i(r)dr) - te_iq_i = (\alpha - \beta Q)q_i - q_iC_{0,caseK,i} - q_i\lambda(c_i + \int_0^{r_i} MAC_i(r)dr) - te_{2015,i}(1 - r_i)q_i$$
(2)

If on this basis, the government subsidizes the enterprise that pays the carbon tax, the profit function of the enterprise can be further expressed as:

$$\pi_{caseK,tax,subsidy,i} = P(Q)q_i - C_iq_i = (\alpha - \beta Q)q_i - q_iC_{0,i} - q_i\lambda(c_i + \int_0^{r_i} MAC_i(r)dr) - te_iq_i + \eta q_i$$

$$= (\alpha - \beta Q)q_i - q_iC_{0,caseK,i} - q_i\lambda(c_i + \int_0^{r_i} MAC_i(r)dr) - te_{2015,i}(1 - r_i)q_i + \eta q_i$$
(3)

In different cases, the social welfare function has been expanded, and the specific form is as follows:

$$W_{CaseK} = CS + PS - D(E) = \int_0^Q P(q) dq - P(Q)Q + \sum_{i=1}^6 \pi_{caseK,i} - \theta E$$

= $\int_0^Q (\alpha - \beta q) dq - (\alpha - \beta \sum_{i=1}^6 q_i) \sum_{i=1}^6 q_i + \sum_{i=1}^6 \pi_{caseK,i} - \theta \sum_{i=1}^6 e_{2015,i}(1 - r_i)q_i$ (4)

Combined with the emission-reduction target R set in this paper, we construct the government decision-making objective function (W) as follows, and its basic form and constraints can be expressed as in Formula (5):

$$\max W \\ s.t. \begin{cases} \sum_{i=1}^{6} e_{i}q_{i} / \sum_{i=1}^{6} q_{i} = e_{2010}(1-R) \\ 0 < r_{i} < 1 \\ e_{i} > 0 \\ q_{i} > 0 \\ i = 1, 2, 3, 4, 5, 6 \\ \dots \end{cases}$$
(5)

3.2. Different Emission Reduction Policy Scenarios

This research will comprehensively follow the emission reduction scenario settings of the previous study [14,44,45] and set some scenario parameters in this section. (It should be pointed out that neither the author's previous research nor the CO₂ emission reduction policy mentioned in this paper has achieved large-scale application. Only some documents involve the overall emission reduction objectives (only 2020) of the steel industry. Therefore, the combination setting of emission reduction policies and emission reduction scenarios in this section will make reasonable assumptions based on the known emission reduction targets, and also refer to some basic data obtained by the author's previous research. In the setting of emission reduction indicators, only the emission reduction target in 2020 is relatively certain (the actual production of steel products in recent years is also known), that is, the comprehensive energy consumption per ton of steel in 2020 is about 85% of the energy consumption level in 2010. Therefore, we set the CO_2 emission intensity of the iron and steel industry in 2020 to decrease by 15% compared with 2010, assume that the CO_2 emission intensity of the iron and steel industry in 2025 will decrease by 20% compared with 2010, and by 2030, the CO₂ emission intensity of the iron and steel industry will decrease by 25% compared with 2010.)

Single carbon tax policy in 2020 (if implemented)

At present, China has not implemented and promoted any carbon emission reduction policies. For comparative research, this section and the corresponding sections below will study the changes in relevant indicators in 2020 if China adopts a single carbon tax emission reduction policy. The changes in various characteristics need to be examined as the emission reduction target is 15–20%. At this time, the basic form of the overall social welfare can be expressed as:

$$W_{Case,2020} = CS + PS + T - D(E) = \int_{0}^{Q} P(q)dq - P(Q)Q + \sum_{i=1}^{6} \pi_{case,2020,i} + \sum_{i=1}^{6} T_{i} - \theta E$$

$$= \int_{0}^{Q} (\alpha - \beta q)dq - (\alpha - \beta \sum_{i=1}^{6} q_{i}) \sum_{i=1}^{6} q_{i} + \sum_{i=1}^{6} \pi_{case,2020,i} + \sum_{i=1}^{6} te_{2015,i}(1 - r_{i})q_{i} - \theta \sum_{i=1}^{6} e_{2015,i}(1 - r_{i})q_{i}$$
(6)

Mixed carbon tax policy scenario in 2025: carbon tax + subsidy.

With the continuous improvement of emission reduction targets, the pressure to reduce the emission of steel enterprises will increase, and they need to increase capital investment to reduce the CO_2 emission intensity of steel and seriously reduce the total profit of production enterprises. If the government provides rebate subsidies to the products produced by enterprises, it will greatly improve the production enthusiasm and production capacity of enterprises, which can be expressed as in Formula (7). Then, changes in various characteristics should be examined when the target is 20–25%. At this time, the basic form of the overall social welfare can be expressed as:

$$W_{Case,2025} = CS + PS + T - S - D(E) = \int_{0}^{Q} P(q) dq - P(Q) Q + \sum_{i=1}^{6} \pi_{case,2025,i} + \sum_{i=1}^{6} T_{i} - \eta \sum_{i=1}^{6} q_{i} - \theta E$$

$$= \int_{0}^{Q} (\alpha - \beta q) dq - (\alpha - \beta \sum_{i=1}^{6} q_{i}) \sum_{i=1}^{6} q_{i} + \sum_{i=1}^{6} \pi_{case,2025,i} + \sum_{i=1}^{6} te_{2015,i}(1 - r_{i})q_{i} - \eta \sum_{i=1}^{6} q_{i} - \theta \sum_{i=1}^{6} e_{2015,i}(1 - r_{i})q_{i}$$
(7)

• Multiple mixed carbon tax policy in 2030: carbon tax + subsidy + CCS

CCS (carbon capture and storage) offers another way to reduce large-scale CO_2 as the two-carbon goal continues to deepen. However, the large-scale investment and technological maturity of CCS projects are also issues of concern to businesses and governments. Likewise, as technological innovation alone is not sufficient to reduce high carbon intensity, carbon taxes and product subsidies will remain necessary policy tools. In this section and the corresponding sections below, carbon taxes, product subsidies and CCS demonstration projects (i.e., 1-2 Mt CO₂ levels) (In this section, the application of CCS is assumed only on a very small scale (1–2 MtCO₂ levels), and optimistic scenarios for its large-scale application are not discussed. Mainly based on the following viewpoints: (1) CCS technology is not mentioned in the latest national policy documents such as "Guiding Opinions on Promoting High-Quality Development of the Iron and Steel Industry" and "Implementation Plan for Carbon Peaking in the Iron and Steel Industry". Therefore, this paper maintains a cautious attitude towards the possibility of CCS technology policy implementation, and this paper believes that CCS technology will not be used on a large scale in 2030. (2) Considering the constraints of technology maturity and capital, CCS technology cannot yet become the main way to reduce CO_2 emissions, and it is not realistic to apply it to the steel industry on a large scale. From the perspective of policymakers, this paper posits that large-scale realistic scenarios are unlikely.) will be considered together. Then, the changes in various characteristics should be examined when the target is 25–30%. At this time, the basic form of overall social welfare can be expressed as:

$$W_{Case,2030} = CS + PS + T - S - D(E) - M = \int_{0}^{Q} P(q) dq - P(Q) Q + \sum_{i=1}^{6} \pi_{case,2030,i} + \sum_{i=1}^{6} T_{i} - \eta \sum_{i=1}^{6} q_{i} - \theta E - (Am + B) = \int_{0}^{Q} (\alpha - \beta q) dq - (\alpha - \beta \sum_{i=1}^{6} q_{i}) \sum_{i=1}^{6} q_{i} + \sum_{i=1}^{6} \pi_{case,2030,i} + \sum_{i=1}^{6} te_{2015,i}(1 - r_{i})q_{i} - \eta \sum_{i=1}^{6} q_{i} - \theta \sum_{i=1}^{6} e_{2015,i}(1 - r_{i})q_{i} - (Am + B)$$
(8)

3.3. Establishment of Dynamic Output Selection Model and Analysis of Local Stability The marginal profit of enterprise *i* in period *k* is obtained as:

$$\frac{\partial \pi_i(q_i(k), q_j(k))}{\partial q_i(k)} = \alpha - C_i - \beta \sum_{j=1, j \neq i}^6 q_j(k) - 2\beta q_i(k) \tag{9}$$

 q_i is taken as the decision variable. The base period profit margin is positive (negative), and the firm will increase (decrease) its output in the next period. The product output of enterprise *i* in period k + 1 is:

$$q_i(k+1) = q_i(k) + \xi_i q_i(k) \frac{\partial \pi_i(q_i(k), q_j(k))}{\partial q_i(k)}$$
(10)

Among them, $\xi_i > 0$ represents the output adjustment speed of enterprise *i*, which includes:

$$q_{1}(k+1) = q_{1}(k) + \xi_{1}q_{1}(k)[\alpha - C_{1} - \beta(q_{2}(k) + q_{3}(k) + q_{4}(k) + q_{5}(k) + q_{6}(k)) - 2\beta q_{1}(k)]$$

$$q_{2}(k+1) = q_{2}(k) + \xi_{2}q_{2}(k)[\alpha - C_{2} - \beta(q_{1}(k) + q_{3}(k) + q_{4}(k) + q_{5}(k) + q_{6}(k)) - 2\beta q_{2}(k)]$$

$$\dots$$

$$q_{6}(k+1) = q_{6}(k) + \xi_{6}q_{6}(k)[\alpha - C_{6} - \beta(q_{1}(k) + q_{2}(k) + q_{3}(k) + q_{4}(k) + q_{5}(k)) - 2\beta q_{6}(k)]$$
(11)

When the market is stable, the output of oligarchs reaches equilibrium. At this time, $q_i(k + 1) = q_i(k)$ is used to solve the fixed point of the system. That is, by solving the variation range of ξ_i (*i* = 1, 2, 3, 4, 5, 6), the stable domain of the market can be obtained (the detailed solution and derivation process can be found in Appendix A).

Then, in the space bounded by $(\xi_1, \xi_2, \xi_3, \xi_4, \xi_5, \xi_6)$, a Nash equilibrium is reached. At this point, this Nash equilibrium point is locally stable. Once an enterprise's parameter adjustment is out of the stable area, the system will bifurcate or even evolve into a chaotic state, which means equilibrium output will no longer exist.

After obtaining the stability region, in order to analyze the stability characteristics of the steel market, this paper will focus on the following two parts: (1) analysis of the factors affecting the stability region and (2) description and analysis of the system dynamic characteristics (bifurcation diagram and Lyapunov exponent).

3.4. Data Sources

The statistical data used in this paper are all from the China Statistical Yearbook [46], the China Industrial Statistical Yearbook [47], the China Energy Statistical Yearbook [48], the China Steel Yearbook [49], and the statistical yearbooks of the various provinces. Relevant economic indicators have been converted to comparable prices in 2010.

Due to the availability of data, the relevant energy consumption data and economic data of the steel industry are derived from the ferrous metal smelting and calendaring processing industry in the Statistical Yearbook. For fossil energy consumption and IPPU CO_2 accounting data, this research refers to IPCC2006 [50] and Duan et al. [51].

4. Results and Discussion

4.1. The Results of Parameter Fitting

According to the research of Duan et al. [14,15,38,44,45] and the scenario settings in Section 3.2, this part will analyze these three time points. The functional relationships and parameters in Table 3 have referred to the previous research results (Duan et al. [14,15,38,44,45], Färe et al. [52], Lee et al. [53], and Guenno and Tiezzi [54]). The values and explanations of some other major parameters are shown in Table 4. (In terms of data verification, the relevant data in this paper come from the relevant accumulated data of the author's previous research, and the production data, cost data, and product price data of enterprises all come from actual statistical data. The calculation results of some indicators have been obtained in the author's previous research. In order to save space, this section will not repeat.).

Notations	Unit	<i>i</i> = 1	<i>i</i> = 2	<i>i</i> = 3	<i>i</i> = 4	<i>i</i> = 5	<i>i</i> = 6
e _{2015,i}	tCO ₂ /t	2.3344	3.5698	2.9040	2.8779	3.2202	4.5864
a_i	-	11,661	17,208	16,932	12,952	6397.2	3485
b_i	-	-169.76	8876.7	-166.92	1483.6	502.52	421.13
c_i	Yuan	2168.2	3511.1	2165.4	3325.1	2368.7	3814.3
	Yuan, 2015	2833.15	4898.47	3453.53	4153.15	3799.03	3832.38
C	Yuan, 2020	2124.86	3918.77	2590.15	2491.89	3609.08	3640.76
$C_{0,case,k,i}$	Yuan, 2025	1699.89	2743.14	2072.12	1868.92	3067.72	3094.64
	Yuan, 2030	1444.91	2194.51	1761.30	1588.58	2454.17	2475.71

Table 4. Some major parameter values in this research.

4.2. Empirical Analysis

4.2.1. Single Carbon Tax Policy in 2020

The equilibrium output E^* of each regional enterprise with different emission reduction targets are in this scenario as shown in Table 5.

Table 5. The equilibrium output E^* of each regional enterprise (emission reduction target: 15–20%).

Emission Reduction Target	15%	16%	17%	18%	19%	20%
	2.5789	2.5803	2.5817	2.5833	2.5850	2.5867
92	0.3823	0.3793	0.3758	0.3720	0.3677	0.3629
93	2.1623	2.1619	2.1614	2.1609	2.1603	2.1597
q_4	1.7354	1.7348	1.7341	1.7333	1.7324	1.7313
95	1.1672	1.1660	1.1648	1.1634	1.1620	1.1606
	0.4867	0.4823	0.4778	0.4731	0.4683	0.4634

The unit is 100 million tons. Each element of the Jacobian matrix can be obtained, as shown in Table 6.

Emission Reduction Target	15%	16%	17%	18%	19%	20%
J ₁₁	$1 - 0.5828\xi_1$	$1 - 0.5831\xi_1$	$1 - 0.5835 \xi_1$	$1 - 0.5838 \xi_1$	$1 - 0.5842 \xi_1$	$1 - 0.5846\xi_1$
$J_{12} = J_{13} = J_{14} = J_{15} = J_{16}$	$-0.2914\xi_{1}$	$-0.2916\xi_1$	$-0.2917\xi_1$	$-0.2919\xi_1$	$-0.2921\xi_{1}$	$-0.2923\xi_1$
J_{22}	$1 - 0.0864 \xi_2$	$1 - 0.0857\xi_2$	$1 - 0.0849\xi_2$	$1 - 0.0841\xi_2$	$1 - 0.0831\xi_2$	$1 - 0.0820\xi_2$
$J_{21} = J_{23} = J_{24} = J_{25} = J_{26}$	$-0.0432\xi_2$	$-0.0429\xi_2$	$-0.0425\xi_{2}$	$-0.0420\xi_2$	$-0.0415\xi_{2}$	$-0.0410\xi_{2}$
J_{33}	$1 - 0.4887 \xi_3$	$1 - 0.4886 \xi_3$	$1 - 0.4885 \xi_3$	$1 - 0.4884 \xi_3$	$1 - 0.4888 \xi_3$	$1 - 0.4881 \xi_3$
$J_{31} = J_{32} = J_{34} = J_{35} = J_{36}$	$-0.2443\xi_{3}$	$-0.2443\xi_{3}$	$-0.2442\xi_{3}$	$-0.2442\xi_{3}$	$-0.2441\xi_3$	$-0.2440\xi_{3}$
J_{44}	$1 - 0.3922\xi_4$	$1 - 0.3921\xi_4$	$1 - 0.3919 \xi_4$	$1 - 0.3917 \xi_4$	$1 - 0.3915 \xi_4$	$1 - 0.3913\xi_4$
$J_{41} = J_{42} = J_{43} = J_{45} = J_{46}$	$-0.1961\xi_4$	$-0.1960\xi_4$	$-0.1960\xi_4$	$-0.1959\xi_4$	$-0.1958\xi_4$	$-0.1956\xi_4$
J_{55}	$1 - 0.2638 \xi_5$	$1 - 0.2635\xi_5$	$1 - 0.2632\xi_5$	$1 - 0.2629\xi_5$	$1 - 0.2626\xi_5$	$1 - 0.2623\xi_5$
$J_{51} = J_{52} = J_{53} = J_{54} = J_{56}$	$-0.1319\xi_5$	$-0.1318\xi_{5}$	$-0.1316\xi_{5}$	$-0.1315\xi_5$	$-0.1313\xi_5$	$-0.1311\xi_5$
J_{66}	$1 - 0.1100\xi_6$	$1 - 0.1090\xi_6$	$1 - 0.1080\xi_6$	$1 - 0.1069\xi_6$	$1 - 0.1058\xi_6$	$1 - 0.1047\xi_6$
$J_{61} = J_{62} = J_{63} = J_{64} = J_{65}$	$-0.0550\xi_{6}$	$-0.0545\xi_{6}$	$-0.0540\xi_{6}$	$-0.0535\xi_{6}$	$-0.0529\xi_{6}$	$-0.0524\xi_{6}$

Table 6. The Jacobian matrix J (emission reduction target: 15–20%).

From the results, the six regions are clearly divided into two parts in terms of output share. The steel outputs of North China, East China, and South Central China always occupy the top three places, and the other three regions, especially Northeast and Northwest China, produced less steel. Based on the ideas of the previous research, this section will investigate the changes in the output adjustment speed and market stability areas in North, East, and South Central China under the condition that the output adjustment speed in Northeast, Southwest, and Northwest China remain unchanged; and investigate the changes in the output adjustment speed and market stability areas the Northeast, Southwest, and Northwest China under the condition that the output adjustment speed in North, East, and South Central China remain unchanged. The same is explored below.

• The output adjustment speed of ξ_2 , ξ_5 , ξ_6 remains unchanged

As the emission reduction target is 16% (previous research has analyzed the results when the target is 15%), while ξ_2 , ξ_5 , ξ_6 are all set to 0 at the same time. The steel market stability domain composed of ξ_1 , ξ_3 , and ξ_4 is analyzed. As can be seen in Figure 1, the adjustment coefficient ξ_1 range is [0, 3.40], ξ_3 range is [0, 4.00], ξ_4 range is [0, 5.00], (the ξ value range considered in this section is [0, 5], and the actual situation will not happen if the value is too large or negative, the same below), which is basically the same as the result when the target is 15%.



Figure 1. The market stability domain ($\xi_2 = \xi_5 = \xi_6 = 0$, emission reduction target: 16%).

Similarly, when the target increases from 17% to 20%, the steel market stability domain composed of ξ_1 , ξ_3 , and ξ_4 is basically the same as when the target is 15%.

When the target is 16%, ξ_2 , ξ_5 , and ξ_6 increase from 1.00 to 5.00 (Figure 2); it can be seen that as the northeast, southwest, and northwest regions adopt positive production adjustment coefficients at the same time, the stability of the steel market gradually decreases. The changing trend of the shape of the stability region is very similar to that when the target is 15%. When ξ_2 , ξ_5 , and ξ_6 are large, the other three regions still have sufficient room for output adjustment.

However, it should be pointed out that when the target is small, the change in the stable region is almost unchanged. However, with the gradual increase in the target (take 20% as an example), the difference in the area of the stable region becomes more obvious. Take the emission reduction targets of 15% and 20%, respectively, when ξ_2 , ξ_5 , and ξ_6 are set to 5 at the same time as an example; the results are shown in Figure 3.



Figure 2. The market stability domain ($\xi_2 = \xi_5 = \xi_6 = 1 \sim 5$, emission reduction target: 16%).



Figure 3. The market stability domain ($\xi_2 = \xi_5 = \xi_6 = 5$, emission reduction target: **left** 15%, **right** 20%).

The value range of ξ_1 is increased from [0, 1.275] to [0, 1.325], the value range of ξ_3 is increased from [0, 1.500] to [0, 1.600], and the value range of ξ_4 is increased from [0, 1.900] to [0, 2.025]. Judging from the results, the area of the stability region shows an increasing trend as the target increases. It shows that under the combined effect of the carbon tax and the output adjustment policy of smaller output enterprises, the larger output enterprises' output adjustment policies will show an increasing trend.

• The output adjustment speed of ξ_1 , ξ_3 , ξ_4 remains unchanged

As the emission reduction target is 16% (previous research has analyzed the results when the target is 15%), and ξ_1 , ξ_3 , ξ_4 are both set to 0, the steel market stability domain composed of ξ_2 , ξ_5 , and ξ_6 is analyzed. As can be seen in Figure 4, the range of ξ_2 is [0, 10.00], ξ_5 is [0, 7.50], ξ_6 is [0, 10.00], or even more. The value range of ξ considered in this section is [0, 10], which is basically the same as the result when the target is 15%.



Figure 4. The market stability domain ($\xi_1 = \xi_3 = \xi_4 = 0$, emission reduction target: 16%).

Similarly, when the target is gradually increased from 17% to 20%, the market stability domain composed of ξ_2 , ξ_5 , and ξ_6 is basically the same as when the target is 15%.

When the target is 16%, ξ_1 , ξ_3 , and ξ_4 simultaneously increase from 0.50 to 2.00 (Figure 5), it can be seen that when the North, East, and South Central China adopt positive production adjustment coefficients at the same time, the stability of the steel market gradually decreases. It can be clearly found that when ξ_1 , ξ_3 , ξ_4 take small positive values, Northeast China, Southwest China, and Northwest China still have greater autonomy in decision-making. However, when ξ_1 , ξ_3 , ξ_4 gradually increase, the stable area of the entire steel market will shrink sharply. When ξ_1 , ξ_3 , ξ_4 are 2, the value range of ξ_2 , ξ_5 , ξ_6 is very small. Obviously, when ξ_1 , ξ_3 , ξ_4 keep increasing, the market is easily out of balance.



Figure 5. Stability domain of the market ($\xi_1 = \xi_3 = \xi_4 = 0.5 \sim 2$, emission reduction target: 16%).

Similarly, the shape and change trends of the stable region are very similar, and when the target is small (close to 15%), the change in the stable region is almost unchanged. However, when the target is high (take 20% as an example), the difference in the area of the stable region becomes more obvious. Take the emission reduction targets of 15% and 20%, respectively, and when ξ_1 , ξ_3 , and ξ_4 take 1.5 at the same time as an example, the results are shown in Figure 6.



Figure 6. The market stability domain ($\xi_1 = \xi_3 = \xi_4 = 1.5$, emission reduction target: **left** 15%, **right** 20%).

The value range of ξ_2 is still maintained at [0, 10] (but through further calculations, the upper limit is increased), the value range of ξ_5 is increased from [0, 3.60] to [0, 3.70], the value range of ξ_6 is increased from [0, 8.80] to [0, 9.20]. Judging from the results, the area of the stability region shows an increasing trend as the target increases. It means that under the combined effect of the single carbon tax and larger output enterprises' output adjustment policies, the smaller output enterprises' output adjustment policies will also increase.

System dynamic characteristics analysis

According to the previous research, this section selects two groups of representative enterprises: North China (representing larger output enterprises) and Southwest China (representing smaller output enterprises). Therefore, in this section, we will discuss ξ_1 , ξ_5 and the change impacts on system stability (we actually calculated all the results with a reduction target of 15–20%, but due to space limitations, this section uses a reduction target of 20% as an example). The results are shown in Figures 7–10.



Figure 7. The bifurcation diagram of ξ_1 (left: $\xi_2 \sim \xi_6 = 0$, right: $\xi_2 \sim \xi_6 = 0.4$, the reduction target is 20%).



Figure 8. The bifurcation diagram of ξ_5 (left: $\xi_1, \xi_2, \xi_3, \xi_4, \xi_6 = 0$, right: $\xi_1, \xi_2, \xi_3, \xi_4, \xi_6 = 1.5$, the reduction target is 20%).



Figure 9. The Lyapunov exponent diagram (**left**: $\xi_2 \sim \xi_6 = 0$, **right**: $\xi_2 \sim \xi_6 = 0.4$, the reduction target is 20%).



Figure 10. The Lyapunov exponent diagram (**left**: ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 0$, **right**: ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 1.5$, the reduction target is 20%).

From Figure 7, some results can be obtained: when $\xi_2 \sim \xi_6 = 0$ (left), the system is stable as ξ_1 is in the range of [0, 3.520]. Then, there is a small interval in which q_1 is unstable. When the value increases to 3.530, the system is no longer balanced and transitions from stable to double-cycle to chaos, but only North China has an output imbalance. When $\xi_2 \sim \xi_6 = 0.4$ (right), the system is stable as ξ_1 is below 3.265. There is then a small interval in which q_1 production is unstable. When the value increases to 3.270, the system is no longer balanced and transitions from stable to double-cycle to chaos. However, the output of other regions appears unbalanced as ξ_1 gradually increases.

This shows that the system is more likely to fall into an unbalanced state when multiple enterprises use dynamic output adjustment at the same time instead of a single enterprise adopting output adjustment. Compared with the previous study (the target is 15%), the bifurcation value of ξ_1 has increased (the results of the first bifurcation in the previous study are 3.230 and 3.250, respectively), which also verifies this conclusion: as the emission reduction target gradually increases, enterprises with a larger output can implement more adjustment policies without causing the system to fall into a state of bifurcation or even chaos.

From Figure 8, when $\xi_1, \xi_2, \xi_3, \xi_4, \xi_6 = 0$ (left), the system remains in equilibrium regardless of ξ_5 . When $\xi_1, \xi_2, \xi_3, \xi_4, \xi_6$ are at 1.5 (right), the system is stable as ξ_5 is below 3.395. There is then a small interval in which all enterprises' production is unstable. When the value increases to 3.410, the system is no longer balanced and transitions from stable to double-cycle to chaos. Similarly, compared with the previous study (the target is 15%), the bifurcation value of ξ_5 has increased (the results of the bifurcation for the first time in the previous study was 3.100), which also verifies the following conclusion: as the emission reduction target gradually increases, enterprises with smaller output can also implement more output adjustment policies without causing the system to fall into a state of bifurcation or even chaos.

From the results of Figures 7 and 8, the larger output enterprises can have a much greater impact on the system balance than those smaller output enterprises, and misadjusted adjustment of output by these larger producers will easily create market imbalance. With the gradually increasing emission reduction targets, the enterprises' policies of output adjustment could be more flexible and diverse, and the system will be in a state of bifurcation and chaos.

Figures 9 and 10 show the Lyapunov exponents for Figures 7 and 8. When $\xi_2 \sim \xi_6 = 0$ and $\xi_1 = 3.520$ (left in Figure 9), the system shows bifurcation. When $\xi_1 > 4.395$, the maximum Lyapunov exponent changes from negative to positive, and the system is in chaos. When $\xi_2 \sim \xi_6$ are 0.4 and $\xi_1 = 3.265$ (right in Figure 9), bifurcation appears and then all enterprises bifurcate. When $\xi_1 > 4.545$, the maximum Lyapunov exponent changes from negative to positive, and the system becomes chaotic.

When ξ_1 , ξ_2 , ξ_3 , ξ_4 , ξ_6 are 0 (left in Figure 10), the maximum Lyapunov exponent is always negative. When ξ_1 , ξ_2 , ξ_3 , ξ_4 , ξ_6 equal 1.5 (right in Figure 10) and ξ_5 range from 3.095 to 3.450, the maximum Lyapunov exponent changes from negative to positive, and there are bifurcations in various regions. When $\xi_5 > 3.455$, the maximum Lyapunov exponent is no longer positive, while the system becomes double-cycle.

4.2.2. Mixed Carbon Tax Policy Scenario in 2025: Carbon Tax + Subsidy

In this scenario, the equilibrium output E^* of each regional enterprise with different emission reduction targets are as shown in Table 7.

Emission Reduction Target	20%	21%	22%	23%	24%	25%
q_1	2.4978	2.5017	2.5057	2.5099	2.5140	2.5184
q_2	0.9221	0.9176	0.9126	0.9071	0.9012	0.8947
93	2.1472	2.1481	2.1488	2.1496	2.1502	2.1508
q_4	1.8109	1.8113	1.8117	1.8119	1.8121	1.8122
95	1.1672	1.1675	1.1677	1.1681	1.1685	1.1689
96	0.4669	0.4639	0.4611	0.4585	0.4563	0.4544

Table 7. The equilibrium output *E** of each regional enterprise (emission reduction target: 20–25%).

And the Jacobian matrix J obtained are as shown in Table 8.

Emission Reduction Target	20%	21%	22%	23%	24%	25%
J_{11}	$1 - 0.5645 \xi_1$	$1 - 0.5654 \xi_1$	$1 - 0.5663 \xi_1$	$1 - 0.5672\xi_1$	$1 - 0.5682 \xi_1$	$1 - 0.5692\xi_1$
$J_{12} = J_{13} = J_{14} = J_{15} = J_{16}$	$-0.2823\xi_1$	$-0.2827\xi_1$	$-0.2831\xi_1$	$-0.2836\xi_1$	$-0.2841\xi_1$	$-0.2846\xi_1$
J ₂₂	$1 - 0.2084 \xi_2$	$1 - 0.2074\xi_2$	$1 - 0.2062\xi_2$	$1 - 0.2050\xi_2$	$1 - 0.2037 \xi_2$	$1 - 0.2022\xi_2$
$J_{21} = J_{23} = J_{24} = J_{25} = J_{26}$	$-0.1042\xi_2$	$-0.1037\xi_2$	$-0.1031\xi_2$	$-0.1025\xi_2$	$-0.1018\xi_{2}$	$-0.1011\xi_2$
J ₃₃	$1 - 0.4853\xi_3$	$1 - 0.4855\xi_3$	$1 - 0.4856\xi_3$	$1 - 0.4858 \xi_3$	$1 - 0.4860 \xi_3$	$1 - 0.4861\xi_3$
$J_{31} = J_{32} = J_{34} = J_{35} = J_{36}$	$-0.2426\xi_{3}$	$-0.2427\xi_{3}$	$-0.2428\xi_{3}$	$-0.2429\xi_{3}$	$-0.2430\xi_{3}$	$-0.2430\xi_{3}$
J_{44}	$1 - 0.4093 \xi_4$	$1 - 0.4094 \xi_4$	$1 - 0.4094 \xi_4$	$1 - 0.4095 \xi_4$	$1 - 0.4095 \xi_4$	$1 - 0.4096 \xi_4$
$J_{41} = J_{42} = J_{43} = J_{45} = J_{46}$	$-0.2046\xi_4$	$-0.2047\xi_4$	$-0.2047\xi_4$	$-0.2047\xi_4$	$-0.2048\xi_4$	$-0.2048\xi_4$
J_{55}	$1 - 0.2638 \xi_5$	$1 - 0.2638\xi_5$	$1 - 0.2639\xi_5$	$1 - 0.2640\xi_5$	$1 - 0.2641 \xi_5$	$1 - 0.2642\xi_5$
$J_{51} = J_{52} = J_{53} = J_{54} = J_{56}$	$-0.1319\xi_5$	$-0.1319\xi_5$	$-0.1320\xi_5$	$-0.1320\xi_{5}$	$-0.1320\xi_5$	$-0.1321\xi_5$
J_{66}	$1 - 0.1055\xi_6$	$1 - 0.1048\xi_6$	$1 - 0.1042\xi_6$	$1 - 0.1036 \xi_6$	$1 - 0.1031\xi_6$	$1 - 0.1027\xi_6$
$J_{61} = J_{62} = J_{63} = J_{64} = J_{65}$	$-0.0528\xi_{6}$	$-0.0524\xi_{6}$	$-0.0521\xi_{6}$	$-0.0518\xi_{6}$	$-0.0516\xi_{6}$	$-0.0513\xi_{6}$

Table 8. The Jacobian matrix J (emission reduction target: 20–25%).

In order to facilitate discussion and save space, this section only discusses the relevant calculation results under the scenarios of 20% and 25% emission reductions.

• The output adjustment speed of ξ_2 , ξ_5 , ξ_6 remains unchanged

As the emission reduction target is 20%, and ξ_2 , ξ_5 , and ξ_6 take 0 at the same time, the steel market stability domain composed of ξ_1 , ξ_3 , and ξ_4 is analyzed. As can be seen in Figure 11, the adjustment coefficient ξ_1 range is [0, 3.50], ξ_3 range is [0, 4.05], and ξ_4 range is [0, 4.80].



Figure 11. The market stability ($\xi_2 = \xi_5 = \xi_6 = 0$, emission reduction target: 20%).

When the target is 20%, ξ_2 , ξ_5 , ξ_6 change from 1.00 to 5.00 (Figure 12), and the stable area is gradually decreasing. The changing trend of its shape is very similar to that of a single carbon tax policy. However, the difference is that when the values of ξ_2 , ξ_5 , and ξ_6 are large (=4), there is still room for output adjustment in the other three regions, but compared to only a single carbon tax scenario, the area of its stability region has been greatly reduced, but when ξ_2 , ξ_5 , and ξ_6 continue to increase to 5, there is not much stability in the region left. It means that with the introduction of the mixed emission reduction policies, enterprises' output adjustment policies have been compressed, and enterprises with larger output have to carefully consider their next production strategy to avoid the entire steel market falling into an imbalance.



Figure 12. The market stability domain ($\xi_2 = \xi_5 = \xi_6 = 1 \sim 5$, emission reduction target: 20%).

On the other hand, the area difference of the stability region becomes more obvious when the targets gradually increase. For a clear comparison, this part takes emission reduction targets of 20% and 25%, respectively, when ξ_2 , ξ_5 , and ξ_6 are set to 5 at the same time as an example, as shown in Figure 13.



Figure 13. The market stability domain ($\xi_2 = \xi_5 = \xi_6 = 5$, emission reduction target: **left** 20%, **right** 25%).

From Figure 13, the stability domain, which is almost nonexistent, becomes significantly larger when the target increases from 20% to 25%. The value range of ξ_1 is expanded to [0, 0.125], the value range of ξ_3 is expanded to [0, 0.150], and the value range of ξ_4 is expanded to [0, 0.200]. This shows that even if there is a mixed emission reduction policy, under the combined effect of the emission reduction policy and the output adjustment policy of an enterprise with a smaller output, as the target gradually increases, the output adjustment policies that enterprises with larger output will show an increasing trend.

• The output adjustment speed of ξ_1 , ξ_3 , ξ_4 remains unchanged

As the emission reduction target is 20%, and ξ_1 , ξ_3 , and ξ_4 are taken as 0 at the same time, the steel market stability domain composed of ξ_2 , ξ_5 , and ξ_6 is analyzed. As can be seen in Figure 14, the adjustment coefficient ξ_2 range is [0, 9.50], ξ_5 range is [0, 7.50], and ξ_6 range is [0, 10.00], or even more.



Figure 14. The market stability domain ($\xi_1 = \xi_3 = \xi_4 = 0$, emission reduction target: 20%).

Figure 15 shows that when the target is 20%, the steel market stability domain of ξ_1 , ξ_3 , and ξ_4 increase from 0.50 to 2.00.



Figure 15. The market stability domain ($\xi_1 = \xi_3 = \xi_4 = 0.5 \sim 2$, emission reduction target: 20%).

From the results, the stability domain is gradually decreasing, but the difference is that the decrease in the area of the stability region under this scenario is even more dramatic. For example, when ξ_1 , ξ_3 , and ξ_4 take 1.5, the output adjustment space of the other three regions is as follows: ξ_2 is [0, 4.70], ξ_5 is [0, 3.70], ξ_6 is [0, 9.20]; compared to only a single carbon tax scenario (the target is 20%), the area of its stability area has been greatly reduced. When the values of ξ_1 , ξ_3 , and ξ_4 are larger, it is foreseeable that the moment of system imbalance will be earlier than in the situation where there is only a single carbon tax policy scenario (the target is 20%).

Similarly, when the target is increased from 20% to 25%, when ξ_1 , ξ_3 , and ξ_4 take 1.5 at the same time, the value range of ξ_2 is increased from [0, 4.70] to [0, 4.80], the value range of ξ_5 is maintained at [0, 3.70], and the value range of ξ_6 is increased from [0, 9.20] to [0, 9.40]. When ξ_1 , ξ_3 , and ξ_4 take other smaller values, there is a similar rule. However, when ξ_1 , ξ_3 , and ξ_4 take larger values at the same time (and there is a stable region), the conclusion is different. When the target increases from 20% to 25%, ξ_1 , ξ_3 , and ξ_4 take 2, and the value range of ξ_2 and ξ_5 is maintained in the interval of [0, 0.40] and [0, 0.30], but the value range of ξ_6 is reduced from [0, 0.80] to [0, 0.70]. These results are shown in Figures 16 and 17.



Figure 16. The market stability domain ($\xi_1 = \xi_3 = \xi_4 = 1.5$, emission reduction target: **left** 20% (2020), **middle** 20% (2025), **right** 25%).



Figure 17. The market stability domain ($\xi_1 = \xi_3 = \xi_4 = 2$, emission reduction target: **left** 20% (2020), **middle** 20% (2025), **right** 25%).

This illustrates that when the government adopts a mix of emission reduction policies, under the combined effect of these policies and output adjustment policy of the larger output enterprise, the smaller output enterprise adjustment policy will be restricted or affected by more factors. The rule of change is different from that of a single carbon tax scenario, which means that enterprises with smaller outputs need to be more cautious in formulating their own production plans to ensure that the enterprises themselves and the entire steel market will not fall into an imbalanced state.

System dynamic characteristics analysis

In this section, we have calculated all the results with a reduction target of 20–25%, but due to space limitations, this section uses a reduction target of 25% as an example for discussion.

From Figure 18, some results can be obtained: when $\xi_2 \sim \xi_6 = 0$ (left), the system is stable as ξ_1 is in the range of [0, 3.625]. Then, there is a small interval wherein q_1 is unstable. When the value increases to 3.630, the system is no longer balanced and transitions from stable to double-cycle to chaos, but only North China has an output imbalance. When $\xi_2 \sim \xi_6 = 0.4$ (right), the system is stable as ξ_1 is below 3.345. Then, there is a small interval in which the q_1 production is unstable. When the value increases to 3.350, the system is no longer balanced and transitions from stable to double-cycle to chaos. However, the output of other regions appears unbalanced as ξ_1 gradually increases.



Figure 18. The bifurcation diagram of ξ_1 (left: $\xi_2 \sim \xi_6 = 0$, right: $\xi_2 \sim \xi_6 = 0.4$, the reduction target is 25%).

From Figure 19, when ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 0$ (left), the system remains in equilibrium regardless of ξ_5 . When ξ_1 , ξ_2 , ξ_3 , ξ_4 , ξ_6 are at 1.5 (right), the system is stable as ξ_5 is below 2.950. Then, there is a small interval in which all enterprises' production is unstable. When the value increases to 2.970, the system is no longer balanced and transitions from stable to double-cycle to chaos.



Figure 19. The bifurcation diagram of ξ_5 (left: ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 0$, right: ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 1.5$, the reduction target is 25%).

Figures 20 and 21 show the Lyapunov exponents for Figures 18 and 19. When $\xi_2 \sim \xi_6 = 0$ and $\xi_1 = 3.625$ (left in Figure 20), the system shows bifurcation. When $\xi_1 > 4.505$, the maximum Lyapunov exponent changes from negative to positive, and the system is in chaos. When $\xi_2 \sim \xi_6$ are 0.4 and $\xi_1 = 3.345$ (right in Figure 20), bifurcation appears and then all enterprises bifurcate. When $\xi_1 > 4.655$, the maximum Lyapunov exponent changes from negative to positive, and the system becomes chaotic.



Figure 20. The Lyapunov exponent diagram (left: $\xi_2 \sim \xi_6 = 0$, right: $\xi_2 \sim \xi_6 = 0.4$, the reduction target is 25%).



Figure 21. The Lyapunov exponent diagram (left: ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 0$, right: ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 1.5$, the reduction target is 25%).

When ξ_1 , ξ_2 , ξ_3 , ξ_4 , ξ_6 are 0 (left in Figure 21), the maximum Lyapunov exponent is always negative. When ξ_1 , ξ_2 , ξ_3 , ξ_4 , ξ_6 equal 1.5 (right in Figure 21) and ξ_5 range from 2.590 to 3.060, the maximum Lyapunov exponent changes from negative to positive, and there are bifurcations in various regions. When $\xi_5 > 3.065$, the maximum Lyapunov exponent is no longer positive, while the system becomes double-cycle.

4.2.3. Multiple Mixed Carbon Tax Policy Implemented in 2030: Carbon Tax + Subsidy + CCS

In this scenario, the equilibrium output E^* of each regional enterprise with different emission reduction targets are as shown in Table 9.

Emission Reduction Target	25%	26%	27%	28%	29%	30%
91	2.4158	2.4198	2.4239	2.4280	2.4321	2.4361
92	1.0427	1.0359	1.0287	1.0210	1.0128	1.0043
93	2.0944	2.0947	2.0950	2.0951	2.0950	2.0948
94	1.7284	1.7283	1.7280	1.7277	1.7271	1.7265
95	1.3805	1.3810	1.3815	1.3822	1.3828	1.3835
q_6	0.6691	0.6680	0.6674	0.6673	0.6676	0.6685

Table 9. The equilibrium output E^* of each regional enterprise (emission reduction target: 25–30%).

And the Jacobian matrix J obtained are as shown in Table 10.

Table 10. The Jacobian matrix J (emission reduction target: 25–30%).

Emission Reduction Target	25%	26%	27%	28%	29%	30%
J_{11}	$1 - 0.5460\xi_1$	$1 - 0.5469\xi_1$	$1 - 0.5478 \xi_1$	$1 - 0.5487 \xi_1$	$1 - 0.5497\xi_1$	$1 - 0.5506\xi_1$
$J_{12} = J_{13} = J_{14} = J_{15} = J_{16}$	$-0.2730\xi_1$	$-0.2734\xi_1$	$-0.2739\xi_1$	$-0.2744\xi_1$	$-0.2748\xi_{1}$	$-0.2753\xi_1$
J ₂₂	$1 - 0.2357\xi_2$	$1 - 0.2341\xi_2$	$1 - 0.2325\xi_2$	$1 - 0.2307\xi_2$	$1 - 0.2289 \xi_2$	$1 - 0.2270\xi_2$
$J_{21} = J_{23} = J_{24} = J_{25} = J_{26}$	$-0.1178\xi_2$	$-0.1171\xi_2$	$-0.1162\xi_2$	$-0.1154\xi_2$	$-0.1145\xi_{2}$	$-0.1135\xi_2$
J ₃₃	$1 - 0.4733\xi_3$	$1 - 0.4734\xi_3$	$1 - 0.4735\xi_3$	$1 - 0.4735\xi_3$	$1 - 0.4735 \xi_3$	$1 - 0.4734 \xi_3$
$J_{31} = J_{32} = J_{34} = J_{35} = J_{36}$	$-0.2367\xi_3$	$-0.2367\xi_{3}$	$-0.2367\xi_{3}$	$-0.2367\xi_{3}$	$-0.2367\xi_{3}$	$-0.2367\xi_{3}$
J_{44}	$1 - 0.3906 \xi_4$	$1 - 0.3906 \xi_4$	$1 - 0.3905\xi_4$	$1 - 0.3904\xi_4$	$1 - 0.3903\xi_4$	$1 - 0.3902\xi_4$
$J_{41} = J_{42} = J_{43} = J_{45} = J_{46}$	$-0.1953\xi_4$	$-0.1953\xi_4$	$-0.1953\xi_4$	$-0.1952\xi_4$	$-0.1952\xi_4$	$-0.1951\xi_4$
J_{55}	$1 - 0.3120\xi_5$	$1 - 0.3121\xi_5$	$1 - 0.3122\xi_5$	$1 - 0.3124\xi_5$	$1 - 0.3125\xi_5$	$1 - 0.3127\xi_5$
$J_{51} = J_{52} = J_{53} = J_{54} = J_{56}$	$-0.1560\xi_5$	$-0.1560\xi_5$	$-0.1561\xi_5$	$-0.1562\xi_5$	$-0.1563\xi_{5}$	$-0.1563\xi_5$
J ₆₆	$1 - 0.1512\xi_6$	$1 - 0.1510\xi_6$	$1 - 0.1508\xi_6$	$1 - 0.1508\xi_6$	$1 - 0.1509\xi_6$	$1 - 0.1511\xi_6$
$J_{61} = J_{62} = J_{63} = J_{64} = J_{65}$	$-0.0756\xi_{6}$	$-0.0755\xi_{6}$	$-0.0754\xi_{6}$	$-0.0754\xi_{6}$	$-0.0754\xi_{6}$	$-0.0755\xi_{6}$

In order to facilitate discussion and save space, this section only discusses the relevant calculation results under the scenarios of 25% and 30% emission reductions.

• The output adjustment speed of ξ_2 , ξ_5 , ξ_6 remains unchanged

As the emission reduction target is 25%, and ξ_2 , ξ_5 , and ξ_6 take 0 at the same time, the steel market stability domain composed of ξ_1 , ξ_3 , and ξ_4 is analyzed. As can be seen in Figure 22, the adjustment coefficient ξ_1 range is [0, 3.60], ξ_3 range is [0, 4.15], and ξ_4 range is [0, 5.00].



Figure 22. The market stability domain ($\xi_2 = \xi_5 = \xi_6 = 0$, emission reduction target: 25%).

When the target is 25%, ξ_2 , ξ_5 , and ξ_6 change from 1.00 to 4.00 (Figure 23), and the stable area is gradually decreasing. The changing trend of its shape is very similar to that of the mixed carbon tax policy (carbon tax+ subsidy, scenario 2025). However, the difference is that when the values of ξ_2 , ξ_5 , and ξ_6 are large (=4), there is still room for output adjustment in the other three regions, but compared to the mixed carbon tax policy scenario (emission reduction target = 25%), the area of its stability region has been greatly reduced; when ξ_2 , ξ_5 , and ξ_6 continue to increase to 5, there is no longer a stable region. It means that with the implementation of multiple emission reduction strategies to avoid output adjustment strategies that would spur the entire steel market into imbalance.

On the other hand, the area difference of the stability region becomes more obvious when the targets gradually increase. For a clear comparison, this part takes emission reduction targets of 25% and 30%, respectively, when ξ_2 , ξ_5 , and ξ_6 are taken as 4 at the same time as an example, as shown in Figure 24.



Figure 23. The market stability domain ($\xi_2 = \xi_5 = \xi_6 = 1 \sim 4$, emission reduction target: 25%).



Figure 24. The market stability domain ($\xi_2 = \xi_5 = \xi_6 = 4$, emission reduction target: **left** 25%, **right** 30%).

As shown in Figure 24, the stability domain, which is very small, became significantly larger when the target increases from 25% to 30%. The value range of ξ_1 is increased from [0, 0.35] to [0, 0.45], the value range of ξ_3 is increased from [0, 0.45] to [0, 0.50], and the value range of ξ_4 is increased from [0, 0.50] to [0, 0.60]. This also shows that even if there are more complex mixed emission reduction policies, under the combined effect of the emission reduction policy and the output adjustment policy of an enterprise with a smaller output, as the target gradually increases, the output adjustment policies that enterprises with larger output will show an increasing trend.

• The output adjustment speed of ξ_1 , ξ_3 , ξ_4 remains unchanged

As the emission reduction target is 25% and ξ_1 , ξ_3 , and ξ_4 are taken as 0 at the same time, the steel market stability domain composed of ξ_2 , ξ_5 , and ξ_6 is analyzed. As can be seen in Figure 25, the adjustment coefficient ξ_2 range is [0, 8.30], ξ_5 range is [0, 6.30], ξ_6 range is [0, 10.00], or even more, which is smaller than the scenario of carbon tax+ subsidy policy with an emission reduction target of 25%. This suggests that when introducing the



multiple emission reduction policies, production plans of enterprises with smaller output will be affected more obviously.





Figure 26. The market stability domain ($\xi_1 = \xi_3 = \xi_4 = 0.5 \sim 2$, emission reduction target: 25%).

From the results, the overall stability domain shows a gradual decreasing trend, but compared with the previous, the conclusion is slightly different. For example, when ξ_1 , ξ_3 , and ξ_4 take 1.5, the output adjustment space of the other three regions is as follows: ξ_2 is [0, 4.40], ξ_5 is [0, 3.30], ξ_6 is [0, 6.90]; compared to the scenario of carbon tax+ subsidy (emission reduction target of 25%), the area of its stability area has been greatly reduced.

However, when the values of ξ_1 , ξ_3 , and ξ_4 are larger (=2), the area of the stability region is larger than the scenario of the carbon tax+ subsidy (the target is 25%). When ξ_1 , ξ_3 , and ξ_4 continue to increase, the system will enter a state of imbalance, but the moment of system imbalance will be later than the scenario of the carbon tax+ subsidy (the target is 25%).

Similarly, when the target increases from 25% to 30% and when ξ_1 , ξ_3 , and ξ_4 take 1.5 at the same time, the value range of ξ_2 is increased from [0, 4.40] to [0, 4.50], the value range of ξ_5 is maintained at [0, 3.30], and the value range of ξ_6 is maintained at [0, 6.90]. When ξ_1 , ξ_3 , and ξ_4 are other smaller values, there is a similar rule. However, when ξ_1 , ξ_3 , and ξ_4 take larger values at the same time (and there is a stable region), the conclusion is different. When the target is increased from 25% to 30%, and when ξ_1 , ξ_3 , and ξ_4 take 2 at the same time, the value range of ξ_2 is maintained in the interval of [0, 1.10], but the value range of ξ_5 is reduced from [0, 0.80] to [0, 0.70], and the value range of ξ_6 is reduced from [0, 1.60] to [0, 1.50]. These results are shown in Figures 27 and 28.



Figure 27. The market stability domain ($\xi_1 = \xi_3 = \xi_4 = 1.5$, emission reduction target: **left** 25% (2025), **middle** 25% (2030), **right** 30%).



Figure 28. The market stability domain ($\xi_1 = \xi_3 = \xi_4 = 2$, emission reduction target: **left** 25% (2025), **middle** 25% (2030), **right** 30%).

This also shows that with the implementation of more complex mixed emission reduction policies, under the combined effect of emission reduction policies and output adjustment policies of larger output enterprises, the smaller output enterprise adjustment policy will be restricted by more factors. The rule of change is different from that of a single carbon tax scenario. This means that enterprises with smaller outputs need to be more cautious in formulating their own production plans to ensure that the enterprises themselves and the entire steel market will not fall into an unbalanced state.

System dynamic characteristics analysis

In this section, we have actually calculated all the results where the emission reduction target is 25–30%, but due to space limitations, this section takes the emission reduction target of 30% as an example for discussion.

From Figure 29, some results can be obtained: when $\xi_2 \sim \xi_6 = 0$ (left), the system is stable as ξ_1 is in the range of [0, 3.730]. There is then a small interval where q_1 is unstable. When the value increases to 3.735, the system is no longer balanced and transitions from stable to double-cycle to chaos, but only North China has output imbalance. When $\xi_2 \sim \xi_6 = 0.4$ (right), the system is stable as ξ_1 is below 3.415. There is then a small interval in which q_1 production is unstable. When the value increases to 3.420, the system is no longer balanced and transitions from stable to double-cycle to chaos. However, the output of other regions appears unbalanced as ξ_1 gradually increases.



Figure 29. The bifurcation diagram of ξ_1 (left: $\xi_2 \sim \xi_6 = 0$, right: $\xi_2 \sim \xi_6 = 0.4$, the reduction target is 30%).

From Figure 30, when ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 0$ (left), the system remains in equilibrium regardless of ξ_5 . When ξ_1 , ξ_2 , ξ_3 , ξ_4 , ξ_6 are at 1.5 (right), the system is stable as ξ_5 is below 2.450. There is then a small interval in which all enterprises' production is unstable. When the value increases to 2.465, the system is no longer balanced and transitions from stable to double-cycle to chaos.



Figure 30. The bifurcation diagram of ξ_5 (**left**: ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 0$, **right**: ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 1.5$, the reduction target is 30%).

Figures 31 and 32 show the Lyapunov exponents for Figures 29 and 30. When $\xi_2 \sim \xi_6 = 0$ and $\xi_1 = 3.730$ (left in Figure 31), the system shows bifurcation. When $\xi_1 > 4.655$, the maximum Lyapunov exponent changes from negative to positive, and the system is in chaos. When $\xi_2 \sim \xi_6$ are 0.4 and $\xi_1 = 3.415$ (right in Figure 31), bifurcation appears and then all enterprises bifurcate. When $\xi_1 > 4.805$, the maximum Lyapunov exponent starts to be positive, and the system becomes chaotic.



Figure 31. The Lyapunov exponent diagram (left: $\xi_2 \sim \xi_6 = 0$, right: $\xi_2 \sim \xi_6 = 0.4$, the reduction target is 30%).



Figure 32. The Lyapunov exponent diagram (**left**: ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 0$, **right**: ξ_1 , ξ_2 , ξ_3 , ξ_4 , $\xi_6 = 1.5$, the reduction target is 30%).

When ξ_1 , ξ_2 , ξ_3 , ξ_4 , ξ_6 are 0 (left in Figure 32), the maximum Lyapunov exponent is always negative. When ξ_1 , ξ_2 , ξ_3 , ξ_4 , ξ_6 equal 1.5 (right in Figure 32) and ξ_5 ranges from 2.165 to 2.535, the maximum Lyapunov exponent changes from negative to positive, and there are bifurcations in various regions. When $\xi_5 > 2.540$, the maximum Lyapunov exponent is no longer positive, while the system becomes double-cycle.

4.3. Further Discussions

Different from the author's previous research [38], this paper calculates the changes in various indicators in the steel market under multiple emission reduction policies and multiple emission reduction targets, and makes corresponding comparisons. This paper does not discuss the optimal emissions intensity. Only the aforementioned three scenarios were analyzed. Moreover, because of certain assumptions in the model, there were some gaps between the calculations and the actual results, but some trends and rules can still be found and identified.

From the calculation results, it can be found that the optimal output obtained by the output selection model of the iron and steel industry is the equilibrium output under the condition of market stability. In terms of production areas, the optimal output obtained by the model is also consistent with the current basic distribution of China's steel industry. That is to say, the optimal output in North China, East China, and Central and South China is much larger than that in other regions, and its impact on the market and production adjustment strategies have always been the focus of government departments. In other regions, because of its low market share, the impact on the market is not obvious. Therefore, in order to make the research conclusions more comparative and representative, the research on the changes in emission reduction targets, the research on the combination of emission

reduction policies, and the research on production adjustment strategies are all based on the two major areas with large output (North China, Northeast China, Central South China) and areas with small production (Northeast China, Southwest China, Northwest China).

For the optimal output of the model, the author's previous research has carried out detailed calculations; this paper does not discuss it, but focuses on the impact of the adjustment of bounded rational production strategies in various regions of the steel market.

In general, changes in the production adjustment strategies of enterprises directly affect the stability of the steel market. Whether the enterprise with a large output or with a small output, excessive production adjustment strategies will affect the stability of the market. However, the possibility of market imbalance is very small (the unit of production adjustment strategy in this paper is 100 million tons, which is almost impossible for enterprises and is almost completely "unreasonable" only for more obvious and outstanding results and calculated). Therefore, for enterprises, the research on the combination of carbon emission reduction goals and carbon emission reduction strategies affects the production decisions of enterprises to a certain extent.

For North China, East China, and Central South China, since their steel production bases will not be fundamentally relocated and eliminated for a long period of time in the future, their market share will still occupy a considerable proportion. From the calculation results, the increase in CO_2 emission reduction targets affects the output of North China, East China, and Central South China but increases the production adjustment strategy of these regions, that is, they can adopt more flexible production plans. Obviously, under the dual carbon goal, it is most important for steel enterprises in these regions to complete the corresponding emission reduction plans (the requirements of emission reduction policy combination can be ignored to a certain extent). Previous studies [14,44,54] have conducted corresponding studies on the choice of CO_2 emission reduction strategies.

For the northeast, southwest and northwest regions, although the possibility of market imbalance is also less, it cannot be ruled out that due to the low market share and poor profits of these enterprises, the decision makers of these enterprises may take "life-threatening" expansion of production, and the final result will cause market imbalance. Of course, in most cases, the production adjustment plans of iron and steel enterprises in the Northeast, Southwest, and Northwest regions are relatively stable. Therefore, under the dual carbon goal, for iron and steel enterprises in the northeast, southwest, and northwest regions, implementing a simple combination of CO_2 emission reduction policies is more conducive to market stability and the realization of emission reduction goals.

5. Research Conclusions and Recommendations

This paper constructs a repeated dynamic game model and introduces the carbon tax mechanism and bounded rationality expectation strategy. Then the output selection and market stability of steel oligarchs under multiple emission reduction targets and policies are analyzed, and the dynamic production adjustment and market imbalance conditions of steel oligarchs under various conditions, as well as the corresponding stability regions, bifurcation diagrams, and Lyapunov exponent are further analyzed and compared. This research draws the following conclusions.

When the industry implements a single or mixed carbon tax policy and output adjustment policy, the market stability domain, and system dynamics characteristics are basically similar to the previous research conclusions. That is, the system balance influence of larger output enterprises is much greater than that of smaller output enterprises. When larger output enterprises adopt weak positive adjustment policies, smaller output enterprises will have more autonomy in output planning. However, when large-scale enterprises adopt improper output adjustment policies, such as an excessive output, it is more dangerous for small-scale enterprises as it will cause their output adjustment space to shrink sharply. In addition, when multiple firms simultaneously employ dynamic output adjustments, the system is more prone to falling into an imbalanced state. When output adjustment policy and a single carbon tax policy are combined to act on the steel market, as emission reduction targets are gradually raised, the adjustment policies that enterprises with larger or smaller output can implement will show an increasing trend, that is, enterprises can implement more output adjustment policies without causing the system to fall into a state of bifurcation or even chaos.

However, if the emission reduction target it consistently raised and the carbon tax policy adds subsidies, CCS, and other mixed emission reduction policies, the conclusion is slightly different. For enterprises with a larger output, even if a more complex mixed emission reduction policy appears, as the target gradually increases, the output adjustment policies that can be implemented will also show an increasing trend. However, for enterprises with smaller output, the output adjustment policy will be restricted and affected by more factors including emission reduction targets. The rule of change is different from that of the single carbon tax scenario, and it even occurs that the stability zone shrinks and the output adjustment policies decrease when the emission reduction target is large. This means that enterprises with smaller output need to be more cautious in formulating their own production plans to ensure that the enterprises themselves and the entire steel market will not fall into a state of imbalance.

Based on the above research analysis, some relevant and reasonable suggestions are put forward for the steel industry's high-quality development of transformation and improvement: the government and enterprises need to consider all factors and differences between enterprises when formulating future production plans. Enterprises with a larger output and larger market share can take more flexible choices in the process of output adjustment; however, enterprises with a smaller output and smaller market share should not adjust their output plans significantly in the process of output adjustment and should observe the output changes in enterprises with a larger output and make corresponding adjustments. When the steel industry implements more stringent emission reduction targets and policies in the future, the department should pay close attention to the adjustment of output plans of various enterprises (especially those with small output) at any time and beware of malicious production, disruption of market competition order, and market imbalance. In short, carbon tax, hybrid emission reduction policies, and output adjustment strategies (including the product differentiation strategies studied previously) have their own reasonable scope of application. The government and enterprises should carefully weigh these strategic issues in their output plans.

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Appendix A

The detailed solution and derivation process of the variation range of ξ_i (*i* = 1, 2, 3, 4, 5, 6):

When $q_i(k+1) = q_i(k)$, there are:

$$\xi_1 q_1(k) [\alpha - C_1 - \beta(q_2(k) + q_3(k) + q_4(k) + q_5(k) + q_6(k)) - 2\beta q_1(k)] = 0$$

$$\xi_2 q_2(k) [\alpha - C_2 - \beta(q_1(k) + q_3(k) + q_4(k) + q_5(k) + q_6(k)) - 2\beta q_2(k)] = 0$$
...
(A1)

$$\xi_6 q_6(k) [\alpha - C_6 - \beta(q_1(k) + q_2(k) + q_3(k) + q_4(k) + q_5(k)) - 2\beta q_6(k)] = 0$$

Among these results, a Nash equilibrium point $E^*(q_1, q_2, q_3, q_4, q_5, q_6)$ can be obtained. The stability linear discrete system $q_i(k+1) = f(q_i(k))$ can be judged by the eigenvalues of its Jacobian matrix. First, calculate its Jacobian matrix *J*,

$$J = \begin{pmatrix} J_{11} & J_{12} & J_{13} & J_{14} & J_{15} & J_{16} \\ J_{21} & J_{22} & J_{23} & J_{24} & J_{25} & J_{26} \\ J_{31} & J_{32} & J_{33} & J_{34} & J_{35} & J_{36} \\ J_{41} & J_{42} & J_{43} & J_{44} & J_{45} & J_{46} \\ J_{51} & J_{52} & J_{53} & J_{54} & J_{55} & J_{56} \\ J_{61} & J_{62} & J_{63} & J_{64} & J_{65} & J_{66} \end{pmatrix}$$
(A2)

where

$$\begin{aligned} J_{11} &= 1 + \xi_1 [\alpha - C_1 - \beta(q_2 + q_3 + q_4 + q_5 + q_6)] - 4\xi_1 \beta q_1, \\ J_{12} &= -\xi_1 \beta q_1, J_{13} = -\xi_1 \beta q_1, J_{14} = -\xi_1 \beta q_1, J_{15} = -\xi_1 \beta q_1, J_{16} = -\xi_1 \beta q_1, \\ J_{22} &= 1 + \xi_2 [\alpha - C_2 - \beta(q_1 + q_3 + q_4 + q_5 + q_6)] - 4\xi_2 \beta q_2, \\ J_{21} &= -\xi_2 \beta q_2, J_{23} = -\xi_2 \beta q_2, J_{24} = -\xi_2 \beta q_2, J_{25} = -\xi_2 \beta q_2, J_{26} = -\xi_2 \beta q_2, \\ J_{33} &= 1 + \xi_3 [\alpha - C_3 - \beta(q_1 + q_2 + q_4 + q_5 + q_6)] - 4\xi_3 \beta q_3, \\ J_{31} &= -\xi_3 \beta q_3, J_{32} = -\xi_3 \beta q_3, J_{34} = -\xi_3 \beta q_3, J_{35} = -\xi_3 \beta q_3, J_{36} = -\xi_3 \beta q_3, \\ J_{44} &= 1 + \xi_4 [\alpha - C_4 - \beta(q_1 + q_2 + q_3 + q_5 + q_6)] - 4\xi_4 \beta q_4, \\ J_{41} &= -\xi_4 \beta q_4, J_{42} = -\xi_4 \beta q_4, J_{43} = -\xi_4 \beta q_4, J_{45} = -\xi_4 \beta q_4, J_{46} = -\xi_4 \beta q_4, \\ J_{55} &= 1 + \xi_5 [\alpha - C_5 - \beta(q_1 + q_2 + q_3 + q_4 + q_6)] - 4\xi_5 \beta q_5, \\ J_{51} &= -\xi_5 \beta q_5, J_{52} = -\xi_5 \beta q_5, J_{53} = -\xi_5 \beta q_5, J_{54} = -\xi_5 \beta q_5, J_{56} = -\xi_5 \beta q_5, \\ J_{66} &= 1 + \xi_6 [\alpha - C_6 - \beta(q_1 + q_2 + q_3 + q_4 + q_5)] - 4\xi_6 \beta q_6, \\ J_{61} &= -\xi_6 \beta q_6, J_{62} = -\xi_6 \beta q_6, J_{63} = -\xi_6 \beta q_6, J_{64} = -\xi_6 \beta q_6, J_{65} = -\xi_6 \beta q_6
\end{aligned}$$

Then the characteristic equation at the equilibrium point of the Jacobian matrix is:

$$f(\lambda) = \lambda^{6} + \mu_{1}\lambda^{5} + \mu_{2}\lambda^{4} + \mu_{3}\lambda^{3} + \mu_{4}\lambda^{2} + \mu_{5}\lambda + \mu_{6} = 0$$
(A4)

where

$$\varphi_{0} = \mu_{6}^{2} - 1, \varphi_{1} = \mu_{6}\mu_{5} - \mu_{1}, \varphi_{2} = \mu_{6}\mu_{4} - \mu_{2}, \varphi_{3} = \mu_{6}\mu_{3} - \mu_{3}, \varphi_{4} = \mu_{6}\mu_{2} - \mu_{4}, \varphi_{5} = \mu_{6}\mu_{1} - \mu_{5};$$

$$\gamma_{0} = \varphi_{0}^{2} - \varphi_{5}^{2}, \gamma_{1} = \varphi_{0}\varphi_{1} - \varphi_{4}\varphi_{5}, \gamma_{2} = \varphi_{0}\varphi_{2} - \varphi_{3}\varphi_{5}, \gamma_{3} = \varphi_{0}\varphi_{3} - \varphi_{2}\varphi_{5}, \gamma_{4} = \varphi_{0}\varphi_{4} - \varphi_{1}\varphi_{5};$$

$$v_{0} = \gamma_{0}^{2} - \gamma_{4}^{2}, v_{1} = \gamma_{0}\gamma_{1} - \gamma_{3}\gamma_{4}, v_{2} = \gamma_{0}\gamma_{2} - \gamma_{2}\gamma_{4}, v_{3} = \gamma_{0}\gamma_{3} - \gamma_{1}\gamma_{4};$$

$$\varepsilon_{0} = v_{0}^{2} - v_{3}^{2}, \varepsilon_{1} = v_{0}v_{1} - v_{2}v_{3}, \varepsilon_{2} = v_{0}v_{2} - v_{1}v_{3}.$$
(A5)

and

$$\begin{cases}
1 + \mu_1 + \mu_2 + \mu_3 + \mu_4 + \mu_5 + \mu_6 > 0 \\
1 - \mu_1 + \mu_2 - \mu_3 + \mu_4 - \mu_5 + \mu_6 > 0 \\
|\mu_6| < 1 \\
|\varphi_0| > |\varphi_5|, |\gamma_0| > |\gamma_4|, |v_0| > |v_3|, |\varepsilon_0| > |\varepsilon_2|
\end{cases}$$
(A6)

Then the stable domain of the market $(\xi_1, \xi_2, \xi_3, \xi_4, \xi_5, \xi_6)$ can be obtained.

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