



# Article Prediction of the Absolute Methane Emission Rate for Longwall Caving Extraction Based on Rock Mass Modelling—A Case Study

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**Abstract:** This article presents a methodology for predicting the absolute methane emission rate for longwall caving extraction based on the determination of destressing zones generated by longwall mining operations, by means of numerical modelling. This methodology was applied for the conditions of the K-2 longwall panel in the KWK Pniówek mine. The finite difference method code FLAC2D was employed as an element of the methodology to determine the destressing zones. All results including the numerical modelling results, empirical results and the measured (in situ) results were gathered in the comparative analysis. As the final results, the accuracy and reliability of the proposed methodology were evaluated.

**Keywords:** methane hazard; absolute methane emission rate; destressing zone; numerical modelling; empirical method

# 1. Introduction

Methane hazard is a common phenomenon in hard coal mines, which intensifies with the increasing depth of the operated mining activities. Methane hazard forecasting is an auxiliary measure intended for the determination of the possible methane emissions from the rock mass to the underground working in a given area subjected to longwall mining. It can be used as the basis for decision making within the scope of: preventive measure selection for methane hazard elimination, ventilation system design and methane drainage methods.

Numerous approaches have been developed for the purpose of forecasting the absolute methane emission rate, including the following:

- Empirical methods: Kirchgessner et al. [1] presented an equation based on the multilinear regression method, comprising the methane content emitted from a given coal seam, the coal extraction rate and the entire mine's methane emission rate. Based on the historical data of underground mine-related methane emissions to the atmosphere in the United Kingdom, Creedy [2] summarized all the methane emissions from mines without methane drainage, from mines with drainage, from transported coal and from coal stored in stockyards on the surface. Lunarzewski [3] also proposed a function of the relationship between the coal extraction and the different variable empirical constants. The empirical method known as dynamic absolute longwall methane emission rate forecasting is commonly employed in Polish hard coal mining [4–13].
- Analytical methods: in Australia, the employed approach is the direct desorption method, which is based on measuring the methane content in coal samples [14].
  - Statistical methods: Methane emission forecasting in China is generally based on the statistical method, which considers the historical methane emission data. The statistical



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**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). approach adopts a number of assumptions concerning the geological conditions and the mining practices at the site encompassed by the forecasting [15]. Karacan and Olea [16] inferred the emission paths based on standard data obtained from the geophysical profiling of boreholes. The proposed technique was employed in the Black Warrior Basin, Alabama, using well logs from a series of boreholes aligned along a linear profile.

- Numerical methods: Many approaches were developed using computational fluid dynamics (CFD). Ren and Edwards [17] used laboratory data for simulating the methane flow through the rock strata surrounding a longwall panel, where the permeability is significantly dependent on the stresses generated by longwall mining. Kurnia et al. [18] simulated the behaviour of air flow and methane dispersion in a working. Results of numerical modelling were used for determining the influence of the caving zone on the methane concentration at the longwall entry [19,20]. More applications of CFD can be found in a number of studies [21-25]. Other approaches were based on finite difference method codes (FLAC2D). Karacan et al. [26] presented the application of geomechanical models for the purposes of inspecting the influence of the longwall length on the behaviour of the rock mass, the permeability variation, the methane emission and the design and performance of boreholes for methane drainage. Whittles et al. [27] described the construction and analysis of the results obtained from twoand three-dimensional geomechanical and gas flow models around a longwall in the United Kingdom. The numerical calculation results enabled the correct design of the orientation, length and support of the boreholes for gas drainage. They proposed a functional relationship that made it possible to forecast the intrinsic bulk permeability of a sheared coal measure rock based on the confining stress. Walentek and Wierzbiński [28] defined the influence of the destressing zones on the final forecasting methane emission rate and provided assessments of the rock mass geomechanical parameters on improving the result accuracy of the absolute methane emission rate from the analysed longwall panels. Others used the finite element method (COMSOL). Teng et al. [29] observed a growth in gas sorption and coal permeability under variable temperatures. They developed a model combining heat, gas and coal and applied it to a computational simulation of the thermal recovery of coal seam methane using COMSOL and MATLAB. Li et al. [30] also used COMSOL Multiphysics to reveal the law of air leakage as well as the gas distribution in a longwall caving zone under Y-type ventilation. Some studies also utilised artificial intelligence for the purposes of methane forecasting. Felka and Brodny [31] used a neuro-fuzzy network to forecast the concentration of methane in a longwall area. They presented the possibility of using artificial intelligence (AI) for forecasting models based on measurement data. Tutak and Brodny [32] presented a methodology for forecasting the methane concentration in a given mine area by means of the artificial neural network method. The forecasting model was constructed based on a multilayer perceptron (MLP) network. Karacan [33] and Karacan and Goodman [34] proposed a model based on principal component analysis (PCA) and an artificial neural network (ANN) to forecast the methane emissions in longwall areas in the United States.
- Combined methods: These approaches utilise one of the aforementioned methods as well as in situ measurements (monitoring) to determine the methane emission rates. Karacan [35] and Dougherty and Karacan [36] presented a "Methane Control and Prediction" software suite which was developed by means of various statistical mathematical approaches as well as artificial neural network prediction and classification methods. Dziurzyński and Wasilewski [37] carried out a computer simulation of the influence of the shearer operation and the methane flow during said operation on the dispersion of the air and methane mixture, and compared the simulation results with data recorded by automated gasometers during a measuring experiment. Dylong [38] described a proposed system enabling methane concentration measurements and forecasting in a longwall, and the application of knowledge regarding the concentrations

to control the operation of the shearer. He also presented the results of a number of experimental studies that revealed the efficiency of the proposed system. Booth et al. [39] proposed a new method for methane emission forecasting that included the basic energy-related principles and computational techniques related to the degree of rock strata variation, the degree of stress variation, the failure mechanism and the degree of pressure variation with reference to space and time.

It should be noted that numerical modelling has been used increasingly often as an auxiliary tool for resolving engineering problems due to the rapid development of computer science. Numerical analyses enable precisely illustrating the specific conditions and the interaction of the studied structures with series of factors as input data, which is not possible in analytical and/or empirical analyses.

In Poland, there are two forecasting methods commonly used for coal mines—relying on the determination of the complex methane pressure, or on the determination of methane emissions by calculating the desorbed methane content [9,10]. The most known method is dynamic absolute longwall methane emission rate forecasting, developed at the Experimental Mine Barbara. It is constantly updated and incorporates the experience gained during its application [11]. In this method, the range of the destressing zone is determined simply by empirical formulas, and geomechanical parameters of the rock mass are not taken into consideration. This is one reason why the average relative error of absolute methane emission rate prediction significantly exceeds the accepted permissible value of 25% (at a level of 40–50%) [12,13].

This article presents an attempt to forecast the absolute methane emission rate of a longwall caving extraction based on the determination of a destressing zone generated by longwall mining operations, by means of numerical modelling. The numerical model was verified based on in situ measurements. The shape and range of the destressing zone around the longwall panel obtained from the numerical modelling were compared with the results of the empirical method. All the numerical calculations were performed, presenting the exact geo-mining conditions of the K-2 longwall panel in the Pniówek coal mine, using the finite difference method code FLAC2D [40]. The measured methane emissions from the studied longwall areas were used in order to evaluate the accuracy of the proposed methodology.

# 2. A Methodology for Forecasting the Absolute Methane Emission Rate in Longwall Caving Extraction

By using the advantages of the numerical results with an extensive underground measurement, a methodology was proposed for the purpose of predicting the absolute methane emission rate in the area of a longwall caving extraction.

#### 2.1. Empirical Method for Determination of Destressing Zone

The prediction method for the absolute methane emission rate that is commonly used in Polish hard coal mining is based on an algorithm developed at the Experimental Mine Barbara, GIG [10]. In this method, the empirical relationships enable defining the degasification range for rock masses below and above a longwall panel as a result of longwall mining operations, regardless of their geomechanical parameters. An upper desorption zone range ( $h_g$ ) is determined for rock layers located above the longwall panel, which are known as overlaying strata, while for underlaying strata, a lower desorption zone range ( $h_d$ ) is determined. The  $h_g$  and  $h_d$  parameters are presented graphically in a vertical section through a methane desorption zone from a destressed mined longwall in Figure 1.

According to the empirical method, the ranges of the upper and lower destressing zones (desorption zones) depend on the longwall length ( $L_s$ ) and the longwall inclination angle (a). The ranges are defined using Equations (1) and (2):

For overlaying coal seams:

$$h_g = \frac{Ls}{G_g} \tag{1}$$

- For underlaying coal seams:

$$h_d = \frac{Ls}{G_d} \tag{2}$$

where  $G_g$  and  $G_d$  are factors depending on the longwall inclination angle.



Figure 1. Section through a methane desorption zone from a destressed mined longwall [10].

The width of the degasification zone for a coal seam within the destressing zone range  $(X_g, X_d)$  is determined using Equations (3) and (4):

For overlaying coal seams:

$$X_g = L_s - G_g \cdot a \tag{3}$$

- For underlaying coal seams:

$$X_d = L_s - G_d \cdot b \tag{4}$$

where *a* and *b* correspond to the distance of the overlaying or underlaying coal seam from the mined coal seam, respectively.

### 2.2. Brief Description of the FDM Software for Determination of Destressing Zone

FLAC2D is based on the finite difference method (FDM). It is one of the most commonly used codes for rock mass modelling. This code has been developed and improved over time by Itasca. All details of this code including advantages over other modelling approaches, the explicit calculation cycle, the modelling procedure, the implementation of material models and result interpretation can be found in the user's guide [40–46]. For the purposes of this work, numerical calculations were carried out using the Mohr–Coulomb elastic–plastic model. The failure envelope for this model corresponds to a Mohr–Coulomb criterion (shear yield function) with a tension cut-off (tensile yield function). The failure criterion may be represented in the plane of principal stresses ( $\sigma_1$ ,  $\sigma_3$ ) as shown in Figure 2.



Figure 2. Mohr–Coulomb failure criterion in FLAC2D [40].

The failure envelope is defined from point A to point B by the Mohr–Coulomb (shear) yield function (Equation (5)) and from B to C by the tension yield function (Equation (6)).

$$f^{s} = \sigma_{1} - \sigma_{3} \frac{1 + \sin\theta}{1 - \sin\theta} + 2c\sqrt{\frac{1 + \sin\theta}{1 - \sin\theta}}$$
(5)

$$f^t = \sigma^t - \sigma_3 \tag{6}$$

where  $\theta$  is the friction angle, *c* is the cohesion and  $\sigma_t$  is the tensile strength.

The destressing zone can be determined by using a numerical code such as the FLAC2D code due to the possibility of defining the potential yield occurring in individual points of the rock mass as a result of tensile and shear stresses. The model results also indicate whether stresses within a zone currently reach the yield surface, or if the zone failed earlier in the model run but now the stresses drop below the yield surface. A failure mechanism is defined if there is a contiguous line of active plastic zones that join two surfaces. It is possible that initial plastic flow can occur at the beginning of the calculation, but subsequent stress redistribution unloads the yielding zones so that their stresses no longer satisfy the yield criterion [40]. Each type of yield is designated with its own mark and colour on the map. An example of determining the destressing zone is shown in Figure 3. The shear-related yield zone is marked with an "\*" in red, and the tensile-related yield zone is marked with an "o" in purple. The zone where yield had occurred earlier over the course of the model but where the stresses now drop below the level of plasticity is marked with an "X" in green.

#### 2.3. Research Methodology

The calculation algorithm is presented in Figure 4. At first, the input data required for the numerical modelling were collected: longwall panel geometry, geological profile of the longwall region, mechanical parameters of each rock layer, etc. Then, the model was performed, representing the exact geological and mining conditions of the analysed longwall panel. The results obtained from the model were verified by in situ measurements. The desorbed methane content in the longwall environment was calculated after determining the size of the destressing zone generated by the longwall extraction. These results were compared to the results of the empirical/analytical method. Finally, the results of both methods were assessed and verified by comparing them with in situ methane measurements.



**Figure 3.** An example of a plasticity indicator map defining the destressing zone around the long-wall panel.



**Figure 4.** Algorithm for absolute methane emission rate forecasting in the area of a longwall caving extraction.

## 3. Case Study

## 3.1. Description of the Geological and Mining Conditions of the Analysed Longwall

The KWK Pniówek hard coal mine is located in southern Poland, in the Silesian Voivodeship, about 300 km south-west of the capital city Warsaw (Figure 5). This coal mine contains one of the largest reserves of hard coal in Poland, estimated at a total of over 100 million tons of coal. The mine's yearly output is about 5.16 million tons of coal. The longwall mining is currently conducted at a depth of 900–1000 m. The K-2 longwall is one of many active longwalls, located in the 362/3 + 363 coal seam.



Figure 5. Location of the Pniówek coal mine.

Figure 6 presents the location and lithological fragment of rock mass around the analysed longwall. The lithological map shows that the analysed coal seam is surrounded by silty shale and partial sandstone.



**Figure 6.** Outline of the K-2 longwall in coal seam 362/3 + 363 (**a**), and fragment of the lithological profile around the K-2 longwall (**b**).

According to the data provided by the Pniówek coal mine, the strength parameters R<sub>c</sub> of the coal and surrounding rocks are as follows:

- Roof rock: Claystone—31.5–63.2 MPa; Sandstone and mudstone—34.2–135.11 MPa;
- Coal—3.03–11.9 MPa;
- Floor—28.2–110.88 MPa.

# 3.2. Description of the Ventilation and Methane Drainage Conditions in the K-2 Longwall, in the 362/3 + 363 Coal Seam

The K-2 longwall is ventilated using a Y-type system, with used air offtake along the gobs. This ventilation system was adopted because of the high methane hazard present in the Pniówek coal mine. The assumed volumetric air flow rates, i.e., 1350–1400 m<sup>3</sup>/min in the longwall and 1600–1650 m<sup>3</sup>/min as the reblow of the upcast air current from the longwall, enable relatively intense ventilation of the longwall environment. The K-2 longwall environment ventilation diagram together with the air flow directions is presented in Figure 7. The air velocity was measured using mAS-4 anemometers (IMG PAN) with a reduced measuring range (<0.2 m/s). The methane concentration was measured using X-am 5000 gas detectors and air testing by the pipette method for chromatographic laboratory analysis. A total of 14 measurement series were performed. The measuring point distribution was adopted in order to determine ventilation parameters such as:

- Methane emitted to the longwall environment;
- Total absolute methane emission rate in the environment;
- Methane flow to the longwall environment with the fresh air current;
- Methane emissions to the longwall environment from the overlaying and underlaying deposits.



**Figure 7.** Ventilation diagram of the K-2 longwall environment in the 362/3 + 363 coal seam (red arrow—fresh air; blue arrow—used air).

Due to the high methane hazard (total longwall methane emission rate typically above  $30 \text{ m}^3 \text{ CH}_4/\text{min}$ ), it was necessary to apply methane drainage in the longwall. The methane capture was accomplished by means of standard methane drainage boreholes, drilled in the K-7 heading. The boreholes were drilled at a distance of about 100 m in front of the longwall face, along the K-7 heading, which was maintained in the gobs. The scheme of



the methane drainage boreholes along the K-7 heading in the K-2 longwall corresponds to the distribution presented in Figure 8.

**Figure 8.** Distribution of methane drainage boreholes along the K-7 heading in the area of the K-2 longwall in the 362 + 363/2 coal seam.

The courses of the methane capture  $(Q_0)$  from the K-2 longwall to the drainage network, the absolute methane emission rate (total,  $Q_t$ ) and the methane emitted to the longwall area (adjacent strata,  $Q_{as}$ ) are presented in Figure 9.



**Figure 9.** Courses of the methane capture ( $Q_o$ ) from the longwall to the drainage network, the absolute methane emission rate (total,  $Q_t$ ) and the methane emitted to the K-2 longwall area (adjacent strata,  $Q_{as}$ ).

The data presented in the chart (Figure 9) demonstrate that:

- The methane capture ranged from  $10 \text{ m}^3 \text{ CH}_4/\text{min}$  to  $28 \text{ m}^3 \text{ CH}_4/\text{min}$ ;
- The methane emitted to the longwall area ranged from 5 m<sup>3</sup> CH<sub>4</sub>/min to 25 m<sup>3</sup> CH<sub>4</sub>/min;
- The total absolute methane emission rate ranged from 20 m<sup>3</sup> CH<sub>4</sub>/min to 45 m<sup>3</sup> CH<sub>4</sub>/min.

The analysis revealed that the applied distribution of drainage boreholes in the K-2 longwall environment provided a methane drainage efficiency ranging from 30% to 60%.

# 3.3. In Situ Measurements

In situ measurements were conducted in order to observe the destressing zone generated by the longwall mining [47–49]. The 4–7 m-long boreholes were drilled in a location about 66 m behind the longwall panel in the K-7 heading of the K-2 longwall. A diagram of these boreholes is presented in Figure 10. The boreholes were observed by means of an Introscope LM45 camera.



Figure 10. Diagram of test boreholes in the K-7 heading of the K-2 longwall panel.

The results demonstrate that the rock mass was heavily fractured in all the boreholes (Figures 11–13). The estimated average spacing between fractures in the diagonal boreholes was about 5–10 cm, and about 1–3 cm in the vertical hole.



Figure 11. Observation in the vertical borehole (7 m) at a length of (a) 1.5 m and (b) 5.9 m.





Figure 12. Observation in the 7 m diagonal borehole at a length of 3.5 m.



Figure 13. Observation in the 4 m diagonal borehole at a length of 3.5 m.

Based on these results, it can be stated that the height of the caving zone above the K-7 heading was greater than 7 m.

# 4. Numerical Modelling

# 4.1. Model Description

Based on the geological profile of the K-2 longwall, numerical models of the rock mass were generated in FLAC2D. The models were built with the following dimensions:  $420 \times 330$  m, with the 362/3 + 363 coal seam having a thickness of 4.2 m. The numerical model was divided into approximately 87,600 quadrilateral elements with a side length of less than 1.4 m. Boundary conditions for all rollers were adopted for the upper and lower edges, as well as both side edges, of the model. The model was loaded with its own weight, resulting from the Earth's gravity (Figure 14).



**Figure 14.** Numerical model of the rock mass surrounding the mined longwall K-2, in coal seam 362/3 + 363.

The basic rock mass mechanical parameter values adopted for numerical modelling are shown in Table 1. The parameters were defined based on the laboratory tests of rocks collected in the area of the analysed longwall.

**Table 1.** Mechanical parameters of the rock mass in the area of the analysed longwall panel adopted for numerical calculations.

Rock Type	Young's Modulus E, GPa	Poisson's Ratio v	Tensile Strength $\sigma_t$ , MPa	Cohesion c, MPa	Angle of Internal Friction $ heta$ , $^{\circ}$
Coal	2.50	0.30	0.039	0.54	24
Silty shale	4.50	0.25	0.074	0.75	27
Sandstone	10.5	0.22	0.240	1.90	33

Hypothetically, the horizontal geostatic stress is equal to the vertical stress. The initial stress value was calculated according to the formula provided by Biliński [50], which describes the Polish geological and mining conditions:

$$q = 0.02 \cdot H \cdot m_c \cdot \cos\alpha \tag{7}$$

where: *q*—geostatic stress, MPa; *H*—average panel depth, m;  $m_c$ —partial rock mass stress reduction coefficient, with an adopted value of 1.0 for the area of KWK Pniówek;  $\alpha$ —coal seam angle of dip, °.

Once the initial state of stress was obtained, the displacement and velocity vectors were reset; after that, a null model was assigned to the zones corresponding to the longwall panel, and the model was recalculated. The range of the destressing zone (rock mass fracturing and caving zone) surrounding the mined longwall panel with caving was calculated and adopted for determining the rock mass degasification range.

### 4.2. Numerical Model Verification

After a longwall panel is mined out, the rock mass surrounding the longwall tends to displace towards the cavern. The total value of the vertical roof and floor displacements cannot exceed the thickness of the extracted panel. An appropriate number of calculation steps were adopted in FLAC2D in order to ensure that the maximum values of the vertical longwall panel roof and floor displacements were not greater than the thickness of the extracted panel. Figure 15 presents an example selection of the number of calculation steps.





After 1000 calculation steps, the maximum sum of the vertical displacements was about 3.15 m, which was lower than the thickness of the extracted panel (4.2 m). However, after 1500 calculation steps, the value was about 4.5 m, which was greater than the thickness of the extracted panel (4.2 m). A total of 1000 calculation steps were thus adopted for the determination of the destressing zone range.

Furthermore, the numerical modelling results were verified on the basis of the underground measurements presented in Section 4.2, according to which the value of the caving zone was greater than 7 m. Figure 16 presents the caved zone (failure as a result of tensile stress) above the longwall working, marked in purple. The caved zone height obtained from the modelling was in good agreement with the values obtained from the underground measurements.

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Figure 16. Caved zone above the longwall working after 1000 calculation steps.

#### 5. Result Analysis and Discussions

# 5.1. Comparison of the Destressing Zone Obtained from Numerical Calculations and the Empirical Method

The results of the numerical calculations obtained for the analysed longwall are presented in the form of rock mass plasticity indicator maps, which demonstrate the range of the failure zone surrounding the longwall (Figure 17). Boundary lines that separate the destressing zones (trapezoid shape) from the remaining part of the undisturbed rock mass are also marked. The vertical distribution of the rock mass degasification level was fitted to the obtained zones, depending on the distance relative to the mined coal seam. Equations (1) and (2) were used for this purpose.



**Figure 17.** Destressing zone range calculation results for rock strata adjacent to longwall K-2 in coal seam 362/3 + 363 using FLAC2D (longwall length,  $L_s = 186$  m), including the implementation of rock mass degasification level distribution.

The FDM numerical calculation results for the rock mass fracturing zone around the longwall working demonstrate that the ranges in the K-2 longwall, in the 362/3 + 363 coal seam, were  $h_g = 133$  m and  $h_d = 72$  m. Table 2 presents a comparison of the destressing zone range calculation results for the FDM calculations and the empirical method [10].

Longwall Length <i>L<sub>s</sub></i> , m	Upper Destressi Zone Ra	ng (Desorption) inge, $h_g$	Lower Destressing (Desorption) Zone Range, $h_d$				
	Empirical Method	FDM	Empirical Method	FDM			
186	128	133	48	72			

Table 2. Destressing zone range results for the FDM and empirical method calculations.

The comparative analysis demonstrates a similar value of the upper destressing zone range. However, there is a significant difference between the lower destressing zone ranges and the shape of the destressing zone obtained using FDM calculations, which consequently has an influence on the coal seam degasification zone width (Equations (3) and (4)) and ultimately on the volume of the emitted methane.

# 5.2. Field Measurements of Methane Emission and Comparative Analysis of Total Absolute Methane Emission Rate Forcasted by Numerical Modelling and Empirical Method

The results of the conducted measurements of methane concentrations  $n_1$ ,  $n_2$ ,  $n_3$ , air flow rates  $Q_1$ ,  $Q_2$ ,  $Q_3$  and methane emission to the drainage network  $Q_0$ , as well as the total absolute longwall environment methane emission rate  $Q_t$  calculations obtained from

the measurements, and the methane emission rates from the overlaying and underlaying strata (adjacent strata)  $Q_{as}$ , are shown in Table 3.

**Table 3.** Ventilation and methane parameter measurement results, calculated total absolute longwall environment methane emission rate  $Q_t$  and methane emission rates from overlaying and underlaying strata  $Q_{as}$ .

					Measurem	Calculation Results					
Measurement Date, Month	Longwall Face Distance	Average Daily Output, W <sub>d</sub>	Q <sub>1</sub>	n <sub>1</sub>	Q <sub>2</sub>	n <sub>2</sub>	Q <sub>3</sub>	n <sub>3</sub>	Qo	Qt	Qas
-	m	Mg/d	m <sup>3</sup> /min	% CH <sub>4</sub>	m <sup>3</sup> /min	% CH <sub>4</sub>	m <sup>3</sup> /min	% CH <sub>4</sub>	m <sup>3</sup> CH <sub>4</sub> /min	m <sup>3</sup> CH <sub>4</sub> /min	m <sup>3</sup> CH <sub>4</sub> /min
3rd	220	3178	1370	0.43	1370	0.84	2970	0.86	12.2	31.85	26.23
4th	325	3698	1370	0.30	1370	0.89	2975	0.80	10.8	30.49	22.41
5th	405	3009	1370	0.22	1370	0.59	2985	0.68	11.7	28.98	23.92
6th	485	2710	1375	0.27	1375	0.61	2990	0.68	10.6	27.22	22.54
7th	520	2371	1375	0.21	1375	0.69	2985	0.92	8.3	32.87	26.27

Comparative result analysis of total absolute methane emission rate forecasting in the F-3 longwall and desorbed methane emission rate forecasting from adjacent strata within the destressing zones with measurement results was conducted. Based on these analysis results, the possibility of applying numerical methods in the determination of the rock mass degasification zone range for methane emission rate forecasting in longwall environments was evaluated. The analysis encompassed longwall extraction cycles where the panel length was approx. 200 m, ensuring the achievement of the full scope of the destressing zone. The sixth month was disregarded for this longwall, as it involved driving the longwall face through a zone of geological disturbances (faults), which resulted in a low daily advance, as well as the occurrence of a local source of additional methane emissions to the longwall, which should not be included in forecasting. The comparative forecasting results according to the empirical method [10] and FDM calculations, including the absolute and relative forecasting errors, are shown in Tables 4 and 5.

The relative error of the total absolute methane emission rate predicted by both methods in comparison to the measured values is similar (25% for the empirical method, and 22% for FDM). However, the total absolute methane emission rate predicted by FDM was higher than the measured values (average 4.8 m<sup>3</sup>), while the total absolute methane emission rate predicted by the empirical method was lower than the measured values (average  $-7.8 \text{ m}^3$ ). This means the value predicted by FDM is more advantageous than the value predicted by the empirical method in terms of methane hazard prevention. Based on the FDM results, a greater range of safety (ventilation equipment, methane hazard prevention measures) would be provided.

In the case of the methane emission rates forecasted from adjacent strata, it should be noted that the FDM forecasting results provided a low difference from the measured values (the first four results did not exceed  $3.0 \text{ m}^3 \text{ CH}_4/\text{min}$ , and the last result did not exceed  $9 \text{ m}^3 \text{ CH}_4/\text{min}$ ), whereas such a high difference occurred in all the empirical forecasting results (11.83 in third month, 11.74 in fourth month, 11.25 in fifth month, 12.58 in sixth month and 17.68 in seventh month) (Table 5). Although the absolute methane emission rate predicted by both methods is less than the measured values, the average empirical value (13.43) is over 4 times higher than the FDM value (2.96). This means the FDM results are closer to the measured results in comparison with the empirical forecasting results. The average relative error of the empirical and FDM results was 55% and 12%, respectively. The empirical value is much higher than the permissible relative error value (25%), while the FDM value is acceptable. This means the FDM forecasting provided a higher accuracy than the empirical method.

**Table 4.** Total absolute methane emission rate from the longwall panel by means of the empirical method and FDM calculations, compared to the measured total absolute methane emission rates.

Month	Average Daily Output, W <sub>d</sub>	Measured Q <sub>c(rej)</sub>	Method	Forecast Q <sub>t</sub>	Difference	Relative Error, %
-	Mg/d	m <sup>3</sup> /min	-	m <sup>3</sup> /min	m <sup>3</sup> /min	
0.1	0150	<b>21</b> 0 <b>5</b>	Empirical	29.29	-2.56	8
3rd	3178	31.85	FDM	42.84	10.99	35
4th	2(00	20.40	Empirical	19.38	-11.11	36
	3698	30.49	FDM	33.26	2.77	9
5th	2000	20.00	Empirical	25.87	-3.11	11
	3009	28.98	FDM	38.97	9.99	34
	0510	27.22	Empirical	20.36	-6.86	25
6th	2710	27.22	FDM	31.91	4.69	17
<b>7</b> .1	0071	22.07	Empirical	17.44	-15.43	47
7th	2371	32.87	FDM	28.14	-4.73	14
Average error of forecasts			Empirical		-7.8	0.25
			FDM		4.8	0.22

**Table 5.** Forecasting results for emitted methane volumes desorbed from adjacent strata to the longwall environment, obtained by means of the empirical method and FDM calculations, compared to the measured methane emission rates from adjacent strata.

Month	Average Daily Output, W <sub>d</sub>	Measured Q <sub>(des)</sub>	Method	Forecast Q <sub>as</sub>	Difference	Relative Error
-	Mg/d	m <sup>3</sup> /min	-	m <sup>3</sup> /min	m <sup>3</sup> /min	
2 1	0150	26.22	Empirical	14.40	-11.83	45
3rd	3178	26.23	FDM	25.70	-0.53	2
4th	2(00	00.41	Empirical	8.67	-13.74	61
	3698	22.41	FDM	20.23	-2.18	10
5th	2000	22.02	Empirical	12.67	-11.25	47
	3009	23.92	FDM	23.56	-0.36	1
(1)	0510	22 5 4	Empirical	9.96	-12.58	56
6th	2710	22.54	FDM	19.58	-2.96	13
	0051	26.25	Empirical	8.59	-17.68	67
7th	2371	26.27	FDM	17.52	-8.75	33
Average error of forecasts			Empirical		-13.42	0.55
			FDM		-2.96	0.12

The same tendency in the case of comparing the total captured methane emission can also be noted (from the longwall and adjacent strata combined), as shown in Table 6. The average empirical result is almost 3 times higher than the FDM result. No relative error of the FDM result exceeded the permissible relative error value (25%), while all relative errors of the empirical results were higher than the permissible value (Table 6, relative error). The

average relative error of the empirical and FDM results was 39% and 13%, respectively. The empirical value is much higher than the permissible relative error value (25%), while the FDM value is acceptable. This, once again, confirms that the FDM forecasting provided a higher accuracy than the empirical method.

**Table 6.** Total captured methane emission obtained by means of the empirical method and FDM calculations.

Total Captured Methane Emission	Total Predicted Value of Methane Emission by Empirical Method	Difference	Relative Error of Empirical Results	Total Predicted Value of Methane Emission by FDM	Difference	Relative Error of FDM Results
m <sup>3</sup> /min	m <sup>3</sup> /min	m <sup>3</sup> /min	%	m <sup>3</sup> /min	m <sup>3</sup> /min	%
58.08	43.69	-14.39	25	68.54	10.46	18
52.90	28.05	-24.85	47	53.49	0.59	1
52.90	38.54	-14.36	27	62.53	9.63	18
49.76	30.32	-19.44	39	51.49	1.73	3
59.14	26.03	-33.11	56	45.66	-13.48	23
	Average value		39			13

#### 5.3. Discussions

The results indicate that the total absolute methane emission rate predicted by FDM was higher than the total absolute methane emission rate predicted by the empirical method and close to measured values in the case of forecasting the methane emission rates from adjacent strata. This is due to the larger range and shape of the destressing zone calculated by FDM, especially the lower destressing zone (floor), where methane emission seems to be unexpected in coal mining practice. The FDM results demonstrate an additional source of methane emission. Consequently, based on the FDM prediction, additional methane hazard prevention measures and ventilation system efficiency are required for particular longwall panels or particular regions, or even the entire mine.

The relative error of the empirical results (25%) was slightly higher than the relative error of the FDM results (22%) in the case of forecasting the methane emission rates from the longwall (Table 4), almost 5 times higher (55% to 12%) in the case of forecasting the methane emission rates from adjacent strata (Table 5) and 3 times higher (39% to 13%) in the case of forecasting the total captured methane emission (Table 6). The lower average relative error in forecasting based on FDM numerical modelling confirms that the results obtained from FDM forecasting are in better agreement with the measured results. This means the FDM forecasting provided a greater accuracy than the empirical method. It can thus be stated that the FDM-determined destressing zones increase the reliability of predicting the total absolute methane emission rates from the longwall and from the surrounding rock mass.

The destressing zone range in modelling results from geo-mining conditions that were considered in the numerical calculations, such as: geomechanical parameters of the rock mass, longwall panel geometry, coal seam inclination, mining depth, presence of water or faults. Therefore, it is necessary to conduct research in order to find new relationships that describe the impact of these factors (individual or combined) on the degasification zone ranges by means of numerical modelling.

The proposed methodology as a combined approach using numerical modelling and in situ measurements proved to be able to predict the absolute methane emission rate with high accuracy in the Pniówek coal mine. The key element of this methodology is the in situ measurements which were used to verify the rock mass model firstly and then assess the accuracy of methane emission predicted by numerical modelling. This process provides reliable results, assisting the mine to make a final decision. There is no doubt that this methodology with the following steps can be applied easily in other coal mine regions. As a result, the effectiveness of the proposed methodology can be evaluated.

#### 6. Conclusions

An attempt was proposed to determine the absolute methane emission rate for longwall K-2 in the KWK Pniówek mine by means of numerical modelling. The finite difference method FLAC2D was employed to define the destressing zone, which relates to the absolute methane emission rate from the longwall and the surrounding rock mass. The empirical method and field measurements were also applied as auxiliary elements to verify the numerical modelling outcomes. The following conclusions can be drawn:

- Numerical calculations based on the finite difference method (FLAC2D) can be a useful tool to determine the destressing zone, with the possibility of taking the number of geomechanical parameters into account. This method improved the accuracy of the absolute methane emission rate prediction by reducing the relative error from 55% to 12% in the case of forecasting the methane emission rates from adjacent strata, and from 39% to 13% in the case of forecasting the total captured methane emission.
- The results confirm the key role of in situ measurements in the verification of rock mass models and assessments of the numerical modelling results.
- The results indicate the influence of the geomechanical parameters of the rock mass on predicting the results of the total absolute methane emission rates.
- The proposed methodology using numerical modelling and in situ measurements managed to predict the absolute methane emission rate with high accuracy for a case study in the Pniówek coal mine. It is suggested to apply the proposed calculation algorithm to various cases with various geo-mining conditions in order to confirm its efficiency.
- Due to the influence of the longwall length and the ventilation method (arrangement of workings) on the methane emission, three-dimensional numerical modelling would achieve a higher accuracy of the results.
- It is recommended to calibrate a general geomechanical model for a specific location (longwall panel or mined coal seam section), which may serve as the basis for the forecasting of specific issues related to the flow of methane or other gases in individual longwall panels in that particular mine.

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